

# Towards deep phase recovery for audio source separation

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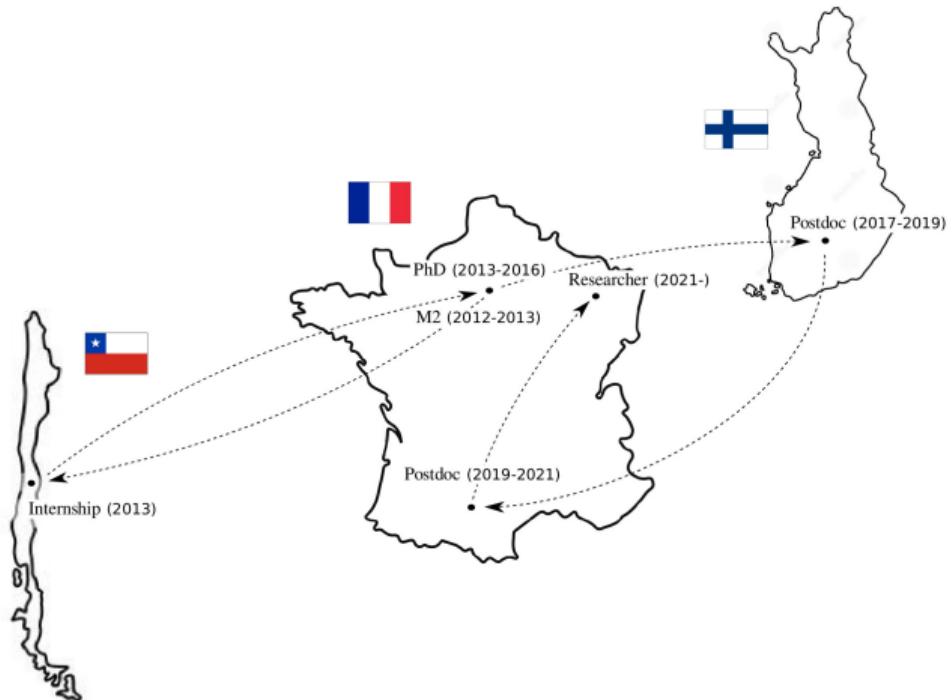
Seminar at Audio Research Group, Tampere University, Finland  
August 30, 2023

Paul Magron

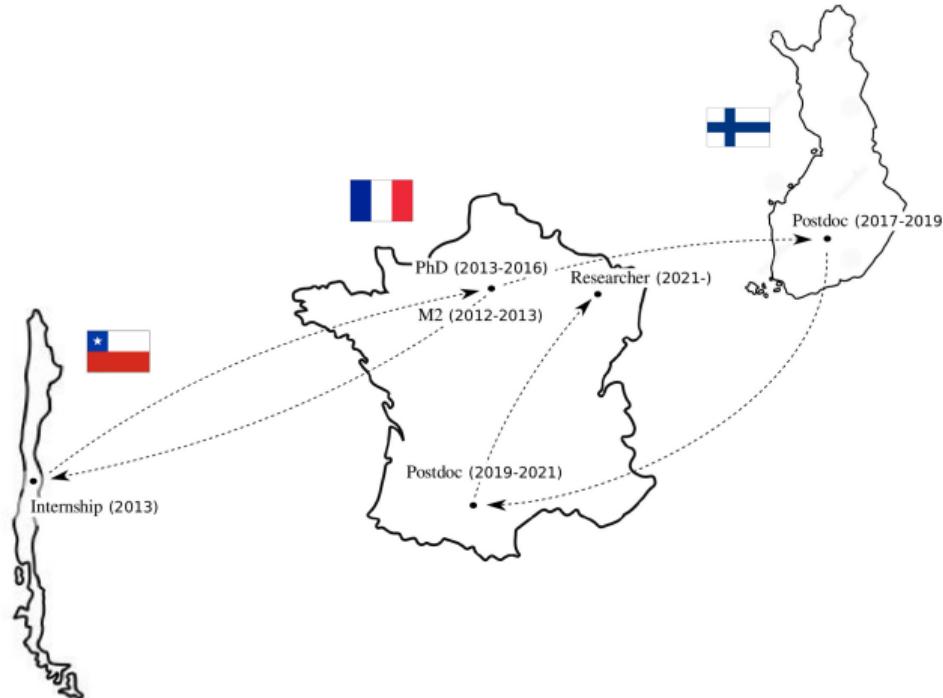
Université de Lorraine, CNRS, Inria, LORIA, Nancy, France



# A brief history of me



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*inria*

MULTISPEECH  
Speech Modeling for Facilitating Oral-Based Communication

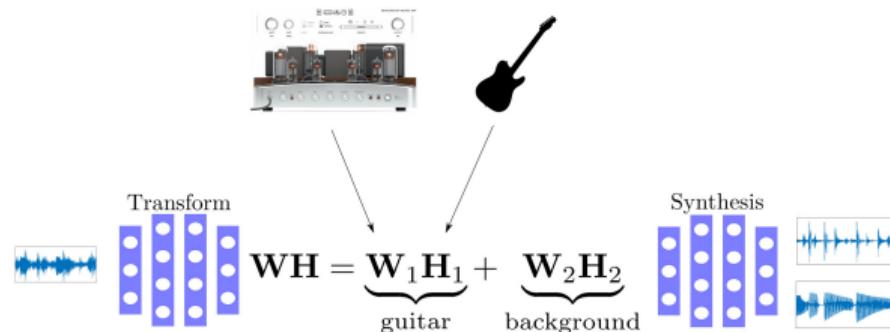


## Research themes

- ▷ Speech enhancement for auditory neuropathy (with N. Monir, R. Serizel).
- ▷ Audio inpainting / restoration (with L. Bahrman, M. Krémé, A. Deleforge).

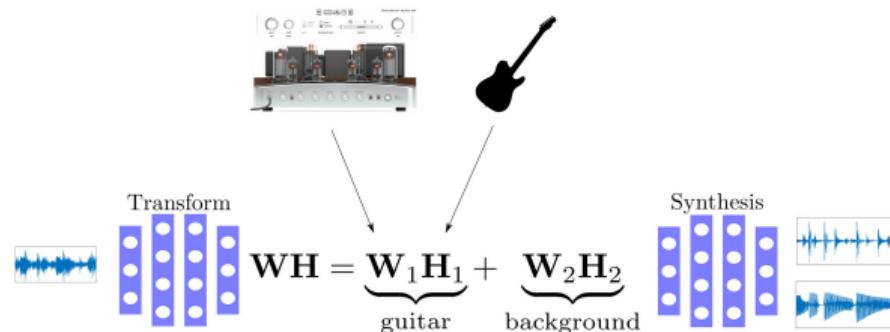
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- ▷ Joint synthesis / source separation.



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- ▷ **Source separation** (with so many people).

## **Audio source separation**

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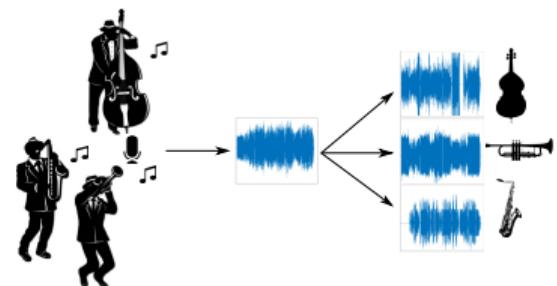
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**Source separation** = recovering the sources from the mixture.

- ▷ Augmented mixing (from mono to stereo).
- ▷ An important preprocessing for many analysis tasks (speech recognition, melody extraction...).

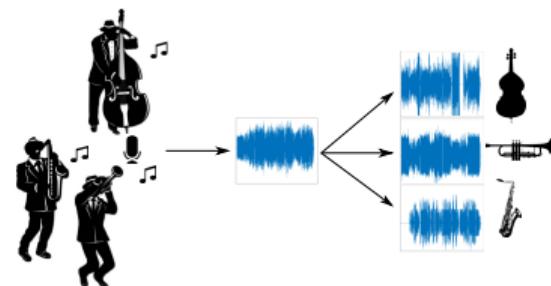


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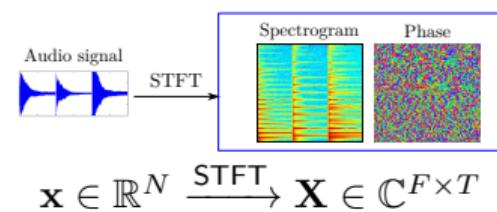
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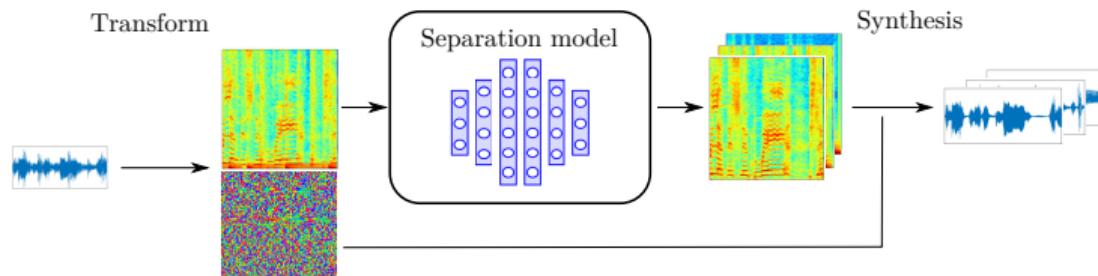
## Framework

- ▷ Monaural signals.
- ▷ Short-time Fourier transform (STFT)-domain separation.
- ▷ Mixture model:  $\mathbf{X} = \sum_{j=1}^J \mathbf{S}_j$ .



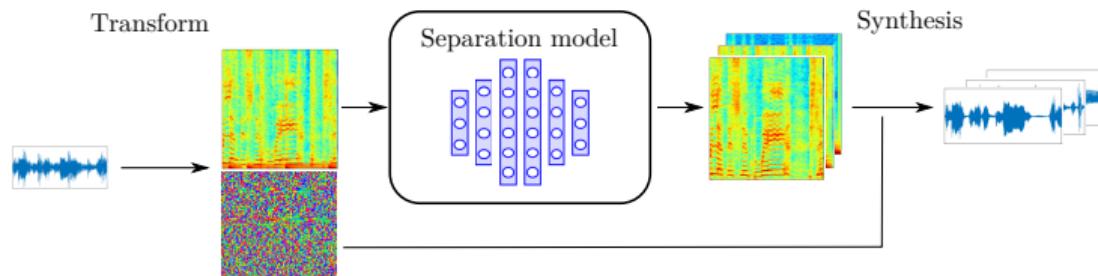
# Typical separation pipeline

Nonnegative time-frequency (TF) masking:



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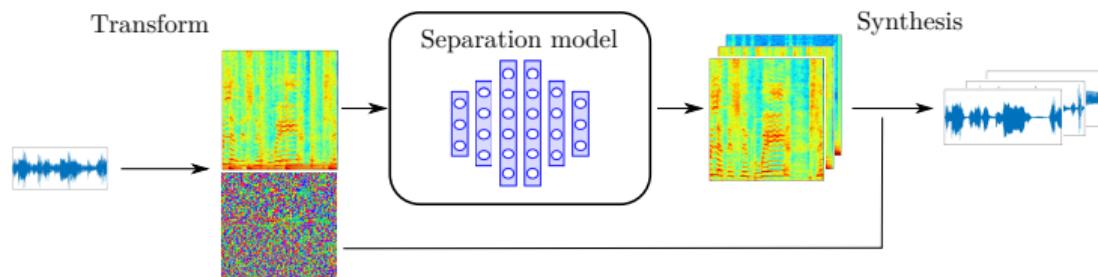
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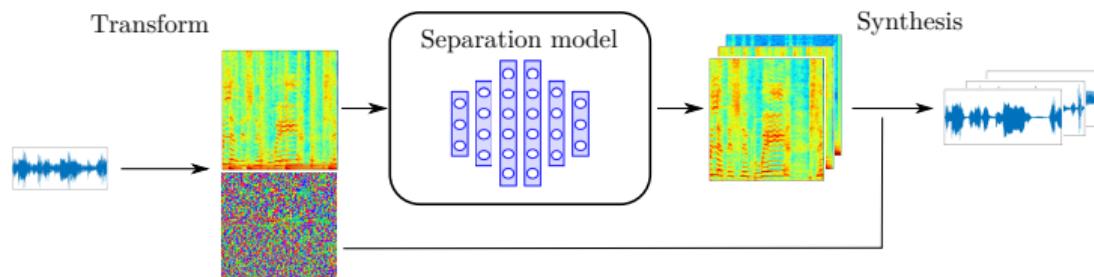
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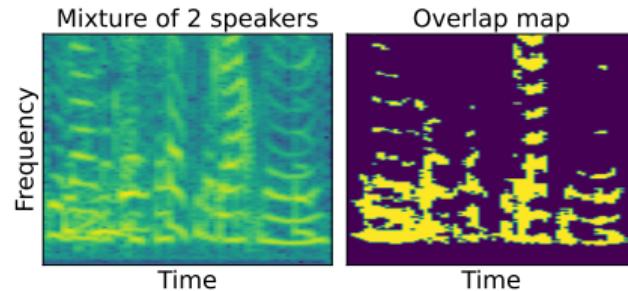


- ▷ A **nonnegative representation** is processed (e.g., magnitude or power spectrogram).
- ▷ The separator is a **deep neural network**, trained using a (large) dataset with isolated sources.
- ▷ The **mixture's phase** is assigned to each source using a Wiener-like filter or masking process.

# The phase problem

- ✗ Nonnegative masking: Issues in sound quality when sources *overlap* in the TF domain.

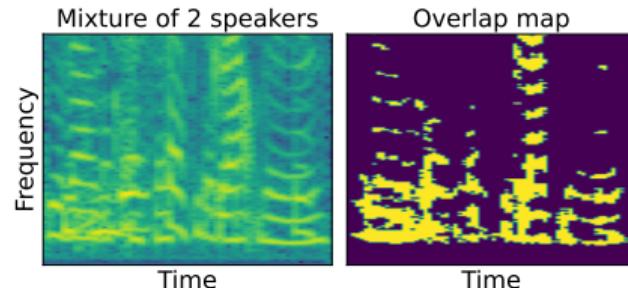
$$|X| \neq |S_1| + |S_2|$$
$$\angle X \neq \angle S_1 \text{ or } \angle S_2$$



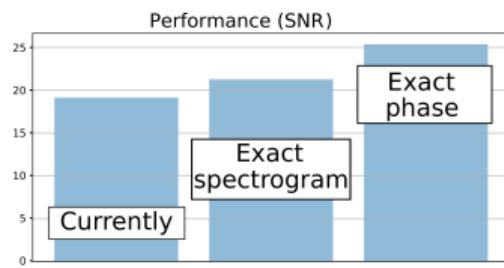
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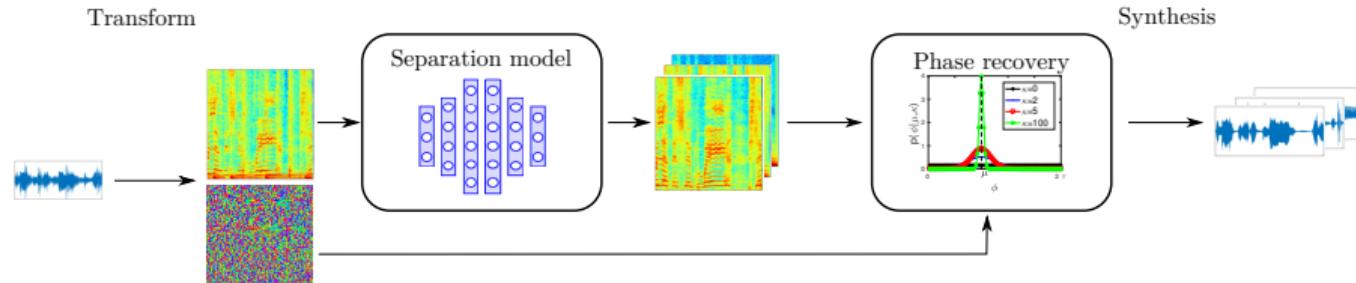


## The potential of phase recovery

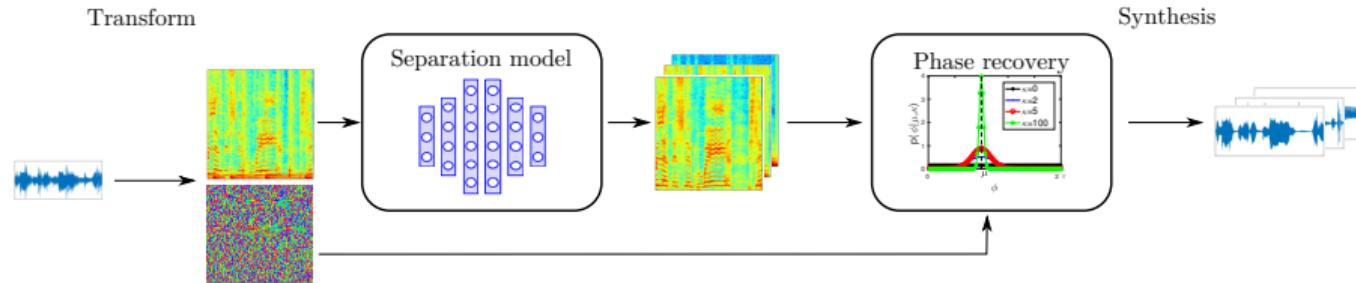


Given the current state-of-the-art, more potential gain in phase recovery than in magnitude estimation.

# Phase recovery for source separation

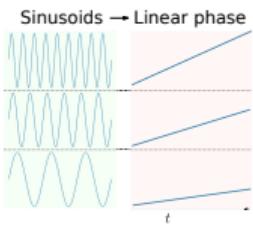


# Phase recovery for source separation

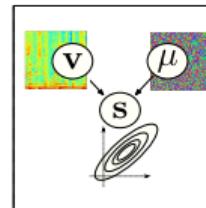


## Main contributions

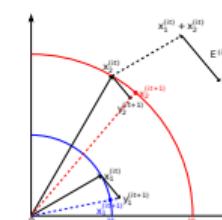
### Phase models



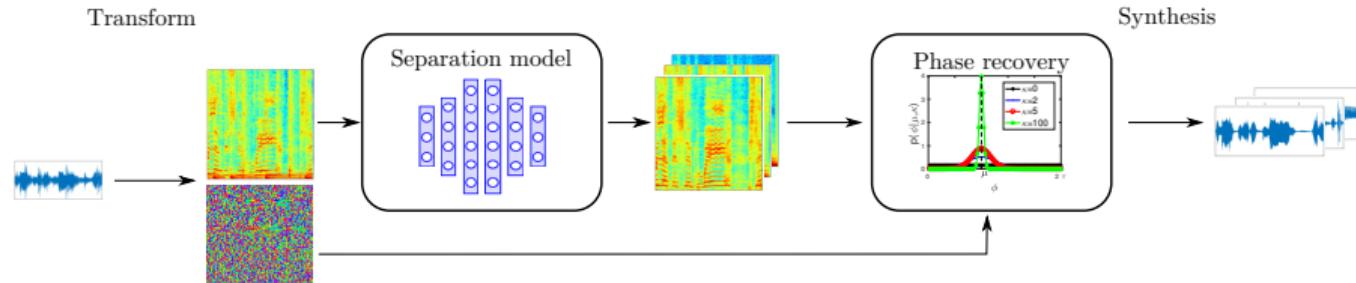
### Statistical framework



### Iterative algorithms

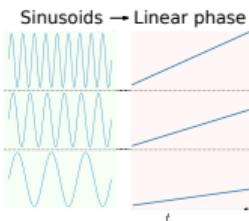


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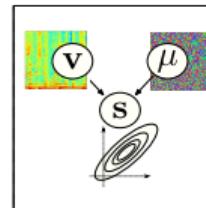


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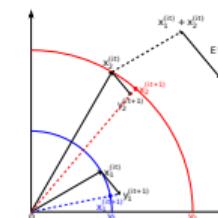
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- ▷ So far using “old-school” signal processing.
- ▷ Perspective: leveraging deep learning for phase recovery.

## **Phase models**

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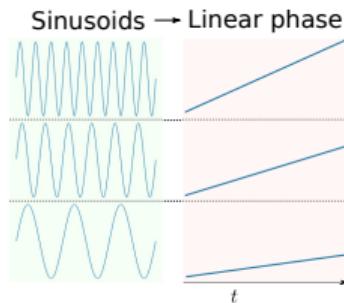
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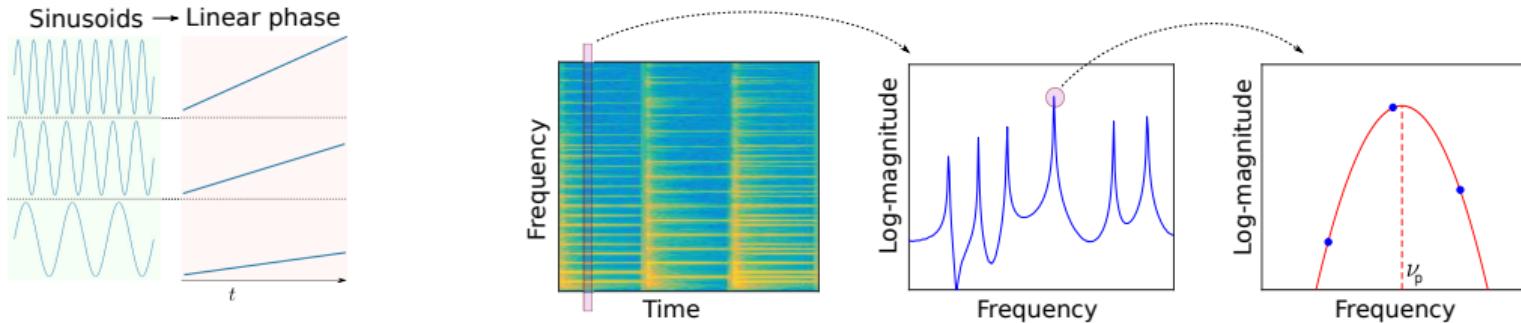
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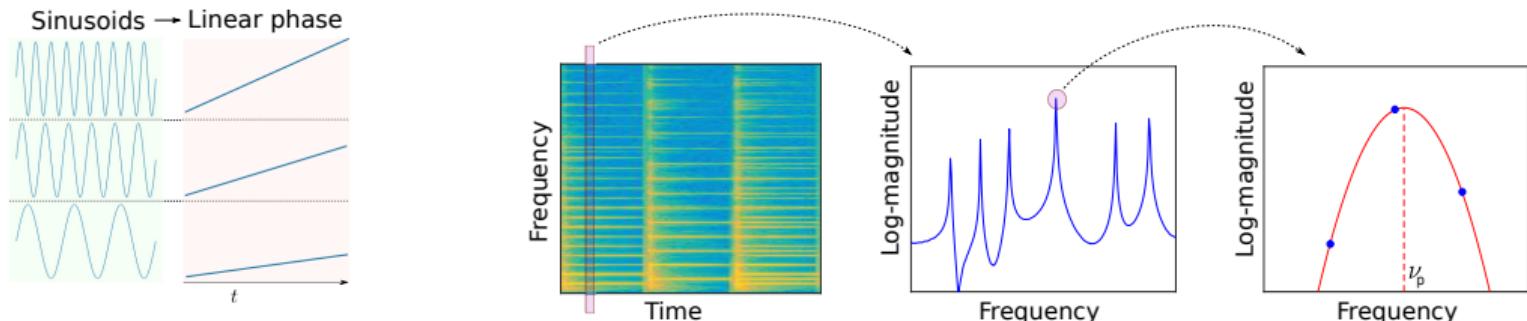
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- ✓ Useful for source separation (and audio inpainting) applications.
- ✗ The performance is limited due to the simplicity of the model.

## Perspective: towards deep phase models

**Recently:** Some attempts at predicting the phase using DNNs.

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- ✗ Cumbersome two-stage approaches to resolve some ambiguities.

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**Proposal:** Generalize phase models from signal analysis using deep learning.

$$\boldsymbol{\mu}_t = \boldsymbol{\mu}_{t-1} + l\boldsymbol{\nu}_t \quad \rightarrow \quad \boldsymbol{\mu}_t = \underbrace{\mathcal{R}(\boldsymbol{\nu}_t, \boldsymbol{\mu}_{t-1}, \dots, \boldsymbol{\mu}_{t-\tau})}_{\text{temporal dynamics}} \quad \text{with} \quad \boldsymbol{\nu}_t = \underbrace{\mathcal{C}(|\mathbf{x}|_t)}_{\text{frequency extraction}}$$

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- ▷ Architectural choices (non-linearities, loss functions) adapted to the phase (periodicity).
- ▷ Identify and exploit perceptual phase invariants.



## **Probabilistic phase modeling**

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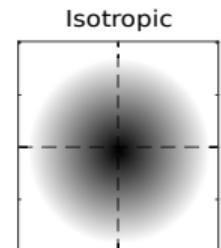
## Phase-aware Gaussian models

The ubiquitous **isotropic Gaussian** model:

$$s \sim \mathcal{N}_{\mathbb{C}}(m, \Gamma) \text{ with } \Gamma = \begin{pmatrix} \gamma & 0 \\ 0 & \gamma \end{pmatrix}$$

Equivalent to assuming a uniform phase  $\angle s \sim \mathcal{U}_{[0, 2\pi[} \cdot$

✗ Impossible to promote any phase structure / prior.



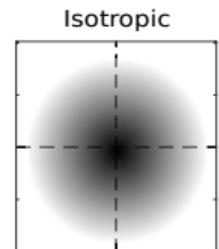
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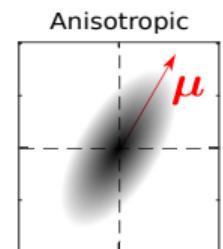


**Anisotropic Gaussian model**

$$s \sim \mathcal{N}_{\mathbb{C}}(m, \Gamma) \text{ with } \Gamma = \begin{pmatrix} \gamma & c \\ \bar{c} & \gamma \end{pmatrix}$$

$c$  is the *relation* term, defined as a function of the phase parameter  $\mu$ .

✓ Allows to incorporate phase priors; nice performance boost for source separation applications (e.g., phase-aware Wiener filter).



## Perspective: anisotropic deep learning

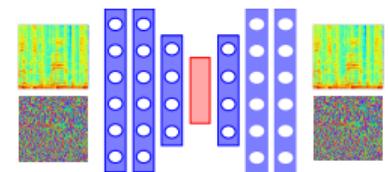
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**Proposal:** Combine deep learning and anisotropic modeling, e.g., via anisotropic VAEs.

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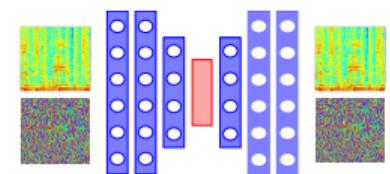


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- ▷ A strong effort in modeling and optimization is needed for deriving appropriate estimation techniques.

## **Spectrogram inversion algorithms**

---

# Spectrogram inversion

**Goal:** retrieve (complex-valued) STFTs from (non-negative) spectrograms.

- ▷ Identify important properties in the STFT domain.
- ▷ Promote them by defining an optimization problem.
- ▷ Solve it using some optimization strategy.

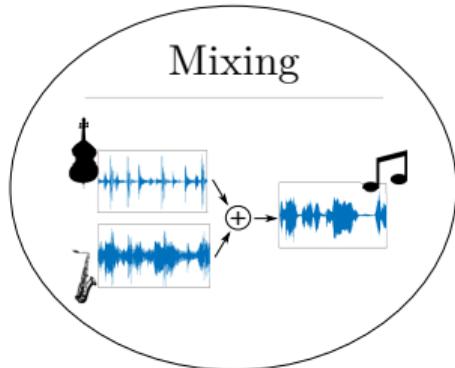
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- 
- ▷ Many algorithms in the literature!
  - ▷ Which problem formulation is the most appropriate in practice?
  - ▷ Proposal: let's define a general spectrogram inversion framework.

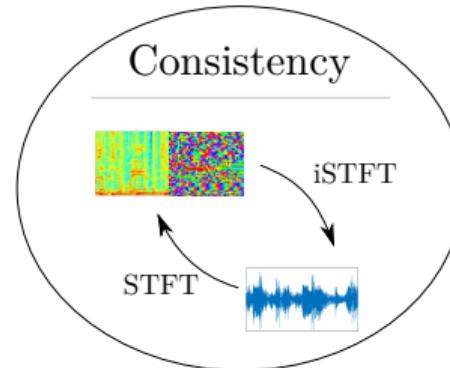
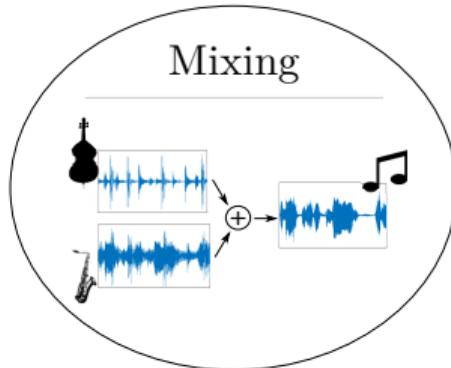


## STFT-domain constraints



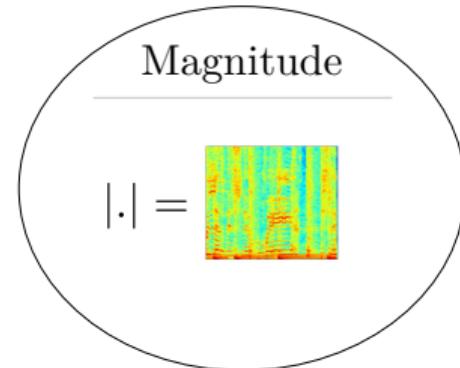
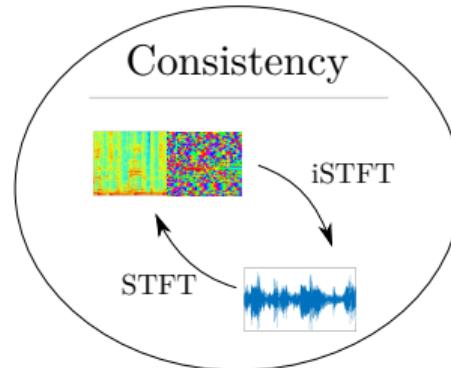
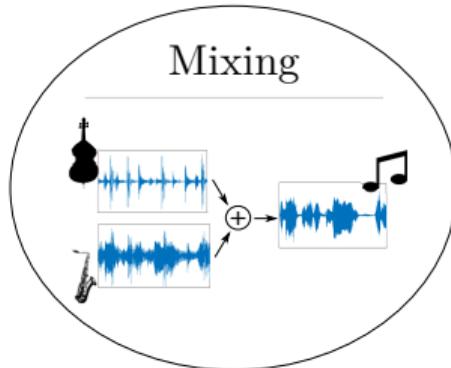
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- ▷ **Consistency:** the estimates (=complex-valued matrices) should be the STFT of time-domain signals.
- ▷ **Magnitude match:** the estimates' magnitude should remain close to the output of the DNN computed beforehand.

## Overview

**Proposal:** A general framework for deriving spectrogram inversion algorithms

- ▷ For each property/objective/constraint, define a loss function (and an auxiliary function).
- ▷ Combine them (soft penalties / hard constraints) to formulate optimization problems.
- ▷ Derive algorithms that alternate projections on the corresponding constraints subspaces.

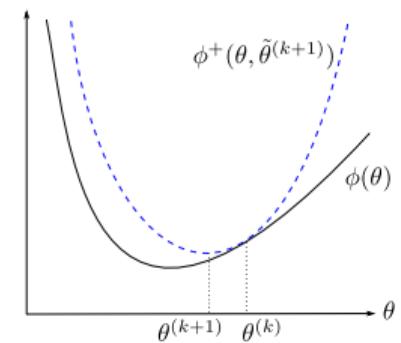
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## Auxiliary function method

- ▷ Considering minimization of  $\phi$ , construct  $\phi^+$  such that:  
$$\phi(\theta) = \min_{\tilde{\theta}} \phi^+(\theta, \tilde{\theta}).$$
- ▷  $\phi$  is non-increasing when minimizing  $\phi^+$  with respect to  $\theta$  and  $\tilde{\theta}$  alternately.
- ✓ Convergence, successfully used in audio, no hyperparameter to tune.

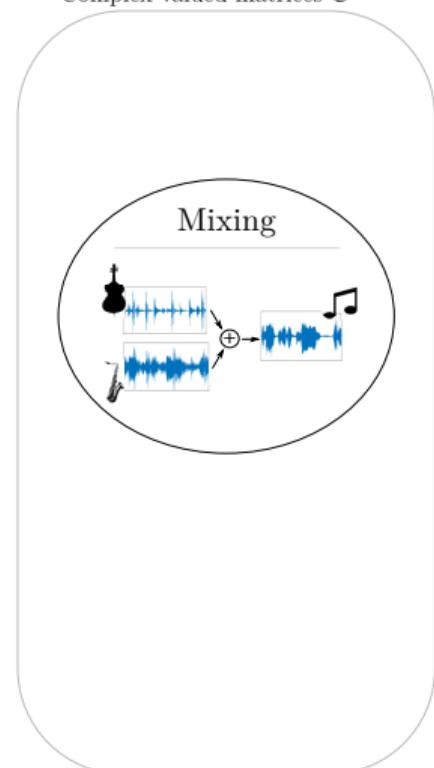


# Mixing constraint

Loss function that promotes conservative estimates:

$$h(\mathbf{S}) = \left\| \mathbf{X} - \sum_j \mathbf{S}_j \right\|^2$$

Complex-valued matrices  $\mathbb{C}^{F \times T}$



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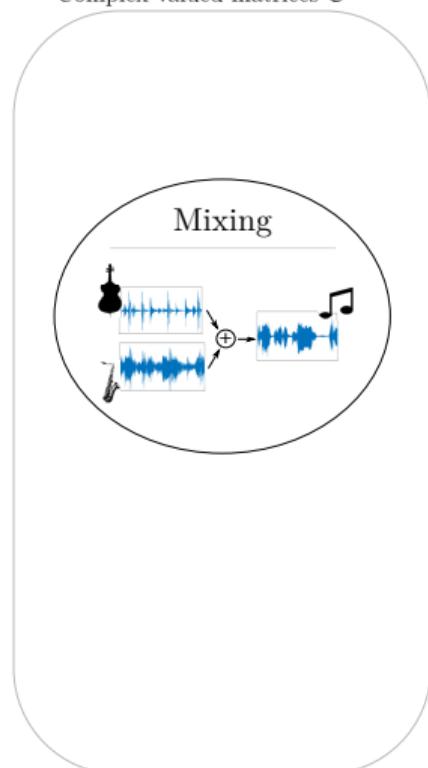
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Auxiliary function

- ▷ Auxiliary parameters  $\mathbf{Y}$  such that  $\sum_j \mathbf{Y}_j = \mathbf{X}$ .
- ▷ Positive weights  $\Lambda_j$  such that  $\sum_j \lambda_{j,f,t} = 1$ .
- ▷ Then the following is an auxiliary function for  $h$ :

$$h^+(\mathbf{S}, \mathbf{Y}) = \sum_{j,f,t} \frac{|y_{j,f,t} - s_{j,f,t}|^2}{\lambda_{j,f,t}}$$

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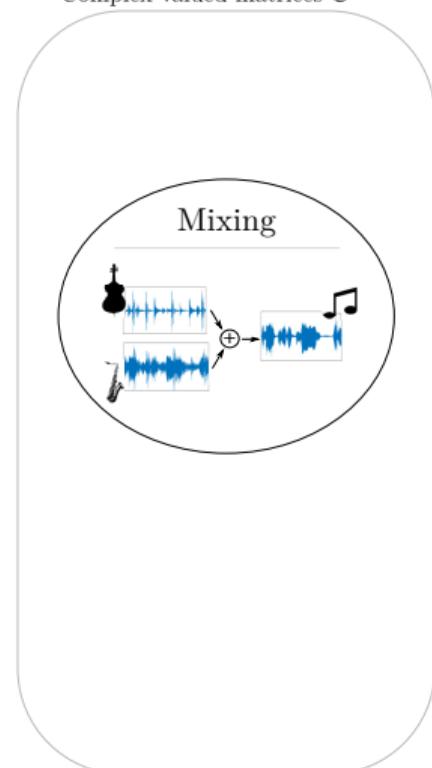
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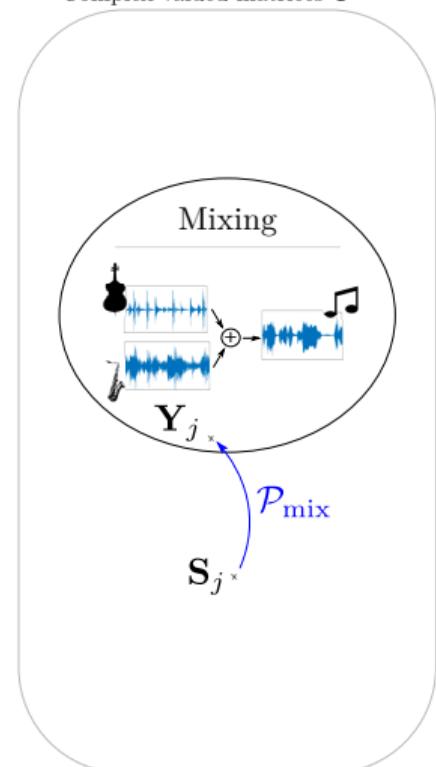
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- ▷ Defines a projector  $\mathcal{P}_{\text{mix}}$  onto the subspace of matrices complying with the mixing constraint.

Complex-valued matrices  $\mathbb{C}^{F \times T}$

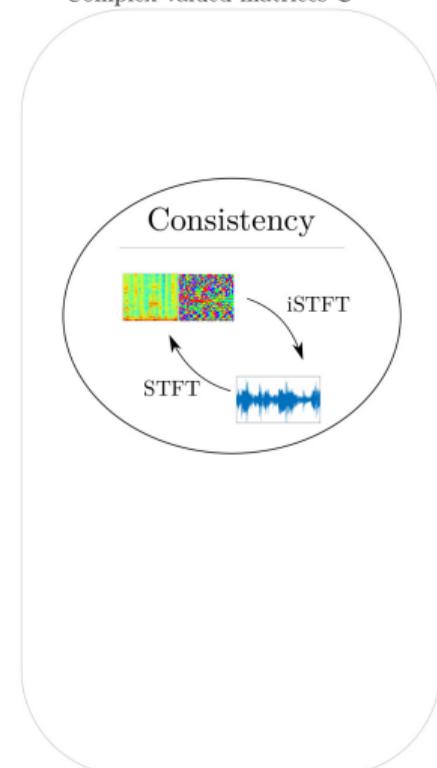


# Consistency constraint

Loss function that promotes consistent estimates:

$$i(\mathbf{S}) = \sum_j \|\mathbf{S}_j - \mathcal{G}(\mathbf{S}_j)\|^2 \text{ with } \mathcal{G} = \text{STFT} \circ \text{iSTFT}$$

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# Consistency constraint

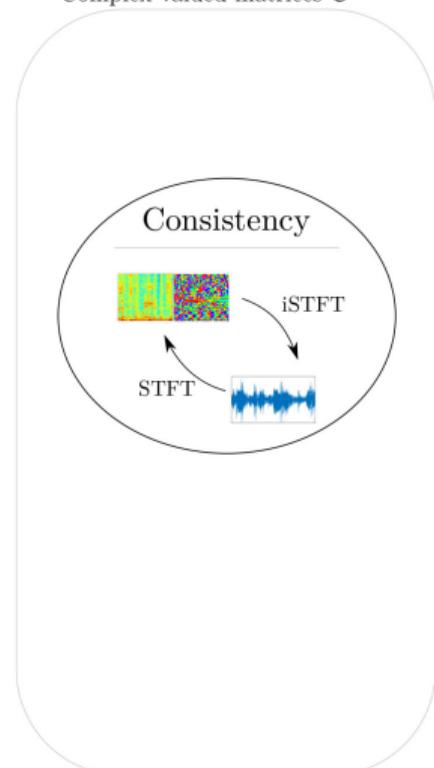
Loss function that promotes consistent estimates:

$$i(\mathbf{S}) = \sum_j \|\mathbf{S}_j - \mathcal{G}(\mathbf{S}_j)\|^2 \text{ with } \mathcal{G} = \text{STFT} \circ \text{iSTFT}$$

Auxiliary function

- ▷  $\mathcal{G}(\mathbf{S}_j)$  is the closest consistent matrix to  $\mathbf{S}_j$ .
- ▷ Then  $i^+(\mathbf{S}, \mathbf{Z}) = \sum_j \|\mathbf{S}_j - \mathbf{Z}_j\|^2$  (where  $\mathbf{Z}_j \in \text{Im}(\text{STFT})$ ) is an auxiliary function for  $i$ .

Complex-valued matrices  $\mathbb{C}^{F \times T}$



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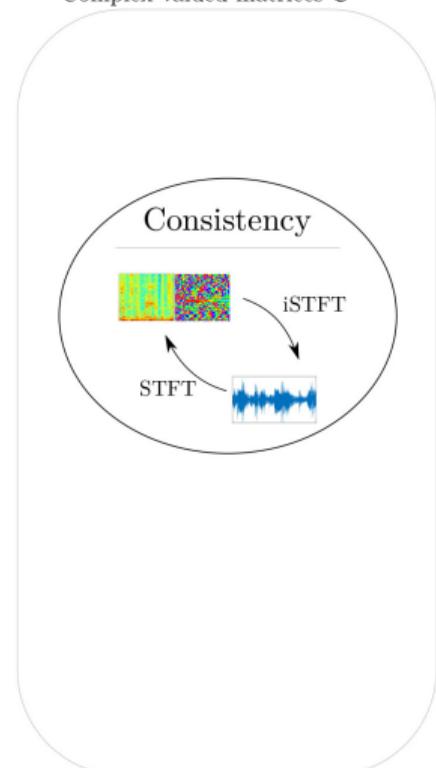
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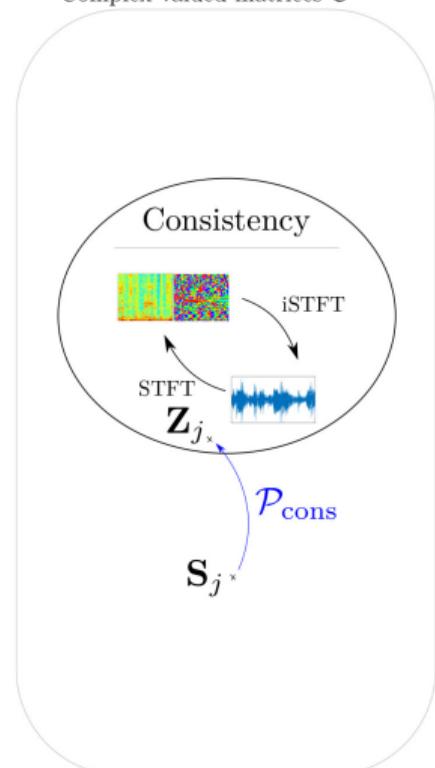
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- ▷ Defines a projector  $\mathcal{P}_{\text{cons}}$  onto the subspace of consistent matrices.

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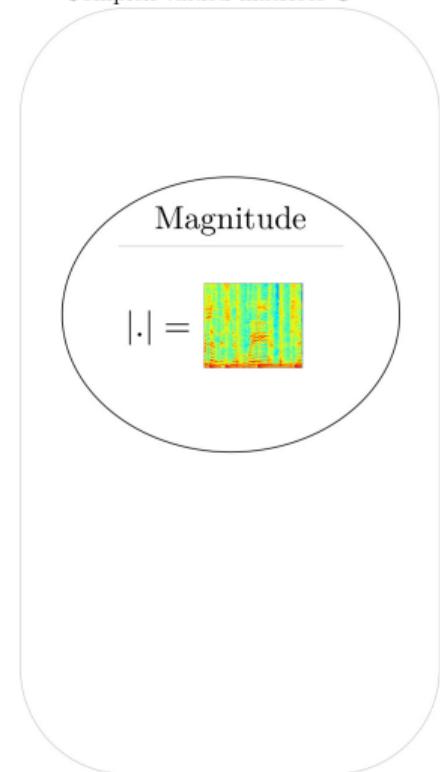


## Magnitude constraint

Loss function that ensures the estimates' magnitudes remain close to the target value  $\mathbf{V}_j$  estimated beforehand (e.g., using a DNN):

$$m(\mathbf{S}) = \sum_j |||\mathbf{S}_j| - \mathbf{V}_j||^2$$

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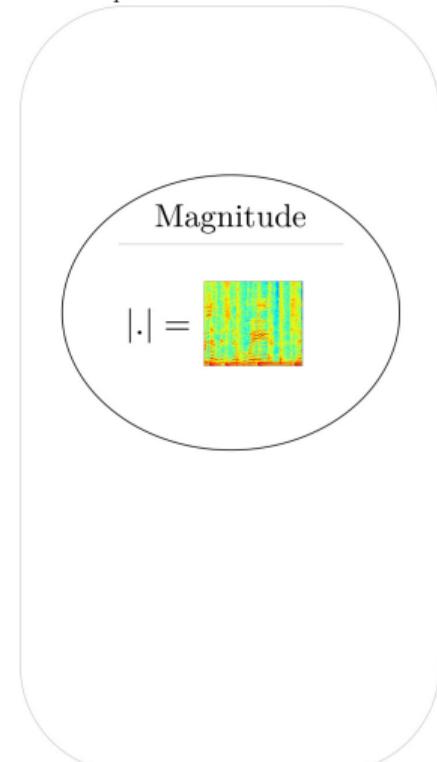
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- ▷ Auxiliary parameters  $\mathbf{U}$  such that  $|\mathbf{U}_j| = \mathbf{V}_j$ .
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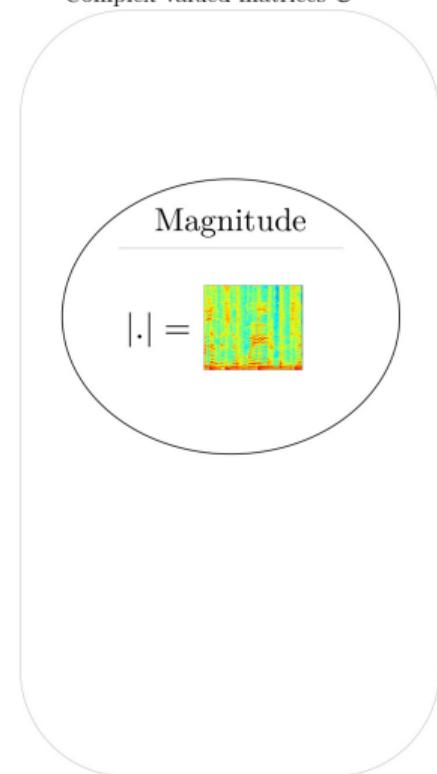
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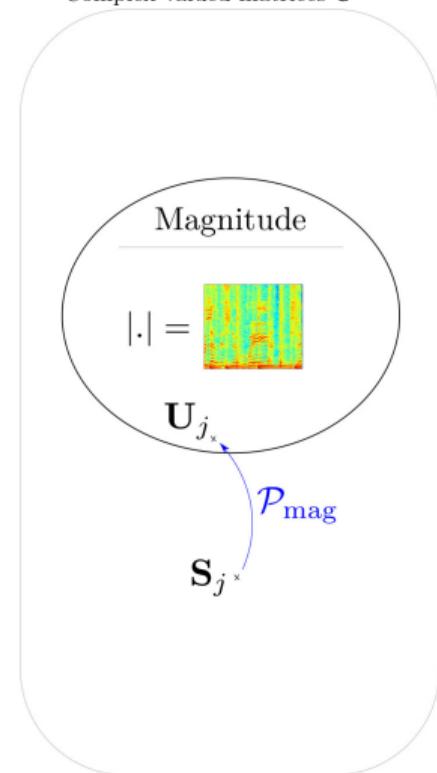
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- ▷ Defines a projector  $\mathcal{P}_{\text{mag}}$  onto the subspace of matrices whose magnitude equals the target value.

Complex-valued matrices  $\mathbb{C}^{F \times T}$



## Algorithm derivation example: problem setting

Main problem: optimize the mixing objective + soft consistency penalty + hard magnitude constraint.

$$\min_{\mathbf{S}} h(\mathbf{S}) + \sigma i(\mathbf{S}) \text{ such that } |\mathbf{S}_j| = \mathbf{V}_j$$

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Using our auxiliary function framework, this rewrites:

$$\min_{\mathbf{S}, \mathbf{Y}, \mathbf{Z}} h^+(\mathbf{S}, \mathbf{Y}) + \sigma i^+(\mathbf{S}, \mathbf{Z}) \quad \text{such that} \quad \begin{cases} |\mathbf{S}_j| = \mathbf{V}_j \\ \sum_j \mathbf{Y}_j = \mathbf{X} \\ \mathbf{Z}_j \in \text{Im(STFT)} \end{cases}$$

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- ▷ Auxiliary parameters updates ( $\mathbf{Y}$  and  $\mathbf{Z}$ ) are already known.
- ▷ So let's focus on the update on  $\mathbf{S}$ .

## Algorithm derivation example: update

### New problem

- ▷ Incorporate the hard constraint using the method of Lagrange multipliers.
- ▷ Find a critical point for:

$$h^+(\mathbf{S}, \mathbf{Y}) + \sigma i^+(\mathbf{S}, \mathbf{Z}) + \sum_{j,f,t} \delta_{j,f,t} (|s_{j,f,t}|^2 - v_{j,f,t}^2)$$

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## Update

- ▷ Set the partial derivative with respect to  $\mathbf{S}$  at 0 and solve:

$$\mathbf{S}_j = \frac{\mathbf{Y}_j + \sigma \boldsymbol{\Lambda}_j \odot \mathbf{Z}_j}{|\mathbf{Y}_j + \sigma \boldsymbol{\Lambda}_j \odot \mathbf{Z}_j|} \odot \mathbf{V}_j$$

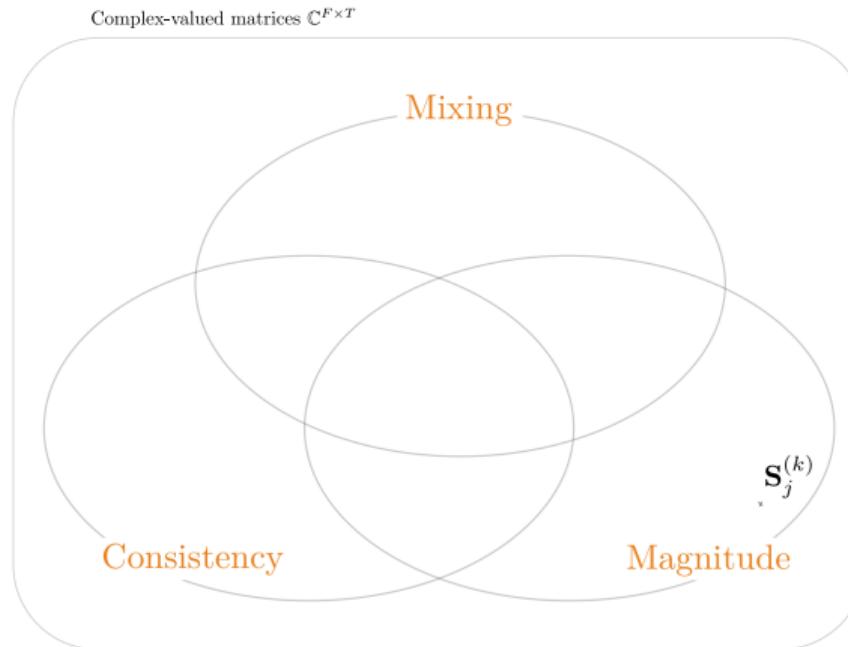
- ▷ Generalizes particular cases from the literature ( $\sigma = 0$  and  $\sigma = +\infty$ ).

## Algorithm derivation example: illustration

Compact update rule using the projectors:  $\mathcal{P}_{\text{mag}} (\mathcal{P}_{\text{mix}}(\mathbf{S}) + \sigma \boldsymbol{\Lambda} \odot \mathcal{P}_{\text{cons}}(\mathbf{S}))$

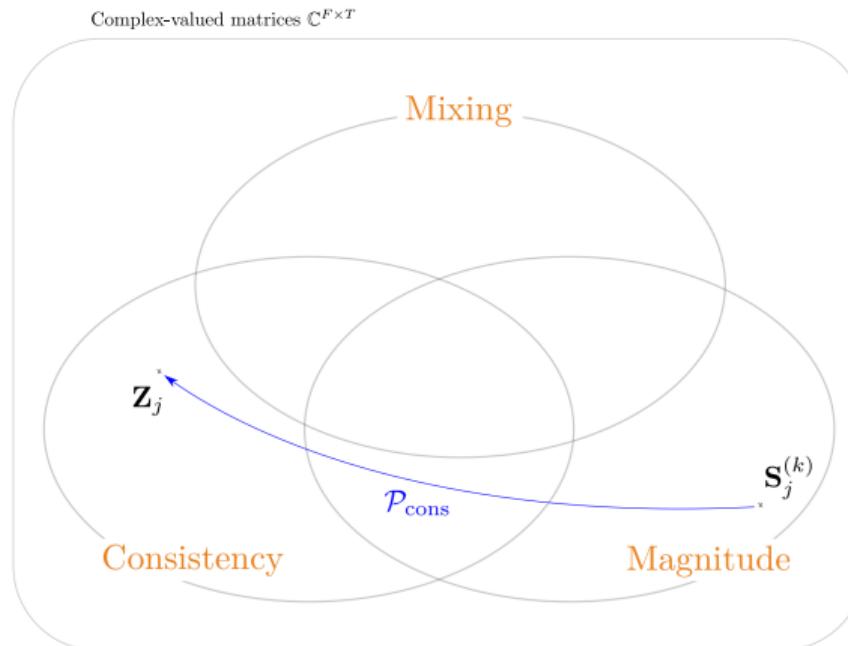
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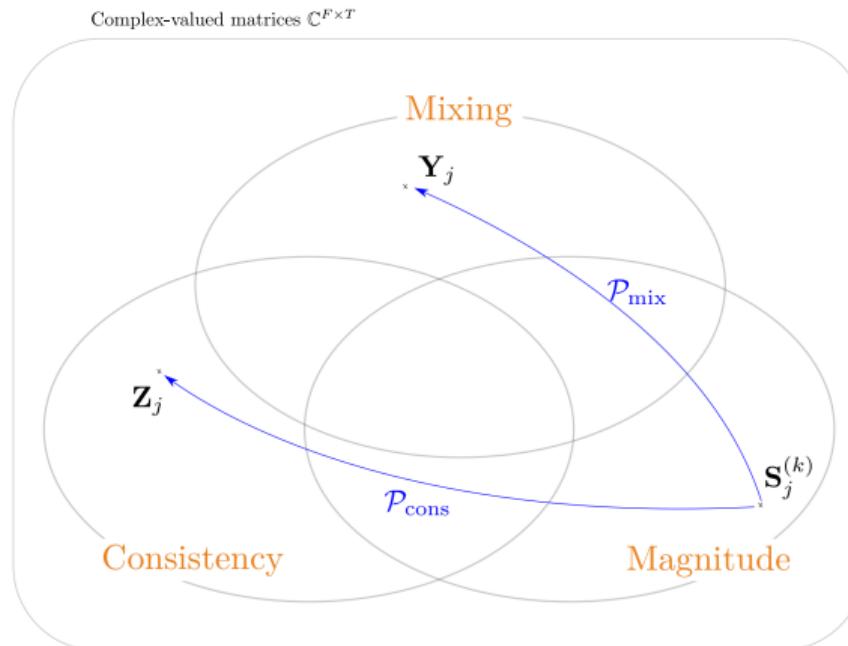
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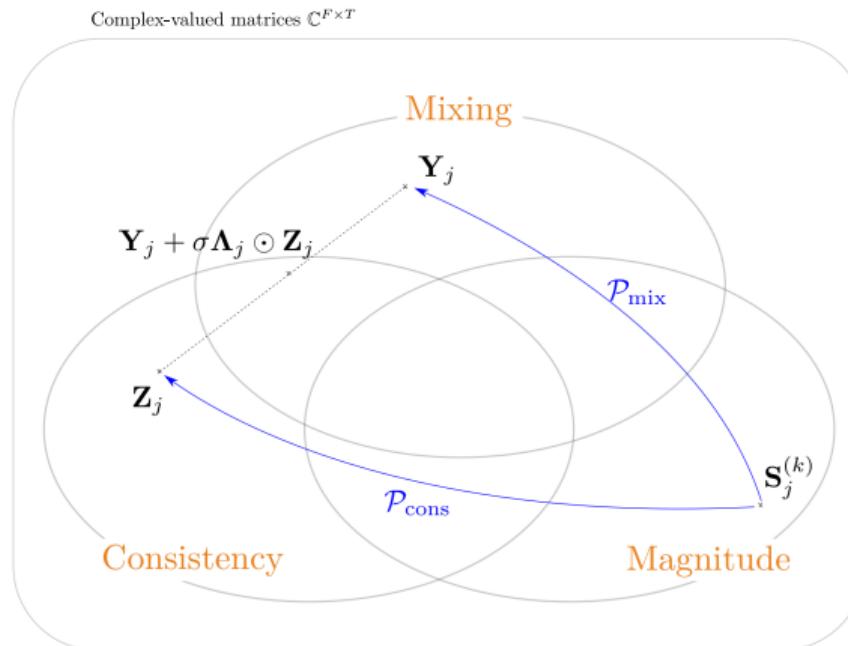
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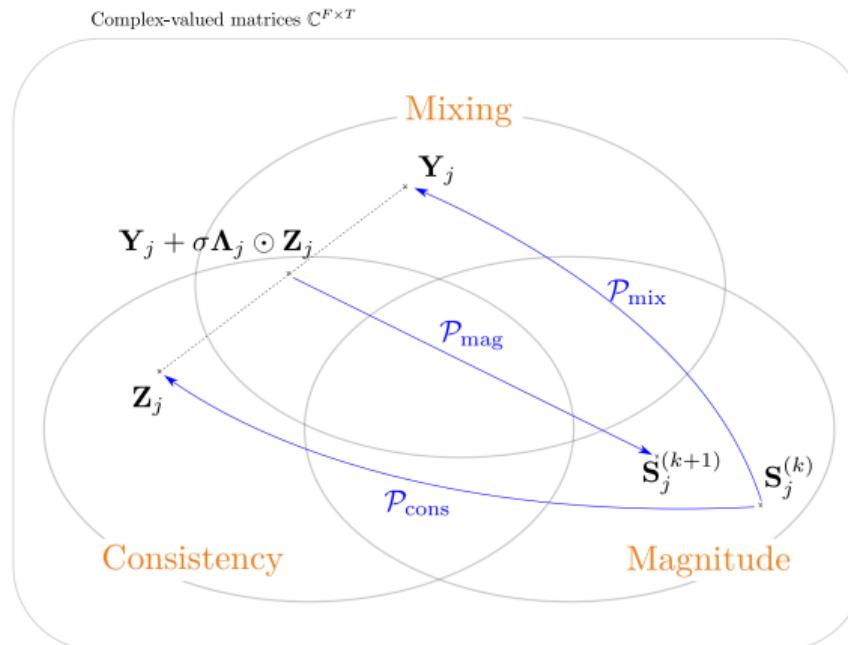
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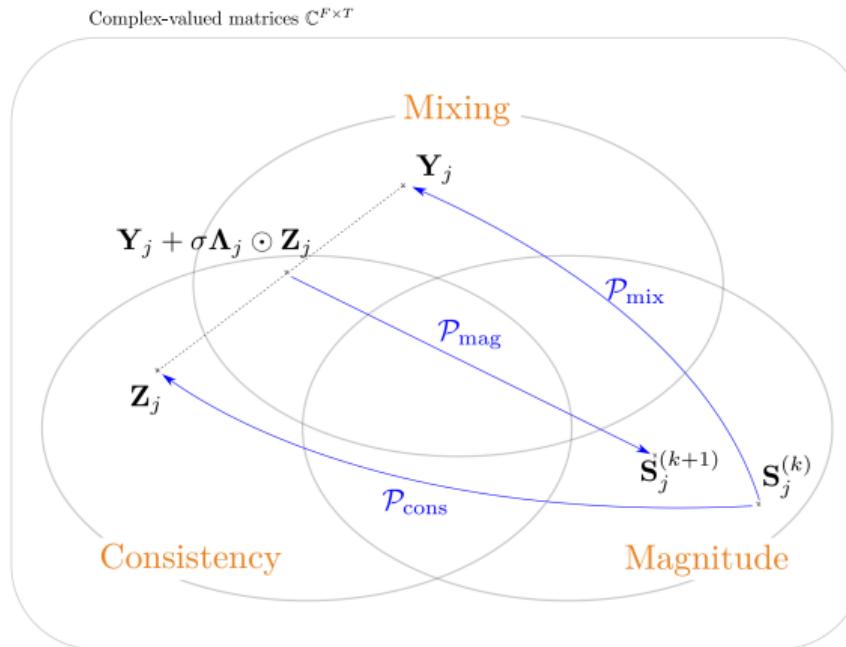
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Check our EUSIPCO paper for all problem formulations / update schemes.

# Experiments

**Task:** speech enhancement

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Separation quality (signal-to-distortion ratio):

	Accurate magnitudes	Less accurate magnitudes
Baseline (MISI)	<b>19.6</b>	7.7
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Proposed (3)	19.3	<b>8.1</b>

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- ▷ Some novel algorithms are interesting alternatives.
- ▷ Perspectives: unfold these into neural networks for time-domain training.

## **Conclusion**

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## Current trends



From nonnegative to time-domain deep learning.

- ✓ Performance in controlled conditions, no more phase problem.

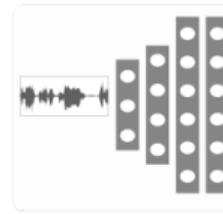
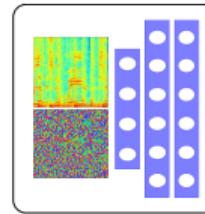
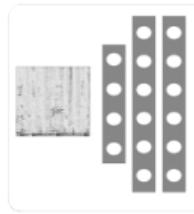
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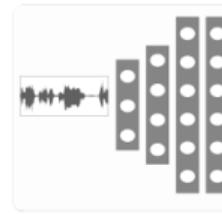
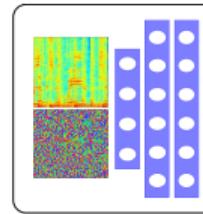
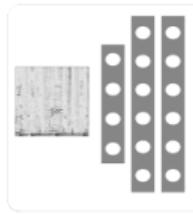
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- ✓ Performance of processing all the data exhaustively.

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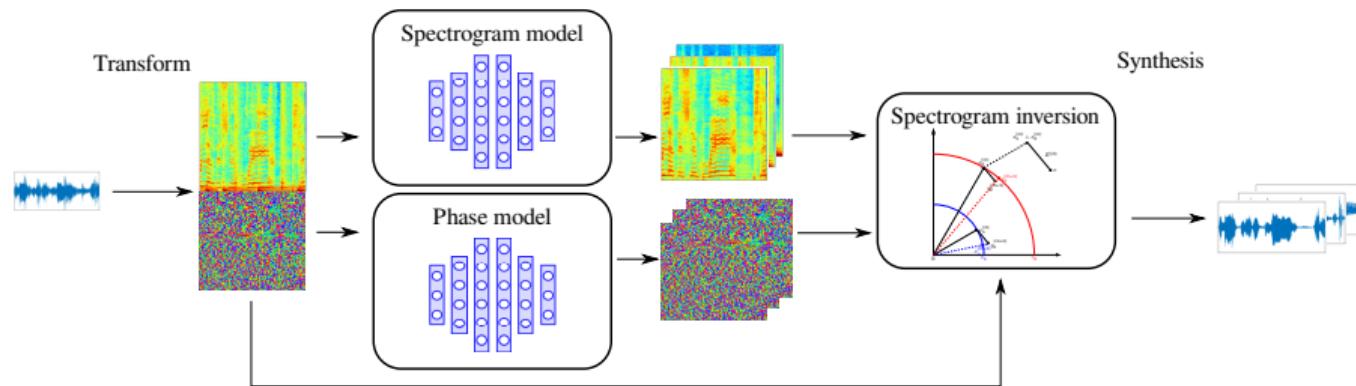
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- ✓ Robustness/flexibility of time-frequency processing.
- ✓ Performance of processing all the data exhaustively.
- ✗ Using a real/imaginary part decomposition of the STFT is sub-optimal.

## The proposed alternative

- ▷ The room for improvement of phase recovery: more potential gain than with magnitudes.
- ▷ Move towards **deep phase recovery** for increased performance.



Work in progress:

- ▷ Design deep phase prior models.
- ▷ Unfold iterative algorithms into neural networks for time-domain separation.

# Thanks!

🌐 <https://magronp.github.io/>

⌚ <https://github.com/magronp/>

