

**Formulário:**

$$\sin(a + b) = \sin a \cos b + \cos a \sin b$$

$$\sin(a - b) = \sin a \cos b - \cos a \sin b$$

$$\cos(a + b) = \cos a \cos b - \sin a \sin b$$

$$\cos(a - b) = \cos a \cos b + \sin a \sin b$$

$$\sin a + \sin b = 2 \sin \left( \frac{a + b}{2} \right) \cos \left( \frac{a - b}{2} \right)$$

$$\sin a - \sin b = 2 \sin \left( \frac{a - b}{2} \right) \cos \left( \frac{a + b}{2} \right)$$

$$\cos a + \cos b = 2 \cos \left( \frac{a + b}{2} \right) \cos \left( \frac{a - b}{2} \right)$$

$$\cos a - \cos b = -2 \sin \left( \frac{a - b}{2} \right) \sin \left( \frac{a + b}{2} \right)$$

$$f(x_0 + h) = f(x_0) + \frac{df}{dx}(x_0)h + \frac{1}{2} \frac{d^2f}{dx^2}(x_0)h^2 + \dots$$

$$y_p = A_p \cos(\omega t) ; A_{p,n} = C \sin(p\theta) = C \sin \left( \frac{pn\pi}{N+1} \right) ;$$

$$\frac{A_{p-1} + A_{p+1}}{A_p} = \frac{2\omega_0^2 - \omega_n^2}{\omega_0^2} = 2 \cos(\theta_n) ; \theta_n = \frac{n\pi}{N+1} ;$$

$$\omega_n^2 = 2\omega_0^2 \left[ 1 - \cos \left( \frac{n\pi}{N+1} \right) \right] \quad n = 1, \dots, N \text{ em que } N \text{ é o número de partículas}$$