



**Faculty of Engineering & Technology Electrical & Computer
Engineering Department**

Communication Lab - ENEE4113

Experiment 4: Frequency Modulation

Prelab #3

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Software Prelab (Simulink MATLAB)

Extract the message signal $m(t)$ from $s(t)$

General form about $s_{FM}(t)$:

$$s_{FM}(t) = A_c \cos(2\pi f_c t + 2\pi K_f \int_0^t m(t) dt)$$

(*) To extract $m(t)$ from $s(t)$ we need to differentiate $s(t)$

$$\frac{d s_{FM}(t)}{dt} = -A_c \sin(2\pi f_c t + 2\pi K_f \int_0^t m(t) dt) \times (2\pi f_c + 2\pi K_f m(t))$$

⇒ [2] Differentiate $s(t)$

$$\frac{d s_{FM}(t)}{dt} = -A_c (2\pi f_c + 2\pi K_f m(t)) \sin(2\pi f_c t + 2\pi K_f \int_0^t m(t) dt)$$

⇒ Now we need envelope detector to get $m(t)$

[3] using envelope detector

$\hat{s}_{FM}(t) \rightarrow$ Envelope Detector $\rightarrow y(t) \approx m(t)$

$$y(t) = A_c (2\pi f_c + 2\pi K_f m(t))$$

$$y(t) = 2\pi f_c A_c + 2\pi A_c K_f m(t) \Rightarrow \text{after envelope detection}$$

We need to canceling dc value using Capacitor

$y(t) \rightarrow \frac{1}{s} \rightarrow r(t) \rightarrow$ extracting $m(t)$ $\Rightarrow r(t) = y(t) - \text{DC value}$

$$r(t) = 2\pi A_c K_f m(t)$$

Output $r(t)$ is proportional to $m(t)$

Figure 1: Steps to Extract the message signal $m(t)$ from $s(t)$

The figure shows the calculation to find the message signal:

$$s(t) = \cos(2\pi(20K)t) + \frac{6}{B} \sin(1000\pi t)$$

$$B = \frac{K_f A_m}{f_m} \quad \rightarrow \quad A_m = 1 \text{ by Assumption}$$

$$f_m = 500 \text{ Hz}$$

$$B = 6$$

$$6 = \frac{K_f \cdot 1}{500}$$

$$K_f = 3000$$

$$m(t) = 1 \cos(1000\pi t) \quad \text{when } K_f = 3000 \text{ and } A_m = 1 \text{ by Assumption}$$

Figure 2: Message Signal

Plot 5 cycle from Message signal $m(t)$ and $s(t)$

Block Diagram

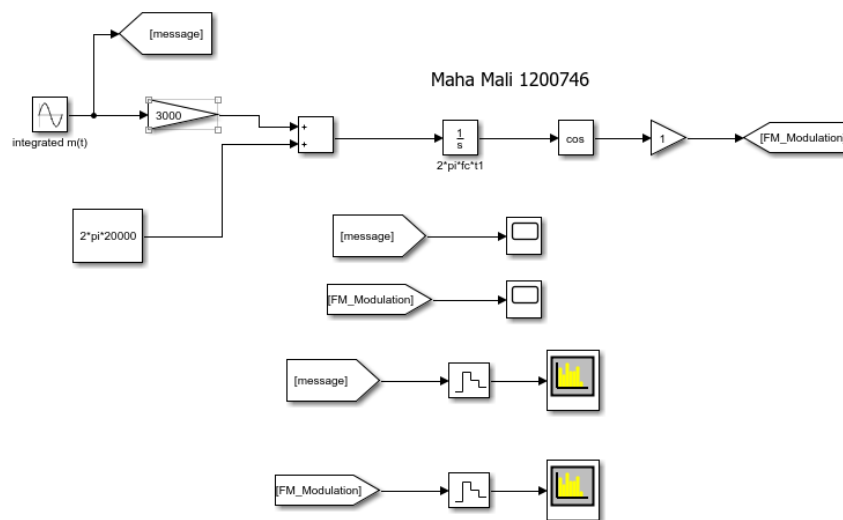


Figure 3: FM Modulation Block Diagram

Message Signal Time Domine

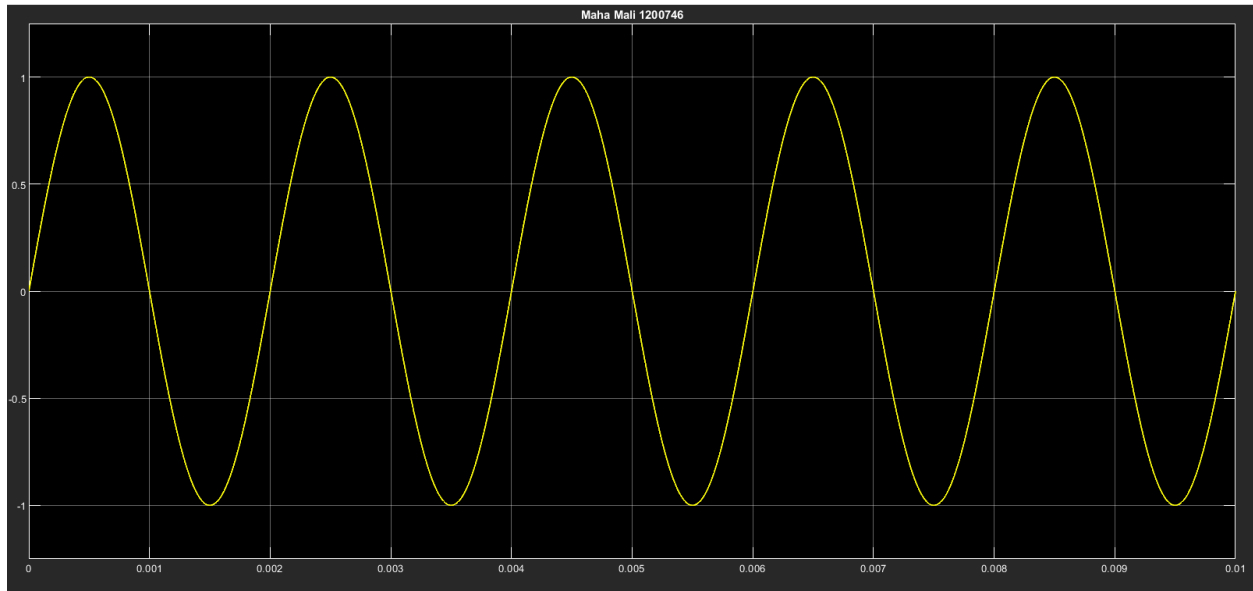


Figure 4: Message Signal in Time domine

From this graph we notice that we got the $m(t)$ that we calculate it by hand with amplitude 1 .

Frequency Domine

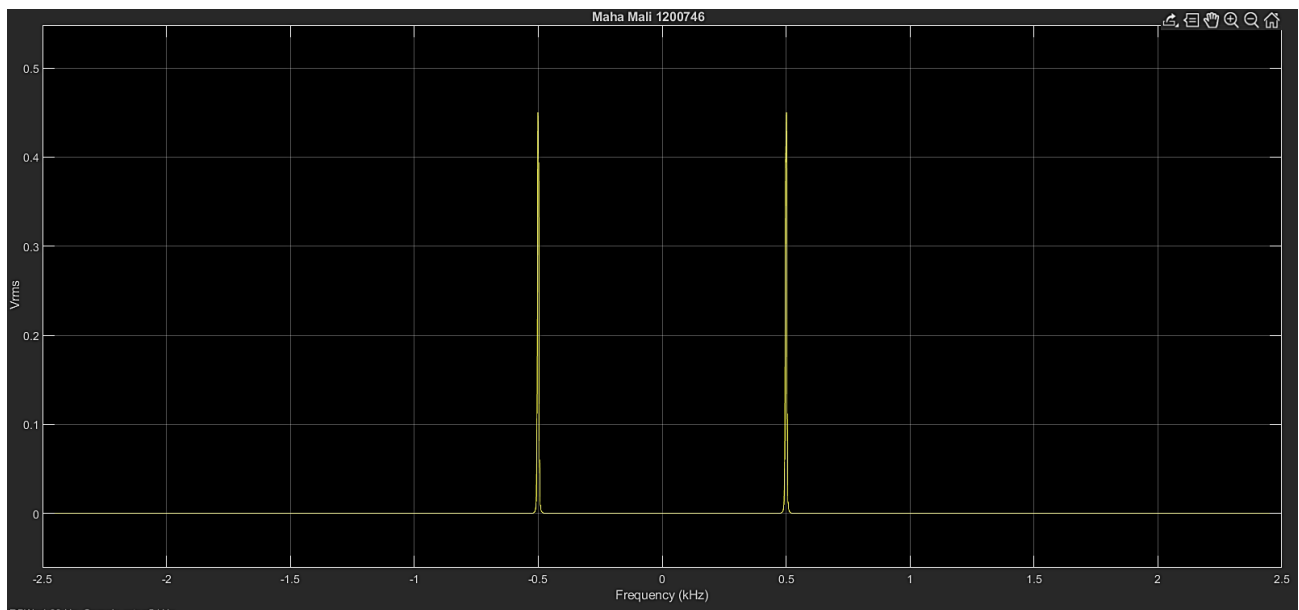


Figure 5: Frequency Domine

$$M(t) = 1\cos(1000\pi t)$$

$$M(f) = \frac{1}{2}\delta(f - 500) + \frac{1}{2}\delta(f + 500)$$

The figure 5 show that we have two delta one at 500 Hz, and another on -500 Hz , according the equation for m(f).

Modulated signal s(t)

Time Domine



Figure 6: Modulated signal In Time Domine

Frequency Domine

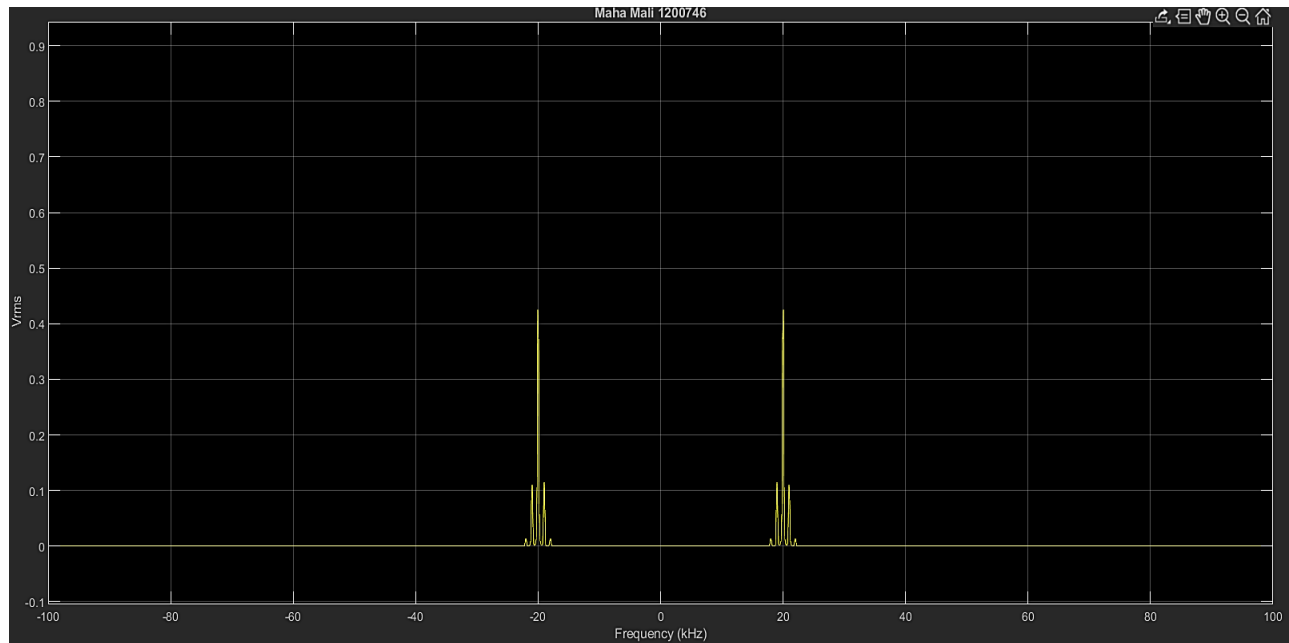


Figure 7: Modulated signal in frequency Domine

Differentiate $s(t)$ with respect to t and plot $ds(t)/dt$ By Hand Solution

General form about $s_{FM}(t)$:

$$s_{FM}(t) = A_c \cos\left(2\pi f_c t + 2\pi K_f \int_0^t m(\tau) d\tau\right)$$

(*) To extract $m(t)$ from $s(t)$ we need to differentiate $s(t)$

$$\frac{ds_{FM}(t)}{dt} = -A_c \sin\left(2\pi f_c t + 2\pi K_f \int_0^t m(\tau) d\tau\right) \cdot (2\pi f_c + 2\pi K_f m(t))$$

⇒ (2) Differentiate $s(t)$

$$\frac{ds_{FM}(t)}{dt} = -A_c (2\pi f_c + 2\pi K_f m(t)) \sin\left(2\pi f_c t + 2\pi K_f \int_0^t m(\tau) d\tau\right)$$

⇒ Now we need envelope detector to get $m(t)$

(3) Using envelope detector

$$s_{FM}(t) \xrightarrow{\text{Envelope Detector}} y(t) \propto m(t)$$

$$y(t) = A_c (2\pi f_c + 2\pi K_f m(t))$$

$$y(t) = 2\pi f_c A_c + 2\pi A_c K_f m(t) \rightarrow \text{after envelope detection}$$

We need to cancel DC value using Capacitor

$$y(t) \xrightarrow{\text{Capacitor}} r(t) \Rightarrow r(t) = y(t) - \text{DC Value}$$

$$\text{extracting } m(t) \quad r(t) = 2\pi A_c K_f m(t) - \text{DC}$$

$$r(t) = 2\pi A_c K_f m(t)$$

Output $r(t)$ is proportional to $m(t)$

$$\frac{ds(t)}{dt} = -\sin(2\pi(20k)t + 6\sin(1000\pi t)) \cdot (2\pi 20k) + 6\cos(1000\pi t) \cdot 1000\pi$$

Figure 8: Differentiate $s(t)$

The differentiation of function $s(t)$ unveils a transition from a rapidly changing frequency modulation (FM) waveform to a slower amplitude modulation (AM) pattern. The original FM waveform, characterized by a 20,000 Hz carrier frequency and modulation, evolves into the

derivative waveform $ds(t)/dt$. This shift from FM to AM-like behavior is a result of differentiation's emphasis on higher frequencies and its impact on reshaping signal traits

Using Simulink

Block Diagram

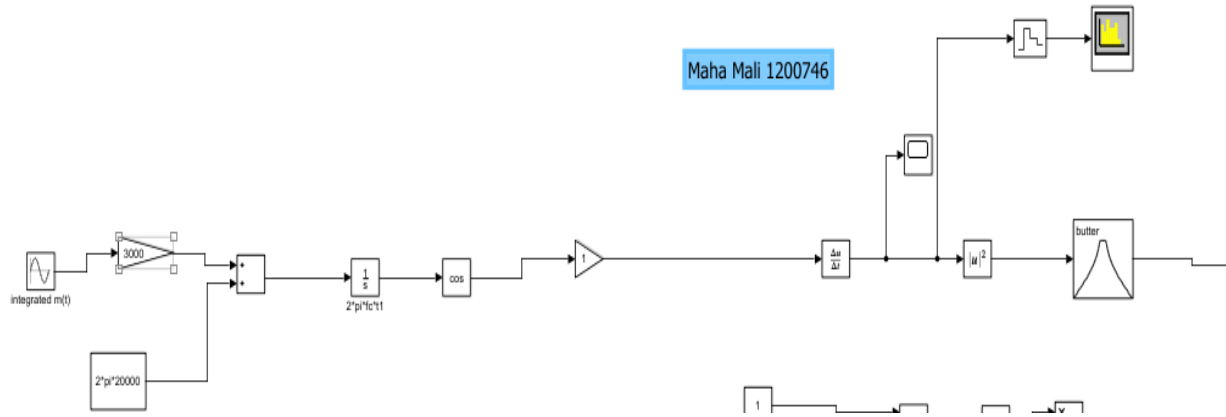


Figure 9: Block Diagram to Differentiate $s(t)$

Time domine

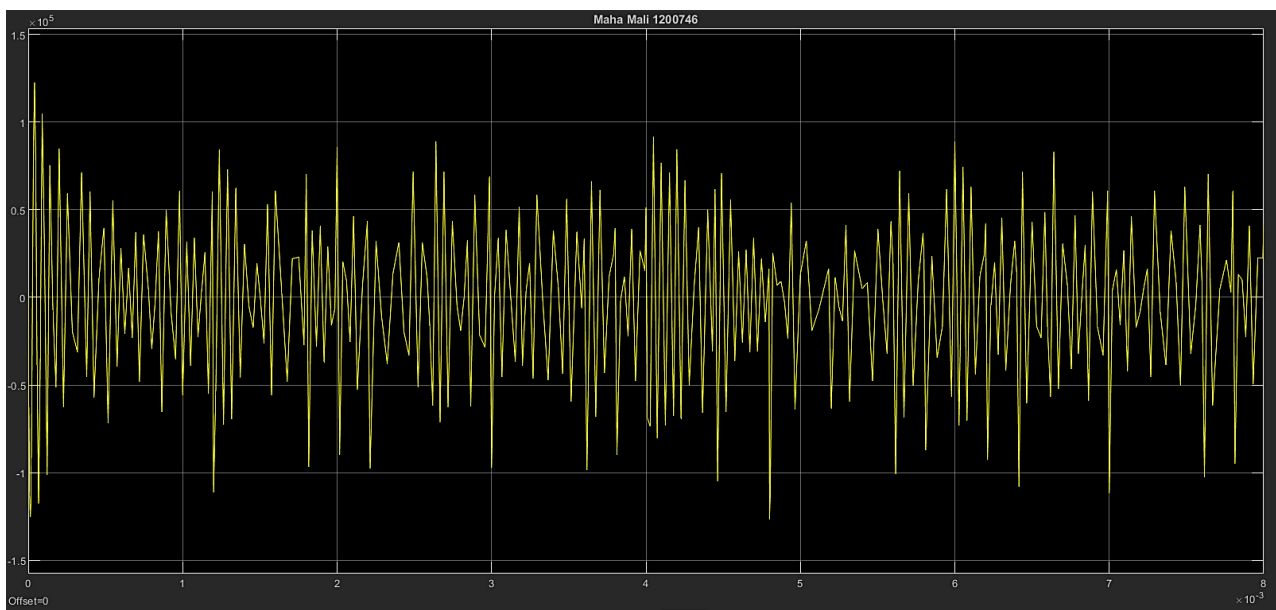


Figure 10: Differentiate $s(t)$ in time domine

Frequency domine

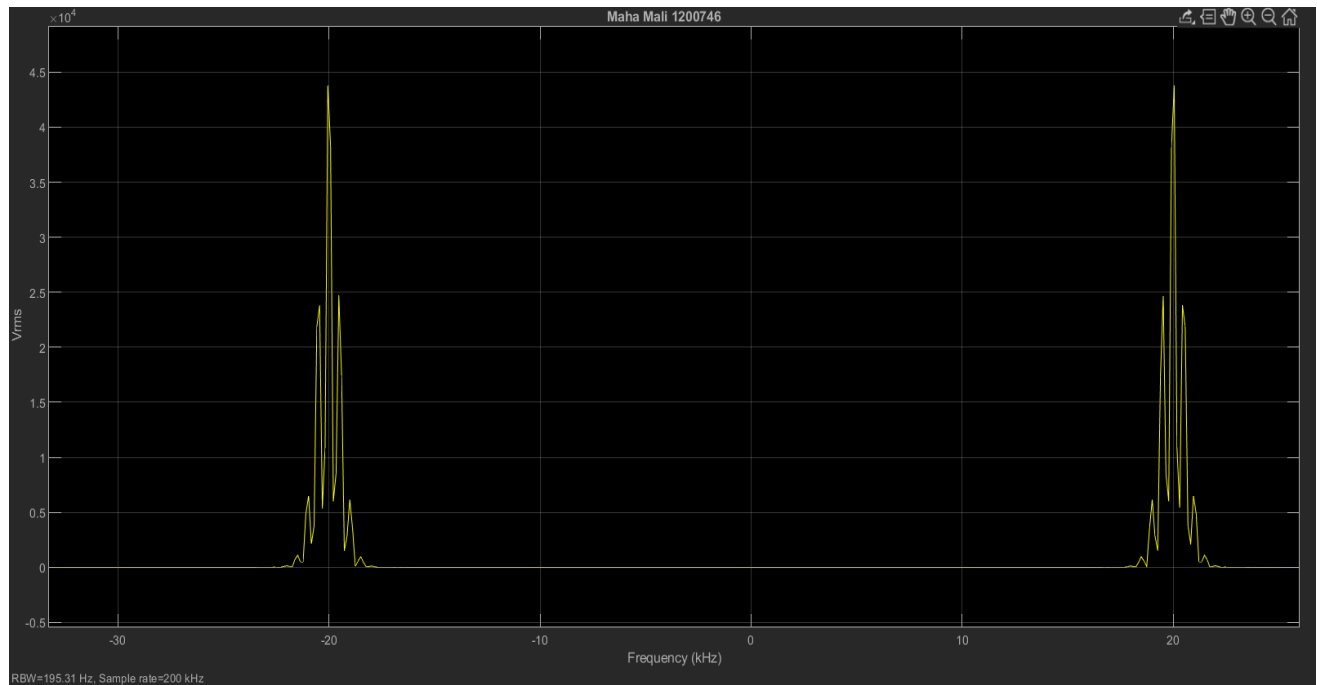


Figure 11: Differentiate $s(t)$ in frequency domine

Apply $ds(t)/dt$ to an ideal envelope detector

By Hand Solution

General form about $s_{FM}(t)$:

$$s_{FM}(t) = A_c \cos\left(2\pi f_c t + 2\pi K_f \int_0^t m(t) dt\right)$$

(*) To extract $m(t)$ from $s(t)$ we need to differentiate $s(t)$

$$\frac{d s_{FM}(t)}{dt} = -A_c \sin\left(2\pi f_c t + 2\pi K_f \int_0^t m(t) dt\right) \times (2\pi f_c + 2\pi K_f m(t))$$

⇒ [2] Differentiate $s(t)$

$$\frac{d s_{FM}(t)}{dt} = -A_c (2\pi f_c + 2\pi K_f m(t)) \sin\left(2\pi f_c t + 2\pi K_f \int_0^t m(t) dt\right)$$

⇒ Now we need envelope detector to get $m(t)$

[3] using envelope detector

$s_{FM}(t) \rightarrow$ Envelope Detector $\rightarrow y(t) \approx m(t)$

$$y(t) = A_c (2\pi f_c + 2\pi K_f m(t))$$

$$y(t) = 2\pi f_c A_c + 2\pi A_c K_f m(t) \Rightarrow \text{after envelope detection}$$

We need to cancel dc value using Capacitor

$y(t) \rightarrow$ Capacitor $\rightarrow r(t)$ □ $\Rightarrow r(t) = y(t) - \text{DC-Value}$

extracting $m(t)$

$$r(t) = 2\pi f_c A_c + 2\pi A_c K_f m(t) - \text{DC}$$

$$r(t) = 2\pi A_c K_f m(t)$$

Output $r(t)$ is proportional to $m(t)$

Figure 12: Apply $ds(t)/dt$ to an ideal envelope detector

Extract message signal by using phase-locked loop (PLL)

Block Diagram

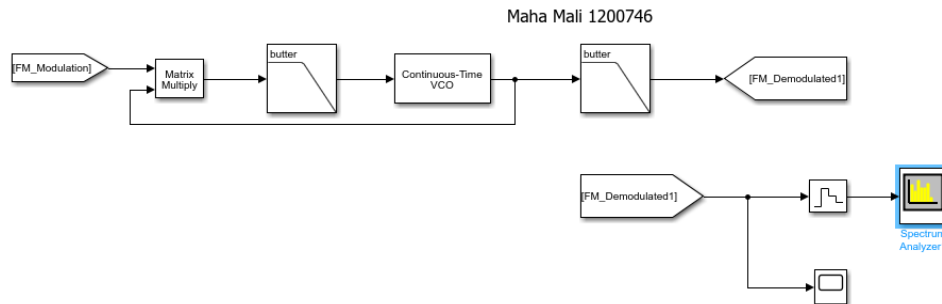


Figure 13: FM Demodulation by PLL Block Diagram

In time Domine

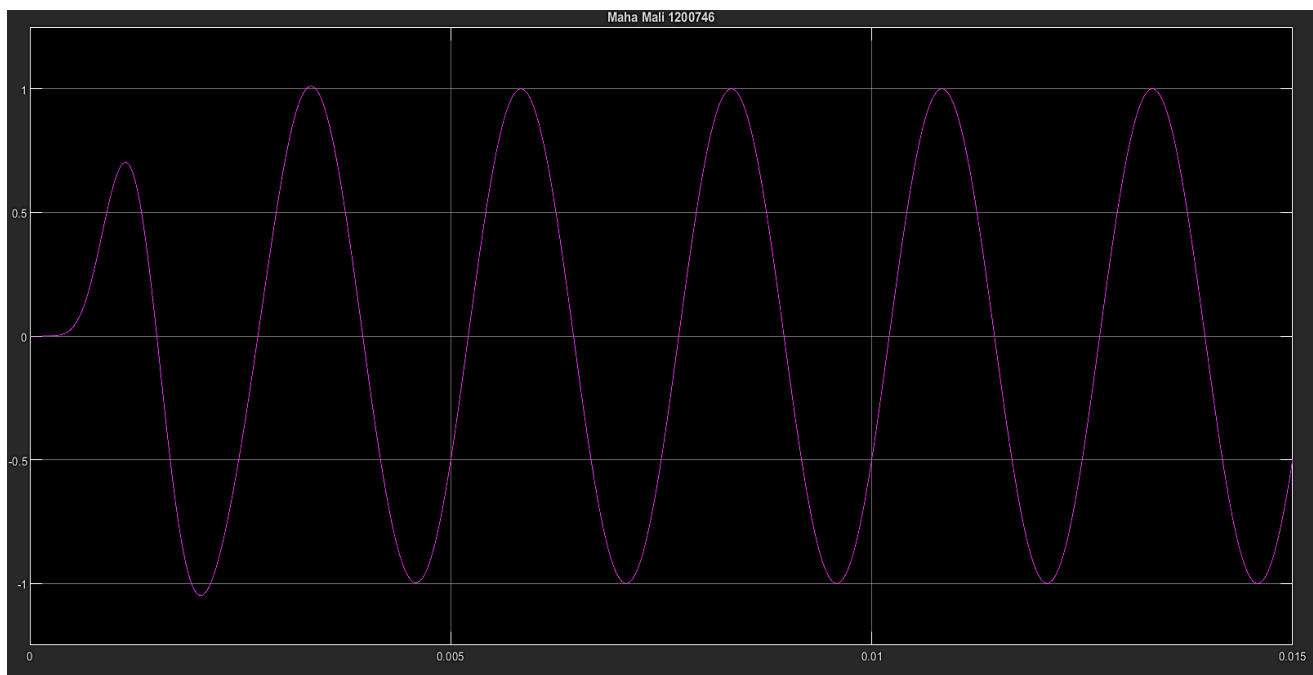


Figure 14: Demodulated signal in time domine

The figure 14 shows the amplitude of the demodulated signal has the same amplitude of message signal which is 1.

In frequency Domine

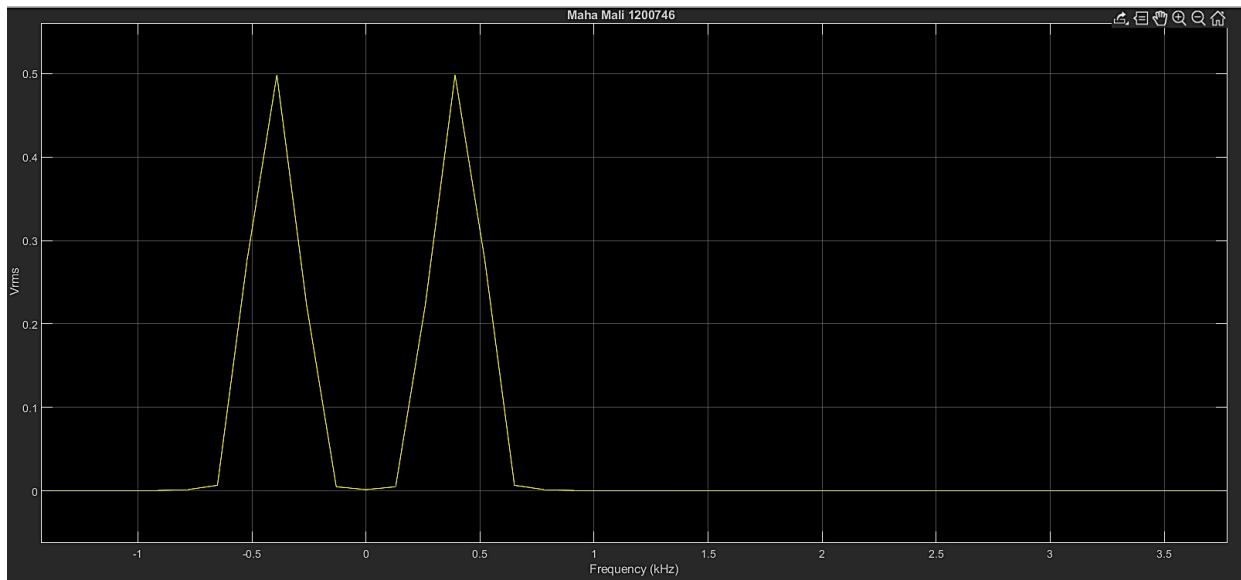


Figure 15: Demodulated signal in frequency domine

The figure show that the demodulated signal has the same frequency of message signal which is 500 Hz.

Extract the message signal by using the envelop detector Block Diagram

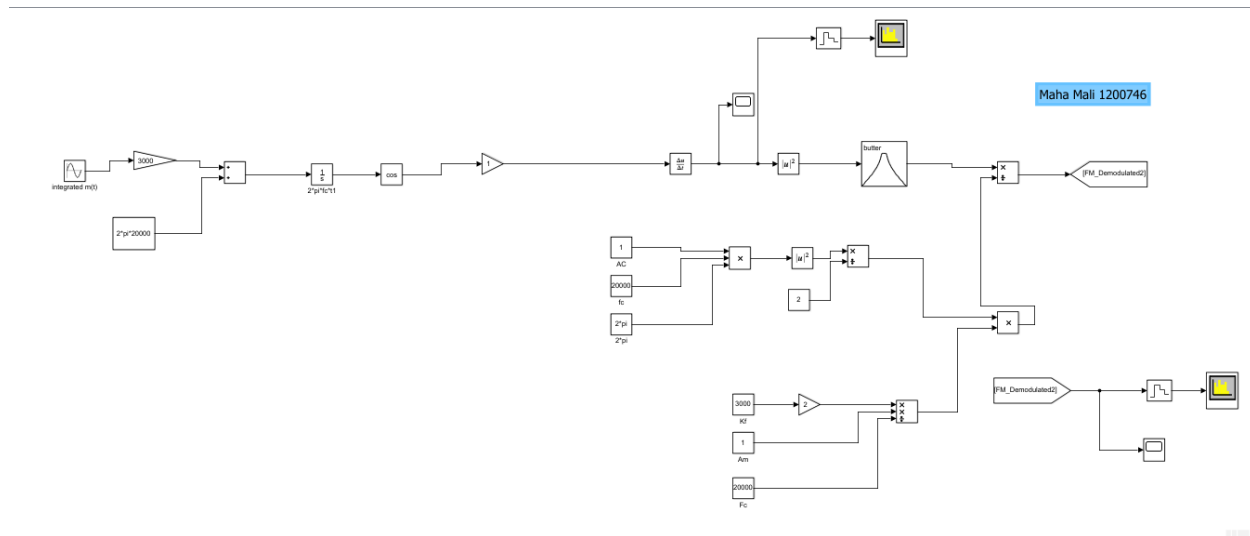


Figure 16::FM Demodulation by using the envelop detector Block Diagram

In Time Domine

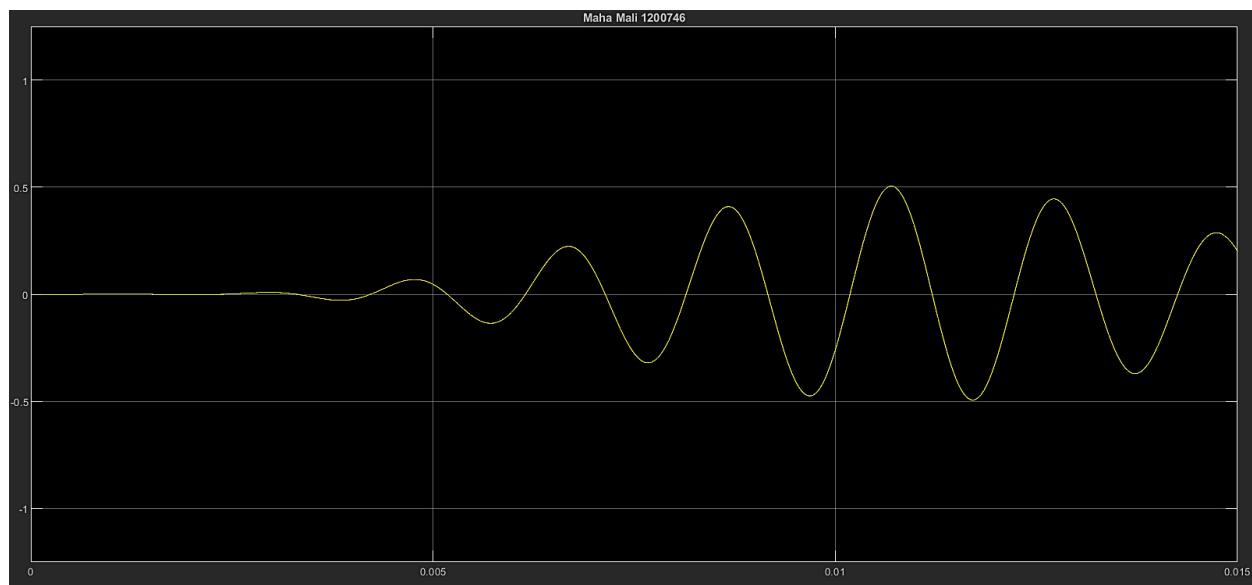


Figure 17: Demodulated signal in time domine

In frequency Domine

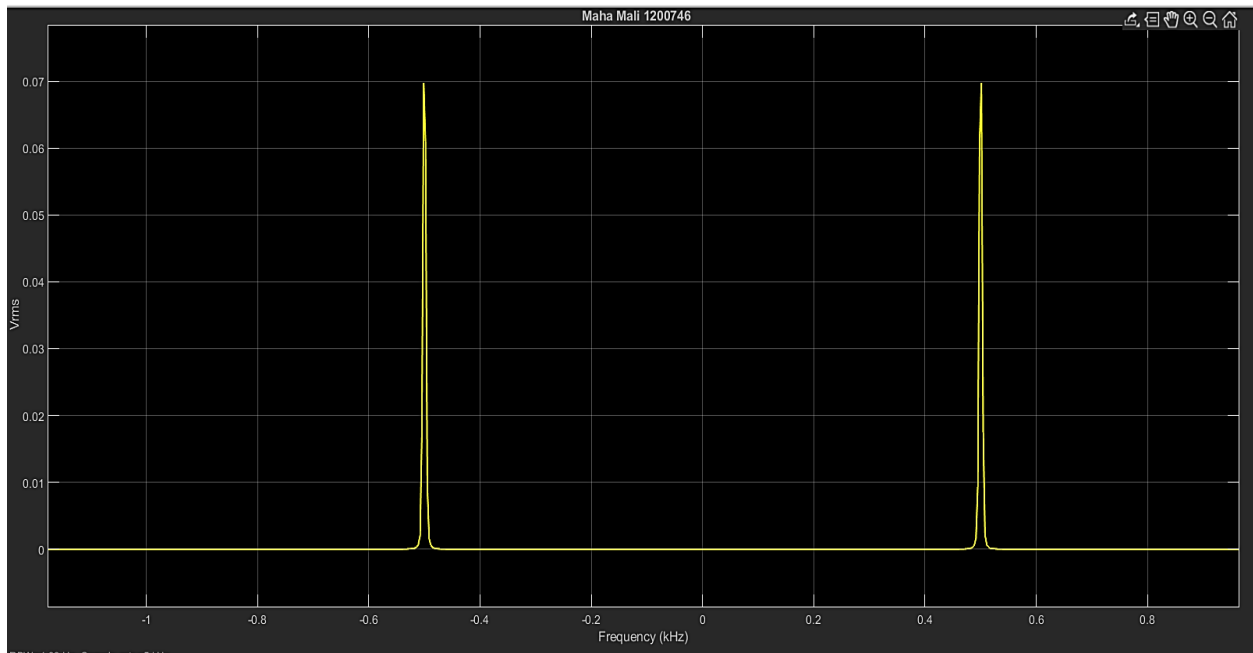


Figure 18: Demodulated signal in time domine

The figure show that the demodulated signal has the same frequency of message signal which is 500 Hz.