

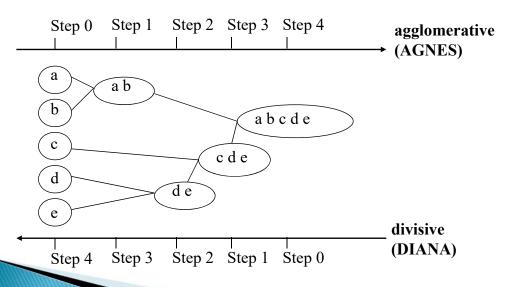
Data Mining -- Clustering

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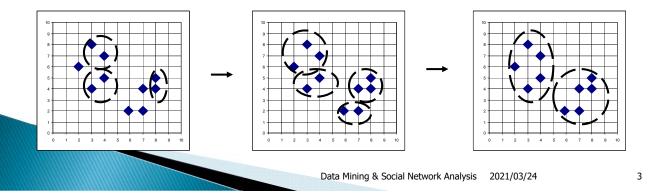
Hierarchical Clustering

Use distance matrix as clustering criteria. This method does not require the number of clusters k as an input, but needs a termination condition



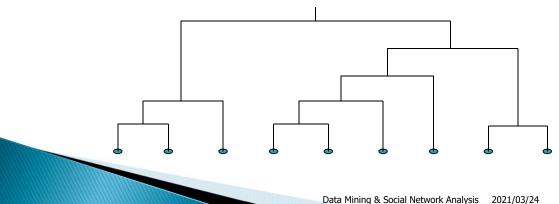
AGNES (Agglomerative Nesting)

- Introduced in Kaufmann and Rousseeuw (1990)
- Implemented in statistical analysis packages, e.g., Splus
- Use the Single-Link method and the dissimilarity matrix.
- Merge nodes that have the least dissimilarity
- Go on in a non-descending fashion
- Eventually all nodes belong to the same cluster



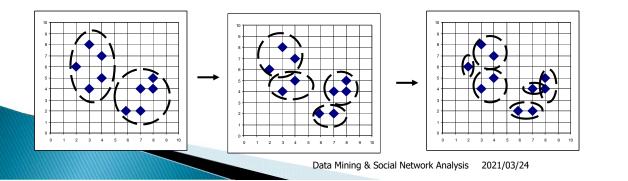
Dendrogram

- Shows how the clusters are merged
- Decompose data objects into a several levels of nested partitioning (tree of clusters), called a dendrogram.
- A clustering of the data objects is obtained by cutting the dendrogram at the desired level, then each connected component forms a cluster.



DIANA (Divisive Analysis)

- ▶ Introduced in Kaufmann and Rousseeuw (1990)
- Implemented in statistical analysis packages, e.g.,
 Splus
- Inverse order of AGNES
- Eventually each node forms a cluster on its own



Comments

- Major weakness of agglomerative clustering methods
 - do not scale well: time complexity of at least $O(n^2)$, where n is the number of total objects
 - can never undo what was done previously
- Integration of hierarchical with distance-based clustering
 - BIRCH (1996): uses CF-tree and incrementally adjusts the quality of sub-clusters
 - ROCK (1999): clustering categorical data by neighbor and link analysis
 - <u>CHAMELEON (1999)</u>: hierarchical clustering using dynamic modeling

BIRCH

- Birch: Balanced Iterative Reducing and Clustering using Hierarchies (Zhang, Ramakrishnan & Livny, SIGMOD'96)
- Incrementally construct a CF (Clustering Feature) tree, a hierarchical data structure for multiphase clustering
 - Phase 1: scan DB to build an initial in-memory CF tree (a multi-level compression of the data that tries to preserve the inherent clustering structure of the data)
 - Phase 2: use an arbitrary clustering algorithm to cluster the leaf nodes of the CF-tree

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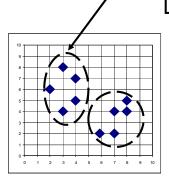
Clustering Feature Vector

- Summary of the statistics for a given subcluster
- Registers crucial measurements for computing cluster and utilizes storage efficiently
- in BIRCH, Clustering Feature: CF = (N, LS, SS)

N: Number of data points

$$LS: \sum_{i=1}^{N} = X_i$$

SS:
$$\sum_{i=1}^{N} = X_i^2$$



CF = (5, (16,30), (54,190))

(3,4)

(2,6)

(4,5)

(4,7)

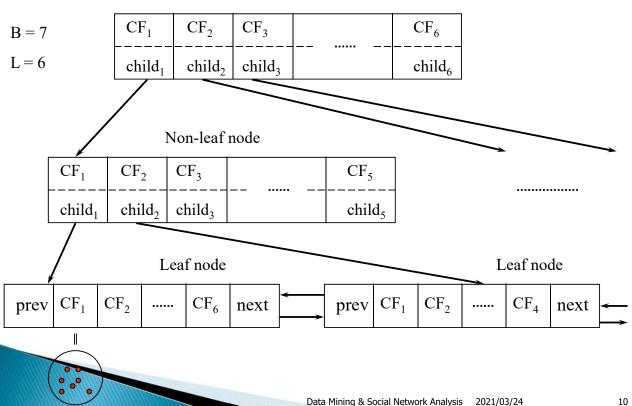
(3,8)

CF-Tree

- A CF tree is a height-balanced tree that stores the clustering features for a hierarchical clustering
 - A nonleaf node in a tree has descendants or "children"
 - The nonleaf nodes store sums of the CFs of their children
- A CF tree has two parameters
 - Branching factor: specify the maximum number of children.
 - threshold: max diameter of sub-clusters stored at the leaf nodes

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CF-Tree



Comments of BIRCH

- Scales linearly: finds a good clustering with a single scan and improves the quality with a few additional scans
- Weakness: handles only numeric data, and sensitive to the order of the data record.



Clustering Categorical Data

- ROCK algorithm: RObust Clustering using links
 - S. Guha, R. Rastogi & K. Shim, ICDE'99
- Major ideas
 - Use links to measure similarity/proximity
 - Not distance-based
 - Computational complexity:
- Algorithm: sampling-based clustering
 - Draw random sample
 - Cluster with links
 - Label data in disk
- Experiments
 - Congressional voting, mushroom data

Similarity Measure

- Traditional measures for categorical data may not work well, e.g., Jaccard coefficient
- Example: Two groups (clusters) of transactions
 - C₁. <a, b, c, d, e>: {a, b, c}, {a, b, d}, {a, b, e}, {a, c, d}, {a, c, e}, {a, d, e}, {b, c, d}, {b, c, e}, {b, d, e}, {c, d, e}
 - \circ C₂. <a, b, f, g>: {a, b, f}, {a, b, g}, {a, f, g}, {b, f, g}
- Jaccard coefficient may lead to wrong clustering result
 - C₁: 0.2 ({a, b, c}, {b, d, e}) to 0.5 ({a, b, c}, {a, b, d})
 - \circ C₁ & C₂: could be as high as 0.5 ({a, b, c}, {a, b, f})
- Jaccard coefficient-based similarity function:

$$Sim(T_1, T_2) = \frac{|T_1 \cap T_2|}{|T_1 \cup T_2|}$$

• Ex. Let $T_1 = \{a, b, c\}, T_2 = \{c, d, e\}$

Sim
$$(T_1, T_2) = \frac{|\{c\}|}{|\{a, b, c, d, e\}|} = \frac{1}{5} = 0.2$$

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Link Measure

- Links: # of common neighbors
 - C₁ <a, b, c, d, e>: {a, b, c}, {a, b, d}, {a, b, e}, {a, c, d}, {a, c, e}, {a, d, e}, {b, c, d}, {b, c, e}, {b, d, e}, {c, d, e}
 - C_2 < a, b, f, g>: {a, b, f}, {a, b, g}, {a, f, g}, {b, f, g}
- Let $T_1 = \{a, b, c\}, T_2 = \{c, d, e\}, T_3 = \{a, b, f\}$
 - link(T_1, T_2) = 4, since they have 4 common neighbors
 - {a, c, d}, {a, c, e}, {b, c, d}, {b, c, e}
 - link(T_{1} , T_{3}) = 3, since they have 3 common neighbors
 - {a, b, d}, {a, b, e}, {a, b, g}
- Thus link is a better measure than Jaccard coefficient

CHAMELEON

- Hierarchical Clustering Using Dynamic Modeling by G. Karypis, E.H. Han, and V. Kumar'99
- Measures the similarity based on a dynamic model
 - Two clusters are merged only if the
 interconnectivity and *closeness (proximity)* between two clusters are high *relative to* the
 internal interconnectivity of the clusters and
 closeness of items within the clusters
 - Cure ignores information about interconnectivity of the objects, Rock ignores information about the closeness of two clusters

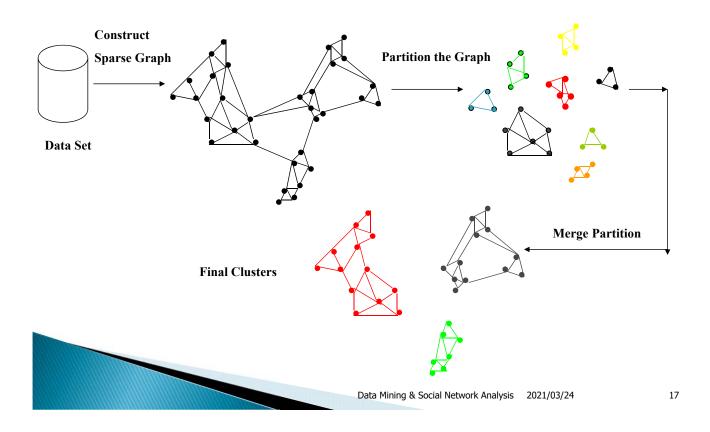
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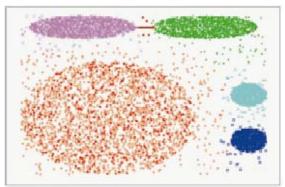
CHAMELEON

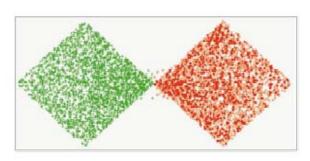
- A two-phase algorithm
 - 1. Use a graph partitioning algorithm: cluster objects into a large number of relatively small sub-clusters
 - Use an agglomerative hierarchical clustering algorithm: find the genuine clusters by repeatedly combining these sub-clusters

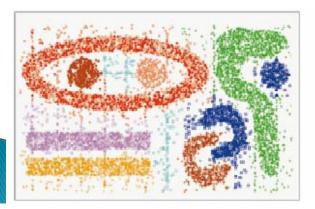
Framework of CHAMELEON

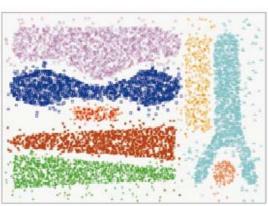


Clustering Complex Objects



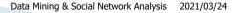






Density-Based Clustering

- Major features:
 - Discover clusters of arbitrary shape
 - Handle noise
 - One scan
 - Need density parameters as termination condition
- Several interesting studies:
 - DBSCAN: Ester, et al. (KDD'96)
 - OPTICS: Ankerst, et al (SIGMOD'99).
 - DENCLUE: Hinneburg & D. Keim (KDD'98)
 - CLIQUE: Agrawal, et al. (SIGMOD'98) (more gridbased)



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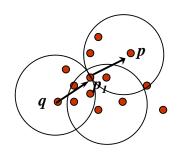
Basic Concepts

- Two parameters:
 - · Eps: Maximum radius of the neighbourhood
 - MinPts: Minimum number of points in an Epsneighbourhood of that point
- $N_{Ens}(p)$: {q belongs to D | dist(p,q) <= Eps}
- Directly density-reachable: A point p is directly density-reachable from a point q w.r.t. Eps, MinPts if
 - p belongs to $N_{Eps}(q)$
 - core point condition:

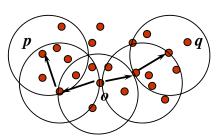
 $|N_{Eps}(q)| >= MinPts$

Density-Reachable and Density-Connected

- Density-reachable:
 - A point p is density-reachable from a point q w.r.t. Eps, MinPtsif there is a chain of points p_1 , ..., p_n , $p_1 = q$, $p_n = p$ such that p_{i+1} is directly density-reachable from p_i



- Density-connected:
 - A point p is density-connected to a point q w.r.t. Eps, MinPts if there is a point o such that both, p and q are density-reachable from o w.r.t. Eps and MinPts

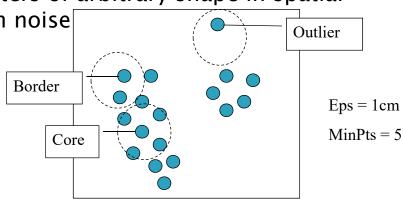


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DBSCAN

- Density Based Spatial Clustering of Applications with Noise
- Relies on a density-based notion of cluster: A cluster is defined as a maximal set of densityconnected points
- Discovers clusters of arbitrary shape in spatial databases with noise



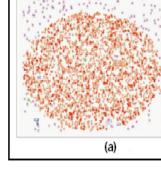
DBSCAN

- Arbitrary select a point p
- Retrieve all points density-reachable from p w.r.t. Eps and MinPts.
- If p is a core point, a cluster is formed.
- If p is a border point, no points are densityreachable from p and DBSCAN visits the next point of the database.
- Continue the process until all of the points have been processed.



Sensitive to Parameters





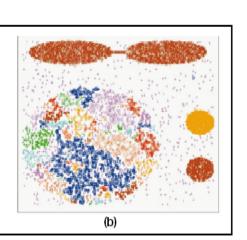
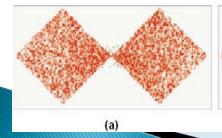
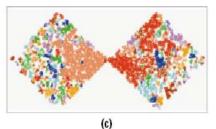


Figure 9. DBScan results for DS2 with MinPts at 4 and Eps at (a) 5.0, (b) 3.5, and (c) 3.0.





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OPTICS

- Ordering Points To Identify the Clustering Structure , Ankerst, Breunig, Kriegel, and Sander (SIGMOD'99)
- Produces a special order of the database wrt its density-based clustering structure
- This cluster-ordering contains info equiv to the density-based clusterings corresponding to a broad range of parameter settings
- Good for both automatic and interactive cluster analysis, including finding intrinsic clustering structure
- Can be represented graphically or using visualization techniques

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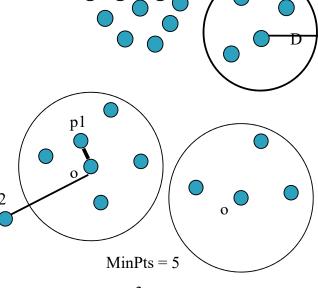
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Some Extension from DBSCAN

- Index-based:
 - k = number of dimensions
 - N = 20
 - p = 75%
 - M = N(1-p) = 5
 - Complexity: O(kN²)
- Core Distance
- Reachability Distance

Max (core-distance (o), d (o, p)) p2

$$r(p1, o) = 2.8cm.$$
 $r(p2, o) = 4cm$



 $\varepsilon = 3 \text{ cm}$

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DENCLUE

- DENsity-based CLUstEring by Hinneburg & Keim (KDD'98)
- Using statistical density functions: $f_{\textit{Gaussian}}(x,y) = e^{\frac{-d(x,y)^2}{2\sigma^2}}$

$$f_{Gaussian}^{D}(x) = \sum_{i=1}^{N} e^{-\frac{d(x,x_i)^2}{2\sigma^2}}$$

Major features

$$\nabla f_{Gaussian}^{D}(x, x_{i}) = \sum_{i=1}^{N} (x_{i} - x) \cdot e^{-\frac{d(x, x_{i})^{2}}{2\sigma^{2}}}$$

- Solid mathematical foundation
- Good for data sets with large amounts of noise
- Allows a compact mathematical description of arbitrarily shaped clusters in high-dimensional data sets
- Significant faster than existing algorithm (e.g., DBSCAN)
- But needs a large number of parameters

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DENCLUE

- Uses grid cells but only keeps information about grid cells that do actually contain data points and manages these cells in a tree-based access structure
- Influence function: describes the impact of a data point within its neighborhood
- Overall density of the data space can be calculated as the sum of the influence function of all data points
- Clusters can be determined mathematically by identifying density attractors
- Density attractors are local maximal of the overall density function

Grid-Based Clustering

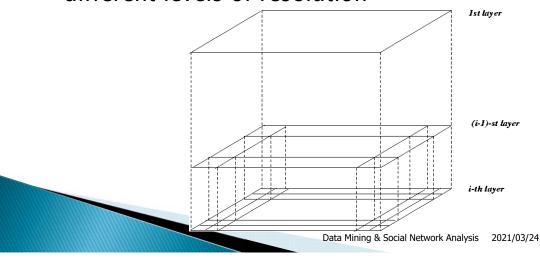
- Using multi-resolution grid data structure
- Several interesting methods
 - STING (a STatistical Information Grid approach)
 by Wang, Yang and Muntz (1997)
 - WaveCluster by Sheikholeslami, Chatterjee, and Zhang (VLDB'98)
 - A multi-resolution clustering approach using wavelet method
 - CLIQUE: Agrawal, et al. (SIGMOD'98)
 - On high-dimensional data (thus put in the section of clustering high-dimensional data



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STING

- A Statistical Information Grid Approach, Wang, Yang and Muntz (VLDB'97)
- The spatial area area is divided into rectangular cells
- There are several levels of cells corresponding to different levels of resolution



STING

- Each cell at a high level is partitioned into a number of smaller cells in the next lower level
- Statistical info of each cell is calculated and stored beforehand and is used to answer queries
- Parameters of higher level cells can be easily calculated from parameters of lower level cell
 - count, mean, s, min, max
 - type of distribution—normal, *uniform*, etc.
- Use a top-down approach to answer spatial data queries
- Start from a pre-selected layer—typically with a small number of cells
- For each cell in the current level compute the confidence interval

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STING

- Remove the irrelevant cells from further consideration
- When finish examining the current layer, proceed to the next lower level
- Repeat this process until the bottom layer is reached
- Advantages:
 - Query-independent, easy to parallelize, incremental update
 - \circ O(K), where K is the number of grid cells at the lowest level
- Disadvantages:
 - All the cluster boundaries are either horizontal or vertical, and no diagonal boundary is detected

WaveCluster

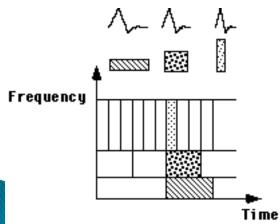
- Clustering by Wavelet Analysis, Sheikholeslami, Chatterjee, and Zhang (VLDB'98)
- A multi-resolution clustering approach which applies wavelet transform to the feature space
- How to apply wavelet transform to find clusters
 - Summarizes the data by imposing a multidimensional grid structure onto data space
 - These multidimensional spatial data objects are represented in a n-dimensional feature space
 - Apply wavelet transform on feature space to find the dense regions in the feature space
 - Apply wavelet transform multiple times which result in clusters at different scales from fine to coarse

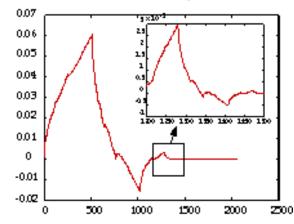


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Wavelet Transform

- Wavelet transform: A signal processing technique that decomposes a signal into different frequency sub-band (can be applied to n-dimensional signals)
- Data are transformed to preserve relative distance between objects at different levels of resolution
- Allows natural clusters to become more distinguishable





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WaveCluster

- Input parameters
 - # of grid cells for each dimension
 - the wavelet, and the # of applications of wavelet transform
- Why is wavelet transformation useful for clustering?
 - Use hat-shape filters to emphasize region where points cluster, but simultaneously suppress weaker information in their boundary
 - · Effective removal of outliers, multi-resolution, cost effective
- Major features:
 - Complexity O(N)
 - Detect arbitrary shaped clusters at different scales
 - Not sensitive to noise, not sensitive to input order
 - Only applicable to low dimensional data
- Both grid-based and density-based

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Model-Based Clustering

- What is model-based clustering?
 - Attempt to optimize the fit between the given data and some mathematical model
 - Based on the assumption: Data are generated by a mixture of underlying probability distribution
- Typical methods
 - Statistical approach
 - · EM (Expectation maximization), AutoClass
 - Machine learning approach
 - COBWEB, CLASSIT
 - Neural network approach
 - SOM (Self-Organizing Feature Map)

EM

- Expectation Maximization (A popular iterative refinement algorithm)
- General idea
 - Starts with an initial estimate of the parameter vector
 - Iteratively rescores the patterns against the mixture density produced by the parameter vector
 - The rescored patterns are used to update the parameter updates
 - Patterns belonging to the same cluster, if they are placed by their scores in a particular component
- Algorithm converges fast but may not be in global optima

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EM

- Initially, randomly assign k cluster centers
- Iteratively refine the clusters based on two steps
 - Expectation step: assign each data point X_i to cluster
 C_i with the following probability

$$P(X_i \in C_k) = p(C_k|X_i) = \frac{p(C_k)p(X_i|C_k)}{p(X_i)},$$

- Maximization step:
 - · Estimation of model parameters

$$m_k = \frac{1}{N} \sum_{i=1}^{N} \frac{X_i P(X_i \in C_k)}{\sum_j P(X_i \in C_j)}.$$

Conceptual Clustering

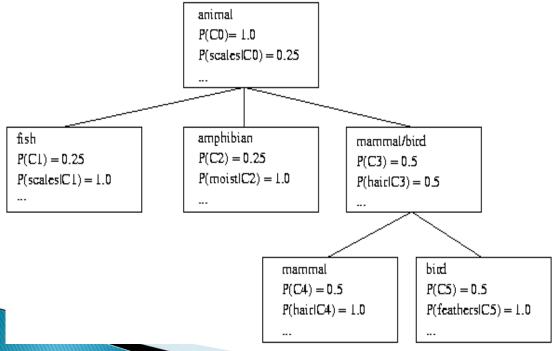
- Conceptual clustering
 - · A form of clustering in machine learning
 - Produces a classification scheme for a set of unlabeled objects
 - Finds characteristic description for each concept (class)
- COBWEB (Fisher'87)
 - A popular and simple method of incremental conceptual learning
 - Creates a hierarchical clustering in the form of a classification tree
 - Each node refers to a concept and contains a probabilistic description of that concept

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COBWEB

▶ A classification tree



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Limitations of COBWEB

- The assumption that the attributes are independent of each other is often too strong because correlation may exist
- Not suitable for clustering large database data skewed tree and expensive probability distributions
- CLASSIT
 - an extension of COBWEB for incremental clustering of continuous data
 - suffers similar problems as COBWEB
- AutoClass (Cheeseman and Stutz, 1996)
 - Uses Bayesian statistical analysis to estimate the number of clusters
 - Popular in industry

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Neural Network

- Neural network approaches
 - Represent each cluster as an exemplar, acting as a "prototype" of the cluster
 - New objects are distributed to the cluster whose exemplar is the most similar according to some distance measure
- Typical methods
 - SOM (Soft-Organizing feature Map)
 - Competitive learning
 - Involves a hierarchical architecture of several units (neurons)
 - Neurons compete in a "winner-takes-all" fashion for the object currently being presented

SOM

- Self-Organizing Feature Map, also called topological ordered maps, or Kohonen Self-Organizing Feature Map (KSOMs)
- It maps all the points in a high-dimensional source space into a 2 to 3-d target space, s.t., the distance and proximity relationship (i.e., topology) are preserved as much as possible
- Similar to k-means: cluster centers tend to lie in a low-dimensional manifold in the feature space



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SOM

- Clustering is performed by having several units competing for the current object
 - The unit whose weight vector is closest to the current object wins
 - The winner and its neighbors learn by having their weights adjusted
- SOMs are believed to resemble processing that can occur in the brain
- Useful for visualizing high-dimensional data in 2or 3-D space

References

- Slides from Prof. J.-W. Han, UIUC
- ▶ Slides from Prof. M.–S. Chen, NTU
- ▶ Slides from Prof. W.–Z. Peng, NCTU

