DSU on Tree

```
#include<bits/stdc++.h>
#include<math.h>
#include<vector>
using namespace std;
#define MAX 100005
#define MOD 100000007
vector<int> *pvec[MAX];
vector<int> Graph[MAX];
int subtree[MAX];
int color[MAX];
int color_counter[MAX];
pair<long long int,int> Info[MAX];
int Subtree(int node,int parent=-1)
   subtree[node]=1;
   int i;
   for(i=0; i<Graph[node].size(); i++)</pre>
       if(Graph[node][i] == parent) continue;
       subtree[node] = subtree[node] + Subtree(Graph[node][i], node);
   return subtree[node];
pair<long long int,int> dfs(int node,int parent=-1,bool
    keep=false)
   int i,j,k,child,hchild=-1;
   for(i=0; i<Graph[node].size(); i++)</pre>
       if(Graph[node][i] == parent) continue;
       if(hchild==-1||subtree[hchild]<subtree[Graph[node][i]])</pre>
           hchild=Graph[node][i];
   for(i=0; i<Graph[node].size(); i++)</pre>
       if (Graph[node][i] == parent | | Graph[node][i] == hchild)
       dfs(Graph[node][i],node,false);
   if(hchild!=-1)
       Info[node] = dfs(hchild, node, true);
       pvec[node] = pvec[hchild];
   else
       pvec[node] = new vector < int > ();
   pvec[node] ->push_back(node);
   color_counter[color[node]]++
   if(color_counter[color[node]]>Info[node].second)
       Info[node].second=color_counter[color[node]];
       Info[node].first=color[node];
   else
        if(color_counter[color[node]] == Info[node].second)
       Info[node].first=Info[node].first+color[node];
   for(i=0; i<Graph[node].size(); i++)</pre>
       if(Graph[node][i] == parent | | Graph[node][i] == hchild)
```

```
child=Graph[node][i]:
       for(j=0; j<(*pvec[child]).size(); j++)</pre>
           k=(*pvec[child])[j];
           pvec[node] ->push_back(k);
           color_counter[color[k]]++
           if(color_counter[color[k]]>Info[node].second)
               Info[node].second=color_counter[color[k]]; |}
               Info[node].first=color[k];
               if(color_counter[color[k]] == Info[node].secondclude <bits/stdc++.h>
               Info[node].first=Info[node].first+color[k]; #include<math.h>
       }
   if(!keep)
       for(j=0; j<(*pvec[node]).size(); j++)</pre>
           k=(*pvec[node])[j];
           color_counter[color[k]]--;
   return Info[node];
int main()
   int n,u,v,i;
scanf("%d",&n);
   for(i=1; i<=n; i++)</pre>
       scanf("%d",&color[i]);
   for(i=1; i<n; i++)
       scanf("%d %d",&u,&v);
       Graph[u].push_back(v);
       Graph[v].push_back(u);
   Subtree(1);
   dfs(1);
   for(i=1: i<=n: i++)
       printf("%I64d ",Info[i].first);
   return 0;
```

Divide and Conquer Optimization

```
vector<long long> dp_before(n), dp_cur(n);
long long C(int i, int j);
// compute dp_cur[1], ... dp_cur[r] (inclusive)
void compute(int 1, int r, int opt1, int optr) {
   if (1 > r)
       return
   int mid = (1 + r) >> 1;
   pair<long long, int> best = {LLONG_MAX, -1};
   for (int k = optl; k <= min(mid, optr); k++) {</pre>
   best = min(best, \{(k ? dp_before[k - 1] : 0) + C(k,
        mid), k});
   dp_cur[mid] = best.first;
   int opt = best.second;
   compute(l, mid - 1, optl, opt);
   compute(mid + 1, r, opt, optr);
```

```
int solve() {
for (int i = 0; i < n; i++)
   dp_before[i] = C(0, i);
for (int i = 1: i < m: i++) {
   compute(0, n - 1, 0, n - 1);
   dp_before = dp_cur;
return dp_before[n - 1];
```

```
Li Chao Tree
#include <vector>
#include<string.h>
using namespace std;
#define MAX 200005
#define MOD 1000000007
#define INF 1000000000
#define EPS 0.0000000001
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class LiChaoTree
   long long L,R;
   bool minimize;
   int lines:
   struct Node
       complex<long long> line;
       Node *children[2];
       Node(complex<long long> ln=
            {0,1000000000000000000})
           line=ln;
           children[0]=0;
           children[1]=0;
   } *root;
   long long dot(complex<long long> a, complex<long</pre>
       long> b)
       return (conj(a) * b).real();
   long long f(complex<long long> a, long long x)
       return dot(a, \{x, 1\});
   void clear(Node* &node)
       if(node->children[0])
           clear(node->children[0]);
       if(node->children[1])
           clear(node->children[1]);
       delete node:
   void add_line(complex<long long> nw, Node* &node,
        long long 1, long long r)
       if (node==0)
           node=new Node(nw);
```

```
long long m = (1 + r) / 2;
       bool lef = (f(nw, 1) < f(node->line,
           1) &&minimize) | | ((!minimize) &&f(nw, 1) >
           f(node->line, 1));
       bool mid = (f(nw. m) < f(node->line.
           m) &&minimize) | | ((!minimize) &&f(nw, m) >
           f(node->line, m));
       if (mid)
           swap(node->line, nw);
       if(r - 1 == 1)
          return;
       else if(lef != mid)
           add_line(nw, node->children[0], 1, m);
       else
       {
           add_line(nw, node->children[1], m, r);
   long long get(long long x, Node* &node, long long 1,
        long long r)
       long long m = (1 + r) / 2;
       if(r - 1 == 1)
           return f(node->line, x);
       else if (x < m)
           if(node->children[0]==0) return f(node->line,
           if(minimize) return min(f(node->line, x),
               get(x, node->children[0], 1, m));
           else return max(f(node->line, x), get(x,
               node->children[0], 1, m));
       else
           if(node->children[1]==0) return f(node->line,
           if(minimize) return min(f(node->line, x),
               get(x, node->children[1], m, r));
           else return max(f(node->line, x), get(x,
               node->children[1], m, r));
public:
   LiChaoTree(long long l=-1000000001,long long
       r=1000000001,bool mn=false)
       L=1;
       R=r;
       root=0;
       minimize=mn:
       lines=0;
   void AddLine(pair<long long,long long> ln)
       add_line({ln.first,ln.second},root,L,R);
       lines++;
   int number_of_lines()
       return lines;
```

```
long long getOptimumValue(long long x)
       return get(x,root,L,R);
    LiChaoTree()
       if(root!=0) clear(root);
int main()
   return 0;
     \mathbf{DS}
      BIT 2D
void update(int x, int y, int val) {
 int y1;
  while (x \le max_x) {
   y1 = y;
   while (y1 <= max_y) {</pre>
     tree[x][y1] += val;
     y1 += (y1 \& -y1);
   x += (x \& -x):
      CD-anikda
// p[u] = parent of u in centroid tree
//d[x][u] = distance from u to a parent of u at level x
    of centroid tree
            if u is in subtree of centroid c, then
    d[lvl[c]][u] = dist(c, 1)
// Taken from Rezwan Arefin
// If (x, y) edge exist, then x must be in adj[y] and y
    must be in adj[x]
const int maxn = 1e5 + 10;
vector<int> adj[maxn];
int lvl[maxn], sub[maxn], p[maxn], vis[maxn],
    d[18] [maxn], ans [maxn];
void calc(int u, int par) { sub[u] = 1;
       for(int v : adj[u]) if(v - par && !vis[v])
              calc(v, u), sub[u] + sub[v];
int centroid(int u, int par, int r) {
       for(int v : adj[u]) if(v - par && !vis[v])
              if(sub[v] > r) return centroid(v, u, r);
       return u:
void dfs(int 1, int u, int par) {
    if(par + 1) d[l][u] = d[l][par] + 1;
       for(int v : adj[u]) if(v - par && !vis[v])
              dfs(1, v, u);
void decompose(int u, int par) {
       calc(u, -1);
       int c = centroid(u, -1, sub[u] >> 1);
       vis[c] = 1, p[c] = par, lvl[c] = 0;
```

if(par + 1) lvl[c] = lvl[par] + 1;

decompose(v, c);

for(int v : adj[c]) if(v - par && !vis[v])

dfs(lvl[c], c, -1);

void update(int u) {

```
for(int v = u; v + 1; v = p[v])
               ans[v] = min(ans[v], d[lvl[v]][u]);
int query(int u) {
       <u>int</u> ret = 1e9;
       for(int v = u; v + 1; v = p[v])
               ret = min(ret, ans[v] + d[lvl[v]][u]);
      HLD-Usaco
#include "bits/stdc++.h"
using namespace std;
const int N = 2e5+5;
const int D = 19:
const int S = (1 << D);
int n, q, v[N];
vector<int> adj[N];
int sz[N], p[N], dep[N];
int st[S], id[N], tp[N];
void update(int idx, int val) {
       st[idx += n] = val;
       for (idx /= 2; idx; idx /= 2)

st[idx] = max(st[2 * idx], st[2 * idx +
                    1]);
int query(int lo, int hi) {
       int ra = 0, rb = 0;
       for (lo += n, hi += n + 1; lo < hi; lo /= 2, hi
            /= 2) {
               if (lo & 1)
                       ra = max(ra, st[lo++]);
               if (hi & 1)
                       rb = max(rb, st[--hi]);
       return max(ra, rb);
int dfs_sz(int cur, int par) {
       sz[cur] = 1;
       p[cur] = par;
       for(int chi : adj[cur]) {
               if(chi == par) continue;
               dep[chi] = dep[cur] + 1;
               p[chi] = cur;
               sz[cur] += dfs_sz(chi, cur);
       return sz[cur];
int ct = 1;
void dfs_hld(int cur, int par, int top) {
       id[cur] = ct++;
       tp[cur] = top;
update(id[cur], v[cur]);
int h_chi = -1, h_sz = -1;
       for(int chi : adj[cur]) {
               if(chi == par) continue;
if(sz[chi] > h_sz) {
                       h_sz = sz[chi];
                       h_{chi} = chi;
       if(h_chi == -1) return;
```

dfs_hld(h_chi, cur, top);

2.4 HLD-anikda

```
LazySegmentTree Tree ;
int sz[MAX];
int in[MAX];
int rin[MAX]
int out [MAX]
int head[MAX];
int par[MAX];
vector<int>g[MAX];
void dfs_sz(int u,int p) {
   sz[u] = 1;
   par[u] = p;
   for(auto &v: g[u]) {
       if(v==p)continue;
       dfs_sz(v,u);
       sz[u] += sz[v];
       if(sz[v] > sz[g[u][0]])
           swap(v,g[u][0]);
void dfs_hld(int u,int p) {
   in[u] = ++t:
   rin[in[u]] = u
   for(auto v: g[u]) {
       if(v==p)continue;
       head[v] = (v == g[u][0] ? head[u] : v);
       dfs_hld(v,u);
   out[u] = t;
bool isParent(int p,int u){
   return in[p]<=in[u]&&out[u]<=out[p];</pre>
int pathQuery(int u,int v){
   int ret = -inf;
   while(true){
       if(isParent(head[u],v))break;
       ret=max(ret,Tree.queryRange(1,1,n,in[head[u]],in[u]));
       u=par[head[u]];
   swap(u,v);
   while(true){
       if(isParent(head[u],v))break;
       ret=max(ret,Tree.queryRange(1,1,n,in[head[u]],in[u]));
       u=par[head[u]];
   if(in[v] < in[u])swap(u,v);
   ret = max(ret,Tree.queryRange(1,1,n,in[u],in[v]));
```

```
return ret;
}
void updateSubTree(int u,int val){
    Tree.updateRange(1,1,n,in[u],out[u],val);
}
void buildHLD(int root){
    dfs_sz(root,root);
    head[root]=root;
    dfs_hld(root,root);
}
// call buildHLD
```

```
Implicit Treap
#include<bits/stdc++.h>
#include<math.h>
#include<vector>
#include<stdlib.h>
using namespace std;
#define MAX 200005
#define MOD 998244353
template <class T>
class implicit_treap
   struct item
       int prior, cnt;
      T value;
       bool rev;
       item *1,*r;
       item(T v)
          value=v;
          rev=false;
          1=NULL:
          r=NULL:
          cnt=1;
          prior=rand();
      }
   } *root,*node;
   int cnt (item * it)
       return it ? it->cnt : 0:
   void upd_cnt (item * it)
       if (it)
          it->cnt = cnt(it->1) + cnt(it->r) + 1;
   void push (item * it)
       if (it && it->rev)
          it->rev = false:
          swap (it->1, it->r);
          if (it->1) it->1->rev ^= true;
          if (it->r) it->r->rev ^= true;
   void merge (item * & t, item * 1, item * r)
       push (1);
       push (r);
       if (!l || !r)
          t = 1 ? 1 : r;
       else if (l->prior > r->prior)
          merge (1->r, 1->r, r), t = 1;
```

```
merge (r->1, 1, r->1), t = r:
   upd_cnt (t);
}
void split (item * t, item * & 1, item * & r, int
    kev. int add = 0)
   if (!t)
       return void( 1 = r = 0 );
   push (t);
   int cur_key = add + cnt(t->1);
   if (key <= cur_key)</pre>
       split (t->1, 1, t->1, key, add), r = t;
       split (t->r, t->r, r, key, add + 1 +
           cnt(t->1)), 1 = t;
   upd_cnt (t);
void insert(item * &t,item * element,int key)
   item *1,*r;
   split(t,1,r,key);
   merge(1,1,element);
   merge(t,1,r);
   1=NŬLL;
   r=NULL:
T elementAt(item * &t,int key)
   push(t);
   if(cnt(t->1)==key) ans=t->value;
   else if(cnt(t->1)>key) ans=elementAt(t->1,key);
   else ans=elementAt(t->r,key-1-cnt(t->l));
   return ans;
void erase (item * & t, int key)
   push(t);
   if(!t) return;
   if (key == cnt(t->1))
       merge (t, t->1, t->r);
   else if(kev<cnt(t->1))
       erase(t->1,key);
       erase(t->r, key-cnt(t->1)-1);
   upd_cnt(t);
void reverse (item * &t, int 1, int r)
   item *t1, *t2, *t3;
   split (t, t1, t2, 1);
   split (t2, t2, t3, r-l+1);
   t2->rev ^= true;
   merge (t, t1, t2);
   merge (t, t, t3);
void cyclic_shift(item * &t,int L,int R)
   if(L==R) return;
   item *1,*r,*m;
   split(t,t,l,L);
   split(1,1,m,R-L+1);
   split(1,1,r,R-L);
   merge(t,t,r);
   merge(t,t,1);
   merge(t,t,m);
   1=NŬLL;
   r=NULL
   m=NULL;
```

```
void output (item * t,vector<T> &arr)
       if (!t) return:
       push (t);
       output (t->1,arr);
       arr.push_back(t->value);
       output (t->r,arr);
public:
   implicit_treap()
       root=NULL:
   void insert(T value,int position)
       node=new item(value);
       insert(root, node, position);
   void erase(int position)
       erase(root, position);
   void reverse(int l,int r)
       reverse(root,1,r);
     elementAt(int position)
       return elementAt(root, position);
   void cyclic_shift(int L,int R)
       cyclic_shift(root,L,R);
   int size()
       return cnt(root);
   void output(vector<T> &arr)
       output(root,arr);
```

2.6 Mo Algorithm

```
#include<bits/stdc++.h>
using namespace std;
#define MOD 998244353
#define MAX 200005
#define MAX_BIT 50
#define PRECISION 0.0000000001
#define INF 200000000
void remove(int idx); // TODO: remove value at idx from
    data structure
void add(int idx); // TODO: add value at idx from data
    structure
int get_answer(); // TODO: extract the current answer of
    the data structure
int block_size;
struct Query {
   int 1, r,k, idx;
   bool operator<(Query other) const
       if(l/block_size!=other.l/block_size) return
           (1<other.1);
       return (1/block size&1)? (r<other.r) :</pre>
           (r>other.r);
```

```
vector<int> mo_s_algorithm(vector<Query> queries) {
    vector<int> answers(queries.size());
    sort(queries.begin(), queries.end());
    // TODO: initialize data structure
    int cur_1 = 0;
    int cur_r = -1;
    // invariant: data structure will always reflect the
        range [cur_1, cur_r]
    for (Query q : queries) {
       while (cur_l > q.1) {
           cur_1--;
           add(cur_1);
       while (cur_r < q.r) {</pre>
           cur_r++;
           add(cur_r);
       while (cur_1 < q.1) {</pre>
           remove(cur_1);
           cur 1++:
       while (cur_r > q.r) {
           remove(cur_r);
           cur_r--;
       answers[q.idx] = get_answer();
    return answers;
int main()
   return 0;
```

2.7 Treap

```
#include<bits/stdc++.h>
#include<math.h>
#include<vector>
#include<stdlib.h>
using namespace std;
#define MAX 400005
#define MOD 998244353
#define INF 2000000000
template <class T>
class treap
   struct item
       int prior, cnt;
       T key;
       item *1,*r;
       item(T v)
           kev=v:
           1=ŇULĹ:
           r=NULL;
           cnt=1;
           prior=rand();
       }
   } *root,*node;
   int cnt (item * it)
       return it ? it->cnt : 0;
   void upd_cnt (item * it)
       if (it)
```

```
it->cnt = cnt(it->1) + cnt(it->r) + 1:
}
void split (item * t, T key, item * & 1, item * & r)
   if (!t)
       1 = r = NULL;
   else if (key < t->key)
       split (t->1, key, 1, t->1), r = t;
       split (t\rightarrow r, key, t\rightarrow r, r), l = t;
   upd_cnt(t);
void insert (item * & t. item * it)
   if (!t)
       t = it;
   else if (it->prior > t->prior)
       split (t, it->key, it->l, it->r), t = it;
       insert (it->key < t->key ? t->l : t->r, it);
   upd_cnt(t);
}
void merge (item * & t, item * 1, item * r)
   if (!l || !r)
       t = 1 ? 1 : r:
   else if (l->prior > r->prior)
       merge (1->r, 1->r, r), t = 1;
       merge (r->1, 1, r->1), t = r;
   upd_cnt(t);
}
void erase (item * & t, T key)
   if (t->key == key)
       merge (t, t->1, t->r);
       erase (key \langle t-\ranglekey ? t->1 : t-\rangler, key);
   upd_cnt(t);
 elementAt(item * &t,int key)
   if(cnt(t->1)==key) ans=t->key;
   else if(cnt(t->1)>key) ans=elementAt(t->1,key);
   else ans=elementAt(t->r,key-1-cnt(t->l));
   upd_cnt(t);
   return ans;
item * unite (item * 1, item * r)
   if (!1 || !r) return 1 ? 1 : r;
   if (l->prior < r->prior) swap (l, r);
   item * lt, * rt;
   split (r, 1->key, lt, rt);
   1->1 = unite (1->1, 1t);
   1->r = unite (1->r, rt);
   upd_cnt(1);
   upd_cnt(r);
   return 1;
void heapify (item * t)
    if (!t) return:
   item * max = t;
```

```
if (t->l != NULL && t->l->prior > max->prior)
           max = t->1:
       if (t->r != NULL && t->r->prior > max->prior)
           \max = t->r;
       if (max != t)
           swap (t->prior, max->prior);
           heapify (max);
   }
   item * build (T * a, int n)
       if (n == 0) return NULL;
       int mid = n / 2:
       item * t = new item (a[mid], rand ());
       t->1 = build (a, mid);
       t->r = build (a + mid + 1, n - mid - 1);
       heapify (t);
       return t;
   void output (item * t,vector<T> &arr)
       if (!t) return;
       output (t->1,arr);
       arr.push_back(t->key);
       output (t->r,arr);
public:
   treap()
       root=NULL:
   treap(T *a, int n)
       build(a,n);
   void insert(T value)
       node=new item(value);
       insert(root, node);
   void erase(T value)
       erase(root, value);
     elementAt(int position)
       return elementAt(root, position);
   int size()
       return cnt(root);
   void output(vector<T> &arr)
       output(root,arr);
   int range_query(T 1,T r) //(1,r]
       item *previous,*next,*current;
       split(root,1,previous,current);
       split(current,r,current,next);
       int ans=cnt(current);
       merge(root, previous, current);
       merge(root,root,next);
       previous=NULL;
       current=NULL;
       next=NULL;
       return ans;
```

```
}
```

3 Flow

3.1 Dinic's Algorithm

```
#include<bits/stdc++.h>
#include<vector>
using namespace std;
#define MAX 100
#define HUGE_FLOW 1000000000
#define BEGIN 1
#define DEFAULT_LEVEL 0
struct FlowEdge {
   int v, u;
    long long cap, flow = 0;
    FlowEdge(int v, int u, long long cap) : v(v), u(u),
        cap(cap) {}
struct Dinic {
    const long long flow_inf = 1e18;
    vector<FlowEdge> edges;
    vector<vector<int>> adj;
    int n, m = 0;
    int s, t;
    vector<int> level, ptr;
    queue<int> q;
    Dinic(int n, int s, int t) : n(n), s(s), t(t) {
       adj.resize(n);
       level.resize(n);
       ptr.resize(n);
    void add_edge(int v, int u, long long cap) {
       edges.emplace_back(v, u, cap);
       edges.emplace_back(u, v, 0);
       adj[v].push_back(m);
       adj[u].push_back(m + 1);
    bool bfs() {
       while (!q.empty()) {
           int v = q.front();
           q.pop();
           for (int id : adj[v]) {
               if (edges[id].cap - edges[id].flow < 1)</pre>
               if (level[edges[id].u] != -1)
                   continue
               level[edges[id].u] = level[v] + 1;
               q.push(edges[id].u);
       return level[t] != -1;
    long long dfs(int v, long long pushed) {
       if (pushed == 0)
           return 0;
       if (v == t)
           return pushed;
       for (int& cid = ptr[v]; cid <</pre>
            (int)adj[v].size(); cid++) {
           int id = adj[v][cid];
           int u = edges[id].u;
           if (level[v] + 1 != level[u] || edges[id].cap
               - edges[id].flow < 1)</pre>
               continue;
```

```
long long tr = dfs(u, min(pushed,
               edges[id].cap - edges[id].flow));
           if (tr == 0)
              continue;
           edges[id].flow += tr;
           edges[id ^ 1].flow -= tr:
           return tr;
       return 0;
   }
   long long flow() {
   long long f = 0;
       while (true) {
           fill(level.begin(), level.end(), -1);
           level[s] = 0;
           q.push(s);
           if (!bfs())
              break:
           fill(ptr.begin(), ptr.end(), 0);
           while (long long pushed = dfs(s, flow_inf)) {
              f += pushed;
      return f;
int main()
   return 0;
```

3.2 Edmond's Blossom Algorithm

```
/***Copied from
    https://codeforces.com/blog/entry/49402***/
GETS:
V->number of vertices
E->number of edges
pair of vertices as edges (vertices are 1..V)
output of edmonds() is the maximum matching
match[i] is matched pair of i (-1 if there isn't a
    matched pair)
#include <bits/stdc++.h>
using namespace std;
const int M=500;
struct struct_edge
   struct_edge* n;
typedef struct_edge* edge;
struct_edge pool[M*M*2];
edge top=pool,adj[M];
int V,E,match[M],qh,qt,q[M],father[M],base[M];
bool ing[M],inb[M],ed[M][M];
void add_edge(int u,int v)
   top->v=v, top->n=adj[u], adj[u]=top++;
   top->v=u,top->n=adj[v],adj[v]=top++;
int LCA(int root,int u,int v)
   static bool inp[M];
   memset(inp,0,sizeof(inp));
   while(1)
```

```
inp[u=base[u]]=true;
       if (u==root) break;
       u=father[match[u]];
   while(1)
       if (inp[v=base[v]]) return v;
       else v=father[match[v]];
void mark_blossom(int lca,int u)
   while (base[u]!=lca)
       int v=match[u];
       inb[base[u]]=inb[base[v]]=true;
       u=father[v];
       if (base[u]!=lca) father[u]=v;
void blossom_contraction(int s,int u,int v)
   int lca=LCA(s,u,v);
   memset(inb,0,sizeof(inb));
   mark_blossom(lca,u);
   mark_blossom(lca,v);
   if (base[u]!=lca)
       father[u]=v;
   if (base[v]!=lca)
       father[v]=u;
      if (inb[base[u]])
{
   for (int u=0; u<V; u++)</pre>
           base[u]=lca;
           if (!inq[u])
              inq[q[++qt]=u]=true;
int find_augmenting_path(int s)
   memset(inq,0,sizeof(inq));
   memset(father,-1,sizeof(father));
   for (int i=0; i<V; i++) base[i]=i;</pre>
   inq[q[qh=qt=0]=s]=true;
   while (qh<=qt)</pre>
       int u=q[qh++];
       for (edge e=adj[u]; e; e=e->n)
           int v=e->v;
           if (base[u]!=base[v]&&match[u]!=v)
               if ((v==s)||(match[v]!=-1 &&
                   father [match[v]]!=-1))
                  blossom_contraction(s,u,v);
               else if (father[v]==-1)
                  father[v]=u;
                  if (match[v] == -1)
                  else if (!ing[match[v]])
                      inq[q[++qt]=match[v]]=true;
       }
   return -1;
int augment_path(int s,int t)
   int u=t,v,w;
```

```
while (u!=-1)
       v=father[u];
       w=match[v];
       match[v]=u;
       match[u]=v;
   return t!=-1;
int edmonds()
   int matchc=0;
   memset(match,-1,sizeof(match));
   for (int u=0; u<V; u++)</pre>
       if (match[u]==-1)
   return matchc;
int main()
   FILE *in=stdin;
   fscanf(in, "%d", &V);
   while(fscanf(in,"%d %d",&u,&v)!=EOF)
       if (!ed[u-1][v-1])
           add_edge(u-1,v-1);
           ed[u-1][v-1]=ed[v-1][u-1]=true;
   printf("%d\n",2*edmonds());
   for (int i=0; i<V; i++)</pre>
       if (i<match[i])</pre>
           printf("%d %d\n",i+1,match[i]+1);
   return 0:
```

|3.3 Hungarian Algorithm

```
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define MOD 1000000007
#define GMAX 19
#define INF 20000000000000000
#define EPS 0.000000001
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class HungarianAlgorithm
   int N, inf, n, max_match;
   int *lx,*ly,*xy,*yx,*slack,*slackx,*prev;
    int **cost;
   bool *S,*T;
   void init_labels()
       for(int x=0;x<n;x++) lx[x]=0;</pre>
       for(int y=0;y<n;y++) ly[y]=0;
       for (int x = 0; x < n; x++)
           for (int y = 0; y < n; y++)
              lx[x] = max(lx[x], cost[x][y]);
   void update_labels()
```

```
int x, y, delta = inf; //init delta as infinity
                                                          for (y = 0; y < n; y++) //calculate delta using
                                                               slack
                                                              if (!T[y])
                                                                  delta = min(delta, slack[y]);
                                                          for (x = 0; x < n; x++) //update X labels
                                                              if (S[x]) lx[x] -= delta;
                                                          for (y = 0; y < n; y++) //update Y labels
                                                              if (T[y]) ly[y] += delta;
                                                          for (y = 0; y < n; y++) //update slack array
                                                              if (!T[y])
                                                                  slack[v] -= delta;
                                                      void add_to_tree(int x, int prevx)
matchc+=augment_path(u,find_augmenting_path(u))//x - current vertex,prevx - vertex from X before x in
                                                       the alternating path,
                                                   //so we add edges (prevx, xy[x]), (xy[x], x)
                                                          S[x] = true; //add x to S
                                                          prev[x] = prevx; //we need this when augmenting
                                                          for (int y = 0; y < n; y++) //update slacks,
                                                               because we add new vertex to S
                                                              if (lx[x] + ly[y] - cost[x][y] < slack[y])
                                                                  slack[y] = lx[x] + ly[y] - cost[x][y];
                                                                  slackx[y] = x;
                                                      void augment() //main function of the algorithm
                                                          if (max_match == n) return; //check wether
                                                              matching is already perfect
                                                          int x, y, root; //just counters and root vertex
                                                          int q[N], wr = 0, rd = 0; //q - queue for bfs,
                                                               wr,rd - write and read
                                                  //pos in queue
                                                          //memset(S, false, sizeof(S)); //init set S
                                                          for(int i=0;i<n;i++) S[i]=false;</pre>
                                                          //memset(T, false, sizeof(T)); //init set T
for(int i=0;i<n;i++) T[i]=false;</pre>
                                                          //memset(prev, -1, sizeof(prev)); //init set
    prev - for the alternating tree
                                                          for(int i=0;i<n;i++) prev[i]=-1;</pre>
                                                          for (x = 0; x < n; x++) //finding root of the
                                                              if (xy[x] == -1)
                                                                  q[wr++] = root = x;
                                                                  prev[x] = -2;
                                                                  S[x] = true;
                                                                  break;
                                                          for (y = 0; y < n; y++) //initializing slack
array</pre>
                                                              slack[y] = lx[root] + ly[y] - cost[root][y];
                                                              slackx[v] = root;
                                                          while (true) //main cycle
                                                              while (rd < wr) //building tree with bfs cycle
                                                                  x = q[rd++]; //current vertex from X part
                                                                  for (y = 0; y < n; y++) //iterate through
                                                                      all edges in equality graph
```

```
,
```

```
if (cost[x][y] == lx[x] + ly[y] &&
                      !T[y])
                     if (yx[y] == -1) break; //an
                          exposed vertex in Y found, so
//augmenting path exists
                     T[y] = true; //else just add y to
                     q[wr++] = yx[y]; //add vertex
                          yx[y], which is matched
//with y, to the queue
                     add_to_tree(yx[y], x); //add edges
                          (x,y) and (y,yx[y]) to the tree
              }
              if (y < n) break; //augmenting path found!
           if (y < n) break; //augmenting path found!</pre>
           update_labels(); //augmenting path not found,
               so improve labeling
          wr = rd = 0;
           for (y = 0; y < n; y++)
              //in this cycle we add edges that were
                  added to the equality graph as a
//result of improving the labeling, we add edge
    (slackx[v], v) to the tree if
//and only if !T[y] && slack[y] == 0, also with this
    edge we add another one
//(y, yx[y]) or augment the matching, if y was exposed
              if (!T[y] && slack[y] == 0)
                  if (yx[y] == -1) //exposed vertex in Y
                      found - augmenting path exists!
                     x = slackx[y];
                     break;
                     T[y] = true; //else just add y to
                     if (!S[yx[y]])
                         q[wr++] = yx[y]; //add vertex
                             yx[y], which is matched
//y, to the queue
                         add_to_tree(yx[y], slackx[y]);
                              //and add edges (x,y) and
//yx[y]) to the tree
           if (v < n) break; //augmenting path found!
       if (y < n) //we found augmenting path!
           max_match++; //increment matching
//in this cycle we inverse edges along augmenting path
           for (int cx = x, cy = y, ty; cx != -2; cx =
               prev[cx], cy = ty)
              ty = xy[cx];
              yx[cy] = cx;
```

```
xy[cx] = cv;
       augment(); //recall function, go to step 1 of
}//end of augment() function
HungarianAlgorithm(int vv,int inf=1000000000)
   n=N:
   max_match=0;
   this->inf=inf;
   lx=new int[N];
   ly=new int[N];//labels of X and Y parts
   xy=new int[N];//xy[x] - vertex that is matched
   yx=new int[N];//yx[y] - vertex that is matched
        with v
   slack=new int[N];//as in the algorithm
        description
    slackx=new int[N];//slackx[y] such a vertex,
        that l(slackx[y]) + l(y) - w(slackx[y],y) =
   prev=new int[N];//array for memorizing
        alternating paths
   S=new bool[N];
   T=new bool[N];//sets S and T in algorithm
   cost=new int*[N];//cost matrix
   for(int i=0; i<N; i++)</pre>
       cost[i]=new int[N];
`HungarianAlgorithm()
   delete []lx;
   delete []ly;
   delete []xy;
   delete []yx;
   delete []slack;
delete []slackx;
   delete []prev;
   delete []$;
   delete []T;
   int i;
   for(i=0; i<N; i++)</pre>
       delete [](cost[i]);
   delete []cost;
void setCost(int i,int j,int c)
   cost[i][j]=c;
int* matching(bool first=true)
    int *ans:
   ans=new int[N];
   for(int i=0;i<N;i++)</pre>
       if(first) ans[i]=xy[i];
       else ans[i]=yx[i];
   return ans;
int hungarian()
   int ret = 0; //weight of the optimal matching
```

```
max match = 0: //number of vertices in current
           matching
       for(int x=0; x<n; x++) xy[x]=-1;
       for(int y=0; y<n; y++) yx[y]=-1;
       init_labels(); //step 0
       augment(); //steps 1-3
       for (int x = 0; x < n; x++) //forming answer
           ret += cost[x][xy[x]];
       return ret;
int main()
   int t,T=1;
scanf("%d",&T);
   for(t=0;t<T;t++)
       int n,i,j;
scanf("%d",&n);
       HungarianAlgorithm h(n);
       int own[n],opposite[n];
       for(i=0;i<n;i++)
           scanf("%d", &own[i]);
       for(j=0;j<n;j++)</pre>
           scanf("%d",&opposite[j]);
       for(i=0:i<n:i++)
           for(j=0;j<n;j++)
              if(own[i]==opposite[j]) v=1;
              else if(own[i]>opposite[j]) v=2;
              else v=0;
              h.setCost(i,j,v);
       int ans=h.hungarian();
       printf("Case %d: %d\n",t+1,ans);
   return 0;
```

3.4 Maximum Bipartite Matching

```
/** Source:
    https://iq.opengenus.org/hopcroft-karp-algorithm/
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define BEGIN 1
#define MOD 100000007
#define INF INT_MAX
#define EPS 0.0000000001
#define CHAINS 18
#define NIL 0
#define NOT_VISITED 0
#define VISTTING 1
#define VISITED 2
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
```

```
#include <ext/pb ds/detail/standard policies.hpp>
// A class to represent Bipartite graph for
// Hopcroft Karp implementation
class BGraph
   // m and n are number of vertices on left
   // and right sides of Bipartite Graph
   // adj[u] stores adjacents of left side
   // vertex 'u'. The value of u ranges from 1 to m.
   // 0 is used for dummy vertex
   std::list<int> *adj;
   // pointers for hopcroftKarp()
   int *pair_u, *pair_v, *dist;
public:
   BGraph(int m, int n); // Constructor
   void addEdge(int u, int v); // To add edge
   // Returns true if there is an augmenting path
   bool bfs();
   // Adds augmenting path if there is one beginning
   // with u
   bool dfs(int u);
   // Returns size of maximum matching
   int hopcroftKarpAlgorithm();
// Returns size of maximum matching
int BGraph::hopcroftKarpAlgorithm()
   // pair_u[u] stores pair of u in matching on left
       side of Bipartite Graph.
   // If u doesn't have any pair, then pair_u[u] is NIL
   pair_u = new int[m + 1];
   // pair_v[v] stores pair of v in matching on right
       side of Biparite Graph.
   // If v doesn't have any pair, then pair_u[v] is NIL
   pair_v = new int[n + 1];
   // dist[u] stores distance of left side vertices
   dist = new int[m + 1];
   // Initialize NIL as pair of all vertices
   for (int u = 0: u \le m: u++)
       pair_u[u] = NIL;
   for (int v = 0; v \le n; v++)
       pair_v[v] = NIL;
   // Initialize result
   int result = 0;
   // Keep updating the result while there is an
   // augmenting path possible.
   while (bfs())
       // Find a free vertex to check for a matching
       for (int u = 1; u <= m; u++)
           // If current vertex is free and there is
           // an augmenting path from current vertex
           // then increment the result
           if (pair_u[u] == NIL && dfs(u))
              result++;
   return result;
```

```
Returns true if there is an augmenting path
    available, else returns false
bool BGraph::bfs()
   std::queue<int> q; //an integer queue for bfs
   // First layer of vertices (set distance as 0)
   for (int u = 1; u <= m; u++)
       // If this is a free vertex, add it to queue
       if (pair_u[u] == NIL)
           // u is not matched so distance is 0
           dist[u] = 0:
           q.push(u);
       }
       // Else set distance as infinite so that this
           vertex is considered next time for
           availibility
           dist[u] = INF;
   // Initialize distance to NIL as infinite
   dist[NIL] = INF:
   // q is going to contain vertices of left side only.
   while (!q.empty())
       // dequeue a vertex
       int u = q.front();
       q.pop();
       // If this node is not NIL and can provide a
           shorter path to NIL then
       if (dist[u] < dist[NIL])</pre>
           // Get all the adjacent vertices of the
               dequeued vertex u
           std::list<int>::iterator it:
           for (it = adj[u].begin(); it != adj[u].end();
              int v = *it;
              // If pair of v is not considered so far
              // i.e. (v, pair_v[v]) is not yet
                   explored edge.
              if (dist[pair_v[v]] == INF)
                  // Consider the pair and push it to
                  dist[pair_v[v]] = dist[u] + 1;
                  q.push(pair_v[v]);
          }
   // If we could come back to NIL using alternating
       path of distinct
   // vertices then there is an augmenting path
       available
   return (dist[NIL] != INF);
  Returns true if there is an augmenting path beginning
    with free vertex u
bool BGraph::dfs(int u)
   if (u != NIL)
```

```
std::list<int>::iterator it;
       for (it = adj[u].begin(); it != adj[u].end();
           ++it)
           // Adjacent vertex of u
          int v = *it;
          // Follow the distances set by BFS search
          if (dist[pair_v[v]] == dist[u] + 1)
              // If dfs for pair of v also returnn true
              if (dfs(pair_v[v]) == true)
              { // new matching possible, store the
                  matching
                  pair_v[v] = u;
                  pair_u[u] = v;
                  return true;
       // If there is no augmenting path beginning with
           u then.
       dist[u] = INF;
       return false:
   return true;
// Constructor for initialization
BGraph::BGraph(int m, int n)
   this->m = m;
   this -> n = n:
   adj = new std::list<int>[m + 1];
// function to add edge from u to {	t v}
void BGraph::addEdge(int u, int v)
   adj[u].push_back(v); // Add v to us list.
     Minimum Cost Maximum Flow
```

```
struct Edge
   int from, to, capacity, cost;
vector<vector<int>> adj, cost, capacity;
const int INF = 1e9;
void shortest_paths(int n, int v0, vector<int>& d,
    vector<int>& p) {
   d.assign(n, INF);
   d[v0] = 0;
   vector<bool> inq(n, false);
   queue<int> q;
   q.push(v0);
   p.assign(n, -1);
   while (!q.empty()) {
       int u = q.front();
       q.pop();
       inq[u] = false;
       for (int v : adj[u]) {
          if (capacity[u][v] > 0 && d[v] > d[u] +
               cost[u][v]) {
              d[v] = d[u] + cost[u][v];
```

```
p[v] = u:
              if (!ina[v]) {
                  inq[v] = true;
                  q.push(v);
          }
      }
int min_cost_flow(int N, vector<Edge> edges, int K, int
    s, int t) {
   adj.assign(N, vector<int>());
   cost.assign(N, vector<int>(N, 0));
   capacity.assign(N, vector<int>(N, 0));
   for (Edge e : edges) {
       adj[e.from].push_back(e.to);
       adj[e.to].push_back(e.from);
       cost[e.from][e.to] = e.cost;
       cost[e.to][e.from] = -e.cost;
       capacity[e.from][e.to] = e.capacity;
   int flow = 0;
   int cost = 0;
   vector<int> d, p;
   while (flow < K) {
       shortest_paths(N, s, d, p);
       if (d[t] == INF)
           break;
       // find max flow on that path
       int f = K - flow;
       int cur = t;
       while (cur != s) {
          f = min(f, capacity[p[cur]][cur]);
           cur = p[cur];
       }
       // apply flow
       flow += f;
       cost += f * d[t];
       cur = t;
       while (cur != s) {
           capacity[p[cur]][cur] -= f;
           capacity[cur][p[cur]] += f;
           cur = p[cur];
   if (flow < K)</pre>
      return -1;
   else
       return cost:
```

4 Geo

4.1 Convex Hull

```
#include<bits/stdc++.h>
#include<vector>
using namespace std;
struct pt {
    double x, y;
};

bool cmp(pt a, pt b) {
    return a.x < b.x || (a.x == b.x && a.y < b.y);
}

bool cw(pt a, pt b, pt c) {
    return a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y) < 0;</pre>
```

```
bool ccw(pt a, pt b, pt c) {
   return a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y) > 0;
vector<pt> a;
vector<pair<double,pair<double,double> > > pp;
void convex_hull(vector<pt>& a) {
   if (a.size() == 1)
   sort(a.begin(), a.end(), &cmp);
   pt p1 = a[0], p2 = a.back();
   vector<pt> up, down;
   up.push_back(p1);
   down.push_back(p1);
   for (int i = 1; i < (int)a.size(); i++) {</pre>
       if (i == a.size() - 1 || cw(p1, a[i], p2)) {
           while (up.size() >= 2 && !cw(up[up.size()-2],
               up[up.size()-1], a[i]))
               up.pop_back();
           up.push_back(a[i]);
       if (i == a.size() - 1 || ccw(p1, a[i], p2)) {
           while(down.size() >= 2 &&
               !ccw(down[down.size()-2]
               down[down.size()-1], a[i]))
               down.pop_back();
           down.push_back(a[i]);
   a.clear();
   for (int i = 0; i < (int)up.size(); i++)</pre>
       a.push_back(up[i]);
   for (int i = down.size() - 2; i > 0; i--)
       a.push_back(down[i]);
```

4.2 Half Plane Intersection

```
#include <bits/stdc++.h>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 200005
#define MOD 1009
#define SMOD 998244353
#define ROOT 318
#define GMAX 19
#define EPS 0.00000001
#define NIL 0
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class HalfPlaneIntersection
   static double eps, inf;
public:
   struct Point
       double x, y;
       explicit Point(double x = 0, double y = 0) :
           x(x), y(y) {}
       // Addition, substraction, multiply by constant,
           cross product.
```

```
friend Point operator + (const Point& p. const
           Point& q)
          return Point(p.x + q.x, p.y + q.y);
      friend Point operator - (const Point& p, const
           Point& q)
          return Point(p.x - q.x, p.y - q.y);
      friend Point operator * (const Point& p, const
           double& k)
          return Point(p.x * k, p.y * k);
      friend double cross(const Point& p, const Point&
          return p.x * q.y - p.y * q.x;
   };
// Basic half-plane struct.
   struct Halfplane
      // 'p' is a passing point of the line and 'pq'
           is the direction vector of the line.
      Point p, pq;
      double angle;
      Halfplane() {}
      Halfplane(const Point& a, const Point& b) :
           p(a), pq(b - a)
          angle = atan21(pq.y, pq.x);
      // Check if point 'r' is outside this half-plane.
      // Every half-plane allows the region to the
           LEFT of its line.
      bool out(const Point& r)
          return cross(pq, r - p) < -eps;</pre>
       // Comparator for sorting.
      // If the angle of both half-planes is equal,
           the leftmost one should go first.
      bool operator < (const Halfplane& e) const
          if (fabsl(angle - e.angle) < eps) return</pre>
              cross(pq, e.p - p) < 0;
          return angle < e.angle;
      // We use equal comparator for std::unique to
           easily remove parallel half-planes.
      bool operator == (const Halfplane& e) const
          return fabsl(angle - e.angle) < eps;</pre>
      // Intersection point of the lines of two
           half-planes. It is assumed they're never
           parallel.
      friend Point inter(const Halfplane& s, const
           Halfplane& t)
```

```
double alpha = cross((t.p - s.p), t.pq) /
           cross(s.pq, t.pq);
       return s.p + (s.pq * alpha);
static vector<Point> hp_intersect(vector<Halfplane>&
   H)
   Point box[4] = // Bounding box in CCW order
       Point(inf, inf)
       Point(-inf, inf)
       Point(-inf, -inf),
       Point(inf, -inf)
   };
   for(int i = 0; i<4; i++) // Add bounding box
       half-planes.
       Halfplane aux(box[i], box[(i+1) % 4]);
       H.push back(aux):
   }
   // Sort and remove duplicates
   sort(H.begin(), H.end());
   H.erase(unique(H.begin(), H.end()), H.end());
   deque<Halfplane> dq;
   int len = 0;
   for(int i = 0; i < int(H.size()); i++)</pre>
       // Remove from the back of the deque while
           last half-plane is redundant
       while (len > 1 && H[i].out(inter(dq[len-1],
           dq[len-2])))
          dq.pop_back();
       // Remove from the front of the deque while
           first half-plane is redundant
       while (len > 1 && H[i].out(inter(dq[0],
           dq[1])))
          dq.pop_front();
           --len;
       // Add new half-plane
       dq.push_back(H[i]);
       ++len:
   }
   // Final cleanup: Check half-planes at the front
       against the back and vice-versa
   while (len > 2 && dq[0].out(inter(dq[len-1],
       dq[len-2])))
       dq.pop_back();
   }
   while (len > 2 && dq[len-1].out(inter(dq[0],
       dq[1])))
       dq.pop_front();
       --len;
   }
```

```
// Report empty intersection if necessary
       if (len < 3) return vector<Point>();
       // Reconstruct the convex polygon from the
            remaining half-planes.
       vector<Point> ret(len);
       for(int i = 0; i+1 < len; i++)
           ret[i] = inter(dq[i], dq[i+1]);
       ret.back() = inter(dq[len-1], dq[0]);
       return ret;
double HalfPlaneIntersection::eps=1e-9;
double HalfPlaneIntersection::inf=1e9;
int main()
    vector<HalfPlaneIntersection::Halfplane> V:
    vector<HalfPlaneIntersection::Point> P;
    //FASTIO;
   int i,j;
scanf("%d",&n);
    for(i=0; i<n; i++)</pre>
       scanf("%d",&c);
       HalfPlaneIntersection::Halfplane h:
       HalfPlaneIntersection::Point p;
       for(j=0; j<c; j++)</pre>
           scanf("%lf %lf",&p.x,&p.y);
           P.push_back(p);
       for(j=0; j<c; j++)</pre>
           h=HalfPlaneIntersection::Halfplane(P[j],P[(j+1)%c]);
           V.push_back(h);
       P.clear();
    P=HalfPlaneIntersection::hp_intersect(V);
    double ans=0;
    n=P.size():
    for(i=0; i<n; i++)</pre>
       ans=ans+P[i].x*P[(i+1)\%n].y-P[i].y*P[(i+1)\%n].x;
   ans=ans/2;
    printf("%.4f",ans);
    return 0;
```

4.3 Line Segment Intersection

```
line() {}
   line(pt p, pt q)
      a = p.y - q.y;
       b = q.x - p.x;
       c = -a * p.x - b * p.y;
       norm():
   void norm()
       double z = sqrt(a * a + b * b);
       if (abs(z) > EPS)
          a /= z, b /= z, c /= z;
   double dist(pt p) const { return a * p.x + b * p.y +
       c; }
double det(double a, double b, double c, double d)
   return a * d - b * c;
inline bool betw(double 1, double r, double x)
   return min(1, r) \le x + EPS \&\& x \le max(1, r) + EPS;
inline bool intersect_1d(double a, double b, double c,
   double d)
   if (a > b)
      swap(a, b):
   if (c > d)
       swap(c, d);
   return max(a, c) \le min(b, d) + EPS;
bool intersect(pt a, pt b, pt c, pt d, pt& left, pt&
   if (!intersect_1d(a.x, b.x, c.x, d.x) ||
       !intersect_1d(a.y, b.y, c.y, d.y))
       return false;
   line m(a, b);
   line n(c, d);
   double zn = det(m.a, m.b, n.a, n.b);
   if (abs(zn) < EPS)
       if (abs(m.dist(c)) > EPS || abs(n.dist(a)) > EPS)
          return false:
       if (b < a)
          swap(a, b);
       if (d < c)
          swap(c, d);
       left = max(a, c)
       right = min(b, d);
       return true;
   } else {
       left.x = right.x = -det(m.c, m.b, n.c, n.b) / zn;
       left.y = right.y = -det(m.a, m.c, n.a, n.c) / zn;
       return betw(a.x, b.x, left.x) && betw(a.y, b.y,
           left.y) &&
             betw(c.x, d.x, left.x) && betw(c.y, d.y,
                 left.y);
   }
int main()
   return 0;
```

4.4 Minimum Perimeter Triangle

```
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define MOD 100000007
#define SMOD 998244353
#define EPS 0.000000001
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
struct pt
    double x, y;
    int id;
};
struct cmp_x
    bool operator()(const pt & a, const pt & b) const
       return a.x < b.x || (a.x == b.x \&\& a.y < b.y);
};
struct cmp_y
    bool operator()(const pt & a, const pt & b) const
       return a.y < b.y;</pre>
int n;
vector<pt> a;
double mindist
pair<int, pair<int, int> > best_pair;
void upd_ans(const pt & a, const pt & b,const pt & c)
    double distC = sqrt((a.x - b.x)*(a.x - b.x) + (a.y - b.x)
        b.y)*(a.y - \bar{b}.y));
    double distA = sqrt((c.x - b.x)*(c.x - b.x) + (c.y - b.x)
        b.y)*(c.y - \bar{b}.y));
    double distB = sqrt((a.x - c.x)*(a.x - c.x) + (a.y - c.x)
        c.v)*(a.v - c.v));
    if (distA + distB + distC < mindist)</pre>
       mindist = distA + distB + distC;
       best_pair = make_pair(a.id,make_pair(b.id,c.id));
vector<pt> t;
void rec(int 1, int r)
   if (r - 1 <= 3 &&r - 1 >=2)
{
       for (int i = 1; i < r; ++i)
           for (int j = i + 1; j < r; ++j)
               for(int k=j+1;k<r;k++)</pre>
```

```
upd_ans(a[i],a[j],a[k]);
           }
       }
   }
   sort(a.begin() + 1, a.begin() + r, cmp_v());
int m = (1 + r) >> 1;
int midx = a[m].x;
rec(1, m);
rec(m, r);
merge(a.begin() + 1, a.begin() + m, a.begin() + m,
    a.begin() + r, t.begin(), cmp_y();
copy(t.begin(), t.begin() + r - 1, a.begin() + 1);
int tsz = 0;
for (int i = 1; i < r; ++i)
   if (abs(a[i].x - midx) < mindist/2)</pre>
       for (int j = tsz - 1; j >= 0 && a[i].y -
           t[j].y < mindist/2; --j)
           if(i+1<r) upd_ans(a[i], a[i+1], t[j]);</pre>
           if(j>0) upd_ans(a[i], t[j-1], t[j]);
       t[tsz++] = a[i]:
   }
}
```

4.5 Minkowski

```
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define BEGIN 1
#define MOD 100000007
#define EPS 0.000000001
#define CHAINS 18
#define NOT_VISITED 0
#define VISTTING 1
#define VISITED 2
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
struct pt
   long long x, y;
   pt() {}
   pt(long long _x, long long _y):x(_x), y(_y) {}
   pt operator+(const pt & p) const
      return pt(x + p.x, y + p.y);
   pt operator-(const pt & p) const
      return pt(x - p.x, y - p.y);
   long long cross(const pt & p) const
       return x * p.y - y * p.x;
   long long dot(const pt & p) const
```

```
return x * p.x + y * p.y;
   long long cross(const pt & a, const pt & b) const
       return (a - *this).cross(b - *this);
   long long dot(const pt & a, const pt & b) const
       return (a - *this).dot(b - *this);
   long long sqrLen() const
       return this->dot(*this);
class pointLocationInPolygon
   bool lexComp(const pt & 1, const pt & r)
       return 1.x < r.x \mid | (1.x == r.x && 1.y < r.y);
   int sgn(long long val)
       return val > 0 ? 1 : (val == 0 ? 0 : -1);
   vector<pt> seq;
   pt translate;
   bool pointInTriangle(pt a, pt b, pt c, pt point)
       long long s1 = abs(a.cross(b, c));
       long long s2 = abs(point.cross(a, b)) +
           abs(point.cross(b, c)) + abs(point.cross(c,
       return s1 == s2;
public:
   pointLocationInPolygon()
   pointLocationInPolygon(vector<pt> & points)
       prepare(points);
   void prepare(vector<pt> & points)
       seq.clear();
       n = points.size();
       int pos = 0;
       for(int i = 1; i < n; i++)
          if(lexComp(points[i], points[pos]))
              pos = i;
       translate.x=points[pos].x;
       translate.y=points[pos].y;
       rotate(points.begin(), points.begin() + pos,
           points.end());
       seq.resize(n);
       for(int i = 0; i < n; i++)
          seq[i] = points[i + 1] - points[0];
   bool pointInConvexPolygon(pt point)
```

```
point.x-=translate.x;
       point.y-=translate.y;
       if(seq[0].cross(point) != 0 &&
           sgn(seq[0].cross(point)) !=
           sgn(seq[0].cross(seq[n-1])))
           return false;
       if(seq[n - 1].cross(point) != 0 && sgn(seq[n -
           1].cross(point)) != sgn(seq[n -
           1].cross(seq[0])))
           return false;
       if(seq[0].cross(point) == 0)
           return seq[0].sqrLen() >= point.sqrLen();
       int 1 = 0, r = n - 1;
       while (r - 1 > 1)
           int mid = (1 + r)/2;
           int pos = mid;
           if(seq[pos].cross(point) >= 0)1 = mid;
           else r = mid;
       int pos = 1;
       return pointInTriangle(seq[pos], seq[pos + 1],
           pt(0, 0), point);
    'pointLocationInPolygon()
       seq.clear();
class Minkowski
   static void reorder_polygon(vector<pt> & P)
       size_t pos = 0;
       for(size_t i = 1; i < P.size(); i++)</pre>
           if(P[i].y < P[pos].y \mid | (P[i].y == P[pos].y
               && P[i].x < P[pos].x)
              pos = i;
       rotate(P.begin(), P.begin() + pos, P.end());
public:
   static vector<pt> minkowski(vector<pt> P, vector<pt>
       // the first vertex must be the lowest
       reorder_polygon(P);
       reorder_polygon(Q);
       // we must ensure cyclic indexing
       P.push_back(P[0]);
       P.push_back(P[1]);
       Q.push_back(Q[0]);
       Q.push_back(Q[1]);
       // main part
       vector<pt> result;
       size_t i = 0, j = 0;
       while(i < P.size() - 2 || j < Q.size() - 2)
           result.push_back(P[i] + Q[j]);
           auto cross = (P[i + 1] - P[i]).cross(Q[j + 1])
               - Q[j]);
           if(cross >= 0)
              ++i;
           if(cross <= 0)
              ++j;
```

```
return result;
   }
};
      Pair of Intersecting Segments
#include<bits/stdc++.h>
#include<string.h>
#include<vector>
#include<string.h>
using namespace std;
#define MAX 100009
#define MAX_NODES 100005
#define MOD 1000000007
#define INF 20000000
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
const double EPS = 1E-9;
struct pt {
   double x, y;
struct seg {
   pt p, q;
    int id;
    double get_y(double x) const {
       if (abs(p.x - q.x) < EPS)
           return p.y;
       return p.y + (q.y - p.y) * (x - p.x) / (q.x - p.x)
            p.x);
bool intersect1d(double 11, double r1, double 12, double
    r2) {
    if (11 > r1)
       swap(l1, r1);
    if (12 > r2)
       swap(12, r2);
    return max(11, 12) \le min(r1, r2) + EPS;
int vec(const pt& a, const pt& b, const pt& c) {
    double s = (b.x - a.x) * (c.y - a.y) - (b.y - a.y) *
        (c.x - a.x);
    return abs(s) < EPS ? 0 : s > 0 ? +1 : -1;
bool intersect(const seg& a, const seg& b)
    return intersect1d(a.p.x, a.q.x, b.p.x, b.q.x) &&
          intersect1d(a.p.y, a.q.y, b.p.y, b.q.y) &&
          vec(a.p, a.q, b.p) * vec(a.p, a.q, b.q) <= 0 &&
          vec(b.\bar{p}, b.\bar{q}, a.\bar{p}) * vec(b.\bar{p}, b.\bar{q}, a.\bar{q}) \leq 0;
bool operator<(const seg& a, const seg& b)</pre>
    double x = max(min(a.p.x, a.q.x), min(b.p.x, b.q.x));
    return a.get_y(x) < b.get_y(x) - EPS;
struct event {
    double x;
    int tp, id;
    event(double x, int tp, int id) : x(x), tp(tp),
        id(id) {}
    bool operator<(const event& e) const {</pre>
```

```
if (abs(x - e.x) > EPS)
          return x < e.x;</pre>
       return tp > e.tp;
   }
set<seg> s;
vector < set < seg > :: iterator > where;
set<seg>::iterator prev(set<seg>::iterator it) {
   return it == s.begin() ? s.end() : --it;
set<seg>::iterator next(set<seg>::iterator it) {
   return ++it;
pair<int, int> solve(const vector<seg>& a) {
   int n = (int)a.size();
   vector<event> e;
   for (int i = 0; i < n; ++i) {
       e.push_back(event(min(a[i].p.x, a[i].q.x), +1,
       e.push_back(event(max(a[i].p.x, a[i].q.x), -1,
           i));
   sort(e.begin(), e.end());
   s.clear();
   where.resize(a.size());
   for (size_t i = 0; i < e.size(); ++i) {</pre>
       int id = e[i].id;
       if (e[i].tp == +1) {
           set<seg>::iterator nxt =
               s.lower_bound(a[id]), prv = prev(nxt);
           if (nxt != s.end() && intersect(*nxt, a[id]))
                  return make_pair(nxt->id, id);
           if (prv != s.end() && intersect(*prv, a[id]))
              return make_pair(prv->id, id);
           where[id] = s.insert(nxt, a[id]);
       } else {
           set<seg>::iterator nxt = next(where[id]), prv
               = prev(where[id]);
           if (nxt != s.end() && prv != s.end() &&
               intersect(*nxt, *prv))
              return make_pair(prv->id, nxt->id);
           s.erase(where[id]);
   }
   return make_pair(-1, -1);
4.7 Vertical Decomposition
```

```
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
typedef double dbl;
const dbl eps = 1e-9;
inline bool eq(dbl x, dbl y){
    return fabs(x - y) < eps;</pre>
inline bool lt(dbl x, dbl y){
    return x < y - eps;</pre>
inline bool gt(dbl x, dbl y){
    return x > y + eps;
inline bool le(dbl x, dbl y){
    return x < y + eps;
inline bool ge(dbl x, dbl y){
   return x > y - eps;
struct pt{
    dbl x, y;
    inline pt operator - (const pt & p)const{
       return pt\{x - p.x, y - p.y\};
    inline pt operator + (const pt & p)const{
       return pt\{x + p.x, y + p.y\};
    inline pt operator * (dbl a)const{
       return pt\{x * a, y * a\};
    inline dbl cross(const pt & p)const{
       return x * p.y - y * p.x;
    inline dbl dot(const pt & p)const{
       return x * p.x + \bar{y} * p.\bar{y};
    inline bool operator == (const pt & p)const{
       return eq(x, p.x) && eq(y, p.y);
};
struct Line{
    pt p[2];
    Line()\{
    Line(pt a, pt b):p{a, b}{}
    pt vec()const{
       return p[1] - p[0];
    pt& operator [](size_t i){
       return p[i];
inline bool lexComp(const pt & 1, const pt & r){
    if(fabs(1.x - r.x) > eps){
       return 1.x < r.x;</pre>
    else return l.y < r.y;</pre>
vector<pt> interSegSeg(Line 11, Line 12){
    if(eq(11.vec().cross(12.vec()), 0)){
       if(!eq(11.vec().cross(12[0] - 11[0]), 0))
           return {};
       if(!lexComp(l1[0], l1[1]))
```

```
swap(11[0], 11[1]);
       if(!lexComp(12[0], 12[1]))
           swap(1\bar{2}[0], 12[1]);
       pt 1 = lexComp(11[0], 12[0]) ? 12[0] : 11[0];
       pt r = lexComp(11[1], 12[1]) ? 11[1] : 12[1];
       if(1 == r)
           return {1};
       else return lexComp(1, r) ? vector<pt>{1, r} :
            vector<pt>();
    else{
       dbl s = (12[0] - 11[0]).cross(12.vec()) /
            11.vec().cross(12.vec());
       pt inter = 11[0] + 11.vec() * s
       if(ge(s, 0) && le(s, 1) && le((12[0] - inter).dot(12[1] - inter), 0))
           return {inter};
       else
           return {};
inline char get_segtype(Line segment, pt other_point){
   if (eq(segment[0].x, segment[1].x))
       return 0;
    if(!lexComp(segment[0], segment[1]))
       swap(segment[0], segment[1]);
    return (segment[1] - segment[0]).cross(other_point -
        segment[0]) > 0 ? 1 : -1;
dbl union_area(vector<tuple<pt, pt, pt> > triangles){
    vector<Line> segments(3 * triangles.size());
    vector<char> segtype(segments.size());
    for(size_t i = 0; i < triangles.size(); i++){</pre>
       pt a, b, c;
       tie(a, b, c) = triangles[i];
       segments[3 * i] = lexComp(a, b) ? Line(a, b) :
            Line(b, a);
       segtype[3 * i] = get_segtype(segments[3 * i], c);
       segments [3 * i + 1] = lexComp(b, c)? Line(b, c)
            : Line(c, b);
       segtype[3 * i + 1] = get_segtype(segments[3 * i
            + 1], a);
       segments [3 * i + 2] = lexComp(c, a)? Line(c, a)
            : Line(a, c);
       segtype[3 * i + 2] = get_segtype(segments[3 * i
            + 2], b);
    vector<dbl> k(segments.size()), b(segments.size());
   for(size_t i = 0; i < segments.size(); i++){</pre>
       if(segtype[i]){
           k[i] = (segments[i][1].y - segments[i][0].y)
                / (segments[i][1].x - segments[i][0].x);
           b[i] = segments[i][0].y - k[i] *
               segments[i][0].x;
       }
    for(size_t i = 0; i < segments.size(); i++){</pre>
       if(!segtype[i])
           continue:
       dbl l = segments[i][0].x, r = segments[i][1].x;
       vector<pair<dbl, int> > evts;
       for(size_t j = 0; j < segments.size(); j++){</pre>
           if(!segtype[j] || i == j)
           dbl l1 = segments[j][0].x, r1 =
               segments[j][1].x;
```

if(ge(11, r) | ge(1, r1))

```
continue:
          dbl common_l = max(l, l1), common_r = min(r, l2)
              r1);
          auto pts = interSegSeg(segments[i],
               segments[i]);
          if(pts.empty()){
              dbl yl1 = k[j] * common_l + b[j];
              dbl yl = k[i] * common_l + b[i];
              if(lt(yl1, yl) == (segtype[i] == 1)){
                  int evt_type = -segtype[i] *
                      segtype[j];
                  evts.emplace_back(common_1, evt_type);
                  evts.emplace_back(common_r, -evt_type);
          else if(pts.size() == 1u){
              dbl \dot{y}l = k[i] * common_l + b[i], yl1 =
                  k[j] * common_l + b[j];
              int evt_type = -segtype[i] * segtype[j];
              if(lt(yl1, yl) == (segtype[i] == 1)){
                  evts.emplace_back(common_1, evt_type);
                  evts.emplace_back(pts[0].x, -evt_type);
              yl = k[i] * common_r + b[i], yl1 = k[j] *
                  common_r + b[j];
              if(lt(yl1, yl) == (segtype[i] == 1)){
                  evts.emplace_back(pts[0].x, evt_type);
                  evts.emplace_back(common_r, -evt_type);
          }
          else{
              if(segtype[j] != segtype[i] || j > i){
                  evts.emplace_back(common_1, -2);
                  evts.emplace_back(common_r, 2);
          }
      evts.emplace_back(1, 0);
      sort(evts.begin(), evts.end());
      size_t j = 0;
      int balance = 0;
      while(j < evts.size()){</pre>
          size_t ptr = j;
          while(ptr < evts.size() && eq(evts[j].first,</pre>
               evts[ptr].first)){
              balance += evts[ptr].second;
              ++ptr;
          if(!balance && !eq(evts[j].first, r)){
              dbl next_x = ptr == evts.size() ? r :
                  evts[ptr].first;
              ans -= segtype[i] * (k[i] * (next_x +
                  evts[j].first) + 2 * b[i]) * (next_x
                  - evts[j].first);
            = ptr;
   return ans/2;
int main()
   return 0;
```

Graph

5.1 Articulation Vertex

```
int n: // number of nodes
vector<vector<int>> adj; // adjacency list of graph
vector<bool> visited;
vector<int> tin, low;
int timer:
void dfs(int v, int p = -1) {
   visited[v] = true;
   tin[v] = low[v] = timer++;
   int children=0:
   for (int to : adj[v]) {
       if (to == p) continue;
       if (visited[to]) {
           low[v] = min(low[v], tin[to]);
       } else {
           dfs(to, v);
           low[v] = min(low[v], low[to]);
           if (low[to] >= tin[v] \&\& p!=-1)
              IS_CUTPOINT(v);
           ++children;
       }
   if(p == -1 &\& children > 1)
       IS_CUTPOINT(v);
void find_cutpoints() {
   timer = 0:
   visited.assign(n, false);
   tin.assign(n, -1);
   low.assign(n, -1);
   for (int i = 0; i < n; ++i) {
       if (!visited[i])
           dfs (i);
```

5.2 Strongly Connected Components

```
vector<vector<int>> adj, adj_rev;
vector<bool> used;
vector<int> order, component;
void dfs1(int v) {
   used[v] = true;
   for (auto u : adj[v])
       if (!used[u])
           dfs1(u):
   order.push_back(v);
void dfs2(int v) {
   used[v] = true:
   component.push_back(v);
   for (auto u : adj_rev[v])
       if (!used[u])
           dfs2(u);
int main() {
   int n:
   // ... read n ...
   for (;;) {
       int a, b;
       // ... read next directed edge (a,b) ...
       adj[a].push_back(b);
       adj_rev[b].push_back(a);
```

```
used.assign(n, false);
for (int i = 0; i < n; i++)
    if (!used[i])
        dfs1(i);
used.assign(n, false);
reverse(order.begin(), order.end());
for (auto v : order)
    if (!used[v]) {
        dfs2 (v);
        // ... processing next component ...
        component.clear();
    }</pre>
```

6 Math

6.1 Combinatrics

```
#include<bits/stdc++.h>
using namespace std;
#define MAX 100000
#define MOD 1000000007
long long int fact[MAX+1],fact_inv[MAX+1];
long long int gcd(long long int a, long long int b)
    if(b==0) return a;
    else return gcd(b,a%b);
long long int egcd(long long int a, long long int b,
    long long int & x, long long int & y) {
    if (a == 0) {
       x = 0:
       y = 1;
       return b;
    long long int x1, y1;
    long long int d = egcd(b % a, a, x1, y1);
   x = y1 - (b / a) * x1;
   y = x1;
   return d;
long long int ModuloInverse(long long int a, long long
    int n)
    long long int x,y;
   x=\gcd(a,n);
   a=a/x;
   n=n/x;
   long long int res = egcd(a,n,x,y);
   x=(x^n+n)^n;
   return x;
void precal()
   fact[0]=fact inv[0]=1:
    for(i=1;i<=MAX;i++)</pre>
       fact[i]=(fact[i-1]*i)%MOD;
   fact_inv[i]=ModuloInverse(fact[i],MOD);
    for(i=MAX-1;i>0;i--)
       fact_inv[i]=(fact_inv[i+1]*(i+1))%MOD;
```

```
}
long long int C(int n,int r)
{
    long long int res=fact[n];
    res=(res*fact_inv[n-r])%MOD;
    res=(res*fact_inv[r])%MOD;
    return res;
}
int main()
{
    precal();
    while(true)
    {
        int n,r;
        scanf("%d %d",&n,&r);
        long long int res=C(n,r);
        long long int mod_inv=ModuloInverse(n,MOD);
        printf("%lld %lld\n",res,mod_inv);
    }
    return 0;
}
```

6.2 Discrete Root

```
#include<bits/stdc++.h>
#include<math.h>
using namespace std;
#define MAX 100000
int prime[MAX+1],Phi[MAX+1];
void sieve()
    int i,j;
    for(i=2: i*i<=MAX: i++)</pre>
       if(prime[i]) continue;
       for(j=i; j*i<=MAX; j++)</pre>
           if(prime[i*j]==0) prime[i*j]=i;
   }
void PhiWithSieve()
    for(i=2; i<=MAX; i++)</pre>
       if(prime[i]==0)
           Phi[i]=i-1;
       else if((i/prime[i])%prime[i]==0)
           Phi[i]=Phi[i/prime[i]]*prime[i];
       else
           Phi[i]=Phi[i/prime[i]]*(prime[i]-1);
int gcd(int a,int b)
    if(b==0) return a;
    else return gcd(b,a%b);
int powmod (int a, int b, int p) {
    int res = 1;
    while (b)
       if (b & 1)
           res = int (res * 111 * a % p), --b;
```

```
a = int (a * 111 * a % p), b >>= 1;
   return res;
int PrimitiveRoot(int p)
   vector<int>fact;
   int phi=Phi[p];
   int n=phi;
   while(n>1)
       if(prime[n]==0)
           fact.push_back(n);
       else
           int f=prime[n]:
           while (n\%f==0)
              n=n/f;
           fact.push_back(f);
   for(res=p-1; res>1; --res)
       for(n=0; n<fact.size(); n++)</pre>
           if (powmod(res,phi/fact[n],p)==1)
              break;
       if(n>=fact.size()) return res;
   return -1:
int DiscreteLog(int a, int b, int m) {
   a %= m, b %= m;
   int n = sqrt(m) + 1;
   map<int, int> vals;
   for (int p = 1; p <= n; ++p)
       vals[powmod(a,(int) (1ll*p*n) %m , m)] = p;
   for (int q = 0; q \le n; ++q) {
       int cur = (powmod(a, q, m) * 111 * b) % m;
       if (vals.count(cur))
           int ans = vals[cur] * n - q;
           return ans;
   return -1;
vector<int> DiscreteRoot(int n,int a,int k)
   int g = PrimitiveRoot(n);
   vector<int> ans;
   int any_ans = DiscreteLog(powmod(g,k,n),a,n);
   if (any_ans == -1)
       return ans;
   int delta = (n-1) / gcd(k, n-1);
   for (int cur = any_ans % delta; cur < n-1; cur +=</pre>
       ans.push_back(powmod(g, cur, n));
   sort(ans.begin(), ans.end());
   return ans;
```

6.3 Fast Fourier Transform

```
#include <bits/stdc++.h>
using namespace std;
#define MOD 1000000007
#define MAX 200005
#define PMAX 55
#define PRECISION 0.000001
#define INF 200000000
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
using cd = complex<double>;
const double PI = acos(-1);
void fft(vector<cd>& a. bool invert)
    int n = a.size();
   for(int i = 1, j = 0; i < n; i++){
       int bit = n > 1;
       for(; j&bit; bit>>=1){
           j^=bit;
        ^= bit;
       if(i < j)
           swap(a[i], a[j]);
   for(int len = 2; len <= n; len <<= 1){
       double ang = 2*PI/len*(invert ? -1 : 1);
       cd wlen(cos(ang), sin(ang));
       for(int i = 0; i < n; i += len){</pre>
           cd w(1);
           for(int j = 0; j < len/2; j++){
              cd u = a[i+j], v = a[i+j+len/2]*w;
              a[i+j] = u+v;
              a[i+j+len/2] = u-v;
              w *= wlen;
   if(invert){
       for(cd &x: a)
          x /= n:
vector<int> multiply(vector<int> const& a, vector<int>
   vector<cd> fa(a.begin(), a.end());
   vector<cd> fb(b.begin(), b.end());
   int n = 1:
   while(n < a.size()+b.size())</pre>
      n <<= 1;
   fa.resize(n);
   fb.resize(n);
   fft(fa, false);
   fft(fb, false);
   for(int i = 0; i < n; i++)
       fa[i] *= fb[i];
   fft(fa, true);
   vector<int> result(n);
```

```
for(int i = 0: i < n: i++)
       result[i] = round(fa[i].real());
   return result:
//Number Theoretic Transformation
long long int gcd(long long int a,long long int b)
   if(b==0) return a;
   else return gcd(b,a%b);
long long int egcd(long long int a, long long int b,
    long long int & x, long long int & y) {
   if (a == 0) {
       x = 0;
       v = 1;
       return b;
   long long int d = egcd(b % a, a, x1, y1);
   x = y1 - (b / a) * x1;
   v = x1;
   return d;
long long int ModuloInverse(long long int a,long long
    int n)
   long long int x,y;
   x=\gcd(a,n);
   a=a/x:
   long long int res = egcd(a,n,x,y);
   x=(\tilde{x}^n+n)^n;
   return x;
const int mod = 998244353:
const int root = 15311432
const int root_1 = 469870224;
const int root_pw = 1 << 23;
void fft(vector<int> & a, bool invert) {
   int n = a.size();
   for (int i = 1, j = 0; i < n; i++) {
       int bit = n >> 1:
       for (; j & bit; bit >>= 1)
    j ^= bit;
       j ^= bit;
       if (i < j)
          swap(a[i], a[j]);
   for (int len = 2; len <= n; len <<= 1) {
       int wlen = invert ? root_1 : root;
       for (int i = len; i < root_pw; i <<= 1)
           wlen = (int)(1LL * wlen * wlen % mod);
       for (int i = 0: i < n: i += len) {
          int w = 1;
          for (int j = 0; j < len / 2; j++) {
  int u = a[i+j], v = (int)(1LL *
                  a[i+j+len/2] * w \% mod);
              a[i+j] = u + v < mod ? u + v : u + v -
              a[i+j+len/2] = u - v >= 0 ? u - v : u - v
                  + mod;
              w = (int)(1LL * w * wlen % mod);
      }
```

```
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```

```
if (invert) {
      int n_1 = (int) ModuloInverse(n, mod);
      for (int & x : a)
         x = (int)(1LL * x * n_1 \% mod);
}
vector<int> multiply(vector<int> const& a, vector<int>
   const&b)
   vector<int> fa(a.begin(), a.end());
   vector<int> fb(b.begin(), b.end());
   int n = 1;
   while(n < a.size()+b.size())</pre>
     n <<= 1:
   fa.resize(n);
   fb.resize(n);
   fft(fa, false);
   fft(fb, false);
   for(int i = 0; i < n; i++)
     fa[i] = (int) (1LL*fa[i]*fb[i]%mod);
   fft(fa, true);
   vector<int> result(n):
   for(int i = 0; i < n; i++)
      result[i] = fa[i]:
   return result;
```

6.4 Polynomial Algebra

```
#include <bits/stdc++.h>
using namespace std;
namespace algebra {
       const int inf = 1e9;
       const int magic = 500; // threshold for sizes to
           run the naive algo
       namespace fft {
               const int maxn = 1 << 18;
               typedef double ftype;
               typedef complex<ftype> point;
               point w[maxn];
               const ftype pi = acos(-1);
               bool initiated = 0;
               void init() {
                      if(!initiated) {
                              for(int i = 1; i < maxn; i</pre>
                                  *= 2) {
                                     for(int j = 0; j <</pre>
                                          i; j++) {
                                             \tilde{w}[i + j] =
                                                  polar(ftype(1),
                                                  pi * j /
                                                  i);
                              initiated = 1:
               template<typename T>
               void fft(T *in, point *out, int n, int k
                   = 1) {
                      if(n == 1) {
```

*out = *in;

} else {

```
fft(in, out, n, 2 * k);
               fft(in + k, out + n, n, 2 *
               for(int i = 0; i < n; i++) {
                      auto t = out[i + n]
                           * w[i + n];
                       out[i + n] = out[i]
                       out[i] += t:
       }
template<typename T>
void mul_slow(vector<T> &a, const
    vector<T> &b) {
       vector<T> res(a.size() + b.size()
            - 1);
       for(size_t i = 0; i < a.size();</pre>
           i++) {
               for(size_t j = 0; j <</pre>
                   b.size(); j++) {
                      res[i + j] += a[i] *
                           b[j];
       \dot{a} = res;
}
```

```
void mul(vector<T> &a, const vector<T>
         %b) {
                if(min(a.size(), b.size()) <</pre>
                          magic) {
                                 mul_slow(a, b);
                                 return:
                init();
static const int shift = 15, mask
                          = (1 << shift) - 1;
                size_t n = a.size() + b.size() - 1;
                while(__builtin_popcount(n) != 1) {
                a.resize(n);
                static point A[maxn], B[maxn];
                static point C[maxn], D[maxn];
                for(size_t i = 0; i < n; i++) {</pre>
                                 A[i] = point(a[i] & mask,
                                          a[i] >> shift);
                                 if(i < b.size()) {</pre>
                                                  B[i] = point(b[i] &
                                                           mask, b[i] >>
                                                            shift):
                                 } else {
                                                  B[i] = 0:
                fft(A, C, n); fft(B, D, n);
                for(size_t i = 0; i < n; i++) {</pre>
                                 point c0 = C[i] + conj(C[(n + conj(C[(n)(c)(c)(c)(c))(c))))))])])])]]])]]
                                          - i) % n]);
                                 point c1 = C[i] - conj(C[(n
                                          - i) % n]);
                                 point d0 = D[i] + conj(D[(n
                                          - i) % n]);
                                 point d1 = D[i] - conj(D[(n
                                          - i) % n]);
```

```
A[i] = c0 * d0 - point(0,
                          1) * c1 * d1:
                      B[i] = c0 * d1 + d0 * c1;
              fft(A, C, n); fft(B, D, n);
reverse(C + 1, C + n);
              reverse(D + 1, D + n);
              int t = 4 * n;
              for(size_t i = 0; i < n; i++) {</pre>
                      int64 t AO =
                          llround(real(C[i]) / t);
                      T A1 = llround(imag(D[i]) /
                          t);
                      T A2 = llround(imag(C[i]) /
                          t);
                      a[i] = A0 + (A1 << shift) +
                           (A2 << 2 * shift);
              return;
template<tvpename T>
T bpow(T x, size_t n) {
       return n ? n % 2 ? x * bpow(x, n - 1) :
           bpow(x * x, n / 2) : T(1);
template<typename T>
T bpow(T x, size_t n, T m) {
       return n ? n % 2 ? x * bpow(x, n - 1, m)
           % m : bpow(x * x % m, n / 2, m) :
           T(1);
template<typename T>
T gcd(const T &a, const T &b) {
       return b == T(0) ? a : gcd(b, a % b);
template<typename T>
T nCr(T n, int r) { // runs in O(r)}
       T res(1);
       for(int i = 0; i < r; i++) {
              res *= (n - T(i));
              res /= (i + 1);
       return res;
template<int m>
struct modular {
       int64_t r;
       modular() : r(0) {}
       modular(int64_t rr) : r(rr) \{if(abs(r) >=
           m) r \% = m; if (r < 0) r += m;
       modular inv() const {return bpow(*this, m
           - 2):}
       modular operator * (const modular &t)
           const {return (r * t.r) % m;}
       modular operator / (const modular &t)
           const {return *this * t.inv();}
       modular operator += (const modular &t) {r
           += t.r; if(r >= m) r -= m; return
       modular operator -= (const modular &t) {r
           -= t.r; if(r < 0) r += m; return
       modular operator + (const modular &t)
           const {return modular(*this) += t;}
       modular operator - (const modular &t)
            const {return modular(*this) -= t;}
       modular operator *= (const modular &t)
           {return *this = *this * t;}
```

```
modular operator /= (const modular &t)
           {return *this = *this / t:}
       bool operator == (const modular &t) const
           {return r == t.r:}
       bool operator != (const modular &t) const
           {return r != t.r;}
       operator int64_t() const {return r;}
template<int T>
istream& operator >> (istream &in, modular<T>
    &x) {
       return in >> x.r;
template<typename T>
struct poly {
       vector<T> a;
       void normalize() { // get rid of leading
              while(!a.empty() && a.back() ==
                  T(0)) {
                      a.pop_back();
       }
       polv(){}
       poly(T a0) : a{a0}{normalize();}
       poly(vector<T> t) : a(t){normalize();}
       poly operator += (const poly &t) {
              a.resize(max(a.size(),
                  t.a.size()));
              for(size_t i = 0; i < t.a.size();</pre>
                  i++) {
                     a[i] += t.a[i];
              normalize();
              return *this;
       poly operator -= (const poly &t) {
              a.resize(max(a.size(),
                  t.a.size()));
              for(size_t i = 0; i < t.a.size();</pre>
                  i++) {
                      a[i] -= t.a[i];
              normalize();
              return *this;
       poly operator + (const poly &t) const
           {return poly(*this) += t;}
       poly operator - (const poly &t) const
           {return poly(*this) -= t;}
       poly mod_xk(size_t k) const { // get same
           polynomial mod x^k
              k = min(k, a.size());
              return vector<T>(begin(a),
                  begin(a) + k);
       poly mul_xk(size_t k) const { // multiply
           by x^k
              poly res(*this);
              res.a.insert(begin(res.a), k, 0);
              return res;
       polv div_xk(size_t k) const { // divide
           by x^k, dropping coefficients
```

```
k = min(k, a.size()):
       return vector<T>(begin(a) + k,
           end(a));
polv substr(size_t 1, size_t r) const {
    // return mod_xk(r).div_xk(l)
       1 = \min(1, a.size());
       r = min(r, a.size());
       return vector<T>(begin(a) + 1,
           begin(a) + r):
poly inv(size_t n) const { // get inverse
    series mod x^n
       assert(!is_zero());
       poly ans = a[0].inv();
       size_t a = 1;
       while(a < n) {</pre>
              polv C = (ans * mod_xk(2 *
                   a)).substr(a, 2 * a);
              ans -= (ans *
                   C).mod_xk(a).mul_xk(a);
              a *= 2;
       return ans.mod_xk(n);
poly operator *= (const polv &t)
    {fft::mul(a, t.a); normalize();
    return *this;}
poly operator * (const poly &t) const
    {return poly(*this) *= t;}
poly reverse(size_t n, bool rev = 0)
    const { // reverses and leaves only n
       poly res(*this);
       if(rev) { // If rev = 1 then tail
           goes to head
              res.a.resize(max(n,
                  res.a.size()));
       std::reverse(res.a.begin(),
           res.a.end());
       return res.mod_xk(n);
pair<poly, poly> divmod_slow(const poly
    &b) const { // when divisor or
    quotient is small
       vector<T> A(a);
       vector<T> res;
       while(A.size() >= b.a.size()) {
              res.push_back(A.back() /
                   b.a.back());
              if(res.back() != T(0)) {
                      for(size_t i = 0; i
                          < b.a.size();
                          i++) {
                             A[A.size() -
                                 i - 1]
                                  -=
                                 res.back()
                                 b.a[b.a.size()
                                 - i - 1];
                      }
              A.pop_back();
       std::reverse(begin(res), end(res)):
       return {res, A};
```

```
pair<poly, poly> divmod(const poly &b)
    const { // returns quotiend and
    remainder of a mod b
       if(deg() < b.deg()) {</pre>
              return {poly{0}, *this};
       int d = deg() - b.deg();
       if(min(d, b.deg()) < magic) {</pre>
              return divmod_slow(b);
       poly D = (reverse(d + 1) *
           b.reverse(d + 1).inv(d +
           1) .mod_xk(d + 1).reverse(d +
           1, 1);
       return \{D, *this - D * b\};
poly operator / (const poly &t) const
    {return divmod(t).first;}
poly operator % (const poly &t) const
    {return divmod(t).second;}
poly operator /= (const poly &t) {return
    *this = divmod(t).first;}
poly operator %= (const poly &t) {return
    *this = divmod(t).second;}
poly operator *= (const T &x) {
       for(auto &it: a) {
              it *= x:
       normalize():
       return *this;
poly operator /= (const T &x) {
       for(auto &it: a) {
              it /= x;
       normalize();
       return *this:
poly operator * (const T &x) const
    {return poly(*this) *= x;}
poly operator / (const T &x) const
    {return poly(*this) /= x;}
void print() const {
       for(auto it: a) {
              cout << it << ' ';
       cout << endl;</pre>
T eval(T x) const { // evaluates in
    single point x
       T res(0);
       for(int i = int(a.size()) - 1; i
           >= 0; i--) {
              rés *= x
              res += a[i];
       return res;
T& lead() { // leading coefficient
       return a.back();
int deg() const { // degree
       return a.empty() ? -inf : a.size()
           - 1;
```

```
bool is_zero() const { // is polynomial
       return a.empty();
T operator [](int idx) const {
       return idx >= (int)a.size() || idx
           < 0 ? T(0) : a[idx];
}
T& coef(size_t idx) { // mutable
    reference at coefficient
       return a[idx];
bool operator == (const poly &t) const
    {return a == t.a;}
bool operator != (const poly &t) const
    {return a != t.a;}
poly deriv() { // calculate derivative
       vector<T> res;
       for(int i = 1; i <= deg(); i++) {
              res.push_back(T(i) * a[i]);
       return res;
poly integr() { // calculate integral
    with C = 0
       vector<T> res = {0};
       for(int i = 0; i <= deg(); i++) {</pre>
              res.push_back(a[i] / T(i +
                   1)):
       return res;
size_t leading_xk() const { // Let p(x) =
    x^k * t(x), return k
       if(is_zero()) {
              return inf;
       int res = 0:
       while(a[res] == T(0)) {
              res++;
       return res;
poly log(size_t n) { // calculate log
    p(x) \mod x^n
       assert(a[0] == T(1));
       return (deriv().mod_xk(n) *
           inv(n)).integr().mod_xk(n);
poly exp(size_t n) { // calculate exp
    p(x) \mod x^n
       if(is_zero()) {
              return T(1);
       assert(a[0] == T(0));
       poly ans = T(1);
       size_t a = 1;
       while(a < n) '{</pre>
              poly C = ans.log(2 *
                   a).div_xk(a) -
                   substr(a, 2 * a);
              ans -= (ans *
                   C).mod_xk(a).mul_xk(a);
              a *= 2:
       return ans.mod_xk(n);
poly pow_slow(size_t k, size_t n) { // if
    k is small
```

```
return k ? k % 2 ? (*this *
           pow_slow(k - 1, n)).mod_xk(n)
            *this).mod_xk(n).pow_slow(k /
           (2, n) : T(1):
poly pow(size_t k, size_t n) { //
    calculate p^k(n) mod x^n
       if(is_zero()) {
              return *this;
       if(k < magic) {</pre>
               return pow_slow(k, n);
       int i = leading_xk();
       T j = a[i];
       poly t = div_xk(i) / j;
       return bpow(j, k) * (t.log(n) *
           T(k) .exp(n).mul_xk(i *
           k).mod_x\bar{k}(n);
poly mulx(T x) { // component-wise
    multiplication with x^k
       T cur = 1;
       poly res(*this);
       for(int i = 0; i <= deg(); i++) {
              res.coef(i) *= cur;
               cur *= x;
       return res:
poly mulx_sq(T x) { // component-wise
    multiplication with x^{-}\{k^{2}\}
       T cur = x;
T total = 1;
       T xx = x * x;
       poly res(*this);
       for(int i = 0; i <= deg(); i++) {
              res.coef(i) *= total;
               total *= cur;
               cur *= xx;
       return res;
vector<T> chirpz_even(T z, int n) { //
    P(1), P(z^2), P(z^4), ..., P(z^2(n-1))
       int m = deg();
       if(is_zero()) {
               return vector<T>(n, 0);
       vector<T> vv(m + n);
       T zi = z.inv();
       T zz = zi * zi;
       T cur = zi;
       T total = 1;
       for(int i = 0; i \le max(n - 1, m);
           i++) {
               if(i \le m) \{vv[m - i] =
                   total;}
               if(i < n) \{vv[m + i] =
                   total;}
               total *= cur:
               cur *= zz;
       poly w = (mulx_sq(z) *
           vv).substr(m, m +
           n).mulx_sq(z);
       vector<T> res(n);
       for(int i = 0: i < n: i++) {
               res[i] = w[i];
```

```
return res:
       vector<T> chirpz(T z, int n) { // P(1),
           P(z), P(z^2), ..., P(z^{(n-1)})
              auto even = chirpz_even(z, (n + 1))
              auto odd = mulx(z).chirpz_even(z,
              vector<T> ans(n);
              for(int i = 0; i < n / 2; i++) {</pre>
                     ans[2 * i] = even[i];
                     ans[2 * i + 1] = odd[i];
              if(n % 2 == 1) {
                     ans[n-1] = even.back();
              return ans;
       template<typename iter>
       vector<T> eval(vector<poly> &tree, int v,
           iter 1, iter r) { // auxiliary
           evaluation function
              if(r - 1 == 1) {
                     return {eval(*1)};
              } else {
                     auto m = 1 + (r - 1) / 2;
                     auto A = (*this % tree[2 *
                          v]).eval(tree, 2 * v,
                          1, m);
                     auto B = (*this % tree[2 *
                          v + 1]).eval(tree, 2 *
                          v + 1, m, r);
                     A.insert(end(A), begin(B),
                          end(B));
                     return A;
       vector<T> eval(vector<T> x) { // evaluate
           polynomial in (x1, ..., xn)
              int n = x.size();
              if(is_zero()) {
                     return vector<T>(n, T(0));
              vector<poly> tree(4 * n);
              build(tree, 1, begin(x), end(x));
              return eval(tree, 1, begin(x),
                  end(x));
       template<typename iter>
       poly inter(vector<poly> &tree, int v,
           iter 1, iter r, iter ly, iter ry) {
           // auxiliary interpolation function
              if(r - 1) == 1) {
                     return {*ly / a[0]};
              } else {
                     auto m = 1 + (r - 1) / 2;
                     auto my = ly + (ry - ly) /
                     auto A = (*this % tree[2 *
                          v]).inter(tree, 2 * v,
                          1, m, ly, my);
                     auto B = (*this % tree[2 *
                          v + 1]).inter(tree, 2 *
                          v + 1, m, r, my, ry);
                     return A * tree[2 * v + 1]
                          + B * tree[2 * v];
template<typename T>
```

```
poly<T> operator * (const T& a, const poly<T>&
              return b * a;
       template<tvpename T>
       poly<T> xk(int k) { // return x^k
              return poly<T>{1}.mul_xk(k);
       template<typename T>
       T resultant(poly<T> a, poly<T> b) { // computes
           resultant of a and b
              if(b.is_zero()) {
                      return 0;
              } else if(b.deg() == 0) {
                      return bpow(b.lead(), a.deg());
              } else {
                      int pw = a.deg();
                      a %= b;
                      pw -= a.deg();
                      T mul = bpow(b.lead(), pw) *
                          T((b.deg() & a.deg() & 1) ? -1
                          : 1);
                      T ans = resultant(b, a);
                      return ans * mul;
       template<typename iter>
       poly<typename iter::value_type> kmul(iter L,
           iter R) { // computes (x-a1)(x-a2)...(x-an)
           without building tree
              if(R - L == \bar{1}) {
                      return vector<typename
                          iter::value_type>{-*L, 1};
              } else {
                      iter M = L + (R - L) / 2;
                      return kmul(L, M) * kmul(M, R);
       template<typename T, typename iter>
       poly<T> build(vector<poly<T>> &res, int v, iter
           L, iter R) { // builds evaluation tree for
           (x-a1)(x-a2)...(x-an)
              if(R - L == 1) {
                      return res[v] = vector<T>{-*L, 1};
              } else {
                      iter M = L + (R - L) / 2;
                      return res[v] = build(res, 2 * v,
                          L, M) * build(res, 2 * v + 1,
                          M, R);
              }
       template<typename T>
       poly<T> inter(vector<T> x, vector<T> y) { //
           interpolates minimum polynomial from (xi,
           vi) pairs
              int n = x.size();
              vector<poly<T>> tree(4 * n);
              return build(tree, 1, begin(x),
                   end(x)).deriv().inter(tree, 1,
                   begin(x), end(x), begin(y), end(y));
};
using namespace algebra;
const int mod = 1e9 + 7;
typedef modular<mod> base;
typedef poly<br/>
base> polyn;
using namespace algebra;
```

```
signed main() {
       ios::sync_with_stdio(0);
       cin.tie(0);
       int n = 100000;
       polyn a;
       vector<br/>base> x;
       for(int i = 0; i <= n; i++) {
              a.a.push_back(1 + rand() % 100);
              x.push_back(1 + rand() \% (2 * n));
       sort(begin(x), end(x));
       x.erase(unique(begin(x), end(x)), end(x));
       auto b = a.eval(x);
       cout << clock() / double(CLOCKS_PER_SEC) << endl;</pre>
       auto c = inter(x, b);
       polyn md = kmul(begin(x), end(x));
       cout << clock() / double(CLOCKS_PER_SEC) << endl;</pre>
       assert(c == a % md):
       return 0;
     String
```

const int K = 26:

Aho Corasick

```
struct Vertex {
   int next[K];
   bool leaf = false;
   int p = -1;
   char pch;
int link = -1;
   int go[K];
   Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
       fill(begin(next), end(next), -1);
       fill(begin(go), end(go), -1);
vector<Vertex> t(1);
void add_string(string const& s) {
   int v = 0;
   for (char ch : s) {
       int c = ch - a
       if (t[v].next[c] == -1) {
           t[v].next[c] = t.size();
           t.emplace_back(v, ch);
       }
       v = t[v].next[c];
   t[v].leaf = true;
int go(int v, char ch);
int get_link(int v) {
   if (t[v].link == -1) {
       if (v == 0 || t[v].p == 0)
           t[v].link = 0;
       else
           t[v].link = go(get_link(t[v].p), t[v].pch);
   return t[v].link;
int go(int v, char ch) {
   int c = ch - 'a';
   if (t[v].go[c] == -1) {
       if (t[v].next[c] != -1)
```

```
t[v].go[c] = t[v].next[c];
   else
       t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
return t[v].go[c];
```

19

Manacher's Algorithm

```
#include<bits/stdc++.h>
#include<vector>
using namespace std;
int main()
   int T,1;
   char s[MAX];
   gets(s);
   int n=strlen(s):
   vector<int> d1(n);
   for (int i = 0, l = 0, r = -1; i < n; i++)
       int k = (i > r) ? 1 : min(d1[l + r - i], r - i +
       while (0 \le i - k \&\& i + k \le n \&\& s[i - k] ==
           s[i + k]
           k++;
       d1[i] = k--;
       if (i + k > r)
          1 = i - k:
          r = i + k;
   vector<int> d2(n);
   for (int i = 0, l = 0, r = -1; i < n; i++)
       int k = (i > r) ? 0 : min(d2[1 + r - i + 1], r - i)
           i + 1);
       while (0 <= i - k - 1 && i + k < n && s[i - k -
           1] == s[i + k])
           k++;
       d2[i] = k--:
       if (i + k > r)
          1 = i - k - 1;
          r = i + k;
   return 0;
```

Suffix Array

```
#include<bits/stdc++.h>
#include<string.h>
using namespace std;
#define MAX 100000
vector<int> sort_cyclic_shifts(char *s) {
   int n = strlen(s);
   const int alphabet = 256;
   vector<int> p(n), c(n), cnt(max(alphabet, n), 0);
   for (int i = 0; i < n; i++)
       cnt[s[i]]++;
   for (int i = 1; i < alphabet; i++)</pre>
       cnt[i] += cnt[i-1];
   for (int i = 0; i < n; i++)
       p[--cnt[s[i]]] = i;
```

```
c[0]q]
   int classes = 1;
   for (int i = 1; i < n; i++) {</pre>
       if (s[p[i]] != s[p[i-1]])
           classes++;
       c[p[i]] = classes - 1;
   vector<int> pn(n), cn(n);
   for (int h = 0; (1 << h) < n; ++h) {
       for (int i = 0; i < n; i++) {</pre>
           pn[i] = p[i] - (1 << h);
           if (pn[i] < 0)
               pn[i] += n;
       fill(cnt.begin(), cnt.begin() + classes, 0);
       for (int i = 0; i < n; i++)
           cnt[c[pn[i]]]++;
       for (int i = 1; i < classes; i++)</pre>
           cnt[i] += cnt[i-1];
       for (int i = n-1; i >= 0; i--)
   p[--cnt[c[pn[i]]]] = pn[i];
       cn[p[0]] = 0;
       classes = 1;
       for (int i = 1; i < n; i++) {
           int ind=p[i] + (1 << h);</pre>
           if(ind>=n) ind=ind-n;
           pair<int, int> cur = {c[p[i]], c[ind]};
           ind=p[i-1] + (1 << h);
           if(ind>=n) ind=ind-n;
           pair < int, int > prev = \{c[p[i-1]], c[ind]\};
           if (cur != prev)
               ++classes:
           cn[p[i]] = classes - 1;
       c.swap(cn);
   return p;
vector<int> suffix_array_construction(char *s) {
   int n=strlen(s):
   s[n]='#';
   vector<int> sorted_shifts = sort_cyclic_shifts(s);
   sorted_shifts.erase(sorted_shifts.begin());
   return sorted_shifts;
vector<int> lcp_construction(char *s, vector<int> const&
   p) {
int n = strlen(s);
   vector<int> rank(n, 0);
   for (int i = 0; i < n; i++)</pre>
       rank[p[i]] = i;
   int k = 0;
   vector < int > lcp(n-1, 0);
   for (int i = 0; i < n; i++) {
       if (rank[i] == n - 1) {
           k = 0;
           continue;
       int j = p[rank[i] + 1];
       while (i + k < n &  j + k < n &  s[i+k] ==
            s[j+k])
           k++;
       lcp[rank[i]] = k;
       if (k)
           k--:
   return lcp;
int lcp(int i, int j) {
```

```
for (int k = log_n; k >= 0; k--) {
   if (c[k][i] == c[k][j]) {
       ans += 1 << k;
       i += 1 << k;
       j += 1 << k;
return ans;
```

```
Suffix Automaton
#include <bits/stdc++.h>
#include <vector>
#include<math.h>
#include<string.h>
using namespace std;
#define MAX 300005
#define BEGIN 1
#define EPS 0.000000001
#define CHAINS 18
#define NOT_VISITED 0
#define VISITING 1
#define VISITED 2
#define FASTIO
    ios_base::sync_with_stdio(false);cin.tie(NULL)
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
class SuffixAutomaton
   bool complete;
   int last;
   set<char> alphabet;
   struct state
       int len, link, endpos,
           first_pos, shortest_non_appearing_string, height;
       long long substrings,length_of_substrings;
       bool is_clone;
       map<char, int> next;
       vector<int> inv_link;
       state(int leng=0,int li=0)
           len=leng;
           link=li;
           first_pos=-1;
           substrings=0;
           length_of_substrings=0;
           endpos=1;
           shortest_non_appearing_string=0;
           is_clone=false;
           height=0;
       }
   véctor<state> st:
   void process(int node)
       map<char, int> ::iterator mit;
       st[node].substrings=1;
       st[node].shortest_non_appearing_string=st.size();
       if((int) st[node].next.size()<(int)</pre>
           alphabet.size())
           st[node].shortest_non_appearing_string=1;
       for(mit=st[node].next.begin();
           mit!=st[node].next.end(); ++mit)
           if(st[mit->second].substrings==0)
               process(mit->second);
           st[node].height=max(st[node].height,1+st[mit->second].Herenty, int> ::iterator mit;
```

```
st[node].substrings=st[node].substrings+st[mit->s
       st[node].length_of_substrings=st[node].length_of_
       st[node].shortest_non_appearing_string=min(st[node])
   if(st[node].link!=-1)
       st[st[node].link].inv_link.push_back(node);
void set_suffix_links(int node)
   for(i=0; i<st[node].inv_link.size(); i++)</pre>
       set_suffix_links(st[node].inv_link[i]);
       st[node].endpos=st[node].endpos+st[st[node].inv_1
void output_all_occurrences(int v, int
    P_length, vector < int > &pos)
   if (!st[v].is_clone)
       pos.push_back(st[v].first_pos - P_length + 1);
   for (int u : st[v].inv_link)
       output_all_occurrences(u, P_length, pos);
void kth_smallest(int node,int k,vector<char> &str)
   if(k==0) return;
   map<char, int> ::iterator mit;
   for(mit=st[node].next.begin();
        mit!=st[node].next.end(); ++mit)
       if(st[mit->second].substrings<k)</pre>
           k=k-st[mit->second].substrings;
           str.push_back(mit->first);
           kth_smallest(mit->second,k-1,str);
           return;
int find_occurrence_index(int node,int
    index, vector < char > & str)
   if(index==str.size()) return node;
   if(!st[node].next.count(str[index])) return -1;
        find_occurrence_index(st[node].next[str[index]],i
void klen_smallest(int node,int k,vector<char> &str)
   if(k==0) return;
   map<char, int> ::iterator mit;
   for(mit=st[node].next.begin();
        mit!=st[node].next.end(); ++mit)
       if(st[mit->second].height>=k-1)
           str.push_back(mit->first);
           klen_smallest(mit->second,k-1,str);
           return;
void minimum_non_existing_string(int
    node.vector<char> &str)
```

```
set<char>::iterator sit:
       for(mit=st[node].next.begin(),sit=alphabet.begin()
           sit!=alphabet.end(); ++sit,++mit)
           if (mit==st[node].next.end()||mit->first!=(*sit))
              str.push_back(*sit);
              return:
           else
              str.push_back(*sit);
              minimum_non_existing_string(mit->second,str);
   void find_substrings(int node,int index,vector<char>
        &str,vector<pair<long long,long long> >
        &sub_info)
       if(index==str.size()) return;
       if(st[node].next.count(str[index]))
       else
           sub_info.push_back(make_pair(0,0));
   void check()
       if(!complete)
          process(0);
           set_suffix_links(0);
          compléte=true;
public:
   SuffixAutomaton(set<char> &alpha)
       st.push_back(state(0,-1));
       last=0:
       complete=false;
       set<char>::iterator sit;
       for(sit=alpha.begin(); sit!=alpha.end(); sit++)
           alphabet.insert(*sit);
       st[0].endpos=0;
   void sa_extend(char c)
       int cur = st.size();
       //printf("New node (%d,%c)\n",cur,c);
       st.push_back(state(st[last].len + 1));
       st[cur].first_pos=st[cur].len-1;
       int p = last;
       while (p != -1 \&\& !st[p].next.count(c))
           st[p].next[c] = cur;
           //printf("Set edge %d -> %d (%c)\n",p,cur,c);
           p = st[p].link;
```

```
if (p == -1)
                                                                st[cur].link = 0;
                                                                //printf("Set link %d -> %d\n",cur,0);
                                                                int q = st[p].next[c];
                                                                if (st[p].len + 1 == st[q].len)
        if(st[node].shortest_non_appearing_string=\frac{1}{1+st[mit->secomet][confirent_non_appearing_string)}
                                                                    //printf("Set link %d -> %d\n".cur.q);
                                                                    int clone = st.size();
                                                                    //printf("Create clone node %d from
                                                                        %d\n".clone.a):
                                                                    //printf("Set link %d ->
                                                                        %d\n",clone,st[q].link);
                                                                    st.push_back(state(st[p].len +
sub_info.push_back(make_pair(st[node].substrings,st[node].length_of_st[side].substrings*index));
if(index-str_gige()) return:
                                                                    st[clone].is_clone=true;
                                                                    st[clone].endpos=0;
   find_substrings(st[node].next[str[index]],index+1,str,sub_info/first_pos=st[q].first_pos=st[q].first_pos;
return:
                                                                        //printf("Change transition %d -> %d :
                                                                            %d -> %d (%c)\n",p,q,p,clone,c);
                                                                        st[p].next[c] = clone;
                                                                        p = st[p].link;
                                                                    //printf("Change link %d -> %d : %d ->
                                                                        %d\n",q,st[q].link,q,clone);
                                                                    //printf("Set link %d -> %d\n",cur,clone);
                                                                    st[q].link = st[cur].link = clone;
                                                             last = cur;
                                                             complete=false;
                                                          SuffixAutomaton()
                                                             for(i=0; i<st.size(); i++)</pre>
                                                                st[i].next.clear();
                                                                st[i].inv_link.clear();
                                                             st.clear();
                                                             alphabet.clear();
                                                         void kth_smallest(int k,vector<char> &str)
                                                             kth_smallest(0,k,str);
                                                         int FindFirstOccurrenceIndex(vector<char> &str)
                                                             check();
                                                             int ind=find_occurrence_index(0,0,str);
                                                             if(ind==0) return -1;
                                                             else if(ind==-1) return st.size();
                                                             else return st[ind].first_pos+1-(int) str.size();
                                                         void FindAllOccurrenceIndex(vector<char>
                                                             &str,vector<int> &pos)
```

```
check():
   int ind=find_occurrence_index(0,0,str);
   if(ind!=-1)
        output_all_occurrences(ind,str.size(),pos);
int Occurrences(vector<char> &str)
   check();
   int ind=find_occurrence_index(0,0,str);
   if(ind==0) return 1;
   else if(ind==-1) return 0;
   else return st[ind].endpos;
void klen_smallest(int k,vector<char> &str)
   check():
   if(st[0].height>=k) klen_smallest(0,k,str);
void minimum_non_existing_string(vector<char> &str)
   check():
   int ind=find_occurrence_index(0,0,str);
   if(ind!=-1) minimum_non_existing_string(ind,str);
long long cyclic_occurrence(vector<char> &str)
   check();
   int i,j,len;
   long long ans=0;
   int n=str.size();
   set<int> S:
   set<int>::iterator it;
   for(i=0, j=0,len=0; i<n*2-1; i++)
       //printf("%d->%c\n",i,str[i½n]);
       if(st[j].next.count(str[i%n]))
          j=st[j].next[str[i%n]];
       else
           while(j!=-1&&(!st[j].next.count(str[i%n])))
              j=st[j].link;
          if(j!=-1)
              len=st[j].len+1;
              j=st[j].next[str[i%n]];
          else
              len=0;
              j=0;
       while(st[j].link!=-1&&st[st[j].link].len>=n)
            i=st[i].link;
           len=st[j].len;
       if(len>=n) S.insert(j);
   for(it=S.begin();it!=S.end();++it)
       ans=ans+st[*it].endpos;
   return ans;
```

```
};
vector<char> X;
int main()
{
   int i;
   set<char> alpha;
   for(i=0; i<26; i++)
   {
      alpha.insert('a'+i);
   }
   SuffixAutomaton sa(alpha);
   char c;</pre>
```

```
for(i=0;; i++)
{
    scanf("%c",&c);
    if(!('a'<=c&&c<='z')) break;
    sa.sa_extend(c);
}
int n,j;
scanf("%d ",&n);
for(j=0; j<n; j++)
{
    for(i=0;; i++)
}</pre>
```