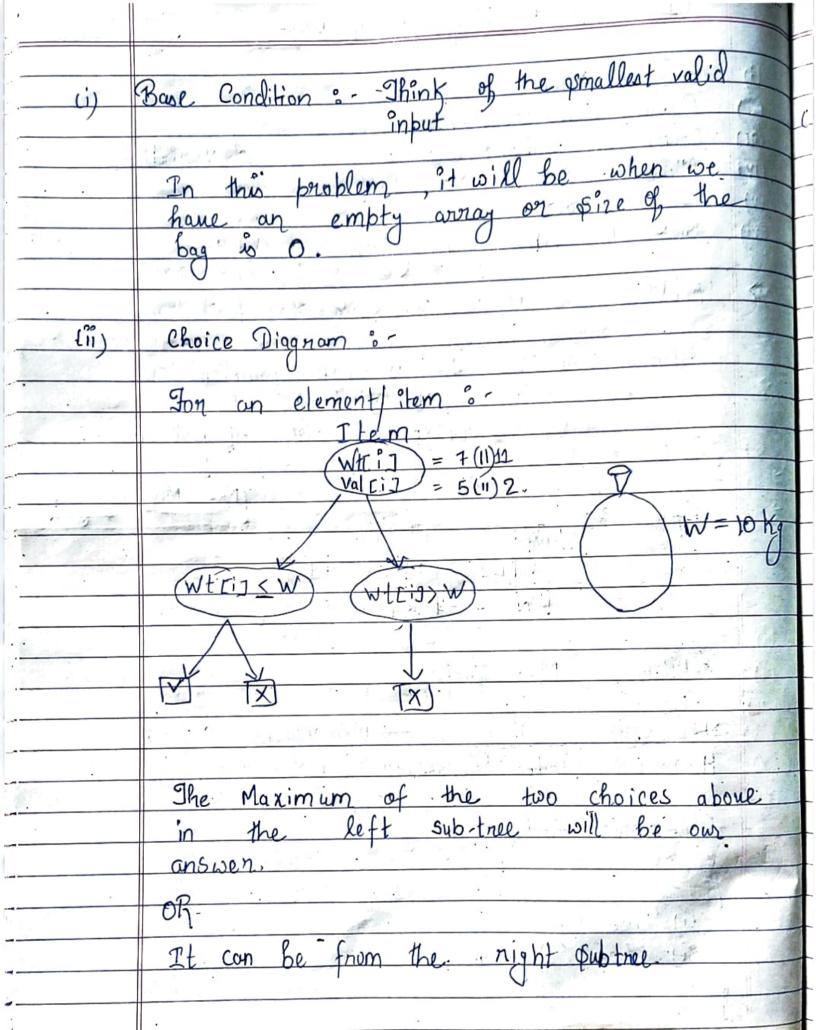
	Date.
	Tynamic Programing Page
	De name inognationing
	$\Omega\Omega = \Omega \Omega = \Omega \Omega$
	DP = Enhanced Recursion.
.>	10hon ha 111 000
-/-	When to apply DP?
(1)	Choices (ii) Optimal
(1)	(2 on mone)
	(Sittlifult)
.>	Note: Novem al + 1: Or bubles d'aille
·	Note: Never estant volving Dp problems directly by making table (Bottom-Up Manner)
	by maning waste of portom - op manier).
٠>	How to Start Writing DP code?
	Proof of
(Ci)	Recursive Approach
(ii)	Memoization (Teepak Manglani
رنس	Bottom - Up (Jabulation)
	Dynamic Programming
9.5	rate the de to the
Ľ)	0-1 Knapsack
ιί)	Un bounded Knapsack
- úii)	Fibonacci .
_(vi)	LCS
(v)	1. I.S Parent Problems
(vi)	Kadone's Algorithm
(vii)	Matrix Chain Multiplication
(viíi)	DP on trees
(ix)	DP on Gnid
1x5	O there
	The state of the s

	Date
	Knapsack Problem
	Mnap sack Trees are
•>	What is Knapsack?
	Knapsack is a kind of Bag in which we have to getone the items I with maximum
	Knowsack is a kind of Bag in which we have
	to ostone the items with maximum
	Bno fit.
	Types of knapsack ?-
	19 pts of map
	Knapsack
	(Map 30 c)
	7. 10 1
	Fractional Unbounded.
2 7 4	
	a la lateration
>	Fractional KNapsack:-
	0 0111 .20 0000
	It is a greedy problem, in which we need
·	to octobe the maximum vallweigh into
	the bag, i.e., we can store a part
9	of an item by cutting it.
(.	0/1 Knapsack:
	- The transfer of the state of
	In this problem, we use do in this
	either we include an item into the
	bag or just exclude it.
•>	Unbounded: - It is pame as 0/1 but, it
	have an infinite supply of every item.
	The state of the s

			•
	1-1		Date:
	(I) 0-	1 Knapsack Problem	Page
		Trapsacy (Honcom)	
(i)	0 20		
/			1
(ii)		Partition	
(iii)	Count of a	Subset Sum bset Sum Diff	Variations
_(iv)	Minimum Su	heat as Dill	· \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
(v)	Jarget Sur	user pun vif	
(M)	N. Quer		1 and 1
(VI)	1400 00	ubset sum given diff.	
		, , ,	7.
•>	Problem:	0/1 Knobsack	
		0/1 Knapsack	The state of the s
	The 1st have		
	Identification	: It is a DP	broblem :-
	31	i) Because of	Chaire
	- 一种的人	Chil Records	CHOICES
		(ii) Because is	Optimal ans
	The same	- Iller 1 - Charlying	
	710		Max, Min, Langest, e
	1/P :-	111111111111111111111111111111111111111	and sudesite
		W(L) - 113 45	
	/ - 10	Va []: 114 5 7	
		W:- 7 kg	from the state of
		+ Kg	A = 8
	10	+ + + + + + + + + + + + + + + + + + + +	
	O/P :- 1	1ax Profit	14 -
	DP Code :	Rasunal a x M	Y.
	dia to	Recursion -> Memoiza	tion -> Jabulation
	now to Wy	ite Recursive Code.	0 -
1	33 11 11	toda of the second second	()
	Recursine (oclaria	
	·	DOCE III III S	· · · ·
	0		1 1 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -
	(i) Base Con	d.	
	Ci) Choice	D'acc	
	Choice (man.	P. 1. P. T.
- 1	Q .	9	



		Page
	Recursive Code :-	7
Ma K Priofit)	rint Knapsack Cint wt [], int valce, int	w, intn)
	Since of the second sec	11
	if $(n = 0 \mid w = 0)$ netwo	0:
		La de de la companya
	if (wt[n-1] < W)	
	The state of the s	
	return max [val[n-1] + Knapsack	(wt, val, W-wt[],n-
	, Knapsack (wt,	val, W, n-1)
	else if (wt [n-1]) W)	· ,
	netwin knapsack wt, val, w	1, n-1);
		. ناب
		· · · · · · · · · · · · · · · · · · ·
	N. A. A. C.	

	Date Page
	Memoize Code :
:	We will add 4 lines to the recursive code
	to memoize it.
	The Basic idea is to make an annay of
	changing variables in the necursive code
	int dp [n+1] [w+1]; memset (dp,-1, size of (dp))
	el la
	int Knapsack (int wt [], int val [], int W, int n)
-	
	if (n == 0 11 W == 0) return 0;
	enter analysis is an extensive contact and
	if (dptn][w] 1=-1) netwn dp[n][W];
3.	if (wt[n-1] \le W)
•	
4	
201	return dp [n][w] = max val[n-1] + Knapsack(istrize)
	The start of the s
	, Knapsack (n-1));
·	
	else if [wt[n-1] > W)
	\
-	return dp[n][w] = Knapsack (wt, val, W, n-1);

	Page
	Jabulation Code (Bottom - Up Code):-
	- (Doctor)
	The basic idea behind Tabulation is to
	remove the recursive calls, that we have
	Seen in the Memoization technique into
	îterative form
	Tabulation can be performed in the following
	two steps:
, 0,	
(1)	Initialization (ii) Changing Recursive functions (Basically these into iterative one
	(Basically these into iterative one
	one the BC
=	of necursion)
	19 1 . 1 . C . 175 1
	Pint dp [n+1][W+1];
	» Initialisation:
	7 411119 113911071 6
	for (int i=0; i <n+1; i++)<="" th=""></n+1;>
	fon (int j = 0; j < W+1? j++)
	dp[i][i] = 0
٠>	Iterative Vervion
e .	for (int i = 1; i< n+1; i++)
	for (int j=1; j< W+1; i++ 10
	if (wt[i-1] ≤ ₩3)
•	1
1 ,	db[i-1][i]);
	else dp [i][j] = dp[i-1][j]; netwon dp[n][W];
1	netwin du [n][W];

	Date
2.	
	Quel cack and Introduction
•>	Revision of Knapsach
- 9	- Linthen broblems
. 3.	How to Identify if a broblem in dp can
8:	How to Identify if a problem
1	be polved wing knapsack
js.	a can along we have
4	Whener we per a battern where we have
الد الد	
1	that capacity with optimal profit
- ,,,,,,,,,	broblem falls under Knapsack
	la happen that
	Than than
	the band only I array started
	two wtl1 and vall)
9/	neglect the value array array
	that array as our weight array
	Example :
System	(Pattern) [7, 12, 13, 14]
•	
,	DEN NON IN

	Choices and a constraint as W.
-	the state of the test
1	that to tare
	Win our ans
W	or all there is also the change in
**	Thria,
**	the initialization in its voliation
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	

	(i) Subset - Sum Problem
•>	Problem :-
	C 0
	Gine an aviay and a sum, tind
	whether by adding some elements of
	Gine an avray and a sum, find whether by adding some elements of the avray we get sum or not.
	Example: - I/p and: \$ 2,8,7,8,10}
•	= 10 10 10 10 10
	Sum: - 11
	D/O . Tula
	O/P :- True
-	I/P ann: \$2,3,7,8,10\$
	I/P ann: $(2,3,7,8,10)$
	Super Control of
	Sum :- 14
	O/P:- False
_	Co el el illora de la compania del compania de la compania del compania de la compania del compania de la compania del compani
•>	Similarity with 0/1 Knapsack:
	0 0
	Its we can see here we have given a
	sigle array, nother than two that we have
	seen in Knapsack. We consider it as our
	weight array as discussed in the newision.
	Also we have choices to include or not to
-	include an average element onto our set.
-	
	And we have given Maximum rapacity as
	grum analogous to (W in Knapsack)

	Date
	Page
•>	Code Variations :-
	(i) Initialisation :-
	If avoing size is Opmorphind sum is O. go, Is it possible to get the sum? Yes, it is always possible empty subset.
	of Is it bossible to get the sum?
	yes, it is always possible empty \$40set
	93
-	DC suchan but O but array
	If sum is greaten that O but array is it possible to get sum?
	No.
	So, we got our initialisation as:
	dp[n+1][sum+1];
	fon (int i = 0; i < n+1; i++)
	fon (int j=0; jKsumt); jtt.)
	if (i==0) dp[i][j] = false;
	if (i == 0) dp Ci] [j = trul;
	The state of the s
	(ii) Main Coll :-
1	wr7> ann c7
1	WEIJ -> annej
int Max P	
- 1111	Pousic Variation

	Page
	There is no purpose of max function in bolean 60 , we use (11) operator. if $(ann \ \Gamma : -1] \le j)$ $dp[i] \Gamma = (dp[i] \Gamma - ann[i-1] dp[i-i] \Gamma];$
	else dp[i][j] = dp[i-1][j];
,	Then, we have to: - Deepak Manglan
	netwen de [n] [sum]; (ii) Equal Sum Partition
<i>^</i> >	Problem 3
	Given an averay, can we partition it into two subsets such that if we take all the elements and put it into these subsets we will get equal sum in these subsets.
	I/p-:- on: 5 1, 5, 5, 11)
	0/p :- True 11 Since, S1,5,53 == S112 T/p : or :- S1, 2, 3,49
4	0/p : False.

Date	
Page	
5	Ł.

·> Some Intuition and Observation: Since, we have to take all the element of the array and partition it into two subsets of equal sum. The total sum of the array should never be odd Proof: Let, say sum of one subset is x Pince, Subsetsums, = Subsetsums2 \propto X + X = 2x Sum of the average It should always be divisible by 2 Otherwise, we written false Also, as we can see it would enough to show that if we get subset of from the whole array of We will get our answer

	Page
	Code :-
	Bool Equal Sum Part (int ann 12, int n, intsum)
	if (sum 1/0 2) neturn false;
	1 if it
	netwon Subset Sum (int ann [], intn, int sum
	2
	1.
	(iii) Count of Subset Sum with a Given Sum
>	Problem :-
-	Given an array and a sum, find how many subsets of given sum are bossible
	Ab U Sard Sard Sard Sard Sard Sard Sard Sard
	Ex: - I/P: - S1, 2, 3, 5, 8, 10 2
•	0/P ° - 3
\int	Call de a C C a a = 3
#	Explonation :- 2 2, 3, 5), \$10), \$2,83
+	
11	A P

•>	Similarity with Subset Sum:
	In Subset Sum problem, we only need to output if a subset of given gruen. Sum is possible on not.
	But here, in this problem we also need to return the count of the subset
•>	Code Vonigtion:
(1)	Initialisation :-
	for (int i=0; i <n+1; (int="" for="" i+t)="" j="0;" j+t)<="" j<sum+1;="" td=""></n+1;>
	if $(i==0)$ dpcil[i] = 0; if $(i==0)$ dpcil[i] = 1;
(")	Main Code :
	if (ann [:-1] > Sum) dp[i][j]=dp[i-1][j]
	else decisej = deci-1] [j-ann ci-1] + deci-1
4	

Page.....

	Page
	(iv) Minimum Subset Sum. Difference!:
•>	Problem:
	Given an averag of integers, we have to fartition it into two subsets of with minimum difference i.e.
	S, - S ₂ = minimum Teepak Manglani
•>	Intution and Observations:
17	Given two pubsests s, and so to to so
2.2	$S_1 - S_2 = \min \left(\text{diff} \right)$
	Letis try to find a range of this difference
	if we have $S_1 = avray$, $S_2 = g$
	of array i.e., nonge will be:
	A Third A Thir
1	Sum (avr)
	Let's claim here that atleast one of
	the subset will always present in the first half completely

This can be proved easily since; SI + S2 = Sum (ann) so, we can find out the difference Sum(arr) -S, = diff diff = Sum(ann) -2xs, Code :int ap[n+1][sum +1]; for (int i=0; i(n+1; i++)
for (int j=0; j<sum+1; j++) if (i = = 0) dprigrijg = false; (j==0) dpri3 [j] = true; for(int i=1; ix n+1; i++) for (intj=1; j<Sumtle; j+t) if (annti-1] < sum) ap[i][j]=[ap[i-1][j-ann[i-1]]-[]-ap[i-1][j] else dp[i][j] = dp[i-1][j]

	Date Page
	for (int i = sum; i > 0; i)
	2
	5.
	if (dp[n][i] = = tnue)
	9.
	dict
	diff = sum - 2 xi
	break;
	S Print of the second of the s
	retion diff.
75	(v) Count the number of Pubset with
	ginen Difference
*	
17	Troblem :-
	Given an array and difference between the two pubset sum count the number of subset with this difference
	subset sum count the number of
	Subset with this giffounds
	Ex 3
	I/P:- S1, 1, 2, 3 2
	. () -) -)
	0/9 : 3
3	Table of the second of the sec
1	Explanation 3 - \$1,22 and \$1,32 \$1,27 and
1	
	91,1,2 g and \$ 3 g

