Time Series Project

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```
library(R.matlab)
## R.matlab v3.7.0 (2022-08-25 21:52:34 UTC) successfully loaded. See ?R.matlab for help.
## Attaching package: 'R.matlab'
## The following objects are masked from 'package:base':
##
       getOption, isOpen
library(depmixS4)
## Loading required package: nnet
## Loading required package: MASS
## Loading required package: Rsolnp
## Loading required package: nlme
data <- readMat("Mouse28-140313_BS0150_HMMready.mat")</pre>
angdata <- as.vector(data$resampledAwakeHeadAngleData)</pre>
# Transpose that data so that there are 71 columns, one column for each cell, and 15243 rows, one for e
celldata <- t(data$celldata)</pre>
# Exclude cells that are active less than 100 times overall
col_idx = which(colSums(celldata)<100)</pre>
celldata = celldata[,-col_idx]
# Reduced to 59 cells
dim(celldata)
## [1] 15243
```

```
cell_data <- data.frame(celldata)</pre>
# Response and list must be on list-form
# Response has to be in a list
res <- list()
# List of families. One for each cell
families <- list()</pre>
# Number of columns(cells)
n_cells <- ncol(cell_data)</pre>
for (i in 1:n_cells) {
  form <- as.formula(paste(colnames(cell_data)[i], "~ 1",sep=""))</pre>
  res[[i]] = form
  families[[i]] = poisson()
# Model with 5 states
model5 <- depmix(response = res, nstates = 5, data= cell_data, family = families)</pre>
fit5 <- fit(model5)</pre>
## converged at iteration 34 with logLik: -948315.1
summary(fit5)
## Initial state probabilities model
## pr1 pr2 pr3 pr4 pr5
   0 0 0 1
## Transition matrix
           toS1 toS2 toS3 toS4 toS5
## fromS1 0.915 0.001 0.052 0.032 0.000
## fromS2 0.001 0.902 0.001 0.042 0.055
## fromS3 0.030 0.000 0.913 0.000 0.056
## fromS4 0.036 0.075 0.000 0.889 0.000
## fromS5 0.000 0.045 0.046 0.000 0.909
## Response parameters
## Resp 1 : poisson
## Resp 2 : poisson
## Resp 3 : poisson
## Resp 4 : poisson
## Resp 5 : poisson
## Resp 6 : poisson
## Resp 7 : poisson
## Resp 8 : poisson
## Resp 9 : poisson
## Resp 10 : poisson
## Resp 11 : poisson
## Resp 12 : poisson
```

```
## Resp 13 : poisson
## Resp 14 : poisson
## Resp 15 : poisson
## Resp 16 : poisson
## Resp 17 : poisson
## Resp 18 : poisson
## Resp 19 : poisson
## Resp 20 : poisson
## Resp 21 : poisson
## Resp 22 : poisson
## Resp 23 : poisson
## Resp 24 : poisson
## Resp 25 : poisson
## Resp 26 : poisson
## Resp 27 : poisson
## Resp 28 : poisson
## Resp 29 : poisson
## Resp 30 : poisson
## Resp 31 : poisson
## Resp 32 : poisson
## Resp 33 : poisson
## Resp 34 : poisson
## Resp 35 : poisson
## Resp 36 : poisson
## Resp 37 : poisson
## Resp 38 : poisson
## Resp 39 : poisson
## Resp 40 : poisson
## Resp 41 : poisson
## Resp 42 : poisson
## Resp 43 : poisson
## Resp 44 : poisson
## Resp 45 : poisson
## Resp 46 : poisson
## Resp 47 : poisson
## Resp 48 : poisson
## Resp 49 : poisson
## Resp 50 : poisson
## Resp 51 : poisson
## Resp 52 : poisson
## Resp 53 : poisson
## Resp 54 : poisson
## Resp 55 : poisson
## Resp 56 : poisson
## Resp 57 : poisson
## Resp 58 : poisson
## Resp 59 : poisson
##
       Re1.(Intercept) Re2.(Intercept) Re3.(Intercept) Re4.(Intercept)
## St1
                 0.036
                                  0.224
                                                 -2.696
                                                                  -2.602
                                                                  -2.131
## St2
                -0.014
                                  0.181
                                                 -3.555
                                                                  -2.347
## St3
                -0.078
                                                 -0.845
                                  0.103
## St4
                -0.144
                                  0.362
                                                 -1.382
                                                                  -2.315
## St5
                 0.100
                                  0.039
                                                 -2.590
                                                                  -1.997
       Re5.(Intercept) Re6.(Intercept) Re7.(Intercept) Re8.(Intercept)
```

```
## St1
                -2.802
                                 -2.100
                                                  -5.844
                                                                   -4.197
## St2
                -4.307
                                 -1.763
                                                  -6.881
                                                                   -0.707
## St3
                                                  -0.344
                                                                   -0.950
                -2.494
                                 -1.738
## St4
                -2.244
                                 -2.906
                                                  -6.871
                                                                   -3.780
## St5
                 -0.609
                                 -3.568
                                                  -2.304
                                                                   -5.337
##
       Re9.(Intercept) Re10.(Intercept) Re11.(Intercept) Re12.(Intercept)
## St1
                                   2.082
                                                     1.694
                 1.798
                                                                      -1.962
## St2
                 1.217
                                   1.942
                                                      1.562
## St3
                 1.355
                                    2.022
                                                      1.666
                                                                      -2.458
## St4
                                                                      -1.479
                  1.810
                                   2.013
                                                      1.574
## St5
                  1.279
                                   1.931
                                                      1.348
                                                                      -3.651
##
       Re13.(Intercept) Re14.(Intercept) Re15.(Intercept) Re16.(Intercept)
## St1
                  0.041
                                    0.009
                                                     -3.250
                                                                         0.536
## St2
                 -1.309
                                   -0.507
                                                     -2.334
                                                                         0.325
## St3
                 -0.953
                                    -0.598
                                                      -0.156
                                                                         0.647
## St4
                 -0.923
                                    0.845
                                                      -3.339
                                                                         0.518
## St5
                 -1.541
                                    -0.271
                                                     -3.213
                                                                         0.358
       Re17.(Intercept) Re18.(Intercept) Re19.(Intercept) Re20.(Intercept)
## St1
                 -3.659
                                   -2.487
                                                     -3.521
                                                                        -1.211
## St2
                 -1.360
                                    -3.962
                                                      -5.513
                                                                        -3.065
## St3
                 -3.845
                                   -2.909
                                                     -0.879
                                                                       -1.598
## St4
                 -3.456
                                   -3.438
                                                      -6.177
                                                                       -2.930
## St5
                 -3.764
                                   -3.592
                                                     -2.264
                                                                       -2.719
       Re21.(Intercept) Re22.(Intercept) Re23.(Intercept) Re24.(Intercept)
## St1
                  0.308
                                                     -3.213
                                    1.737
                                                                       -1.288
## St2
                 -0.240
                                    1.788
                                                      0.427
                                                                        1.152
## St3
                 -0.588
                                     1.828
                                                      -3.260
                                                                        -0.943
## St4
                                    1.626
                                                                        -0.897
                  1.098
                                                      -2.425
## St5
                 -0.412
                                    1.512
                                                     -2.877
                                                                        0.274
       Re25.(Intercept) Re26.(Intercept) Re27.(Intercept) Re28.(Intercept)
## St1
                   1.693
                                    -2.364
                                                     -2.063
                                                                         1.910
## St2
                   1.511
                                    -1.194
                                                      -2.039
                                                                         1.775
## St3
                   1.878
                                   -2.594
                                                     -2.192
                                                                         1.886
## St4
                   1.722
                                   -2.614
                                                                         2.035
                                                      -2.148
## St5
                   1.684
                                    -2.579
                                                      -2.180
                                                                         1.817
       Re29.(Intercept) Re30.(Intercept) Re31.(Intercept) Re32.(Intercept)
## St1
                   1.915
                                    1.315
                                                      0.814
                                                                        -1.757
## St2
                   1.471
                                    1.288
                                                       0.717
                                                                        -1.772
## St3
                   1.750
                                    1.301
                                                       0.865
                                                                        -1.512
## St4
                                    1.282
                                                       0.716
                                                                       -1.513
                   1.771
## St5
                   1.467
                                    1.241
                                                       0.907
       Re33.(Intercept) Re34.(Intercept) Re35.(Intercept) Re36.(Intercept)
                                   -1.224
## St1
                 -0.483
                                                       0.519
                                                                        -0.863
## St2
                 -2.525
                                                                       -1.379
                                    -1.382
                                                       0.579
## St3
                                                                       -1.295
                 -1.367
                                   -1.128
                                                       0.605
## St4
                                    -1.163
                                                       0.479
                                                                        -1.139
                 -3.971
## St5
                 -2.736
                                    -1.346
                                                       0.425
                                                                        -1.909
##
       Re37.(Intercept) Re38.(Intercept) Re39.(Intercept) Re40.(Intercept)
## St1
                   1.972
                                   -1.139
                                                     -2.890
                                                                        -4.467
## St2
                                                      -2.935
                   1.976
                                    -0.819
                                                                        0.134
## St3
                   1.910
                                   -1.993
                                                     -2.314
                                                                        -3.944
## St4
                                                                       -2.204
                   1.975
                                   -0.314
                                                     -0.433
## St5
                   1.801
                                   -1.364
                                                     -2.596
                                                                        -3.421
##
       Re41.(Intercept) Re42.(Intercept) Re43.(Intercept) Re44.(Intercept)
```

```
## St1
                 -2.363
                                    0.575
                                                     -0.883
                                                                      -2.177
## St2
                  0.822
                                   -2.894
                                                     -1.254
                                                                       -4.293
                                   -0.212
                                                     -2.344
## St3
                 -2.958
                                                                       2.486
                 -3.017
                                                                      -6.465
## St4
                                    2.079
                                                     -1.991
## St5
                  1.076
                                   -2.459
                                                     -1.571
                                                                      -1.227
##
       Re45.(Intercept) Re46.(Intercept) Re47.(Intercept) Re48.(Intercept)
## St1
                 -1.741
                                   -0.143
                                                     -3.596
                                                                      -5.587
                                                     -4.587
                                                                      -4.315
## St2
                 -1.554
                                    0.863
## St3
                 -3.439
                                   -0.091
                                                     0.781
                                                                       0.039
## St4
                                   -0.263
                 -0.724
                                                     -3.400
                                                                      -3.196
## St5
                 -1.425
                                    0.953
                                                     0.753
                                                                       0.310
##
       Re49.(Intercept) Re50.(Intercept) Re51.(Intercept) Re52.(Intercept)
## St1
                 -5.133
                                   -1.326
                                                     1.414
                                                                      -3.076
## St2
                 -0.019
                                   -4.326
                                                                       0.801
                                                     -5.116
## St3
                 -5.766
                                   -2.955
                                                     -4.579
                                                                      -1.085
## St4
                 -0.859
                                   -1.429
                                                     -1.607
                                                                       1.985
## St5
                 -2.296
                                   -2.805
                                                     -3.589
                                                                      -0.427
       Re53.(Intercept) Re54.(Intercept) Re55.(Intercept) Re56.(Intercept)
## St1
                 -0.887
                                   -1.425
                                                     -2.845
                                                                      -5.230
## St2
                                   -2.267
                 -5.455
                                                     -4.010
                                                                       -0.757
                                                                      -0.042
## St3
                 -4.273
                                   -2.148
                                                     -4.006
## St4
                 -1.375
                                   -2.500
                                                     -2.511
                                                                      -0.784
## St5
                 -3.904
                                   -0.400
                                                     -2.910
                                                                       2.277
##
       Re57.(Intercept) Re58.(Intercept) Re59.(Intercept)
                 -1.030
                                   0.052
## St1
                                                     -0.648
## St2
                 -4.318
                                   -3.324
                                                     -0.401
## St3
                  2.774
                                   -4.277
                                                     -0.822
## St4
                                   -2.409
                                                     -0.461
                 -6.465
## St5
                 -0.841
                                   -4.503
                                                     -0.652
```

AIC(model5)

[1] 4579341

Fit models with more than 5 states

```
# Dette tar tid!
# Model with 10 states
#mod10 <- depmix(response = res, nstates = 10, data = cell_data, family = families)
#fit10 <- fit(mod10)
# Model with 15 states
#mod15 <- depmix(response = res, nstates = 15, data = cell_data, family = families)
#fit15 <- fit(mod15)</pre>
```

#summary(fit10)

Model selection based on AIC

```
# Model selection based on AIC

AIC(fit5)

## [1] 1897268

# AIC(fit10)

# AIC(fit15)

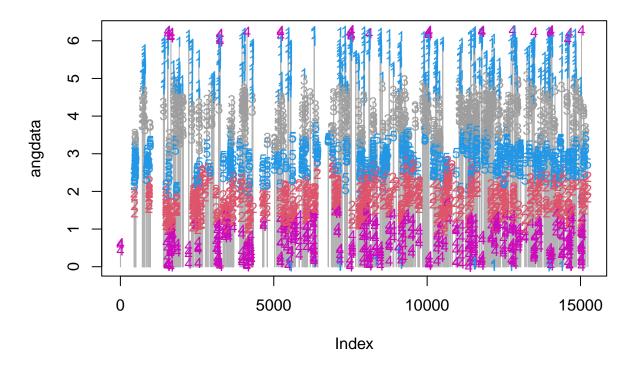
# AIC(fit20)
```

Indices of each state

```
# States for all time intervals
states = posterior(fit5)$state
## Warning in .local(object, ...): Argument 'type' not specified and will default
## to 'viterbi'. This default may change in future releases of depmixS4. Please
## see ?posterior for alternative options.
# Indices for which state is 1
idx_state1 <- which(states == 1)</pre>
idx_state2 <- which(states == 2)</pre>
idx state3 <- which(states == 3)</pre>
idx_state4 <- which(states == 4)</pre>
idx_state5 <- which(states == 5)</pre>
#Avrege for of
avg_state1 <- mean(angdata[idx_state1], na.rm = TRUE)</pre>
avg_state2 <- mean(angdata[idx_state2], na.rm = TRUE)</pre>
avg_state3 <- mean(angdata[idx_state3], na.rm = TRUE)</pre>
avg_state4 <- mean(angdata[idx_state4], na.rm = TRUE)</pre>
avg_state5 <- mean(angdata[idx_state5], na.rm = TRUE)</pre>
avg <- c(avg_state1, avg_state2, avg_state3, avg_state4, avg_state5)</pre>
```

Histogram over head direction for each state

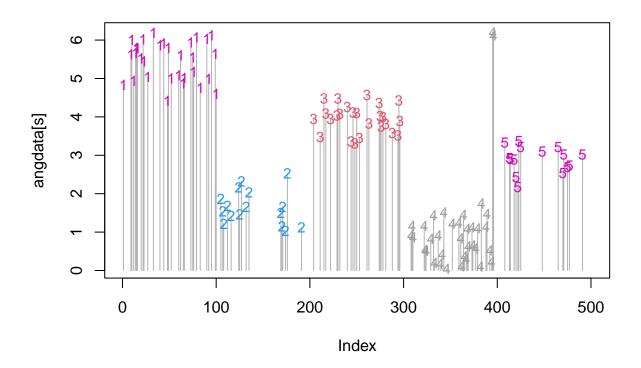
```
plot(angdata, main="", type="h", col = gray(.7))
text(angdata, col=6*states-2, labels=states, cex=.9)
```



Difficult to see. Take a random sample of the angle data

```
# Don't plot all head angles. Take a random sample. Easier to visualize
s_1 = sample(idx_state1, 100)
s_2 = sample(idx_state2, 100)
s_3 = sample(idx_state3, 100)
s_4 = sample(idx_state4, 100)
s_5 = sample(idx_state5, 100)
s=c(s_1, s_2, s_3, s_4, s_5)

plot(angdata[s], type = "h", col=gray(.7))
text(angdata[s], col = 6*states[s], labels = states[s], cex=.9)
```



Plotting the average head direction of each state

```
## Plot of mean head
avg
```

[1] 5.255357 1.773650 4.004686 1.037438 2.848121

plot(avg, type="h")

