

Linkage and segregation analysis in medical genetics

Statistical methods in genetic relatedness and pedigree analysis

NORBIS course, 13th – 17th of June 2022, Oslo

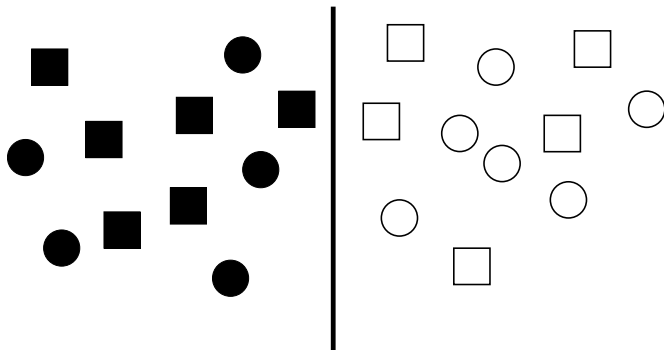
Magnus Dehli Vigeland

Outline

- Monogenic diseases: Inheritance patterns
- Traditional linkage analysis
- Segregation analysis in modern genetic diagnostics

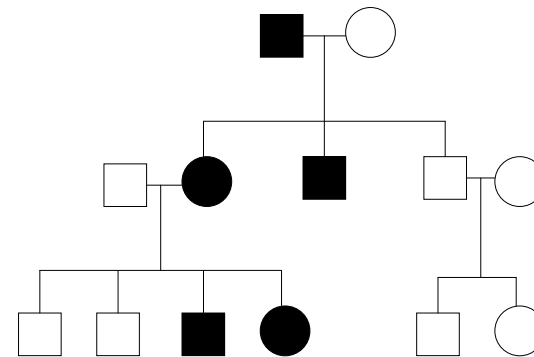
Finding the cause of genetic diseases: Two main approaches

Multifactorial disease



- Association analysis
- Case/control design
- Population based

Monogenic disease



- Linkage analysis
- Family design

Monogenic diseases: Inheritance patterns

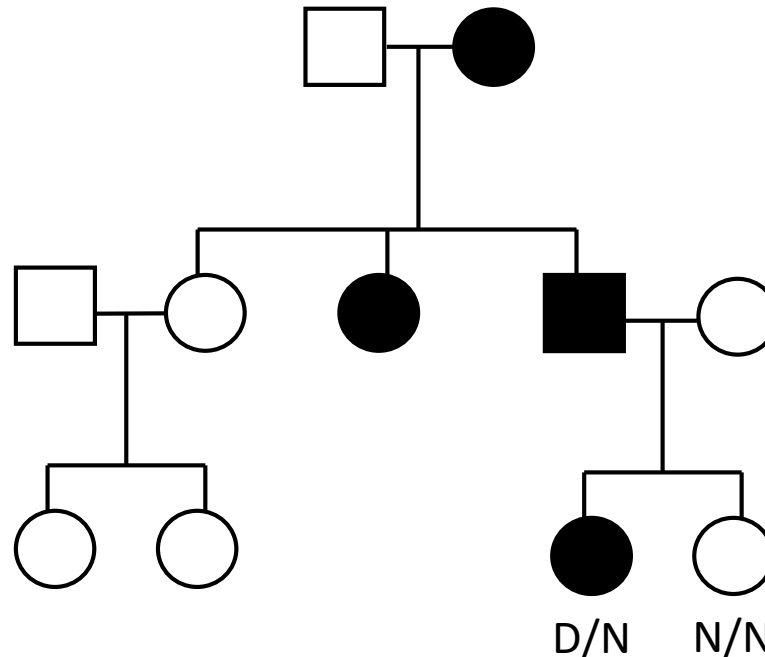
Autosomal dominant (AD) inheritance

Penetrance parameters

$$f_0 = P(\text{aff} \mid NN)$$

$$f_1 = P(\text{aff} \mid DN)$$

$$f_2 = P(\text{aff} \mid DD)$$



Penetrance values:

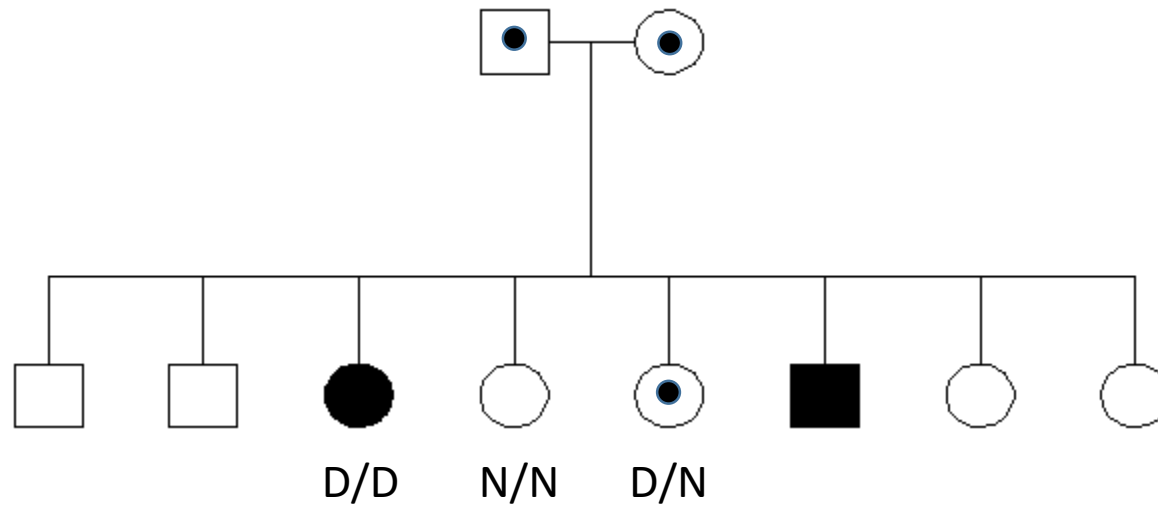
$$f_0 = 0$$

$$f_1 = 1$$

$$f_2 = 1$$

- ~50% affected children of an affected mother or father
- Affected male:female ratio is ~1
- Can be inherited from mother or father to both sons and daughters

Autosomal recessive (AR) inheritance



Penetrance values:

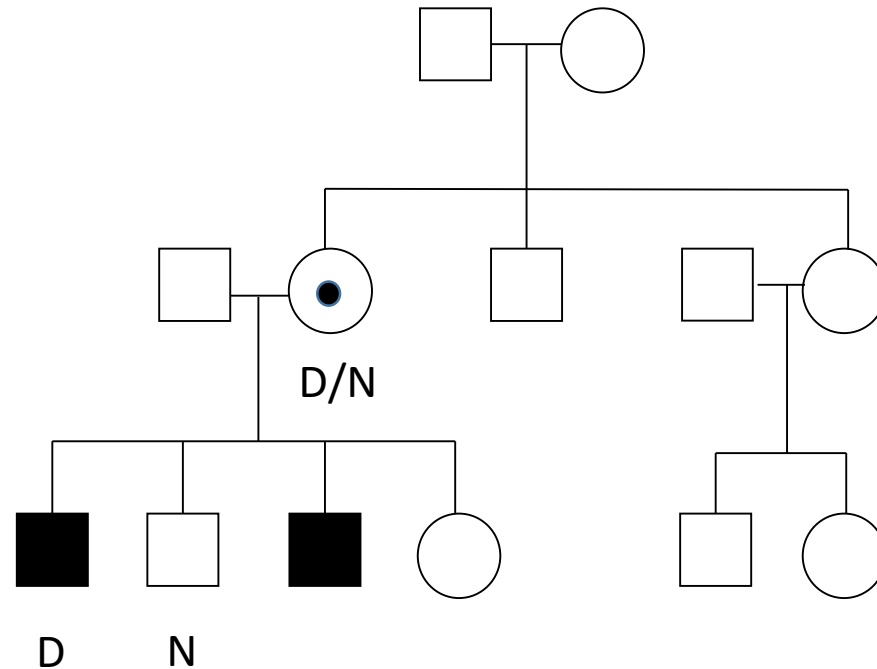
$$f_0 = 0$$

$$f_1 = 0$$

$$f_2 = 1$$

- Usually healthy parents
- ~25% of the children are affected
- Affected male:female ratio is ~1

X-linked recessive inheritance



Penetrance values:

Females:

$$f_0 = 0$$

$$f_1 = 0$$

$$f_2 = 1$$

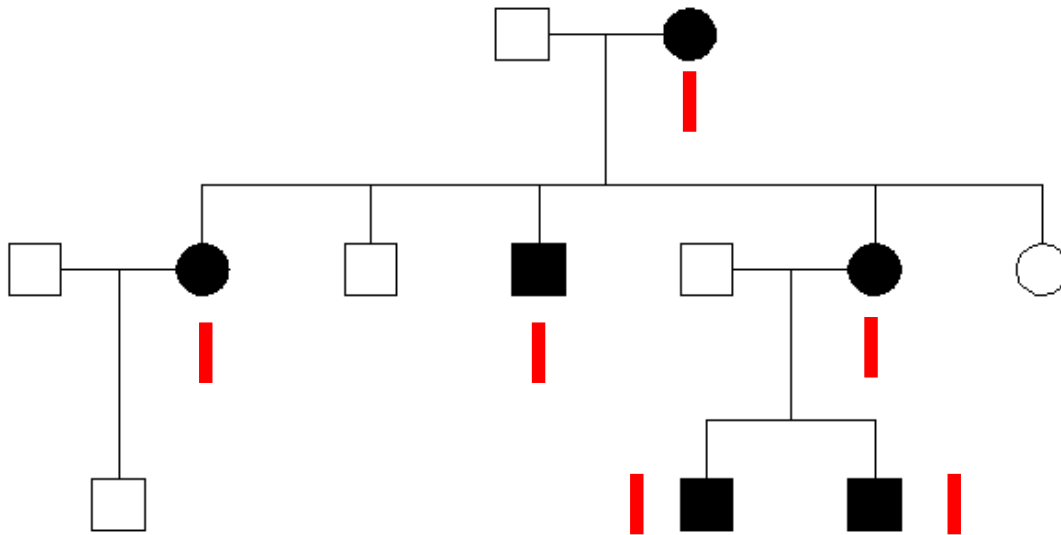
Males:

$$f_0 = 0$$

$$f_1 = 1$$

- Only males are affected
- Usually inherited through healthy females

Linkage analysis – the basic principle



Compare

- the inheritance pattern of the disease
- IBD pattern across the genome

Goal: Identify the region harbouring the disease-causing locus

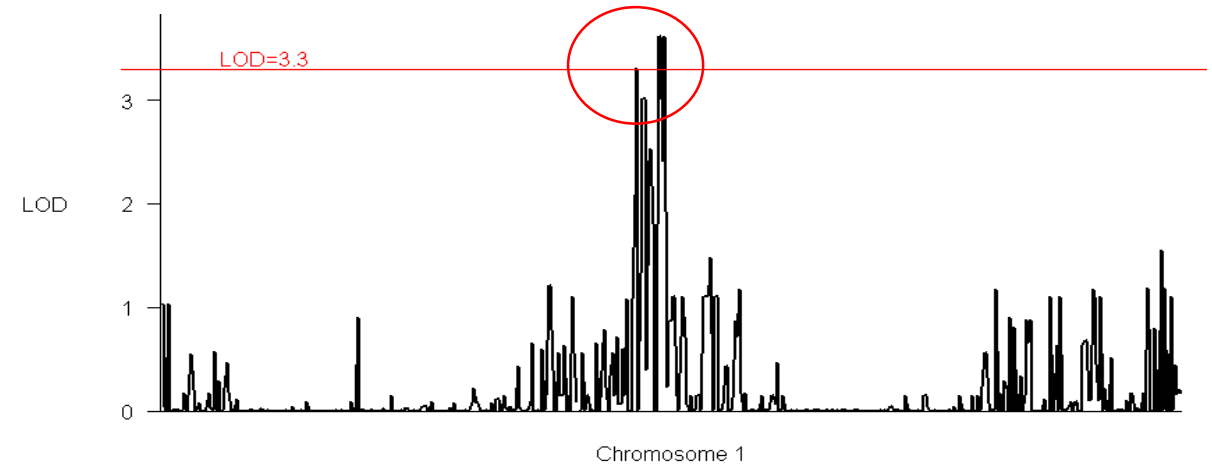
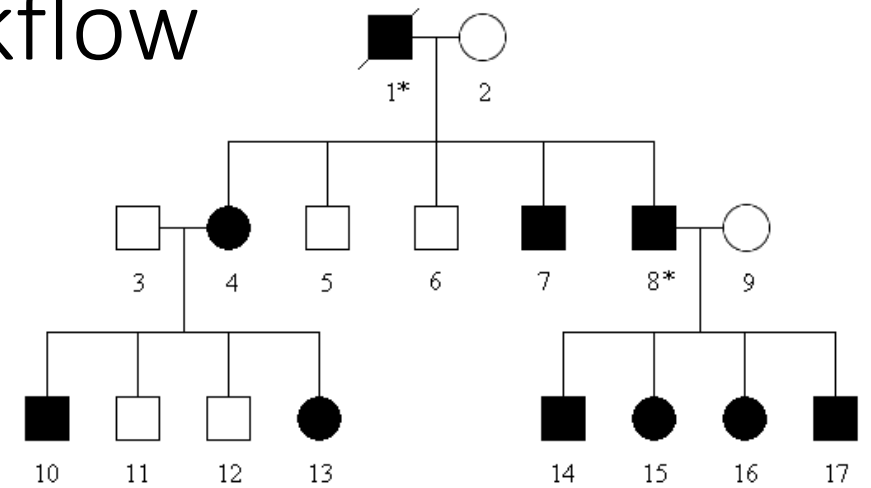
Linkage analysis - traditional workflow

1. Starting point: Large affected family

2. SNP genotyping

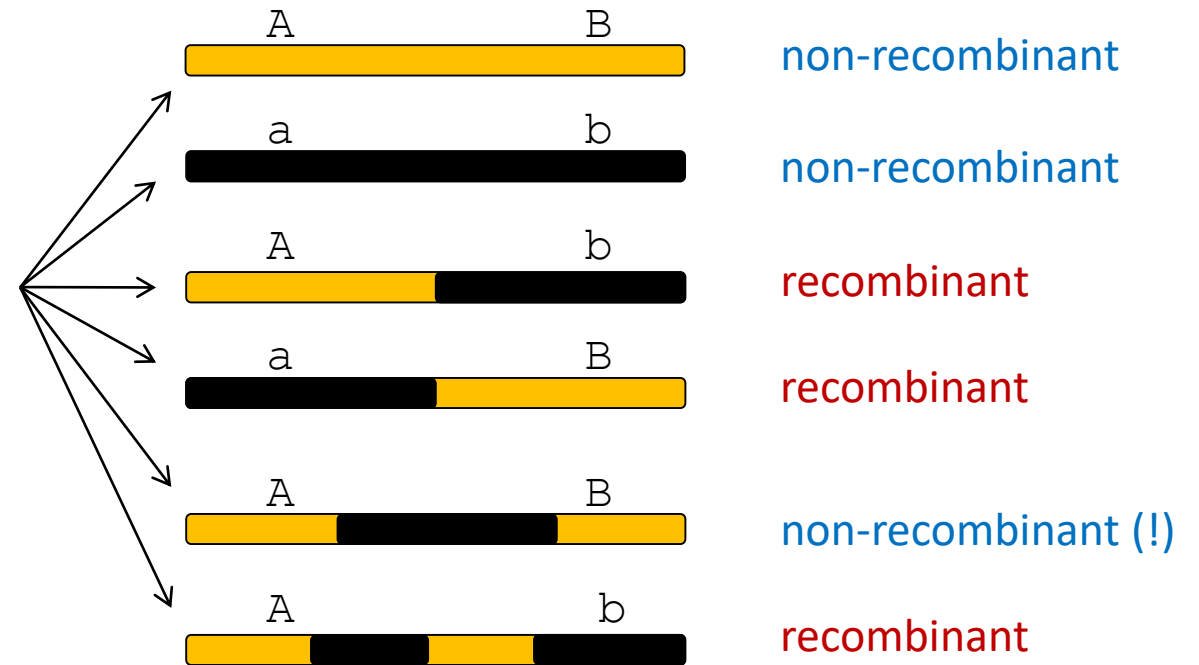
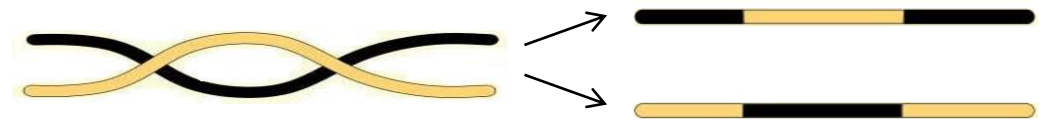
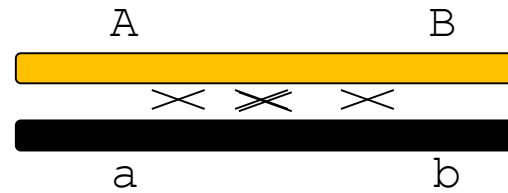
3. Parametric linkage analysis

4. Sequence genes in linkage peak → identify causal mutation



Recombination rate

- The **recombination rate** between two loci
= average number of recombinant gametes



Loci on different chromosomes: $\theta = 0.5$

Loci far apart on the same chromosome: $\theta \approx 0.5$

Loci right next to each other: $\theta = 0$

Definition: Two loci are *linked* if $\theta < 0.5$

"On the same chromosome, not too far apart"

Crossover rate vs. recombination rate

Crossover rate (= *genetic distance*)

$$d = E[\text{\#crossovers}]$$

- Based on a fundamental property of the meiosis
- Statistically well-behaved
- But:
Hard to observe directly

Recombination rate

$$\theta = E[\text{\#recombinant gametes}]$$

- Not as intuitive
- Relative to markers
- But:
Easy to estimate using genotyping

Haldane's map function:

$$\theta = \frac{1}{2}(1 - e^{-2d})$$

Hypothesis testing in linkage

- Hypotheses:

$$H_0: \theta = 0.5 \quad (\text{no linkage})$$

$$H_A: \theta < 0.5 \quad (\text{linkage})$$

θ = recombination rate
between marker and disease

- For historical reasons the test statistic is

$$\text{LOD} = \log_{10} \frac{P(\text{data} \mid \theta = \theta)}{P(\text{data} \mid \theta = 0.5)}$$

LOD = "logarithm of the odds"

- Traditional significance thresholds:

- Autosomal loci: $\text{LOD} = 3$ ($p \approx 0.0001$)

- X-linked loci: $\text{LOD} = 1.8$

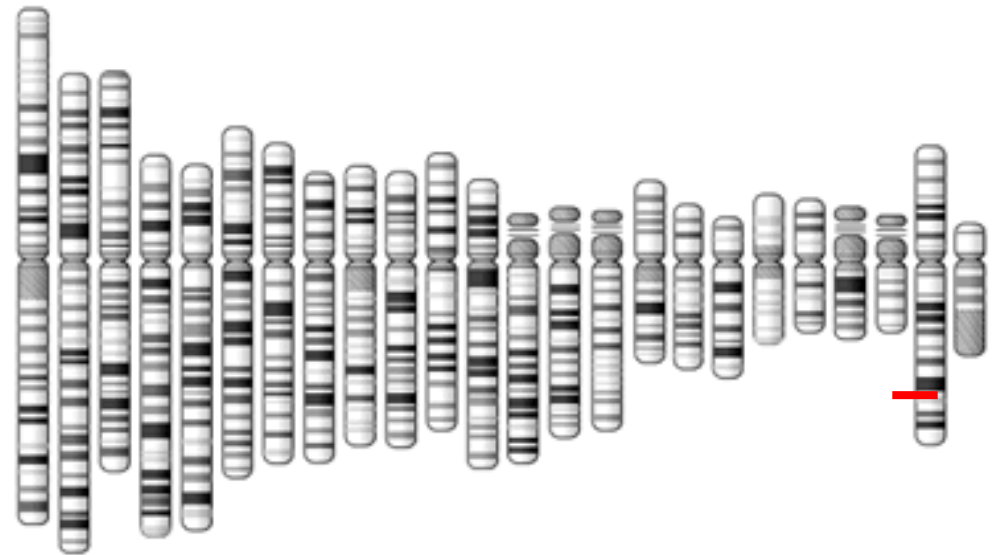
Why the LOD? Why not $p < 0.05$?

- The common significance level $\alpha = 0.05$ is not used in linkage analysis
- Reason: Low *a priori* probability of H_A

$H_0: \theta = 0.5$ (no linkage)

$H_A: \theta < 0.5$ (linkage)

$$P(H_A) = P(\text{random marker near the disease}) \\ \approx 1/50$$



© Clinical Tools, Inc.

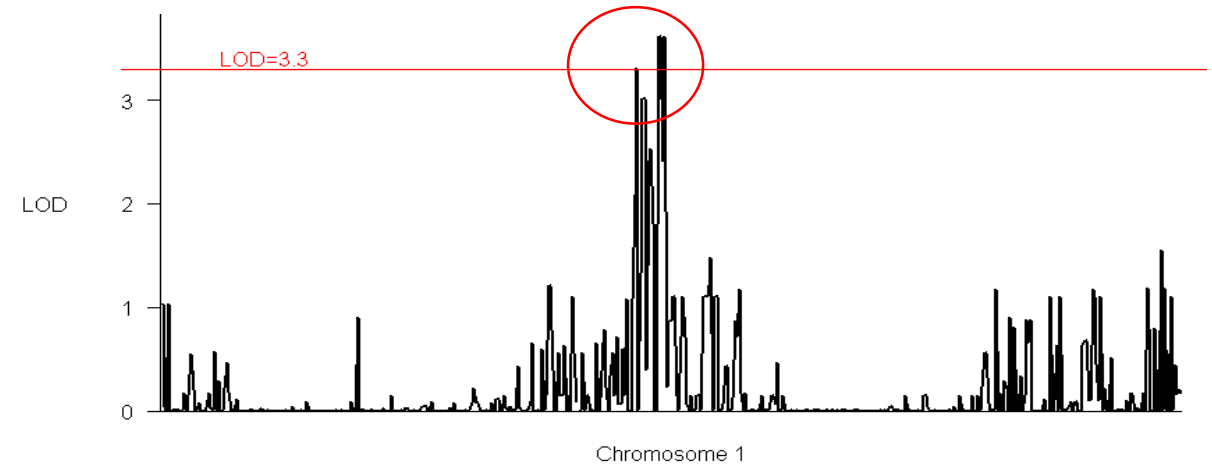
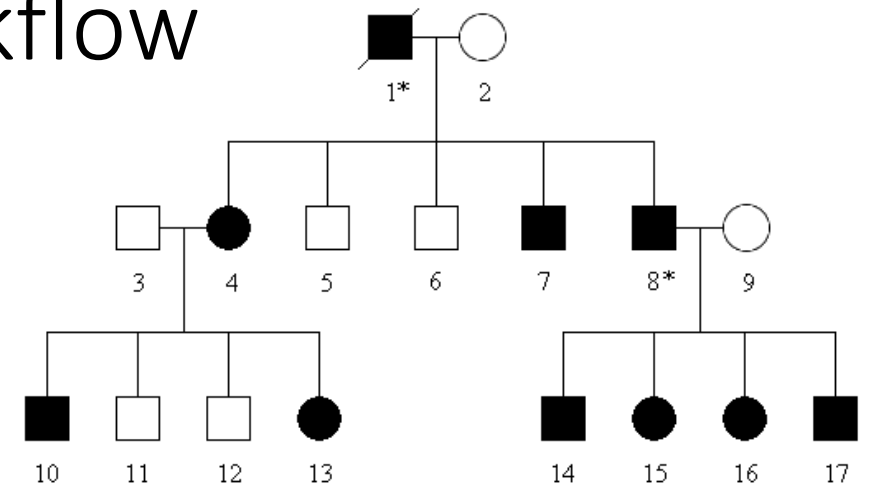
Linkage analysis - traditional workflow

1. Starting point: Large affected family

2. SNP genotyping

3. Parametric linkage analysis

4. Sequence genes in linkage peak → identify causal mutation



Modern approach (last decade)

1. Patient genome



identify the causal variant



Interpretation
guidelines

1. Sequence



High-throughput sequencing

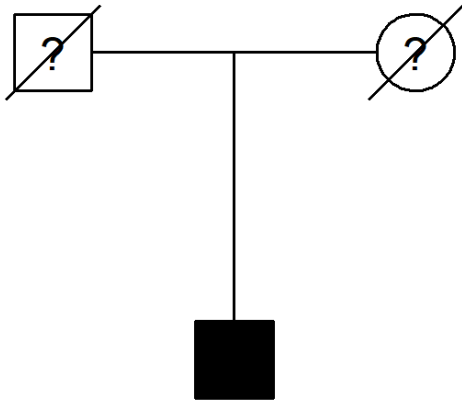


2. List of variants

Databases

- dbSNP / dbVAR
- 1000 Genomes / ExAC / gnomAD
- OMIM / ClinVar / HGMD
- + many others!

Segregation: Motivating example



- Autosomal dominant disease
- Suspected DNA variant identified:
 - Rare/novel
 - Predicted damaging
 - But...no previous connection with disease

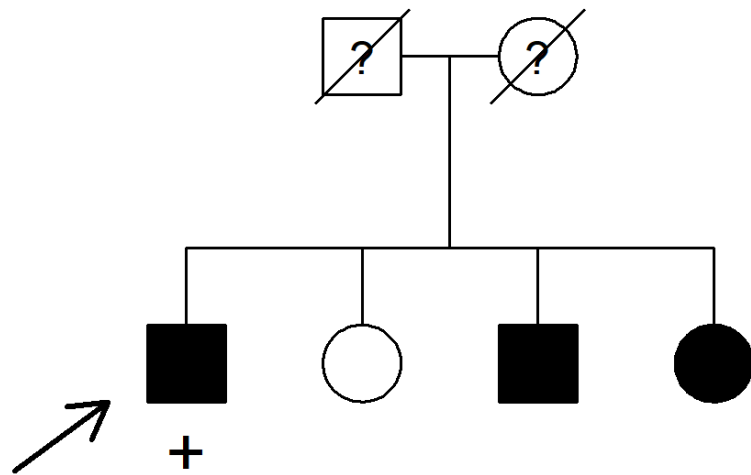
Classification: VUS
(Variant of uncertain significance)



What to do?

- ~~Replicate in unrelated patient~~
- ~~Functional studies~~
- Segregation?

Segregation: Motivating example



+ Confirmed carrier
- Confirmed noncarrier
↗ Proband/index patient

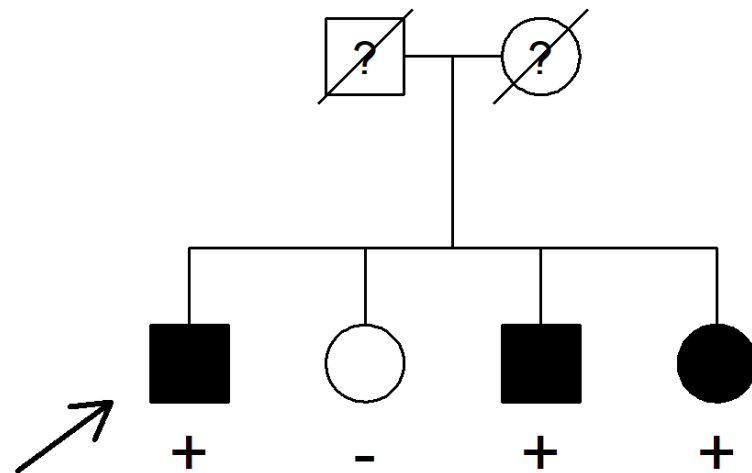
- Autosomal dominant disease
- Suspected DNA variant identified:
 - Rare/novel
 - Predicted damaging
 - But...no previous connection with disease

Classification: VUS
(Variant of uncertain significance)

What to do?

- ~~Replicate in unrelated patient~~
- ~~Functional studies~~
- Segregation?

Segregation: Motivating example



+ Confirmed carrier
- Confirmed noncarrier
↗ Proband/index patient

- Autosomal dominant disease
- Suspected DNA variant identified:
 - Rare/novel
 - Predicted damaging
 - But...no previous connection with disease

Classification: VUS
(Variant of uncertain significance)

What to do?

- ~~Replicate in unrelated patient~~
- ~~Functional studies~~
- Segregation?


Co-segregation
supports
pathogenicity!

But **how much?**

The ACMG framework for variant interpretation

[Published: 05 March 2015](#)

Standards and guidelines for the interpretation of sequence variants: a joint consensus recommendation of the American College of Medical Genetics and Genomics and the Association for Molecular Pathology

[Sue Richards PhD](#) , [Nazneen Aziz PhD](#), [Sherri Bale PhD](#), [David Bick MD](#), [Soma Das PhD](#), [Julie Gastier-Foster PhD](#), [Wayne W. Grody MD, PhD](#), [Madhuri Hegde PhD](#), [Elaine Lyon PhD](#), [Elaine Spector PhD](#), [Karl Voelkerding MD](#) & [Heidi L. Rehm PhD](#) on behalf of ; on behalf of the ACMG Laboratory Quality Assurance Committee

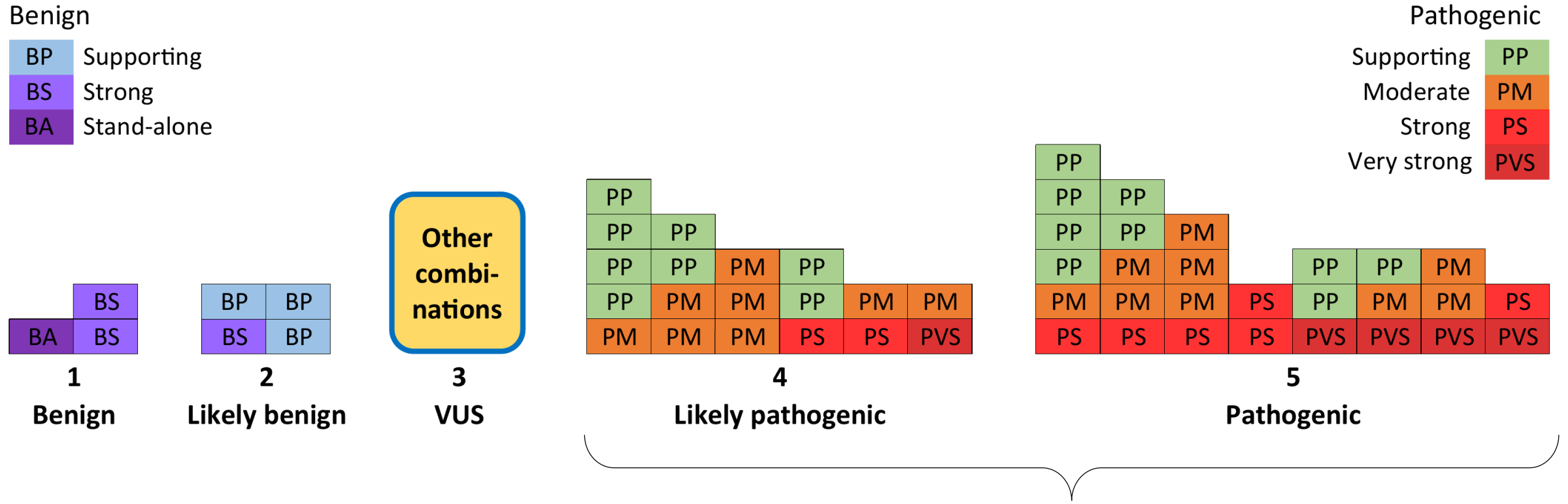
[Genetics in Medicine](#) **17**, 405–423 (2015) | [Cite this article](#)

228k Accesses | **9421** Citations | **299** Altmetric | [Metrics](#)

ACMG evidence framework

	Benign		Pathogenic			
	Strong	Supporting	Supporting	Moderate	Strong	Very strong
Population data	MAF is too high for disorder BA1/BS1 OR observation in controls inconsistent with disease penetrance BS2			Absent in population databases PM2	Prevalence in affecteds statistically increased over controls PS4	
Computational and predictive data		Multiple lines of computational evidence suggest no impact on gene /gene product BP4 Missense in gene where only truncating cause disease BP1	Multiple lines of computational evidence support a deleterious effect on the gene /gene product PP3	Novel missense change at an amino acid residue where a different pathogenic missense change has been seen before PM5 Protein length changing variant PM4	Same amino acid change as an established pathogenic variant PS1	Predicted null variant in a gene where LOF is a known mechanism of disease PVS1
Functional data	Well-established functional studies show no deleterious effect BS3		Missense in gene with low rate of benign missense variants and path. missenses common PP2	Mutational hot spot or well-studied functional domain without benign variation PM1	Well-established functional studies show a deleterious effect PS3	
Segregation data	Nonsegregation with disease BS4		Cosegregation with disease in multiple affected family members PP1	Increased segregation data →		
De novo data				De novo (without paternity & maternity confirmed) PM6	De novo (paternity and maternity confirmed) PS2	
Allelic data		Observed in <i>trans</i> with a dominant variant BP2 Observed in <i>cis</i> with a pathogenic variant BP2		For recessive disorders, detected in <i>trans</i> with a pathogenic variant PM3		
Other database		Reputable source w/out shared data = benign BP6	Reputable source = pathogenic PP5			
Other data		Found in case with an alternate cause BP5	Patient's phenotype or FH highly specific for gene PP4			

ACMG classification rules



= genetic diagnosis

⇒ access to treatment & follow-up of patient and family

ACMG evidence framework



PP1 BS4 Segregation analysis

...

Statistical evaluation of co-segregation may be difficult in the clinical laboratory setting. If appropriate families are identified, clinical laboratories are encouraged to work with experts in statistical or population genetics to ensure proper modeling and to avoid incorrect conclusions of the relevance of the variant to the disease.

(Richards et al., 2015)

	BS3		path. missenses common PP2	without benign variation PM1	effect PSS	
Segregation data	Nonsegregation with disease BS4		Cosegregation with disease in multiple affected family members PP1	Increased segregation data →		
De novo data				De novo (without paternity & maternity confirmed) PM6	De novo (paternity and maternity confirmed) PS2	
Allelic data		Observed in <i>trans</i> with a dominant variant BP2 Observed in <i>cis</i> with a pathogenic variant BP2		For recessive disorders, detected in <i>trans</i> with a pathogenic variant PM3		
Other database		Reputable source w/out shared data = benign BP6	Reputable source = pathogenic PP5			
Other data		Found in case with an alternate cause BP5	Patient's phenotype or FH highly specific for gene PP4			

How to **quantify** segregation evidence?

- 2003: Thompson et al. (Am J Hum Genet)

A full-likelihood method for the evaluation of causality of sequence variants from family data

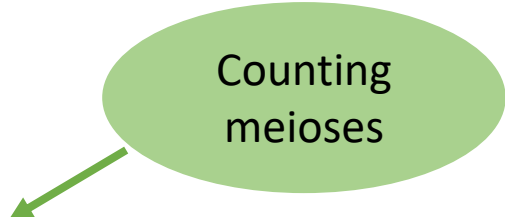
- 2008: Bayrak-Toydemir et al (Exp Mol Pathol)

Likelihood ratios to assess genetic evidence for clinical significance of uncertain variants: Hereditary hemorrhagic telangiectasia as a model



Bayes factor

Counting
meioses



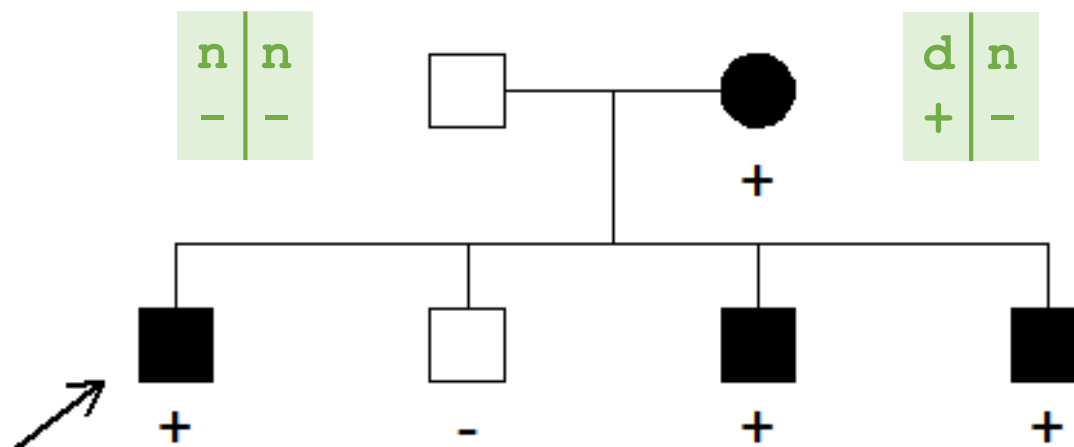
-
- 2016: Jarvik & Browning (Am J Hum Genet)

Consideration of cosegregation in the pathogenicity classification of genomic variants

Jarvik & Browning (2016)

1. Segregation score based on counting: $N = (1/2)^m$

m = number of meioses
informative for cosegregation



$m = 4$
(moderate evidence)

2. Suggested ACMG thresholds

- $N \leq \frac{1}{32} \approx 0.03$: **strong** ($m \geq 5$)
- $N \leq \frac{1}{16} \approx 0.06$: **moderate** ($m \geq 4$)
- $N \leq \frac{1}{8} = 0.125$: **supportive** ($m \geq 3$)

Jarvik & Browning



	Benign		Pathogenic			
	Strong	Supporting	Supporting	Moderate	Strong	Very Strong
Population Data	MAF is too high for disorder <i>BA1/BS1</i> OR observation in controls inconsistent with disease penetrance <i>BS2</i>			Absent in population databases <i>PM2</i>	Prevalence in affecteds statistically increased over controls <i>PS4</i>	
Computational And Predictive Data		Multiple lines of computational evidence suggest no impact <i>BP4</i> Missense when only truncating cause disease <i>BP1</i> Silent variant with non predicted splice impact <i>BP7</i> In-frame indels in repeat w/out known function <i>BP3</i>	Multiple lines of computational evidence support a deleterious effect on the gene /gene product <i>PP3</i>	Novel missense change at an amino acid residue where a different pathogenic missense change has been seen before <i>PM5</i> Protein length changing variant <i>PM4</i>	Same amino acid change as an established pathogenic variant <i>PS1</i>	Predicted null variant in a gene where LOF is a known mechanism of disease <i>PVS1</i>
Functional Data	Well-established functional studies show no deleterious effect <i>BS3</i>		Missense in gene with low rate of benign missense variants and path. missenses common <i>PP2</i>	Mutational hot spot or well-studied functional domain without benign variation <i>PM1</i>	Well-established functional studies show a deleterious effect <i>PS3</i>	
Segregation Data	Non-segregation with disease <i>BS4</i>		$N \leq 1/8$ if 1 family $N \leq 1/4$ if > 1 family	$N \leq 1/16$ if 1 family $N \leq 1/8$ if > 1 family	$N \leq 1/32$ if 1 family $N \leq 1/16$ if > 1 family	
De novo Data				<i>De novo</i> (without paternity & maternity confirmed) <i>PM6</i>	<i>De novo</i> (paternity & maternity confirmed) <i>PS2</i>	
Allelic Data		Observed in <i>trans</i> with a dominant variant <i>BP2</i> Observed in <i>cis</i> with a pathogenic variant <i>BP2</i>		For recessive disorders, detected in <i>trans</i> with a pathogenic variant <i>PM3</i>		
Other Database		Reputable source w/out shared data = benign <i>BP6</i>	Reputable source = pathogenic <i>PP5</i>			
Other Data		Found in case with an alternate cause <i>BP5</i>	Patient's phenotype or FH highly specific for gene <i>PP4</i>			

Jarvik & Browning (2016)

- Advantage
 - Works well in **simple cases**
- What are **simple cases**?
 - no phenocopies
 - complete penetrance
 - allele entered pedigree only once
 - "everyone" genotyped
- Disadvantage:
 - Confusing and potentially inaccurate in other cases

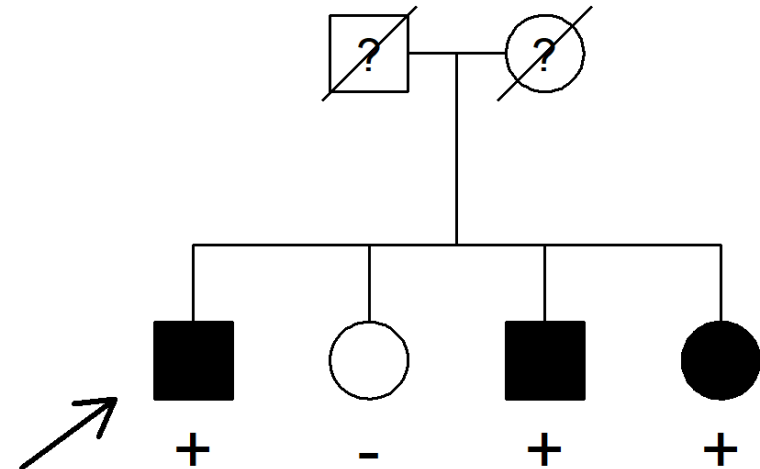
Disease model (f_0, f_1, f_2)

$$f_0 = P(\text{affected} \mid \text{genotype} = n/n)$$

$$f_1 = P(\text{affected} \mid \text{genotype} = d/n)$$

$$f_2 = P(\text{affected} \mid \text{genotype} = d/d)$$

- f_0 = phenocopy rate
- f_1 = penetrance



*"[Thompson's method is more accurate], but **requires training and tools.**" (J&B 2016)*

The Bayes factor approach

- Recall, for models M_1 and M_2 :

$$\frac{P(M_1 \mid \text{data})}{P(M_2 \mid \text{data})} = \frac{P(\text{data} \mid M_1)}{P(\text{data} \mid M_2)} \cdot \frac{P(M_1)}{P(M_2)}$$
$$\text{Posterior odds} = \text{Bayes factor} \cdot \text{Prior odds}$$

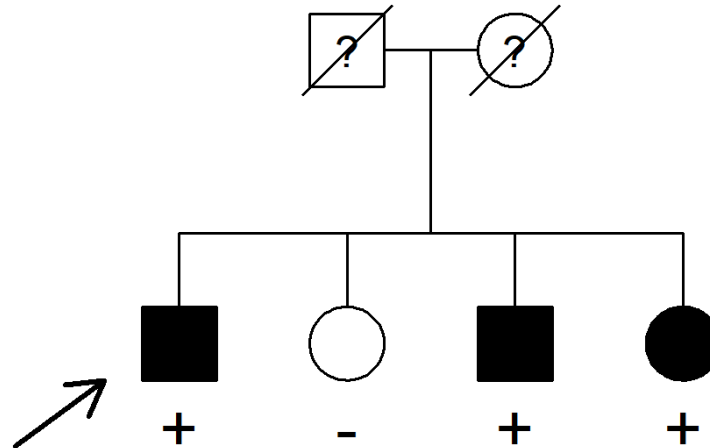
- Our **models**

\mathcal{C} : variant is causal

$\bar{\mathcal{C}}$: variant is not causal

- Our **data**

- Carrier statuses g
- Affection statuses a



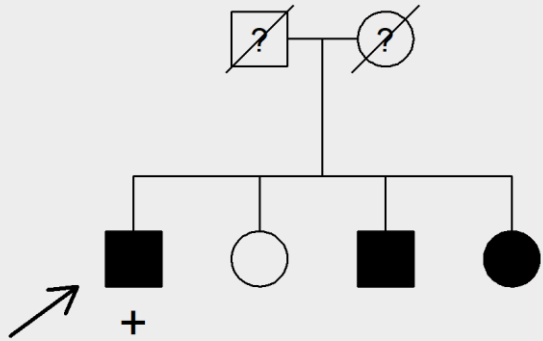
Fixed parameters

- Pedigree
- Allele freqs
- Disease model
- +++

The Bayes factor approach (2)

a = affection status vector
 g = genotype vector
 g_0 = proband genotype

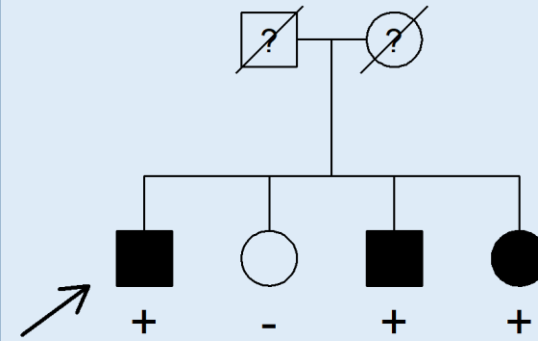
Original situation



$$\frac{P(\mathcal{C} \mid g_0, a)}{P(\bar{\mathcal{C}} \mid g_0, a)} = B_0 \cdot \frac{P(\mathcal{C})}{P(\bar{\mathcal{C}})}$$

$$\text{where } B_0 = \frac{P(g_0, a \mid \mathcal{C})}{P(g_0, a \mid \bar{\mathcal{C}})}$$

After additional genotyping



$$\frac{P(\mathcal{C} \mid g, a)}{P(\bar{\mathcal{C}} \mid g, a)} = B_1 \cdot \frac{P(\mathcal{C})}{P(\bar{\mathcal{C}})}$$

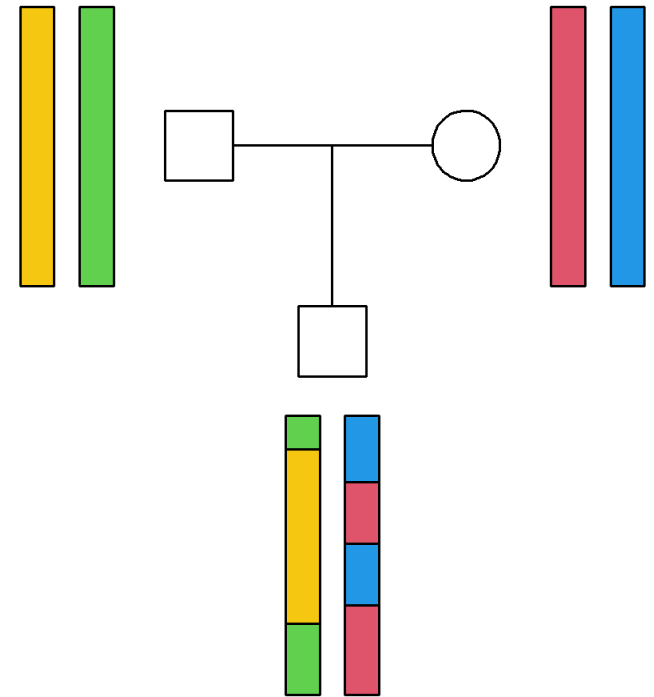
$$\text{where } B_1 = \frac{P(g, a \mid \mathcal{C})}{P(g, a \mid \bar{\mathcal{C}})}$$

Contribution of segregation analysis:

$$\frac{B_1}{B_0} = \frac{P(g, a \mid \mathcal{C})}{P(g, a \mid \bar{\mathcal{C}})} \bigg/ \frac{P(g_0, a \mid \mathcal{C})}{P(g_0, a \mid \bar{\mathcal{C}})}$$

Parametrization of models \mathcal{C} and $\bar{\mathcal{C}}$

- $\bar{\mathcal{C}}$ (variant independent of disease allele)
 - Unlinked $\rho = 0.5$
 - Linkage equilibrium $r = 0$
- \mathcal{C} (variant ~~is~~ ^{inseparable from} the disease allele)
 - Complete linkage $\rho = 0$
 - Complete LD $r = 1$

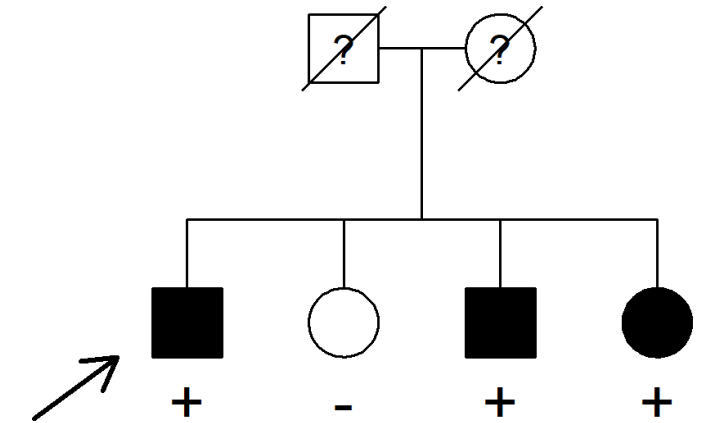


ρ = recombination rate
 r = linkage disequilibrium

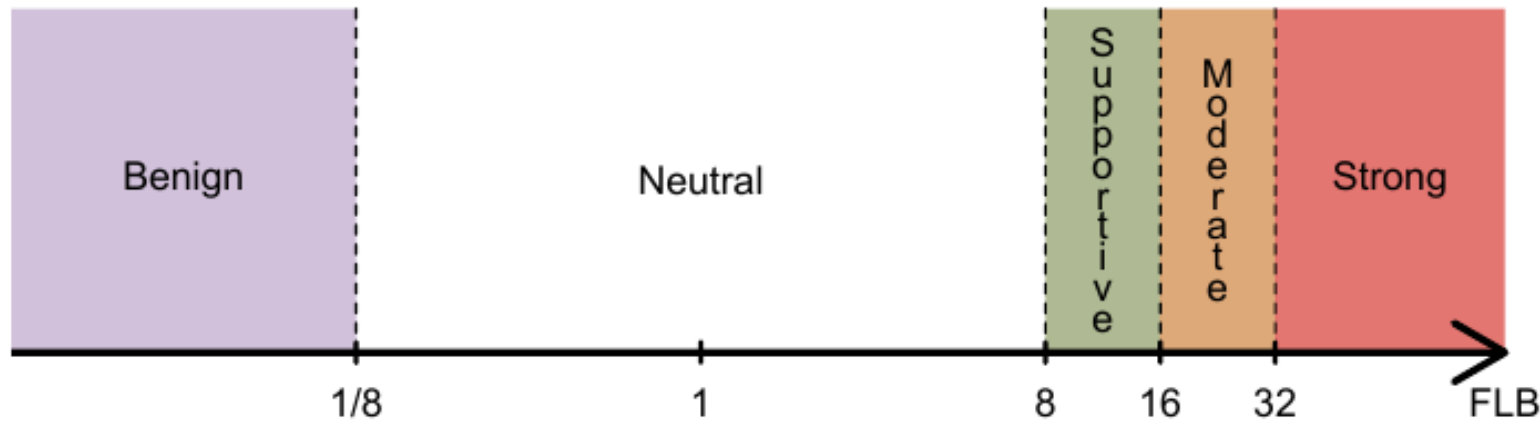
The full-likelihood Bayes factor (FLB)*

$$\text{FLB} = \frac{P(\mathbf{g}, \mathbf{a} \mid \rho = 0, r = 1)}{P(\mathbf{g}, \mathbf{a} \mid \rho = \frac{1}{2}, r = 0)} \bigg/ \frac{P(g_0, \mathbf{a} \mid \rho = 0, r = 1)}{P(g_0, \mathbf{a} \mid \rho = \frac{1}{2}, r = 0)}$$

- FLB = "LOD score adjusted for proband"
- FLB = 1/N (as given by J & B, under ideal conditions)



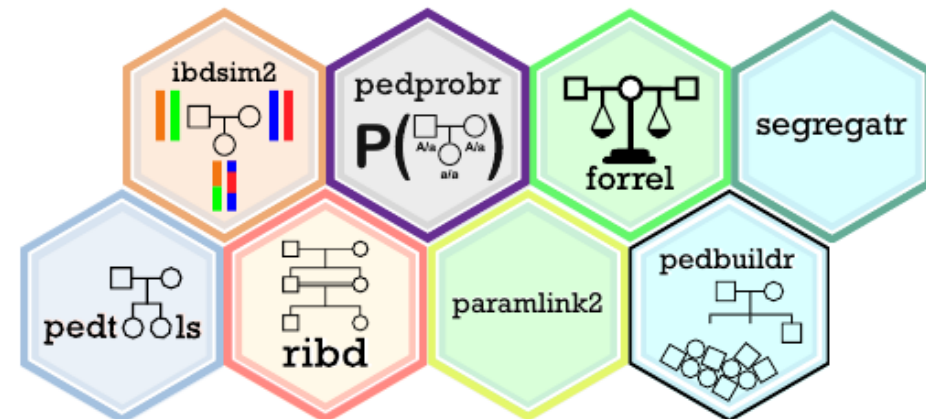
\mathbf{a} = affection status vector
 \mathbf{g} = genotype vector
 g_0 = proband genotype
 ρ = recombination rate
 r = linkage disequilibrium



Computing FLB

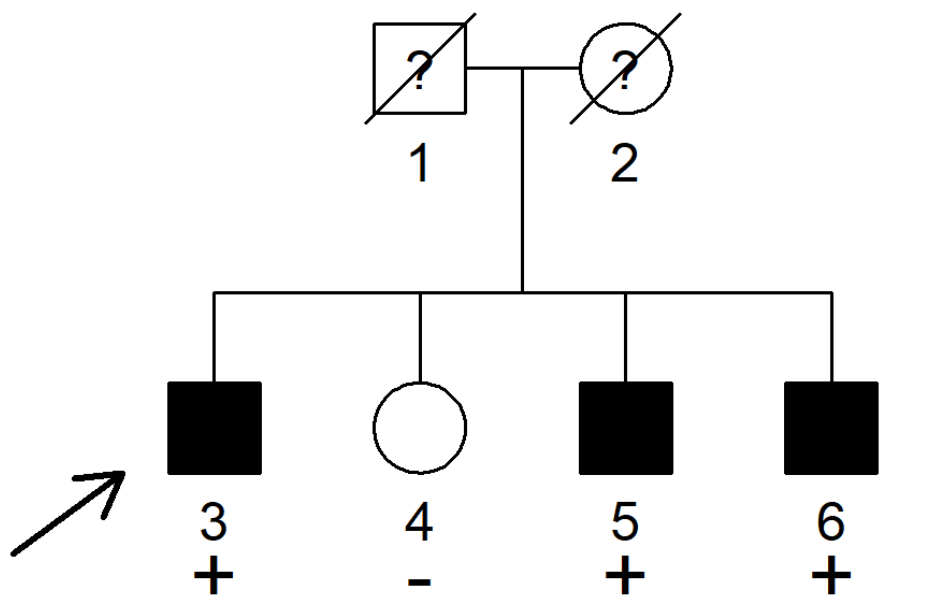
$$\text{FLB} = \frac{P(\mathbf{g}, \mathbf{a} \mid \rho = 0, r = 1)}{P(\mathbf{g}, \mathbf{a} \mid \rho = \frac{1}{2}, r = 0)} \bigg/ \frac{P(g_0, \mathbf{a} \mid \rho = 0, r = 1)}{P(g_0, \mathbf{a} \mid \rho = \frac{1}{2}, r = 0)}$$

- All terms are **pedigree likelihoods**: $P(\textit{genotypes} \mid \textit{pedigree}; \theta)$
- Implementations notoriously cumbersome
- Old software still prevailing (require bioinformatic training):
 - LINKAGE, FastLink, Allegro, GeneHunter (**Elston-Stewart algorithm**)
 - MERLIN (**Lander-Green algorithm**)
- R: pedsuite/segregatr



segregatr: Segregation analysis

segregatr



Not enough to qualify as
supportive evidence



```
➤ library(segregatr)
```

```
➤ x = nuclearPed(nch = 4, sex = c(1,2,1,1))
```

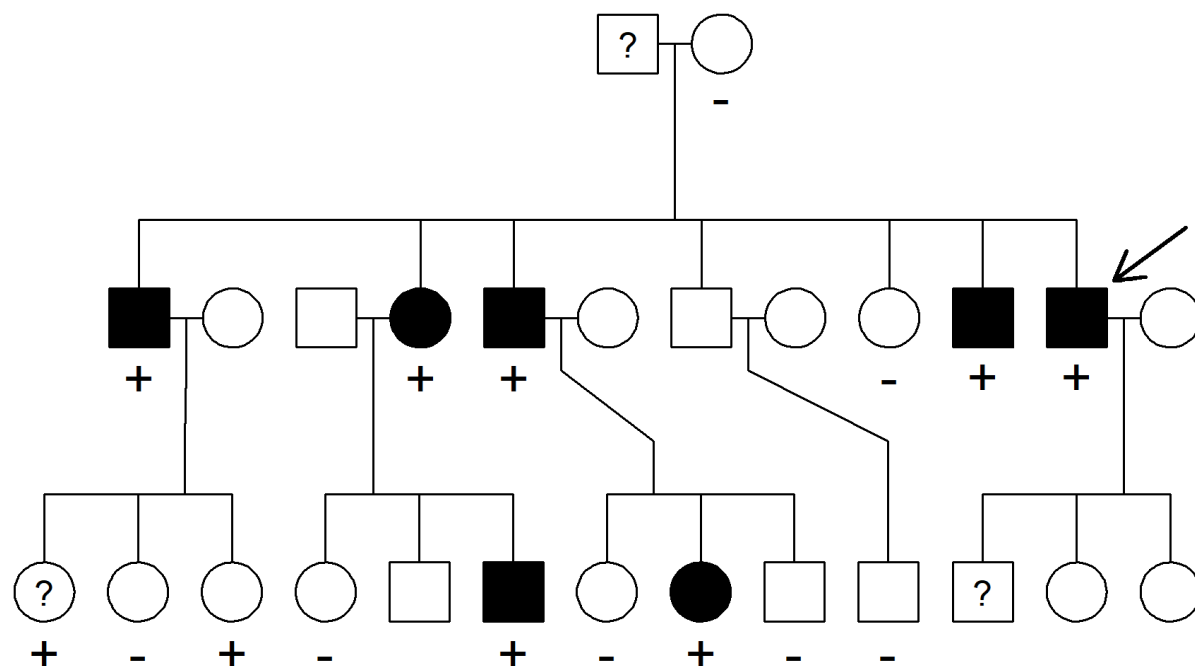
```
➤ FLB(x,  
      aff = c(3, 5, 6),  
      unknown = c(1, 2),  
      proband = 3,  
      carrier = c(3, 5, 6),  
      noncarrier = 4,  
      freq = 0.00001,  
      penetrances = c(0.01, 0.9, 0.9))
```

```
[1] 7.107237
```


segrepatr: Segregation analysis

segrepatr

Example from research

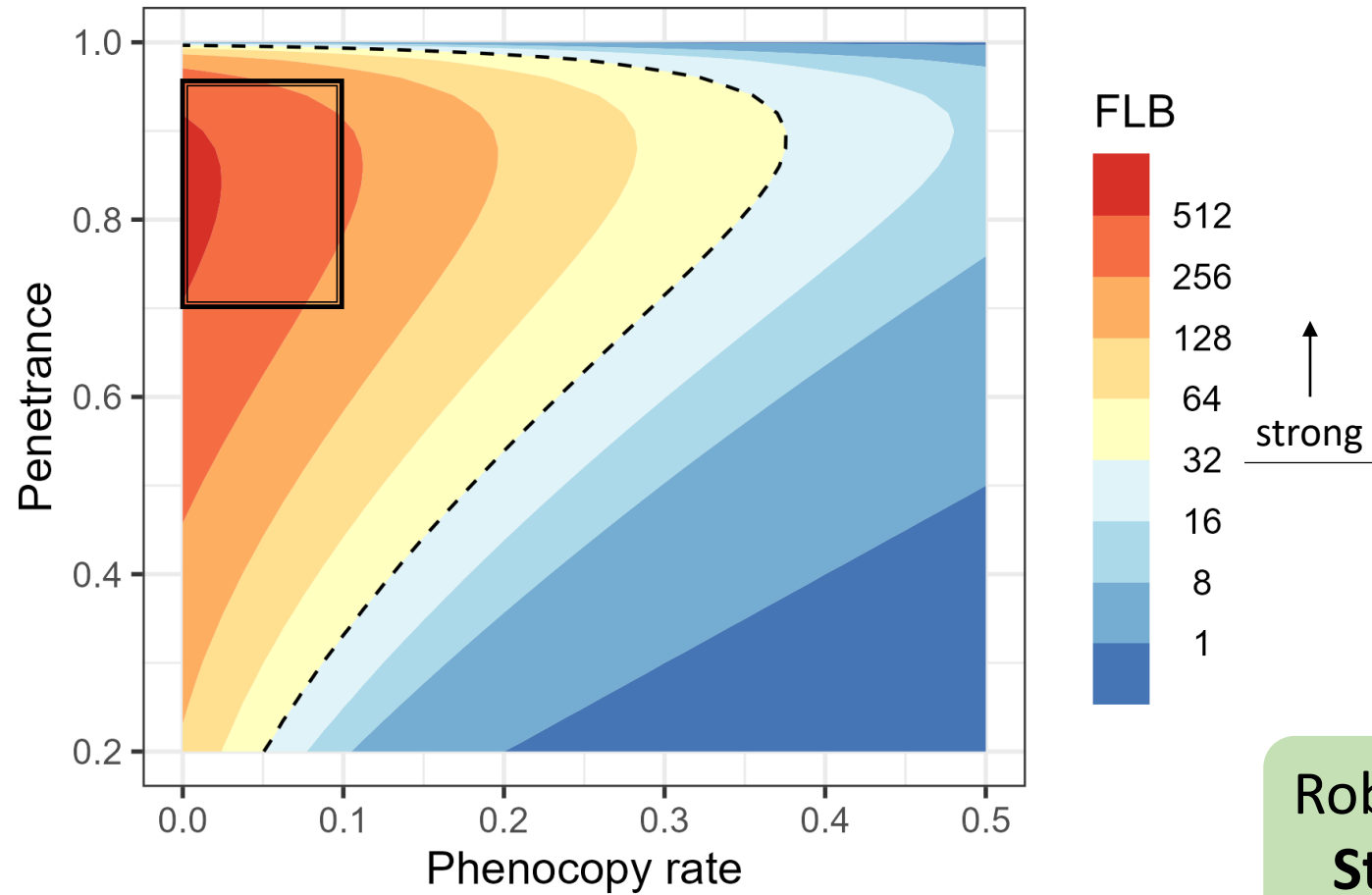


- Heritable thoracic aortic aneurysms with dissections (HTAAD)
- Potential cause: *SMAD3*:c.XXXG>A
- Classified as VUS
- Challenges:
 - Reduced penetrance
 - Phenocopies

Case report: *The use of segregation analysis in interpretation of sequence variants in SMAD3*

A Ratajska, MD Vigeland, KV Wirgenes, K Krohg-Sørensen, B Paus

Contours of FLB



Robust conclusion:
Strong evidence

Resulted in genetic diagnosis

Now try the exercises!