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## Equation for circles intersection

In[52]:= **Xsol** = **Flatten**[**Solve**[ $(x - d)^2 + y^2 == R^2$ ] /. { $y^2 \rightarrow (r^2 - x^2)$ }, **x**]

Out[52]=  $\left\{ x \rightarrow \frac{d^2 + r^2 - R^2}{2 d} \right\}$

In[53]:= **Ysol** = **FullSimplify**[**Flatten**[**Solve**[ $(y^2 + x^2 == r^2) \&\& x < r \&\& x > -r$ ] /. **Xsol**, **y**]]]

Out[53]=  $\left\{ y \rightarrow -\frac{1}{2} \sqrt{-\frac{(d - r - R)(d + r - R)(d - r + R)(d + r + R)}{d^2}} \text{ if } \text{condition} \right\},$   
 $y \rightarrow \frac{1}{2} \sqrt{-\frac{(d - r - R)(d + r - R)(d - r + R)(d + r + R)}{d^2}} \text{ if } \text{condition} \right\}$

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## Test cases

In[54]:= **Solve**[ $\{x^2 + y^2 == 1, (x - 1)^2 + y^2 == 1\}$ , {**x**, **y**}]

Out[54]=  $\left\{ \left\{ x \rightarrow \frac{1}{2}, y \rightarrow -\frac{\sqrt{3}}{2} \right\}, \left\{ x \rightarrow \frac{1}{2}, y \rightarrow \frac{\sqrt{3}}{2} \right\} \right\}$

In[55]:= **ArcTan** $\left[\frac{1}{2}, \frac{\sqrt{3}}{2}\right] - \left(\frac{1}{2} \times \frac{\sqrt{3}}{2}\right) + \text{ArcTan}\left[\frac{1}{2}, \frac{\sqrt{3}}{2}\right] - \left(\frac{1}{2} \times \frac{\sqrt{3}}{2}\right)$

Out[55]=  $-\frac{\sqrt{3}}{2} + \frac{2 \pi}{3}$

In[56]:= **Solve**[ $\{x^2 + y^2 == 1, \left(x - \frac{3}{2}\right)^2 + y^2 == 1\}$ , {**x**, **y**}]

Out[56]=  $\left\{ \left\{ x \rightarrow \frac{3}{4}, y \rightarrow -\frac{\sqrt{7}}{4} \right\}, \left\{ x \rightarrow \frac{3}{4}, y \rightarrow \frac{\sqrt{7}}{4} \right\} \right\}$

In[57]:= **N** $\left[\frac{\sqrt{3}}{2}, 50\right]$

Out[57]= 0.86602540378443864676372317075293618347140262690519

In[58]:= **N** $\left[\frac{\sqrt{7}}{4}, 50\right]$

Out[58]= 0.66143782776614764762540393840981510642756479577061

In[59]:= **N** $\left[-\frac{\sqrt{3}}{2} + \frac{2 \pi}{3}, 50\right]$

Out[59]= 1.2283696986087568455447057514333990726600436393449

In[60]:= **N**[ $\pi$ , 50]

Out[60]= 3.1415926535897932384626433832795028841971693993751

In[61]:=  $\mathbf{N}\left[\frac{\pi}{2}, 50\right]$

Out[61]= 1.5707963267948966192313216916397514420985846996876

In[62]:=  $\mathbf{N}\left[\frac{\pi}{4}, 50\right]$

Out[62]= 0.78539816339744830961566084581987572104929234984378

In[63]:=  $\mathbf{N}\left[\frac{1}{\sqrt{2}}, 50\right]$

Out[63]= 0.70710678118654752440084436210484903928483593768847