

In the following we consider the price of a discrete Asian option given by :

$$\text{Asian-Price} = e^{-rT} \mathbb{E}[(\frac{1}{n} \sum_{i=0}^{n-1} s_{ti} - k)_+]$$

We will use two variate control to reduce the variance of our computations :

- for the first variate control we will use the random variable
$$Y = e^{-rT} \exp(\frac{1}{T} \int_0^T \log(S_u) du)$$
- for the second variate control we will use the random variable
$$Z = e^{-rT} (\exp(\frac{1}{T} \int_0^T \log(S_u) du) - K)_+$$
- Finally, we compute the Greek parameter  $v$  (Vega) of the option price, using both pathwise derivative and the log-likelihood ratio methods.