CS: Deep Learning

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1 Private Deep Learning

1.1 Two hidden layer neural network

Let $\phi : \mathbb{R} \to \mathbb{R}$ denote the ReLU activation, i.e., $\phi(u) = \max\{u, 0\}$.

We consider a two hidden layer neural network $f: \mathbb{R}^d \to \mathbb{R}$ (which can be decomposed into two functions $h: \mathbb{R}^d \to \mathbb{R}^{m_a}$ and $g: \mathbb{R}^{m_a} \to \mathbb{R}^{m_b}$) as follows:

$$h(x) = \phi(W_A x),$$

$$g(z) = W_C^{\top} \phi(z),$$

$$f(x) = g(h(x)) = W_C^{\top} \phi(W_B \phi(W_A x)),$$

where $W_A \in \mathbb{R}^{m_a \times d}$, $W_B \in \mathbb{R}^{m_b \times m_a}$ and $W_C \in \mathbb{R}^{m_b}$.

Let $\{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\} \subset \mathbb{R}^d \times \mathbb{R}$ denote a set of n input data points. We can think of x_i s are images and y_i s are the corresponding labels.

In classical deep learning training, the task is to find weights W_A, W_B and W_C such that \mathcal{L} is minimized.

$$\mathcal{L} = \sum_{i=1}^{n} \|f(x_i) - y_i\|_2^2$$

In this lecture, we describe a slightly different goal. The purpose is to find some W_A , W_B and W_C such that

- 1. Utility: $f(x_i) \approx y_i, \forall i \in [n]$
- 2. Privacy: Given $h(x_i)$ and W_A , it is "hard" recover x_i

There are several ways of modifying deep neural networks to make it more private

- 1. Modify input data points [HSLA20]
- 2. Modify weights [HSR⁺20]

References

[HSLA20] Yangsibo Huang, Zhao Song, Kai Li, and Sanjeev Arora. Instahide: Instace-hiding schemes for private distributed learning. In *ICML*, 2020.

[HSR⁺20] Yangsibo Huang, Yushan Su, Sachin Ravi, Zhao Song, Sanjeev Arora, and Kai Li. Privacy-preserving learning via deep net pruning. In *arXiv preprint*. https://arxiv.org/pdf/2003.01876.pdf, 2020.