# Simulation Class: Wave equations, Standing Wave, Voltage and Current time evolution, Reflection Coefficient, Impedance and Admittance

Please: Install the RF Toolbox; annotate each figure adequately by using legends, axis labels and titles.

### Input data:

- Generator:  $V_g$ =2 V,  $Z_g$ = $Z_0$ = $50\Omega$
- Line length (air dielectric): 1. 25 m
- Line characteristic impedance:  $Z_0$ =50  $\Omega$
- Frequency: 300 MHz
- Attenuation constant: α (*start simulations with 0 and then change to 0.2 Neper/m at point 6*)
- Load impedance *Z*<sub>L</sub>: *user input (can be complex)*.

## Problem solving steps

- 1. Compute the wavelength  $\lambda$ , the period T, the load reflection coefficient  $\rho_L$ , the propagation constant, the angular frequency  $\omega$  and generate a vector of distance x with 1000 points.
- 2. Compute the general phasor equations for:
  - a. Incident Voltage and Current - $V_i(x)$  e  $I_i(x)$  (2 vectors)
  - b. Reflected Voltage and Current - $V_r(x)$  e  $I_r(x)$  (2 vectors)
- 3. Compute the standing wave voltage amplitude vector  $V_{stand}$  in the transmission line (absolute value of sum of the incident and reflected voltage phasors), plot it as a function of x (activate the grid) and estimate, by hand or using graphical facilities, the VSWR;
- 4. Do as above **for the current**  $I_{stand}$ : use the previous figure but plot the current multiplied by 50 (for easier reading simultaneously with the voltage standing wave) and in red color;
- 5. Plot, in the same figure the symmetrical of the standing waves.
- 6. Develop an animation showing the propagation of the voltage along the line. Using a time step of  $T_{\text{step}}=T/32$  (T is the period):
  - a. Make as the active figure the figure of previous point 3 and 4 (standing wave);
  - b. Freeze the ranges: use function *ylim* (or *axis*) for a symmetric ranging of y axis (or both axis);
  - c. hold the figure (hold on);
  - d. Set time to 0: t1=0;
  - e. Do in a loop (suggested number of snapshots 5\*32) *Note: do not use j or i for the loop control variable* 
    - i. Plot at time  $t_1$  a snapshot of the line voltage vector  $real(V(x)e^{j\omega t_1})$  as a function of x getting an handle to the plot hy (hv=plot(...)); (the use of the time domain equations can also be used and are likely to be more efficient: try at home)
    - ii. Plot at time  $t_1$  a snapshot of the scaled line current vector  $real(I(x)e^{j\omega t_1})$  as a function of **x** getting an handle to the plot hi (hi=plot(...));
    - iii. Pause for a fraction of second (0.25s for example);
    - iv. Increase t<sub>1</sub> by T<sub>step</sub>
    - v. Delete the two plots deleting the handles (delete(hv); delete(hi))<sup>1</sup>.
- 7. Comment the results and simulate for other load impedances and mainly for the SC and CA.
- 8. Compute and plot, in a new figure, a polar plot of the (complex) reflection coefficient (use the definition that is:  $\rho(x) = V_r(x)/V_i(x)$ .

### Input impedance and susceptance

- 1. Compute the line input impedance  $\mathbf{Z}_{in}(x)$  (use the definition  $(\mathbf{V}(x)/\mathbf{I}(x))$ ) and plot in a new figure the resistance and reactance as a function of x (use different colors for real –resistance- and imaginary – reactance-parts).
- 2. Identify manually, or moving a point in the plot using graphical facilities, the closest distances to the load,  $x_1$  and  $x_2$ , adequate to match the system by using a reactance in series with the line;
- 3. Compute the input admittance  $Y_{in}(x)$  (1/ $Z_{in}(x)$ ) and plot the conductance and susceptance (as above) in a new figure;
- 4. Identify the closest distances to the load,  $x'_1$  and  $x'_2$ , adequate to match the system by inserting a parallel susceptance;
- 5. Plot as well, in a new figure, the complex impedance in a plane and make the "axis equal". Plot also, in a new figure, the reflection coefficient in a Smith Chart (use the function *smithplot()*).
- 6. Run again the full script you have till now but using  $\alpha$ =0.2 Np/m or other values.

#### Home work

1. Study carefully all the subjects addressed in this simulation class.

Some useful MatLab functions: atan2(y,x); abs(); angle(); plot(x,y,'b'); axis([x1 x2 y1 y2]), polar( $\theta$ , r); grid on; axis square; polarplot(); hold on; linspace; xlim(); ylim(); pause(); real(); imag(); pause(), figure(); legend(); xlabel(); ylabel(); title(); ylim(); xlim(); title(); smithplot()

*Latex use in labels, legends, etc is possible: Z\_{in} looks like Zin ()* 

Note: Use ".\*" "./" and ".^2" instead of "\*" "/" "^" to make operation point by point.

```
pause_time = .1;
nx = 150; x=linspace(0,2*pi,nx); y=sin(x);
figure(1); clf; plot(x,y); hold on; grid on;
h = plot(x(1),y(1),'ro'); %Gets an handle to the plotted point to be moved
  set(h,'XData',x(n),'YData',y(n)); %Replaces the moving point plotted
  pause(pause_time)
end
```

A possible solution is also to use the function *linkdata* that automatically updates the plot if plotted data is changed

```
Example
t=1:10;
x = randn(10,1);
plot(t,x);
linkdata on;
                  %Any future update to x is automatically updated in the plot;
pause(2);
x=randn(10,1);
```

<sup>&</sup>lt;sup>i</sup> To execute the animation you can also retrieve the handle to the plotted data and update it. The example plots a moving point over a sine plot