



Dynamic Programming

Introduction



Dynamic Programming (DP) is one of the most powerful techniques every programmer should know.



Many people think it's complicated, but it's simply a way of thinking to solve big problems efficiently.

When to Use DP

1

When the solution of a problem depends on solutions of smaller parts.

2

Those smaller parts might also depend on even smaller ones.

Core Idea



- **Break a big problem into smaller subproblems.**
- **Subproblems can be broken down further until they reach the simplest form.**
- **The solution of the main problem depends on the solutions of its subproblems.**

Two Approaches

Top-Down:

- Start from the main problem and break it into smaller ones.
- Usually implemented using recursion.

Bottom-Up:

- Start from the smallest subproblem and build up to the final solution.
- Usually implemented using loops.

Example: Fibonacci Sequence

- Each element = sum of the previous two elements.
- Formula: $\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$
- Base cases: $\text{Fib}(0) = 1$, $\text{Fib}(1) = 1$
- With this, we can compute the value of any index n .