



Image Analysis

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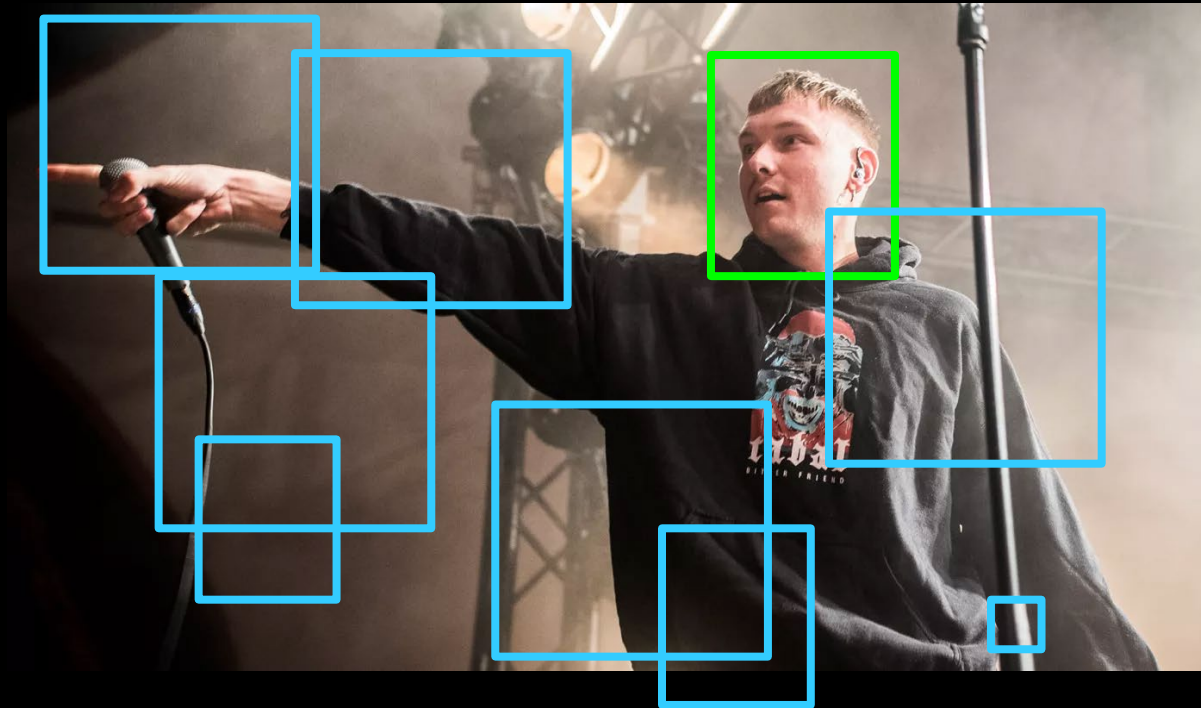
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Lecture 11 – Face detection using the Viola Jones method

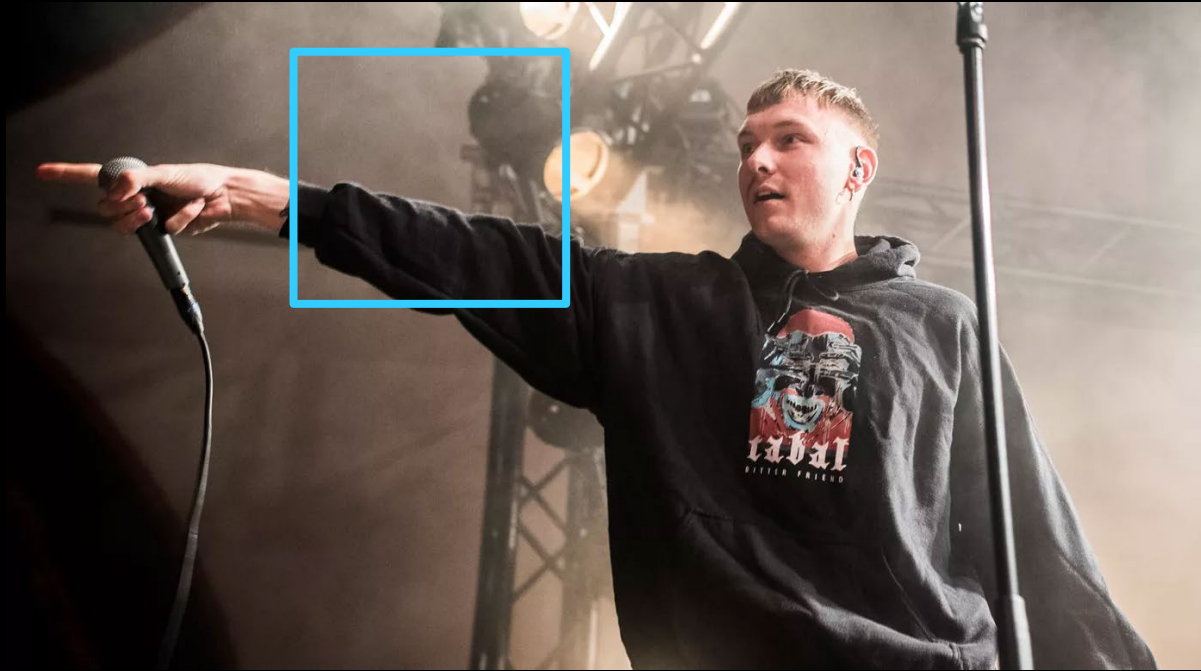




What can you do after today?

- Describe the concept of face detection
- Describe the concept of Haar features
- Compute the values of 2, 3 and 4 rectangle Haar features
- Describe the integral image
- Compute the sum of pixels values in a rectangle using an integral image
- Describe the concept of a weak classifier
- Describe how several weak classifiers can be combined into a strong classifier
- Describe the attentional cascade
- Describe how faces can be detected using a moving window

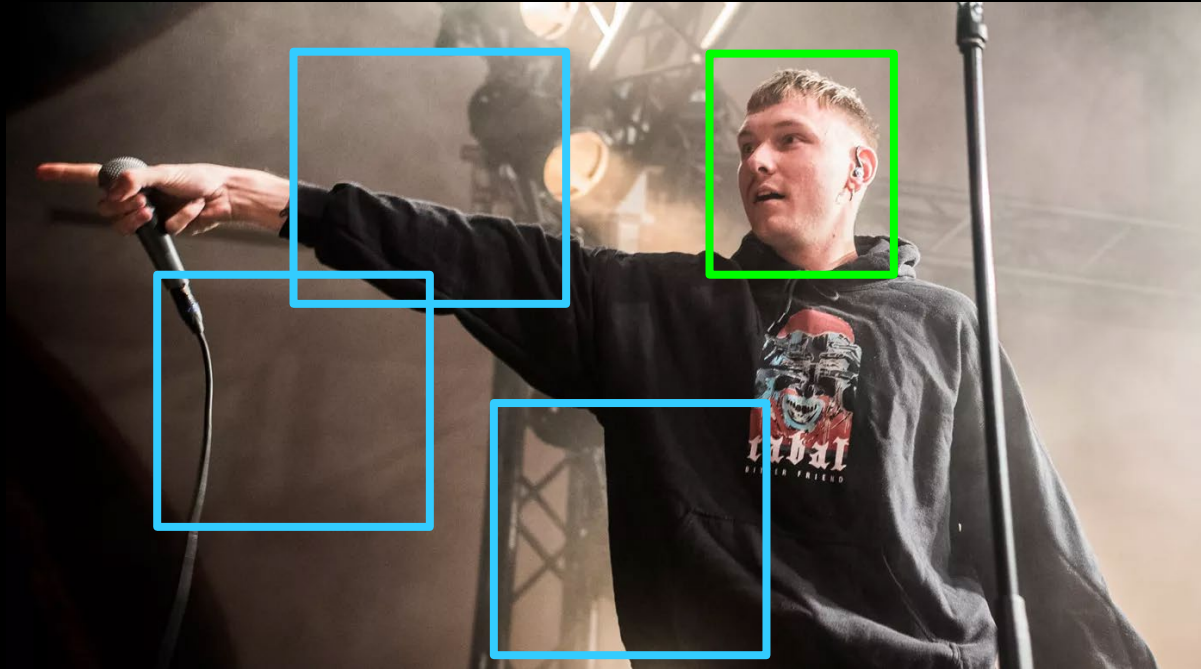
Face detection



■ First problem

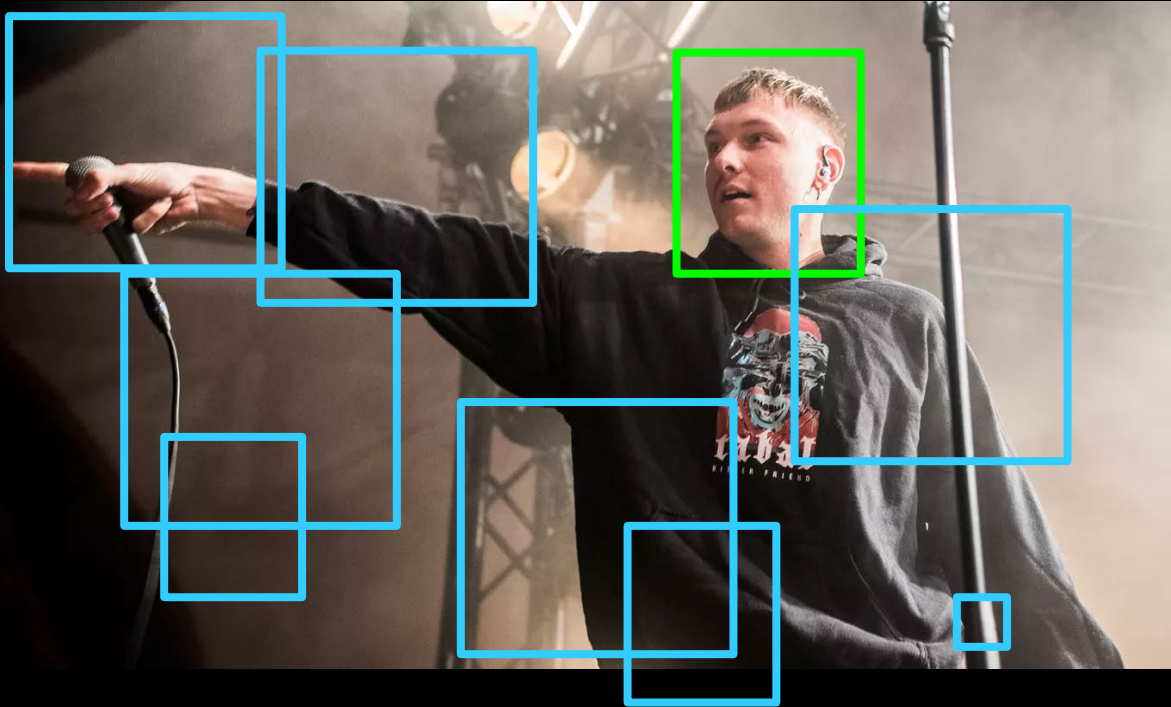
- Analyze a **window** in an image
- Is there a face in that window?

Face detection



- Slightly more advanced
 - Analyze many **windows** in an image
 - How many (if any) **windows** contain faces?

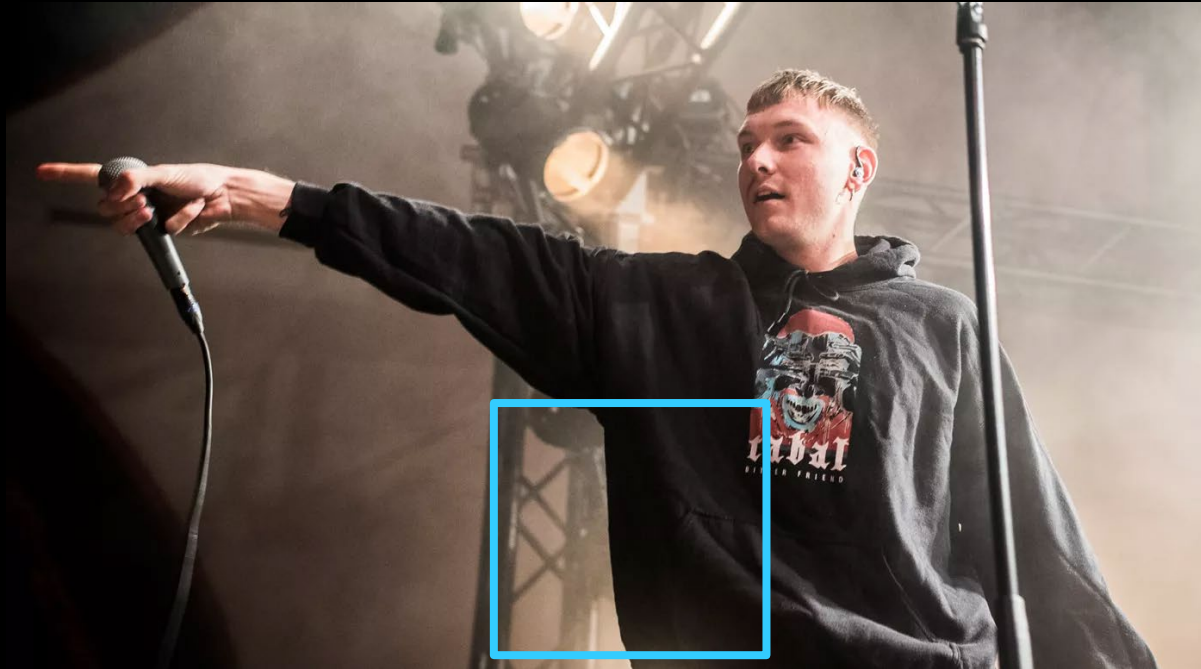
Face detection



■ Ideal

- Analyze (almost) all possible **windows** in an image
- How many (if any) **windows** contain faces?

What is needed?



- A fast method to determine if a *window* contains a face

Primary task – image feature based classification

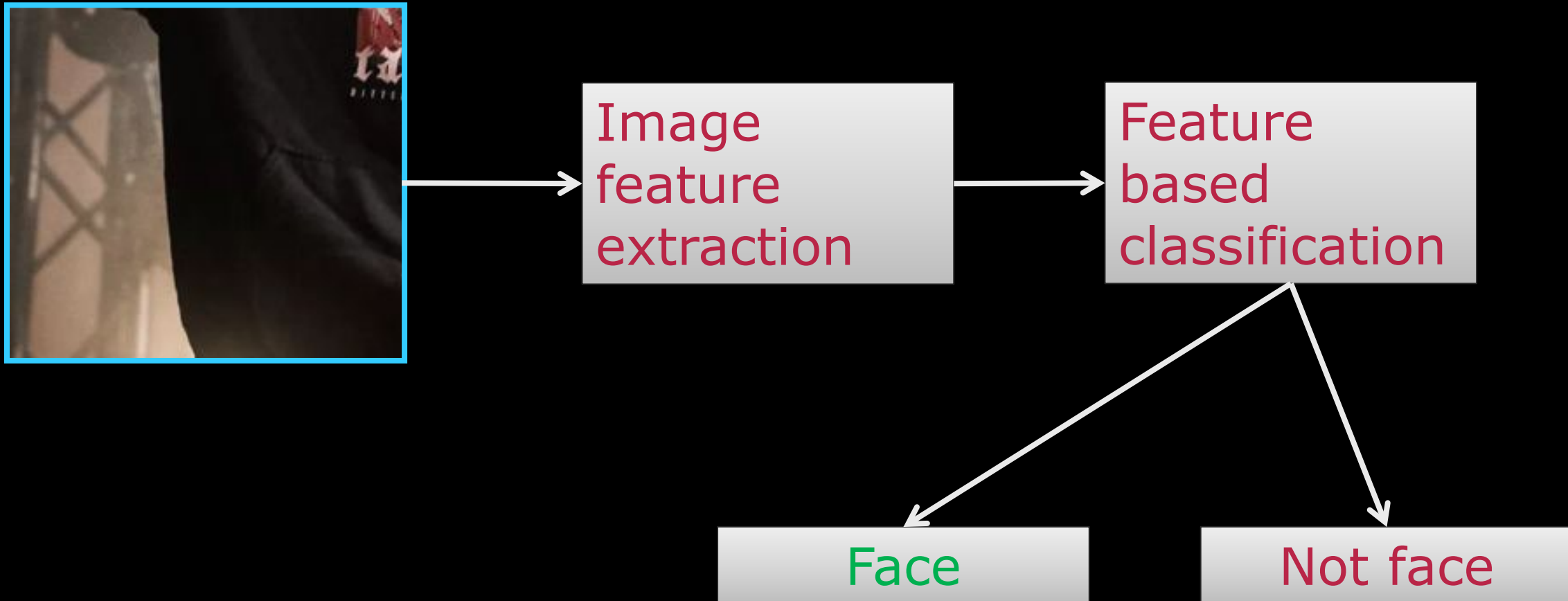
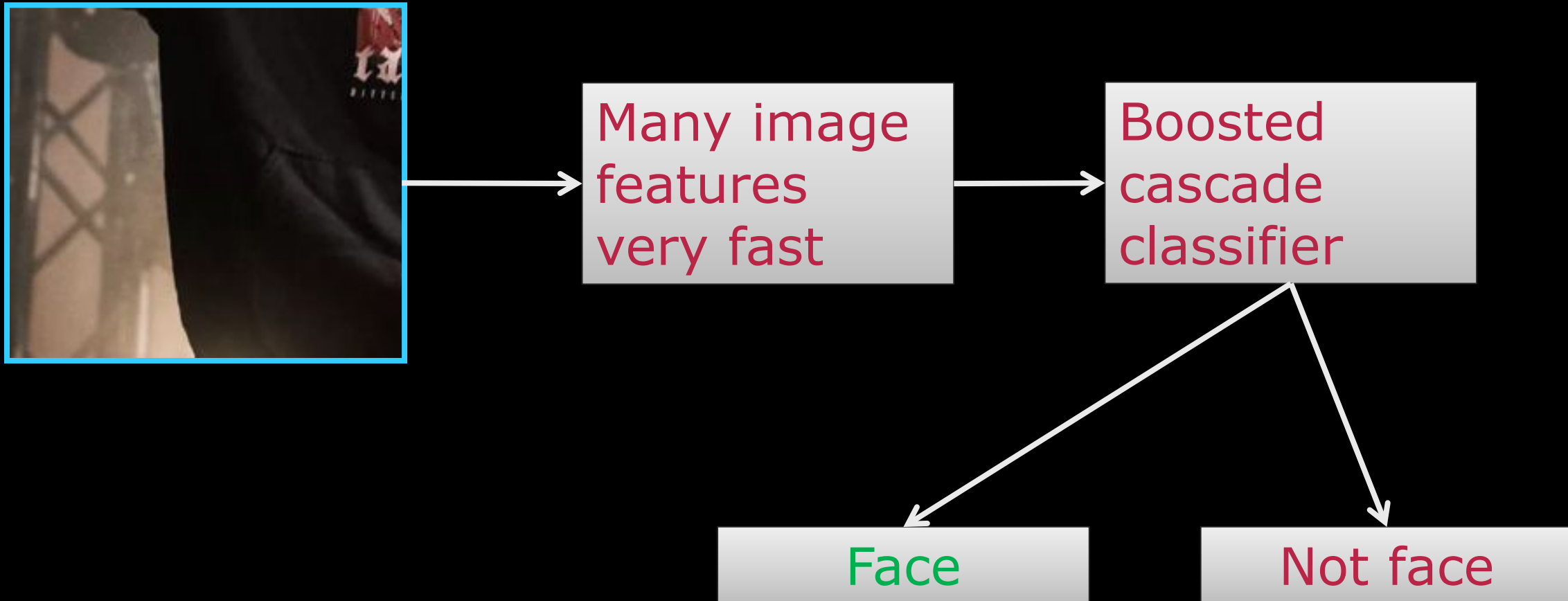


Image based features - what features can you think of?



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Viola Jones – fast features and smart classification



Training data



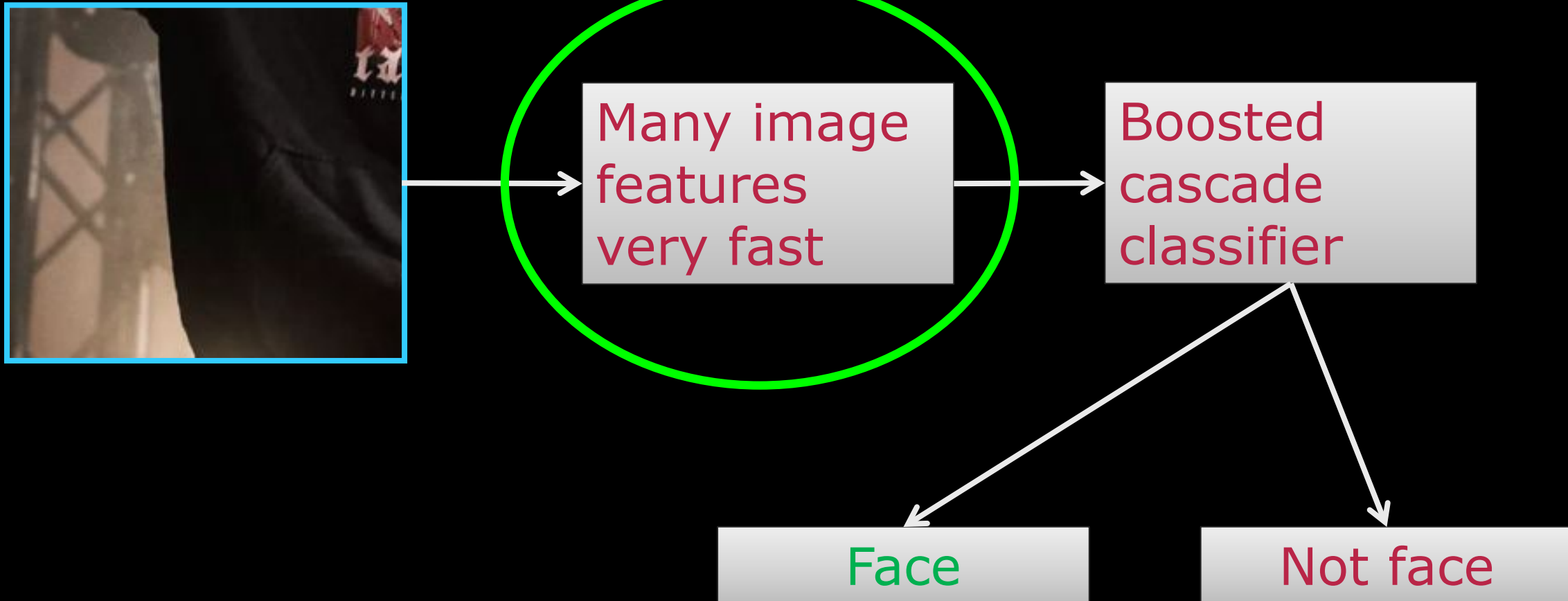
■ Face images:

- 4916 hand labelled faces
- Aligned and scaled to 24x24 pixels

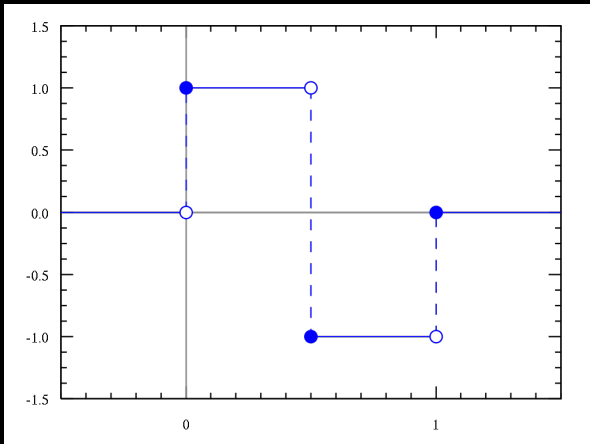
■ Non-face images:

- 9544 images with no faces
- 350 million sub-windows sampled from these

Viola Jones – fast features and smart classification



Haar features



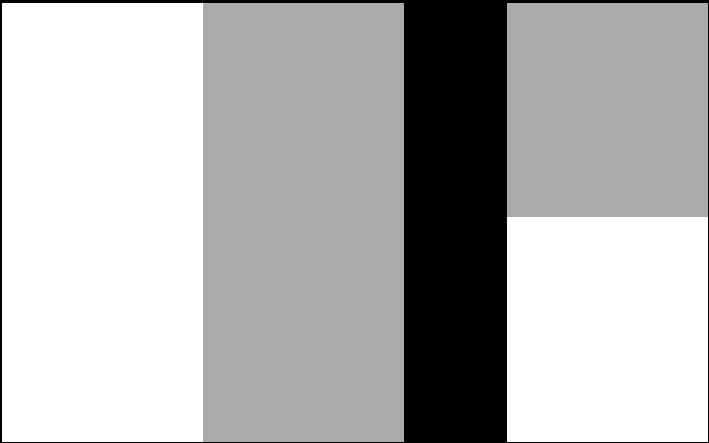
https://en.wikipedia.org/wiki/Haar_wavelet

- Alfred Haar (1885-1933)
 - Hungarian Mathematician
- Introduced the Haar wavelet in 1909
- *A wavelet is a wave-like oscillation with an amplitude that begins at zero, increases or decreases, and then returns to zero one or more times.*
- Simplest possible wavelet

<https://en.wikipedia.org/wiki/Wavelet>

Haar features

Two rectangle features



A

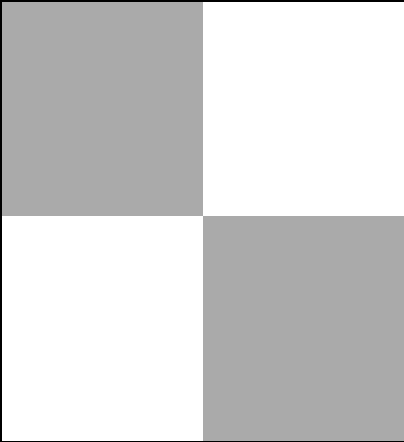
B

Three rectangle feature



C

Four rectangle feature



D

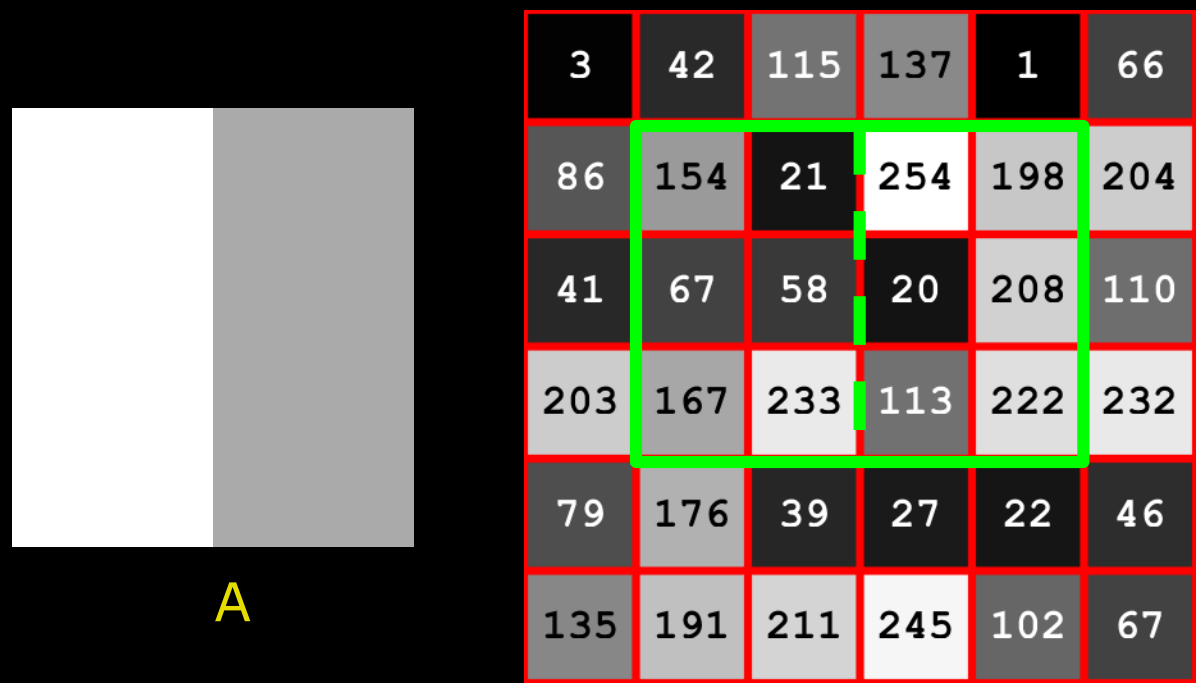
Feature =

Sum of
pixel
values
in image

-

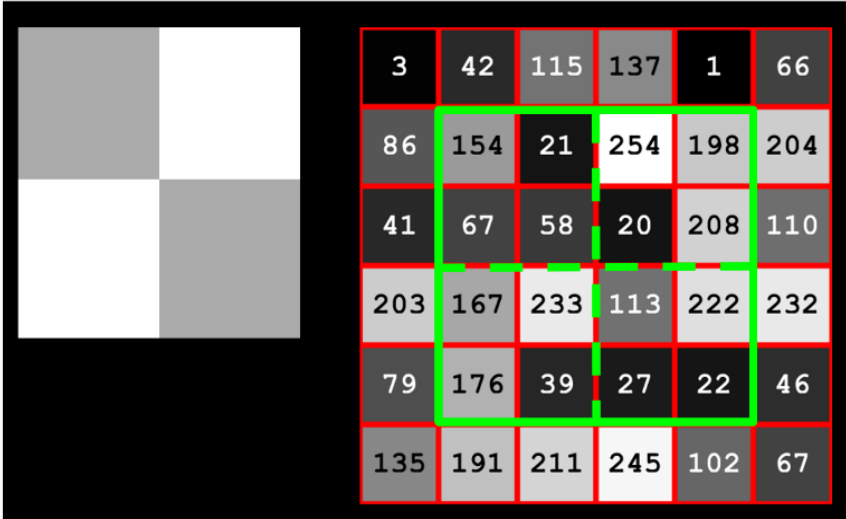
Sum of
pixel
values
in image

One Haar feature



Feature = 254+198+20+208+113+222-154-21-67-58-167-233 = 1015-700 = 315

Four rectangle Haar feature - what is the feature value?

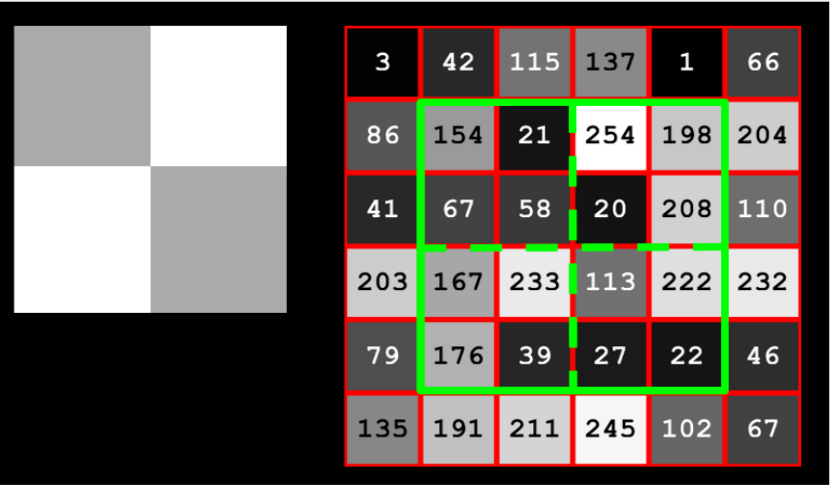


| | | | | | |
|-----|-----|-----|-----|-----|-----|
| 3 | 42 | 115 | 137 | 1 | 66 |
| 86 | 154 | 21 | 254 | 198 | 204 |
| 41 | 67 | 58 | 20 | 208 | 110 |
| 203 | 167 | 233 | 113 | 222 | 232 |
| 79 | 176 | 39 | 27 | 22 | 46 |
| 135 | 191 | 211 | 245 | 102 | 67 |

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Four rectangle Haar feature - what is the feature value?



567

179

-611

-113

76

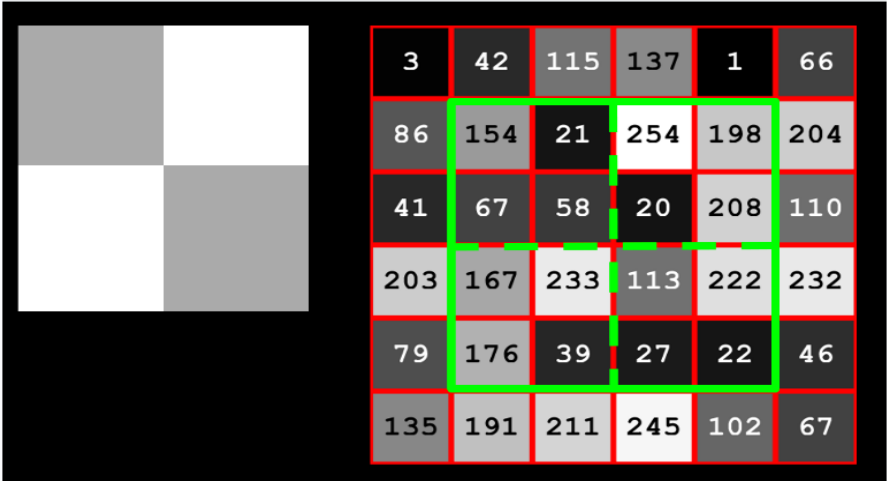
I do not know

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Four rectangle Haar feature - what is the feature value?



567

179

-611

✓ 0%

-113

76

I do not know

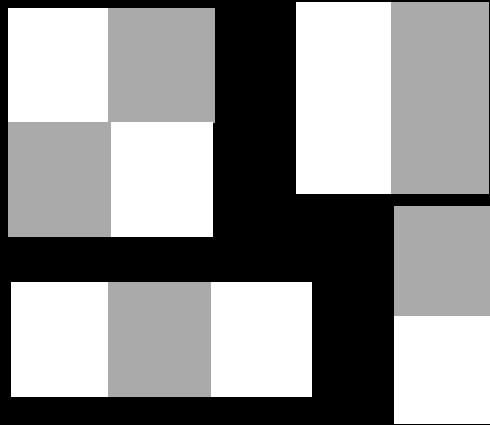
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Fast computing of Haar features

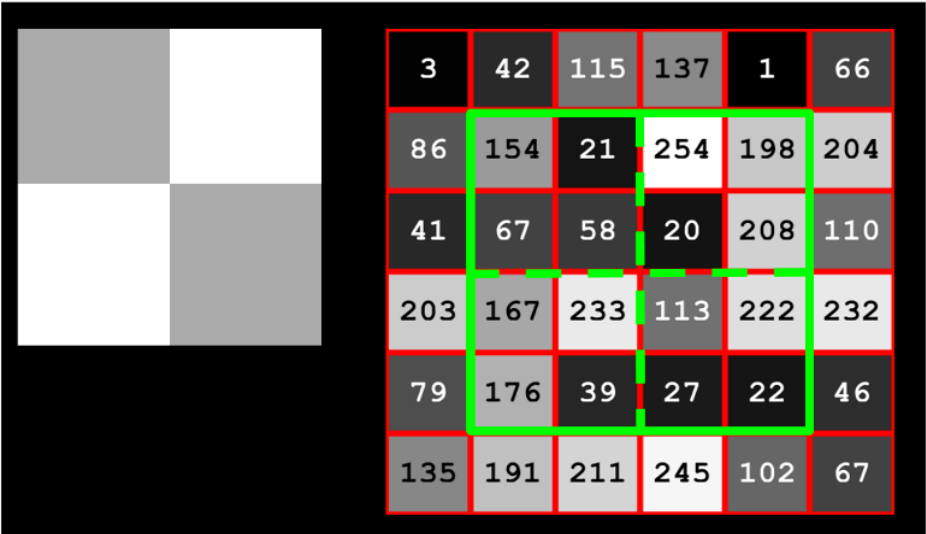


24 x 24 pixels



- Even for small Haar features, there are quite a lot of basic operations
- The larger the Haar feature, the more operations
- We need a fast way to compute Haar features

How many basic operations (plus and minus) are needed to compute the feature?



15

6

9

21

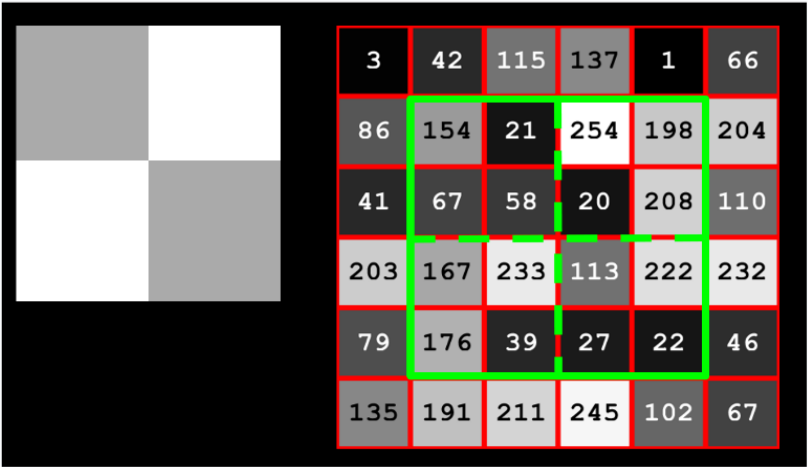
3

I do not know





How many basic operations (plus and minus) are needed to compute the feature?



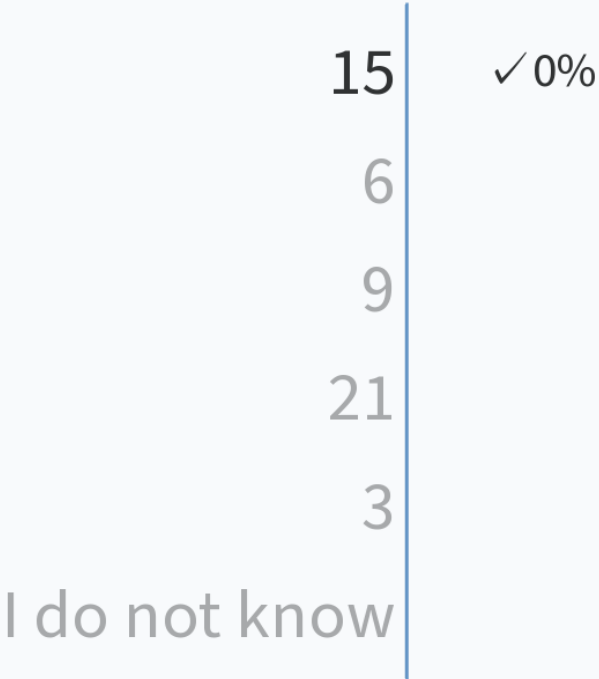
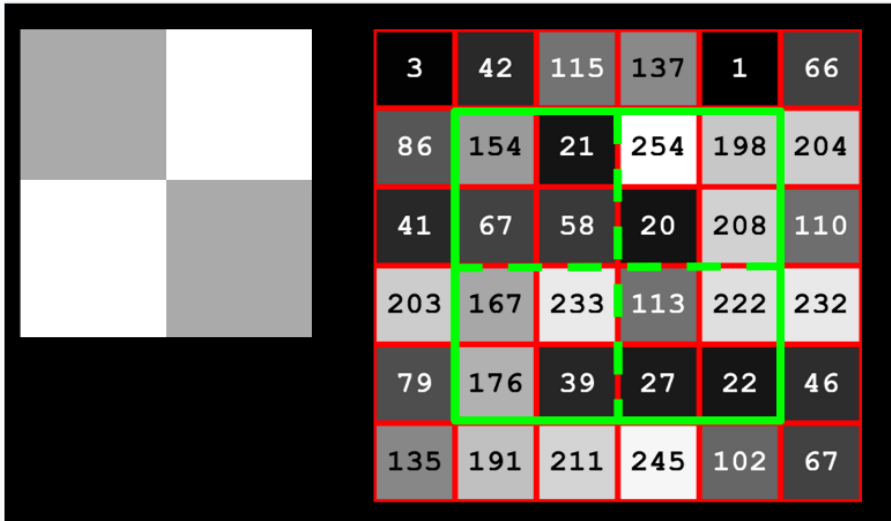
15
6
9
21
3

I do not know





How many basic operations (plus and minus) are needed to compute the feature?



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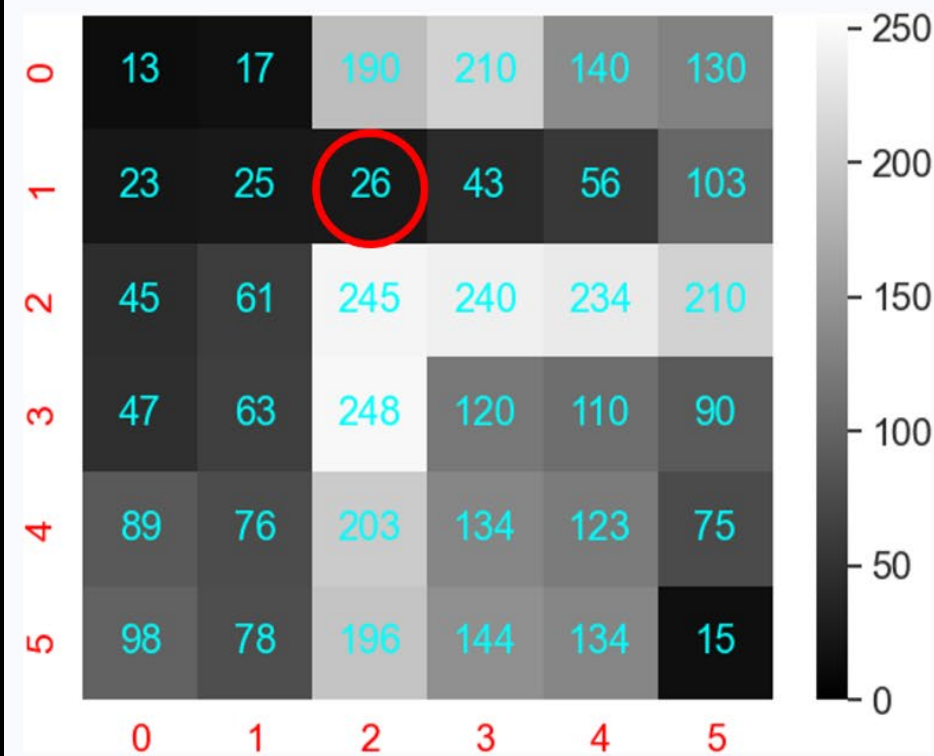


Fast computation of Haar features – the integral image



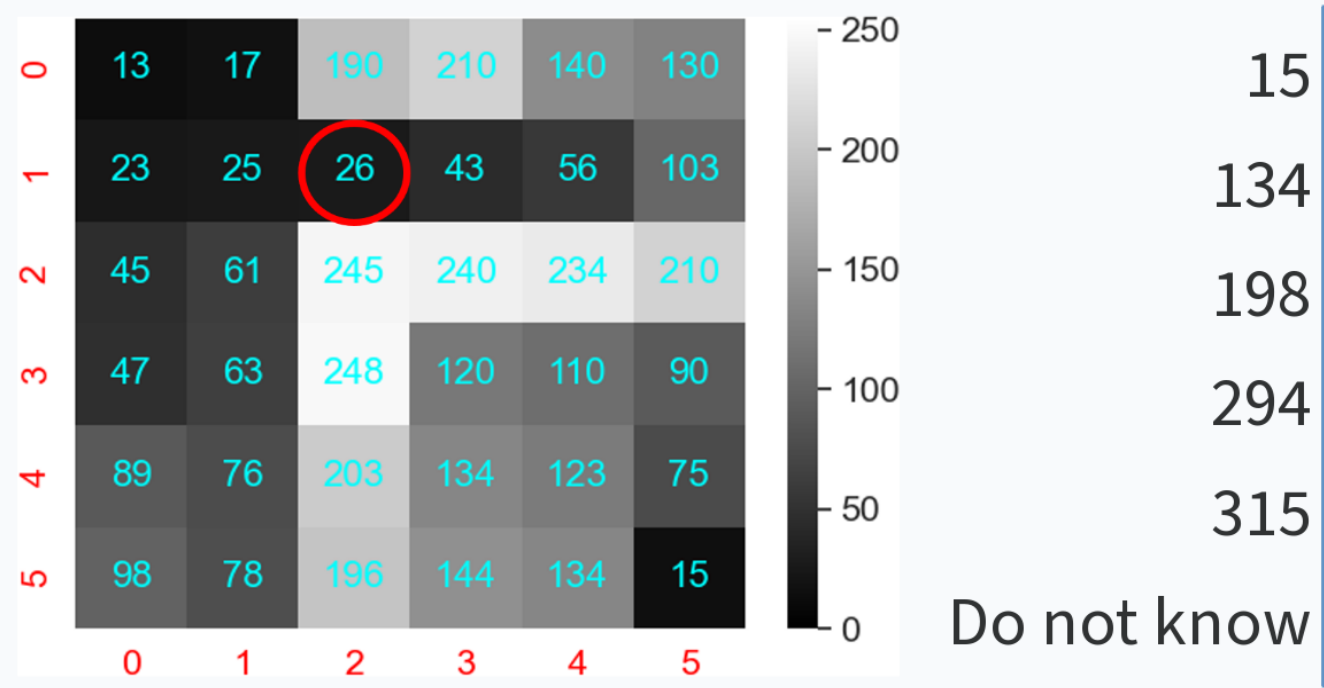
- In an integral image the pixel value is:
 - The sum of pixel above it and to the left of it in the original image
 - Including the pixel itself
- Can be computed very fast

Computing the integral image - what is the value in the marked pixel?



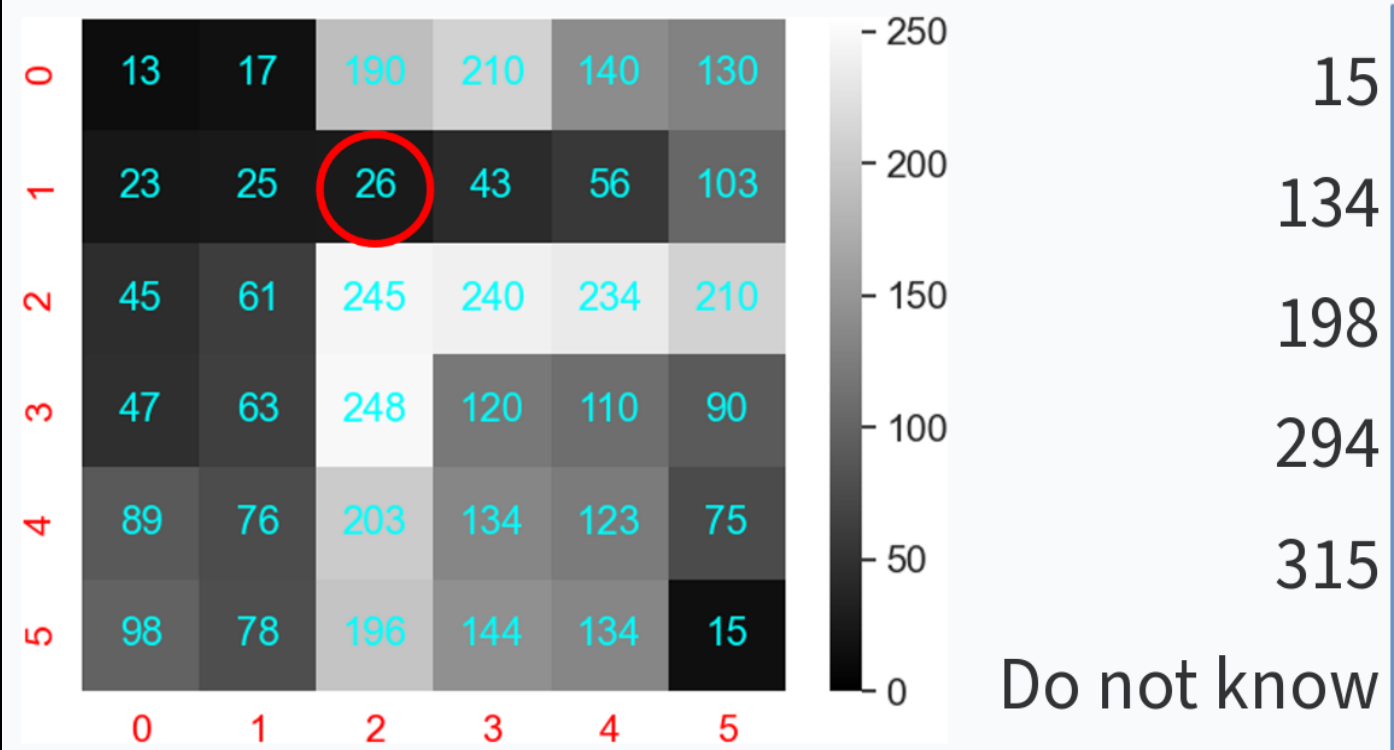
- 15
- 134
- 198
- 294
- 315
- Do not know

Computing the integral image - what is the value in the marked pixel?



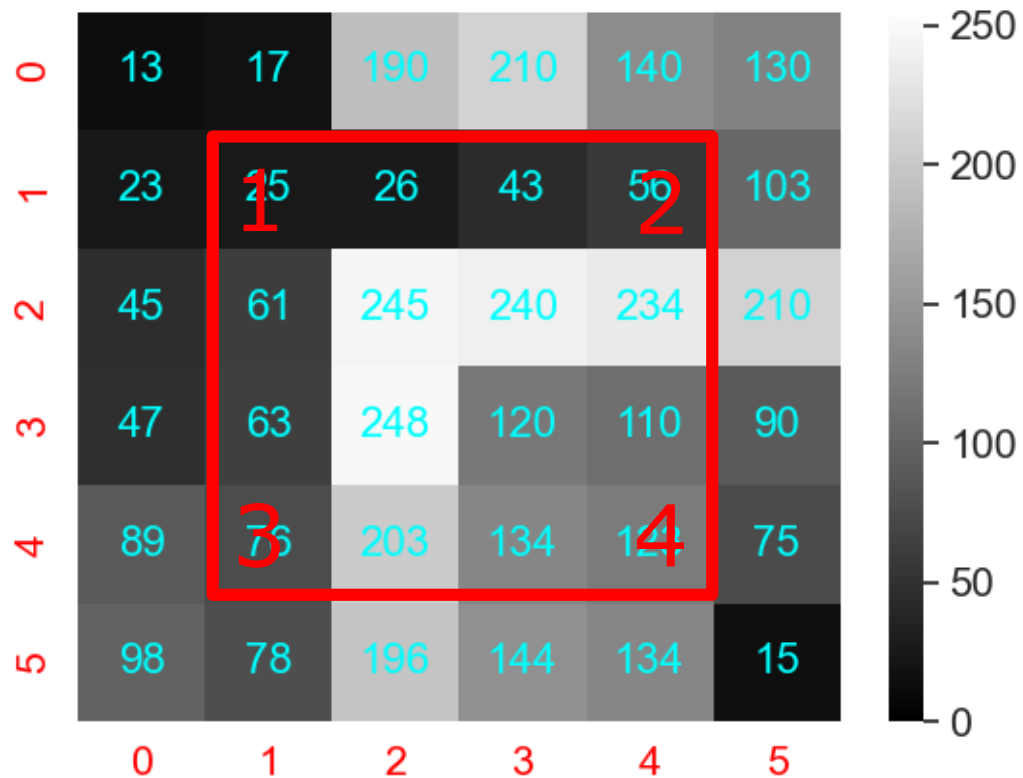
Start the presentation to see live content. For screen share software, share the entire screen. Get help at pollev.com/app

Computing the integral image - what is the value in the marked pixel?



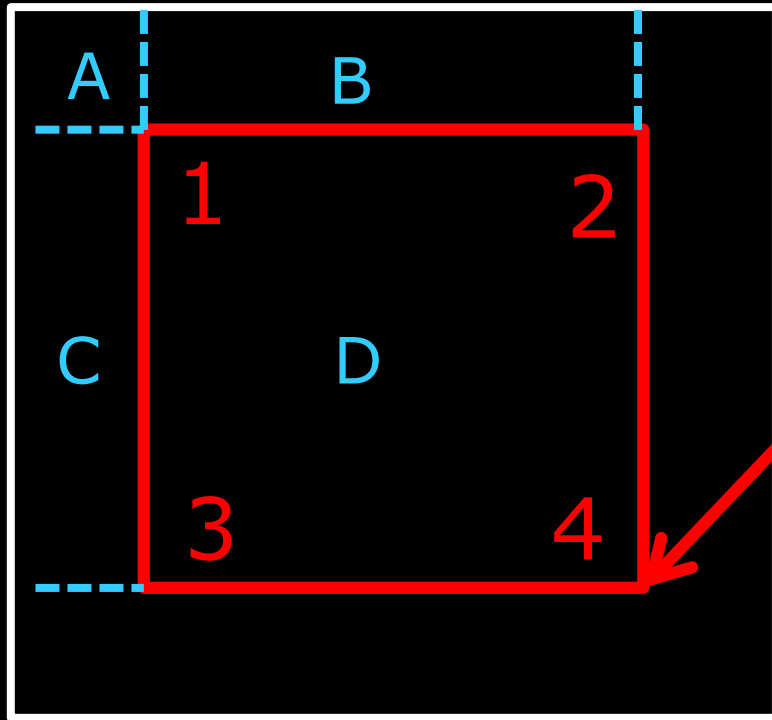
Start the presentation to see live content. For screen share software, share the entire screen. Get help at pollev.com/app

Using the integral image



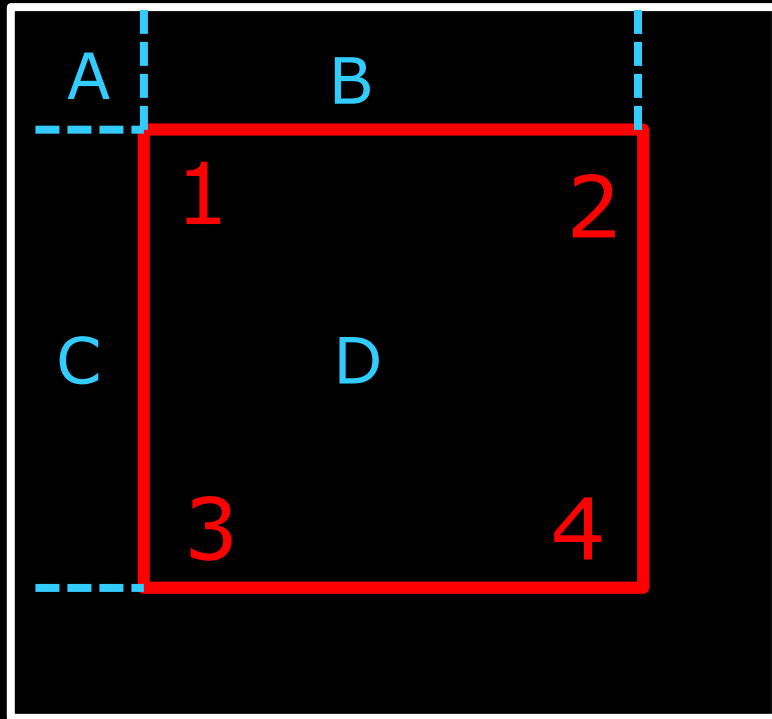
- We want to compute the pixel sum in the rectangle
- Defined by four corners: 1, 2, 3, 4

Using the integral image



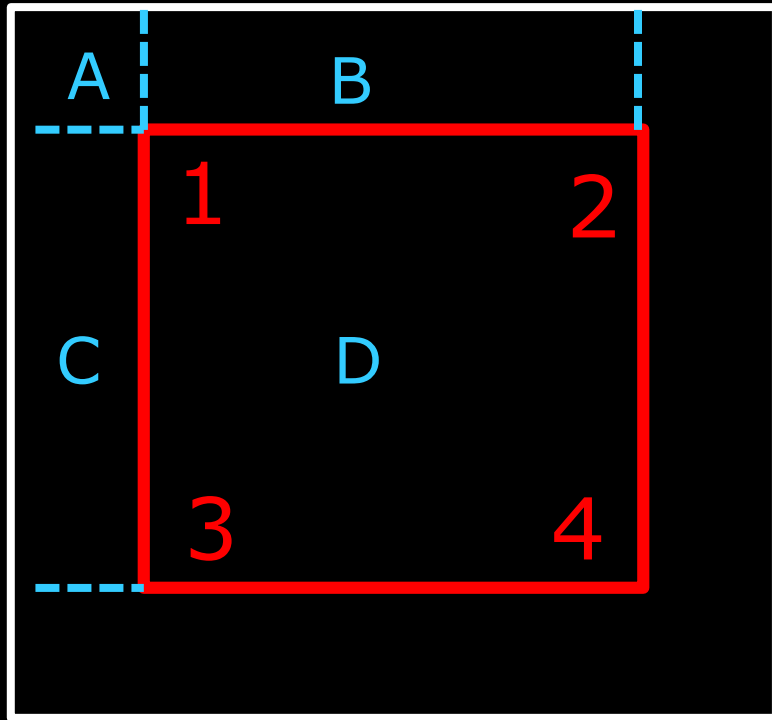
- Define four regions:
 - A, B, C, D
- The sum of pixels in the area
 - $A+B+C+D$ is the value of the integral image at point 4

Using the integral image



- The sum of pixels in the area
 - $A+B$ is the value of the integral image at point 2
 - $A+C$ is the value of the integral image at point 3

Using the integral image – short notation



■ The sum of pixels in the area

- $ii(2) = A+B$

- $ii(3) = A+C$

- $ii(4) = A+B+C+D$

- $ii(1) = A$

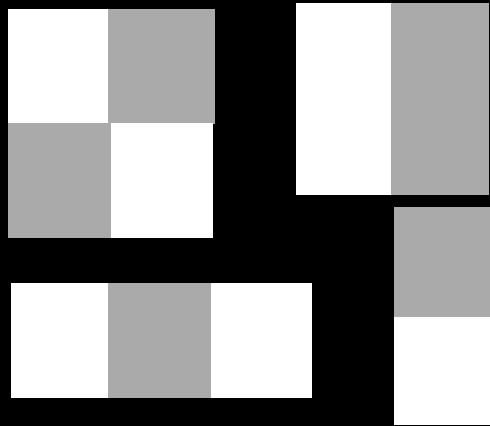
- $ii(4)-ii(3)-ii(2) = D - A$

■ $ii(4)-ii(3)-ii(2)+ii(1) = D$

Haar features in an image window



24 x 24 pixels



- Image window of 24 x 24 pixels
- All possible sizes and shapes of Haar features
- More than 180.000 features according to Viola and Jones
- They are *overcomplete* – meaning there is a very high redundancy
- We need *feature selection*

Possible features

$f_1 =$

$f_2 =$

$f_3 =$

$f_4 =$

$f_5 =$

$f_6 =$

$f_7 =$

$f_8 =$

...

$f_{180000} =$

Feature selection – from the article



- There are over 180,000 rectangle features associated with each image sub-window, a number far larger than the number of pixels.
- Even though each feature can be computed very efficiently, computing the complete set is prohibitively expensive.
- Our hypothesis, which is borne out by experiment, is that a very small number of these features can be combined to form an effective classifier.
- The main challenge is to find these features



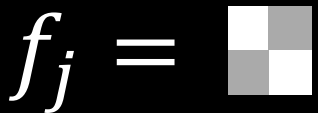
Learning Classification Functions

Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$



24 x 24 sub-window



Feature value computed on the sub-window

$$p_j \in [-1, 1]$$

Parity – determines if the feature value should be positive or negative

$$\theta_j$$

Feature threshold

Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$

$$x = \text{img} \quad f_j(\text{crop}) = \text{feature} = 2049$$

Learnt by training: $p_j = 1 \quad \theta_j = 456$

$$\rightarrow 1 * 2049 < 1 * 456 \rightarrow h_j(\text{crop}) = 0$$



What is this parity?

Weak classifier

$$h_j(x) = \begin{cases} 1 & \text{if } p_j f_j(x) < p_j \theta_j \\ 0 & \text{otherwise} \end{cases}$$

$$x = \text{img} \quad f_j(\text{crop}) = \text{feature} = 2049$$

Learnt by training: $p_j = -1$ $\theta_j = 456$

$$\rightarrow -1 * 2049 < -1 * 456 \rightarrow h_j(\text{crop}) = 1$$

Creating a strong classifier from weak classifiers

$$h(x) = \begin{cases} 1 & \sum_{t=1}^T \alpha_t h_t(x) \geq \frac{1}{2} \sum_{t=1}^T \alpha_t \\ 0 & \text{otherwise} \end{cases}$$

$$h_1(\text{img}) = \text{img}$$

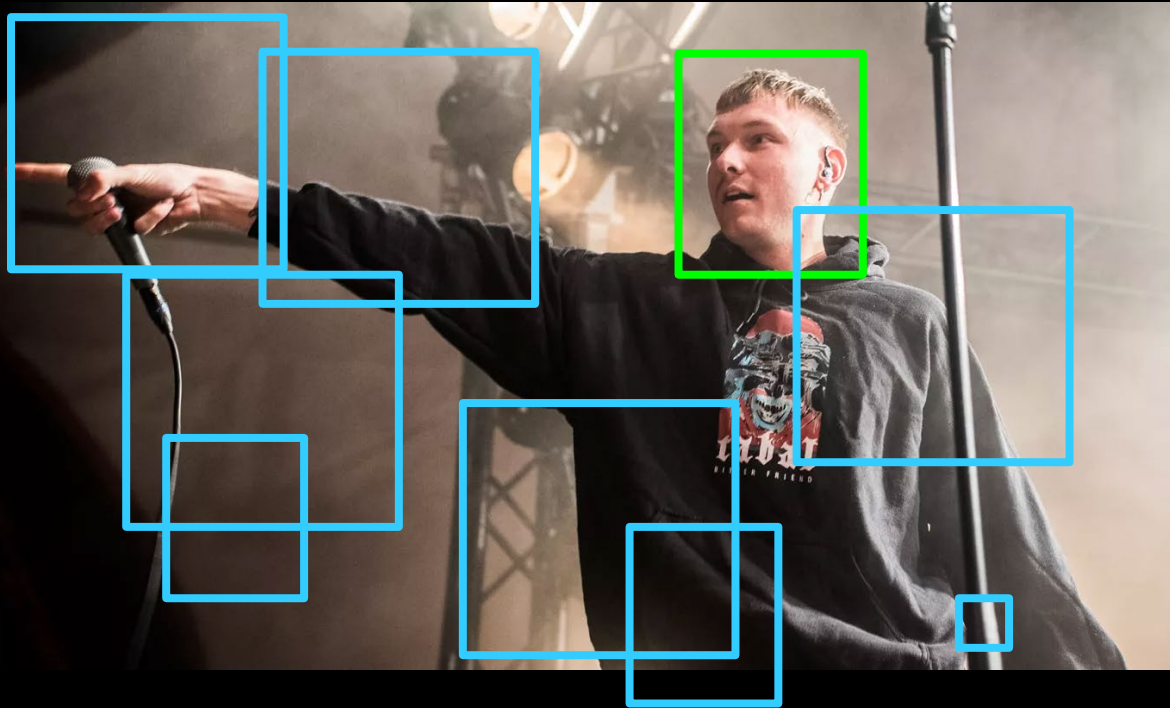
$$h_2(\text{img}) = \text{img}$$

...

$$h(\text{img}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost

Boosted features – good performance but not enough



- Frontal face classifier with
 - T=200 features
 - Detection rate 95%
 - False positives 1 in 14084
 - 0.7 seconds for a 384 x 288

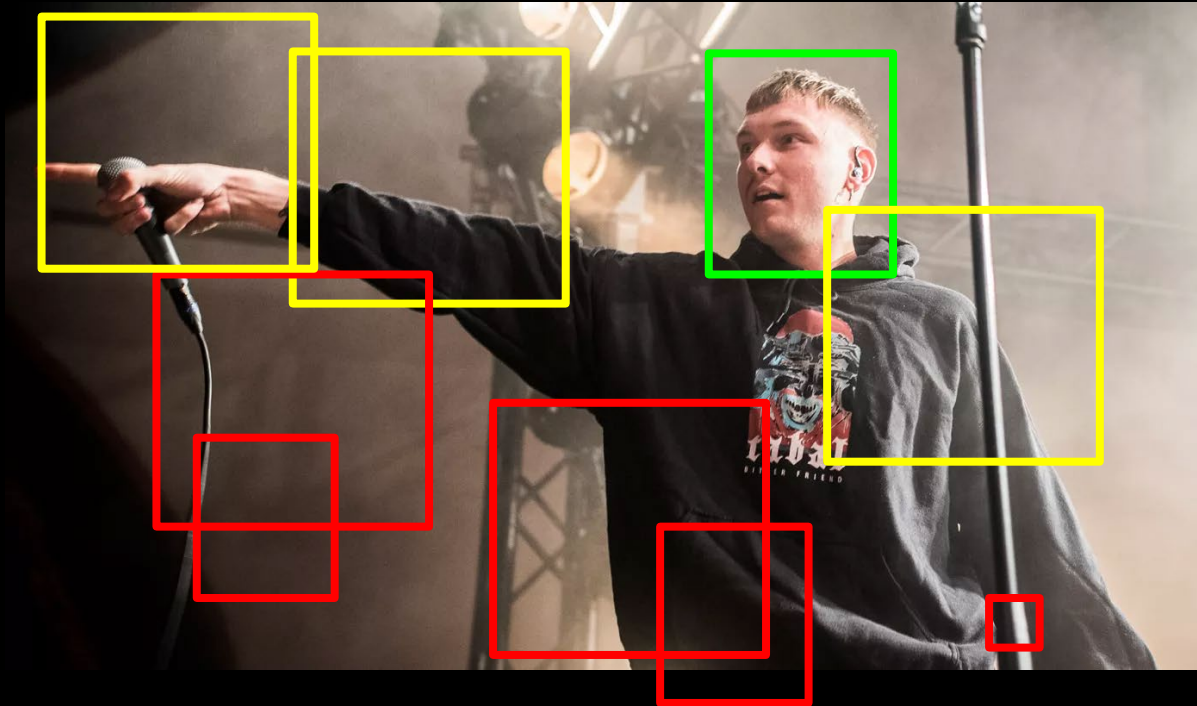
$$h_1(\text{image}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

The Attentional Cascade



Image Attention

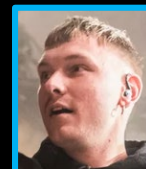
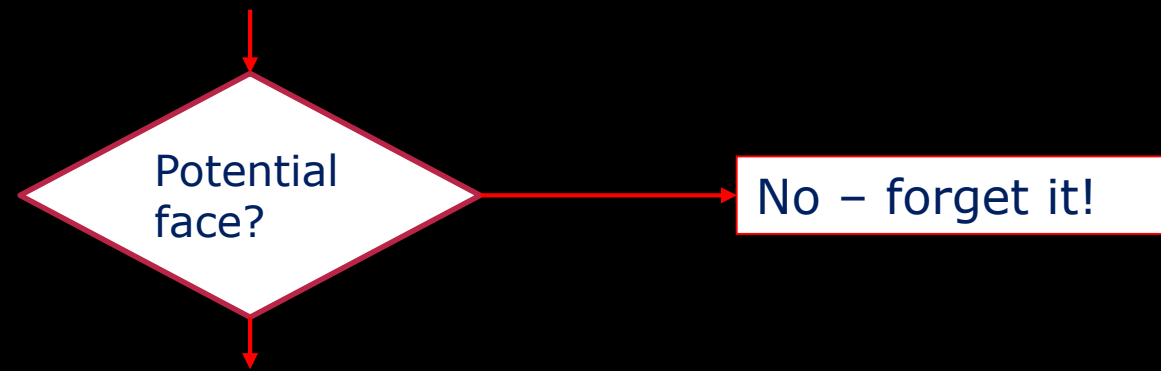
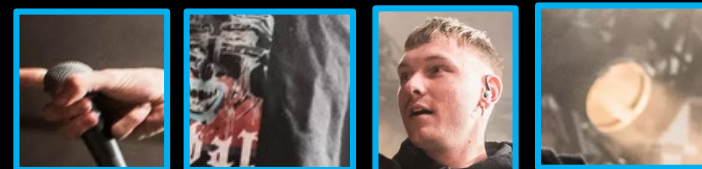
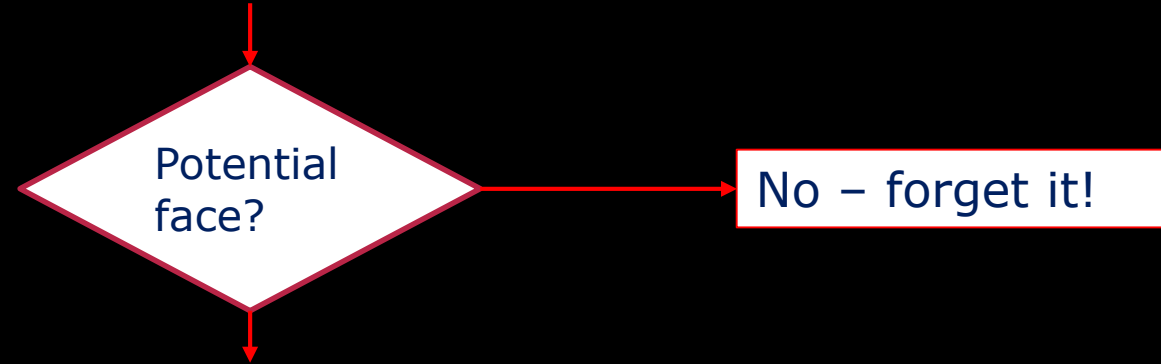
- The process of focusing on specific parts of an image
 - Followed by fine grained analysis of selected windows



Focusing on potential face regions



Cascaded classifier



Also called a *degenerate decision tree*

What is a false negative?

A face window classified as face window

A background window classified as a face window

A face window classified as a background window

A background window classified as a background window

I do not know

What is a false negative?

A face window classified as face window

A background window classified as a face window

A face window classified as a background window

A background window classified as a background window

I do not know

What is a false negative?

A face window classified as face window

A background window classified as a face window

A face window classified as a background window

A background window classified as a background window

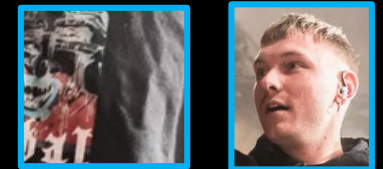
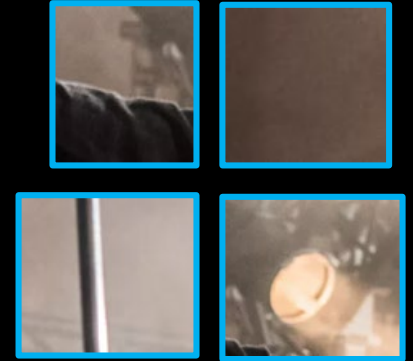
I do not know

✓ 0%

The attentional cascade



- Quickly reject negative sub-windows
 - Detect almost all positive sub-windows
 - False-negatives close to zero
 - Keep all potential face windows
 - Using the training set to find weights that fulfils this criterion
- Later more complex classifier
 - Low false positive rate



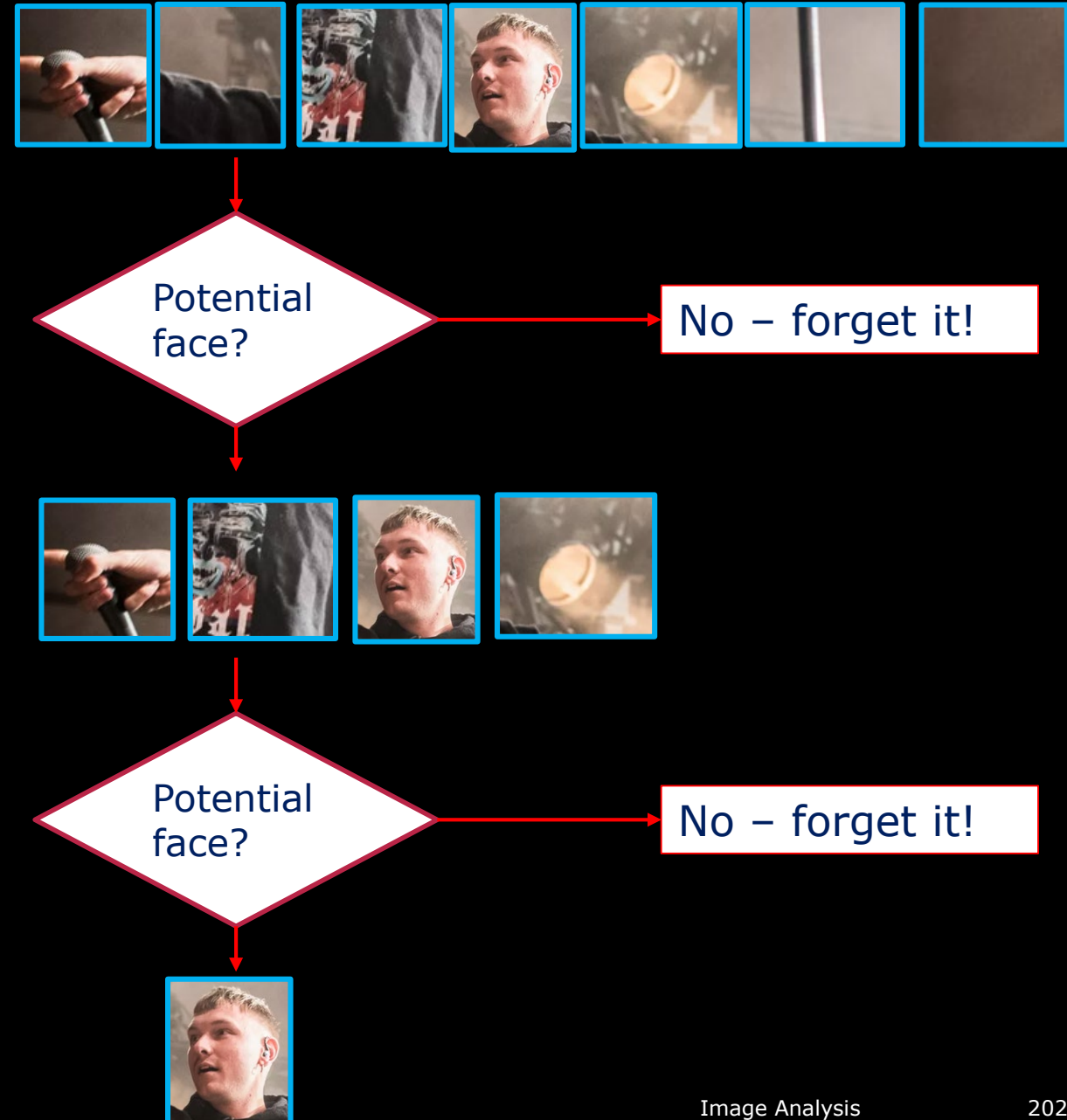
Training a cascade

$$h(\text{img}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost

$$h(\text{img}) = \alpha_1 h_1 + \alpha_2 h_2 + \dots + \alpha_T h_T$$

Learnt using AdaBoost



First stage classifier

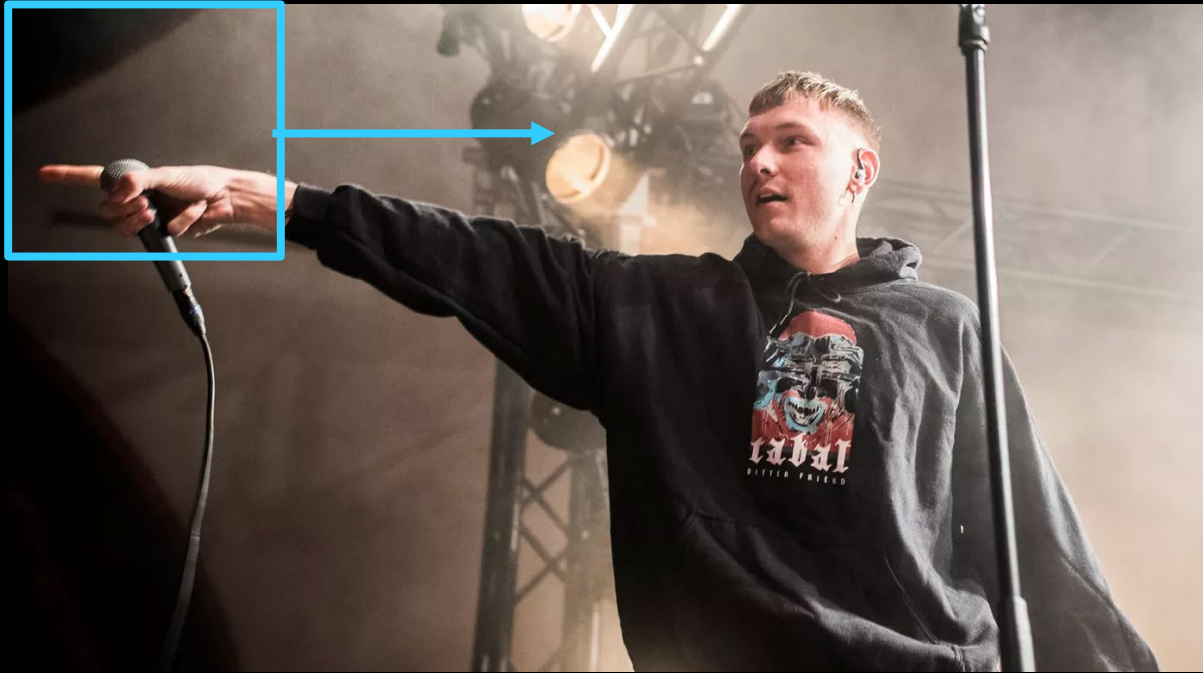


Final classifier



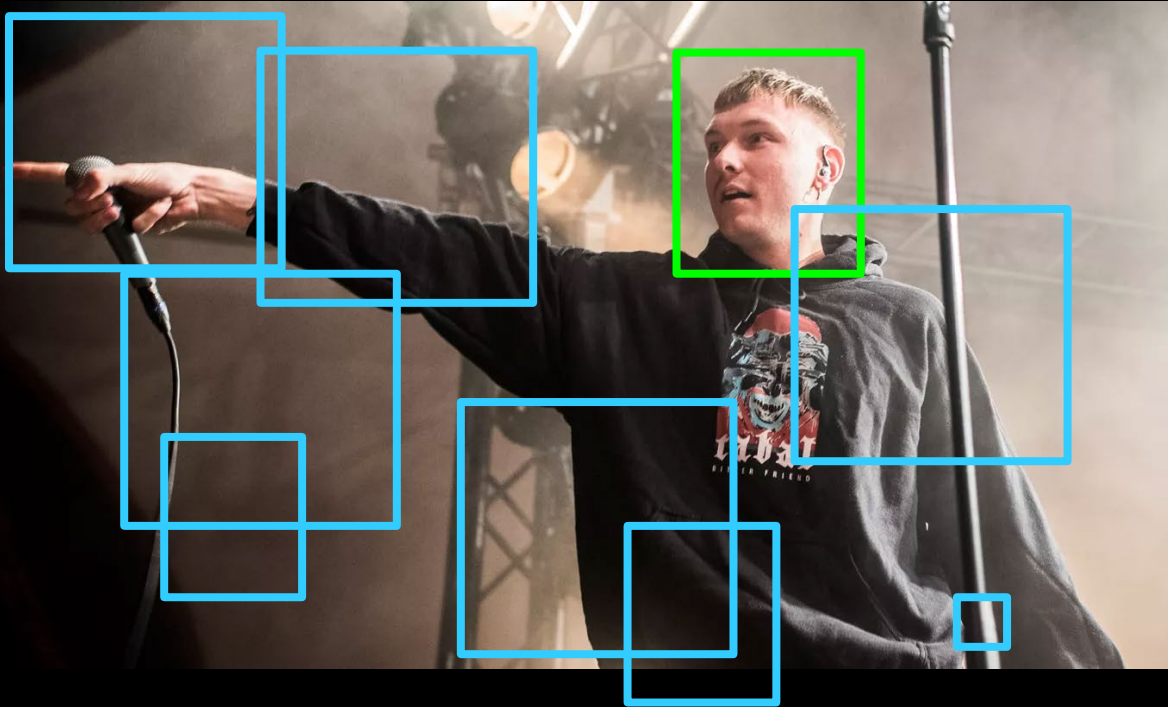
- 38 stages (step in the cascade)
- Total 6000 features (over the entire cascade)
- Faces are detected using on average 10 features per sub-window

Finding all faces in an image



- Slide a sub-window over the entire image
- Do a face detection for all positions
- Scale the features in a certain interval
 - To find faces of different sizes

Conclusion



- One of the most important algorithms before deep learning
- Uses many interesting concepts
 - Attention
 - Boosted weak classifiers
 - Very fast feature computation



Demo



Next week

- Statistical models of shape and appearance