Substitution: Suess upper bound, solve with indu ons Solving recurrence. Algorithms midterm 1 Topics: recurrence, Devide and Conquer, Greedy, Dynamic Programming Divide & Conquer \* Asymptotic notation \* general recipe: time complexity? 1. Divide: loreak into subproblem: . T(n)= IL(f(n)) if I constants (>0 and that are instance of some problem no > 0 Sich that T(n) 7, c.f(n) & n7, no 2. Conquer: solve subproblems recurrely. - T(n)=O(f(n)) if 3 constants c>0 and no >0 if Small enough; solve straight Such that T(n) & C.C.(n) yn 7,00 . T(n)=O(f(n)) if 3 constants e>o and 3. Combine: Combine solvinas clevely no so such that T(n) = c.f(n) 4 n >, and 0(1) <0(10glogn) <0(10gn) < 0((10gn)) < Example. det multipy(x, y): O(n°) < O(n) < o(nlogn)=O(tognn)= input inbit pos x 19 into our : product Q(10gn!) < O(n2) < O(nc) < O(cn) < if n=1 retorn xy XL9 XR= leftmost [1/2] (ightmost [1/2] bits of X O(n1) Master Theorem: YL, YR = ... T(n)=aT([N/b])+O(nd) P. = Multiply (XL) YL) a70,671, d70; a= # subprobs Pz=multiply (XRIVE) P3: moltiply (X1+XR) Y1+(R) [1/2] + return: P1 x 221-121 + (P3-P1-P2) x 2 + M/b = Size of subproblems , not - time for combination T(n) = 0(nd)(09n) i dz 109 a mergesort: Mlogn) (00 n 109 b); d < 109 ba det mergesort (all, -n)). marge sort retire mergel mergesort(al1-n/2)). if n71: proof of correctness use induction for proof of collectness magesort (a[Nz+1] ... n]) of any divide and conquer algoritm . hase case n= 1: algo does nothing > eise : return ou correctly there ACV-m? [n-1] 6: means Concatenate det marge(xC1,-13, yC1,-18): If k=0; revor yC1,-2) a[m+1, -- n] are correctly sorted since size < n-1 if L= 0: renor X[1,-. K] Ternma: Marge: Corretty merges 2 IE XCIJE ACIJE rewin XII] merge (xca) - k) Solved on rangs. rontine: merge sort return YCIJ-merge (XCI,-K), Tan) 527(1/2)+C.n. O(nlogn)

Texas	10	matriod: ACI is a basis is
Creedy algorithm ! Tecipe		A \$ of a set in I (not a proper subset)
make whichever more seems best alt		graphic matriod:
moment and not willy too much about		· non emphases & independent (V, Ø)
FUNDRE Consequences.		· (VII) acyclic so is (U, I') & ISI
build solvior piece by piece. Choose		· exchange: o.it create oxiles
next piece which offers most obvious		Dynamic Programming: moduchin
and insuidiate effect.		identify collection of subproblems and factors.
try with very simple example first. *		Common subproblems. (runtime).
Aces of Collectivess.		O x, x n i y, - y m indu x y y y (mn)
Mirocr of confedencess.		3 x, - x n i y, - y m indut xp - x; 3 (m n)
exchange greed	y Stays	(3 X, X n Sub : x; x; o(a2)
argument who	ead	a tree input: supproblem choose
reassure ophinal solution A: great	y out 501.	a note in tree and reat subproble
exchange two of Size	K elema	
a i a po plement i to l U. Upl	nal sizem	FACK! Choose subprolens such that
get o' mck		all intal information is fremembered and
XI argue cost of o' is		carried forward.
STREAM	A [ Tri]	example: optimal binary search trees.
	ICLER	went in total access cost. (0 (43))
curpopers of in my k		
vertices to two groups add in	1 m	[1-n] [1-h] = company
- Ladibya		7/10/10
		OPT Ciri-13e o
min spanning mes	Cor de o ho n-d	
MST: connected graph with no. Cycles.		Opt Ei,i+d] = Ei,i+d] +
perustrals: - repeatedly choose edge lightest		ministra continuitans
		return opt (1, m)
(Union-Find) keep track of disjon on elements &	compute [FC1,-n):-	
(Union find) keep track of	car in range (130)	
i) make set (x): make a set	Ar jeitoni-	
1) make set (x): volume 2) Union (A1B): O(1) 2) Union (A1B): O(1)	) FC1/47 = FC1/4-17 ++607	
2) Union (AIB) Octor Set containing 3) Find(x) (ethin set containing	1 . E. C.	
Kroskals: MST Prim: (G, W)	1 2 C C C C C C C C C C C C C C C C C C	
CAEV: CARVINV	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	
makesette		1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
sa grace by weight any niedle up		S COUNTY OF THE
for each said cost (no)		13 × 22 137 + 17 12 5 5 19 19 1
if find (u) + find (v).  It = make quenc (V)  add edge 2 wv) tox while H not empto		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
( to ) repolate ( to )		12 7 Ex 2 4 Lis
TAR & for 24, 2	2 4 0 6 1 2 4	
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	1 3 13 C	
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SERIAL SOLUTION TO THE PORT OF		
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