



**Faculty of Engineering & Technology Electrical & Computer
Engineering Department**

Communication Lab - ENEE4113

Experiment 1: Normal Amplitude Modulation and Demodulation

Prelab #1

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Theoretical Prelab

Definition Normal Amplitude Modulation (AM)

Is the process of varying the amplitude of a sinusoidal carrier wave in synchronism with, and in direct proportion, to the amplitude of a modulating signal.[1]

Mathematical Representation of AM

$$s(t) = A_c(1 + K_a m(t)) \cos(2\pi f_c t)$$

Where:

- A_c : The amplitude of carrier signal
- f_c : The frequency of carrier signal
- $m(t)$: Message signal
- k_a : The amplitude sensitivity

AM transmitters vary the amplitude of the carrier wave:

- The amplitude of the carrier wave is proportional to the amplitude of the signal being modulated.[2]
- If the modulation signal frequency increases, the amplitude of the carrier changes at a greater rate.[2]
- If the modulation signal frequency increases, the sidebands move further from the carrier. [2]

Frequency Spectrum of AM signal

The frequency spectrum of an AM signal can be obtained using Fourier analysis, and it is given by:

$$s(f) = \frac{A_c k_a}{2} [M(f - f_c) + M(f + f_c)] + \frac{A_c}{2} [\delta(f - f_c) + \delta(f + f)]$$

Where:

- $M(f)$ is the Fourier transform of the modulating signal.
- $\delta(f)$ is the delta function.

Demodulation of an AM Signal

Demodulation is defined as extracting the original information-carrying signal from a modulated carrier wave. A demodulator is an electronic circuit that is mainly used to recover the information content from the modulated carrier wave. [3]

The demodulated signal can be expressed as:

$$m(t) = A_c s(t) \cos(2\pi f_c t)$$

Which is the product of the received signal and a local oscillator at the carrier frequency. This signal is then passed through a low-pass filter to remove the carrier frequency and obtain the modulating signal.

Software Prelab

Message signal

$$m(t) = 0.85 \cos(2\pi(1000)t)$$

Plot Message signal in Time Domine

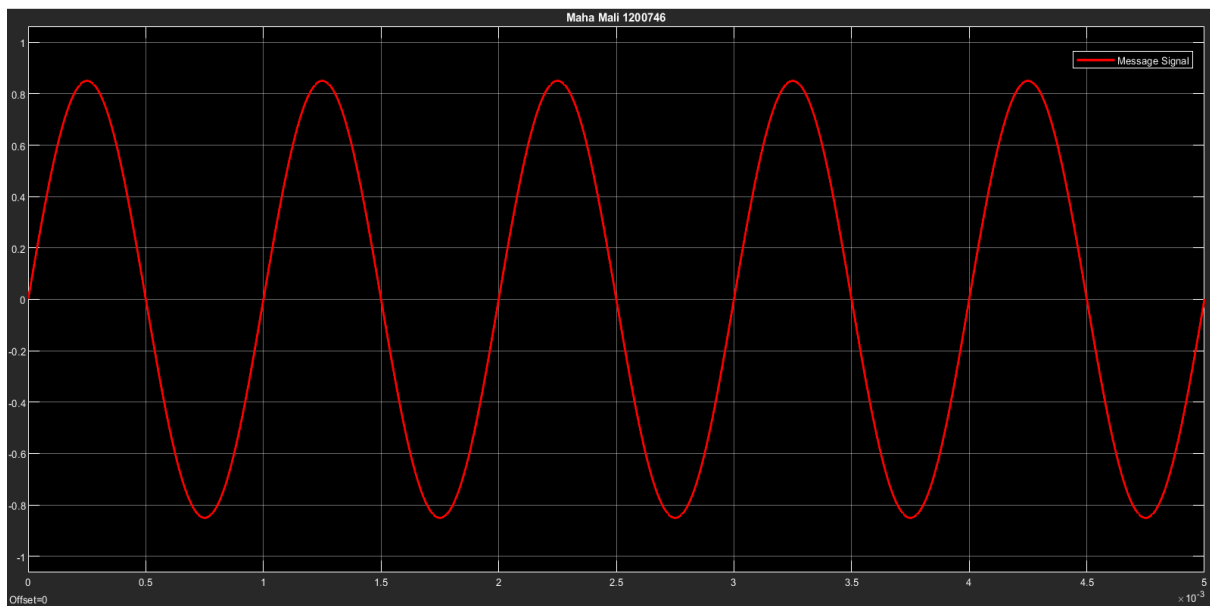


Figure 1: Message signal in time domain

We notice from the graph that the amplitude of the Message signal is greater than 0.8, and this is very similar to the amplitude value in the Message signal equation.

Plot Message signal in Frequency Domine

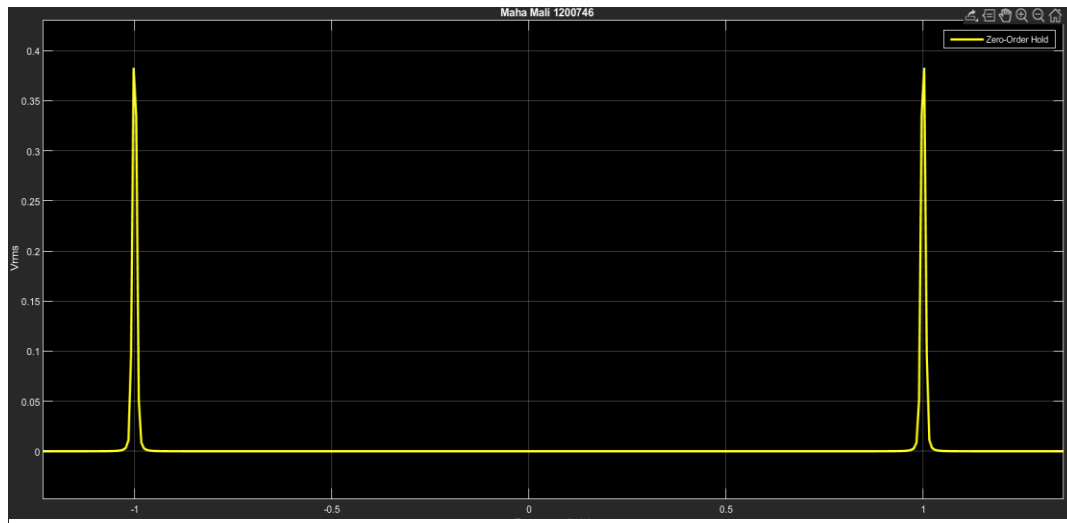


Figure 2: spectrum of message signal

From the graph for the spectrum of message signal we notice that there is two delta function one around -1khz, and another one around 1khz.

Carrier signal

$$c(t) = 1\cos(2\pi(15000)t)$$

Plot Carrier signal in Time Domine

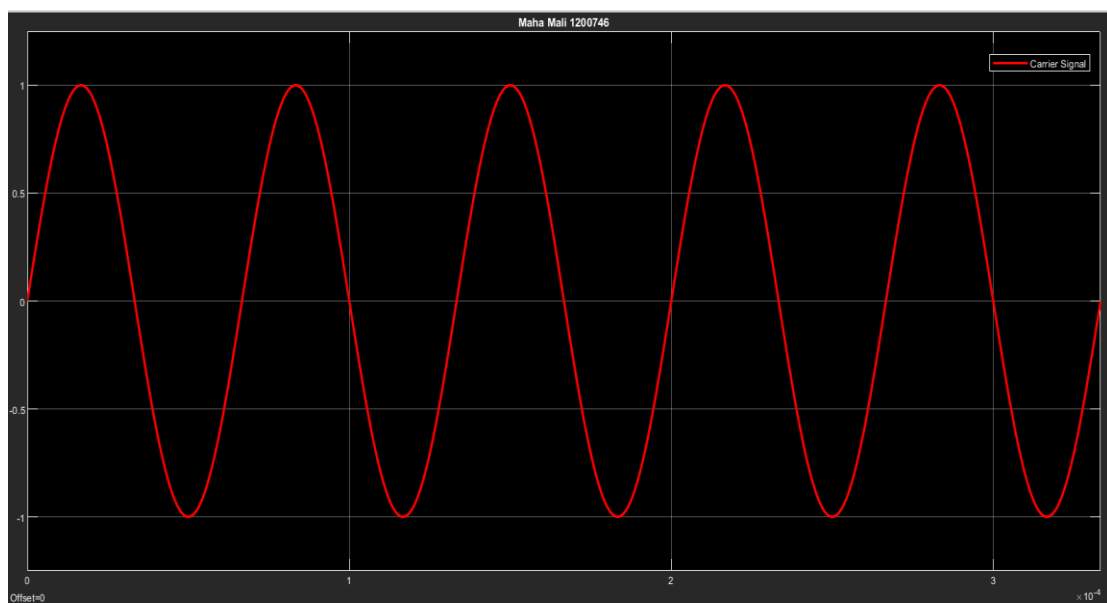


Figure 3 :carrier signal in time domain

We notice from the graph that the amplitude of the carrier signal is 1, and this is very similar to the amplitude value in the carrier signal equation.

Plot Carrier signal in Frequency Domine

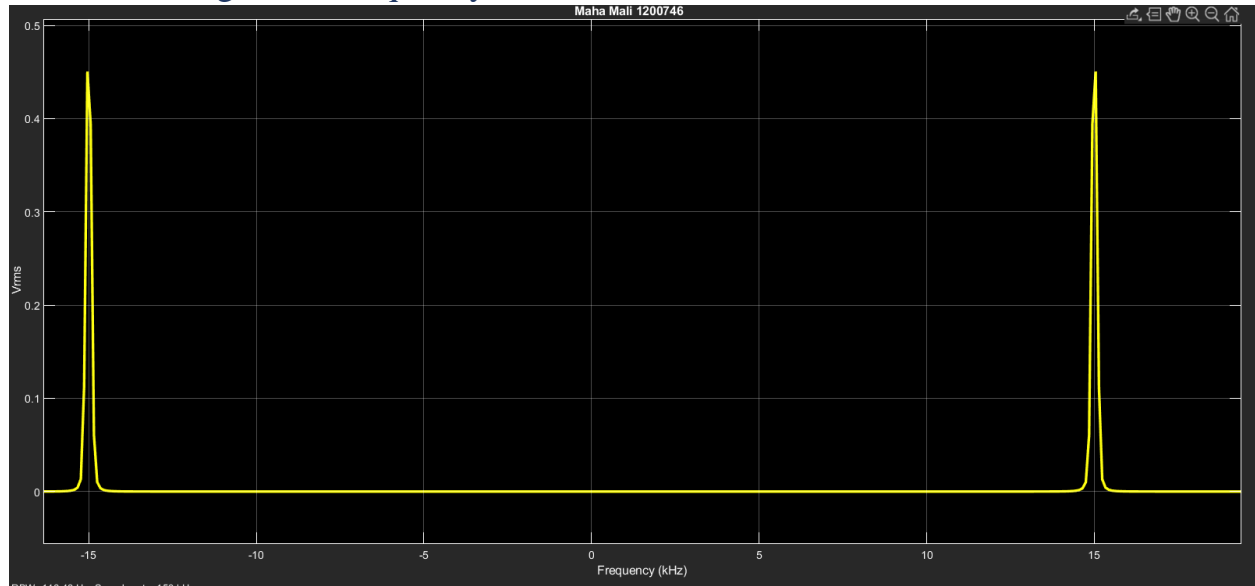


Figure 4: carrier signal in frequency domain

From the graph for the spectrum of carrier signal we notice that there is two delta function one around -15khz, and another one around 15khz.

When ($\mu=1$)

Calculate the value of k_a

$$\mu = k_a \cdot A_m, \text{ given } m(t) = 0.85 \cos(2\pi(1000)t) \text{ so } A_m = 0.85$$

$$k_a = (\mu) / (A_m)$$

$$= (1) / (0.85)$$

$$= 1.1765$$

Mathematical Representation of AM Signal in Time Domain

Given

- $m(t) = 0.85 \cos(2\pi(1000)t)$
- $c(t) = 1 \cos(2\pi(15000)t)$
-

$$s(t) = A_c(1 + K_a m(t)) \cos(2\pi f_c t)$$

$$s(t) = (1)(1 + 1.1765 (0.85 \cos(2\pi(1000)t)) \cos(2\pi(15000)t)$$

Mathematical Representation of AM Signal in Frequency Domain

$$S(f) = (A_c) / 2 [\delta(f - f_c) + \delta(f + f_c)] + ((A_c) (\mu) / 4) [\delta(f - (f_c + f_m)) + \delta(f + (f_c + f_m))] +$$
$$((A_c) (\mu) / 4) [\delta(f - (f_c - f_m)) + \delta(f + (f_c - f_m))]$$

$$= (1) / 2 [\delta(f - 15k) + \delta(f + 15k)] + ((1) (1) / 4) [\delta(f - (16000)) + \delta(f + (16000))] +$$
$$((1) (1) / 4) [\delta(f - (14000)) + \delta(f + (14000))]$$

Build The Diagram When Modulation Index =1 ($\mu=1$) Step by Step

Modulation

The figure below shows the general block diagram for AM modulation we can build it easily by using mathematical representation of AM signal in time domain

$$s(t) = A_c(1 + K_a m(t)) \cos(2\pi f_c t)$$

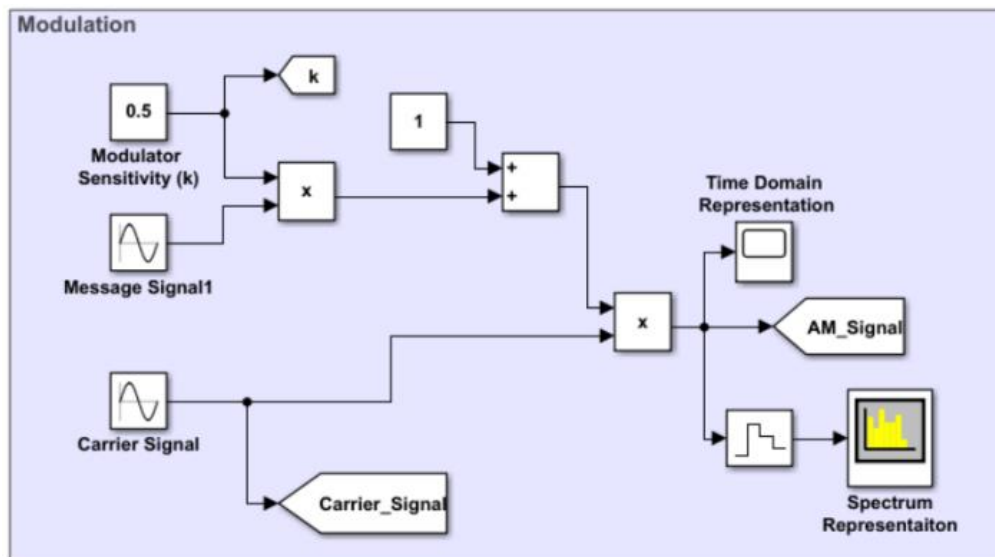


Figure 5: General Modulation

The figure shows the modulation block diagram for $\mu=1$ by using MATLAB

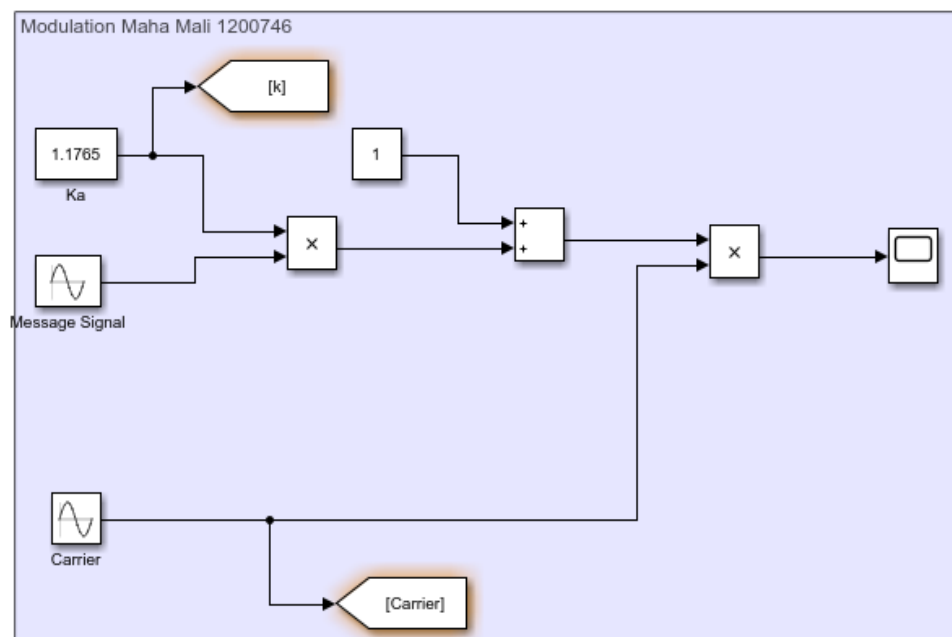


Figure 6: Modulation Block Diagram for $\mu=1$

Amplitude: 0.85

Bias: 0

Frequency (rad/sec): $2\pi \cdot 1000$

Phase (rad): 0

Sample time: 0

☒ Interpret vector parameters as 1-D

OK Cancel Help Apply

Figure 7: properties of $m(t)$

Amplitude: 1

Bias: 0

Frequency (rad/sec): $2\pi \cdot 15000$

Phase (rad): 0

Sample time: 0

☒ Interpret vector parameters as 1-D

OK Cancel Help Apply

Figure 8: properties of $c(t)$

To plot one cycle of $s(t)$ we calculate the periodic time which is:

- Period time = $1/f_m$
 $= 8/1000 = 0.008 \text{ s}$

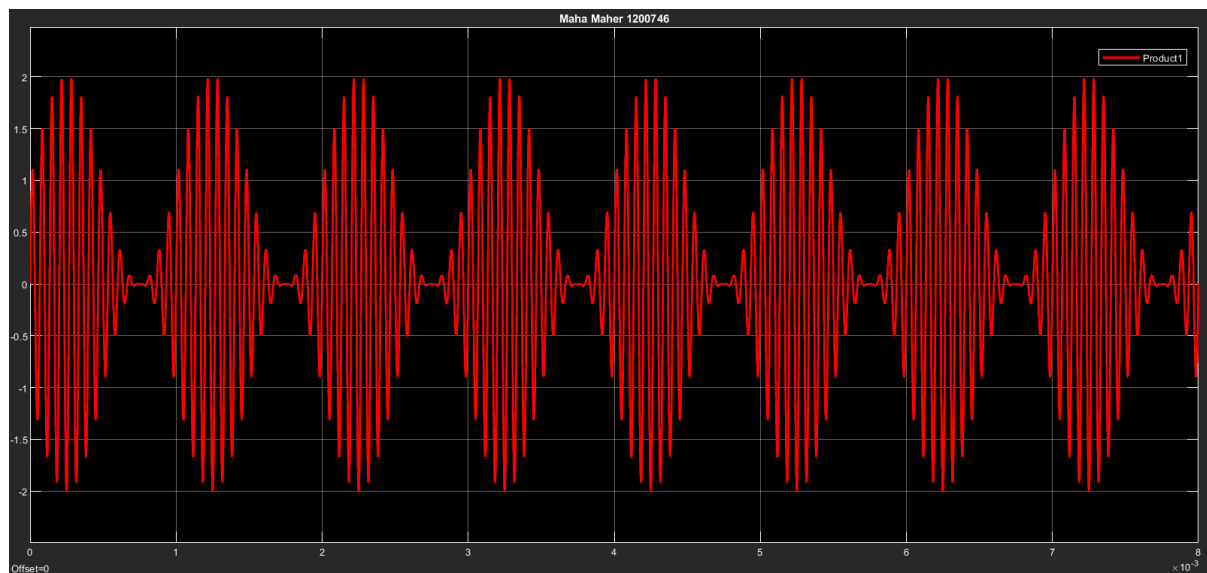


Figure 9: $s(t)$ in time domain

Because of $u = 1$ we notice that the type of modulation is normal.

To plot $s(f)$ we add Zero-order hold and Spectrum analyzer

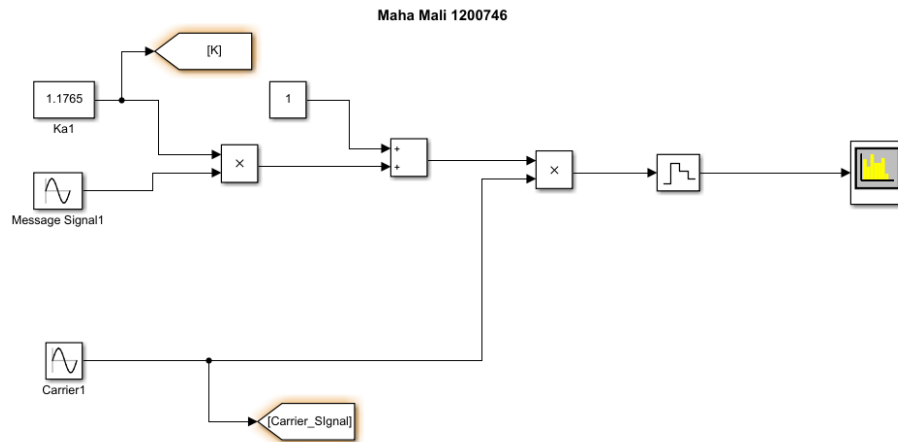


Figure 10: modulation block with spectrum analyzer

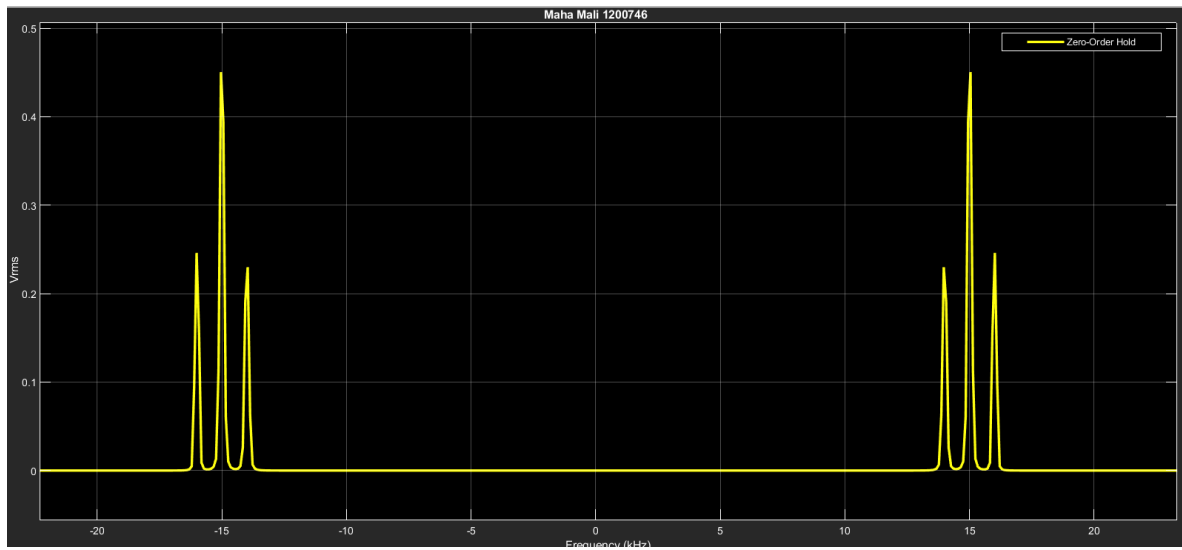


Figure 11: Spectrum for modulated signal ($u=1$)

From the graph of Spectrum, we got almost the same results based on this equation:

$$\begin{aligned}
 S(f) &= (A_c) / 2 [\delta(f - f_c) + \delta(f + f_c)] + ((A_c) (\mu) / 4) [\delta(f - (f_c + f_m)) + \delta(f + (f_c + f_m))] + \\
 &\quad ((A_c) (\mu) / 4) [\delta(f - (f_c - f_m)) + \delta(f + (f_c - f_m))] \\
 &= (1) / 2 [\delta(f - 15k) + \delta(f + 15k)] + ((1) (1) / 4) [\delta(f - (16000)) + \delta(f + (16000))] + \\
 &\quad ((1) (1) / 4) [\delta(f - (14000)) + \delta(f + (14000))]
 \end{aligned}$$

Demodulation

Coherent demodulation

The figure below shows the general block diagram for AM Coherent demodulation we can build it easily by using this formula:

$$s(t)_{de} = c(t) * s(t)$$

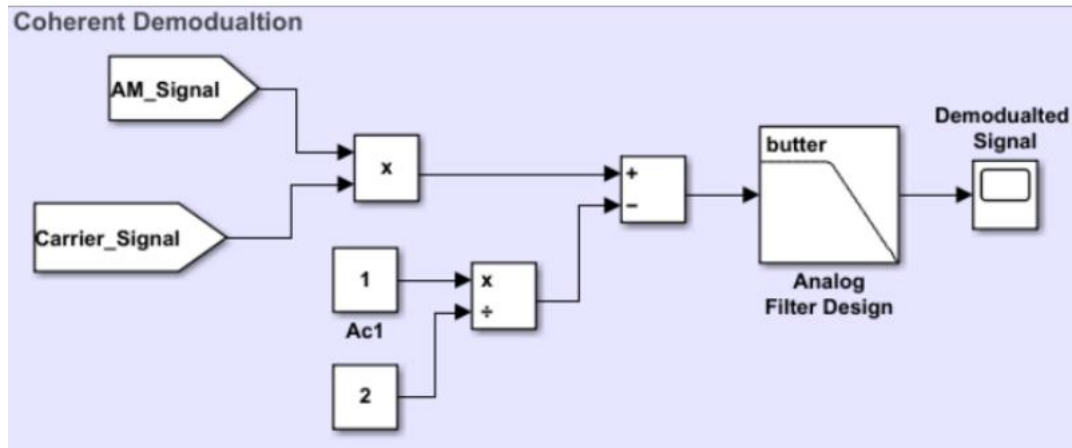


Figure 12: General Coherent Demodulation

$$\begin{aligned} s(t)_{de} &= (\cos(2\pi(15k)t)) (\cos(2\pi(15k)t) + 0.5 \cos(2\pi(16k)t) + 0.5 \cos(2\pi(14k)t)) \\ &= 0.5 \cos(2\pi(30k)t) + 0.5 \cos(0) + 0.25 \cos(2\pi(31k)t) + 0.25 \cos(2\pi(1k)t) + 0.25 \\ &\quad \cos(2\pi(29k)t) + 0.25 \cos(2\pi(1k)t) \end{aligned}$$

The figure 13 shows the build of modulation block diagram for $\mu=1$ by using MATLAB:

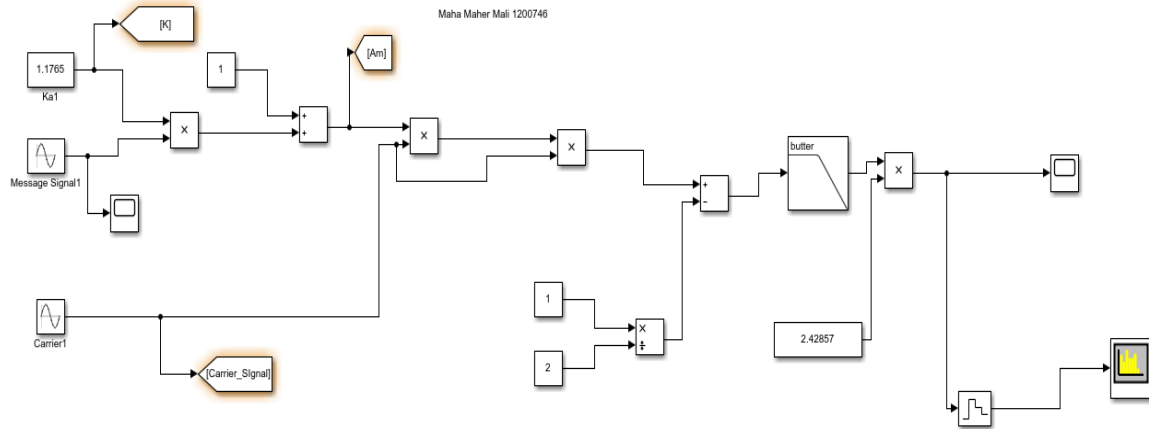


Figure 13: Demodulation Block Diagram for $\mu=1$

Due to the difficulty in controlling the gain value of the filter, the filter output was multiplied by a factor of 2.429 to obtain the signal amplitude that corresponds to the original amplitude of 0.85.

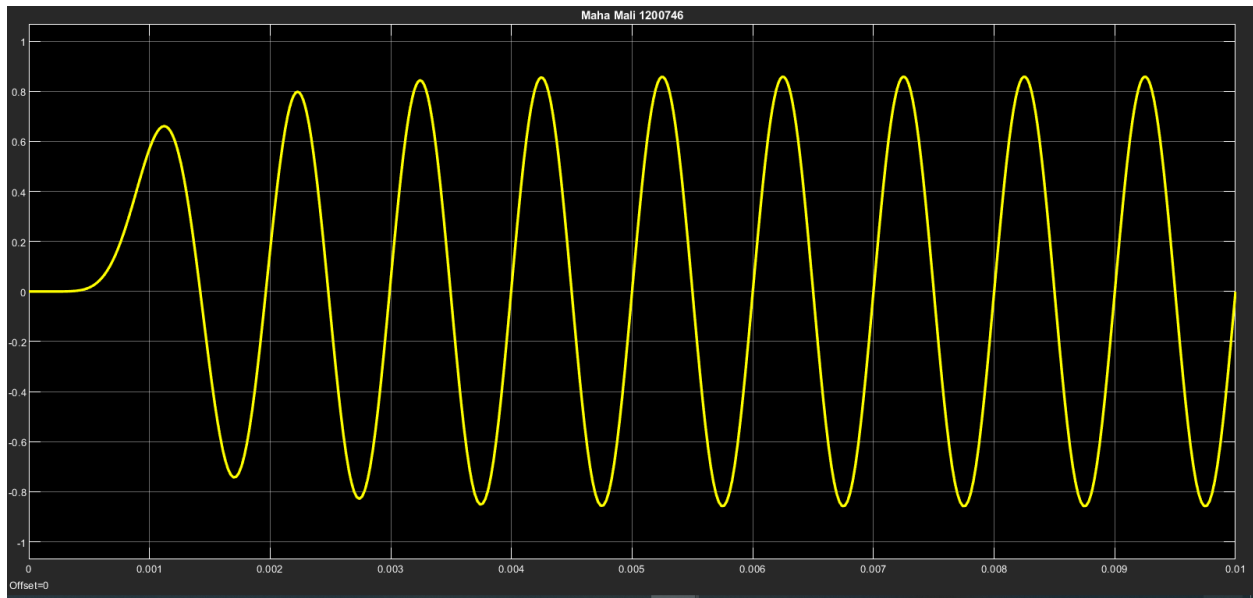


Figure 14: coherent demodulation output in time domain

As we see in the figure below, the output of the demodulation process is equal to the message signal. that's mean that we got the message signal after demodulation.

$$m(t) = 0.85 (2 \pi (1000) t)$$

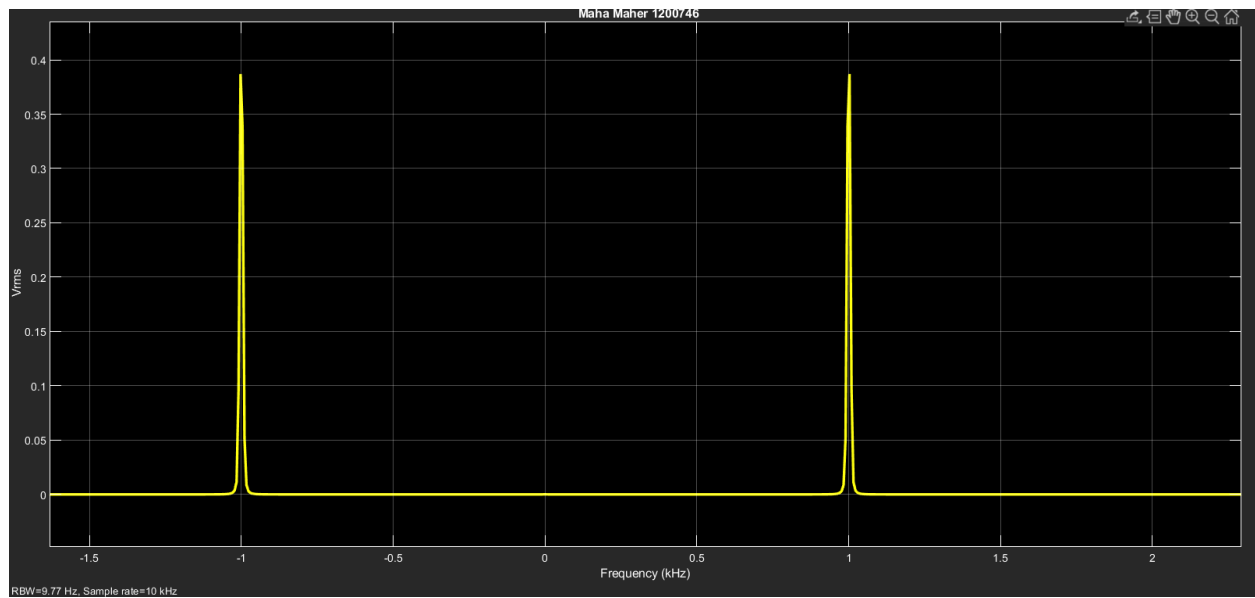


Figure 15: coherent demodulation output in frequency domain

Envelope detector demodulation

The figure below shows the general block diagram for AM Envelope detector demodulation

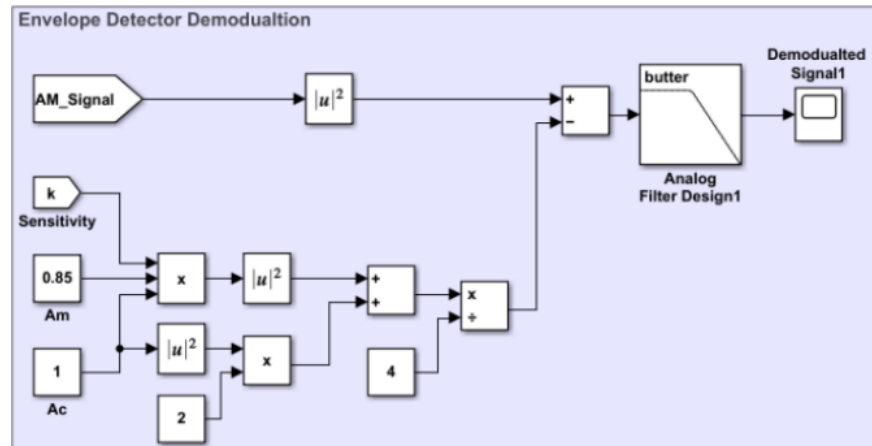
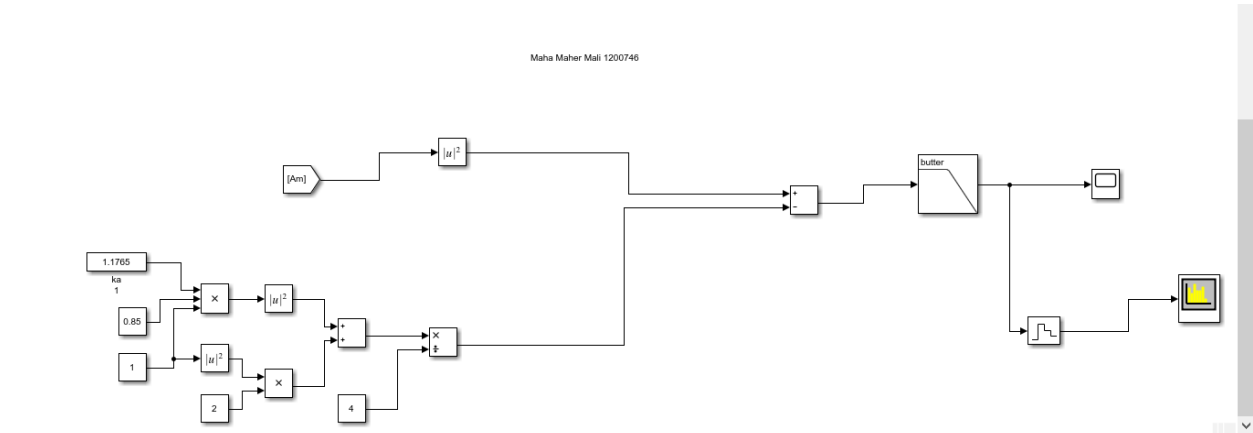


Figure 16: Envelope detector demodulation general formula

now we should build the modulation block diagram for $\mu=1$ by using MATLAB:



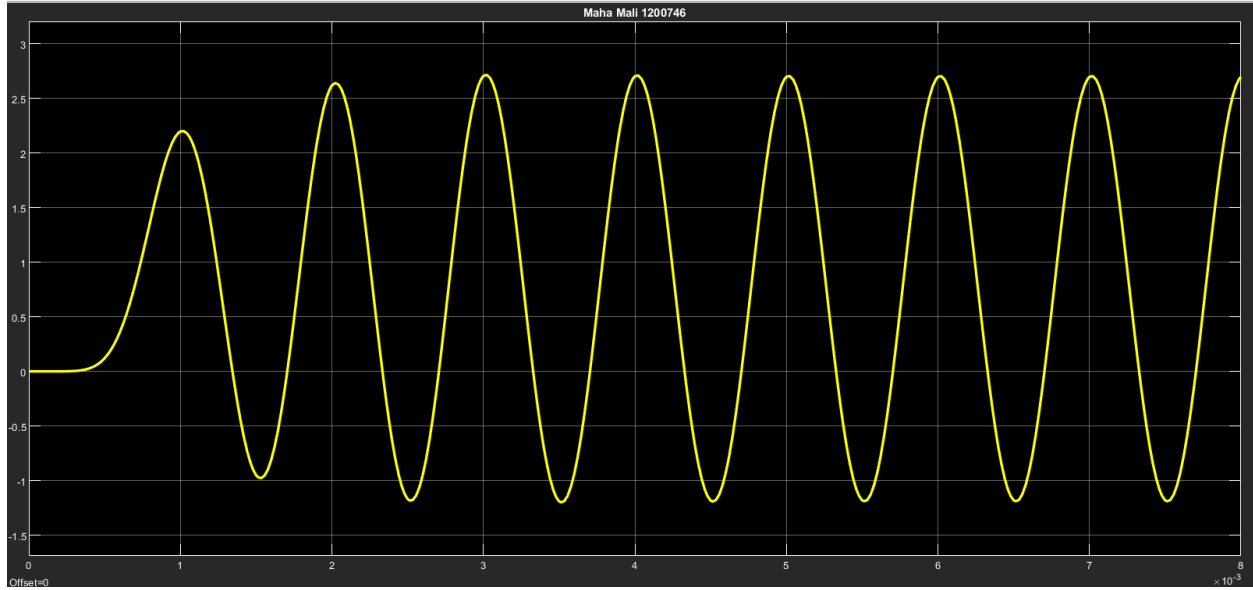


Figure 17: Envelope detector demodulation output in time domain

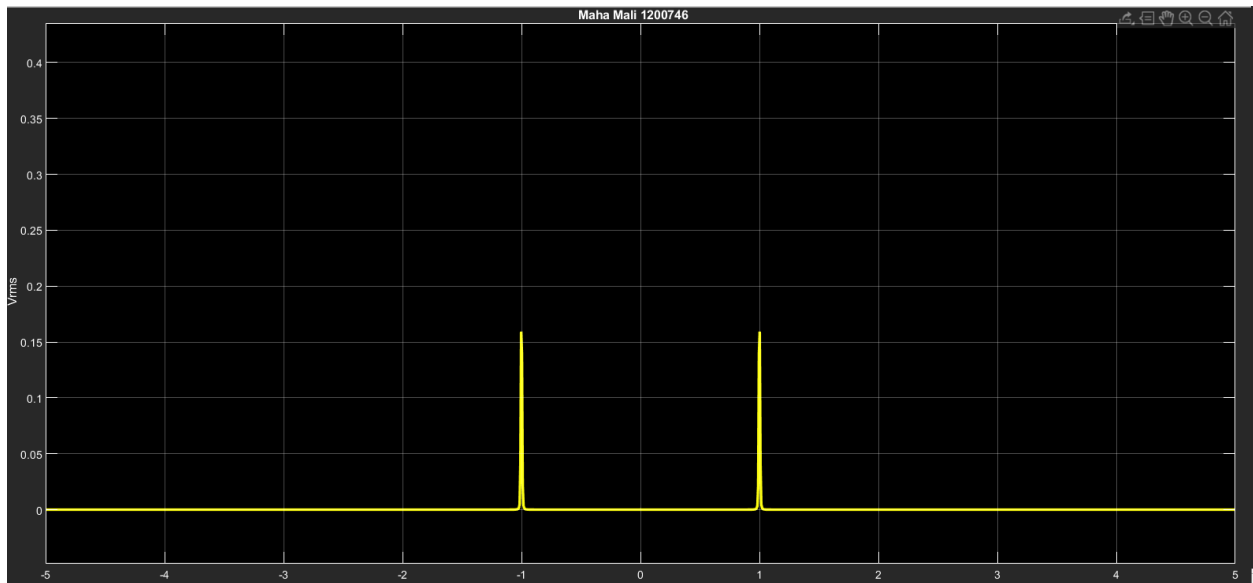


Figure 18: Envelope detector demodulation output in frequency domain

When ($\mu=0.5$)

Calculate the value of k_a

$$\mu = k_a \cdot A_m, \text{ given } m(t) = 0.85 \cos(2\pi(1000)t) \text{ so } A_m=0.85$$

$$k_a = (\mu) / (A_m)$$

$$= (0.5) / (0.85)$$

$$= 0.588$$

Mathematical Representation of AM Signal in Time Domain

Given

- $m(t) = 0.85 \cos(2\pi(1000)t)$
- $c(t) = 1 \cos(2\pi(15000)t)$
-

$$s(t) = A_c(1 + K_a m(t)) \cos(2\pi f_c t)$$

$$s(t) = (1)(1 + 0.588(0.85 \cos(2\pi(1000)t))) \cos(2\pi(15000)t)$$

Build The Diagram When Modulation Index =0.5 ($\mu=0.5$) Step by Step Modulation

The figure shows the modulation block diagram for $\mu=0.5$ by using MATLAB

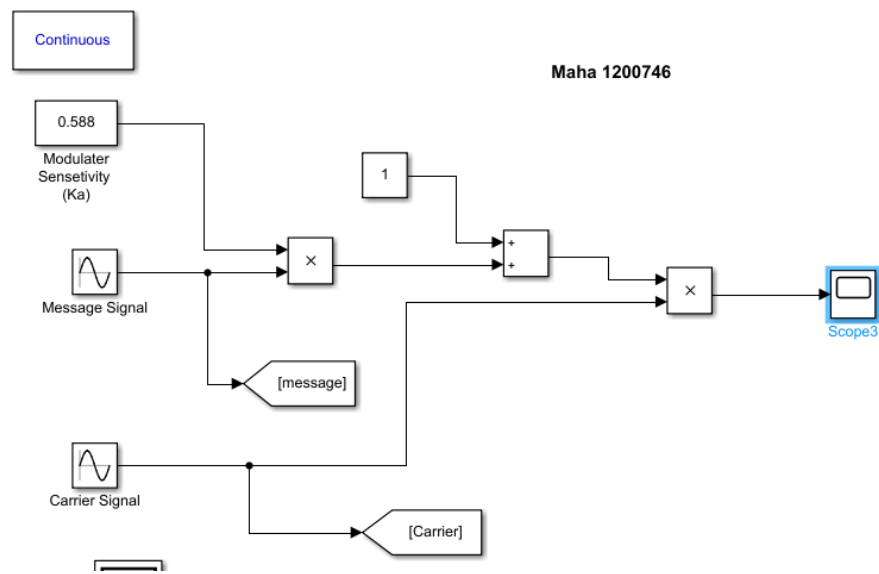


Figure 19: block diagram for case 2 ($u=0.5$)

To plot five cycle of $s(t)$ we calculate the periodic time which is:

- Period time = $1/f_m$
 $= 5/1000$

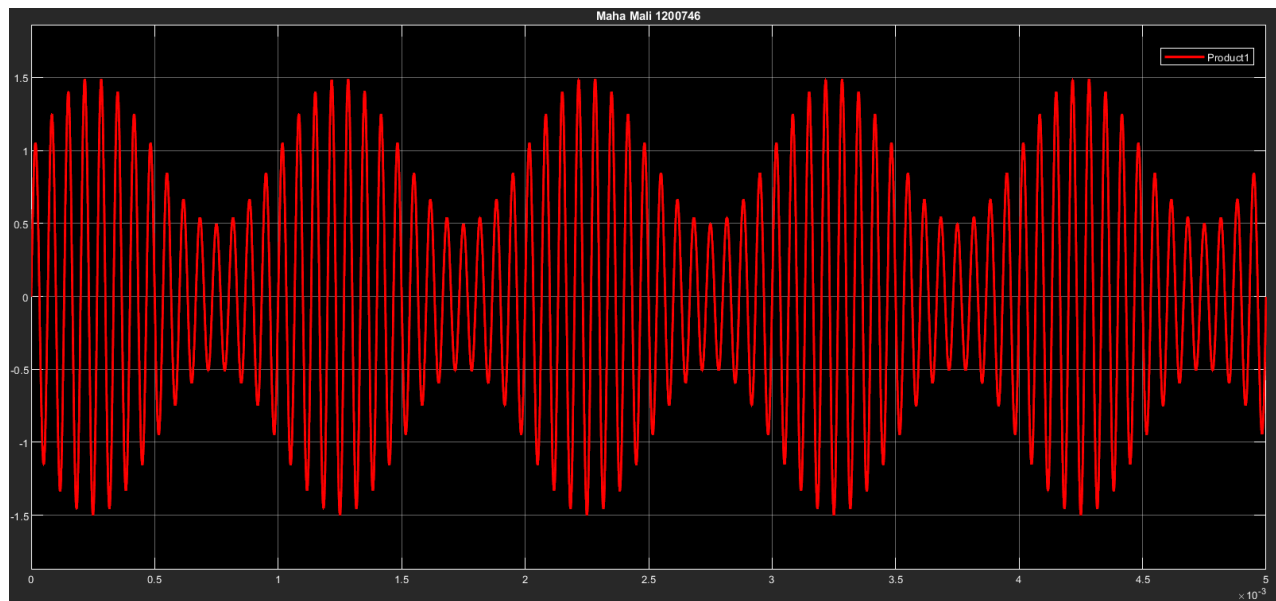


Figure 20: $s(t)$ in time domine

Because of $\mu=0.5$ we notice that the type of modulation is under modulation.

To plot $s(f)$ we add Zero-order hold and Spectrum analyzer

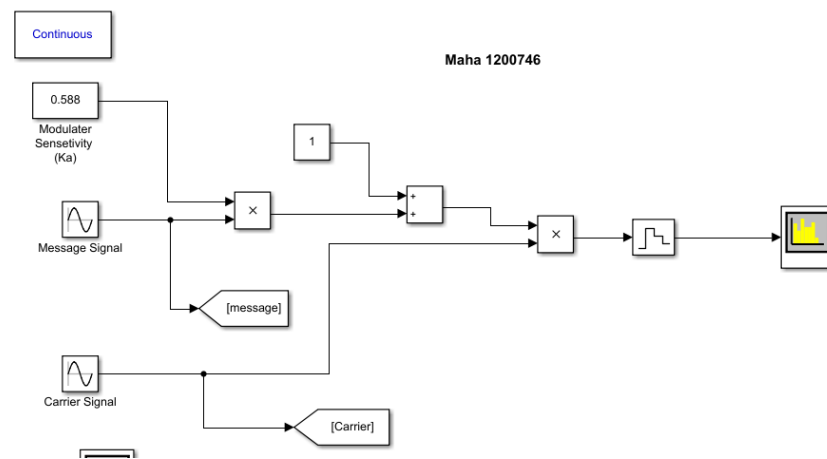


Figure 21: diagram to plot spectrum

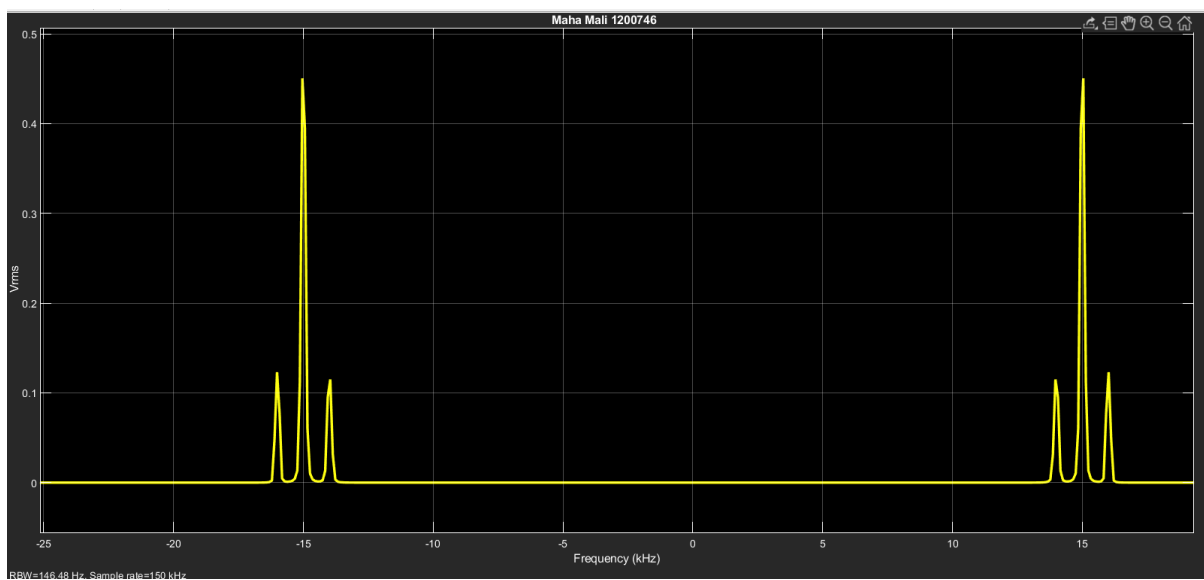


Figure 22: Spectrum for modulated signal ($u=0.5$)

Demodulation

Coherent demodulation

The figure shows the build of modulation block diagram for $\mu=1$ by using MATLAB:

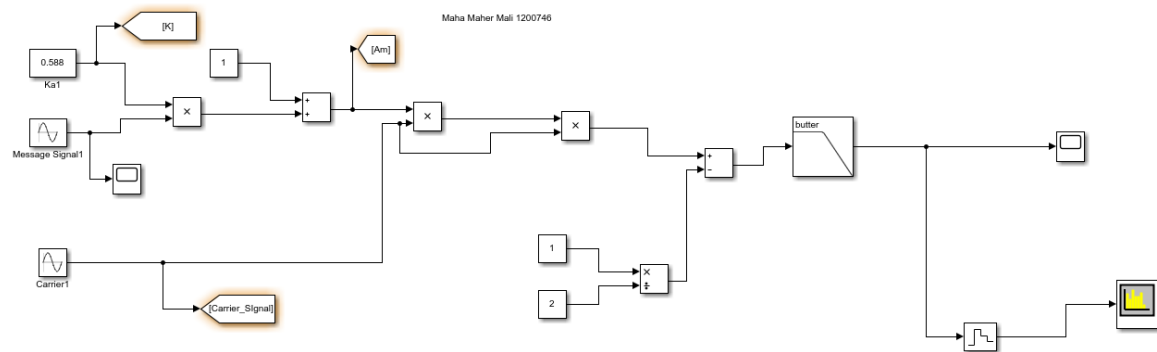


Figure 23: Coherent demodulation block diagram

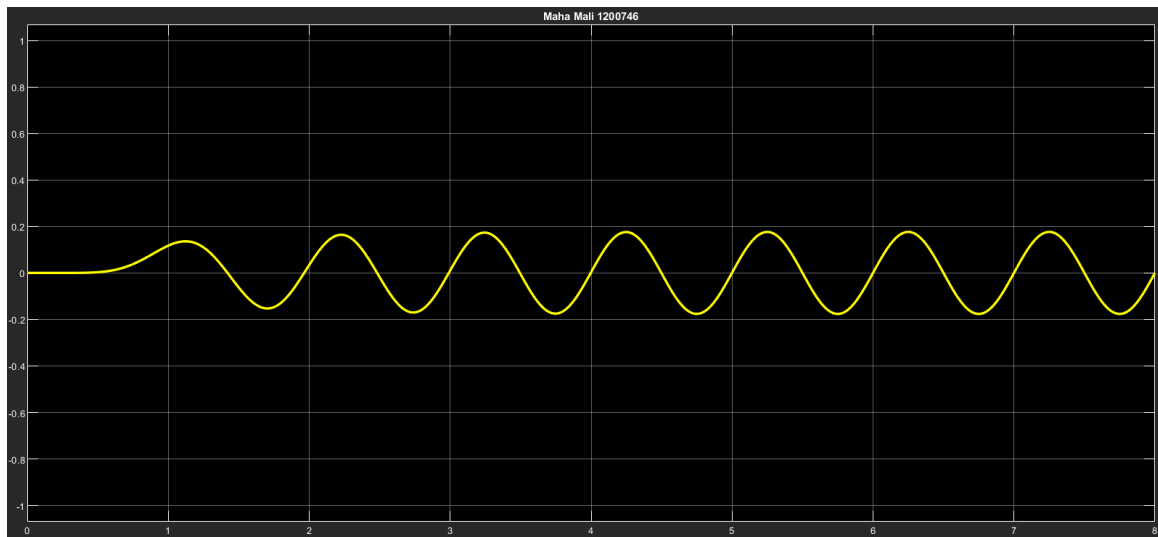


Figure 24: Coherent demodulation in time domine

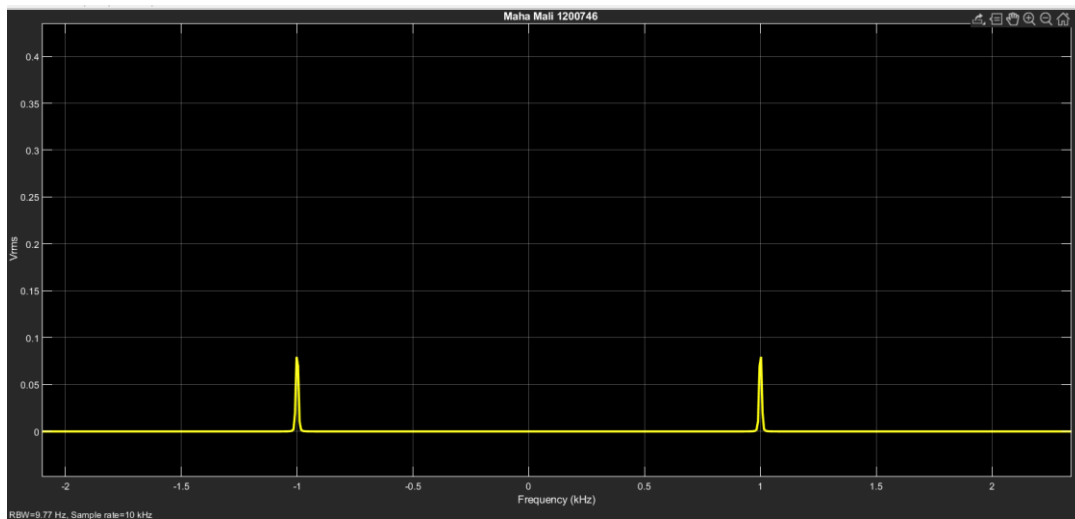


Figure 25: Coherent demodulation in frequency domine

Envelope detector demodulation

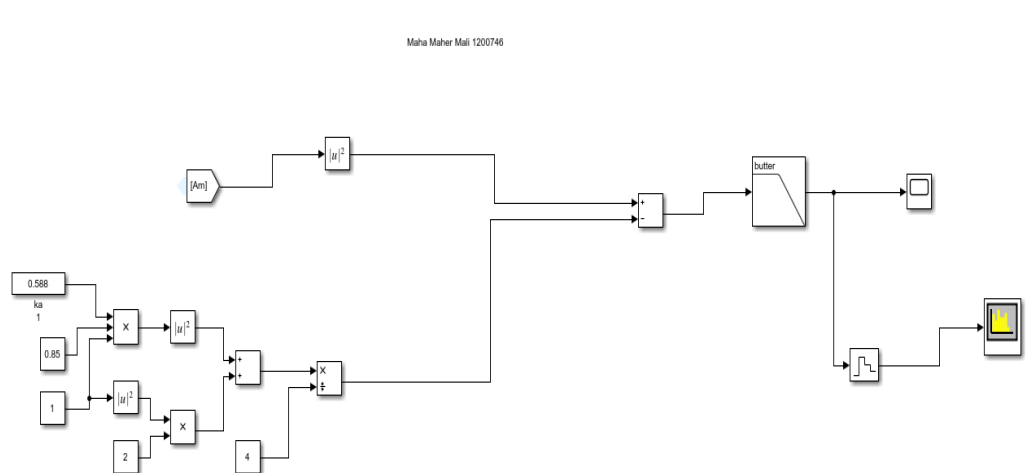


Figure 26: Envelope detector demodulation block digram when ($u=0.5$)



Figure 27: Envelope detector demodulation in time domine

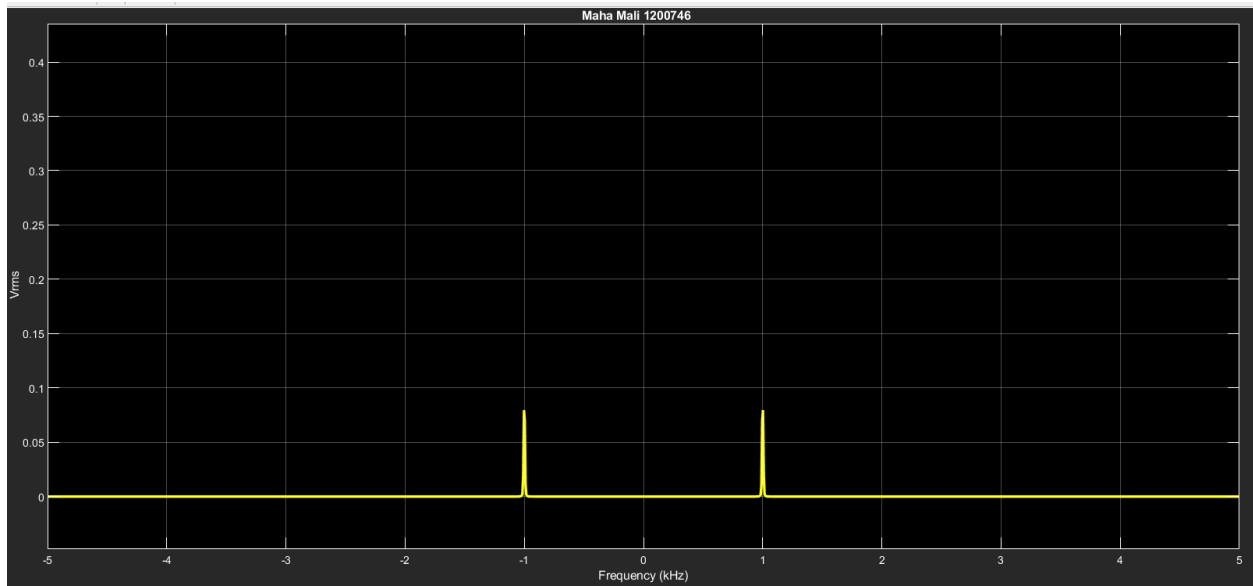


Figure 28: Envelope detector demodulation in freqancy domine

When ($\mu=1.5$)

Calculate the value of k_a

$$\mu = k_a \cdot A_m, \text{ given } m(t) = 0.85 \cos(2\pi(1000)t) \text{ so } A_m=0.85$$

$$k_a = (\mu) / (A_m)$$

$$= (1.5) / (0.85)$$

$$= 1.765$$

Mathematical Representation of AM Signal in Time Domain

Given

- $m(t) = 0.85 \cos(2\pi(1000)t)$
- $c(t) = 1 \cos(2\pi(15000)t)$

$$s(t) = A_c(1 + K_a m(t)) \cos(2\pi f_c t)$$

$$s(t) = (1)(1 + 0.588 (1.765 \cos(2\pi(1000)t)) \cos(2\pi(15000)t)$$

Build The Diagram When Modulation Index =0.5 ($\mu=0.5$) Step by Step Modulation

The figure shows the modulation block diagram for $\mu=1.5$ by using MATLAB

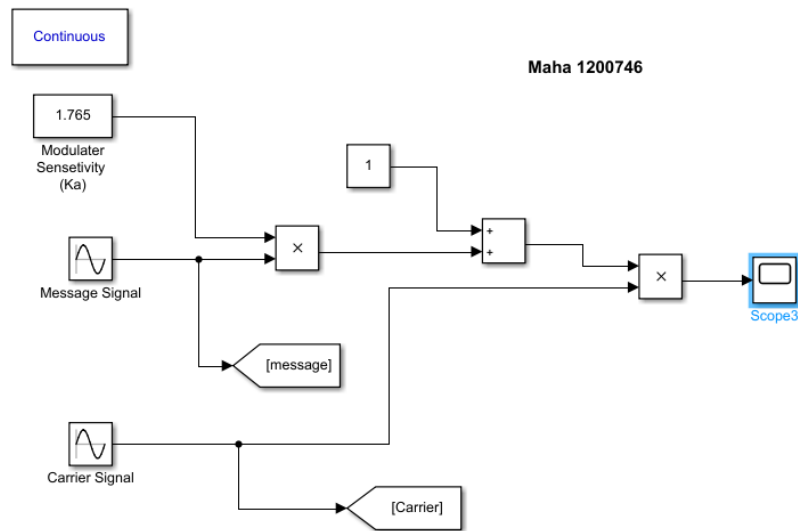


Figure 29: Block diagram for $\mu=1.5$

To plot five cycle of $s(t)$ we calculate the periodic time which is:

- Period time = $1/f_m$
 $= 5/1000$

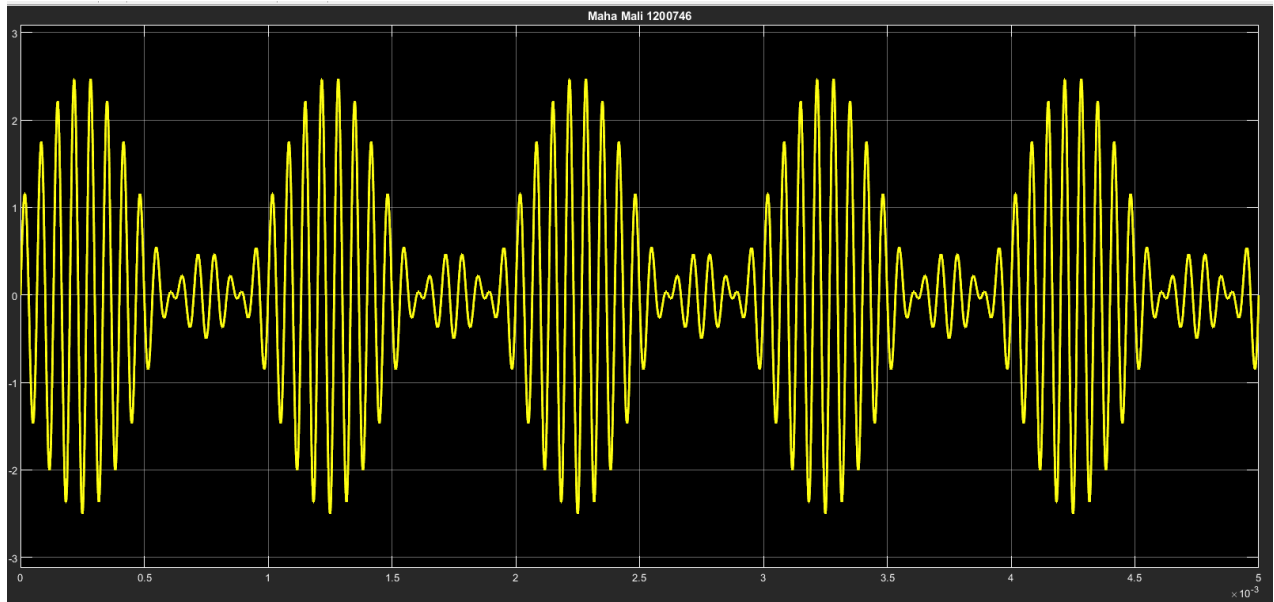
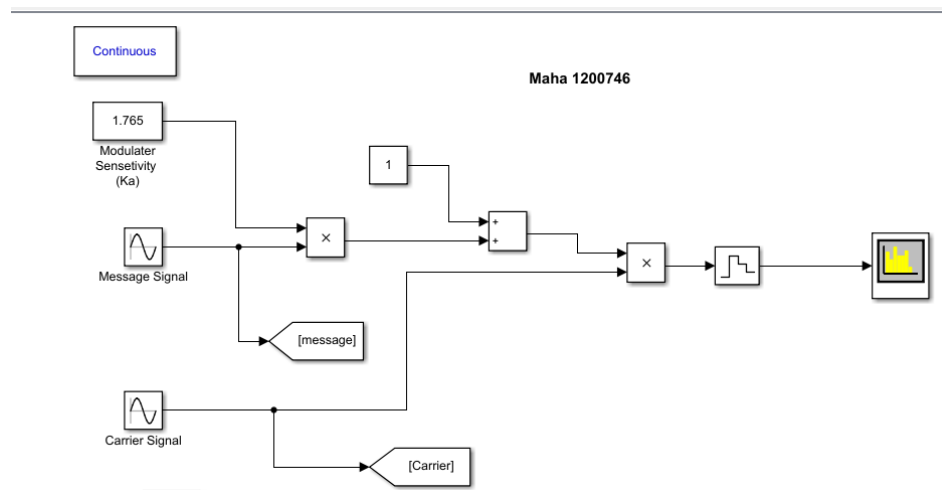


Figure 30 : $s(t)$ in time domine

Because of $\mu=1.5$ we notice that the type of modulation is over modulation.

To plot $s(f)$ we add Zero-order hold and Spectrum analyzer



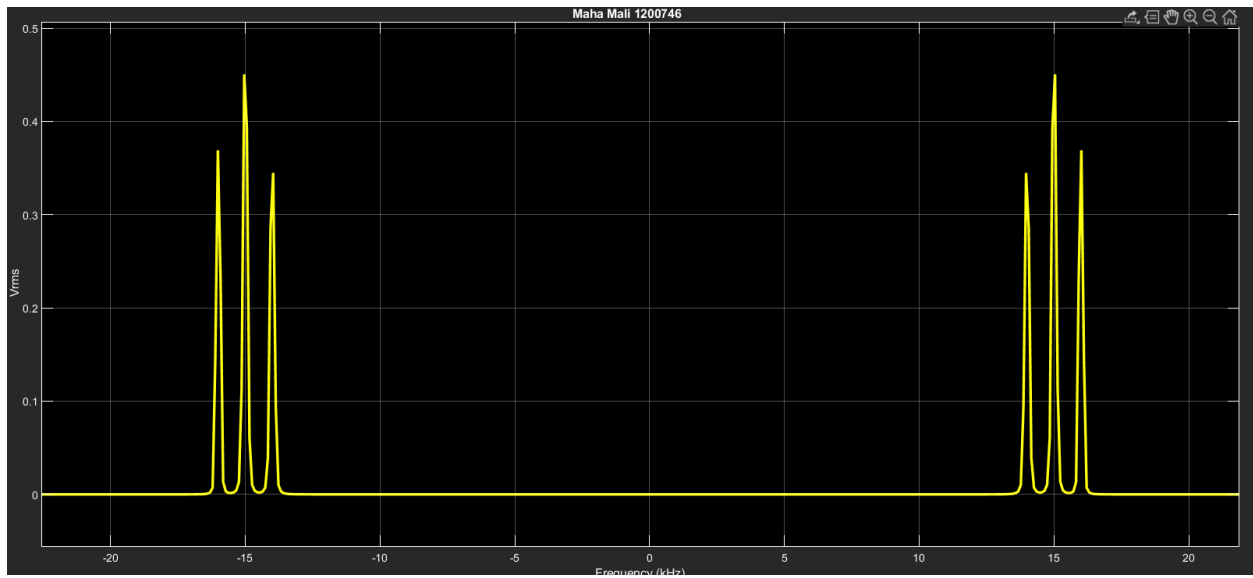


Figure 31:s(f) in frequency domine

Demodulation

Coherent demodulation

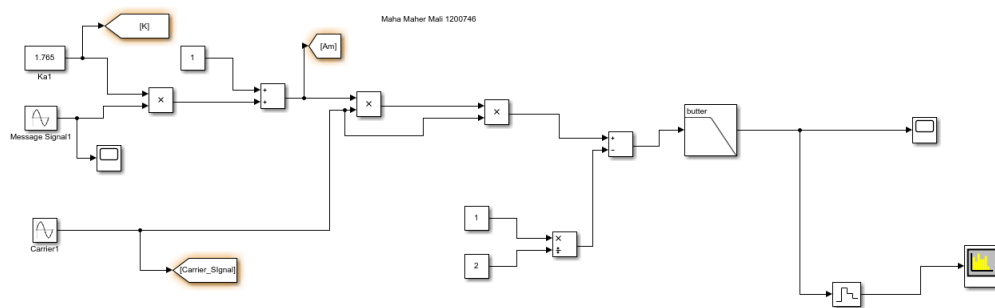


Figure 32: Coherent demodulation block digram

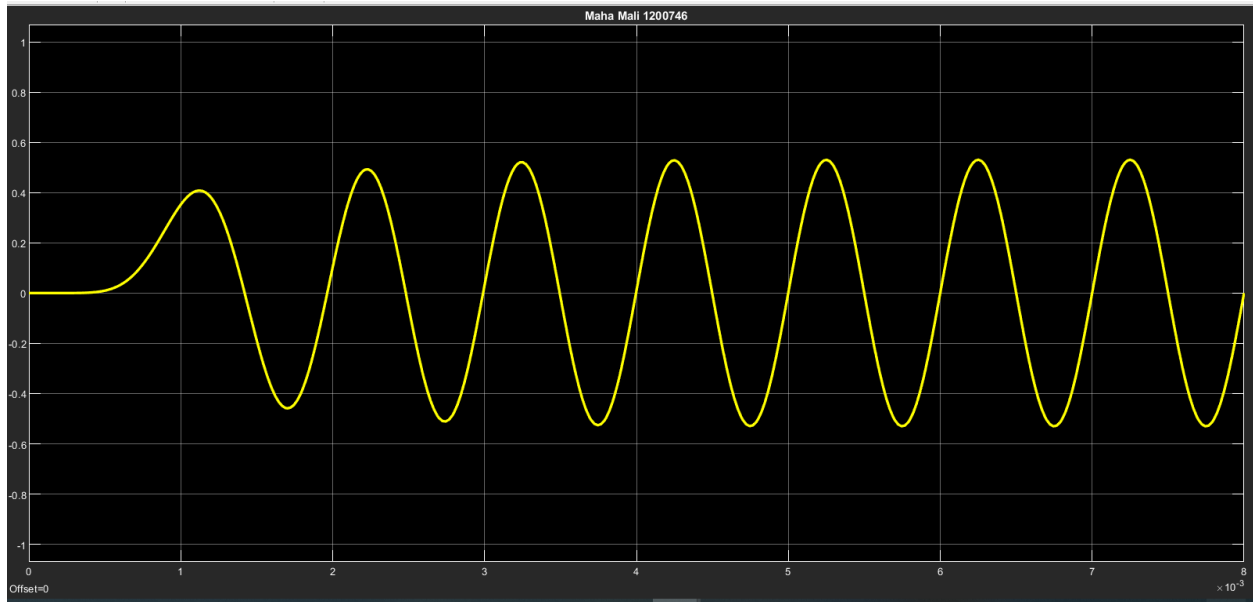


Figure 33: $s(t)$ in time domine

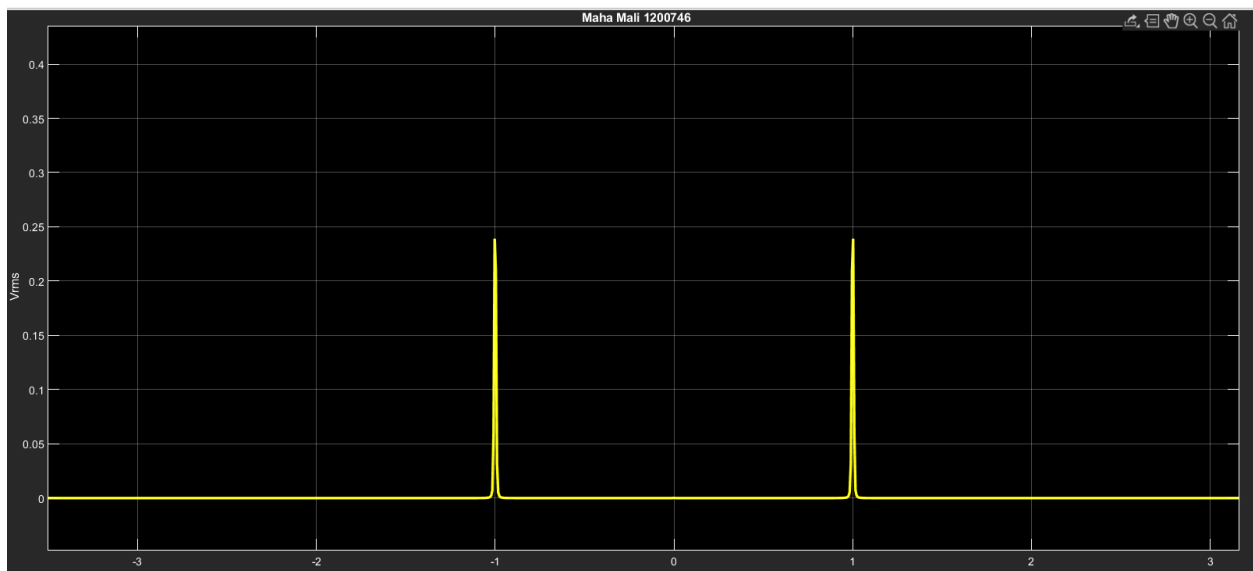


Figure 34: $s(F)$ in frequency domine

Envelope detector demodulation

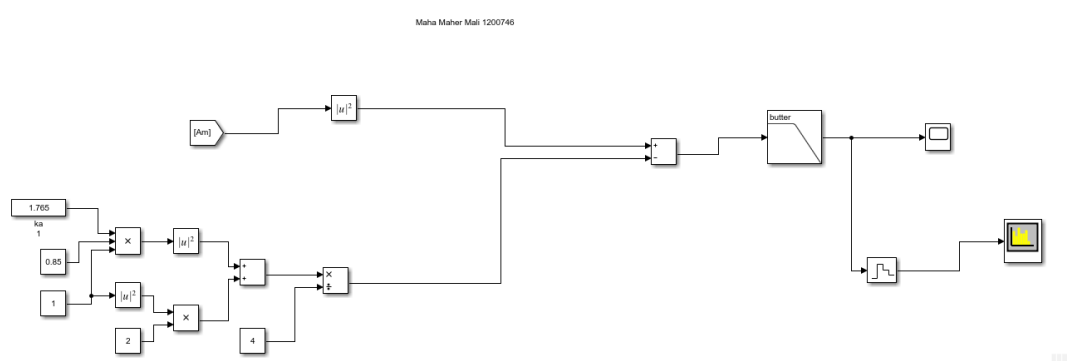


Figure 35: Envelope detector demodulation

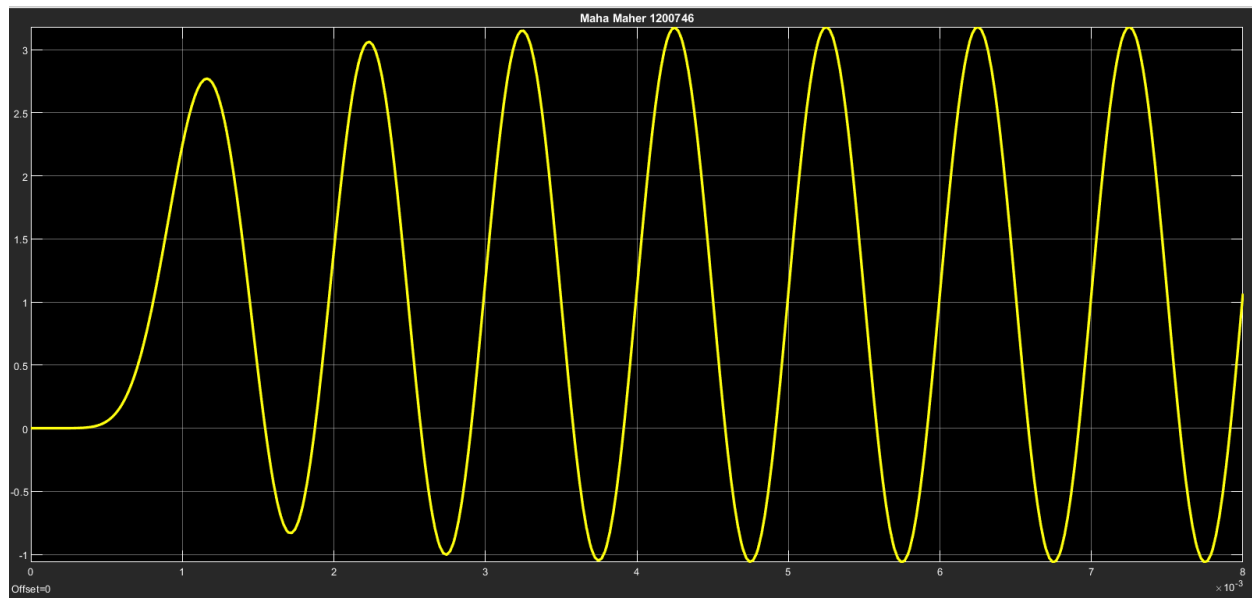


Figure 36: $s(t)$ in time domine

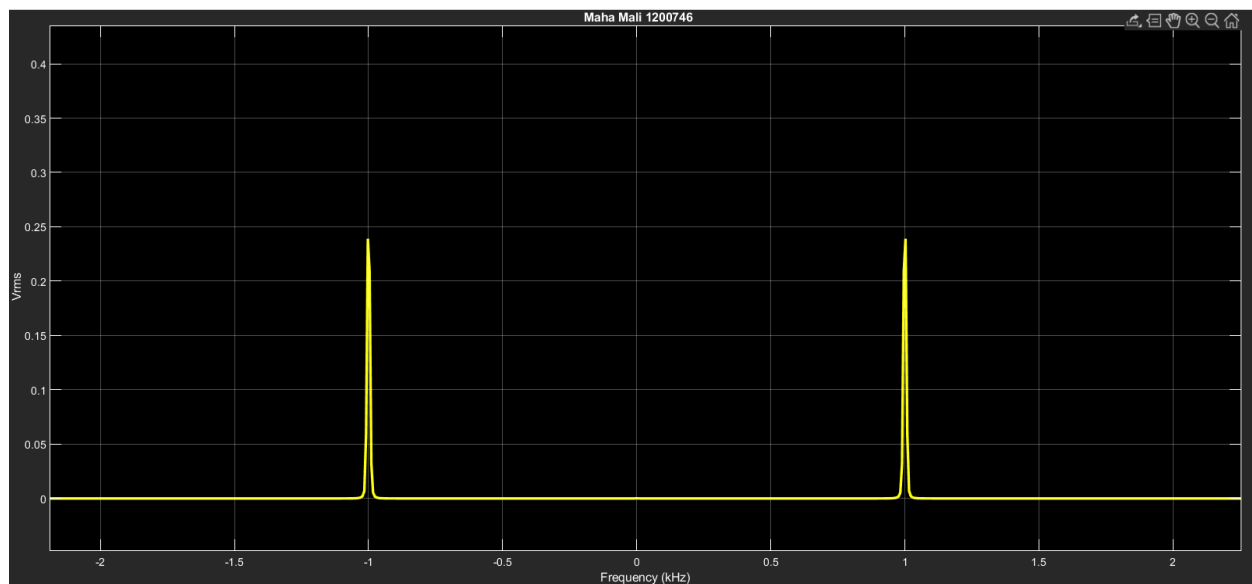


Figure 37: $s(f)$ in frequency domine

References

- [1] <https://uotechnology.edu.iq/dep/coe/lectures/Analog%20Communication%20%20Systems%20I-pdf/3.%20Amplitude%20Modulation%20Systems.pdf>
- [2] <https://reviseomatic.org/help/2-modulation/Amplitude%20Modulation.php>
- [3] <https://byjus.com/physics/modulation-and-demodulation/>