

This supplementary numerical analysis aims to further illustrate the sensitivity of the proposed iterative algorithm with respect to the scalar parameters  $\beta$  and  $\delta$ . To this end, simulations were conducted for 12 logarithmically spaced values of  $\beta$  in the interval  $[1, 100]$  and 12 logarithmically spaced values of  $\delta$  in the interval  $[10^{-6}, 10^{-5}]$ , resulting in a total of 144 parameter combinations. For each simulation scenario, the algorithm was executed for all considered cases (Case I, Case II, and Case III) and for each admissible filter order  $n_f \in \{4, 3, 2, 1\}$ , using the same convergence tolerance  $\varepsilon = 1 \times 10^{-3}$  and maximum number of iterations  $\kappa_{\max} = 100$ . The results are reported in Table 1, where, for each configuration, the guaranteed cost ( $\gamma^*$ ) and the number of iterations ( $n_\kappa$ ) are summarized using the format “average±standard deviation” computed over the corresponding set of simulations. Although the number of iterations is an integer-valued quantity, its average and standard deviation are reported as real-valued statistics, rounded to one decimal place.

Table 1: Guaranteed cost ( $\gamma^*$ ) and number of iterations ( $n_\kappa$ ), reported as average (standard deviation), for different values of  $\beta$  and  $\delta$ , considering filters orders  $n_f \in \{4, 3, 2, 1\}$  and Cases I–III.

Filter Order	Case I		Case II		Case III	
	$\gamma^*$	$n_\kappa$	$\gamma^*$	$n_\kappa$	$\gamma^*$	$n_\kappa$
$n_f = 4$	7.2379 (0.0380)	4.7 (1.9)	7.2289 (0.0407)	3.7 (3.2)	7.1652 (0.0000)	1.0 (0.0)
$n_f = 3$	7.2253 (0.0002)	12.3 (1.1)	7.2269 (0.0374)	5.2 (4.0)	7.1652 (0.0000)	1.0 (0.0)
$n_f = 2$	7.2658 (0.0001)	2.3 (0.5)	7.2628 (0.0319)	3.6 (1.9)	7.1668 (0.0075)	1.3 (2.1)
$n_f = 1$	7.8071 (0.0000)	4.0 (0.0)	7.7203 (0.0000)	4.0 (0.0)	7.2673 (0.0000)	6.9 (0.2)

This results clarify the role of  $\beta$  and  $\delta$  in the initialization step and their effect on the convergence behavior of Algorithm 1. The tests with different values of  $\beta$  and  $\delta$  indicate that these parameters mainly influence the convergence speed: the number of iterations exhibits only moderate variability, while the final guaranteed cost shows very limited dispersion across all tested cases. This confirms that variations in  $\beta$  and  $\delta$  affect convergence speed rather than the achieved performance level.