

---

```

clear;
close all;

a1 = 0.4;
a2 = 0.4;
a3 = 0.4;
% theta d a alpha
L(1) = Link([ 0      0    a1  0], 'standard');
L(2) = Link([ 0      0    a2  0], 'standard');
L(3) = Link([ 0      0    a3  0], 'standard');

threelink = SerialLink(L, 'name', 'three link', ...
    'comment', 'from Spong, Hutchinson, Vidyasagar');
threelink.base = [1 0 0 0;
                  0 0 -1 0;
                  0 1 0 0;
                  0 0 0 1];

syms q1 q2 q3
qz = [q1 q2 q3];
% threelink.plot(qz);

T_1 = threelink.A(1,qz);
T_c1 = T_1;
T_c1(1:3,4) = T_c1(1:3,4)/2;
T_c1;

temp_t2 = threelink.A(2,qz);
T_2 = T_1*temp_t2;
temp_c2 = temp_t2;
temp_c2(1:3,4) = temp_c2(1:3,4)/2;
T_c2 = T_1*temp_c2;

temp_t3 = threelink.A(3,qz);
T_3 = T_2*temp_t3;
temp_c3 = temp_t3;
temp_c3(1:3,4) = temp_c3(1:3,4)/2;
T_c3 = T_2*temp_c3;

z = [0; 0; 1];
jacobian_c1 = [cross(z,T_c1(1:3,4)) zeros(3,2); z zeros(3,2)];
jacobian_c2 = [cross(z,T_c2(1:3,4)) cross(z,T_c2(1:3,4)-T_1(1:3,4))
    zeros(3,1); z z zeros(3,1)];
jacobian_c3 = [cross(z,T_c3(1:3,4)) cross(z,T_c3(1:3,4)-T_1(1:3,4))
    cross(z,T_c3(1:3,4)-T_2(1:3,4)); z z z];

syms Ixx Iyy Izz q_dot1 q_dot2 q_dot3
q_dot = [q_dot1; q_dot2; q_dot3];

mass = 1;

```

---

---

```

K_rot = 1/2*q_dot.*(jacobian_c1(4:6,:).'*[Ixx 0 0; 0 Iyy 0; 0 0
    Izz]*jacobian_c1(4:6,:)...
    + jacobian_c2(4:6,:).'*[Ixx 0 0; 0 Iyy 0; 0 0
    Izz]*jacobian_c2(4:6,:)...
    + jacobian_c3(4:6,:).'*[Ixx 0 0; 0 Iyy 0; 0 0
    Izz]*jacobian_c3(4:6,:))*q_dot;

K_trans = 1/2*q_dot.*(mass*jacobian_c1(1:3,:).'*jacobian_c1(1:3,:) +
    mass*jacobian_c2(1:3,:).'*jacobian_c2(1:3,:)...
    +
    mass*jacobian_c3(1:3,:).'*jacobian_c3(1:3,:))*q_dot;
K_total = K_rot+K_trans;

D = jacobian_c1(4:6,:).'*[Ixx 0 0; 0 Iyy 0; 0 0
    Izz]*jacobian_c1(4:6,:)...
    + jacobian_c2(4:6,:).'*[Ixx 0 0; 0 Iyy 0; 0 0
    Izz]*jacobian_c2(4:6,:)...
    + jacobian_c3(4:6,:).'*[Ixx 0 0; 0 Iyy 0; 0 0
    Izz]*jacobian_c3(4:6,:)...
    + mass*jacobian_c1(1:3,:).'*jacobian_c1(1:3,:) +
    mass*jacobian_c2(1:3,:).'*jacobian_c2(1:3,:)...
    + mass*jacobian_c3(1:3,:).'*jacobian_c3(1:3,:);

for k=1:3
    for i=1:3
        for j=1:3
            c(i,j,k) = 1/2 * (diff(D(k,j),qz(i)) + diff(D(k,i),qz(j))
            - diff(D(i,j),qz(k)));
        end
    end
end

gravity = [0; 9.81; 0];
P = gravity'*T_c1(1:3,4) + gravity'*T_c2(1:3,4) +
    gravity'*T_c3(1:3,4);
g1 = diff(P,q1);
g2 = diff(P,q2);
g3 = diff(P,q3);
g = [g1; g2; g3];
% Plug into the EOM equation
D
c
g

D =

[

```

$$3*I_{zz} + ((2*\cos(q_1))/5 + (\cos(q_1)*\cos(q_2))/5$$

---


$$\begin{aligned}
& - (\sin(q_1) \sin(q_2))/5)^2 + ((2 \sin(q_1))/5 + (\cos(q_1) \sin(q_2))/5 \\
& + (\cos(q_2) \sin(q_1))/5)^2 + \cos(q_1)^2/25 + \sin(q_1)^2/25 + \\
& ((2 \cos(q_1))/5 + (2 \cos(q_1) \cos(q_2))/5 - (2 \sin(q_1) \sin(q_2))/5 \\
& + (\cos(q_3) (\cos(q_1) \cos(q_2) - \sin(q_1) \sin(q_2)))/5 - \\
& (\sin(q_3) (\cos(q_1) \sin(q_2) + \cos(q_2) \sin(q_1)))/5)^2 + \\
& ((2 \sin(q_1))/5 + (2 \cos(q_1) \sin(q_2))/5 + (2 \cos(q_2) \sin(q_1))/5 \\
& + (\cos(q_3) (\cos(q_1) \sin(q_2) + \cos(q_2) \sin(q_1)))/5 + \\
& (\sin(q_3) (\cos(q_1) \cos(q_2) - \sin(q_1) \sin(q_2)))/5)^2, 2 I_{zz} + \\
& ((\cos(q_1) \cos(q_2))/5 - (\sin(q_1) \sin(q_2))/5) * ((2 \cos(q_1))/5 + \\
& (\cos(q_1) \cos(q_2))/5 - (\sin(q_1) \sin(q_2))/5) + ((\cos(q_1) \sin(q_2))/5 \\
& + (\cos(q_2) \sin(q_1))/5) * ((2 \sin(q_1))/5 + (\cos(q_1) \sin(q_2))/5 \\
& + (\cos(q_2) \sin(q_1))/5) + ((2 \cos(q_1) \cos(q_2))/5 - \\
& (2 \sin(q_1) \sin(q_2))/5 + (\cos(q_3) (\cos(q_1) \cos(q_2) \\
& - \sin(q_1) \sin(q_2)))/5 - (\sin(q_3) (\cos(q_1) \sin(q_2) + \\
& \cos(q_2) \sin(q_1)))/5) * ((2 \cos(q_1))/5 + (2 \cos(q_1) \cos(q_2))/5 \\
& - (2 \sin(q_1) \sin(q_2))/5 + (\cos(q_3) (\cos(q_1) \cos(q_2) \\
& - \sin(q_1) \sin(q_2)))/5 - (\sin(q_3) (\cos(q_1) \sin(q_2) \\
& + \cos(q_2) \sin(q_1)))/5) + ((2 \cos(q_1) \sin(q_2))/5 + \\
& (2 \cos(q_2) \sin(q_1))/5 + (\cos(q_3) (\cos(q_1) \sin(q_2) \\
& + \cos(q_2) \sin(q_1)))/5 + (\sin(q_3) (\cos(q_1) \cos(q_2) - \\
& \sin(q_1) \sin(q_2)))/5) * ((2 \sin(q_1))/5 + (2 \cos(q_1) \sin(q_2))/5 \\
& + (2 \cos(q_2) \sin(q_1))/5 + (\cos(q_3) (\cos(q_1) \sin(q_2) \\
& + \cos(q_2) \sin(q_1)))/5 + (\sin(q_3) (\cos(q_1) \cos(q_2) - \\
& \sin(q_1) \sin(q_2)))/5), I_{zz} + ((\cos(q_3) (\cos(q_1) \cos(q_2) \\
& - \sin(q_1) \sin(q_2)))/5 - (\sin(q_3) (\cos(q_1) \sin(q_2) + \\
& \cos(q_2) \sin(q_1)))/5) * ((2 \cos(q_1))/5 + (2 \cos(q_1) \cos(q_2))/5 \\
& - (2 \sin(q_1) \sin(q_2))/5 + (\cos(q_3) (\cos(q_1) \cos(q_2) \\
& - \sin(q_1) \sin(q_2)))/5 - (\sin(q_3) (\cos(q_1) \sin(q_2) \\
& + \cos(q_2) \sin(q_1)))/5) + ((\cos(q_3) (\cos(q_1) \sin(q_2) \\
& + \cos(q_2) \sin(q_1)))/5 + (\sin(q_3) (\cos(q_1) \cos(q_2) - \\
& \sin(q_1) \sin(q_2)))/5) * ((2 \sin(q_1))/5 + (2 \cos(q_1) \sin(q_2))/5 \\
& + (2 \cos(q_2) \sin(q_1))/5 + (\cos(q_3) (\cos(q_1) \sin(q_2) \\
& + \cos(q_2) \sin(q_1)))/5 + (\sin(q_3) (\cos(q_1) \cos(q_2) - \\
& \sin(q_1) \sin(q_2)))/5)] \\
& [ 2 I_{zz} + ((\cos(q_1) \cos(q_2))/5 - (\sin(q_1) \sin(q_2))/5) * ((2 \cos(q_1))/5 \\
& + (\cos(q_1) \cos(q_2))/5 - (\sin(q_1) \sin(q_2))/5) + ((\cos(q_1) \sin(q_2))/5 \\
& + (\cos(q_2) \sin(q_1))/5) * ((2 \sin(q_1))/5 + (\cos(q_1) \sin(q_2))/5 \\
& + (\cos(q_2) \sin(q_1))/5) + ((2 \cos(q_1) \cos(q_2))/5 - \\
& (2 \sin(q_1) \sin(q_2))/5 + (\cos(q_3) (\cos(q_1) \cos(q_2) \\
& - \sin(q_1) \sin(q_2)))/5 - (\sin(q_3) (\cos(q_1) \sin(q_2) + \\
& \cos(q_2) \sin(q_1)))/5) * ((2 \cos(q_1))/5 + (2 \cos(q_1) \cos(q_2))/5 \\
& - (2 \sin(q_1) \sin(q_2))/5 + (\cos(q_3) (\cos(q_1) \cos(q_2) \\
& - \sin(q_1) \sin(q_2)))/5 - (\sin(q_3) (\cos(q_1) \sin(q_2) + \\
& \cos(q_2) \sin(q_1)))/5) + ((2 \cos(q_1) \sin(q_2))/5 + (2 \cos(q_2) \sin(q_1))/5 \\
& + (\cos(q_3) (\cos(q_1) \sin(q_2) + \cos(q_2) \sin(q_1)))/5 + \\
& (\sin(q_3) (\cos(q_1) \cos(q_2) - \sin(q_1) \sin(q_2)))/5) * ((2 \sin(q_1))/5 \\
& + (2 \cos(q_1) \sin(q_2))/5 + (2 \cos(q_2) \sin(q_1))/5 + \\
& (\cos(q_3) (\cos(q_1) \sin(q_2) + \cos(q_2) \sin(q_1)))/5 + \\
& (\sin(q_3) (\cos(q_1) \cos(q_2) - \sin(q_1) \sin(q_2)))/5),
\end{aligned}$$


---

---


$$\begin{aligned}
& 2*Izz + ((2*\cos(q1)*\cos(q2))/5 - (2*\sin(q1)*\sin(q2))/5 \\
& + (\cos(q3)*(\cos(q1)*\cos(q2) - \sin(q1)*\sin(q2)))/5 - \\
& (\sin(q3)*(\cos(q1)*\sin(q2) + \cos(q2)*\sin(q1)))/5)^2 \\
& + ((2*\cos(q1)*\sin(q2))/5 + (2*\cos(q2)*\sin(q1))/5 + \\
& (\cos(q3)*(\cos(q1)*\sin(q2) + \cos(q2)*\sin(q1)))/5 + \\
& (\sin(q3)*(\cos(q1)*\cos(q2) - \sin(q1)*\sin(q2)))/5)^2 \\
& + ((\cos(q1)*\cos(q2))/5 - (\sin(q1)*\sin(q2))/5)^2 + \\
& ((\cos(q1)*\sin(q2))/5 + (\cos(q2)*\sin(q1))/5)^2, \\
& Izz + ((\cos(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5 + (\sin(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5)*((2*\cos(q1)*\sin(q2))/5 + \\
& (2*\cos(q2)*\sin(q1))/5 + (\cos(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5 + (\sin(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5) + ((\cos(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5 - (\sin(q3)*(\cos(q1)*\sin(q2) + \\
& \cos(q2)*\sin(q1)))/5)*((2*\cos(q1)*\cos(q2))/5 - (2*\sin(q1)*\sin(q2))/5 \\
& + (\cos(q3)*(\cos(q1)*\cos(q2) - \sin(q1)*\sin(q2)))/5 - \\
& (\sin(q3)*(\cos(q1)*\sin(q2) + \cos(q2)*\sin(q1)))/5)] \\
& [
\end{aligned}$$

$$\begin{aligned}
& Izz + ((\cos(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5 - (\sin(q3)*(\cos(q1)*\sin(q2) + \\
& \cos(q2)*\sin(q1)))/5)*((2*\cos(q1))/5 + (2*\cos(q1)*\cos(q2))/5 \\
& - (2*\sin(q1)*\sin(q2))/5 + (\cos(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5 - (\sin(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5) + ((\cos(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5 + (\sin(q3)*(\cos(q1)*\cos(q2) - \\
& \sin(q1)*\sin(q2)))/5)*((2*\sin(q1))/5 + (2*\cos(q1)*\sin(q2))/5 \\
& + (2*\cos(q2)*\sin(q1))/5 + (\cos(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5 + (\sin(q3)*(\cos(q1)*\cos(q2) - \\
& \sin(q1)*\sin(q2)))/5),
\end{aligned}$$

$$\begin{aligned}
& Izz + ((\cos(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5 + (\sin(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5)*((2*\cos(q1)*\sin(q2))/5 + \\
& (2*\cos(q2)*\sin(q1))/5 + (\cos(q3)*(\cos(q1)*\sin(q2) \\
& + \cos(q2)*\sin(q1)))/5 + (\sin(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5) + ((\cos(q3)*(\cos(q1)*\cos(q2) \\
& - \sin(q1)*\sin(q2)))/5 - (\sin(q3)*(\cos(q1)*\sin(q2) + \\
& \cos(q2)*\sin(q1)))/5)*((2*\cos(q1)*\cos(q2))/5 - (2*\sin(q1)*\sin(q2))/5 \\
& + (\cos(q3)*(\cos(q1)*\cos(q2) - \sin(q1)*\sin(q2)))/5 - \\
& (\sin(q3)*(\cos(q1)*\sin(q2) + \cos(q2)*\sin(q1)))/5),
\end{aligned}$$

$$Izz + ((\cos(q3)*(\cos(q1)*\sin(q2) + \cos(q2)*\sin(q1)))/5$$


---

---

```

+ (sin(q3)*(cos(q1)*cos(q2) - sin(q1)*sin(q2)))/5)^2
+ ((cos(q3)*(cos(q1)*cos(q2) - sin(q1)*sin(q2)))/5 -
(sin(q3)*(cos(q1)*sin(q2) + cos(q2)*sin(q1)))/5)^2]

c(:, :, 1) =

[

0, ((cos(q1)*cos(q2))/5 - (sin(q1)*sin(q2))/5)*((2*sin(q1))/5
+ (cos(q1)*sin(q2))/5 + (cos(q2)*sin(q1))/5) - ((cos(q1)*sin(q2))/5
+ (cos(q2)*sin(q1))/5)*((2*cos(q1))/5 + (cos(q1)*cos(q2))/5
- (sin(q1)*sin(q2))/5) - ((2*cos(q1)*sin(q2))/5 +
(2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1))/5 + (2*cos(q1)*cos(q2))/5
- (2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5) + ((2*cos(q1)*cos(q2))/5 -
(2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5)*((2*sin(q1))/5 + (2*cos(q1)*sin(q2))/5
+ (2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5), ((cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5)*((2*sin(q1))/5 + (2*cos(q1)*sin(q2))/5
+ (2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5) - ((cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1))/5 + (2*cos(q1)*cos(q2))/5
- (2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5)]
[ ((cos(q1)*cos(q2))/5 - (sin(q1)*sin(q2))/5)*((2*sin(q1))/5 +
(cos(q1)*sin(q2))/5 + (cos(q2)*sin(q1))/5) - ((cos(q1)*sin(q2))/5
+ (cos(q2)*sin(q1))/5)*((2*cos(q1))/5 + (cos(q1)*cos(q2))/5
- (sin(q1)*sin(q2))/5) - ((2*cos(q1)*sin(q2))/5 +
(2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1))/5 + (2*cos(q1)*cos(q2))/5
- (2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5)]

```

---

---


$$\begin{aligned}
& \cos(q_2)*\sin(q_1))/5) + ((2*\cos(q_1)*\cos(q_2))/5 - (2*\sin(q_1)*\sin(q_2))/5 \\
& + (\cos(q_3)*(\cos(q_1)*\cos(q_2) - \sin(q_1)*\sin(q_2)))/5 - \\
& (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \cos(q_2)*\sin(q_1)))/5)*((2*\sin(q_1))/5 \\
& + (2*\cos(q_1)*\sin(q_2))/5 + (2*\cos(q_2)*\sin(q_1))/5 + \\
& (\cos(q_3)*(\cos(q_1)*\sin(q_2) + \cos(q_2)*\sin(q_1)))/5 + \\
& (\sin(q_3)*(\cos(q_1)*\cos(q_2) - \sin(q_1)*\sin(q_2)))/5), \\
& ((\cos(q_1)*\cos(q_2))/5 - (\sin(q_1)*\sin(q_2))/5)*((2*\sin(q_1))/5 + \\
& (\cos(q_1)*\sin(q_2))/5 + (\cos(q_2)*\sin(q_1))/5) - ((\cos(q_1)*\sin(q_2))/5 \\
& + (\cos(q_2)*\sin(q_1))/5)*((2*\cos(q_1))/5 + (\cos(q_1)*\cos(q_2))/5 \\
& - (\sin(q_1)*\sin(q_2))/5) - ((2*\cos(q_1)*\sin(q_2))/5 + \\
& (2*\cos(q_2)*\sin(q_1))/5 + (\cos(q_3)*(\cos(q_1)*\sin(q_2) \\
& + \cos(q_2)*\sin(q_1)))/5 + (\sin(q_3)*(\cos(q_1)*\cos(q_2) - \\
& \sin(q_1)*\sin(q_2)))/5)*((2*\cos(q_1))/5 + (2*\cos(q_1)*\cos(q_2))/5 \\
& - (2*\sin(q_1)*\sin(q_2))/5 + (\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) \\
& + \cos(q_2)*\sin(q_1)))/5) + ((2*\cos(q_1)*\cos(q_2))/5 - \\
& (2*\sin(q_1)*\sin(q_2))/5 + (\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5)*((2*\sin(q_1))/5 + (2*\cos(q_1)*\sin(q_2))/5 \\
& + (2*\cos(q_2)*\sin(q_1))/5 + (\cos(q_3)*(\cos(q_1)*\sin(q_2) \\
& + \cos(q_2)*\sin(q_1)))/5 + (\sin(q_3)*(\cos(q_1)*\cos(q_2) - \\
& \sin(q_1)*\sin(q_2)))/5), ((\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5)*((2*\sin(q_1))/5 + (2*\cos(q_1)*\sin(q_2))/5 \\
& + (2*\cos(q_2)*\sin(q_1))/5 + (\cos(q_3)*(\cos(q_1)*\sin(q_2) \\
& + \cos(q_2)*\sin(q_1)))/5 + (\sin(q_3)*(\cos(q_1)*\cos(q_2) - \\
& \sin(q_1)*\sin(q_2)))/5) - ((\cos(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5 + (\sin(q_3)*(\cos(q_1)*\cos(q_2) - \\
& \sin(q_1)*\sin(q_2)))/5)*((2*\cos(q_1))/5 + (2*\cos(q_1)*\cos(q_2))/5 \\
& - (2*\sin(q_1)*\sin(q_2))/5 + (\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5)]
\end{aligned}$$

[

$$\begin{aligned}
& ((\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5)*((2*\sin(q_1))/5 + (2*\cos(q_1)*\sin(q_2))/5 \\
& + (2*\cos(q_2)*\sin(q_1))/5 + (\cos(q_3)*(\cos(q_1)*\sin(q_2) \\
& + \cos(q_2)*\sin(q_1)))/5 + (\sin(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5) - ((\cos(q_3)*(\cos(q_1)*\sin(q_2) \\
& + \cos(q_2)*\sin(q_1)))/5 + (\sin(q_3)*(\cos(q_1)*\cos(q_2) - \\
& \sin(q_1)*\sin(q_2)))/5)*((2*\cos(q_1))/5 + (2*\cos(q_1)*\cos(q_2))/5 \\
& - (2*\sin(q_1)*\sin(q_2))/5 + (\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5),
\end{aligned}$$

$$\begin{aligned}
& ((\cos(q_3)*(\cos(q_1)*\cos(q_2) \\
& - \sin(q_1)*\sin(q_2)))/5 - (\sin(q_3)*(\cos(q_1)*\sin(q_2) + \\
& \cos(q_2)*\sin(q_1)))/5)*((2*\sin(q_1))/5 + (2*\cos(q_1)*\sin(q_2))/5
\end{aligned}$$

---

```

+ (2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5) - ((cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1))/5 + (2*cos(q1)*cos(q2))/5
- (2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5), ((cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5)*((2*sin(q1))/5 + (2*cos(q1)*sin(q2))/5
+ (2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5) - ((cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1))/5 + (2*cos(q1)*cos(q2))/5
- (2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5)]

```

```

c(:, :, 2) =

```

```

[ ((cos(q1)*sin(q2))/5 + (cos(q2)*sin(q1))/5)*((2*cos(q1))/5 +
(cos(q1)*cos(q2))/5 - (sin(q1)*sin(q2))/5) - ((cos(q1)*cos(q2))/5
- (sin(q1)*sin(q2))/5)*((2*sin(q1))/5 + (cos(q1)*sin(q2))/5
+ (cos(q2)*sin(q1))/5) + ((2*cos(q1)*sin(q2))/5 +
(2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1))/5 + (2*cos(q1)*cos(q2))/5
- (2*sin(q1)*sin(q2))/5 + (cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2) +
cos(q2)*sin(q1)))/5) - ((2*cos(q1)*cos(q2))/5 - (2*sin(q1)*sin(q2))/5
+ (cos(q3)*(cos(q1)*cos(q2) - sin(q1)*sin(q2)))/5 -
(sin(q3)*(cos(q1)*sin(q2) + cos(q2)*sin(q1)))/5)*((2*sin(q1))/5
+ (2*cos(q1)*sin(q2))/5 + (2*cos(q2)*sin(q1))/5 +
(cos(q3)*(cos(q1)*sin(q2) + cos(q2)*sin(q1)))/5 +
(sin(q3)*(cos(q1)*cos(q2) - sin(q1)*sin(q2)))/5),

```

```

0, ((cos(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5 - (sin(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5)*((2*cos(q1)*sin(q2))/5 +
(2*cos(q2)*sin(q1))/5 + (cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2)
- sin(q1)*sin(q2)))/5) - ((cos(q3)*(cos(q1)*sin(q2)
+ cos(q2)*sin(q1)))/5 + (sin(q3)*(cos(q1)*cos(q2) -
sin(q1)*sin(q2)))/5)*((2*cos(q1)*cos(q2))/5 - (2*sin(q1)*sin(q2))/5
+ (cos(q3)*(cos(q1)*cos(q2) - sin(q1)*sin(q2)))/5 -
(sin(q3)*(cos(q1)*sin(q2) + cos(q2)*sin(q1)))/5)]

```

---

[

0,

0, ((cos(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5 - (sin(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5)\*((2\*cos(q1)\*sin(q2))/5 +  
(2\*cos(q2)\*sin(q1))/5 + (cos(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5 + (sin(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5) - ((cos(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5 + (sin(q3)\*(cos(q1)\*cos(q2) -  
sin(q1)\*sin(q2)))/5)\*((2\*cos(q1)\*cos(q2))/5 - (2\*sin(q1)\*sin(q2))/5  
+ (cos(q3)\*(cos(q1)\*cos(q2) - sin(q1)\*sin(q2)))/5 -  
(sin(q3)\*(cos(q1)\*sin(q2) + cos(q2)\*sin(q1)))/5)]

[

((cos(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5 - (sin(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5)\*((2\*cos(q1)\*sin(q2))/5 +  
(2\*cos(q2)\*sin(q1))/5 + (cos(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5 + (sin(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5) - ((cos(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5 + (sin(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5)\*((2\*cos(q1)\*cos(q2))/5 -  
(2\*sin(q1)\*sin(q2))/5 + (cos(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5 - (sin(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5), ((cos(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5 - (sin(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5)\*((2\*cos(q1)\*sin(q2))/5 +  
(2\*cos(q2)\*sin(q1))/5 + (cos(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5 + (sin(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5) - ((cos(q3)\*(cos(q1)\*sin(q2)  
+ cos(q2)\*sin(q1)))/5 + (sin(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5)\*((2\*cos(q1)\*cos(q2))/5 -  
(2\*sin(q1)\*sin(q2))/5 + (cos(q3)\*(cos(q1)\*cos(q2)  
- sin(q1)\*sin(q2)))/5 - (sin(q3)\*(cos(q1)\*sin(q2)





---

[

0,

0, 0]

$g =$

$$\begin{aligned} & (981*\cos(q1))/100 + (2943*\cos(q1)*\cos(q2))/500 - \\ & (2943*\sin(q1)*\sin(q2))/500 + (981*\cos(q3)*(cos(q1)*cos(q2) \\ & - \sin(q1)*\sin(q2)))/500 - (981*\sin(q3)*(cos(q1)*sin(q2) + \\ & \cos(q2)*sin(q1)))/500 \\ & \quad (2943*\cos(q1)*\cos(q2))/500 - \\ & (2943*\sin(q1)*\sin(q2))/500 + (981*\cos(q3)*(cos(q1)*cos(q2) \\ & - \sin(q1)*\sin(q2)))/500 - (981*\sin(q3)*(cos(q1)*sin(q2) + \\ & \cos(q2)*sin(q1)))/500 \\ & \quad (981*\cos(q3)*(cos(q1)*cos(q2) - \sin(q1)*\sin(q2)))/500 - \\ & (981*\sin(q3)*(cos(q1)*sin(q2) + \cos(q2)*sin(q1)))/500 \end{aligned}$$

*Published with MATLAB® R2016a*