DSU on Tree

```
vector<int> *pvec[MAX];
vector<int> G[MAX];
int sz[MAX],color[MAX],color_counter[MAX];
pair<ll,int> Info[MAX];
pair<ll,int>dfs(int u,int p=-1,bool keep=false)
   int i,j,k,child,hchild=-1;
   for(i=0; i<G[u].size(); i++)</pre>
       if(G[u][i]==p) continue;
       if(hchild==-1||sz[hchild]<sz[G[u][i]])</pre>
           hchild=G[u][i];
   for(i=0; i<G[u].size(); i++)</pre>
       if(G[u][i]==p||G[u][i]==hchild) continue;
       dfs(G[u][i],u,false);
   if(hchild!=-1)
       Info[u] = dfs(hchild, u, true);
       pvec[u] = pvec[hchild];
   else
       pvec[u]=new vector<int> ();
   pvec[u]->push_back(u);
   color_counter[color[u]]++;
   if(color_counter[color[u]]>Info[u].second)
       Info[u].second=color_counter[color[u]];
       Info[u].first=color[u];
   else if(color_counter[color[u]] == Info[u].second)
       Info[u].first=Info[u].first+color[u]:
   for(i=0; i<G[u].size(); i++)</pre>
       if(G[u][i]==p||G[u][i]==hchild) continue;
       child=G[u][i];
       for(j=0; j<(*pvec[child]).size(); j++)</pre>
           k=(*pvec[child])[j];
           pvec[u]->push_back(k);
           color_counter[color[k]]++;
           if(color_counter[color[k]]>Info[u].second)class LiChaoTree
               Info[u].second=color_counter[color[k]]
               Info[u].first=color[k];
     else if(color_counter[color[k]] == Info[u].second)
               Info[u].first=Info[u].first+color[k];
```

```
if(!keep)
    for(j=0; j<(*pvec[u]).size(); j++)</pre>
       k=(*pvec[u])[j];
        color_counter[color[k]]--;
return Info[u];
```

Divide and Conquer Optimization

```
vector<long long> dp_before(n), dp_cur(n);
long long C(int i, int j);
// compute dp_cur[1], ... dp_cur[r] (inclusive)
void compute(int 1, int r, int optl, int optr) {
   if (\bar{1} > r)
       return:
   int mid = (1 + r) >> 1;
   pair<long long, int> best = {LLONG_MAX, -1};
   for (int k = optl; k <= min(mid, optr); k++) {</pre>
   best = min(best, {(k ? dp_before[k - 1] : 0) + C(k, mid) k}; k}; code;
   dp_cur[mid] = best.first;
   int opt = best.second;
   compute(1, mid - 1, optl, opt);
   compute(mid + 1, r, opt, optr);
   int solve() {
   for (int i = 0; i < n; i++)
       dp_before[i] = C(0, i);
   for (int i = 1; i < m; i++) {
       compute(0, n - 1, 0, n - 1);
       dp_before = dp_cur;
   return dp_before[n - 1];
```

Li Chao Tree

```
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
|#include<string.h>
using namespace std;
#define MAX 200005
#define MOD 1000000007
#define INF 1000000000
#define EPS 0.000000001
#define FASTIO ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
   long long L,R;
   bool minimize;
   int lines;
   struct Node
       complex<long long> line;
       Node *children[2];
       Node(complex<long long> ln= {0,1000000000000000000})
```

```
line=ln;
                        children[0]=0;
                       children[1]=0;
} *root:
long long dot(complex<long long> a, complex<long l</pre>
           return (conj(a) * b).real();
long long f(complex<long long> a, long long x)
           return dot(a, \{x, 1\});
void clear(Node* &node)
            if(node->children[0])
                       clear(node->children[0]);
           if(node->children[1])
                       clear(node->children[1]);
void add_line(complex<long long> nw, Node* &node,
           if (node==0)
                       node=new Node(nw);
                       return:
           long long m = (1 + r) / 2;
           bool lef = (f(nw, 1) < f(node->line, 1)&&minim
           bool mid = (f(nw, m) < f(node->line, m) & min = min 
                       swap(node->line, nw);
            if(r - 1 == 1)
                      return;
           else if(lef != mid)
                       add_line(nw, node->children[0], 1, m);
           else
                      add_line(nw, node->children[1], m, r);
long long get(long long x, Node* &node, long long
           long long m = (1 + r) / 2;
           if(r - 1 == 1)
                      return f(node->line, x);
           else if (x < m)
                        if(node->children[0]==0) return f(node->lin
                        if(minimize) return min(f(node->line, x), g
```

for (int j = m - 1; $j \ge 0$; --j) {

decompose(heavy[v], h, adj);

for (int c : adj[v]) {

```
else return max(f(node->line, x), get(x, node->children[0]t, plop(m)););
                                                                                                                       query(x2,y1-1,1)*x2 +
                                                                   d2[j] = st.empty() ? m : st.top();
                                                                                                                       query(x2,y1-1,3) +
       else
                                                                   st.push(j);
                                                                                                                       query(x2,y1-1,2)*(y1-1);
                                                                                                                 LL v3=query(x1-1,y2,0)*(x1-1)*y2 +
           if(node->children[1]==0) return f(node->line, x); while (!st.empty())
if(minimize) return min(f(node->line, x), get(x, nodes>children[1], m, r));
                                                                                                                       query(x1-1,y2,2)*y2+
                                                                                                                       query(x1-1,y2,1)*(x1-1) +
           else return max(f(node->line, x), get(x, node->children[1], m,or);; < m; ++j)
                                                                                                                       query(x1-1,y2,3);
                                                             ans = \max(\text{ans}, (i - d[j]) * (d2[j] - d1[j] - 1)); LL v4=query(x1-1,y1-1,0)*(x1-1)*(y1-1) +
                                                                                                                       query(x1-1,y1-1,1)*(x1-1) +
public:
   LiChaoTree(long long l=-1000000001,long long r=100000001,bool mn=false)
                                                                                                                       query(x1-1,y1-1,2)*(y1-1) +
                                                                                                                       query(x1-1,y1-1,3);
                                                                                                                 LL ans=v1-v2-v3+v4;
                                                            DS
                                                                                                                 return ans;
       R=r;
                                                       2.1 BIT 2D
       root=0;
       minimize=mn:
                                                                                                                2.2
                                                                                                                      CD - hellbent
                                                        const int mx = 1002, my = 1002;
       lines=0;
                                                        long long bit[4][mx][my];
                                                                                                                vector <int> g[N]; int n, child[N], done[N];
                                                        void update( int x, int y, int val, int i ) {
   void AddLine(pair<long long,long long> ln)
                                                                                                                void dfs_size(int u, int par) {
                                                         int \bar{y}1;
                                                                                                                 child[u] = 1;
                                                          while( x<=mx ) {</pre>
       add_line({ln.first,ln.second},root,L,R);
                                                                                                                 for (int v: g[u]) {
                                                           y1=y;
       lines++;
                                                                                                                   if (done[v] or v == par) continue;
                                                           while( y1<=my)</pre>
                                                                                                                   dfs_size(v, u); child[u] += child[v];
                                                             bit[i][x][y1] += val, y1 += (y1\&-y1);
   int number_of_lines()
                                                           x += (x\&-x);
       return lines;
                                                                                                                int dfs_find_centroid(int u, int par, int sz) {
                                                                                                                 for (int v: g[u]) {
   long long getOptimumValue(long long x)
                                                        long\ long\ query(\ int\ x,\ int\ y,\ int\ i\ ) {
                                                                                                                   if (!done[v] and v != par and child[v] > sz) {
                                                         long long ans=0; int y1;
                                                                                                                     return dfs_find_centroid(v,u,sz);
       return get(x,root,L,R);
                                                          while (x>0)
                                                           y1 = y;
                                                           while( y1>0 )
    ~LiChaoTree()
                                                                                                                 return u;
                                                             ans += bit[i][x][y1], y1 -= (y1&-y1);
                                                           x = (x\&-x);
       if(root!=0) clear(root);
                                                                                                                void solve (int u) {/**problem specific things */}
                                                                                                                void dfs_decompose(int u) {
                                                         return ans;
                                                                                                                 dfs_size(u, -1);
int main()
                                                                                                                 int centroid=dfs_find_centroid(u,-1,child[u]/2);
                                                        // add value k from (x1,y1) to (x2,y2) inclusive
                                                                                                                 solve(centroid);
                                                        void add( int x1, int y1, int x2, int y2, int k) {
   return 0;
                                                                                                                 done[centroid] = 1;
                                                         update(x1,y1,k,0);
                                                                                                                 for (int v : g[centroid]) {
                                                         update(x1, y2+1, -k, 0);
                                                                                                                   if (!done[v]) dfs_decompose(v);
1.4 zero_m atrix
                                                          update(x2+1,y1,-k,0);
                                                          update(x2+1,y2+1,k,0);
int zero_matrix(vector<vector<int>> a) {
                                                          update(x1,y1,k*(1-y1),1);
   int n = a.size();
                                                          update(x1, y2+1, k*y2, 1);
                                                                                                                      Hld - cpalgo
   int m = a[0].size();
                                                         update(x2+1,y1,k*(y1-1),1);
   int ans = 0;
                                                                                                                vector<int> parent, depth, heavy, head, pos;
                                                          update(x2+1,y2+1,-y2*k,1);
   vector\langle int \rangle d(m, -1), d1(m), d2(m);
                                                                                                                int cur_pos;
                                                         update(x1,y1,k*(1-x1),2);
   stack<int> st;
                                                                                                                int dfs(int v, vector<vector<int>> const& adj) {
                                                          update(x1,y2+1,k*(x1-1),2);
   for (int i = 0; i < n; ++i) {
                                                                                                                    int size = 1;
                                                          update(x2+1,y1,k*x2,2);
       for (int j = 0; j < m; ++j) {
                                                                                                                   int max_c_size = 0;
           if (a[i][i] == 1)
                                                          update(x2+1,y2+1,-x2*k,2);
                                                                                                                   for (int c : adj[v]) {
                d[j] = i;
                                                         update(x1,y1,(x1-1)*(y1-1)*k,3);
                                                                                                                       if (c != parent[v]) {
                                                         update(x1,y2+1,-y2*(x1-1)*k,3);
                                                                                                                           parent[c] = v, depth[c] = depth[v] + 1;
       for (int j = 0; j < m; ++j) {
                                                         update(x2+1,y1,-x2*(y1-1)*k,3);
                                                                                                                           int c_size = dfs(c, adj);
           while (!st.empty() && d[st.top()] <= d[j])</pre>
                                                          update(x2+1,y2+1,x2*y2*k,3);
                                                                                                                           size += c_size;
               st.pop();
                                                                                                                           if (c_size > max_c_size)
           d1[j] = st.empty() ? -1 : st.top();
                                                        // get value from (x1,y1) to (x2,y2) inclusive
                                                                                                                               max_c_size = c_size, heavy[v] = c;}}
                                                        long long get( int x1, int y1, int x2, int y2 ) {
           st.push(j);
                                                                                                                   return size;}
                                                         LL v1=query(x2,y2,0)*x2*y2 +
                                                                                                                decompose(int v,int h,vector<vector<int>> const& adj){
                                                               query(x2, y2, 1)*x2 +
       while (!st.empty())
                                                                                                                   head[v] = h, pos[v] = cur_pos++;
           st.pop();
                                                               query(x2,y2,2)*y2 +
                                                                                                                   if (heavy[v] != -1)
```

query(x2,y2,3);

while (!st.empty() && d[st.top()] <= d[j]) LL v2=query(x2,y1-1,0)*x2*(y1-1) +

```
if (c != parent[v] && c != heavy[v])
           decompose(c, c, adj);}
void init(vector<vector<int>> const& adj) {
   int n = adj.size();
   parent = vector<int>(n);
   depth = vector<int>(n);
   heavy = vector<int>(n, -1);
   head = vector<int>(n);
   pos = vector<int>(n):
   \overline{\text{cur}}_{\text{pos}} = 0;
   dfs(\bar{0}, adj);
   decompose(0, 0, adj);
int query(int a, int b) {
 int res = 0;
 for (; head[a] != head[b]; b = parent[head[b]]) {
     if (depth[head[a]] > depth[head[b]])
         swap(a, b);
int cur_heavy_path_max =
segment_tree_query(pos[head[b]], pos[b]);
     res = max(res, cur_heavy_path_max);
 if (depth[a] > depth[b])
     swap(a, b);
 int last_heavy_path_max =
 segment_tree_query(pos[a], pos[b]);
 res = max(res, last_heavy_path_max);
 return res;
```

2.4 Implicit Treap

```
#include<bits/stdc++.h>
#include<math.h>
#include<vector>
#include<stdlib.h>
using namespace std;
#define MAX 200005
#define MOD 998244353
template <class T>
class implicit_treap
   struct item
      int prior, cnt;
      T value;
      bool rev:
      item *1,*r;
      item(T v)
          value=v;
          rev=false:
          1=NULL;
          r=NULL:
          cnt=1;
          prior=rand();
   } *root,*node;
   int cnt (item * it)
      return it ? it->cnt : 0;
```

```
void upd_cnt (item * it)
       if (it)
           it \rightarrow cnt = cnt(it \rightarrow l) + cnt(it \rightarrow r) + 1;
    void push (item * it)
       if (it && it->rev)
           it->rev = false:
           swap (it->1, it->r);
           if (it->1) it->1->rev ^= true;
           if (it->r) it->r->rev ^= true;
   }
    void merge (item * & t, item * 1, item * r)
       push (1);
       push (r);
       if (!1 || !r)
           t = 1 ? 1 : r;
       else if (l->prior > r->prior)
           merge (1->r, 1->r, r), t = 1;
           merge (r->1, 1, r->1), t = r;
       upd_cnt (t);
   }
    void split (item * t, item * & 1, item * & r, int key, int Nauld = 0)
       if (!t)
           return void( 1 = r = 0 );
       push (t);
       int cur_key = add + cnt(t->1);
       if (kev <= cur kev)
           split (t->1, 1, t->1, key, add), r = t;
           split (t->r, t->r, r, key, add + 1 + cnt(t->1)), output (t->r, arr);
ll = t;
       upd_cnt (t);
    void insert(item * &t,item * element,int key)
       item *1.*r:
       split(t,1,r,key);
       merge(1,1,element);
       merge(t,1,r);
       l=NŬLL:
       r=NULL;
   T elementAt(item * &t, int key)
       push(t);
       T ans;
       if(cnt(t->1)==key) ans=t->value;
       else if(cnt(t->1)>key) ans=elementAt(t->1,key);
       else ans=elementAt(t->r,key-1-cnt(t->l));
       return ans;
    void erase (item * & t, int key)
       push(t);
```

```
if(!t) return;
       if (key == cnt(t->1))
           merge (t, t->1, t->r);
       else if(kev<cnt(t->1))
           erase(t->1,key);
           erase(t->r,key-cnt(t->1)-1);
       upd_cnt(t);
   void reverse (item * &t, int 1, int r)
       item *t1, *t2, *t3;
       split (t, t1, t2, 1);
       split (t2, t2, t3, r-l+1);
       t2->rev ^= true;
       merge (t, t1, t2);
       merge (t, t, t3);
   void cyclic_shift(item * &t,int L,int R)
       if(L==R) return:
       item *1,*r,*m;
       split(t,t,l,L);
       split(1,1,m,R-L+1);
       split(1,1,r,R-L);
       merge(t,t,r);
       merge(t,t,1);
       merge(t,t,m);
       1=NULL:
       m=NULL:
   void output (item * t,vector<T> &arr)
       if (!t) return;
       push (t);
       output (t->1,arr);
       arr.push_back(t->value);
public:
   implicit_treap()
       root=NULL;
   void insert(T value,int position)
       node=new item(value);
       insert(root, node, position);
   void erase(int position)
       erase(root, position);
   void reverse(int 1,int r)
       reverse(root,1,r);
     elementAt(int position)
       return elementAt(root, position);
```

```
void cyclic_shift(int L,int R)
                                                                                                                    void merge (item * & t, item * 1, item * r)
                                                        int main()
       cyclic_shift(root,L,R);
                                                                                                                        if (!l || !r)
                                                                                                                           t = 1 ? 1 : r;
                                                           return 0;
                                                                                                                        else if (l->prior > r->prior)
   int size()
                                                                                                                           merge (1->r, 1->r, r), t = 1;
       return cnt(root);
                                                        2.6
                                                              Treap
                                                                                                                            merge (r->1, 1, r->1), t = r;
   void output(vector<T> &arr)
                                                        #include<bits/stdc++.h>
                                                                                                                        upd_cnt(t);
                                                        #include<math.h>
                                                        #include<vector>
       output(root,arr);
                                                        #include<stdlib.h>
                                                                                                                    void erase (item * & t, T key)
                                                        using namespace std;
#define MAX 400005
};
                                                                                                                        if (t->key == key)
                                                        #define MOD 998244353
                                                                                                                            merge (t, t->1, t->r);
     Mo Algorithm
                                                        #define INF 200000000
                                                        template <class T>
                                                                                                                            erase (key < t->key ? t->1 : t->r, key);
#include<bits/stdc++.h>
                                                        class treap
                                                                                                                        upd_cnt(t);
using namespace std;
#define MOD 998244353
                                                            struct item
#define MAX 200005
#define MAX BIT 50
                                                                                                                    T elementAt(item * &t, int key)
                                                                int prior, cnt;
#define PRECISION 0.0000000001
                                                               T key;
#define INF 2000000000
                                                                                                                        T ans;
void remove(int idx); // TODO: remove value at idx from data item *1 *r
                                                                                                                        if(cnt(t->1)==key) ans=t->key;
void add(int idx); // TODO: add value at idx from data structure int get_answer(); // TODO: extract the current answer of the data structure
                                                                                                                        else if(cnt(t->1)>key) ans=elementAt(t->1,key):
                                                                                                                        else ans=elementAt(t->r,key-1-cnt(t->1));
int block_size;
                                                                   1=ŇULĹ:
                                                                                                                        upd cnt(t):
struct Query {
                                                                   r=NULL;
                                                                                                                        return ans;
   int 1, r,k, idx;
                                                                   cnt=1;
   bool operator<(Query other) const</pre>
                                                                   prior=rand();
                                                                                                                    item * unite (item * 1, item * r)
       if(1/block_size!=other.1/block_size) return (1<other=bot.*node;
                                                                                                                        if (!1 || !r) return 1 ? 1 : r;
       return (1/block_size&1)? (r<other.r) : (r>other.r) int cnt (item * it)
                                                                                                                        if (l->prior < r->prior) swap (l, r);
                                                                                                                        item * lt, * rt;
};
                                                               return it ? it->cnt : 0;
                                                                                                                        split (r, 1->key, lt, rt);
vector<int> mo_s_algorithm(vector<Query> queries) {
                                                                                                                        1->1 = unite (1->1. lt):
   vector<int> answers(queries.size());
                                                                                                                        1->r = unite (1->r, rt);
                                                            void upd_cnt (item * it)
   sort(queries.begin(), queries.end());
                                                                                                                        upd_cnt(1);
   // TODO: initialize data structure
                                                               if (it)
                                                                                                                        upd_cnt(r);
                                                                                                                        return 1;
                                                                   it->cnt = cnt(it->1) + cnt(it->r) + 1;
   int cur_1 = 0;
   int cur_r = -1;
                                                                                                                    void heapify (item * t)
   // invariant: data structure will always reflect the rangespre-ditemerat, T key, item * & 1, item * &
   for (Query q : queries) {
                                                                                                                        if (!t) return;
       while (cur_1 > q.1) {
                                                                if (!t)
                                                                                                                        item * max = t;
           cur_1--;
                                                                   1 = r = NULL;
                                                                                                                        if (t->1 != NULL && t->1->prior > max->prior)
           add(cur_1);
                                                               else if (key < t->key)
                                                                                                                            max = t->1:
                                                                   split (t->1, key, 1, t->1), r = t;
                                                                                                                        if (t->r != NULL && t->r->prior > max->prior)
       while (cur_r < q.r) {</pre>
                                                                                                                            max = t->r;
           cur_r++;
                                                                   split (t\rightarrow r, key, t\rightarrow r, r), l = t;
                                                                                                                        if (max != t)
           add(cur_r);
                                                                upd_cnt(t);
                                                                                                                            swap (t->prior, max->prior);
       while (cur_1 < q.1) {
                                                                                                                            heapify (max);
           remove(cur_1);
                                                            void insert (item * & t, item * it)
           cur_1++;
                                                               if (!t)
       while (cur_r > q.r) {
                                                                   t = it;
                                                                                                                    item * build (T * a, int n)
                                                               else if (it->prior > t->prior)
           remove(cur_r);
           cur_r--;
                                                                   split (t, it->key, it->l, it->r), t = it;
                                                                                                                        if (n == 0) return NULL;
                                                                                                                        int mid = n / 2;
       answers[q.idx] = get_answer();
                                                                   insert (it->key < t->key ? t->l : t->r, it);
                                                                                                                        item * t = new item (a[mid], rand ());
                                                                upd_cnt(t);
                                                                                                                        t->1 = build (a, mid);
   return answers;
                                                                                                                        t->r = build (a + mid + 1, n - mid - 1);
```

```
heapify (t);
       return t;
   void output (item * t,vector<T> &arr)
       if (!t) return;
       output (t->1,arr);
       arr.push_back(t->key);
       output (t->r,arr);
public:
   treap()
       root=NULL;
   treap(T *a,int n)
       build(a,n);
   void insert(T value)
       node=new item(value);
       insert(root, node);
   void erase(T value)
       erase(root, value);
     elementAt(int position)
       return elementAt(root, position);
   int size()
       return cnt(root);
   void output(vector<T> &arr)
       output(root,arr);
   int range_query(T 1,T r) //(1,r]
       item *previous,*next,*current;
       split(root,1,previous,current);
       split(current, r, current, next);
       int ans=cnt(current);
       merge(root,previous,current);
       merge(root,root,next);
       previous=NULL;
       current=NULL;
       next=NULL;
       return ans;
};
```

2.7 sparse table 2d

```
int st[K][K][N][N]; int lg[N];
void pre() {
 lg[1] = 0;
 for (int i=2; i<N; i++) lg[i] = lg[i/2]+1;
int query(int 11, int r1, int 12, int r2) {
```

```
int xx = lg[12-11+1], yy = lg[r2-r1+1];
  return max(max(st[xx][yy][l1][r1]
        st[xx][yy][12-(1<<xx)+1][r1]),
max(st[xx][yy][11][r2-(1<<yy)+1],
        st[xx][yy][12-(1<<xx)+1][r2-(1<<yy)+1]);
void build() {
 for (int x=0; x<K; x++) {</pre>
   for (int y=0; y<K; y++) {</pre>
     for (int i=1; i<=n; i++) {
       for (int j=1; j<=m; j++) {</pre>
          if (i+(1<< x)-1>n | j+(1<< y)-1>m)
            continue;
          if (!x&&!y) st[0][0][i][j]=flag[i][j];
          else if (x>0) st[x][y][i][j] =
\max(st[x-1][y][i][j],st[x-1][y][i+(1<<(x-1))][j]);
          else if (y>0) st[x][y][i][j] =
\max(st[x][y-1][i][j], st[x][y-1][i][j+(1<<(y-1))]);
    Flow
```

Dinic's Algorithm

```
#include<bits/stdc++.h>
#include<vector>
using namespace std;
#define MAX 100
#define HUGE_FLOW 1000000000
#define BEGIN 1
#define DEFAULT_LEVEL 0
struct FlowEdge {
   int v, u;
   long long cap, flow = 0;
struct Dinic {
   const long long flow_inf = 1e18;
   vector<FlowEdge> edges;
   vector<vector<int>> adj;
   int n, m = 0;
   int s, t;
   vector<int> level, ptr;
   queue<int> q;
   Dinic(int n, int s, int t) : n(n), s(s), t(t) {
       adj.resize(n);
       level.resize(n);
       ptr.resize(n);
   void add_edge(int v, int u, long long cap) {
       edges.emplace_back(v, u, cap);
       edges.emplace_back(u, v, 0);
       adj[v].push_back(m);
       adj[u].push_back(m + 1);
   bool bfs() {
       while (!q.empty()) {
```

```
int v = q.front();
                                                               q.pop();
                                                               for (int id : adj[v]) {
                                                                  if (edges[id].cap - edges[id].flow < 1)</pre>
                                                                  if (level[edges[id].u] != -1)
                                                                       continue;
                                                                  level[edges[id].u] = level[v] + 1;
                                                                  q.push(edges[id].u);
                                                           return level[t] != -1;
                                                       long long dfs(int v, long long pushed) {
                                                           if (pushed == 0)
                                                               return 0;
                                                           if (v == t)
                                                               return pushed;
                                                           for (int& cid = ptr[v]; cid < (int)adj[v].size</pre>
                                                               int id = adj[v][cid];
                                                               int u = edges[id].u;
                                                               if (level[v] + 1 != level[u] || edges[id].c
                                                               long long tr = dfs(u, min(pushed, edges[id]
                                                               if (tr == 0)
                                                                  continue;
                                                               edges[id].flow += tr;
                                                               edges[id ^ 1].flow -= tr;
                                                               return tr;
                                                           return 0;
                                                       long long flow() -
                                                           long long f = 0;
                                                           while (true) {
FlowEdge(int v, int u, long long cap): v(v), u(u), cap(cap)fill(level.begin(), level.end(), -1); level[s] = 0;
                                                               q.push(s)
                                                               if (!bfs())
                                                                  break;
                                                               fill(ptr.begin(), ptr.end(), 0);
                                                               while (long long pushed = dfs(s, flow_inf))
                                                                  f += pushed;
                                                           return f;
                                                    int main()
                                                       return 0:
                                                        Edmond's Blossom Algorithm
```

```
/***Copied from https://codeforces.com/blog/entry/4940
V->number of vertices
E->number of edges
pair of vertices as edges (vertices are 1..V)
```

```
GIVES:
output of edmonds() is the maximum matching
match[i] is matched pair of i (-1 if there isn't a matched pair)
#include <bits/stdc++.h>
using namespace std:
const int M=500;
struct struct_edge
   int v;
   struct_edge* n;
typedef struct_edge* edge;
struct_edge pool[M*M*2];
edge top=pool,adj[M];
int V,E,match[M],qh,qt,q[M],father[M],base[M];
bool inq[M],inb[M],ed[M][M];
void add_edge(int u,int v)
   top->v=v,top->n=adj[u],adj[u]=top++;
   top->v=u,top->n=adj[v],adj[v]=top++;
int LCA(int root,int u,int v)
   static bool inp[M];
   memset(inp,0,sizeof(inp));
   while(1)
       inp[u=base[u]]=true;
       if (u==root) break;
       u=father[match[u]];
   while(1)
       if (inp[v=base[v]]) return v;
       else v=father[match[v]];
void mark_blossom(int lca,int u)
   while (base[u]!=lca)
       int v=match[u];
       inb[base[u]]=inb[base[v]]=true;
       u=father[v];
       if (base[u]!=lca) father[u]=v;
void blossom_contraction(int s,int u,int v)
   int lca=LCA(s,u,v);
   memset(inb,0,sizeof(inb));
   mark_blossom(lca,u);
   mark_blossom(lca,v);
   if (base[u]!=lca)
       father[u]=v;
   if (base[v]!=lca)
       father[v]=u;
   for (int u=0; u<V; u++)
    if (inb[base[u]])
    {</pre>
           base[u]=lca;
```

```
if (!inq[u])
               inq[q[++qt]=u]=true;
int find_augmenting_path(int s)
   memset(inq,0,sizeof(inq));
   memset(father,-1,sizeof(father));
   for (int i=0; i<V; i++) base[i]=i;</pre>
   inq[q[qh=qt=0]=s]=true;
   while (qh<=qt)
       int u=q[qh++];
       for (edge e=adj[u]; e; e=e->n)
           int v=e->v:
           if (base[u]!=base[v]&&match[u]!=v)
               if ((v==s)||(match[v]!=-1 && father[ma#define MOD 1000000007
                   blossom_contraction(s,u,v);
               else if (father[v]==-1)
                   father[v]=u;
                   if (match[v] == -1)
                      return v;
                   else if (!inq[match[v]])
                      inq[q[++qt]=match[v]]=true;
   return -1;
int augment_path(int s,int t)
   int u=t,v,w;
   while (\dot{\mathbf{u}}!=-1)
       v=father[u];
       w=match[v];
       match[v]=u:
       match[u]=v:
   return t!=-1;
int edmonds()
   int matchc=0;
   memset(match,-1,sizeof(match));
   for (int u=0; u<V; u++)</pre>
       if (match[u] == -1)
           matchc+=augment_path(u,find_augmenting_path(u));
   return matchc:
int main()
                                                        //x - current vertex,prevx - vertex from X before x ir
   FILE *in=stdin;
                                                        //so we add edges (prevx, xy[x]), (xy[x], x)
   fscanf(in, "%d", &V);
   while(fscanf(in, "%d %d", &u, &v)!=EOF)
       if (!ed[u-1][v-1])
{
           add_edge(u-1,v-1);
```

```
ed[u-1][v-1]=ed[v-1][u-1]=true;
   printf("%d\n",2*edmonds());
   for (int i=0; i<V; i++)</pre>
       if (i<match[i])</pre>
           printf("%d %d\n",i+1,match[i]+1);
     Hungarian Algorithm
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define FASTIO ios_base::sync_with_stdio(false);cin.ti
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class HungarianAlgorithm
    int N,inf,n,max_match;
   int *1x,*1y,*xy,*yx,*slack,*slackx,*prev;
```

int **cost;

bool *S,*T;

void init_labels()

void update_labels()

for(int x=0; x<n; x++) lx[x]=0;

for(int y=0; y< n; y++) ly[y]=0;

for (int y = 0; y < n; y++)
lx[x] = max(lx[x], cost[x][y]);</pre>

int x, y, delta = inf; //init delta as infinity

for (y = 0; y < n; y++) //calculate delta using

delta = min(delta, slack[y]);

for (y = 0; y < n; y++) //update slack array if (!T[y])

prev[x] = prevx; //we need this when augmenting

for (int y = 0; y < n; y++) //update slacks, be

if (lx[x] + ly[y] - cost[x][y] < slack[y])

slack[y] = lx[x] + ly[y] - cost[x][y];

for (x = 0; x < n; x++) //update X labels

for (y = 0; y < n; y++) //update Y labels

if (S[x]) lx[x] -= delta;

if (T[y]) ly[y] += delta;

slack[y] -= delta;

void add_to_tree(int x, int prevx)

S[x] = true; //add x to S

for (int x = 0; x < n; x++)</pre>

```
slackx[v] = x;
                                                                          if (yx[y] == -1) //exposed vertex in Y foundeletaughenackx; path exists!
                                                                                                                      delete []prev;
                                                                             x = slackx[y];
                                                                                                                      delete []S;
   void augment() //main function of the algorithm
                                                                              break;
                                                                                                                      delete []T;
                                                                                                                      int i;
                                                                                                                      for(i=0: i<N: i++)</pre>
       if (max_match == n) return; //check wether matching is already perfect
       int x, y, root; //just counters and root vertex
       int q[N], wr = 0, rd = 0; //q - queue for bfs, wr,rd - write and re\overline{d}[y] = true; //else just add y to T,
                                                                                                                          delete [](cost[i]);
                                                                             if (!S[yx[y]])
//pos in queue
                                                                                                                      delete []cost;
       //memset(S, false, sizeof(S)); //init set S
                                                                                 q[wr++] = yx[y]; //add vertex yx[y], which is matched with
       for(int i=0;i<n;i++) S[i]=false;</pre>
                                                                                                                  void setCost(int i,int j,int c)
       //memset(T, false, sizeof(T)); //init set T
                                                       //y, to the queue
                                                                                 add_to_tree(yx[y], slackx[y]); {\( / \) and add edges (x,y) and (y,
       for(int i=0;i<n;i++) T[i]=false;</pre>
                                                                                                                      cost[i][j]=c;
       //memset(prev, -1, sizeof(prev)); //init set brew Lyfbrtthealtragating tree
       for(int i=0;i<n;i++) prev[i]=-1;</pre>
                                                                                                                  int* matching(bool first=true)
       for (x = 0; x < n; x++) //finding root of the tree
                                                                                                                      int *ans;
           if (xy[x] == -1)
                                                                                                                      ans=new int[N];
                                                                  if (y < n) break; //augmenting path found
                                                                                                                      for(int i=0;i<N;i++)</pre>
               q[wr++] = root = x;
                                                              if (y < n) //we found augmenting path!
              prev[x] = -2;
                                                                                                                          if(first) ans[i]=xy[i];
               S[x] = true;
                                                                                                                          else ans[i]=yx[i];
                                                                  max_match++; //increment matching
               break;
                                                       //in this cycle we inverse edges along augmenting pa{f t}h
                                                                                                                prev[cxturn ansty)
                                                                  for (int cx = x, cy = y, ty; cx != -2; cx |=
       for (y = 0; y < n; y++) //initializing slack array</pre>
                                                                                                                  int hungarian()
                                                                      ty = xy[cx];
                                                                      yx[cy] = cx;
           slack[y] = lx[root] + ly[y] - cost[root][y];
                                                                                                                      int ret = 0; //weight of the optimal matching
                                                                      xy[cx] = cy;
           slackx[y] = root;
                                                                                                                      max_match = 0; //number of vertices in current
                                                                                                               of the for (int x=0; x<n; x++) xy[x]=-1; for (int y=0; y<n; y++) yx[y]=-1;
                                                                  augment(); //recall function, go to step
       while (true) //main cycle
                                                                                                                      init_labels(); //step 0
           while (rd < wr) //building tree with bfs dycle}//end of augment() function
                                                                                                                      augment(); //steps 1-3
                                                                                                                      for (int x = 0; x < n; x++) //forming answer the
              x = q[rd++]; //current vertex from X part HungarianAlgorithm(int vv,int inf=1000000000)
                                                                                                                          ret += cost[x][xy[x]];
              for (y = 0; y < n; y++) //iterate through all edges in equality graph
                                                                                                                      return ret;
                                                              n=N:
                  if (cost[x][y] == lx[x] + ly[y] &&|!T[y])
                                                               max_match=0;
                      if (yx[y] == -1) break; //an exposed vertex int [N] int
                                                                                                               int main()
//augmenting path exists!
                                                               ly=new int[N];//labels of X and Y parts
                      T[y] = true; //else just add y to T,
                                                               xy=new int[N];//xy[x] - vertex that is matched wiskamf("%d",&T);
                      q[wr++] = yx[y]; //add vertex yx[y],
                                                             whichers matchel withry t=0;t<f;t++)
//with y, to the queue
                                                               slack=new int[N];//as in the algorithm description
                      add_to_tree(yx[y], x); //add edges (x, ylackx=ne, ylackx[y] such a vertex, that 1(slackx[y]; + 1(y) - w(slackx[y], y) = slack[y]
                                                               prev=new int[N];//array for memorizing alternating pasagin ( % , an); hungarianAlgorithm h(n);
                                                                                                                      int own[n],opposite[n];
                                                               T=new bool[N];//sets S and T in algorithm
              if (y < n) break; //augmenting path found!
                                                                                                                      for(i=0:i<n:i++)
                                                               cost=new int*[N];//cost matrix
                                                               for(int i=0; i<N; i++)</pre>
           if (y < n) break; //augmenting path found!</pre>
                                                                                                                          scanf("%d", &own[i]);
           update_labels(); //augmenting path not found, so improve labeling wr = rd = 0: cost[i]=new int[N];
           wr = rd = 0:
                                                                                                                      for(j=0;j<n;j++)
           for (y = 0; y < n; y++)
                                                                                                                          scanf("%d",&opposite[j]);
                                                           ~HungarianAlgorithm()
               //in this cycle we add edges that were add€d to the equality graph as a
                                                                                                                      for(i=0;i<n;i++)</pre>
//result of improving the labeling, we add edge (slackx[y], deletethelxree if
//and only if !T[y] && slack[y] == 0, also with this edge wededeten of the one
                                                                                                                          for(j=0;j<n;j++)
//(y, yx[y]) or augment the matching, if y was exposted
                                                              delete []xy;
              if (!T[y] && slack[y] == 0)
                                                               delete [] yx;
                                                               delete []slack;
                                                                                                                             if(own[i] == opposite[j]) v=1;
```

```
else if(own[i]>opposite[j]) v=2;
             else v=0;
             h.setCost(i,j,v);
    int ans=h.hungarian();
    printf("Case \( \frac{\frac{1}{2}}{d} \tag{\n",t+1,ans} \);
return 0;
```

3.4 Maximum Bipartite Matching

```
/** Source: https://iq.opengenus.org/hopcroft-karp-algorithmpat*/u[u] = NIL;
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std; #define MAX 300005
#define BEGIN 1
#define MOD 100000007
#define INF INT MAX
#define EPS 0.0000000001
#define CHAINS 18
#define NIL 0
#define NOT_VISITED 0
#define VISTTING 1
#define VISITED 2
#define FASTIO ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
// A class to represent Bipartite graph for
// Hopcroft Karp implementation
class BGraph
    // m and n are number of vertices on left
    // and right sides of Bipartite Graph
   int m, n;
    // adj[u] stores adjacents of left side
    // vertex 'u'. The value of u ranges from 1 to m.
    // 0 is used for dummy vertex
    std::list<int> *adj;
    // pointers for hopcroftKarp()
   int *pair_u, *pair_v, *dist;
public:
    BGraph(int m, int n); // Constructor
   void addEdge(int u, int v); // To add edge
   // Returns true if there is an augmenting path
   bool bfs();
   // Adds augmenting path if there is one beginning
    // with u
   bool dfs(int u);
   // Returns size of maximum matching
    int hopcroftKarpAlgorithm();
};
// Returns size of maximum matching
int BGraph::hopcroftKarpAlgorithm()
```

```
q.pop();

// pair_u[u] stores pair of u in matching on left side of Bipartite Graph.

// If u docan't have any pair then pair u[u] is NII. // If this node is not NIL and can provide a sh
      // If u doesn't have any pair, then pair_u[u] is NIL
                                                                                                              if (dist[u] < dist[NIL])</pre>
      pair_u = new int[m + 1];
      // pair_v[v] stores pair of v in matching on right side of BipaGeteaGlaphe adjacent vertices of the deq
                                                                                                                    std::list<int>::iterator it;
      // If v doesn't have any pair, then pair_u[v] is NIL
                                                                                                                    for (it = adj[u].begin(); it != adj[u].end(
      pair v = new int[n + 1]:
      // dist[u] stores distance of left side vertices
                                                                                                                           int v = *it;
      dist = new int[m + 1];
                                                                                                                           // If pair of v is not considered so far
      // Initialize NIL as pair of all vertices
                                                                                                                           // i.e. (v, pair_v[v]) is not yet explo
      for (int u = 0; u <= m; u++)
                                                                                                                          if (dist[pair_v[v]] == INF)
      for (int v = 0; v \le n; v++)
                                                                                                                                  // Consider the pair and push it to
            pair_v[v] = NIL;
                                                                                                                                  dist[pair_v[v]] = dist[u] + 1;
                                                                                                                                  q.push(pair_v[v]);
      // Initialize result
      int result = 0;
                                                                                                                   }
      // Keep updating the result while there is an
      // augmenting path possible.
      while (bfs())
                                                                                                       // If we could come back to NIL using alternating
                                                                                                       // vertices then there is an augmenting path avail
             // Find a free vertex to check for a matching
                                                                                                       return (dist[NIL] != INF);
            for (int u = 1; u <= m; u++)</pre>
                   // If current vertex is free and there is
                                                                                                  // Returns true if there is an augmenting path beginni
                   // an augmenting path from current vertex
                                                                                                 bool BGraph::dfs(int u)
                   // then increment the result
                   if (pair_u[u] == NIL && dfs(u))
                                                                                                       if (u != NIL)
                          result++;
                                                                                                              std::list<int>::iterator it;
      return result;
                                                                                                              for (it = adj[u].begin(); it != adj[u].end(); -
// Returns true if there is an augmenting path available, else returdisacemitsevertex of u
                                                                                                                    int v = *it;
bool BGraph::bfs()
                                                                                                                    // Follow the distances set by BFS search
      std::queue<int> q; //an integer queue for bfs
                                                                                                                    if (dist[pair_v[v]] == dist[u] + 1)
      // First layer of vertices (set distance as 0)
                                                                                                                           // If dfs for pair of v also return tr
      for (int u = 1: u <= m: u++)
                                                                                                                           if (dfs(pair_v[v]) == true)
             // If this is a free vertex, add it to queue
                                                                                                                           { // new matching possible, store the
             if (pair_u[u] == NIL)
                                                                                                                                 pair_v[v] = u;
                                                                                                                                 pair_u[u] = v;
                                                                                                                                  return true;
                   // u is not matched so distance is 0
                   dist[u] = 0;
                   q.push(u);
            // Else set distance as infinite so that this vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a taken to real this else vertex 1/5 this next a tak
            else
                                                                                                             return false;
                   dist[u] = INF;
                                                                                                       return true;
      // Initialize distance to NIL as infinite
      dist[NIL] = INF;
                                                                                                  // Constructor for initialization
      // q is going to contain vertices of left side on BGraph::BGraph(int m, int n)
      while (!q.empty())
                                                                                                       this->m = m:
                                                                                                       this -> n = n;
             // dequeue a vertex
                                                                                                       adj = new std::list<int>[m + 1];
             int u = q.front();
```

```
// function to add edge from u to v
void BGraph::addEdge(int u, int v)
   adj[u].push_back(v); // Add v to us list.
    Minimum Cost Maximum Flow
struct Edge
   int from, to, capacity, cost;
vector<vector<int>> adj, cost, capacity;
const int INF = 1e9;
void shortest_paths(int n, int v0, vector<int>& d, vector<infetuph 11;
   d.assign(n, INF);
   d[v0] = 0;
   vector<bool> inq(n, false);
   queue<int> q;
   q.push(v0);
   p.assign(n, -1);
   while (!q.empty()) {
       int u = q.front();
       q.pop();
       inq[u] = false;
       for (int v : adj[u]) {
          if (capacity[u][v] > 0 && d[v] > d[u] + cose(u)[v][pt{a, pt b, pt c}]
              d[v] = d[u] + cost[u][v];
              p[v] = u;
              if (!inq[v]) {
                  inq[v] = true;
                  q.push(v);
          }
       }
   }
int min_cost_flow(int N, vector<Edge> edges, int K, int spt init =t)a[0], p2 = a.back();
   adj.assign(N, vector<int>());
   cost.assign(N, vector<int>(N, 0));
   capacity.assign(N, vector<int>(N, 0));
   for (Edge e : edges) {
       adj[e.from].push_back(e.to);
       adj[e.to].push_back(e.from);
       cost[e.from][e.to] = e.cost;
       cost[e.to][e.from] = -e.cost;
       capacity[e.from][e.to] = e.capacity;
   }
   int flow = 0;
   int cost = 0;
   vector<int> d, p;
   while (flow < K) {</pre>
       shortest_paths(N, s, d, p);
       if (d[t] == INF)
       // find max flow on that path
       int f = K - flow;
```

```
int cur = t;
       while (cur != s) {
           f = min(f, capacity[p[cur]][cur]);
           cur = p[cur];
        // apply flow
       flow += f;
       cost += f * d[t];
       cur = t;
       while (cur != s) {
           capacity[p[cur]][cur] -= f;
           capacity[cur][p[cur]] += f;
           cur = p[cur];
       return cost:
    Geo
4.1 Convex Hull
struct pt {double x, y;};
bool cmp(pt a, pt b)
   return a.x < b.x \mid \mid (a.x == b.x \&\& a.y < b.y);
return a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y)<0;
bool ccw(pt a, pt b, pt c) {
 return a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y)>0
vector<pt> a;
vector<pair<double,pair<double,double> > > pp;
void convex_hull(vector<pt>& a) {
    if (a.size() == 1)
       return;
    sort(a.begin(), a.end(), &cmp);
    vector<pt> up, down;
    up.push_back(p1);
    down.push_back(p1);
   for (int i = 1; i < (int)a.size(); i++) {</pre>
       if (i == a.size() - 1 || cw(p1, a[i], p2)) {
           while (up.size() >= 2 &&
       !cw(up[up.size()-2], up[up.size()-1], a[i]))
               up.pop_back();
           up.push_back(a[i]);
       if (i == a.size() - 1 \mid | ccw(p1, a[i], p2)) {
           while(down.size() >= 2 &&!
ccw(down[down.size()-2], down[down.size()-1], a[i]))
               down.pop_back();
           down.push_back(a[i]);
   a.clear();
```

for(int i=0;i<(int)up.size();i++)a.push_back(up[i])</pre>

for(int i=down.size()-2;i>0;i--)a.push_back(down[i])

```
4.2 Half Plane Intersection
#include <bits/stdc++.h>
#include<math.h>
#include<string.h>
using namespacē std;
#define MAX 200005
#define MOD 1009
#define SMOD 998244353
#define ROOT 318
#define GMAX 19
#define EPS 0.00000001
#define NIL 0
#define FASTIO ios_base::sync_with_stdio(false);cin.ti
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class HalfPlaneIntersection
   static double eps, inf;
public:
   struct Point
       double x, y;
       explicit Point(double x = 0, double y = 0) : x
       // Addition, substraction, multiply by constant
       friend Point operator + (const Point& p, const
          return Point(p.x + q.x, p.y + q.y);
       friend Point operator - (const Point& p, const
          return Point(p.x - q.x, p.y - q.y);
       friend Point operator * (const Point& p, const
          return Point(p.x * k, p.y * k);
       friend double cross(const Point& p, const Point
          return p.x * q.y - p.y * q.x;
// Basic half-plane struct.
   struct Halfplane
       // 'p' is a passing point of the line and 'pq'
       Point p, pq;
       double angle;
       Halfplane() {}
       Halfplane(const Point& a, const Point& b) : p(a
          angle = atan21(pq.y, pq.x);
```

```
// Check if point 'r' is outside this half-plane.
                                                                      --len:
                                                                                                                    for(i=0; i<n; i++)</pre>
   // Every half-plane allows the region to the LEFT of its line.
                                                                                                                        ans=ans+P[i].x*P[(i+1)\%n].y-P[i].y*P[(i+1)\%n].x
   bool out(const Point& r)
                                                                  // Add new half-plane
                                                                 dq.push_back(H[i]);
                                                                                                                    ans=ans/2;
printf("%.4f",ans);
       return cross(pq, r - p) < -eps;</pre>
                                                                 ++len;
                                                                                                                    return 0;
   // Comparator for sorting.
                                                      the leftmost cleanup: Check half-planes at the front against the back and vice-versa while (len > 2 kk aq[0].out(inter(dq[len-1], dq[]en 2]he Segment Intersection
   // If the angle of both half-planes is equal,
   bool operator < (const Halfplane& e) const
                                                                                                                struct pt {
       if (fabsl(angle - e.angle) < eps) return cross(pq, e.p-1-p) -back();
                                                                                                                    double x, y;
        return angle < e.angle;
                                                                                                                    bool operator < (const pt& p) const
                                                      easily while (len > 2 && dq[len-1] out(inter(dq[0], dq[th)) x<p.x-EPS||(abs(x-p.x)<EPS && y < p.y- EPS);
   // We use equal comparator for std::unique to
   bool operator == (const Halfplane& e) const
                                                                  dq.pop_front();
                                                                                                                struct line {
        return fabsl(angle - e.angle) < eps;</pre>
                                                                                                                    double a, b, c;
   // Intersection point of the lines of two half-planes if Itles assympetute yet beyon half-planes to receive the point inter(const Halfplanes s, const Halfplanes t)
                                                                                                                    line() {}
                                                                                                                   line(pt p, pt q){
    a = p.y - q.y;
                                                              ne& t)
// Reconstruct the convex polygon from the remaining halfqpHanes.x;
c = -a * p.x - b * p.y;
        double alpha = cross((t.p - s.p), t.pq) / cross(symeqtors) point> ret(len);
                                                                                                                        norm();
                                                             for(int i = 0; i+1 < len; i++)
       return s.p + (s.pq * alpha);
                                                                                                                    void norm(){
                                                                 ret[i] = inter(dq[i], dq[i+1]);
                                                                                                                        double z = sqrt(a * a + b * b);
static vector<Point> hp_intersect(vector<Halfplane>& H) }
                                                                                                                        if (abs(z) > \overline{EPS}) a /= z, b /= z, c /= z;
                                                             ret.back() = inter(dq[len-1], dq[0]);
                                                                                                                    double dist(pt p){ return a * p.x + b * p.y + c;}
   Point box[4] = // Bounding box in CCW order
                                                                                                                double det(double a, double b, double c, double d){
                                                      double HalfPlaneIntersection::eps=1e-9;
        Point(inf, inf)
                                                      double HalfPlaneIntersection::inf=1e9;
                                                                                                                    return a * d - b * c;
        Point(-inf, inf)
       Point(-inf, -inf),
                                                      int main()
                                                                                                                inline bool betw(double 1, double r, double x){
        Point(inf, -inf)
                                                          vector<HalfPlaneIntersection::Halfplane> V;
                                                                                                                    return min(1, r) \leq x + EPS && x \leq max(1,r)+EPS;
   };
                                                          vector<HalfPlaneIntersection::Point> P;
   for(int i = 0; i<4; i++) // Add bounding box half iptames
                                                                                                                bool intersect_1d(double a, double b, dbl c, dbl d)
                                                          //FASTIO;
        Halfplane aux(box[i], box[(i+1) % 4]);
                                                          int i,j;
scanf("%d",&n);
                                                                                                                    if (a > b)
        H.push_back(aux);
                                                                                                                        swap(a, b);
                                                          for(i=0; i<n; i++)</pre>
                                                                                                                    if (c > d)
                                                                                                                        swap(c, d);
   // Sort and remove duplicates
                                                                                                                    return max(a, c) \le min(b, d) + EPS;
                                                              scanf("%d",&c);
   sort(H.begin(), H.end());
                                                              HalfPlaneIntersection::Halfplane h;
   H.erase(unique(H.begin(), H.end()), H.end());
                                                                                                                |intersect(pt a,pt b,pt c,pt d,pt& left,pt& right){
                                                              HalfPlaneIntersection::Point p;
                                                                                                                    if (!intersect_1d(a.x, b.x, c.x, d.x) ||
   deque<Halfplane> dq;
                                                             for(j=0; j<c; j++)
                                                                                                                      !intersect_1d(a.y, b.y, c.y, d.y))return false;
   int len = 0:
                                                                                                                    line m(a, b); line n(c, d);
   for(int i = 0; i < int(H.size()); i++)</pre>
                                                                 scanf("%lf %lf",&p.x,&p.y);
                                                                                                                    double zn = det(m.a, m.b, n.a, n.b);
                                                                 P.push_back(p);
                                                                                                                    if (abs(zn) < EPS) {</pre>
                                                      last half-plane is redundant , dq[lef-2]); j<c; j++)
        // Remove from the back of the deque while
                                                                                                                    if (abs(m.dist(c)) > EPS || abs(n.dist(a)) > EPS)
        while (len > 1 && H[i].out(inter(dq[len-1]
                                                                                                                           return false;
                                                                                                                          (b < a) swap(a, b);
                                                                 h=HalfPlaneIntersection::Halfplane(P[j],P[(j+1)%c];;(d < c) swap(c, d);
           dq.pop_back();
                                                                 V.push_back(h);
                                                                                                                       left = max(a, c); right = min(b, d);
            --len:
                                                                                                                        return true;
                                                              P.clear();
                                                                                                                    } else {
        // Remove from the front of the deque while first half-plane is redundant
                                                                                                                left.x = right.x = -det(m.c, m.b, n.c, n.b) / zn;
       while (len > 1 && H[i].out(inter(dq[0], dq[1])) HalfPlaneIntersection::hp_intersect(V);
                                                                                                                left.y = right.y = -det(m.a, m.c, n.a, n.c) / zn;
                                                          double ans=0;
                                                                                                                return betw(a.x,b.x,left.x)&&betw(a.y,b.y,left.y) &&
                                                          n=P.size();
           dq.pop_front();
                                                                                                                    betw(c.x, d.x, left.x) && betw(c.y, d.y, left.y);
```

```
return pt(x - p.x, y - p.y);
                                                                     for(int k=j+1; k< r; k++)
                                                                                                                long long cross(const pt & p) const
     Minimum Perimeter Triangle
                                                                        upd_ans(a[i],a[j],a[k]);
                                                                                                                    return x * p.y - y * p.x;
#include <bits/stdc++.h>
#include <vector>
                                                                                                                long long dot(const pt & p) const
#include<math.h>
                                                             sort(a.begin() + 1, a.begin() + r, cmp_v());
#include<string.h>
                                                                                                                    return x * p.x + y * p.y;
                                                             return;
using namespace std;
#define MAX 300005
                                                                                                                long long cross(const pt & a, const pt & b) const
#define MOD 100000007
                                                          int m = (1 + r) >> 1;
#define SMOD 998244353
                                                          int midx = a[m].x;
return (a - *this).cross(b - *this);
#define EPS 0.000000001
                                                         rec(1, m);
#define FASTIO ios_base::sync_with_stdio(false);cin.tie(MMAC(m, r);
                                                                                                                long long dot(const pt & a, const pt & b) const
#include <ext/pb_ds/assoc_container.hpp>
                                                                                                              a.begin() + r, t.begin(), cmp_y());
return (a - *this).dot(b - *this);
                                                          merge(a.begin() + 1, a.begin() + m, a.begin() + m
#include <ext/pb_ds/tree_policy.hpp>
                                                          copy(t.begin(), t.begin() + r - 1, a.begin() + 1);
#include <ext/pb_ds/detail/standard_policies.hpp>
struct pt
                                                          int tsz = 0;
                                                                                                                long long sqrLen() const
                                                          for (int i = 1: i < r: ++i)
   double x, y;
                                                                                                                   return this->dot(*this);
   int id;
                                                             if (abs(a[i].x - midx) < mindist/2)</pre>
                                                                                                            [j].y < mindist/2; --j)
                                                                 for (int j = tsz - 1; j >= 0 && a[i].y -
struct cmp_x
                                                                                                            class pointLocationInPolygon
                                                                     if(i+1<r) upd_ans(a[i], a[i+1], t[j]);</pre>
   bool operator()(const pt & a, const pt & b) const
                                                                     if(j>0) upd_ans(a[i], t[j-1], t[j]);
                                                                                                                bool lexComp(const pt & 1, const pt & r)
       return a.x < b.x \mid | (a.x == b.x && a.y < b.y)
                                                                 t[tsz++] = a[i]:
                                                                                                                    return 1.x < r.x \mid | (1.x == r.x \&\& 1.y < r.y);
struct cmp_y
                                                                                                                int sgn(long long val)
   bool operator()(const pt & a, const pt & b) const
                                                                                                                    return val > 0 ? 1 : (val == 0 ? 0 : -1);
                                                            Minkowski
       return a.y < b.y;</pre>
                                                      #include <bits/stdc++.h>
                                                                                                                vector<pt> seq;
                                                      #include <vector>
                                                                                                                int n;
                                                      #include<math.h>
                                                                                                                pt translate;
                                                      #include<string.h>
                                                                                                                bool pointInTriangle(pt a, pt b, pt c, pt point)
int n;
                                                      using namespace std;
vector<pt> a;
                                                      #define MAX 300005
double mindist;
                                                                                                                    long long s1 = abs(a.cross(b, c));
                                                      #define BEGIN 1
pair<int, pair<int, int> > best_pair;
                                                      #define MOD 100000007
                                                                                                                    long long s2 = abs(point.cross(a, b)) + abs(point.cross(a, b))
                                                    return s1 == s2;
void upd_ans(const pt & a, const pt & b,const pt &
                                                      #define EPS 0.0000000001
   double distC = sqrt((a.x - b.x)*(a.x - b.x) + (a.y+define CHAINS 18 ));
                                                                                                            public:
                                                                                                                pointLocationInPolygon()
   double distA = sqrt((c.x - b.x)*(c.x - b.x) + (c. #defbny) *(SITINGb1y));
   double distB = sqrt((a.x - c.x)*(a.x - c.x) + (a.y*defciny)*I(SIJED 2.y));
   if (distA + distB + distC < mindist)</pre>
                                                      #define FASTIO ios_base::sync_with_stdio(false);cin.tie(NULL)
                                                      #include <ext/pb_ds/assoc_container.hpp>
                                                                                                                pointLocationInPolygon(vector<pt> & points)
       mindist = distA + distB + distC;
                                                      #include <ext/pb_ds/tree_policy.hpp>
      best_pair = make_pair(a.id, make_pair(b.id, c.id)) include <ext/pb_ds/detail/standard_policies.hpp>
                                                                                                                    prepare(points);
                                                      struct pt
                                                                                                                void prepare(vector<pt> & points)
                                                         long long x, y;
vector<pt> t;
                                                         pt() {}
                                                                                                                    seq.clear();
                                                          pt(long long _x, long long _y):x(_x), y(_y) {}
void rec(int 1, int r)
                                                                                                                    n = points.size():
                                                          pt operator+(const pt & p) const
                                                                                                                    int pos = 0;
   if (r - 1 <= 3 &&r - 1 >=2)
                                                                                                                    for(int i = 1; i < n; i++)
                                                             return pt(x + p.x, y + p.y);
       for (int i = 1; i < r; ++i)
                                                                                                                       if(lexComp(points[i], points[pos]))
                                                          pt operator-(const pt & p) const
                                                                                                                           pos = i;
          for (int j = i + 1; j < r; ++j)
```

```
vector<pt> result;
       translate.x=points[pos].x;
                                                              size_t i = 0, j = 0;
                                                                                                                 double x = max(min(a.p.x, a.q.x), min(b.p.x, b.q.x)
                                                              while(i < P.size() - 2 \mid j < Q.size() - 2)
                                                                                                                 return a.get_y(x) < b.get_y(\bar{x}) - EPS;
       translate.y=points[pos].y;
       rotate(points.begin(), points.begin() + pos, points.end());
                                                                  result.push_back(P[i] + Q[j]);
                                                                                                              structoevent {
    double x;
                                                                  auto cross = (P[i + 1] - P[i]).cross(Q[j
       seq.resize(n);
                                                                  if(cross >= 0)
                                                                                                                 int tp, id;
       for(int i = 0; i < n; i++)
                                                                      ++i;
           seq[i] = points[i + 1] - points[0];
                                                                  if(cross <= 0)</pre>
                                                                                                                 event() {}
                                                                      ++j;
                                                                                                                 event(double x, int tp, int id) : x(x), tp(tp), id
   bool pointInConvexPolygon(pt point)
                                                              return result;
                                                                                                                 bool operator<(const event& e) const {</pre>
                                                                                                                     if (abs(x - e.x) > EPS)
       point.x-=translate.x;
                                                                                                                         return x < e.x;</pre>
       point.y-=translate.y;
                                                                                                                     return tp > e.tp;
       if(seq[0].cross(point) != 0 && sgn(seq[0].cross(point)) != sgn(seq[0].cross(seq[n - 1])))
                                                       4.6 Pair of Intersecting Segments
           return false:
                                                       - 1].cross(point)) != sgn(seq[n - 1].cross(seq[0])))
#include<br/>bits/stdc++.h>
       if(seq[n - 1].cross(point) != 0 && sgn(seq[n
           return false:
                                                                                                              set<seg> s;
                                                       #include<string.h>
                                                                                                              vector < set < seg >:: iterator > where;
       if(seq[0].cross(point) == 0)
                                                       #include<vector>
           return seq[0].sqrLen() >= point.sqrLen(); |#include<string.h>
                                                                                                              set<seg>::iterator prev(set<seg>::iterator it) {
                                                       using namespace std;
                                                                                                                 return it == s.begin() ? s.end() : --it;
       int 1 = 0, r = n - 1;
                                                       #define MAX 100009
                                                       #define MAX_NODES 100005
       while (r - 1 > 1)
                                                       #define MOD 1000000007
                                                                                                              set<seg>::iterator next(set<seg>::iterator it) {
                                                       #define INF 20000000
           int mid = (1 + r)/2;
                                                      #define FASTIO ios_base::sync_with_stdio(false);cin.tie(NULL) ++it;
           int pos = mid;
                                                       const double EPS = 1E-9;
           if(seq[pos].cross(point) >= 0)1 = mid;
                                                                                                              pair<int, int> solve(const vector<seg>& a) {
           else r = mid;
                                                       struct pt {
                                                                                                                 int n = (int)a.size();
                                                          double x, y;
                                                                                                                 vector<event> e;
       int pos = 1;
       return pointInTriangle(seq[pos], seq[pos + 1], pt(0, 0), point);
                                                                                                                 for (int i = 0; i < n; ++i) {
                                                                                                                     e.push_back(event(min(a[i].p.x, a[i].q.x), +1,
                                                       struct seg {
                                                                                                                     e.push_back(event(max(a[i].p.x, a[i].q.x), -1,
    pointLocationInPolygon()
                                                          pt p, q;
int id;
                                                                                                                 sort(e.begin(), e.end());
       seq.clear();
                                                          double get_y(double x) const {
                                                              if (abs(p.x - q.x) < EPS)
                                                                                                                 s.clear();
                                                                                                                 where.resize(a.size());
                                                                  return p.y;
class Minkowski
                                                              return p.y + (q.y - p.y) * (x - p.x) / (q.x - | p.x) for (size_t i = 0; i < e.size(); ++i) {
                                                                                                                     int id = e[i].id;
                                                                                                                     if (e[i].tp == +1) {
   static void reorder_polygon(vector<pt> & P)
                                                                                                                         set<seg>::iterator nxt = s.lower_bound(a[id
                                                       bool intersect1d(double 11, double r1, double 12, double r2) {
                                                                                                                        if (nxt != s.end() && intersect(*nxt, a[id]
       size_t pos = 0;
                                                          if (11 > r1)
       for(size_t i = 1; i < P.size(); i++)</pre>
                                                              swap(11, r1);
                                                                                                                                return make_pair(nxt->id, id);
           if (prv != s.end() && intersect(*prv, a[id]
                                                          return max(11, 12) <= min(r1, r2) + EPS;</pre>
       rotate(P.begin(), P.begin() + pos, P.end());
                                                                                                                             return make_pair(prv->id, id);
                                                       int vec(const pt& a, const pt& b, const pt& c) {
public:
                                                          dguble s = (b.x - a.x) * (c.y - a.y) - (b.y - a.y) * (c.x - ahrefe [id] = s.insert(nxt, a[id]);
return abs(s) < EPS ? 0 : s > 0 ? +1 : -1;
   static vector<pt> minkowski(vector<pt> P, vector<pt>
                                                                                                                         set<seg>::iterator nxt = next(where[id]), p
       // the first vertex must be the lowest
                                                                                                                         if (nxt != s.end() && prv != s.end() && int
       reorder_polygon(P);
                                                       bool intersect(const seg& a, const seg& b)
                                                                                                                             return make_pair(prv->id, nxt->id);
       reorder_polygon(Q);
                                                                                                                         s.erase(where[id]);
       // we must ensure cyclic indexing
                                                          return intersect1d(a.p.x, a.q.x, b.p.x, b.q.x) &&
       P.push_back(P[0]);
                                                                 intersect1d(a.p.y, a.q.y, b.p.y, b.q.y) &&
       P.push_back(P[1]);
                                                                 vec(a.p, a.q, b.p) * vec(a.p, a.q, b.q) <= 0 &&
                                                                 vec(b.p, b.q, a.p) * vec(b.p, b.q, a.q) <= 0; return make_pair(-1, -1);
       Q.push_back(Q[0]);
       Q.push_back(Q[1]);
       // main part
                                                      |bool operator<(const seg& a, const seg& b)
```

```
Vertical Decomposition
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define MOD 1000000007
#define GMAX 19
#define INF 20000000000000000
#define EPS 0.00000001
#define FASTIO ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
typedef double dbl;
const dbl eps = 1e-9;
inline bool eq(dbl x, dbl y){
   return fabs(x - y) < eps;
inline bool lt(dbl x, dbl y){
   return x < y - eps;
inline bool gt(dbl x, dbl y){
   return x > y + eps;
inline bool le(dbl x, dbl y){
   return x < y + eps;
inline bool ge(dbl x, dbl y){
   return x > y - eps;
struct pt{
   inline pt operator - (const pt & p)const{
       return pt\{x - p.x, y - p.y\};
   inline pt operator + (const pt & p)const{
       return pt\{x + p.x, y + p.y\};
   inline pt operator * (dbl a)const{
       return pt\{x * a, y * a\};
   inline dbl cross(const pt & p)const{
       return x * p.y - y * p.x;
   inline dbl dot(const pt & p)const{
       return x * p.x + y * p.y;
   inline bool operator == (const pt & p)const{
       return eq(x, p.x) && eq(y, \overline{p}.y);
struct Line{
   pt p[2];
   Line(){}
   Line(pt a, pt b):p{a, b}{}
```

```
pt vec()const{
       return p[1] - p[0];
   pt& operator_[](size_t i){
       return p[i];
inline bool lexComp(const pt & 1, const pt & r){
   if(fabs(l.x - r.x) > eps){
       return 1.x < r.x;</pre>
   else return l.y < r.y;</pre>
vector<pt> interSegSeg(Line 11, Line 12){
   if(eq(11.vec().cross(12.vec()), 0)){
       if(!eq(l1.vec().cross(l2[0] - l1[0]), 0))
       return {};
if(!lexComp(l1[0], l1[1]))
           swap(11[0], 11[1]);
       if(!lexComp(12[0], 12[1]))
           swap(12[0], 12[1]);
       pt 1 = lexComp(11[0], 12[0]) ? 12[0] : 11[0];
       pt r = lexComp(11[1], 12[1]) ? 11[1] : 12[1];
       if(1 == r)
           return {1}:
       else return lexComp(1, r) ? vector<pt>{1, r} ;
   else{
       pt inter = 11[0] + 11.vec() * s;
           return {inter};
       else
           return {};
inline char get_segtype(Line segment, pt other_point){
   if(eq(segment[0].x, segment[1].x))
       return 0;
   if(!lexComp(segment[0], segment[1]))
       swap(segment[0], segment[1]);
dbl union_area(vector<tuple<pt, pt, pt> > triangles){
   vector<Line> segments(3 * triangles.size());
   vector<char> segtype(segments.size());
   for(size_t i = 0; i < triangles.size(); i++){</pre>
       pt a, b, c;
       tie(a, b, c) = triangles[i];
       segments[3 * i] = lexComp(a, b) ? Line(a, b) ! Line(bwha)e(j < evts.size()){
       segtype[3 * i] = get_segtype(segments[3 * i], c);
       segments[3 * i + 2] = lexComp(c, a)? Line(c, a) : Line(a, c); ptr;
   vector<dbl> k(segments.size()), b(segments.size());
   for(size_t i = 0; i < segments.size(); i++){</pre>
       if(segtype[i]){
```

```
k[i] = (segments[i][1].y - segments[i][0].y
                                                                                                                                         b[i] = segments[i][0].y - k[i] * segments[i
                                                                                                                         dbl ans = 0;
                                                                                                                        for(size_t i = 0; i < segments.size(); i++){</pre>
                                                                                                                                 if(!segtype[i])
                                                                                                                                 dbl l = segments[i][0].x, r = segments[i][1].x
                                                                                                                                 vector<pair<dbl, int> > evts;
                                                                                                                                 for(size_t j = 0; j < segments.size(); j++){</pre>
                                                                                                                                         if(!segtype[j] || i == j)
                                                                                                                                         dbl l1 = segments[j][0].x, r1 = segments[j]
                                                                                                                                         if(ge(l1, r) || ge(l, r1))
                                                                                                                                                  continue;
                                                                                                                                         dbl common_l = max(l, l1), common_r = min(r)
                                                                                                                                         auto pts = interSegSeg(segments[i], segment
                                                                                                                                         if(pts.empty()){
                                                                                                                                                 dbl yll = k[j] * common_l + b[j];
                                                                                                                                                 dbl yl = k[i] * common_l + b[i];
                                                                                                                                                 if(lt(yl1, yl) == (segtype[i] == 1)){
                                                                                                                                                          int evt_type = -segtype[i] * segtype
                                                                                                                                                          evts.emplace_back(common_l, evt_type
                                                                                                                                                          evts.emplace_back(common_r, -evt_type
                                                                                                                  vector<pt>close if(pts.size() == 1u){
                                                                                                                                                  dbl \ yl = k[i] * common_l + b[i], yl1 = 1
        et
dbl s = (12[0] - 11[0]).cross(12.vec()) / 11.vec().cross(12.vec().cross(12.vec().cross(12.vec().cross(12.vec().cross(12.vec().cross(12.vec().cross(12.vec().cross(12.vec().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().cross().
        pt inter = 11[0] + 11.vec() * s;

if(ge(s, 0) && le(s, 1) && le((12[0] - inter) dot(12[1] - inter)evt3.emplace_back(common_1, evt_type

evts.emplace_back(pts[0].x, -evt_type
                                                                                                                                                 yl = k[i] * common_r + b[i], yl1 = k[j]
                                                                                                                                                 if(lt(yl1, yl) == (segtype[i] == 1)){
                                                                                                                                                          evts.emplace_back(pts[0].x, evt_type
                                                                                                                                                          evts.emplace_back(common_r, -evt_tyr
                                                                                                                                         else{
                                                                                                                                                 if(segtype[j] != segtype[i] || j > i){
return (segment[1] - segment[0]).cross(other_point - segment[0]) > @vts1emplace_back(common_1, -2);
                                                                                                                                                          evts.emplace_back(common_r, 2);
                                                                                                                                 evts.emplace_back(1, 0);
                                                                                                                                 sort(evts.begin(), evts.end());
                                                                                                                                 size_t j = 0;
                                                                                                                                 int balance = 0;
                                                                                                                                        size_t ptr = j;
        segments[3 * i + 1] = lexComp(b, c) ? Line(b, c) : Line(v)hib)e;(ptr < evts.size() && eq(evts[j].first segtype[3 * i + 1] = get_segtype(segments[3 * i + 1], a); balance += evts[ptr].second;
        segments[3 * i + 2] = get_segtype(segments[3 * i + 2], b);
if(!balance && !eq(evts[j].first, r)){
                                                                                                                                                 dbl next_x = ptr == evts.size() ? r : e
                                                                                                                                                 ans -= segtype[i] * (k[i] * (next_x + e
                                                                                                                                         j = ptr;
```

```
}
   return ans/2;
int main()
   return 0;
4.8 common tangent
struct pt {
   double x, y;
   pt operator- (pt p) {
   pt res = { x-p.x, y-p.y };
       return res;
};
struct circle : pt {
   double r;
struct line {
   double a, b, c;
const double EPS = 1E-9;
double sqr (double a) {
   return a * a;
void tangents (pt c, double r1, double r2,
         vector<line> & ans) {
   double r = r2 - r1;
   double z = sqr(c.x) + sqr(c.y);
   double d = z - sqr(r);
   if (d < -EPS) return:
   d = sqrt (abs (d));
   line \bar{l}; l.a = (c.x * r + c.y * d) / z;
   1.b = (c.v * r - c.x * d) / z; 1.c = r1;
   ans.push_back (1);
vector<line> tangents (circle a, circle b) {
   vector<line> ans;
   for (int i=-1; i<=1; i+=2)
       for (int j=-1; j<=1; j+=2)
           tangents (b-a, a.r*i, b.r*j, ans);
   for (size_t i=0; i<ans.size(); ++i)</pre>
       ans[i].c = ans[i].a * a.x + ans[i].b * a.y;
   return ans;
    Graph
```

Articulation Vertex

```
int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph
vector<bool> visited;
vector<int> tin, low;
int timer;
void dfs(int v, int p = -1) {
   visited[v] = true;
   tin[v] = low[v] = timer++;
   int children=0;
   for (int to : adj[v]) {
```

```
if (to == p) continue;
       if (visited[to]) {
          low[v] = min(low[v], tin[to]);
      } else {
          dfs(to, v);
          low[v] = min(low[v], low[to]);
          if (low[to] >= tin[v] && p!=-1)
              IS_CUTPOINT(v);
          ++children;
   if(p == -1 && children > 1)
       IS_CUTPOINT(v);
void find_cutpoints() {
   timer = 0:
   visited.assign(n, false);
   tin.assign(n, -1);
   low.assign(n, -1);
   for (int i = 0; i < n; ++i) {
       if (!visited[i])
          dfs (i);
```

5.2 Strongly Connected Components

```
vector<vector<int>> adj, adj_rev;
vector<bool> used;
vector<int> order, component;
void dfs1(int v) {
   used[v] = true;
   for (auto u : adj[v])
       if (!used[u])
          dfs1(u);
   order.push_back(v);
void dfs2(int v) {
   used[v] = true;
   component.push_back(v);
   for (auto u : adj_rev[v])
       if (!used[u])
          dfs2(u);
int main() {
   int n;
   // ... read n ...
   for (;;) {
       int a, b;
       // ... read next directed edge (a,b) ...
       adj[a].push_back(b);
       adj_rev[b].push_back(a);
   used.assign(n, false);
   for (int i = 0; i < n; i++)</pre>
       if (!used[i])
          dfs1(i);
```

```
used.assign(n, false);
reverse(order.begin(), order.end());
for (auto v : order)
   if (!used[v]) {
       dfs2 (v):
       // ... processing next component ...
       component.clear();
```

Math

```
Combinatrics
#include<bits/stdc++.h>
using namespace std;
#define MAX 100000
#define MOD 1000000007
long long int fact[MAX+1],fact_inv[MAX+1];
long long int gcd(long long int a, long long int b)
   if(b==0) return a;
   else return gcd(b,a%b);
long long int egcd(long long int a, long long int b, l
   if (a == 0) {
       x = 0;
       y = 1;
       return b;
   long long int x1, y1;
   long long int d = egcd(b % a, a, x1, y1);
   x = y1 - (b / a) * x1;
   v = x1;
   return d;
long long int ModuloInverse(long long int a, long long
   long long int x,y;
   x=gcd(a,n);
   a=a/x;
   long long int res = egcd(a,n,x,y);
   x=(x^n+n)^n;
   return x;
void precal()
   fact[0] = fact_inv[0] = 1;
   for(i=1;i<=MAX;i++)</pre>
       fact[i]=(fact[i-1]*i)%MOD;
   fact_inv[i]=ModuloInverse(fact[i],MOD);
   for(i=MAX-1;i>0;i--)
       fact_inv[i]=(fact_inv[i+1]*(i+1))%MOD;
```

```
long long int C(int n,int r)
   long long int res=fact[n];
   res=(res*fact_inv[n-r])%MOD;
   res=(res*fact_inv[r])%MOD;
   return res;
int main()
   precal();
   while(true)
       int n,r;
       scanf("%d %d",&n,&r);
       long long int res=C(n,r);
       long long int mod_inv=ModuloInverse(n,MOD);
       printf("%lld %lld\n",res,mod_inv);
   return 0;
     Discrete Root
#include<bits/stdc++.h>
#include<math.h>
using namespace std;
#define MAX 100000
int prime [MAX+1], Phi [MAX+1];
void sieve()
   int i,j;
   for(i=2; i*i<=MAX; i++)</pre>
       if(prime[i]) continue;
       for(j=i; j*i<=MAX; j++)</pre>
```

```
if(prime[i*j]==0) prime[i*j]=i;
void PhiWithSieve()
   for(i=2; i<=MAX; i++)</pre>
       if(prime[i]==0)
           Phi[i]=i-1;
       else if((i/prime[i])%prime[i]==0)
           Phi[i]=Phi[i/prime[i]]*prime[i];
       else {
           Phi[i]=Phi[i/prime[i]]*(prime[i]-1);
int gcd(int a,int b)
   if(b==0) return a;
   else return gcd(b,a%b);
```

```
int powmod (int a, int b, int p) {
   int res = 1;
   while (b)
       if (b & 1)
          res = int (res * 111 * a % p), --b;
          a = int (a * 111 * a % p), b >>= 1;
   return res;
int PrimitiveRoot(int p)
   vector<int>fact;
   int phi=Phi[p];
   int n=phi;
   while(n>1)
       if(prime[n]==0)
          fact.push_back(n);
          int f=prime[n];
          while (n\%f==0)
              n=n/f;
          fact.push_back(f);
   for(res=p-1; res>1; --res)
       for(n=0; n<fact.size(); n++)</pre>
           if(powmod(res,phi/fact[n],p)==1)
              break;
       if(n>=fact.size()) return res;
   return -1;
int DiscreteLog(int a, int b, int m) {
   a \%= m, b \%= m;
   int n = sqrt(m) + 1;
   map<int, int> vals;
   for (int p = 1; p \le n; ++p)
       vals[powmod(a,(int) (1ll*p*n) %m, m)] = p;
   for (int q = 0; q <= n; ++q) {
       int cur = (powmod(a, q, m) * 111 * b) % m;
       if (vals.count(cur))
           int ans = vals[cur] * n - q;
          return ans;
   return -1;
vector<int> DiscreteRoot(int n,int a,int k)
   int g = PrimitiveRoot(n);
```

```
15
    vector<int> ans;
    int any_ans = DiscreteLog(powmod(g,k,n),a,n);
    if (anv_ans == -1)
       return ans;
   int delta = (n-1) / gcd(k, n-1);
   for (int cur = any_ans % delta; cur < n-1; cur +=</pre>
       ans.push_back(powmod(g, cur, n));
   sort(ans.begin(), ans.end());
   return ans;
     Fast Fourier Transform
#include <bits/stdc++.h>
using namespace std;
#define MOD 1000000007
#define MAX 200005
#define PMAX 55
#define PRECISION 0.000001
#define INF 200000000
#define FASTIO ios_base::sync_with_stdio(false);cin.ti
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
using cd = complex<double>;
const double PI = acos(-1);
void fft(vector<cd>& a, bool invert)
    int n = a.size();
   for(int i = 1, j = 0; i < n; i++){
       int bit = n > 1;
       for(; j&bit; bit>>=1){
           j^=bit;
       i ^= bit;
```

if(i < j)

if(invert){

for(cd &x: a) x /= n;

cd w(1);

swap(a[i], a[j]);

for(int len = 2; len <= n; len <<= 1){

for(int i = 0; i < n; i += len){</pre>

a[i+j+len/2] = u-v;

cd wlen(cos(ang), sin(ang));

a[i+j] = u+v;

w *= wlen;

double ang = 2*PI/len*(invert ? -1 : 1);

for(int j = 0; j < len/2; j++){

|vector<int> multiply(vector<int> const& a, vector<int>

cd u = a[i+j], v = a[i+j+len/2]*w;

```
vector<cd> fa(a.begin(), a.end());
   vector<cd> fb(b.begin(), b.end());
   int n = 1;
   while(n < a.size()+b.size())</pre>
       n <<= 1;
   fa.resize(n);
   fb.resize(n);
   fft(fa, false);
   fft(fb, false);
   for(int i = 0; i < n; i++)
       fa[i] *= fb[i];
   fft(fa, true);
   vector<int> result(n);
   for(int i = 0; i < n; i++)
       result[i] = round(fa[i].real());
   return result;
//Number Theoretic Transformation
long long int gcd(long long int a, long long int b)
   if(b==0) return a;
   else return gcd(b,a%b);
long long int egcd(long long int a, long long int b, long ekotog sint & fb, bloog intong intend ()); {
   if (a == 0) {
       x = 0:
       v = 1:
       return b;
   long long int x1, y1;
   long long int d = egcd(b % a, a, x1, y1);
   x = y1 - (b / a) * x1;
   v = x1;
   return d;
long long int ModuloInverse(long long int a,long long int m) int m);
   long long int x,y;
   x=\gcd(a,n);
   a=a/x;
   n=n/x;
   long long int res = egcd(a,n,x,y);
   x=(x^n+n)^n;
   return x;
const int mod = 998244353;
const int root = 15311432
const int root_1 = 469870224;
const int root_pw = 1 << 23;
void fft(vector<int> & a, bool invert) {
   int n = a.size();
   for (int i = 1, j = 0; i < n; i++) {
       int bit = n >> 1;
       for (; j & bit; bit >>= 1)
           j ^= bit;
       j ^= bit;
       if (i < j)
           swap(a[i], a[j]);
```

```
for (int len = 2; len <= n; len <<= 1) {
      int wlen = invert ? root_1 : root;
      for (int i = len; i < root_pw; i <<= 1)
         wlen = (int)(1LL * wlen * wlen % mod);
      for (int i = 0; i < n; i += len) {
         int w = 1;
         for (int j = 0; j < len / 2; j++) {
             int u = a[i+j], v = (int)(1LL * a[i+j+len/2])* w % mod);
             a[i+j] = u + v < mod ? u + v : u + v - mod 
             a[i+j+len/2] = u - v >= 0 ? u - v : u
             w = (int)(1LL * w * wlen % mod);
   }
   if (invert) {
      int n_1 = (int) ModuloInverse(n, mod);
      for (int & x : a)
         x = (int)(1LL * x * n_1 \% mod);
vector<int> multiply(vector<int> const& a, vector<int> const&b)
   vector<int> fa(a.begin(), a.end());
   int \tilde{n} = 1;
   while(n < a.size()+b.size())</pre>
      n <<= 1;
   fa.resize(n);
   fb.resize(n);
   fft(fa, false);
   fft(fb, false);
   for(int i = 0; i < n; i++)
      fa[i] = (int) (1LL*fa[i]*fb[i]%mod);
   vector<int> result(n);
   for(int i = 0; i < n; i++)
      result[i] = fa[i];
   return result;
6.4 Polynomial Algebra
#include <bits/stdc++.h>
```

```
using namespace std;
namespace algebra {
 const int inf = 1e9;
 const int magic = 500; // threshold for sizes to run the nair( albosize()) {
 namespace fft {
   const int maxn = 1 << 18;
   typedef double ftype;
   typedef complex<ftype> point;
   point w[maxn];
   const ftype pi = acos(-1);
```

```
bool initiated = 0;
    void init() {
      if(!initiated) {
        for(int i = 1; i < maxn; i *= 2) {</pre>
         for(int j = 0; j < i; j++) {
            w[i + j] = polar(ftype(1), pi * j / i);
        initiated = 1;
template<typename T>
   void ffft(T *in, point *out, int n, int k = 1) {
      if(n == 1) {
        *out = *in;
      } else {
        n /= 2;
        fft(in, out, n, 2 * k);
        fft(in + k, out + n, n, 2 * k);
        for(int i = 0; i < n; i++) {
          auto t = out[i + n] * w[i + n];
          out[i + n] = out[i] - t;
          out[i] += t;
    template<typename T>
    void mul_slow(vector<T> &a, const vector<T> &b) {
      vector<T> res(a.size() + b.size() - 1);
     for(size_t i = 0; i < a.size(); i++) {
  for(size_t j = 0; j < b.size(); j++) {</pre>
          res[i + j] += a[i] * b[j];
        = res;
    template<typename T>
   void mul(vector<T> &a, const vector<T> &b) {
  if(min(a.size(), b.size()) < magic) {</pre>
        mul_slow(a, b);
        return:
      static const int shift = 15, mask = (1 << shift)</pre>
      a.resize(n);
      static point A[maxn], B[maxn];
      static point C[maxn], D[maxn];
      for(size_t i = 0; i < n; i++) {</pre>
        A[i] = point(a[i] & mask, a[i] >> shift);
          B[i] = point(b[i] & mask, b[i] >> shift);
        } else {
         B[i] = 0;
     fft(A, C, n); fft(B, D, n);
      for(size_t i = 0; i < n; i++) {
```

```
point c0 = C[i] + conj(C[(n - i) \% n]);
                                                                                                       istream& operator >> (istream &in, modular<T> &x)
                                                                                                          return in >> x.r;
                                                                                                                                                                                                                     return ans.mod_xk(n);
          point c1 = C[i] - conj(C[(n - i) \% n]);
          point d0 = D[i] + conj(D[(n - i) \% n]);
          point d1 = D[i] - conj(D[(n - i) \% n]);
                                                                                                                                                                                                                  poly operator *= (const poly &t) {fft::mul(a, t.a)
          \bar{A}[i] = c0 * d0 - point(0, 1) * c1 * d1;
                                                                                                       template<typename T>
                                                                                                                                                                                                                  poly operator * (const poly &t) const {return poly
          B[i] = c0 * d1 + d0 * c1;
                                                                                                       struct poly {
                                                                                                          vector<T> a;
                                                                                                                                                                                                                  poly reverse(size_t n, bool rev = 0) const { // re
      fft(A, C, n); fft(B, D, n);
reverse(C + 1, C + n);
                                                                                                                                                                                                                     poly res(*this);
                                                                                                           void normalize() { // get rid of leading zeroes
                                                                                                                                                                                                                     if(rev) { // If rev = 1 then tail goes to head
                                                                                                              while(!a.empty() && a.back() == T(0)) {
       reverse(D + 1, D + n);
                                                                                                                                                                                                                         res.a.resize(max(n, res.a.size()));
                                                                                                                  a.pop_back();
       int t = 4 * n;
       for(size_t i = 0; i < n; i++) {</pre>
                                                                                                                                                                                                                      std::reverse(res.a.begin(), res.a.end());
          int64_t A0 = llround(real(C[i]) / t);
                                                                                                                                                                                                                     return res.mod_xk(n);
          T A1 = llround(imag(D[i]) / t);
                                                                                                          poly(){}
          T A2 = llround(imag(C[i]) / t);
                                                                                                          poly(T a0) : a{a0}{normalize();}
          a[i] = A0 + (A1 << shift) + (A2 << 2 * shift);
                                                                                                                                                                                                                  pair<poly, poly> divmod_slow(const poly &b) const
                                                                                                          poly(vector<T> t) : a(t){normalize();}
                                                                                                                                                                                                                      vector<T> A(a):
      return;
                                                                                                                                                                                                                      vector<T> res;
                                                                                                          poly operator += (const poly &t) {
  a.resize(max(a.size(), t.a.size()));
                                                                                                                                                                                                                      while(A.size() >= b.a.size()) {
                                                                                                                                                                                                                         res.push_back(A.back() / b.a.back());
                                                                                                              for(size_t i = 0; i < t.a.size(); i++) {</pre>
template<typename T>
                                                                                                                                                                                                                         if(res.back() != T(0)) {
                                                                                                                  a[i] += t.a[i];
T bpow(T x, size_t n) {
                                                                                                                                                                                                                            for(size_t i = 0; i < b.a.size(); i++) {</pre>
   return n? n \% 2 ? x * bpow(x, n - 1) : bpow(x * x, n / 2) : T(1); normalize();
                                                                                                                                                                                                                                A[A.size() - i - 1] -= res.back() * b.a[b.a]
                                                                                                              return *this;
template<typename T>
T bpow(T x, size_t n, T m) {
   return n ? n % 2 ? x * bpow(x, n - 1, m) % m : bpow(x *a resize(max(a.size()), t.a.size()));
                                                                                                                                                                                                                         A.pop_back();
                                                                                                                                                                                                                     std::reverse(begin(res), end(res));
                                                                                                              for(size_t i = 0; i < t.a.size(); i++) {</pre>
template<typename T>
                                                                                                                                                                                                                     return {res, A};
                                                                                                                 a[i] = t.a[i];
T gcd(const T &a, const T &b) {
   return b == T(0) ? a : gcd(b, a \% b);
                                                                                                              normalize();
                                                                                                                                                                                                                  pair<poly, poly> divmod(const poly &b) const { //
                                                                                                              return *this;
template<typename T>
                                                                                                                                                                                                                     if(deg() < b.deg()) {
T \ nCr(T \ n, int \ r) \ \{ // runs in O(r) \}
                                                                                                          poly operator + (const poly &t) const {return poly(*this)return; }{poly{0}, *this};
                                                                                                          poly operator + (const poly &t) const {return poly(*this) -= t;}
poly operator - (const poly &t) const {return poly(*this) -= t;}
int d = deg() - b.deg();
   T res(1);
   for(int i = 0; i < r; i++) {
      res *= (n - T(i));
                                                                                                          poly mod_xk(size_t k) const { // get same polynomial modf(mikn(d, b.deg()) < magic) {
      res /= (i + 1);
                                                                                                              k = min(k, a.size());
                                                                                                                                                                                                                         return divmod_slow(b);
                                                                                                              return vector<T>(begin(a), begin(a) + k);
   return res;
                                                                                                                                                                                                                     poly D = (reverse(d + 1) * b.reverse(d + 1).inv(d))
                                                                                                          poly mul_xk(size_t k) const { // multiply by x^k
                                                                                                                                                                                                                     return {D, *this - D * b};
                                                                                                              poly res(*this);
template<int m>
                                                                                                              res.a.insert(begin(res.a), k, 0);
struct modular {
                                                                                                                                                                                                                  poly operator / (const poly &t) const {return divm
   int64_t r;
                                                                                                                                                                                                                  poly operator % (const poly &t) const {return divm
   modular() : r(0) {}
   modular(int64_t rr): r(rr) {if(abs(r) >= m) r %= m; pety dip)xk(siza; t k) const { // divide by x k, droppenty const poly &t) {return *this = d
                                                                                                                                                                                                                  poly operator %= (const poly &t) {return *this = d
                                                                                                             k = min(k, a.size());
   modular inv() const {return bpow(*this, m - 2);} |
                                                                                                                                                                                                                  poly operator *= (const T &x) {
   modular operator * (const modular &t) const {return (r neturn) % of or (begin(a) + k, end(a));
                                                                                                                                                                                                                     for(auto &it: a) {
   modular operator / (const modular &t) const {return *this * t.iny();}
   modular operator += (const modular &t) {r += t.r; if (Poly mybstrisizertimnsizertimnsizert) const { // return mod_xk(rt).*tiv_xk(1)
   modular operator -= (const modular &t) {r -= t.r; if (r \ 7)\min \frac{1}{2}, m; \frac{1}{2} \frac{1}{
                                                                                                                                                                                                                     normalize();
   modular operator + (const modular &t) const {return modular wthis a size());
                                                                                                                                                                                                                     return *this;
   modular operator - (const modular &t) const {return modular(*times)or≤T}(begin(a) + 1, begin(a) + r);
  modular operator *= (const modular &t) {return *this = *this * t;}
modular operator /= (const modular &t) {return *this = *this * t;}
modular operator /= (const modular &t) {return *this = *this * t;}
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modular operator /= (const modular &t) {return *this = *this * t;}
modular operator /= (const modular &
                                                                                                              assert(!is_zero());
                                                                                                                                                                                                                         it /= x;
   bool operator == (const modular &t) const {return r == poly;}ans = a[0].inv();
   bool operator != (const modular &t) const {return r != $1.76, t a = 1;
                                                                                                                                                                                                                     normalize();
                                                                                                              while (a < n) {
                                                                                                                                                                                                                     return *this;
   operator int64_t() const {return r;}
                                                                                                                 poly C = (ans * mod_xk(2 * a)).substr(a, 2 * a);
                                                                                                                  ans -= (ans * C).mod_xk(a).mul_xk(a);
                                                                                                                                                                                                                  poly operator * (const T &x) const {return poly(*t
template<int T>
                                                                                                                                                                                                                  poly operator / (const T &x) const {return poly(*t
```

```
if(is_zero()) {
                                                                                                             cur *= zz;
void print() const {
                                                        return T(1);
  for(auto it: a) {
                                                                                                            poly w = (mulx_sq(z) * vv).substr(m, m + n).mulx_s
   cout << it << ''';
                                                      assert(a[0] == T(0));
                                                                                                            vector<T> res(n);
                                                      poly ans = T(1);
                                                                                                            for(int i = 0; i < n; i++) {
  cout << endl;</pre>
                                                       size_t a = 1;
                                                                                                             res[i] = w[i];
                                                       while(a < n) {
T eval(T x) const { // evaluates in single point x
                                                        poly C = ans.log(2 * a).div_xk(a) - substr(a, 2 * a)eturn res;
                                                        ans -= (ans * C).mod_xk(a).mul_xk(a);
                                                                                                          vector<T> chirpz(T z, int n) { // P(1), P(z), P(z^
  for(int i = int(a.size()) - 1; i >= 0; i--) {
   res *= x;
                                                                                                            auto even = \bar{c}hirpz_even(z, (n + 1) / 2);
   res += a[i];
                                                      return ans.mod_xk(n);
                                                                                                            auto odd = mulx(z).chirpz_even(z, n / 2);
                                                                                                            vector<T> ans(n);
  return res;
                                                                                                            for(int i = 0; i < n / 2; i++) {
                                                     poly pow_slow(size_t k, size_t n) { // if k is small
                                                      T& lead() { // leading coefficient
 return a.back();
                                                     poly pow(size_t k, size_t n) { // calculate p^k(n) mod xf(n % 2 == 1) {
                                                       if(is_zero()) {
                                                                                                             ans[n-1] = even.back();
int deg() const { // degree
                                                        return *this;
 return a.empty() ? -inf : a.size() - 1;
                                                                                                            return ans;
                                                       if(k < magic) {</pre>
bool is_zero() const { // is polynomial zero
                                                        return pow_slow(k, n);
                                                                                                          template<typename iter>
 return a.empty();
                                                                                                          vector<T> eval(vector<poly> &tree, int v, iter 1,
                                                       int i = leading_xk();
                                                                                                            if(r - 1 == 1) {
T operator [](int idx) const {
                                                       T j = a[i];
                                                                                                             return {eval(*1)};
                                                 a[idx]idy t = div_xk(i) / j;
 return idx >= (int)a.size() || idx < 0 ? T(0) :|
                                                                                                            } else {
                                                       return bpow(j, k) * (t.\log(n) * T(k)).\exp(n).mull_xk(i *aukt)a.mmod=xlk(tn)(r - 1) / 2;
                                                                                                             auto A = (*this % tree[2 * v]).eval(tree, 2 * v
T& coef(size_t idx) { // mutable reference at coefficient return a[idx]; auto A = (*this % tree[2 * V]).eVal(tree, 2 * V return a[idx]; with x@nto B = (*this % tree[2 * V + 1]).eval(tree, 2 * V return a[idx];
 return a[idx];
                                                      T cur = 1;
                                                                                                             A.insert(end(A), begin(B), end(B));
bool operator == (const poly &t) const {return a |== t.apoly res(*this);
                                                                                                             return A;
bool operator != (const poly &t) const {return a | != t.afor(int i = 0; i <= deg(); i++) {
                                                        res.coef(i) *= cur;
                                                        cur *= x;
                                                                                                          vector<T> eval(vector<T> x) { // evaluate polynomi
polv deriv() { // calculate derivative
  vector<T> res;
                                                                                                            int n = x.size();
                                                      return res;
                                                                                                            if(is_zero()) {
 for(int i = 1; i <= deg(); i++) {
                                                     res.push_back(T(i) * a[i]);
                                                       T cur = x;
                                                                                                            vector<poly> tree(4 * n);
  return res;
                                                       T total = 1;
                                                                                                            build(tree, 1, begin(x), end(x));
                                                      T xx = x * x;
poly integr() { // calculate integral with C = 0
                                                                                                            return eval(tree, 1, begin(x), end(x));
                                                       poly res(*this);
 vector<T> res = {0};
                                                       for(int i = 0; i <= deg(); i++) {
  for(int i = 0; i <= deg(); i++) {</pre>
                                                                                                          template<typename iter>
                                                        res.coef(i) *= total:
   res.push_back(a[i] / T(i + 1));
                                                                                                          poly inter(vector<poly> &tree, int v, iter 1, iter
                                                        total *= cur;
                                                                                                            if(r - 1 == 1) {
                                                         cur *= xx;
  return res;
                                                                                                             return {*ly / a[0]};
                                                                                                            } else {
                                                      return res;
size_t leading_xk() const { // Let p(x) = x^k * t(x), return k
                                                                                                             auto m = 1 + (r - 1) / 2;
  if(is_zero()) {
                                                     vector<T> chirpz_even(T z, int n) { // P(1), P(2^2), P(2^2), P(2^2) my. = P(2^2) (ryl) ly) / 2;
   return inf;
                                                       int m = deg();
                                                                                                             auto A = (*this % tree[2 * v]).inter(tree, 2 *
                                                       if(is_zero()) {
                                                                                                             auto B = (*this % tree[2 * v + 1]).inter(tree,
  int res = 0;
                                                        return vector<T>(n, 0);
                                                                                                             return A * tree[2 * v + 1] + B * tree[2 * v];
  while(a[res] == T(0)) {
   res++;
                                                       vector < T > vv(m + n);
                                                      T zi = z.inv();
  return res;
                                                       T zz = zi * zi;
                                                                                                        template<typename T>
                                                       T cur = zi;
                                                                                                        poly<T> operator * (const T& a, const poly<T>& b) {
poly log(size_t n) { // calculate log p(x) mod x în
                                                      T \text{ total} = 1;
                                                                                                          return b * a;
  assert(a[0] == T(1));
 assert(a[0] == 1(1));
return (deriv().mod_xk(n) * inv(n)).integr().mod_xk(n); if(i <= m) [{vv[m - i] = total;}]
                                                                                                        template<typename T>
                                                        if(i < n) \{vv[m + i] = total;\}
poly exp(size_t n) { // calculate exp p(x) mod x în
                                                                                                        poly<T> xk(int k) { // return x^k
                                                        total *= cur;
```

```
auto b = a.eval(x);
   return poly<T>{1}.mul_xk(k);
                                                         cout << clock() / double(CLOCKS_PER_SEC) << endl;</pre>
                                                         auto c = inter(x, b);
  template<typename T>
                                                         polyn md = kmul(begin(x), end(x));
 T resultant(poly<T> a, poly<T> b) { // computes resultant(poly<T) double(CLOCKS_PÉR_SEC) << endl;
    if(b.is_zero()) {
                                                         assert(c == a % md);
     return 0:
                                                         return 0;
   } else if(b.deg() == 0) {
     return bpow(b.lead(), a.deg());
   } else {
                                                       6.5 all comb
     int pw = a.deg();
                                                       vector<int> ans;
     a %= b;
     pw -= a.deg();
T mul = bpow(b.lead(), pw) * T((b.deg() & a.deg() & if)(k ≥1n.|1)k < 0) return;
                                                       void gen(int n, int k, int idx, bool rev) {
                                                              for (int i = 0; i < idx; ++i) {
     return ans * mul;
                                                                  if (ans[i])
                                                                      cout << i + 1:
  template<typename iter>
 poly<typename iter::value_type> kmul(iter L, iter R) { // county(ss "(x-a1)(x-a2)...(x-an) without building tretturn ret;
   if(R - L == 1) {
     return vector<typename iter::value_type>{-*L, 1};
                                                           ans[idx] = rev;
   } else {
                                                           gen(n-1, k-rev, idx + 1, false);
     iter M = L + (R - L) / 2;
                                                           ans[idx] = !rev:
     return kmul(L, M) * kmul(M, R);
                                                           gen(n-1, k-!rev, idx + 1, true);
                                                       void all_combinations(int n, int k) {
  template<typename T, typename iter>
 poly<T> build(vector<poly<T>> &res, int v, iter L, iterafly resize(n); evaluation tree for (x-a1)(x-a2) if(R - L == 1) {
   if(R - L == 1) {
     return res[v] = vector<T>{-*L, 1};
   } else {
                                                       6.6 gauss elimination
     iter M = L + (R - L) / 2;
     return res[v] = build(res, 2 * v, L, M) * build(pesn 20 * y equations R) m + 1 columns, m variables
                                                           calculates determinant, rank and ans [] ->value
                                                           for variables
  template<typename T>
                                                           returns {0, 1, INF} -> number of solutions */
 poly<T> inter(vector<T> x, vector<T> y) { // interpolaresdmibleuEPSolymen9al from (xi, yi) pairs
                                                       #define MAX 105
   int n = x.size():
                                                       #define INF 100000000
   vector<poly<T>> tree(4 * n);
   return build(tree, 1, begin(x), end(x)).deriv().inter where [MAX] begin(x), end(x), begin(y), end(y));
                                                       int gauss(double a[MAX][MAX],
};
                                                                double ans[MAX], int n, int m) {
using namespace algebra;
                                                         Det = 1.0, Rank = 0;
                                                         memset(where, -1, sizeof(where));
const int mod = 1e9 + 7;
                                                         for(int col=0,row = 0;col<m&&row < n; ++col) {
typedef modular<mod> base;
                                                           int sel = row;
typedef poly<br/>base> polyn;
                                                           for(int i = row+1; i < n; ++i)
  if(fabs(a[i][col])>fabs(a[sel][col])) sel=i;
using namespace algebra;
                                                           if(fabs(a[sel][col]) < EPS) {Det=0.0; continue;}</pre>
signed main() {
                                                         for(int j=0; j<=m;++j)swap(a[sel][j],a[row][j]);</pre>
                                                           if(row != sel) Det = -Det:
 ios::sync_with_stdio(0);
                                                           Det *= a[row][col];
  cin.tie(0);
 int n = 100000:
                                                           where[col] = row:
                                                           double s = (1.0 / a[row][col]);
 polyn a;
  vector<base> x;
                                                           for(int j = 0; j <= m; ++j) a[row][j] *= s;</pre>
                                                           for(int i = 0; i < n; ++i) if (i != row &&
 for(int i = 0; i <= n; i++) {
   a.a.push_back(1 + rand() \% 100):
                                                                fabs(a[i][col]) > EPS) {
   x.push_back(1 + rand() \% (2 * n));
                                                              double t = a[i][col];
                                                              for(int j = 0; j \le m; ++j)
 sort(begin(x), end(x));
                                                               a[i][j] -= a[row][j] * t;
 x.erase(unique(begin(x), end(x)), end(x));
                                                           ++row, ++Rank;
```

```
for(int i = 0; i < m; ++i)</pre>
   ans[i] = (where[i] == -1) ?0.0:a[where[i]][m];
 for(int i = Rank; i < n; ++i)</pre>
   if(fabs(a[i][m]) > EPS) return 0;
 for(int i = 0; i < m; ++i)</pre>
   if(where[i] == -1) return INF;
 return 1:
// calculates gauss modulo a prime
long long Det;
long long bigmod(long long x,
               long long pow, long long mod) {
  long long ret = 1;
  while(pow > 0) {
     if(pow & 1) ret = (ret * x) % mod;
     x = (x * x) \% mod;
     pow >>= 1;
#define INVERSE(a, m) bigmod(a, m-2, m)
int gauss(long long a[MAX][MAX],
 long long ans [MAX], int n, int m, long long mod) {
Det = 1, Rank = 0;
memset(where, -1, sizeof(where));
for(int col = 0, row = 0; col<m&&row<n;++col){</pre>
 int sel = row:
..f(x_{in})t i = row + 1; i < n; + + i)
    if(abs(a[i][col]) > abs(a[sel][col])) sel=i;
 if(!a[sel][col]) { Det = 0; continue; }
 for(int j=0;j<=m;++j) swap(a[sel][j],a[row][j]);</pre>
 if(row != sel) Det = -Det;
 Det = (Det * a[row][col]) % mod;
 where[col] = row:
                     // inverse of a[row][col]
 long long s = INVERSE(a[row][col], mod);
 for(int j = 0; j <= m; ++j)
   a[row][j] = (a[row][j] * s) % mod;
 for(int i = 0; i < n; ++i) if (i != row &&
                               a[i][col] > 0) {
    long long t = a[i][col];
    for(int j = 0; j <= m; ++j) a[i][j] =
     (a[i][i] - (a[row][i]*t)^{mod} + mod)^{mod};
 ++row, ++Rank;
for(int i = 0; i < m; ++i)
 ans[i] = (where[i] == -1) ? 0 : a[where[i]][m]:
for(int i = Rank; i < n; ++i)</pre>
 if(a[i][m]) return 0;
for(int i = 0; i < m; ++i)</pre>
 if(where[i] == -1) return INF;
return 1;
// calculates 32 times faster for modulo 2
int Det; // number of variables (must be defined)
int gauss(vector < bitset<MAX> > &a,
         bitset<MAX> &ans, int n, int m) {
 Det = 1, Rank = 0;
  memset(where, -1, sizeof(where));
  for(int col=0,row=0; col < m && row < n;++col){</pre>
     int sel = row:
```

```
for(int i = row; i < n; ++i)</pre>
       if(a[i][col]) { sel = i; break; }
      if(!a[sel][col]) { Det = 0; continue; }
      swap(a[sel], a[row]);
      if(row != sel) Det = -Det;
      Det &= a[row][col];
      where [col] = row;
      for(int i = 0; i < n; ++i)</pre>
       if (i != row&&a[i](col) > 0)a[i]^=a[row];
      ++row, ++Rank;
   for(int i = 0; i < m; ++i)
  ans[i] = (where[i] == -1)?0:a[where[i]][m];</pre>
   for(int i = Rank;i<n;++i)if(a[i][m]) return 0;</pre>
   for(int i = 0; i < m; ++i)</pre>
   if(where[i] == -1) return INF;
   return 1:
6.7 linear sieve
vector<int> lp(N+1);
vector<int> pr;
for (int i=2; i <= N; ++i) {
   if (lp[i] == 0) {</pre>
       lp[i] = i;pr.push_back(i);}
for (int j=0; j < (int)pr.size()</pre>
&& pr[j] <= lp[i] && i*pr[j] <= N; ++j)
   lp[i * pr[j]] = pr[j];
     String
7.1 Aho Corasick
const int K = 26:
struct Vertex {
    int next[K];
    bool leaf = false;
   int p = -1;
    char pch;
   int link = -1;
   int go[K];
   Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
       fill(begin(next), end(next), -1);
       fill(begin(go), end(go), -1);
};
vector<Vertex> t(1);
void add_string(string const& s) {
   int v = 0;
   for (char ch : s) {
       int c = ch - 'a';
if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace_back(v, ch);
       v = t[v].next[c]:
    t[v].leaf = true;
int go(int v, char ch);
```

```
int get_link(int v) {
    if (t[v].link == -1) {
        if (v == 0 || t[v].p == 0)
            t[v].link = 0:
           t[v].link = go(get_link(t[v].p), t[v].pch vector<int> sort_cyclic_shifts(char *s) {
    int n = strlan(a).
   return t[v].link;
int go(int v, char ch) {
    int c = ch - 'a';
    if (t[v].go[c] = -1) {
        if (t[v].next[c] != -1)
            t[v].go[c] = t[v].next[c];
           t[v].go[c] = v == 0 ? 0 : go(get_link(v), |ch); int classes = 1;
    return t[v].go[c];
7.2 Manacher's Algorithm
#include<bits/stdc++.h>
#include<vector>
using namespace std;
int main()
    int T,1;
    char s[MAX];
    gets(s);
    int n=strlen(s);
    vector<int> d1(n);
    for (int i = 0, l = 0, r = -1; i < n; i++)
        int k = (i > r)? 1: min(d1[1 + r - i], r - [i + 1); for (int i = n-1; i >= 0; i--)
       while (0 \le i - k \&\& i + k \le n \&\& s[i - k] == s[i + k]) p[--cnt[c[pn[i]]]] = pn[i];
            k++:
       d1[i] = k--;
        if (i + k > r)
            l = i - k;
            r = i + k;
    vector<int> d2(n);
    for (int i = 0, l = 0, r = -1; i < n; i++)
       int k = (i > r) ? 0 : min(d2[1 + r - i + 1], r - i + \frac{1}{2})swap(cn); while (0 \le i - k - 1) \& k i + k \le n \& k s[i - k] - 1] == s[i + k];
            k++:
        d2[i] = k--;
       if (i + k > r)
           1 = i - k - 1:
           r = i + k;
    return 0;
```

```
7.3 Suffix Array
#include<bits/stdc++.h>
#include<string.h>
using namespace std;
#define MAX 100000
    const int alphabet = 256;
    vector<int> p(n), c(n), cnt(max(alphabet, n), 0);
    for (int i = 0; i < n; i++)
        cnt[s[i]]++;
    for (int i = 1; i < alphabet; i++)</pre>
        cnt[i] += cnt[i-1];
    for (int i = 0; i < n; i++)</pre>
        p[--cnt[s[i]]] = i;
    c[p[0]] = 0;
   for (int i = 1; i < n; i++) {
    if (s[p[i]] != s[p[i-1]])
           classes++;
        c[p[i]] = classes - 1;
   vector<int> pn(n), cn(n);
   for (int h = 0; (1 << h) < n; ++h) {
        for (int i = 0; i < n; i++) {</pre>
           pn[i] = p[i] - (1 << h);
           if (pn[i] < 0)
               pn[i] += n;
       fill(cnt.begin(), cnt.begin() + classes, 0);
        for (int i = 0; i < n; i++)
           cnt[c[pn[i]]]++;
        for (int i = 1; i < classes; i++)</pre>
           cnt[i] += cnt[i-1];
        cn[p[0]] = 0;
        classes = 1;
        for (int i = 1; i < n; i++) {</pre>
           int ind=p[i] + (1 << h);</pre>
           if(ind>=n) ind=ind-n;
pair<int, int> cur = {c[p[i]], c[ind]};
           ind=p[i-1] + (1 << h);
           if(ind>=n) ind=ind-n;
           pair<int, int> prev = {c[p[i-1]], c[ind]};
           if (cur != prev)
               ++classes;
           cn[p[i]] = classes - 1;
   return p;
vector<int> suffix_array_construction(char *s) {
    int n=strlen(s);
    s[n] = '#';
   vector<int> sorted_shifts = sort_cyclic_shifts(s);
    sorted_shifts.erase(sorted_shifts.begin());
   return sorted_shifts;
vector<int> lcp_construction(char *s, vector<int> cons
    int n = strlen(s);
```

```
vector<int> rank(n, 0);
   for (int i = 0; i < n; i++)
       rank[p[i]] = i;
   int k = 0;
   vector<int> lcp(n-1, 0);
   for (int i = 0; i < n; i++) {
       if (rank[i] == n - 1) {
           k = 0:
           continue;
       int j = p[rank[i] + 1];
       while (i + k < n \&\& j + k < n \&\& s[i+k] == s[j+k]) poid process(int node)
       lcp[rank[i]] = k;
       if (k)
   return lcp;
int lcp(int i, int j) {
   int ans = 0;
   for (int k = log_n; k \ge 0; k--) {
       if (c[k][i] == c[k][i]) {
           ans += 1 << k;
           i += 1 << k;
           j += 1 << k;
   return ans;
```

7.4 Suffix Automaton

```
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define BEGIN 1
#define MOD 1000000007
#define EPS 0.0000000001
#define CHAINS 18
#define NOT_VISITED 0
#define VISITING 1
#define VISITED 2
#define FASTIO ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class SuffixAutomaton
   bool complete;
   int last;
   set<char> alphabet;
   struct state
       long long substrings,length_of_substrings;
       bool is_clone;
       map<char, int> next;
       vector<int> inv_link;
       state(int leng=0,int li=0)
```

```
21
                                                                                                        len=leng;
                                                                                                        link=li;
                                                                                                                                                                                                   if(index==str.size()) return node;
                                                                                                        first_pos=-1;
                                                                                                                                                                                                   if(!st[node].next.count(str[index])) return -1;
                                                                                                        substrings=0;
                                                                                                                                                                                                   else return find_occurrence_index(st[node].next
                                                                                                        length_of_substrings=0;
                                                                                                        endpos=1;
                                                                                                                                                                                             void klen_smallest(int node,int k,vector<char> &st
                                                                                                        shortest_non_appearing_string=0;
                                                                                                        is_clone=false;
                                                                                                                                                                                                   if(k==0) return;
                                                                                                        height=0;
                                                                                                                                                                                                   map<char, int> ::iterator mit;
                                                                                                                                                                                                   for(mit=st[node].next.begin(); mit!=st[node].next.begin();
                                                                                           véctor<state> st;
                                                                                                                                                                                                          if(st[mit->second].height>=k-1)
                                                                                                                                                                                                                 str.push_back(mit->first);
                                                                                                 map<char, int> ::iterator mit;
                                                                                                                                                                                                                klen_smallest(mit->second,k-1,str);
                                                                                                  st[node].substrings=1;
                                                                                                  st[node].shortest_non_appearing_string=st.size();
                                                                                                  if((int) st[node].next.size()<(int) alphabet.size()) st[node].shortest_non_appearing_string=1;
                                                                                                  for(mit=st[node].next.begin(); mit!=st[node].hext.end(); ++mit)
                                                                                                        if(st[mit->second].substrings==0) process(mit->second);
                                                                                                        st[node].height=max(st[node].height,1+st[mit->secondkchaightht> ::iterator mit;
                                                                                                        st[node].substrings=st[node].substrings+st[mit->secondingnus;inode].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node].length_of_substrings=st[node
                                                                                                        st[node].shortest_non_appearing_string=min(st[node].shortest_non_appearing_string,1+st[mit->seco
                                                                                                                                                                                                          if(mit==st[node].next.end()||mit->first!=(*
                                                                                                  if(st[node].link!=-1)
                                                                                                                                                                                                                str.push_back(*sit);
                                                                                                        st[st[node].link].inv_link.push_back(node);
                                                                                                                                                                                                                return:
                                                                                                                                                                                                          else if(st[node].shortest_non_appearing_str
                                                                                           void set_suffix_links(int node)
                                                                                                                                                                                                                 str.push_back(*sit);
                                                                                                                                                                                                                minimum_non_existing_string(mit->second
                                                                                                  for(i=0; i<st[node].inv_link.size(); i++)</pre>
                                                                                                        set_suffix_links(st[node].inv_link[i]);
                                                                                                        st[node].endpos=st[node].endpos+st[st[node].inv_link[i]].endpos;
                                                                                                                                                                                             void find_substrings(int node,int index,vector<cha</pre>
                                                                                           void output_all_occurrences(int v, int P_length, wector<instrib_diptof(so).push_back(make_pair(st[node].substring
                                                                                                                                                                                                   if(index==str.size()) return;
                                                                                                                                                                                                   if(st[node].next.count(str[index]))
                                                                                                 if (!st[v].is_clone)
                                                                                                        pos.push_back(st[v].first_pos - P_length + 1);
                                                                                                                                                                                                          find_substrings(st[node].next[str[index]],i
                                                                                                 for (int u : st[v].inv_link)
                                                                                                        output_all_occurrences(u, P_length, pos);
                                                                                                                                                                                                          return;
                                                                                                                                                                                                   else
                                                                                           void kth_smallest(int node,int k,vector<char> &str)
                                                                                                                                                                                                          sub_info.push_back(make_pair(0,0));
                                                                                                  if(k==0) return;
                                                                                                  map<char, int> ::iterator mit;
                                                                                                 for(mit=st[node].next.begin(); mit!=st[node].hext; end(); ++mit)
{
    void check()
                                                                                                        if(st[mit->second].substrings<k) k=k-st[mit->second].substrings;
else
if(!complete)
                                                                                                                                                                                                          process(0);
int len, link, endpos, first_pos, shortest_non appearing_stringh_back(mit->first);
appearing_stringh_back(mit->second, k-1, str);
                                                                                                                                                                                                          set_suffix_links(0);
                                                                                                                                                                                                          complete=true;
                                                                                           int find_occurrence_index(int node,int index,vectoredex'> &str)
```

```
j=st[j].next[str[i%n]];
SuffixAutomaton(set<char> &alpha)
                                                        {\tilde{\ }}SuffixAutomaton()
                                                            int i;
                                                                                                                       else
   st.push_back(state(0,-1));
                                                            for(i=0; i<st.size(); i++)</pre>
   last=0;
   complete=false;
                                                                                                                           while(j!=-1&&(!st[j].next.count(str[i%n]
   set<char>::iterator sit;
                                                               st[i].next.clear();
   for(sit=alpha.begin(); sit!=alpha.end(); sit++)
                                                               st[i].inv_link.clear();
                                                                                                                               j=st[j].link;
       alphabet.insert(*sit);
                                                           st.clear();
                                                                                                                           if(j!=-1)
                                                           alphabet.clear();
   st[0].endpos=0;
                                                                                                                               len=st[j].len+1;
                                                        void kth_smallest(int k,vector<char> &str)
                                                                                                                               j=st[j].next[str[i%n]];
void sa_extend(char c)
                                                            check();
                                                                                                                           else
   int cur = st.size();
//printf("New node (%d,%c)\n",cur,c);
                                                           kth_smallest(0,k,str);
                                                                                                                               len=0:
   st.push_back(state(st[last].len + 1));
                                                        int FindFirstOccurrenceIndex(vector<char> &str)
                                                                                                                               j=0;
   st[cur].first_pos=st[cur].len-1;
                                                            check();
   int p = last;
                                                           int ind=find_occurrence_index(0,0,str);
                                                                                                                       while(st[j].link!=-1&&st[st[j].link].len>=n
   while (p != -1 \&\& !st[p].next.count(c))
                                                           if(ind==0) return -1;
                                                           else if(ind==-1) return st.size();
                                                                                                                            j=st[j].link;
       st[p].next[c] = cur;
       //printf("Set edge %d -> %d (%c)\n",p,cur,c);
                                                           else return st[ind].first_pos+1-(int) str.size();
                                                                                                                            len=st[j].len;
       p = st[p].link;
                                                        void FindAllOccurrenceIndex(vector<char> &str,vedtor<int> &pos(len>=n) S.insert(j);
   if (p == -1)
                                                            check();
                                                                                                                   for(it=S.begin();it!=S.end();++it)
                                                            int ind=find_occurrence_index(0,0,str);
       st[cur].link = 0;
                                                           if(ind!=-1) output_all_occurrences(ind,str.size(),pos); ans=ans+st[*it].endpos;
       //printf("Set link %d -> %d\n",cur,0);
                                                        int Occurrences(vector<char> &str)
                                                                                                                   return ans;
   else
                                                            check();
       int q = st[p].next[c];
                                                                                                            vector<char> X;
                                                           int ind=find_occurrence_index(0,0,str);
       if (st[p].len + 1 == st[q].len)
                                                                                                            int main()
                                                           if(ind==0) return 1;
                                                           else if(ind==-1) return 0;
           st[cur].link = q;
                                                           else return st[ind].endpos;
           //printf("Set link %d -> %d\n",cur,q);
                                                                                                               set<char> alpha;
                                                                                                                for(i=0; i<26; i++)
                                                        void klen_smallest(int k,vector<char> &str)
       else
                                                                                                                   alpha.insert('a'+i);
                                                           check();
           int clone = st.size();
           //printf("Create clone node %d from %d\n",clonef,(pt,[0].height>=k) klen_smallest(0,k,str);
                                                                                                               SuffixAutomaton sa(alpha);
           //printf("Set link %d -> %d\n",clone,st[q]!link)
           st.push_back(state(st[p].len + 1,st[q]|.linky); minimum_non_existing_string(vector<char> &str)
                                                                                                                char c;
                                                                                                                for(i=0;; i++)
           st[clone].next = st[q].next;
                                                           check();
           st[clone].is_clone=true;
                                                                                                                   scanf("%c",&c);
                                                           int ind=find_occurrence_index(0,0,str);
           st[clone].endpos=0;
                                                                                                                   if(!('a'<=c&&c<='z')) break;
                                                            if(ind!=-1) minimum_non_existing_string(ind,str);
           st[clone].first_pos=st[q].first_pos;
                                                                                                                   sa.sa_extend(c);
           while (p != -1 \&\& st[p].next[c] == q)
                                                        long long cyclic_occurrence(vector<char> &str)
                                                                                                               int n,j;
                                                           \stackrel{->}{\text{check}}() (%c)\n",p,q,p,clone,c);
               //printf("Change transition %d -> %d
                                                                                                                scanf("%d ",&n);
               st[p].next[c] = clone;
                                                                                                                for(j=0; j<n; j++)
                                                            int i,j,len;
               p = st[p].link;
                                                           long long ans=0;
                                                                                                                   for(i=0;; i++)
                                                          int n=str.size();
, set nt ligk,q,clone);
           //printf("Change link %d -> %d : %d -> %d\n",
           //printf("Set link %d -> %d\n",cur,clone);
                                                                                                                       scanf("%c",&c);
                                                           set<int>::iterator it;
           st[q].link = st[cur].link = clone;
                                                                                                                       if(!('a'<=c&&c<='z')) break;
                                                           for(i=0, j=0, len=0; i<n*2-1; i++)
                                                                                                                       X.push_back(c);
                                                               //printf("%d->%c\n",i,str[i%n]);
                                                                                                                   long long ans=sa.cyclic_occurrence(X);
   last = cur;
                                                               if(st[j].next.count(str[i%n]))
   complete=false;
                                                                                                                   X.clear():
                                                                                                                   printf("%164d\n",ans);
                                                                   len++;
```

return 0;