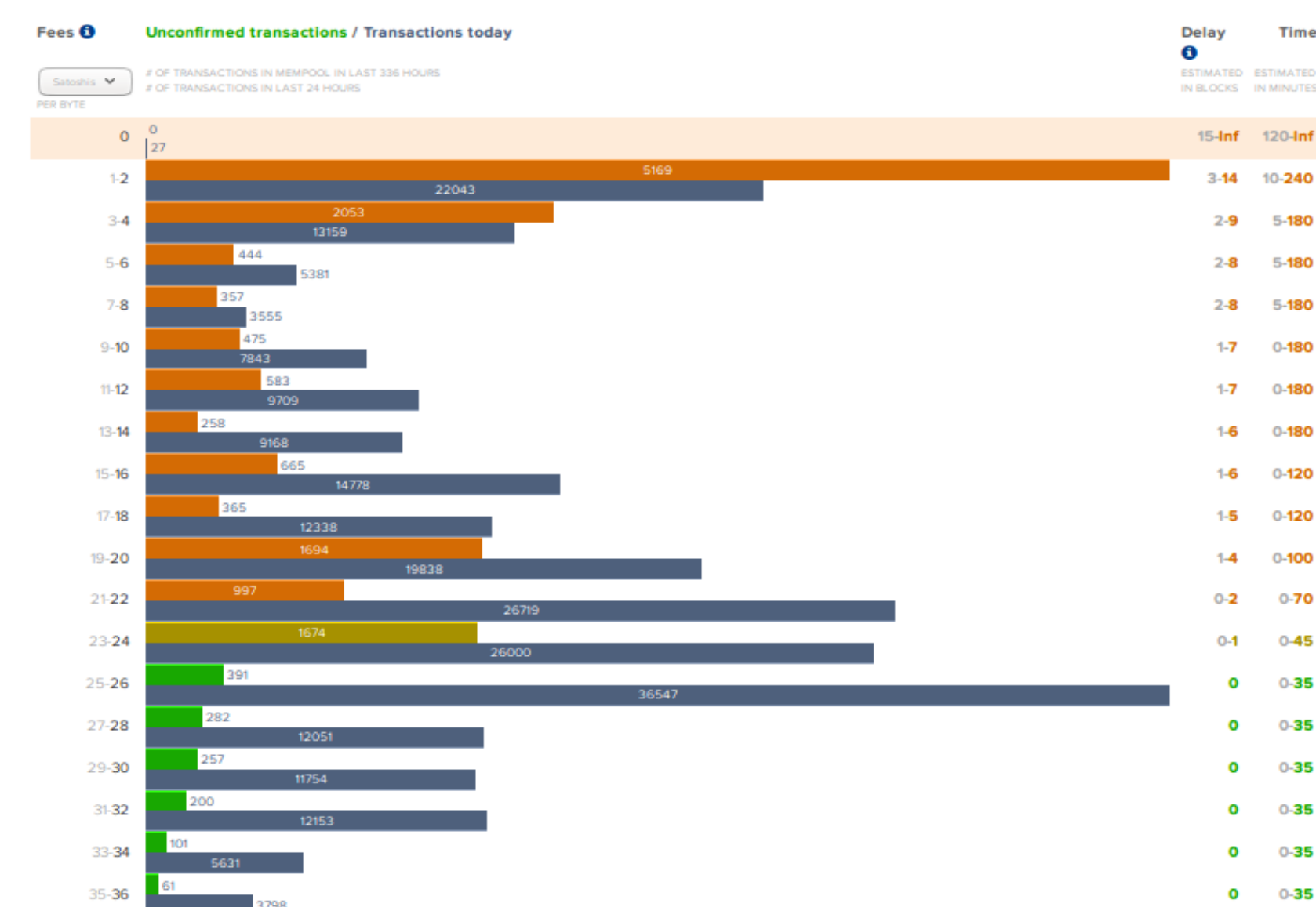


Are transaction fees in Bitcoin/Ethereum fair?



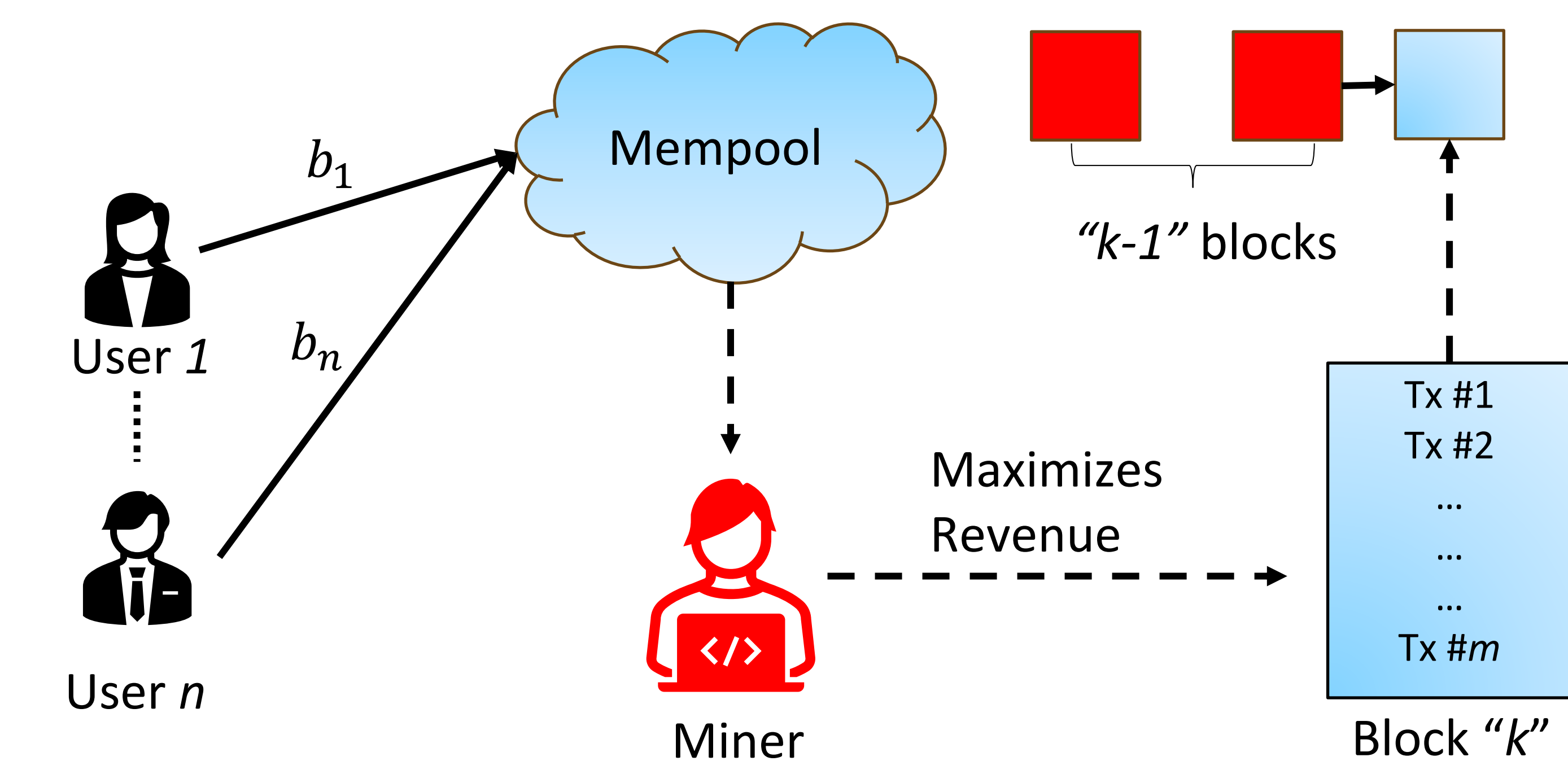
- Transaction fees in Bitcoin were envisioned to be 'optional'
- In practice, transactions with marginal fee fail to get confirmed
- E.g., Users paying less fees have a waiting time of  $\geq 9$  blocks, while it is  $\geq 14$  blocks for those who pay an insignificant amount [4]

**Bitcoin's Unfinished Business: Why Micropayments Still Matter**  
Tiny, cheap-to-deliver payments can open new markets for small digital goods. Can a new wave of crypto-inflected startups plug a longstanding gap in the internet? This piece is part of CoinDesk's Payments Week.  
By David Z. Morris | Apr 29, 2022 at 12:15 a.m. | Updated Sep 19, 2023 at 9:33 p.m. | Layer 2

Credit: Coindesk

**India's UPI Hits Record Volume**  
NOVEMBER 2, 2023

Credit: Global Finance



Transaction Fee Mechanisms (TFMs) [1]

Popular TFMs

First-price Auction (FPA)

Second-price Auction (SPA)

EIP-1559

Incentive Properties

User Incentive Compatibility (UIC)

Miner Incentive Compatibility (MIC)

Off-chain Collusion Properties

**Goal:** To design TFMs that are fairer to the transaction creators (or users), while simultaneously preserving the incentive compatibility for both the miner and the users.

## Fairness Notions for Transaction Fee Mechanisms

- Zero-free Transaction Inclusion (ZTi)**  
The probability with which a transaction  $t$  with transaction fee  $b_t = 0$  gets included in a block  $B_k$  is strictly non-zero. That is,  $\Pr(t \in B_k) > 0$ .
- Monotonicity**  
The probability with which a transaction  $t$  gets included in a block  $B_k$  increases with an increase in its transaction fee  $b_t$ , given the remaining bids  $b_{-t}$  are fixed. That is,  $\Pr(t \in B_k | b_{-t}, b_t + \epsilon) > \Pr(t \in B_k | b_{-t}, b_t)$  for any  $\epsilon > 0$  and fixed  $b_{-t}$ .

A TFM satisfying both our fairness notions ensures that each transaction has a non-zero probability of getting accepted!

## Impossibility of Simultaneously Maximizing Miner Utility and Satisfying ZTi

**Theorem (Informal).** No TFM with a non-trivial payment rule, which provides a strategic miner complete control over the transactions to add to its block, satisfies Zero-free Transaction Inclusion (ZTi).

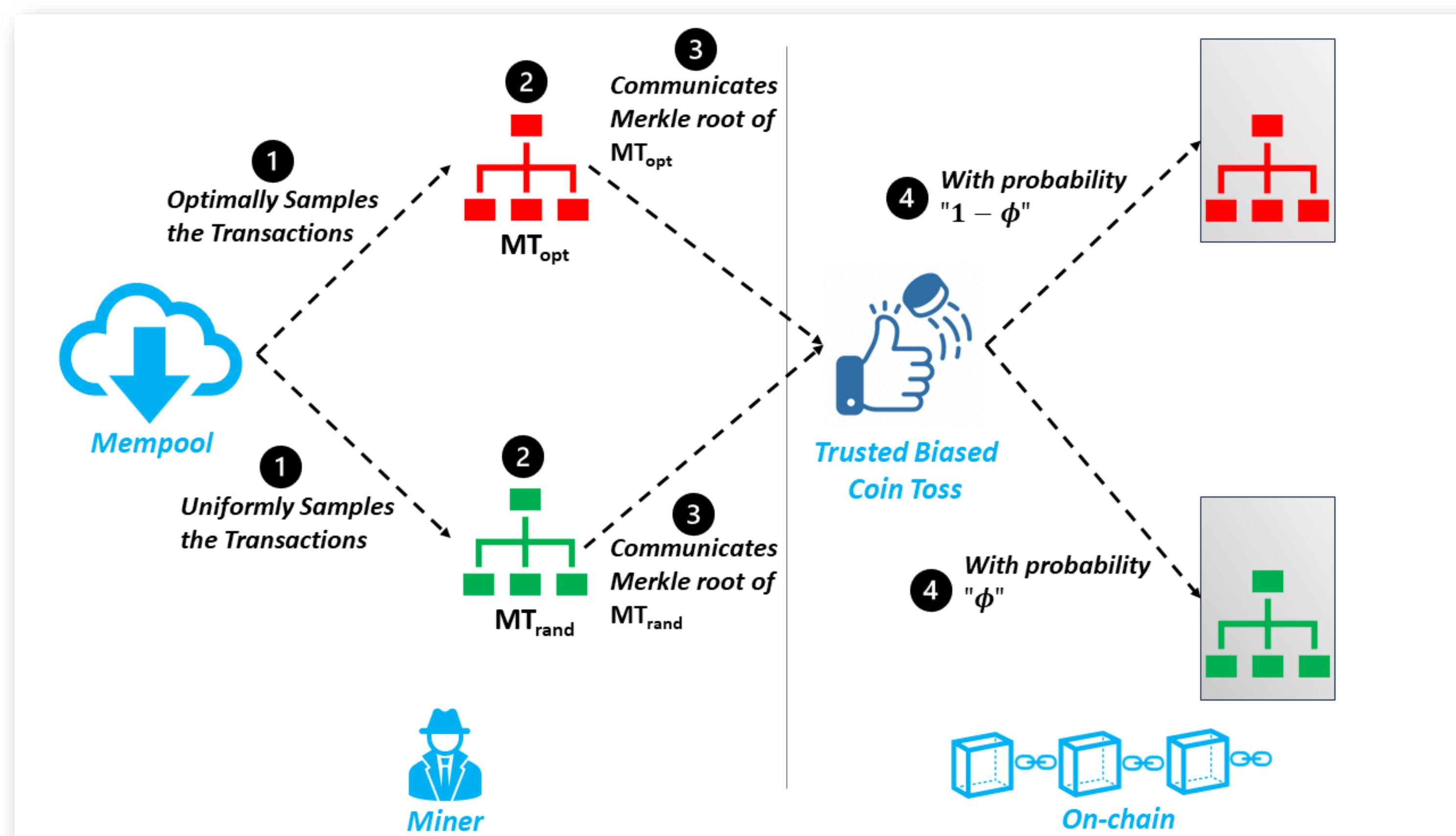
## Results Summary:

We note that most existing TFMs do not satisfy ZTi. In contrast, rTFM – with an appropriate payment and burning rule – simultaneously satisfies our fairness notions along with UIC and MIC.

★ Only if the base fee is "excessively low"

TFM	UIC	MIC	ZTi	Monotonicity
FPA [1]	✗	✓	✗	✓
SPA [1]	✓	✗	✗	✓
EIP-1559 [1]	✓★	✓	✗	✓
BitcoinZF [4]	✓	✗	✓	✓
rTFM + FPA	✗	✓	✓	✓
rTFM + FPA	✓★	✓	✓	✓

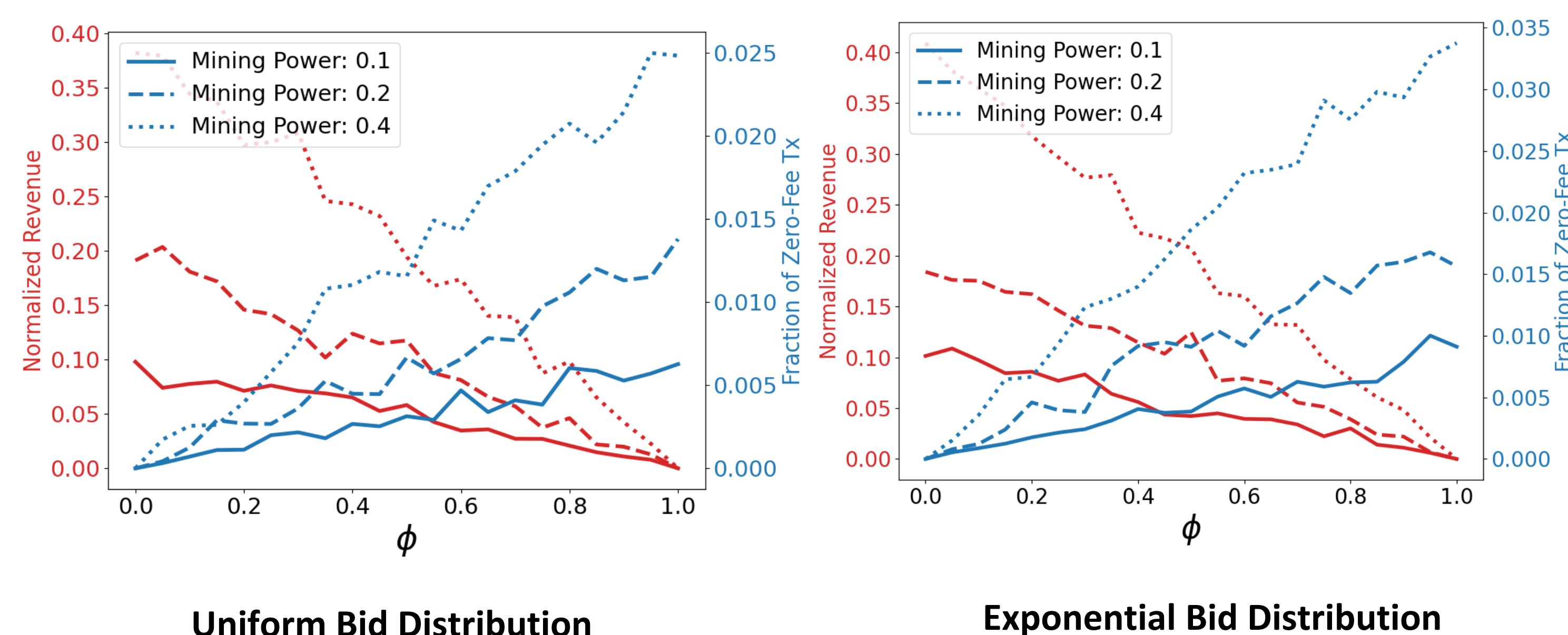
## rTFM: Fairness in TFMs using On-chain Randomization



## Trusted Biased Coin Toss:

$$O(\text{Hash}(B_k, \phi)) = \text{Hash}(B_k) < \phi \cdot TD ? \text{MT}_{\text{rand}} : \text{MT}_{\text{opt}}$$

## rTFM: Empirical Evaluation



## Key References

- Roughgarden (2021). Transaction Fee Mechanism Design. In: EC
- Chung and Shi (2023). Foundations of transaction fee mechanism design. In: SODA
- Siddiqui et al. (2020). BitcoinF: Achieving Fairness for Bitcoin in Transaction-Fee-Only Model. In: AAMAS