DODI

1.1 divide-and-conquer-optimization

```
vector<long long> dp_before(n), dp_cur(n);
long long C(int i, int j);
// compute dp_cur[1], ... dp_cur[r] (inclusive)
void compute(int 1, int r, int opt1, int optr){
    if (\hat{1} > r)
    int mid = (1 + r) >> 1;
    pair<long long, int> best = {LLONG_MAX, -1};
    for (int k = optl; k <= min(mid, optr); k++){</pre>
         best = min(best, \{(k ? dp_before[k - 1] : 0) + C(k,
               mid), k}):
    dp_cur[mid] = best.first;
    int opt = best.second;
    compute(1, mid - 1, optl, opt);
    compute(mid + 1, r, opt, optr);
int solve(){
    for (int i = 0; i < n; i++)
    dp_before[i] = C(0, i);</pre>
    for (int i = 1; i < m; i++){
   compute(0, n - 1, 0, n - 1);</pre>
         dp_before = dp_cur;
    return dp_before[n - 1];
```

1.2 knuth-optimization

1.3 li-chao-tree

```
typedef long long ll;
class LiChaoTree{
    11 L,R;
    bool minimize;
    int lines;
    struct Node{
        complex<11> line;
        Node *children[2];
        Node(complex<11> ln= {0,1000000000000000000}){
            line=ln;
            children[0]=0;
            children[1]=0;
        }
} *root;
ll dot(complex<11> a, complex<11> b){
        return (conj(a) * b).real();
```

```
il f(complex<11> a. 11 x){
       return dot(a, \{x, 1\});
   void clear(Node* &node){
        if (node->children[0]){
            clear(node->children[0]);
        if (node->children[1]){
            clear(node->children[1]);
        delete node;
   void add_line(complex<ll> nw, Node* &node, ll l, ll r){
        if(node==0){
            node=new Node(nw);
            return;
       ll m = (1 + r) / 2;

bool lef = (f(nw, 1) < f(node->line,

1)&&minimize)||((!minimize)&&f(nw, 1) >
       f(node->line, 1));
bool mid = (f(nw, m) < f(node->line,
    m)&&minimize)||((!minimize)&&f(nw, m) >
             f(node->line, m));
        if (mid) {
            swap(node->line, nw);
       if(r - 1 == 1){
           return;
        else if(lef != mid){
            add_line(nw, node->children[0], 1, m);
        else{
            add_line(nw, node->children[1], m, r);
   11 get(ll x, Node* &node, ll l, ll r){
       11 \text{ m} = (1 + r) / 2;
        if(r - 1) == 1){
           return f(node->line, x);
            if(node->children[0]==0) return f(node->line, x);
            if(minimize) return min(f(node->line, x), get(x,
                 node->children[0], 1, m));
            else return max(f(node->line, x), get(x,
                 node->children[0], 1, m));
       else{
           if(node->children[1]==0) return f(node->line, x);
if(minimize) return min(f(node->line, x), get(x,
                 node->children[1], m, r));
            else return max(f(node->line, x), get(x,
                 node->children[1], m, r));
public:
   LiChaoTree(ll l=-1000000001,ll r=1000000001,bool mn=false){
       L=1;
R=r;
       root=0:
        minimiźe=mn;
        lines=0:
   void AddLine(pair<11,11> ln){
        add_line({ln.first,ln.second},root,L,R);
        lines++;
   int number_of_lines(){
        return lines:
   11 getOptimumValue(11 x){
       return get(x,root,L,R);
    LiChaoTree(){
       if(root!=0) clear(root);
```

1.4 zero-matrix

```
int zero matrix(vector<vector<int>> a) {
   int n = a.size();
    int m = a[0].size();
   int ans = 0;
   vector<int> d(m, -1), d1(m), d2(m);
   stack<int> st;
   for (int i = 0; i < n; ++i) {
  for (int j = 0; j < m; ++j) {
    if (a[i][j] == 1)
        d[j] = i;
        for (int j = 0; j < m; ++j) {
            while (!st.empty() && d[st.top()] <= d[j])</pre>
                 st.pop();
            d1[j] = st.empty() ? -1 : st.top();
            st.push(j);
        while (!st.empty())
            st.pop();
        for (int j = m - 1; j >= 0; --j) {
  while (!st.empty() && d[st.top()] <= d[j])</pre>
                st.pop();
            d2[j] = st.empty() ? m : st.top();
            st.push(j);
        while (!st.empty())
            st.pop();
        for (int j = 0; j < m; ++j)
            ans = \max(ans, (i - d[j]) * (d2[j] - d1[j] - 1));
   return ans;
```

2 DS

2.1 Heavy light decomposition

```
int value[N];
int Tree[N]:
int parent[N], depth[N], heavy[N], head[N], pos[N];
int cur_pos;
int n;
vector<int > adj[N];
int dfs(int v) {
   int size = 1:
    int max_c_size = 0
   for (int c : adj[v])
       if (c != parent[v]) {
           parent[c] = v, depth[c] = depth[v] + 1;
           int c_size = dfs(c);
           size += c_size;
           if (c_size > max_c_size)
               max_c_size = c_size, heavy[v] = c;
       }
   return size;
void update(int idx, int x,int nn)
        // Let, n is the number of elements and our queries are
        // of the form query(n)-query(1-1), i.e range queries
        // Then, we should never put N or MAX in place of n
            here.
        while(idx<=nn)</pre>
               Tree[idx]+=x;
               idx + = (idx \& - idx):
void decompose(int v, int h) {
   head[v] = h, pos[v] = cur_pos;
update(cur_pos,value[v],n+1);
   if (heavy[v] != -1)
       decompose(heavy[v], h);
   for (int c : adj[v]) {
       if (c != parent[v] && c != heavy[v])
```

```
decompose(c, c);
int query_bit(int idx)
       int sum=0:
       while(idx>0)
               sum+=Tree[idx];
               idx = (idx \& - idx);
       return sum:
void init_hld(int root,int n)
   memset(Tree, 0.sizeof Tree):
   memset(heavy,-1,sizeof heavy);
   cur_pos = 1
   parent[root]=-1;
   assert(dfs(root)==n):
   decompose(root, root):
int segment_tree_query(int x,int y)
   if(y < x) swap(x,y);
   return query_bit(y)-query_bit(x-1);
int query_hld(int a, int b) {
   int res = 0;
for (; head[a] != head[b]; b = parent[head[b]]) {
       if (depth[head[a]] > depth[head[b]])
           swap(a. b):
       int cur_heavy_path_max =
       segment_tree_query(pos[head[b]], pos[b]);
res += cur_heavy_path_max;
   if (depth[a] > depth[b])
       swap(a, b);
   /// now a is the lca or quert(a,b)
   int last_heavy_path_max = segment_tree_query(pos[a],
   pos[b]);
res += last_heavy_path_max;
   return res;
```

2.2 MO_with_update

```
const int N = 1e5 + 5;
const int P = 2000; \frac{1}{3}
struct query{
   int t, I, r, k, i;
vector<query> q;
vector<array<int, 3>> upd;
vector<int> ans;
vector<int>a;
void add(int x)
void rem(int x);
int get_answer();
void mos algorithm(){
    sort(q.begin(), q.end(), [](const query &a, const query
         &b){
        if (a.t / P != b.t / P)
        return a.t < b.t;
if (a.1 / P != b.1 / P)
             return a.1 < b.1;
        if ((a.1 / P) & 1)
        return a.r < b.r;
return a.r > b.r;
   for (int i = upd.size() - 1; i >= 0; --i)
a[upd[i][0]] = upd[i][1];
int L = 0, R = -1, T = 0;
auto apply = [&](int i, int fl){
        int p = upd[i][0];
        int x = upd[i][fl + 1];
        if (L \le \hat{p} \&\& p \le R){
             rem(a[p]);
             add(x):
```

```
a[p] = x;
    ans.clear();
    ans.resize(q.size());
   for (auto qr : q) {
   int t = qr.t, l = qr.l, r = qr.r, k = qr.k;
   while (T < t)</pre>
        apply(T++, 1);
while (T > t)
            apply(--T, 0);
        while (R < r)
            add(a[++R]);
        while (L > 1)
            add(a[--L]);
        while (R > r)
            rem(a[R--]);
        while (L < 1)
            rem(a[L++]);
        ans[qr.i] = get_answer();
void TEST_CASES(int cas){
   int n, m;
cin>>n>>m;
   a.resize(n);
for(int i=0;i<n;i++){</pre>
        cin>>a[i];
    for(int i=0:i<m:i++){</pre>
        int tp;
scanf("%d", &tp);
        if (tp == 1){
             int 1, r, k;
             cin>>1>>r>>k:
            q.push_back(\{upd.size(), l-1, r-1, k,
                  q.size()});
        else{
            int p, x;
             cin>>p>>x;
            upd.push_back({p, a[p], x});
            a[p] = x;
    mos_algorithm();
```

2.3 bipartite-disjoint-set-union

```
void make_set(int v) {
   parent[v] = make_pair(v, 0);
    rank[v] = 0:
   bipartite[v] = true;
pair<int, int> find_set(int v) {
   if (v != parent[v].first) {
        int parity = parent[v].second;
        parent[v] = find_set(parent[v].first);
       parent[v].second ^= parity;
   return parent[v];
void add_edge(int a, int b) {
   pair<int, int> pa = find_set(a);
a = pa.first:
    int x = pa.second;
   pair<int, int> pb = find_set(b);
b = pb.first:
   int y = pb.second;
    if (a == b) {
        if (x == y)
           bipartite[a] = false:
        if (rank[a] < rank[b])</pre>
           swap (a, b);
        parent[b] = make_pair(a, x^y^1);
        bipartite[a] &= bipartite[b];
        if (rank[a] == rank[b])
```

```
++rank[a]:
bool is_bipartite(int v) {
  return bipartite[find_set(v).first];
```

2.4 bitset

```
typedef unsigned long long ull;
int LEN; // length of Bitset array t
struct Bitset{
        ull t[N/64+5]:
        Bitset(){memset(t,0,sizeof t);}
        void set(int p){ t[p>>6] |=111u<<(p&63); }</pre>
        void shift(){
                ull last=01lu;
                for(int i=0;i<LEN;i++){</pre>
                        ull curr=t[i]>>63llu;
                        (t[i]<<=1)|=last;
last = curr:
                }
        int count(){
                         int ret=0;
                        for(int i=0;i<LEN;i++){</pre>
                                ret+=__builtin_popcountll(t[i]);
                        return ret:
        Bitset &operator = (Bitset const&b){
                memcpv(t,b,t,sizeof (t)):
                return *this;
        Bitset & operator |=(Bitset &b){
                for(int i=0:i<LEN:i++)</pre>
                                t[i]|=b.t[i];
                return *this;
        Bitset &operator &=(Bitset &b){
                for(int i=0;i<LEN;i++)</pre>
                                t[i]&=b.t[i];
                return *this:
        Bitset &operator ^=(Bitset &b){
                for(int i=0;i<LEN;i++)</pre>
                                 t[i]^=b.t[i];
                return *this;
Bitset operator-(const Bitset &a,const Bitset &b){
        Bitset tmp:
        for(int i=0;i<LEN;i++){
    ull curr = (a.t[i] < b.t[i] + last);</pre>
                tmp.t[i]=a.t[i]-b.t[i]-last;
                last = curr:
        return tmp;
// https://loj.ac/p/6564
// lcs formula: let x = m_old | Occur[char] 
// m_new = ((x - ((m_old<1)+1)) ^x)& x;
```

2.5 centroid decomposition

```
set<int> g[N];
int par[N],sub[N],level[N],ans[N];
int DP[LOGN][N]:
int n,m;
int nn;
void dfs1(int u,int p){
        sub[u]=1;
        for(auto it=g[u].begin();it!=g[u].end();it++)
                if(*it!=p)
                        dfs1(*it,u);
                       sub[u]+=sub[*it]:
```

```
int dfs2(int u,int p){
       for(auto it=g[u].begin();it!=g[u].end();it++)
              if(*it!=p && sub[*it]>nn/2)
                     return dfs2(*it,u);
       return u:
void decompose(int root,int p){
       dfs1(root,root);
       int centroid = dfs2(root,root);
       if (p==-1)p=centroid;
       par[centroid]=p;
       for(auto
            it=g[centroid].begin();it!=g[centroid].end();it++)
               g[*it].erase(centroid);
              decompose(*it,centroid);
       g[centroid].clear();
```

dsu-rollback

```
struct dsu_save {
   int v, rnkv, u, rnku;
dsu_save() {}
   dsu_save(int _v, int _rnkv, int _u, int _rnku)
       : v(v), rnkv(rnkv), u(u), rnku(rnku) {}
struct dsu with rollbacks {
   vector<int> p, rnk;
   int comps;
   stack<dsu save> op:
   dsu_with_rollbacks() {}
   dsu_with_rollbacks(int n) {
       p.resize(n);
       rnk.resize(n):
       for (int i = 0; i < n; i++) {
           p[i] = i;
rnk[i] = 0;
       comps = n;
   int find_set(int v)
       return (v == p[v]) ? v : find_set(p[v]);
   bool unite(int v, int u) {
       v = find set(v):
       u = find_set(u);
       if (v == u)
       return false; comps--;
       if (rnk[v] > rnk[u])
           swap(v, u);
        op.push(dsu_save(v, rnk[v], u, rnk[u]));
       p[v] = u;
if (rnk[u] == rnk[v])
           rnk[u]++;
       return true;
   void rollback() {
       if (op.empty())
           return;
       dsu_save x = op.top();
       op.pop();
comps++;
       p[x.v] = x.v;
       rnk[x.v] = x.rnkv;
       p[x.u] = x.u;
       rnk[x.u] = x.rnku;
struct query {
   int v, u;
   bool united;
   query(int _v, int _u) : v(_v), u(_u) {
struct QueryTree {
```

```
vector<vector<query>> t;
dsu_with_rollbacks dsu;
QueryTree() {}
QueryTree(int _T, int n) : T(_T) {
    dsu = dsu_with_rollbacks(n);
    t.resize(\bar{4} * \bar{T} + 4):
void add_to_tree(int v, int l, int r, int ul, int ur,
    query& q) {
    if (ul > ur)
    return;
if (1 == ul && r == ur) {
       t[v].push_back(q);
    int mid = (1 + r) / 2;
    add_to_tree(2 * v, 1, mid, ul, min(ur, mid), q);
    add_to_tree(2 * v + 1, mid + 1, r, max(ul, mid + 1),
void add_query(query q, int 1, int r) {
    add_to_tree(1, 0, T - 1, 1, r, q);
void dfs(int v, int 1, int r, vector<int>& ans) {
   for (query& q : t[v]) {
       q.united = dsu.unite(q.v, q.u);
    if (1 == r)
        ans[1] = dsu.comps;
    else {
       int mid = (1 + r) / 2;
       dfs(2 * v, 1, mid, ans);
       dfs(2 * v + 1, mid + 1, r, ans);
    for (query q : t[v]) {
       if (q.united)
           dsu.rollback();
vector<int> solve() -
    vector<int> ans(T);
    dfs(1, 0, T - 1, ans);
```

2.7 link cut tree

```
const int MOD = 998244353;
int sum(int a, int b) {
   return a+b >= MOD ? a+b-MOD : a+b;
int mul(int a, int b) {
   return (a*1LL*b)%MOD;
typedef pair< int , int >Linear;
Linear compose(const Linear &p, const Linear &q) {
   return Linear(mul(p.first, q.first), sum(mul(q.second,
        p.first), p.second));
struct SplayTree {
   struct Node {
        int ch[2] = {0, 0}, p = 0;
        long long self = 0, path = 0;
                                            // Path aggregates
                                            // Subtree aggregates
        long long sub = 0, vir = 0;
        bool flip = 0;
                                            // Lazy tags
        int size = 1:
        Linear _self{1, 0}, _path_shoja{1, 0}, _path_ulta{1, 0};
    véctor<Node> T;
   SplayTree(int n) : T(n + 1) {
       \tilde{T}[0].size = 0;
   void push(int x) {
        if (!x || !T[x].flip) return;
        int 1 = T[x].ch[0], r = T[x].ch[1];
        T[l].flip ^= 1, T[r].flip ^= 1;
swap(T[x].ch[0], T[x].ch[1]);
```

```
T[x].flip = 0;
        swap(T[x]._path_shoja, T[x]._path_ulta);
   void pull(int x) {
        int 1 = T[x].ch[0], r = T[x].ch[1]; push(1); push(r);
       compose(T[x]._self, T[r]._path_ulta));
   void set(int x, int d, int y) {
       T[x].ch[d] = y; T[y].p = x; pull(x);
   void splay(int x) {
   auto dir = [&](int x) {
     int p = T[x].p; if (!p) return -1;
     return T[p].ch[0] == x ? 0 : T[p].ch[1] == x ? 1 :
        auto rotate = [&](int x) {
   int y = T[x].p, z = T[y].p, dx = dir(x), dy =
                  dir(v);
            set(y, dx, T[x].ch[!dx]);
            set(x, !dx, y);
            if (~dy) set(z, dy, x);
            T[x].p = z;
       for (push(x); ~dir(x); ) {
           int y = T[x].p, z = T[y].p;
push(z); push(y); push(x);
            int dx = dir(x), dy = dir(y);
            if (~dy) rotate(dx != dy ? x : y);
            rotate(x);
   int KthNext(int x, int k) {
        assert(k > 0);
        splay(x);
       x = T[x].ch[1];
if (T[x].size < k) return -1;</pre>
        while (true) {
            push(x);
            int l = T[x].ch[0], r = T[x].ch[1];
            if (T[1].size+1 == k) return x;
            if (k \le T[1].size) x = 1;
            else k \rightarrow T[1].size+1, x = r;
   }
struct LinkCut : SplayTree {
   LinkCut(int n) : SplayTree(n) {}
   int access(int x) {
  int u = x, v = 0;
        for (; u; v = u, u = T[u].p) {
            splay(u);
            int& ov = T[u].ch[1];
           T[u].vir += T[ov].sub;
T[u].vir -= T[v].sub;
            ov = v; pull(u);
       splay(x);
return v;
   void reroot(int x) {
   access(x); T[x].flip ^= 1; push(x);
   ///makes v parent of u (optional: u must be a root)
   void Link(int u, int v) {
        reroot(u): access(v):
        T[v].vir += T[u].sub;
        T[u].p = v; pull(v);
   ///removes edge between u and v
   void Cut(int u, int v) {
        int _u = FindRoot(u);
```

3

```
reroot(u); access(v);
T[v].ch[0] = T[u].p = 0; pull(v);
        reroot(_u);
    // Rooted tree LCA. Returns 0 if u and v arent connected.
   int LCA(int u, int v) {
   if (u == v) return u;
        access(u); int ret = access(v);
return T[u].p ? ret : 0;
    // Query subtree of u where v is outside the subtree.
    long long Subtree(int u, int v) {
        int _v = FindRoot(v);
        reroot(v); access(u);
long long ans = T[u].vir + T[u].self;
        reroot(_v);
                                                                           2.8 \quad \text{mo}
        return ans
    // Query path [u..v]
    long long Path(int u, int v) {
        int _u = FindRoot(u);
        reroot(u); access(v);
long long ans = T[v].path;
        reroot(_u);
        return ans
    Linear _Path(int u, int v) {
        reroot(u); access(v); return T[v]._path_shoja;
    // Update vertex u with value v
    void Update(int u, long long v) {
        access(u); T[u].self = v; pull(u);
    // Update vertex u with value v
    void _Update(int u, Linear v) {
        access(u); T[u]._self = v; pull(u);
    int FindRoot(int u) {
        access(u);
while (T[u].ch[0]) {
            u = T[u].ch[0];
            push(u);
        access(u);
        return u:
    ^{\prime}///k-th node (0-indexed) on the path from u to v
    int KthOnPath(int u, int v, int k) {
        if (u == v) return k == 0 ? u : -1;
        int _u = FindRoot(u);
        reroot(u); access(v);
int ans = KthNext(u, k);
        reroot(u):
        return ans
};
// tested on
     https://old.yosupo.jp/problem/dynamic_tree_vertex_set_path_
int main() {
    ios::sync_with_stdio(false);
    cin.tie(0);
    int n, q;
cin >> n >> q;
    LinkCut lct(n);
                                                                           void ini(){
    for (int i = 1; i <= n; i++) {
        Linear 1;
cin >> 1.first >> 1.second:
        lct._Update(i, 1);
    for (int i = 1; i < n; i++) {
        int u, v;
cin >> u >> v;
        lct.Link(u+1, v+1);
    while (q--) {
        int op;
        cin >> op;
        if (op = 0) {
            int u, v, w, x;
cin >> u >> v >> w >> x;
```

```
lct.Cut(u+1, v+1)
         lct.Link(w+1, x+1);
} else if (op == 1) {
             int p; Linear 1;
cin >> p >> 1.first >> 1.second;
              lct._Update(p+1, 1);
         } else {
              int u, v, x;
cin >> u >> v >> x;
              Linear l = lct._Path(u+1, v+1);
              cout << sum(mul(l.first, x), l.second) << "\n";</pre>
    return 0:
struct Query {
   int l, r,k, idx;
    bool operator<(Query other) const
         if(1/block_size!=other.1/block_size) return (1<other.1);
return (1/block_size&1)? (r<other.r) : (r>other.r);
vector<int> mo_s_algorithm(vector<Query> queries) {
    vector<int> answers(queries.size());
    sort(queries.begin(), queries.end());
     // TODO: initialize data structure
    int cur_1 = 0;
int cur_r = -1;
     // invariant: data structure will always reflect the range
           [cur_1, cur_r]
    for (Query q : queries) {
   while (cur_l > q.1) {
              cur_1--;
              add(cur_1);
         while (cur_r < q.r) {</pre>
              cur_r++;
              add(cur_r);
         while (cur_1 < q.1) {
              remove(cur_l);
              cur_1++;
         while (cur_r > q.r) {
             remove(cur_r);
         answers[q.idx] = get_answer();
    return answers;
       sparse table 2d
const int N=500;
const int K = 8; /// k >= ceil(lg22(n)) +1
int arr[N][N];
int st[K+1][K+1][N][N];
int lg2[N+1];
    lg2[1] = 0;
    for (int i = 2; i <= N; i++)
lg2[i] = lg2[i/2] + 1;
int f(int i,int j){
    return max(i,j);
void pre( int n,int m){
    for (int x=0:x<=K:x++) {
         for(int y=0;y<=K;y++){</pre>
              for(int i=0;i<n;i++){</pre>
                  for(int j=0;j<m;j++){</pre>
if(i+(1<<x)>n or j+(1<<y) > m) continue;
if(x>0) st[x][y][i][j] = f(st[x-1][y][i][j] ,
    st[x-1][y][i+(1<<(x-1))][j]);</pre>
```

```
else if(y>0) st[x][y][i][j] = f(st[x][y-1][i][j] ,
    st[x][y-1][i][j+(1<<(y-1))]);
else st[x][y][i][j] = f(arr[i][j] , arr[i][j]);</pre>
        }
   }
int getf( int R1 ,int C1 , int R2 , int C2){
   if(R1>R2) swap(R1,R2);
    if(C1>C2) swap(C1,C2);
int x = lg2[R2 - R1 + 1];
    int y = lg2[C2 - C1 + 1]
    return f(f(f(st[x][y][R1][C1],st[x][y][R2-(1<<x)+1][C1]),
         st[x][y][R1][C2 - (1<<y)+1]),
st[x][y][R2-(1<<x)+1][C2-(1<<y)+1]);
2.10 treap
template <class T>
class treap{
    struct item{
        int prior, cnt;
T key;
item *1,*r;
         item(T v)
             1=NULL:
             r=NULL;
             prior=rand();
    } *root,*node;
    int cnt (item * it){
        return it ? it->cnt : 0;
    void upd_cnt (item * it){
         if^{-}(it) it \rightarrow cnt = cnt(it \rightarrow l) + cnt(it \rightarrow r) + 1;
    void split (item * t, T key, item * & 1, item * & r){
        if '(!t)
    1 = r = NULL;
         else if (key < t->key)
             split (t->1, key, 1, t->1), r = t;
             split (t\rightarrow r, key, t\rightarrow r, r), l = t;
         upd_cnt(t);
    void insert (item * & t, item * it){
        if (!t)
            t = it;
         else if (it->prior > t->prior)
            split (t, it->key, it->l, it->r), t = it;
             insert (it->key < t->key ? t->l : t->r, it);
         upd_cnt(t);
    // keys(1) < keys(r)
    void merge (item * & t, item * 1, item * r){
        if (!1 || !r)
t = 1 ? 1 : r:
        else if (l->prior > r->prior)
            merge (1->r, 1->r, r), t = 1;
             merge (r->1, 1, r->1), t = r:
         upd_cnt(t);
    void erase (item * & t, T key){
        if (t->key == key)
            merge (t, t->1, t->r);
             erase (key < t->key ? t->1 : t->r, key);
         upd_cnt(t);
    T elementAt(item * &t, int key){
        T ans:
```

if(cnt(t->1)==key) ans=t->key;

```
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```

```
else if(cnt(t->1)>key) ans=elementAt(t->1,key);
        else ans=elementAt(t->r,key-1-cnt(t->l));
        upd_cnt(t);
        return ans;
    item * unite (item * 1. item * r){
        if (!1 || !r) return 1 ? 1 : r;
        if (1->prior < r->prior) swap (1, r);
       item * lt, * rt;
split (r, l->key, lt, rt);
l->l = unite (l->l, lt);
        1->r = unite (1->r, rt):
        upd_cnt(1);
        upd_cnt(r);
        return 1;
    void heapify (item * t){
   if (!t) return;
        item * max = t
        if (t->1 != NULL && t->1->prior > max->prior)
            max = t -> 1:
        if (t->r != NULL && t->r->prior > max->prior)
            \max = t->r;
           (max != t)
            swap (t->prior, max->prior);
            heapify (max);
    item * build (T * a, int n){
   if (n == 0) return NULL;
        int mid = n / 2;
        item * t = new item (a[mid], rand ());
        t->1 = build (a, mid);
        t->r = build (a' + mid' + 1, n - mid - 1):
        heapify (t);
return t;
    void output (item * t,vector<T> &arr){
        if (!t) return;
        output (t->1,arr);
        arr.push_back(t->key);
        output (t->r,arr);
public:
    treap(){
        root=NULL:
    treap(T *a,int n){
        build(a.n):
    void insert(T value){
        node=new item(value);
        insert(root.node):
    void erase(T value){
        erase(root, value);
    T elementAt(int position){
        return elementAt(root, position);
    int size(){
        return cnt(root);
    void output(vector<T> &arr){
        output(root,arr);
    int range_query(T 1,T r){ //(1,r]
        item *previous,*next,*current;
        split(root,1,previous,current);
        split(current,r,current,next);
        int ans=cnt(current);
        merge(root,previous,current);
        merge(root,root,next);
previous=NULL;
       current=NULL;
next=NULL;
return ans;
};
```

```
template <class T>
class implicit_treap{
   struct item{
       int prior, cnt;
       T value;
        bool rev;
        item *1, *r;
        item(T v){
           value=v;
           rev=false;
l=NULL:
           r=NULL;
           cnt=1;
           prior=rand();
   } *root,*node;
   int cnt (item * it){
   return it ? it->cnt : 0;
   void upd_cnt (item * it){
       if (it)
           it->cnt = cnt(it->1) + cnt(it->r) + 1;
   void push (item * it){
       if (it && it->rev){
           it->rev = false;
           swap (it->l, it->r);
           if (it->1) it->1->rev ^= true:
           if (it->r) it->r->rev ^= true;
   void merge (item * & t, item * 1, item * r){
       push (1);
       push (r);
       if (!1 || !r)
t = 1 ? 1 : r:
        else if (l->prior > r->prior)
           merge (1-r, 1-r, r), t = 1;
       else
           merge (r->1, 1, r->1), t = r:
       upd_cnt (t);
   void split (item * t, item * & 1, item * & r, int key, int
        add = 0){
        if (!t)
           return void( 1 = r = 0 );
       push (t);
        int cur_key = add + cnt(t->1);
       if (key <= cur_key)</pre>
           split (t->1, 1, t->1, key, add), r = t;
           split (t->r, t->r, r, key, add + 1 + cnt(t->1)). 1
       upd_cnt (t);
   void insert(item * &t,item * element,int key){
       item *1,*r;
split(t,1,r,key);
       merge(1,1,element);
       merge(t,1,r);
       1=NULL;
       r=NULL;
   T elementAt(item * &t, int key){
       push(t);
        if(cnt(t->1)==key) ans=t->value;
        else if(cnt(t->1)>key) ans=elementAt(t->1,key);
        else ans=elementAt(t->r, kev-1-cnt(t->1)):
   void erase (item * & t, int key){
       push(t);
       if(!t) return;
        if (\text{key} == \text{cnt}(t->1))
           merge (t, t->1, t->r);
        else if(kev<cnt(t->1))
           erase(t->1,key);
           erase(t->r,key-cnt(t->1)-1);
```

```
upd_cnt(t);
   void reverse (item * &t, int 1, int r){
       item *t1, *t2, *t3;

split (t, t1, t2, 1);

split (t2, t2, t3, r-l+1);
       t2->rev ^= true:
       merge (t, t1, t2);
       merge (t, t, t3);
   void cyclic_shift(item * &t,int L,int R){
       if(L==R) return;
        itèm *1,*r,*m;
        split(t,t,l,L)
        split(1,1,m,R-L+1);
       split(1,1,r,R-L);
       merge(t,t,r);
       merge(t,t,1);
       merge(t,t,m);
1=NULL;
r=NULL;
        m=NULL;
   void output (item * t,vector<T> &arr){
       if (!t) return:
       push (t);
       output (t->1,arr);
       arr.push_back(t->value);
       output (t->r,arr);
public:
   implicit_treap(){
   root=NULL:
   void insert(T value, int position){
       node=new item(value);
        insert(root, node, position);
   void erase(int position){
        erase(root, position);
    void reverse(int 1,int r){
       reverse(root.1.r):
   T elementAt(int position){
       return elementAt(root, position);
   void cvclic shift(int L.int R){
        cyclic_shift(root,L,R);
    int size(){
       return cnt(root);
   void output(vector<T> &arr){
        output(root.arr):
2.11 wavelet tree
```

```
#include <bits/stdc++.h>
using namespace std;
#define fo(i,n) for(i=0;i< n;i++)
#define 11 long long
#define pb push_back
#define mp make_pair
typedef pair<int, int> pii;
typedef pair<11, ll> pl;
typedef vector<int>
const int N = 3e5, M = N;
const int MAX = 1e6;
int a[N];
struct wavelet_tree{
#define vi vector<int>
#define pb push_back
   int lo, hi;
wavelet_tree *l=0, *r=0;
    vi b:
    vi c; // c holds the prefix sum of elements
```

```
6
```

```
//nos are in range [x,y]
//array indices are [from, to)
wavelet_tree(int *from, int *to, int x, int y){
   lo = x, hi = y;
    if( from >= to)
        return:
    if( hi == lo ){
       b.reserve(to-from+1):
       b.pb(0);
       c.reserve(to-from+1);
       c.pb(0);
       for(auto it = from; it != to; it++){
            b.pb(b.back() + 1);
            c.pb(c.back()+*it);
       return :
    int mid = (lo+hi)/2;
    auto f = [mid](int x){
       return x <= mid:
   b.reserve(to-from+1):
    b.pb(0);
    c.reserve(to-from+1):
    c.pb(0);
    for(auto it = from; it != to; it++){
       b.pb(b.back() + f(*it));
       c.pb(c.back() + *it);
    //see how lambda function is used here
    auto pivot = stable_partition(from, to, f);
   1 = new wavelet_tree(from, pivot, lo, mid);
   r = new wavelet_tree(pivot, to, mid+1, hi);
// swap a[i] with a[i+1] , if a[i]!=a[i+1] call
     swapadjacent(i)
void swapadjacent(int i){
   if(lo == hi)
   b[i] = b[i-1] + b[i+1] - b[i];
c[i] = c[i-1] + c[i+1] - c[i];
if( b[i+1]-b[i] == b[i] - b[i-1]){
       if(b[i]-b[i-1])
           return this->l->swapadjacent(b[i]);
           return this->r->swapadjacent(i-b[i]);
       return ;
//kth smallest element in [1, r]
int kth(int 1, int r, int k){
    if(1 > r)
       return 0;
    if(lo == hi)
       return lo;
    int inLeft = b[r] - b[1-1];
    int lb = b[1-1]; //amt of nos in first (1-1) nos that
         go in left
    int rb = b[r]: //amt of nos in first (r) nos that go in
        left
    if(k <= inLeft)</pre>
       return this->l->kth(lb+1, rb, k):
    return this->r->kth(l-lb, r-rb, k-inLeft);
//count of nos in [1, r] Less than or equal to k
int LTE(int 1, int r, int k){
    if(1 > r or k < 1o)
       return 0:
    if(hi <= k)
    return r - 1 + 1;
int lb = b[1-1], rb = b[r];
   return this->l->LTE(lb+1, rb, k) + this->r->LTE(l-lb,
        r-rb. k):
//count of nos in [1, r] equal to k
int count(int 1, int r, int k){
    if(1 > r or k < lo or k > hi)
    return 0;
if(lo == hi)
```

```
return r - 1 + 1;
int lb = b[1-1], rb = b[r], mid = (1o+hi)/2;
        if(k \le mid)
            return this->l->count(lb+1, rb, k);
        return this->r->count(1-1b, r-rb, k);
    //sum of nos in [l ,r] less than or equal to k
    int sumk(int 1, int r, int k){
        if(1 > r or k < 1o)
            return 0;
         if(hi \le k)
        return c[r] - c[l-1];
int lb = b[l-1], rb = b[r];
        return this->l->sumk(lb+1, rb, k) + this->r->sumk(l-lb,
             r-rb, k);
     wavelet_tree(){
        if(1)
        delete 1;
        if(r)
        delete r;
int main(){
    ios base::svnc with stdio(false):
    cin.tie(NULL);
    srand(time(NULL)):
    int i,n,k,j,q,l,r;
    cin >> n;
    fo(i, n) cin >> a[i+1]:
    wavelet_tree T(a+1, a+n+1, 1, MAX);
    cin >> q;
    while (q--) {
        int x;
cin >> x;
cin >> 1 >> r >> k;
        if(x == 0)
            //kth smallest
            cout << "Kth smallest: ";
cout << T.kth(1, r, k) << endl;</pre>
        if(x == 1){
             //less than or equal to K
            cout << "LTE: "
            cout << T.LTE(1, r, k) << endl;</pre>
            //count occurence of K in [1, r]
cout << "Occurence of K: ";
cout << T.count(1, r, k) << endl;</pre>
             //sum of elements less than or equal to K in [1, r]
            cout << "Sum: '
            cout << T.sumk(1, r, k) << endl:</pre>
    return 0;
     Geo
```

3.1 3dGeo

```
int dcmp(double x) \{ return abs(x) < EPS ? 0 : (x<0 ? -1 : 1); \}
double degreeToRadian(double rad) { return rad*PI/180; }
struct Point {
   double x, y, z;
   Point(): x(0), y(0), z(0) {}
   Point(double X, double Y, double Z): x(X), v(Y), z(Z) {}
   Point operator + (const Point& u) const {
       return Point(x + u.x, y + u.y, z + u.z);
   Point operator - (const Point& u) const {
       return Point(x - u.x. v - u.v. z - u.z):
   Point operator * (const double u) const {
       return Point(x * u, y * u, z * u);
   Point operator / (const double u) const {
       return Point(x / u, y / u, z / u);
```

```
friend std::ostream &operator << (std::ostream &os. const
         Point &p) {
        return os << p.x << " " << p.y <<" "<<p.z;
    friend std::istream & operator >> (std::istream &is, Point
        return is >> p.x >> p.y >> p.z;
 double dot(Point a, Point b) {
    return a.x * b.x + a.y * b.y + a.z * b.z;
Point cross(Point a, Point b) {
    return Point(a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z, a.x*b.y
         - a.v*b.x);
 double length(Point a)
    return sqrt(dot(a, a));
 double distance(Point a. Point b) {
    return length(a-b);
Point unit(const Point &p) {
    return p/length(p);
 // Rotate p around axis x, with angle radians.
Point rotate(Point p, Point axis, double angle) {
    axis = unit(axis):
    Point comp1 = p * cos(angle);
    Point comp2 = axis * (1-cos(angle)) * dot(axis, p);
    Point comp3 = cross(axis, p) * sin(angle);
    return comp1 + comp2 + comp3;
 struct Line {Point a, v;}; ///a+tv
 // returns the distance from point a to line l
 double distancePointLine(Point p, Line 1) {
    return length(cross(l.v, p - l.a)) / length(l.v);
 /// distance from Line ab to Line cd
 double distanceLineLine(Line a, Line b) {
    Point cr = cross(a.v, b.v);
    double crl = length(cr);
    if (dcmp(crl) == 0) return distancePointLine(a.a, b);
    return abs(dot(cr. a.a-b.a))/crl:
 struct Plane {
    Point normal; /// Normal = (A, B, C)
double d: /// dot(Normal) = d <--> Ax + By + Cz = d
                 /// anyPoint on the plane, optional
    Point P;
    Plane(Point normal, double d) {
        double len = length(normal);
        assert(dcmp(len) > 0);
        normal = normal / len:
        d = d / len;
        if (dcmp(normal.x)) P = Point(d/normal.x, 0, 0);
        else if (dcmp(normal.y)) P = Point(0, d/normal.y, 0);
                               P = Point(0, 0, d/normal.z):
     ///Plane given by three Non-Collinear Points
    Plane(Point a, Point b, Point c) {
        normal = unit(cross(b-a, c-a));
        d = dot(normal, a);
        \tilde{P} = \tilde{a};
     bool onPlane(Point a) {
        return dcmp(dot(normal, a) - d) == 0;
    double distance(Point a) {
        return abs(dot(normal, a) - d);
    double isParallel(Line 1) {
        return dcmp(dot(1.v, normal)) == 0;
    //return t st l.a + t*l.v is a point on the plane, check
         parallel first
    double intersectLine(Line 1) {
        return dot(P-1.a, normal)/dot(1.v, normal);
```

```
};
```

3.2 Circle Cover

```
///Check if the all of the area of circ(0, R) in
///Circ(OO, RR) is covered by some other circle
bool CoverCircle(PT O, double R, vector<PT> &cen,
       vector<double> &rad, PT 00, double RR) {
  int n = cen.size();
vector<pair<double, double>> arcs;
  for (int i=0; i<n; i++) {
  PT P = cen[i]; double r = rad[i];</pre>
    if (i = 0 && R + sqrt(dist2(0, P))<r) return 1;
if (i = 0 && r + sqrt(dist2(0, P))<R) return 1;</pre>
     vector<PT> inter =
                 CircleCircleIntersection(0, P, R, r);
     if (inter.size() <= 1) continue;</pre>
    If (Inter-12e() - 1) continue,
PT X = inter[0], Y = inter[1];
if (cross(0, X, Y) < 0) swap(X, Y);
if (!(cross(0, X, P) >= 0 &&
cross(0, Y, P) <= 0)) swap(X, Y);
    if (i==0) swap(X, Y);
X = X-0: Y=Y-0:
     double 11 = atan2(X.y, X.x);
     double rr = atan2(Y.y, Y.x);
    if (rr < 11) rr += 2*PI;
arcs.emplace_back(11, rr);</pre>
  if (arcs.empty()) return false;
  sort(arcs.begin(), arcs.end());
double st = arcs[0].ff, en = arcs[0].ss,ans = 0;
for (int i=1; i<arcs.size(); i++) {</pre>
     if (arcs[i].first <= en + EPS)</pre>
     en = max(en, arcs[i].second);
else st = arcs[i].first, en = arcs[i].second;
     ans = max(ans, en-st);
  return ans >= 2*PI;
```

3.3 Circle Union Area

```
struct Point {
  LD x,y;
  LD operator*(const Point &a)const {
  return x*a.y-y*a.x;}
LD operator/(const Point &a)const {
     return sqrt((a.x-x)*(a.x-x)+(a.y-y)*(a.y-y));}
}po[N];
ĹĎ r[N];
int sgn(LD x) {return fabs(x) < EPS?0:(x > 0.0?1:-1):}
pair<LD,bool> ARG[2*N]
LD cir_union(Point c[],LD r[],int n) {
   LD sum = 0.0 , sum1 = 0.0 ,d,p1,p2,p3 ;
   for(int i = 0 ; i < n ; i++) {
     bool f = 1;
     for(int j = 0 ; f&&j<n ; j++)
  if(i!=j && sgn(r[j]-r[i]-c[i]/c[j])!=-1)f=0;</pre>
     if(!f) swap(r[i],r[--n]),swap(c[i--],c[n]);
  for(int i = 0; i < n; i++) {
       int k = 0, cnt = 0;
       for(int j = 0; j < n; j++) {
   if(i!=j&&sgn((d=c[i]/c[j])-r[i]-r[j])<=0){</pre>
            p3=acos((r[i]*r[i]+d*d-r[j]*r[j])/
                                              (2.0*r[i]*d)):
            p2=atan2(c[j].y-c[i].y,c[j].x-c[i].x);
p1 = p2-p3; p2 = p2+p3;
if(sgn(p1+PI)==-1) p1+=2*PI,cnt++;
            if(sgn(p2-PI)==1) p2-=2*PI,cnt++;
ARG[k++] = make_pair(p1,0);
            ARG[k++] = make_pair(p2,1);
       if(k) {
          sort(ARG,ARG+k);
         p1 = ARG[k-1].first-2*PI;
          p3 = r[i]*r[i];
```

3.4 basic-area-geometry

```
struct point2d {
   ftype x, y;
point2d() {}
   point2d(ftype x, ftype y): x(x), y(y) {}
    point2d& operator+=(const point2d &t)
       x += t.x;
y += t.y;
        return *this:
   point2d& operator-=(const point2d &t) {
       x -= t.x;
y -= t.y;
        return *this;
   point2d& operator*=(ftype t) {
       x *= t;
        y *= t;
        return *this;
   point2d& operator/=(ftype t) {
       x /= t;
       y /= t;
        return *this;
   point2d operator+(const point2d &t) const {
        return point2d(*this) += t;
   point2d operator-(const point2d &t) const {
        return point2d(*this) -= t;
   point2d operator*(ftype t) const {
        return point2d(*this) *= t;
   point2d operator/(ftype t) const {
       return point2d(*this) /= t;
point2d operator*(ftype a, point2d b) {
   return b * a;
struct point3d {
   ftype x, y, z;
point3d() {}
    point3d(ftype x, ftype y, ftype z): x(x), y(y), z(z) {}
    point3d& operator+=(const point3d &t) {
       x += t.x;
y += t.y;
        z += t.z;
        return *this;
   point3d& operator = (const point3d &t) {
       x -= t.x;
y -= t.y;
        z = t.z;
        return *this:
   point3d& operator*=(ftype t) {
       x *= t;
y *= t;
z *= t;
        return *this:
```

```
point3d& operator/=(ftype t) {
       x /= t;
       y /= t;
       z /= t;
       return *this:
   point3d operator+(const point3d &t) const {
       return point3d(*this) += t:
   point3d operator-(const point3d &t) const {
       return point3d(*this) -= t;
   point3d operator*(ftype t) const {
       return point3d(*this) *= t;
   point3d operator/(ftype t) const {
       return point3d(*this) /= t;
point3d operator*(ftype a, point3d b) {
   return b * a:
ftype dot(point2d a, point2d b) {
   return a.x * b.x + a.y * b.y;
ftype dot(point3d a, point3d b) {
   return a.x * b.x + a.y * b.y + a.z * b.z;
ftype norm(point2d a) {
   return dot(a, a);
double abs(point2d a) {
   return sqrt(norm(a));
double proj(point2d a, point2d b) {
   return dot(a, b) / abs(b);
double angle(point2d a, point2d b) {
   return acos(dot(a, b) / abs(a) / abs(b));
point3d cross(point3d a, point3d b) {
   return point3d(a.v * b.z - a.z * b.v,
                 a.z * b.x - a.x * b.z,
                 a.x * b.y - a.y * b.x);
ftype triple(point3d a, point3d b, point3d c) {
   return dot(a, cross(b, c));
ftype cross(point2d a, point2d b) {
   return a.x * b.y - a.y * b.x;
point2d intersect(point2d a1, point2d d1, point2d a2, point2d
    d2) {
   return a1 + cross(a2 - a1, d2) / cross(d1, d2) * d1:
point3d intersect(point3d a1, point3d n1, point3d a2, point3d
   n2, point3d a3, point3d n3) {
point3d x(n1.x, n2.x, n3.x);
   point3d y(n1.y, n2.y, n3.y);
   point3d z(n1.z, n2.z, n3.z);
   point3d d(dot(a1, n1), dot(a2, n2), dot(a3, n3));
   return point3d(triple(d, y, z),
                 triple(x, d, z),
                 triple(x, y, d)) / triple(n1, n2, n3);
int signed_area_parallelogram(point2d p1, point2d p2, point2d
   return cross(p2 - p1, p3 - p2);
double triangle_area(point2d p1, point2d p2, point2d p3) {
   return abs(signed_area_parallelogram(p1, p2, p3)) / 2.0;
bool clockwise(point2d p1, point2d p2, point2d p3) {
   return signed_area_parallelogram(p1, p2, p3) < 0;
bool counter_clockwise(point2d p1, point2d p2, point2d p3) {
   return signed_area_parallelogram(p1, p2, p3) > 0;
```

```
double area(const vector<point>& fig) {
   double res = 0;
   for (unsigned i = 0; i < fig.size(); i++) {</pre>
       point p = i ? fig[i - 1] : fig.back();
       point q = fig[i];
       res += (p.x - q.x) * (p.y + q.y);
   return fabs(res) / 2;
//Pick: S = I + B/2 - 1
int count_lattices(Fraction k, Fraction b, long long n) {
   auto fk = k.floor();
   auto fb = b.floor()
   auto cnt = OLL;
   if (k >= 1 || b >= 1) {
       cnt += (fk * (n - 1) + 2 * fb) * n / 2;
       k -= fk;
b -= fb;
   auto t = k * n + b:
   auto ft = t.floor();
   if (ft >= 1) {
       cnt += count_lattices(1 / k, (t - t.floor()) / k,
            t.floor());
   return cnt;
```

3.5 delaunay-voronoi

```
typedef long long ll;
bool ge(const ll& a, const ll& b) { return a >= b; }
bool le(const ll& a, const ll& b) { return a <= b; }
bool eq(const ll& a, const ll& b) { return a == b; }
bool gt(const ll& a, const ll& b) { return a > b; }
bool lt(const ll& a, const ll& b) { return a < b; }
int sgn(const ll& a) { return a >= 0 ? a ? 1 : 0 : -1; }
struct pt {
    11 x, y;
    pt() { }
    pt(ll _x, ll _y) : x(_x), y(_y) { }
    pt operator-(const pt& p) const {
        return pt(x - p.x, \bar{y} - p.y);
    11 cross(const pt& p) const {
        return x * p.y - y * p.x;
    11 cross(const pt& a, const pt& b) const {
        return (a - *this).cross(b - *this):
    11 dot(const pt% p) const {
        return x * p.x + y * p.y;
    11 dot(const pt& a, const pt& b) const {
         return (a - *this).dot(b - *this);
    11 sqrLength() const {
         return this->dot(*this);
    bool operator==(const pt& p) const {
        return eq(x, p.x) && eq(y, p.y);
const pt inf_pt = pt(1e18, 1e18);
struct QuadEdge {
    pt origin;
    QuadEdge* rot = nullptr;
    QuadEdge* onext = nullptr;
    bool used = false;
    QuadEdge* rev() const {
        return rot->rot:
    QuadEdge* lnext() const {
        return rot->rev()->onext->rot;
    QuadEdge* oprev() const {
        return rot->onext->rot:
    pt dest() const {
         return rev()->origin;
```

```
QuadEdge* make_edge(pt from, pt to) {
   QuadEdge* e1 = new QuadEdge;
   QuadEdge* e2 = new QuadEdge;
   QuadEdge* e3 = new QuadEdge;
   QuadEdge* e4 = new QuadEdge;
   e1->origin = from;
   e2->oriğin = to;
   e3->origin = e4->origin = inf_pt;
   e1->rot = e3:
   e2->rot = e4;
   e3 \rightarrow rot = e2;
   e4->rot = e1;
   e1->onext = é1
   e2 - > onext = e2
   e3 \rightarrow onext = e4
   e4 \rightarrow onext = e3;
   return e1;
void splice(QuadEdge* a, QuadEdge* b) {
   swap(a->onext->rot->onext, b->onext->rot->onext);
   swap(a->onext, b->onext):
void delete_edge(QuadEdge* e) {
   splice(e, e->oprev());
   splice(e->rev(), e->rev()->oprev());
   delete e->rev()->rot;
   delete e->rev();
   delete e->rot;
   delete e;
QuadEdge* connect(QuadEdge* a, QuadEdge* b) {
   QuadEdge* e = make_edge(a->dest(), b->origin);
   splice(e, a->lnext());
   splice(e->rev(), b);
   return e;
bool left_of(pt p, QuadEdge* e) {
   return gt(p.cross(e->origin, e->dest()), 0);
bool right_of(pt p, QuadEdge* e) {
   return lt(p.cross(e->origin, e->dest()), 0);
T det3(T a1, T a2, T a3, T b1, T b2, T b3, T c1, T c2, T c3)
   return a1 * (b2 * c3 - c2 * b3) - a2 * (b1 * c3 - c1 * b3)
          a3 * (b1 * c2 - c1 * b2);
bool in_circle(pt a, pt b, pt c, pt d) {
// If there is __int128, calculate directly.
// Otherwise, calculate angles.
#if defined(__LP64__) || defined(_WIN64)
    __int128 det = -det3<__int128>(b.x, b.y, b.sqrLength(),
        c.x, c.y,
                                c.sqrLength(), d.x, d.y,
                                     d.sqrLength());
   det += det3 < _int128 > (a.x, a.y, a.sqrLength(), c.x, c.y,
        c.sqrLength(), d.x,
                        d.y, d.sqrLength());
   det -= det3<__int128>(a.x, a.y, a.sqrLength(), b.x, b.y,
        b.sqrLength(), d.x,
                        d.y, d.sqrLength());
   det += det3<__int128>(a.x, a.y, a.sqrLength(), b.x, b.y,
        b.sqrLength(), c.x,
                        c.y, c.sqrLength());
   return det > 0:
   auto ang = [](pt 1, pt mid, pt r) {
       ll x = mid.dot(l, r);
       ll v = mid.cross(l, r)
       long double res = atan2((long double)x, (long double)y);
   long double kek = ang(a, b, c) + ang(c, d, a) - ang(b, c,
        d) - ang(d, a, b);
   if (kek > 1e-8)
       return true:
   else
```

```
return false:
#endif
pair<QuadEdge*, QuadEdge*> build_tr(int 1, int r, vector<pt>&
   if(r-1+1==2) {
       QuadEdge* res = make_edge(p[1], p[r]);
       return make_pair(res, res->rev());
   if (r - 1 + 1 == 3) {
       QuadEdge *a = make_edge(p[1], p[1 + 1]), *b =
            make_edge(p[1 + 1], p[r]);
       splice(a->rev(), b);
int sg = sgn(p[1].cross(p[1 + 1], p[r]));
       if (sg == 0)
           return make_pair(a, b->rev());
       QuadEdge* c = connect(b, a);
       if (sg == 1)
           return make_pair(a, b->rev());
       else
           return make_pair(c->rev(), c);
   int mid = (1 + r) / 2;
QuadEdge *ldo, *ldi, *rdo, *rdi;
   tie(ldo, ldi) = build_tr(1, mid, p);
   tie(rdi, rdo) = build_tr(mid + 1, r, p);
   while (true) {
       if (left_of(rdi->origin, ldi)) {
           ldi = ldi->lnext();
           continue;
       if (right_of(ldi->origin, rdi)) {
           rdi = rdi->rev()->onext;
           continue;
       break:
   QuadEdge* basel = connect(rdi->rev(), ldi);
   auto valid = [&basel](QuadEdge* e) { return
        right_of(e->dest(), basel); };
   if (ldi->origin == ldo->origin)
       ldo = basel->rev();
   if (rdi->origin == rdo->origin)
       rdo = basel:
    while (true) {
       QuadEdge* lcand = basel->rev()->onext:
       if (valid(lcand)) {
           while (in_circle(basel->dest(), basel->origin,
                lcand->dest().
                          lcand->onext->dest())) {
               QuadEdge* t = lcand->onext;
               delete_edge(lcand);
               lcand = t:
       QuadEdge* rcand = basel->oprev();
       if (valid(rcand)) {
           while (in_circle(basel->dest(), basel->origin,
                rcand->dest().
                          rcand->oprev()->dest())) {
               QuadEdge* t = rcand->oprev();
               delete edge(rcand):
              rcand = t:
       if (!valid(lcand) && !valid(rcand))
           break:
       if (!valid(lcand) ||
           (valid(rcand) && in_circle(lcand->dest(),
                lcand->origin,
                                    rcand->origin,
                                         rcand->dest())))
           basel = connect(rcand, basel->rev());
       else
           basel = connect(basel->rev(), lcand->rev());
   return make_pair(ldo, rdo);
vector<tuple<pt, pt, pt>> delaunay(vector<pt> p) {
```

```
sort(p.begin(), p.end(), [](const pt& a, const pt& b)
    return lt(a.x, b.x) | | (eq(a.x, b.x) && lt(a.y, b.y));
auto res = build_tr(0, (int)p.size() - 1, p);
QuadEdge* e = res.first;
vector<QuadEdge*> edges = {e};
while (lt(e->onext->dest().cross(e->dest(), e->origin), 0))
    e = e->onext:
auto add = [&p, &e, &edges]() {
  QuadEdge* curr = e;
    do {
        curr->used = true:
        p.push_back(curr->origin);
        edges.push_back(curr->rev());
        curr = curr->lnext():
    } while (curr != e):
add();
p.clear();
int kek = 0;
while (kek < (int)edges.size()) {</pre>
    if (!(e = edges[kek++])->used)
        add():
vector<tuple<pt, pt, pt>> ans;
for (int i = 0; i < (int)p.size(); i += 3) {</pre>
    ans.push_back(make_tuple(p[i], p[i + 1], p[i + 2]);
return ans;
```

3.6 half-plane-intersection

```
class HalfPlaneIntersection{
   static double eps, inf;
public:
   struct Point{
       double x, y;
       explicit Point(double x = 0, double y = 0) : x(x), y(y)
       // Addition, substraction, multiply by constant, cross
           product.
       friend Point operator + (const Point& p, const Point&
          return Point(p.x + q.x, p.y + q.y);
       friend Point operator - (const Point& p, const Point&
          return Point(p.x - q.x, p.y - q.y);
       friend Point operator * (const Point& p. const double&
          return Point(p.x * k, p.v * k):
       friend double cross(const Point& p, const Point& q){
          return p.x * q.y - p.y * q.x;
// Basic half-plane struct.
   struct Halfplane{
       // 'p' is a passing point of the line and 'pq' is the
            direction vector of the line.
       Point p, pq;
       double angle;
       Halfplane() {}
       Halfplane(const Point& a, const Point& b) : p(a), pq(b
          angle = atan21(pq.y, pq.x);
         Check if point 'r' is outside this half-plane.
       // Every half-plane allows the region to the LEFT of
       bool out(const Point& r){
          return cross(pq, r - p) < -eps;</pre>
       // Comparator for sorting.
       // If the angle of both half-planes is equal, the
            leftmost one should go first.
       bool operator < (const Halfplane& e) const{
```

```
if (fabsl(angle - e.angle) < eps) return cross(pq,
                e.p - p) < 0;
           return angle < e.angle;
       // We use equal comparator for std::unique to easily remove parallel half-planes.
       bool operator == (const Halfplane& e) const{
           return fabsl(angle - e.angle) < eps;
       // Intersection point of the lines of two half-planes.
            It is assumed they're never parallel.
       friend Point inter(const Halfplane& s, const Halfplane&
            t){
           double alpha = cross((t.p - s.p), t.pq) /
           cross(s.pq, t.pq);
return s.p + (s.pq * alpha);
   };
   static vector<Point> hp_intersect(vector<Halfplane>& H){
       Point box[4] = //Bounding box in CCW order{
           Point(inf, inf),
           Point(-inf, inf)
           Point(-inf, -inf)
           Point(inf, -inf)
       for (int i = 0; i < 4; i++) // Add bounding box
            half-planes.{
           Halfplane aux(box[i], box[(i+1) % 4]);
           H.push_back(aux);
       // Sort and remove duplicates
       sort(H.begin(), H.end());
       H.erase(unique(H.begin(), H.end()), H.end());
       deque < Halfplane > dq;
       int len = 0;
       for(int i = 0; i < int(H.size()); i++){</pre>
           // Remove from the back of the deque while last
                half-plane is redundant
           while (len > 1 && H[i].out(inter(dq[len-1],
                dq[len-2]))){
               dq.pop_back();
--len:
           // Remove from the front of the deque while first
                half-plane is redundant
           while (len > 1 && H[i].out(inter(dq[0], dq[1]))){
               dq.pop_front();
--len:
           // Add new half-plane
dq.push_back(H[i]);
++len;
       // Final cleanup: Check half-planes at the front
            against the back and vice-versa
       while (len > 2 && dq[0].out(inter(dq[len-1],
            dq[len-2]))){
           dq.pop_back();
--len:
       while (len > 2 && dq[len-1].out(inter(dq[0], dq[1]))){
           dq.pop_front();
--len:
       // Report empty intersection if necessary
       if (len < 3) return vector<Point>();
       // Reconstruct the convex polygon from the remaining
            half-planes.
       vector<Point> ret(len);
       for(int i = 0; i+1 < len; i++){
   ret[i] = inter(dq[i], dq[i+1]);</pre>
       ret.back() = inter(dq[len-1], dq[0]);
       return ret:
double HalfPlaneIntersection::eps=1e-9;
double HalfPlaneIntersection::inf=1e9;
```

3.7 heart-of-geometry-2d

```
typedef double ftype;
const double EPS = 1E-9;
struct pt{
   ftype x, y; int id:
   pt() {}
   pt(ftype _x, ftype _y):x(_x), y(_y) {}
   pt operator+(const pt & p) const{
       return pt(x + p.x, y + p.y);
   pt operator-(const pt & p) const{
       return pt(x - p.x, y - p.y);
   ftype cross(const pt & p) const{
       return x * p.y^- y * p.x;
   ftype dot(const pt & p) const{
        return x * p.x + y * p.y;
   ftype cross(const pt & a, const pt & b) const{
       return (a - *this).cross(b - *this);
   ftype dot(const pt & a, const pt & b) const{
       return (a - *this).dot(b - *this);
   ftype sqrLen() const{
       return this->dot(*this);
   bool operator<(const pt& p) const{
   return x < p.x - EPS || (abs(x - p.x) < EPS && y < p.y
             - EPS):
   bool operator==(const pt% p) const{
       return abs(x-p.x)<EPS && abs(y-p.y)<EPS;
int sign(double x) { return (x > EPS) - (x < -EPS); }</pre>
inline int orientation(pt a, pt b, pt c) { return
     sign(a.cross(b,c)); }
bool is_point_on_seg(pt a, pt b, pt p) {
   if (fabs(b.cross(p,a)) < EPS) {</pre>
        if (p.x < min(a.x, b.x) - EPS \mid\mid p.x > max(a.x, b.x) +
             EPS) return false;
        if (p.y < min(a.y, b.y) - EPS \mid\mid p.y > max(a.y, b.y) +
             EPS) return false:
        return true:
   return false:
bool is_point_on_polygon(vector<pt> &p, const pt& z) {
   int n = p.size();
   for (int i = 0; i < n; i++) {
        if (is_point_on_seg(p[i], p[(i + 1) % n], z)) return 1;
   return 0:
int winding_number(vector<pt> &p, const pt& z) { // O(n)
   if (is_point_on_polygon(p, z)) return 1e9;
   int n = p.size(), ans = 0;
for (int i = 0; i < n; ++i) {</pre>
       int j = (i + 1) \% n;
       bool below = p[i].y < z.y;
        if (below != (p[j].y < z.y)) {</pre>
           auto orient = orientation(z, p[j], p[i]);
           if (orient == 0) return 0:
           if (below == (orient > 0)) ans += below ? -1 : 1;
       }
   return ans:
double dist_sqr(pt a,pt b){
   return ((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
double dist(pt a, pt b){
   return \operatorname{sqrt}((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y));
```

```
double angle(pt a,pt b,pt c){
    if(b==a | b==c) return 0;
    double A2 = dist_sqr(b,c);
    double C2 = dist_sqr(a,b);
    double B2 = dist_sqr(c,a);
    double A = \operatorname{sqrt}(\overline{A2}), C = \operatorname{sqrt}(C2);
    double ans = (A2 + C2 - B2)/(A*C*2);
    if(ans<-1) ans=acos(-1);
    else if(ans>1) ans=acos(1):
    else ans = acos(ans):
    return ans:
bool cmp(pt a, pt b){
    return a.x < b.x || (a.x == b.x && a.v < b.v);</pre>
bool ccw(pt a, pt b, pt c, bool include_collinear=false) {
    int o = orientation(a, b, c);
    return o > 0 || (include_collinear && o == 0);
bool cw(pt a, pt b, pt c, bool include_collinear=false) {
    int o = orientation(a, b, c);
    return o < 0 || (include_collinear && o == 0);
bool collinear(pt a, pt b, pt c) { return orientation(a, b, c)
double area(pt a, pt b, pt c){
    return (a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y))/2;
struct cmp_x{
    bool operator()(const pt & a, const pt & b) const{
        return a.x < b.x |  (a.x == b.x && a.y < b.y);
};
struct cmp_y{
    bool operator()(const pt & a, const pt & b) const{
return a.y < b.y | [ (a.y == b.y && a.x < b.x);
struct circle : pt {
   ftype r;
bool insideCircle(circle c, pt p){
    return dist_sqr(c,p) <= c.r*c.r + EPS;</pre>
    ftype a, b, c;
    line() {}
    line(pt p, pt q){
    a = p.y - q.y;
    b = q.x - p.x;
        c = -a * p.x - b * p.y;
        norm();
    void norm(){
        double z = sqrt(a * a + b * b);
        if (abs(z) > EPS)
            a /= z, b /= z, c /= z;
    line getParallel(pt p){
        line ans = *this:
        ans.c = -(ans.a*p.x+ans.b*p.y);
        return ans;
    ftype getValue(pt p){
        return a*p.x+b*p.y+c;
    line getPerpend(pt p){
        line ans;
ans.a=this->b:
        ans.b=-(this->a);
        ans.c = -(ans.a*p.x+ans.b*p.y);
        return ans;
    //dist formula is wrong but don't change
    double dist(pt p) const { return a * p.x + b * p.y + c; }
double sqr (double a) {
   return a * a;
```

```
double det(double a, double b, double c, double d) {
   return a*d - b*c:
bool intersect(line m, line n, pt & res) {
   double zn = det(m.a, m.b, n.a, n.b);
   if (abs(zn) < EPS)
        return false;
   res.x = -det(m.c, m.b, n.c, n.b) / zn;
   res.y = -det(m.a, m.c, n.a, n.c) / zn;
   return true;
bool parallel(line m, line n) {
   return abs(det(m.a, m.b, n.a, n.b)) < EPS;
bool equivalent(line m, line n) {
   return abs(det(m.a, m.b, n.a, n.b)) < EPS
        && abs(det(m.a, m.c, n.a, n.c)) < EPS
        && abs(det(m.b, m.c, n.b, n.c)) < EPS;
double det(double a. double b. double c. double d) {
   return a * d - b * c:
inline bool betw(double 1, double r, double x){
   return min(1, r) \le x + EPS && x \le max(1, r) + EPS;
inline bool intersect_1d(double a, double b, double c, double
   d) {
  if (a > b)
       swap(a, b);
    if (c > d)
       swap(c, d):
    return max(a, c) <= min(b, d) + EPS;</pre>
bool intersect_segment(pt a, pt b, pt c, pt d, pt& left, pt&
   if (!intersect_1d(a.x, b.x, c.x, d.x) ||
   !intersect_1d(a.y, b.y, c.y, d.y))
        return false;
    line m(a, b);
   line n(c, d);
   double zn = det(m.a, m.b, n.a, n.b);
    if (abs(zn) < EPS)
        if (abs(m.dist(c)) > EPS || abs(n.dist(a)) > EPS)
            return false;
        if (b < a)
           swap(a, b);
        if (d < c)
           swap(c, d);
        left = max(a, c)
       right = min(b, d);
       return true;
   } else {
       left.x = right.x = -det(m.c, m.b, n.c, n.b) / zn;
       left.y = right.y = -det(m.a, m.c, n.a, n.c) / zn;
        return betw(a.x, b.x, left.x) && betw(a.y, b.y, left.y)
              betw(c.x, d.x, left.x) && betw(c.y, d.y, left.y);
void tangents (pt c, double r1, double r2, vector<line> & ans)
    double r = r2 - r1:
   double z = sqr(c.x) + sqr(c.y);
   double d = z - sqr(r);
    if (d < -EPS) return;
   d = sqrt (abs (d));
   line I;
   1.a = (c.x * r + c.y * d) / z;
   1.b = (c.y * r - c.x * d) / z;
   1.c = r1;
   ans.push_back (1);
vector<line> tangents (circle a, circle b) {
    vector<line> ans;
    for (int i=-1; i<=1; i+=2)
       for (int j=-1; j<=1; j+=2)
    tangents (b-a, a.r*i, b.r*j, ans);</pre>
    for (size_t i=0; i<ans.size(); ++i)</pre>
       ans[i].c = ans[i].a * a.x + ans[i].b * a.y;
    return ans;
```

```
class pointLocationInPolygon{
   bool lexComp(const pt & 1, const pt & r){
    return 1.x < r.x || (1.x == r.x && 1.y < r.y);
   int sgn(ftype val){
       return val > 0 ? 1 : (val == 0 ? 0 : -1):
   vector<pt> seq;
   int n;
   pt tránslate:
   bool pointInTriangle(pt a, pt b, pt c, pt point){
  ftype s1 = abs(a.cross(b, c));
       ftype s2 = abs(point.cross(a, b)) + abs(point.cross(b,
            c)) + abs(point.cross(c, a));
       return s1 == s2:
public:
   pointLocationInPolygon(){
   pointLocationInPolygon(vector<pt> & points){
       prepare(points);
   void prepare(vector<pt> & points){
       seq.clear();
       n = points.size();
        int pos = 0:
       for(int i = 1; i < n; i++){
           if(lexComp(points[i], points[pos]))
               pos = i:
        translate.x=points[pos].x;
        translate.y=points[pos].y;
       rotate(points.begin(), points.begin() + pos,
            points.end());
       seq.resize(n);
        for(int i = 0; i < n; i++)
           seq[i] = points[i + 1] - points[0];
   bool pointInConvexPolygon(pt point){
       point.x-=translate.x;
        point.y-=translate.y;
        if(seq[0].cross(point) != 0 && sgn(seq[0].cross(point))
             != sgn(seq[0].cross(seq[n-1])))
       if(seq[n - 1].cross(point) != 0 && sgn(seq[n - 1].cross(point)) != sgn(seq[n - 1].cross(seq[0])))
           return false:
        if(seq[0].cross(point) == 0)
           return seq[0].sqrLen() >= point.sqrLen();
        int 1 = 0, r = n - 1:
        while(r - 1 > 1){
           int mid = (1 + r)/2;
           int pos = mid;
           if(seq[pos].cross(point) >= 0)1 = mid;
           else \hat{r} = mid:
        int pos = 1;
       return pointInTriangle(seq[pos], seq[pos + 1], pt(0,
             0), point);
     pointLocationInPolygon(){
       seq.clear();
class Minkowski{
   static void reorder_polygon(vector<pt> & P){
       size_t pos = 0;
       for(size_t i = 1; i < P.size(); i++){</pre>
           if(P[i].y < P[pos].y \mid | (P[i].y == P[pos].y &&
                P[i].x < \bar{P}[pos].x)
               pos = i;
       rotate(P.begin(), P.begin() + pos, P.end());
public:
   static vector<pt> minkowski(vector<pt> P, vector<pt> Q){
       // the first vertex must be the lowest
```

```
11
```

```
reorder_polygon(P);
        reorder_polygon(Q);
        // we must ensure cyclic indexing
        P.push_back(P[0]);
        P.push_back(P[1]);
        Q.push_back(Q[0]);
        Q.push_back(Q[1]);
        // main part
vector<pt> result;
        size_t i = 0, j = 0;
        while(i < P.size() - 2 || j < Q.size() - 2){
    result.push_back(P[i] + Q[j]);</pre>
            auto cross = (P[i + 1] - P[i]).cross(Q[j + 1] -
                 Q[j]);
            if(cross >= 0)
                ++i;
            if(cross <= 0)
                ++j;
       return result;
vector<pt> circle_line_intersections(circle cir,line 1){
   double r = cir.r, a = 1.a, b = 1.b, c = 1.c + 1.a*cir.x +
        1.b*cir.v:
    vector<pt> ans;
   double x_0 = -a*c/(a*a+b*b), y_0 = -b*c/(a*a+b*b);
   if (c*c > r*r*(a*a+b*b)+EPS):
    else if (abs (c*c - r*r*(a*a+b*b)) < EPS){
       \hat{p}.x=\hat{x}0:
       p.y=y0;
        ans.push_back(p);
   else{
        double d = r*r - c*c/(a*a+b*b);
        double mult = sqrt (d / (a*a+b*b));
double ax, ay, bx, by;
        ax = x0 + b * mult:
        bx = x0 - b * mult;
        \overline{ay} = y\overline{0} - \overline{a} * \overline{mult};
        by = y0 + a * mult;
        pt p; 
p.x = ax;
        ans.push_back(p);
       p.x = bx
       \hat{p}.y = by:
        ans.push_back(p);
   for(int i=0;i<ans.size();i++){</pre>
        ans[i] = ans[i] + cir:
double circle_polygon_intersection(circle c,vector<pt> &V){
   int n = V.size();
   double ans = 0;
   for(int i=0; i<n; i++){
   line l(V[i],V[(i+1)%n]);</pre>
        vector<pt> lpts = circle_line_intersections(c,1);
        int sz=lpts.size();
        for(int j=sz-1; j>=0; j--){
            if(!is_point_on_seg(V[i],V[(i+1)%n],lpts[j])){
                swap(lpts.back(),lpts[j]);
                lpts.pop_back();
            }
        lpts.push_back(V[i]);
        lpts.push_back(V[(i+1)%n]);
        sort(lpts.begin(),lpts.end());
        sz=lpts.size();
        if(V[(i+1)%n]<V[i])
            reverse(lpts.begin(),lpts.end());
        for(int j=1; j<sz; j++){</pre>
            if(insideCircle(c, lpts[j-1])
               &&insideCircle(c,lpts[j]))
                ans = ans + area(lpts[j-1],lpts[j],c);
            else{
                double ang = angle(lpts[j-1],c,lpts[j]);
```

```
double aa = c.r*c.r*ang/2;
                if(ccw(lpts[j-1],lpts[j],c))
                    ans = ans+aa;
                else
                    ans = ans-aa;
       }
    ans = abs(ans):
void convex_hull(vector<pt>& a, bool include_collinear =
    pt p0 = *min_element(a.begin(), a.end(), [](pt a, pt b) {
        return make_pair(a.y, a.x) < make_pair(b.y, b.x);
    sort(a.begin(), a.end(), [&p0](const pt& a, const pt& b) {
        int o = orientation(p0, a, b);
        if (o == 0)
            return (p0.x-a.x)*(p0.x-a.x) + (p0.y-a.y)*(p0.y-a.y)
               < (p0.x-b.x)*(p0.x-b.x) + (p0.y-b.y)*(p0.y-b.y);
        return o < 0;
    if (include_collinear) -
        int i = (int)a.size()-1;
        while (i >= 0 && collinear(p0, a[i], a.back())) i--;
        reverse(a.begin()+i+1, a.end());
    for (int i = 0; i < (int)a.size(); i++) {
   while (st.size() > 1 && !cw(st[st.size()-2], st.back(),
             a[i], include_collinear))
            st.pop_back();
        st.push_back(a[i]);
    \dot{a} = st;
    int m = a.size();
    for(int i = 0; i < m-1-i; i++){
        swap(a[i],a[m-1-i]);
double mindist;
pair<int, pair<int, int> > best_pair;
void upd_ans(const pt & a, const pt & b,const pt & c){
    double distC = sqrt((a.x - b.x)*(a.x - b.x) + (a.y - b.x)
        b.v)*(a.v - b.v));
    double distA = sqrt((c.x - b.x)*(c.x - b.x) + (c.y - b.x)
        b.y)*(c.y - b.y);
    double distB = sqrt((a.x - c.x)*(a.x - c.x) + (a.y - c.x)
         c.v)*(a.v - c.v));
    if (distA + distB + distC < mindist){
  mindist = distA + distB + distC;</pre>
        best_pair = make_pair(a.id,make_pair(b.id,c.id));
vector<pt> t;
//Min possible triplet distance
void rec(int 1, int r){
   if (r - 1 <= 3 &&r - 1 >= 2){
        for (int i = 1; i < r; ++i){
            for (int j = i + 1; j < r; ++j){
                for(int k=j+1;k<r;k++){</pre>
                    upd_ans(a[i],a[j],a[k]);
           }
        sort(a.begin() + 1, a.begin() + r, cmp_y());
    int m = (1 + r) >> 1:
    int midx = a[m-1].x;
    /*
     * Got WA in a team contest
     * for putting midx = a[m].x;
     * Don't know why. Maybe due to
     * floating point numbers.
    rec(1, m);
    rec(m, r);
```

```
3.8 intersecting-segments-pair
const double EPS = 1E-9;
struct pt {
   double x, y;
struct seg {
   pt p, q;
   double get_y(double x) const {
       if (abs(p.x - q.x) < EPS)
           return p.y;
        return p.y + (q.y - p.y) * (x - p.x) / (q.x - p.x);
bool intersect1d(double 11, double r1, double 12, double r2) {
   if (l1 > r1)
       swap(11, r1):
   if (12 > r2)
       swap(12, r2);
   return \max(11, 12) \leq \min(r1, r2) + EPS;
int vec(const pt& a, const pt& b, const pt& c) {
   double s = (b.x - a.x) * (c.y - a.y) - (b.y - a.y) * (c.x
        - a.x);
   return abs(s) < EPS ? 0 : s > 0 ? +1 : -1;
bool intersect(const seg& a, const seg& b){
   return intersect1d(a.p.x, a.q.x, b.p.x, b.q.x) &&
          intersect1d(a.p.y, a.q.y, b.p.y, b.q.y) && vec(a.p, a.q, b.p) * vec(a.p, a.q, b.q) <= 0 &&
          vec(b.p, b.q, a.p) * vec(b.p, b.q, a.q) <= 0;
bool operator<(const seg& a, const seg& b){
   double x = max(min(a.p.x, a.q.x), min(b.p.x, b.q.x));
   return a.get_y(x) < b.get_y(x) - EPS;
struct event {
   double x;
int tp, id;
event() {}
   event(double x, int tp, int id) : x(x), tp(tp), id(id) {}
   bool operator<(const event& e) const {</pre>
       if^*(abs(x - e.x) > EPS)
       return x < e.x;
return tp > e.tp;
vector < set < seg >:: iterator > where;
set<seg>::iterator prev(set<seg>::iterator it) {
   return it == s.begin() ? s.end() : --it;
set<seg>::iterator next(set<seg>::iterator it) {
pair<int, int> solve(const vector<seg>& a) {
   int n = (int)a.size();
   vector<event> e;
   for (int i = 0; i < n; ++i) {
       e.push_back(event(min(a[i].p.x, a[i].q.x), +1, i));
        e.push_back(event(max(a[i].p.x, a[i].q.x), -1, i));
```

```
sort(e.begin(), e.end());
s.clear();
where.resize(a.size());
for (size_t i = 0; i < e.size(); ++i) {</pre>
   int id = e[i].id;
   if (e[i].tp == +1) {
       set<seg>::iterator nxt = s.lower_bound(a[id]), prv
            = prev(nxt);
       if (nxt != s.end() && intersect(*nxt, a[id]))
           return make_pair(nxt->id, id);
       if (prv != s.end() && intersect(*prv, a[id]))
           return make_pair(prv->id, id);
       where[id] = s.insert(nxt, a[id]);
       set<seg>::iterator nxt = next(where[id]), prv =
            prev(where[id]);
       if (nxt != s.end() && prv != s.end() &&
            intersect(*nxt, *prv))
           return make_pair(prv->id, nxt->id);
       s.erase(where[id]):
return make_pair(-1, -1);
```

point-location

```
typedef long long ll;
bool ge(const ll& a, const ll& b) { return a >= b; }
bool le(const ll& a, const ll& b) { return a <= b; }
bool eq(const ll& a, const ll& b) { return a == b; }
bool gt(const ll& a, const ll& b) { return a > b; }
bool lt(const ll& a, const ll& b) { return a < b; }
int sgn(const ll& x) { return le(x, 0) ? eq(x, 0) ? 0 : -1 :
      Ĭ; }
struct pt {
    ll x, y;
pt() {}
    pt(ll _x, ll _y) : x(_x), y(_y) {}
    pt operator-(const pt& a) const { return pt(x - a.x, y -
    11 dot(const pt& a) const { return x * a.x + y * a.y; }
    11 dot(const pt& a, const pt& b) const { return (a -
          *this).dot(b - *this); }
    11 cross(const pt& a) const { return x * a.y - y * a.x; }
    ll cross(const pt& a, const pt& b) const { return (a -
          *this).cross(b - *this); }
    bool operator == (const pt& a) const { return a.x == x &&
struct Edge {
    pt 1, r;
bool edge_cmp(Edge* edge1, Edge* edge2){
    const pt a = edge1->1, b = edge1->r;
const pt c = edge2->1, d = edge2->r;
    int val = sgn(a.cross(b, c)) + sgn(a.cross(b, d));
    if (val != 0)
         return val > 0;
    val = sgn(c.cross(d, a)) + sgn(c.cross(d, b));
return val < 0:</pre>
enum EventType { DEL = 2, ADD = 3, GET = 1, VERT = 0 };
struct Event {
    EventType type;
    bool operator<(const Event& event) const { return type <</pre>
          event.type; }
vector<Edge*> sweepline(vector<Edge*> planar, vector<pt>
      queries){
    using pt_type = decltype(pt::x);
// collect all x-coordinates
         set<pt_type, std::function<bool(const pt_type&, const</pre>
              pt_type&)>>(lt);
    for (pt p : queries)
         s.insert(p.x);
```

```
for (Edge* e : planar) {
   s.insert(e->1.x):
   s.insert(e->r.x)
// map all x-coordinates to ids
int cid = 0:
auto id =
   map<pt_type, int, std::function<bool(const pt_type&,
        const pt_type&)>>(
       lt);
for (auto x : s)
   id[x] = cid++;
// create events
auto t = set<Edge*, decltype(*edge_cmp)>(edge_cmp);
auto vert_cmp = [](const pair<pt_type, int>& 1,
                 const pair<pt_type, int>& r) {
    if (!eq(l.first, r.first))
   return lt(1.first, r.first);
return l.second < r.second;</pre>
vector<vector<Event>> events(cid);
for (int i = 0; i < (int)queries.size(); i++) {</pre>
   int x = id[queries[i].x];
   events[x].push_back(Event(GET, i));
for (int i = 0; i < (int)planar.size(); i++) {</pre>
   int lx = id[planar[i]->l.x], rx = id[planar[i]->r.x];
    if (lx > rx)^{-}
       swap(lx, rx);
       swap(planar[i]->1, planar[i]->r);
   if (lx == rx) {
       events[lx].push back(Event{VERT, i}):
   } else {
       events[lx].push_back(Event{ADD, i});
       events[rx].push_back(Event{DEL, i});
// perform sweep line algorithm
vector<Edge*> ans(queries.size(), nullptr);
for (int x = 0; x < cid; x++) {
   sort(events[x].begin(), events[x].end());
    vert.clear();
   for (Event event : events[x]) {
       if (event.type == DEL) {
          t.erase(planar[event.pos]);
       if (event.type == VERT) {
           vert.insert(make_pair(
              min(planar[event.pos]->1.y,
                   planar[event.pos]->r.y),
              event.pos));
       if (event.type == ADD) {
          t.insert(planar[event.pos]);
       if (event.type == GET) {
           auto jt = vert.upper_bound(
              make_pair(queries[event.pos].y,
                   planar.size()));
           if (jt != vert.begin()) {
              --jt;
              int i = jt->second;
              ans[event.pos] = planar[i];
                  continue;
           Édge* e = new Edge:
           e->1 = e->r = queries[event.pos];
           auto it = t.upper_bound(e);
           if (it != t.begin())
              ans[event.pos] = *(--it);
           delete e:
```

```
for (Event event : events[x]) {
           if (event.type != GET)
           if (ans[event.pos] != nullptr &&
               eq(ans[event.pos]->1.x, ans[event.pos]->r.x))
           continue;
Edge* e = new Edge;
           e->1 = e->r = queries[event.pos];
           auto it = t.upper_bound(e);
           delete e;
           if (it == t.begin())
               e = nullptr;
           else
               e = *(--it);
           if (ans[event.pos] == nullptr) {
               ans[event.pos] = e;
               continue:
           if (e == nullptr)
               continue;
           if (e == ans[event.pos])
               continue;
           if (id[ans[event.pos]->r.x] == x) {
               if (id[e->1.x] == x) {
                   if (gt(e->1.y, ans[event.pos]->r.y))
                       ans[event.pos] = e;
           } else {
               ans[event.pos] = e;
       }
   return ans;
struct DCEL {
   struct Edge {
       pt origin;
       Edge* nxt = nullptr;
       Edge* twin = nullptr;
       int face;
   vector<Edge*> body;
vector<pair<int, int>> point_location(DCEL planar, vector<pt>
     queries){
   vector<pair<int, int>> ans(queries.size());
vector<Edge*> planar2;
   map<intptr_t, int> pos;
map<intptr_t, int> added_on;
   int n = planar.body.size();
   for (int i = 0; i < n; i++) {
       if (planar.body[i]->face > planar.body[i]->twin->face)
           continue;
       Edge* e = new Edge;
e->1 = planar.body[i]->origin;
       e->r = planar.body[i]->twin->origin;
       added_on[(intptr_t)e] = i;
       pos[(intptr_t)e] =
           lt(planar.body[i]->origin.x,
                planar.body[i]->twin->origin.x)
               ? planar.body[i]->face
               : planar.body[i]->twin->face;
       planar2.push_back(e);
   auto res = sweepline(planar2, queries);
   for (int i = 0; i < (int)queries.size(); i++) {</pre>
       if (res[i] == nullptr) {
           ans[i] = make_pair(1, -1);
           continue;
       pt p = queries[i];
       pt 1 = res[i]->1, r = res[i]->r;
       if (eq(p.cross(l, r), 0) && le(p.dot(l, r), 0)) {
           ans[i] = make_pair(0, added_on[(intptr_t)res[i]]);
       ans[i] = make pair(1, pos[(intptr t)res[i]]):
```

```
for (auto e : planar2)
    delete e;
return ans;
```

3.10 vertical-decomposition

```
typedef double dbl;
const dbl eps = 1e-9;
inline bool eq(dbl x, dbl y){
   return fabs(x - y) < eps;</pre>
inline bool lt(dbl x, dbl y){
    return x < y - eps;</pre>
inline bool gt(dbl x, dbl y){
   return x > y + eps;
inline bool le(dbl x, dbl y){
    return x < y + eps;</pre>
inline bool ge(dbl x, dbl y){
   return x > y - eps;
struct pt{
    dbl x, y;
    inline pt operator - (const pt & p)const{
        return pt\{x - p.x, y - p.y\};
    inline pt operator + (const pt & p)const{
        return pt\{x + p.x, y + p.y\};
    inline pt operator * (dbl a)const{
        return pt\{x * a, y * a\};
    inline dbl cross(const pt & p)const{
   return x * p.y - y * p.x;
    inline dbl dot(const pt & p)const{
   return x * p.x + y * p.y;
    inline bool operator == (const pt & p)const{
        return eq(x, p.x) && eq(y, \hat{p}.y);
struct Line{
    pt p[2];
    Line(){}
    Line(pt a, pt b):p{a, b}{}
    pt vec()const{
        return p[1] - p[0];
    pt& operator [](size_t i){
        return p[i];
inline bool lexComp(const pt & 1, const pt & r){
    if(fabs(1.x - r.x) > eps){
        return 1.x < r.x;</pre>
    else return 1.y < r.y;</pre>
vector<pt> interSegSeg(Line 11, Line 12){
    if(eq(11.vec().cross(12.vec()), 0)){
         if(!eq(11.vec().cross(12[0] - 11[0]), 0))
         return {};
if(!lexComp(l1[0], l1[1]))
         swap(11[0], 11[1]);
if(!lexComp(12[0], 12[1]))
             swap(12[0], 12[1]);
        pt l = lexComp(l1[0], 12[0]) ? 12[0] : 11[0];
pt r = lexComp(l1[1], 12[1]) ? 11[1] : 12[1];
if(l == r)
             return {1};
         else return lexComp(l, r) ? vector<pt>{l, r} :
              vector<pt>();
    else{
```

```
pt inter = 11[0] + 11.vec() * s
         if(ge(s, 0) && le(s, 1) && le((12[0] - inter).dot(12[1]
              - inter), 0))
            return {inter}:
        else
            return {};
inline char get_segtype(Line segment, pt other_point){
    if(eq(segment[0].x, segment[1].x))
         return 0;
    if(!lexComp(segment[0], segment[1]))
        swap(segment[0], segment[1]);
    return (segment[1] - segment[0]).cross(other_point -
         segment[0]) > 0 ? 1 : -1:
dbl union_area(vector<tuple<pt, pt, pt> > triangles){
   vector<Line> segments(3 * triangles.size());
    vector<char> segtype(segments.size());
    for(size t i = 0: i < triangles.size(): i++){</pre>
        pt a, b, c;
tie(a, b, c) = triangles[i];
         segments[3 * i] = lexComp(a, b) ? Line(a, b) : Line(b,
        segtype[3 * i] = get_segtype(segments[3 * i], c);
segments[3 * i + 1] = lexComp(b, c) ? Line(b, c) :
             Line(c, b);
         segtype[3 * i + 1] = get_segtype(segments[3 * i + 1],
         segments [3 * i + 2] = lexComp(c, a)? Line(c, a):
             Line(a, c);
         segtype[3 * i + 2] = get_segtype(segments[3 * i + 2].
    vector<dbl> k(segments.size()), b(segments.size());
    for(size_t i = 0; i < segments.size(); i++){</pre>
        if(segtype[i]){
   k[i] = (segments[i][1].y - segments[i][0].y) /
            (segments[i][1].x - segments[i][0].x);
b[i] = segments[i][0].y - k[i] * segments[i][0].x;
    dbl ans = 0:
    for(size_t i = 0; i < segments.size(); i++){</pre>
        if(!segtype[i])
        continue;
dbl l = segments[i][0].x, r = segments[i][1].x;
        vector<pair<dbl, int> > evts;
        for(size_t j = 0; j < segments.size(); j++){
    if(!segtype[j] || i == j)</pre>
            dbl l1 = segments[j][0].x, r1 = segments[j][1].x;
            if(ge(l1, r) || ge(l, r1))
             dbl common_1 = max(1, 11), common_r = min(r, r1);
            auto pts = interSegSeg(segments[i], segments[j]);
            if(pts.empty()){
                dbl yl1 = k[j] * common_l + b[j];
dbl yl = k[i] * common_l + b[i];
if(lt(yl1, yl) == (segtype[i] == 1)){
                     int evt_type = -segtype[i] * segtype[j];
                     evts.emplace_back(common_1, evt_type);
                     evts.emplace_back(common_r, -evt_type);
            else if(pts.size() == 1u){
    dbl yl = k[i] * common_l + b[i], yl1 = k[j] *
                      common_1 + b[j];
                int evt_type = -segtype[i] * segtype[j];
if(lt(yl1, yl) == (segtype[i] == 1)){
                     evts.emplace_back(common_1, evt_type);
                     evts.emplace_back(pts[0].x, -evt_type);
                 yl = k[i] * common_r + b[i], yl1 = k[j] *
```

common_r + b[i];

```
if(lt(yl1, yl) == (segtype[i] == 1)){
                    evts.emplace_back(pts[0].x, evt_type);
                    evts.emplace_back(common_r, -evt_type);
           else{
               if(segtype[j] != segtype[i] || j > i){
    evts.emplace_back(common_1, -2);
                    evts.emplace_back(common_r, 2);
        evts.emplace_back(1, 0);
        sort(evts.begin(), evts.end());
        size_t j = 0;
        int balance = 0;
        while(j < evts.size()){</pre>
           siže_t ptr = j;
           while(ptr < evts.size() && eq(evts[j].first,</pre>
                 evts[ptr].first)){
               balance += evts[ptr].second;
           if(!balance && !eq(evts[j].first, r)){
               dbl next_x = ptr == evts.size() ? r :
    evts[ptr].first;
                ans -= segtype[i] * (k[i] * (next_x +
                     evts[j].first) + 2 * b[i]) * (next_x -
                     evts[i].first):
           j = ptr:
   return ans/2:
pair<dbl,dbl> union_perimeter(vector<tuple<pt, pt, pt> >
     triangles){
    //Same as before
   pair<dbl,dbl> ans = make_pair(0,0);
   for(size t i = 0: i < segments.size(): i++){</pre>
        //Same as before
        double
             dist=(segments[i][1].x-segments[i][0].x)*(segments[i][1
        dist=sart(dist):
        while(j < evts.size()){</pre>
           size_t ptr = j;
           while(ptr < evts.size() && eq(evts[j].first;</pre>
                 evts[ptr].first)){
                balance += evts[ptr].second;
           if(!balance && !eq(evts[j].first, r)){
               dbl next_x = ptr == evts.size() ? r :
    evts[ptr].first;
                ans.first += dist * (next x - evts[i].first) /
                     (r-1):
                if(eq(segments[i][1].y,segments[i][0].y))
                     ans.second+=(next_x - evts[j].first);
              = ptr;
       }
   return ans;
```

4 Graph

4.1 DMST with solution

```
// not tested yet
const int INF = 1029384756;
#define MAXN 1000
#define FOR(i,x) for(auto i :x )
struct edge_t {
   int u,v,w;
   set< pair<int,int> > add, sub;
   edge_t() : u(-1), v(-1), w(0) {}
   edge_t(int _u, int _v, int _w) {
        u = _u;
        v = _v;
   }
```

```
add.insert({u, v}):
    edge_t& operator += (const edge_t& obj) {
        w += obj.w;
         for (auto it : obi.add) {
             if (!sub.count(it)) add.insert(it);
             else sub.erase(it):
         for (auto it : obj.sub) {
             if (!add.count(it)) sub.insert(it);
             else add.erase(it):
        return *this;
    edge_t& operator -= (const edge_t& obj) {
        \overline{w} -= obj.w;
         for (auto it : obj.sub) {
             if (!sub.count(it)) add.insert(it);
             else sub.erase(it);
         for (auto it : obj.add) {
             if (!add.count(it)) sub.insert(it);
             else add.erase(it):
        return *this:
} eg[MAXN*MAXN],prv[MAXN],EDGE_INF(-1,-1,INF);
int N,M;
int cid,incyc[MAXN],contracted[MAXN];
vector<int> E[MAXN];
edge_t dmst(int rt) {
    edge_t cost;
    for (int i=0; i<N; i++) {
    contracted[i] = incyc[i] = 0;</pre>
        prv[i] = EDGE_INF;
    cid = 0;
    int u,v;
while (true) {
        for (v=0; v<N; v++) {</pre>
             if (v != rt && !contracted[v] && prv[v].w == INF)
        if (v >= N) break; // end
for (int i=0; i<M; i++) {
    if (eg[i].v == v. && eg[i] .w < prv[v].w)</pre>
                 prv[v] = eg[i];
         if (prv[v].w == INF) // not connected
             return EDGE_INF;
         cost += prv[v];
         for (u=prv[v].u; u!=v && u!=-1; u=prv[u].u);
        if (u = -1) continue;
        incyc[v] = ++cid;
        for (u=prv[v].u; u!=v; u=prv[u].u) {
  contracted[u] = 1;
  incyc[u] = cid;
         for (int i=0; i<M; i++) {
    if (incyc[eg[i].u] != cid && incyc[eg[i].v] ==</pre>
                 eg[i] -= prv[eg[i].v];
             }
        for (int i=0; i<M; i++) {
    if (incyc[eg[i].u] == cid) eg[i].u = v;
    if (incyc[eg[i].v] == cid) eg[i].v = v;</pre>
             if (eg[i].u == eg[i].v) eg[i--] = eg[--M];
         for (int i=0; i<N; i++) {
             if (contracted[i]) continue;
             if (prv[i].u>=0 && incyc[prv[i].u] == cid)
                 prv[i].u = v;
        prv[v] = EDGE_INF;
    return cost;
```

```
#define F first
#define S second
void solve() {
   edge_t cost = dmst(0);
   for (auto it : cost.add) { // find a solution
        E[it.F].push_back(it.S);
        prv[it.S] = edge_t(it.F,it.S,0);
   }
}
```

4.2 DMST

```
// tested on https://lightoj.com/problem/teleport
const int inf = 1e9;
struct edge {
    int u, v, w;
edge() {}
    edge(int a,int b,int c) : u(a), v(b), w(c) {}
    bool operator < (const edge& o) const {
        if'(u == o.u)
            if (v == o.v)return w < o.w;</pre>
             else return v < o.v;
        return u < o.u;</pre>
int dmst(vector<edge> &edges, int root, int n) {
    int ans = 0:
    int cur_nodés = n;
    while (true) {
        vector<int> lo(cur_nodes, inf), pi(cur_nodes, inf);
        for (int i = 0; i < edges.size(); ++i) {</pre>
            int u = edges[i].u, v = edges[i].v, w = edges[i].w;
            if (w < lo[v] and u != v) {
                lo[v] = w;
pi[v] = u;
        lo[root] = 0;
        for (int i = 0; i < lo.size(); ++i) {</pre>
            if (i == root) continue;
            if (lo[i] == inf) return -1;
        vector<int> id(cur_nodes, -1), mark(cur_nodes, -1);
        for (int i = 0; i < cur_nodes; ++i) {
    ans += lo[i]:</pre>
            int u = i;
while (u != root and id[u] < 0 and mark[u] != i) {
    mark[u] = i;</pre>
                 u = pi[u]:
             if (u != root and id[u] < 0) { // Cycle}
                 for (int v = pi[u]; v != u; v = pi[v]) id[v] =
                      cur_id;
                 id[u] = cur_id++;
         if (cur_id == 0) break;
        for (int i = 0; i < cur_nodes; ++i)
    if (id[i] < 0) id[i] = cur_id++;
        for (int i = 0; i < edges.size(); ++i) {
   int u = edges[i].u, v = edges[i].v, w = edges[i].w;</pre>
            edges[i].u = id[u];
            edges[i].v = id[v];
            if (id[u] != id[v]) edges[i].w -= lo[v];
         cur_nodes = cur_id;
        root = id[root]:
    return ans;
```

4.3 articulation-vertex

```
int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph
vector<bool> visited;
vector<int> tin, low;
int timer;
void dfs(int v, int p = -1) {
```

```
visited[v] = true;
tin[v] = low[v] = timer++;
    int children=0;
    for (int to : adj[v]) {
         if (to == p) continue;
         if (visited[to]) {
             low[v] = min(low[v], tin[to]);
             dfs(to, v);
low[v] = min(low[v], low[to]);
if (low[to] >= tin[v] && p!=-1)
             IS_CUTPOINT(v);
++children;
   if(p == -1 && children > 1)
   IS_CUTPOINT(v);
void find_cutpoints() {
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
   for (int i = 0; i < n; ++i) {
   if (!visited[i])</pre>
             dfs (i);
```

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4.4 bellman-ford

```
struct Edge {
   int a, b, cost;
int n, m;
vector<Edge> edges;
const int INF = 1000000000:
void solve(){
    vector<int> d(n);
    vector<int> p(n, -1);
    int x:
    for (int i = 0; i < n; ++i) {
         x = -1;
         for (Edge e : edges) {
            if (d[e.a] + e.cost < d[e.b]) {
    d[e.b] = d[e.a] + e.cost;
    p[e.b] = e.a;
                  \bar{x} = e.b;
        }
   if (x == -1) {
   cout << "No negative cycle found.";</pre>
    } else {
        for (int i = 0; i < n; ++i)
         x = p[x];
vector<int> cycle;
         for (int v = x;; v = p[v]) {
    cycle.push_back(v);
             if (v == x && cycle.size() > 1)
                  break:
        reverse(cycle.begin(), cycle.end());
         cout << "Negative cycle: ":
         for (int v : cycle)
             cout << v << '';
         cout << endl:
   }
```

4.5 bridge

```
const int vmax = 2e5+10, emax = 2e5+10;
namespace Bridge {///edge, nodes, comps 1 indexed
  vector<int> adj[vmax]; /// edge-id
  pair<int, int> edges[emax]; /// (u, v)
  bool isBridge[emax];
  int visited[vmax]; ///0-unvis,1-vising,2-vis
  int st[vmax], low[vmax], clk = 0, edgeId = 0;
  /// For bridge tree components
```

```
int who[vmax], compId = 0;
vector<int> stk;
/// For extra end time calc
int en[vmax];
void dfs(int u, int parEdge) {
 visited[u] = 1: low[u] = st[u] = ++clk:
 stk.push_back(u);
 for (auto e : adj[u]) {
  if (e == parEdge) continue;
   int v=edges[e].first^edges[e].second^u;
if (visited[v] == 1) {
   low[u] = min(low[u], st[v]);
} else if(visited[v] == 0){
      dfs(v, e); low[u] = min(low[u], low[v]);
 visited[u] = 2;
 if(st[u] == low[u]){/// found
    ++compId; int cur;
      cur = stk.back(); stk.pop_back();
     who[cur] = compId;
    }while(cur != u):
    if(parEdge != -1){isBridge[parEdge] = true;}
 en[u] = clk;
void clearAll(int n){
 for(int i = 0; i<=n; i++) {
   adj[i].clear(); visited[i] = st[i] = 0; }
 for(int i = 0; i<=edgeId; i++) isBridge[i]=0;
clk = compId = edgeId = 0;</pre>
void findBridges(int n){
 for(int i = 1; i<=n; i++){
  if(visited[i] == 0) dfs(i, -1); }</pre>
bool isReplacable(int eid, int u, int v){
 if(!isBridge[eid]) return true;
 int a=edges[eid].first,b=edges[eid].second;
 if(st[a] > st[b]) swap(a, b);
return (st[b] <= st[u] && st[u] <= en[b])
 != (st[b] <= st[v] && st[v] <= en[b]);
void addEdge(int u, int v){
 edgeId++; edges[edgeId] = {u, v};
 adj[u].emplace_back(edgeId);
 adj[v].emplace_back(edgeId);
```

4.6 edmond-blossom

```
/***Copied from https://codeforces.com/blog/entry/49402***/
/*
GETS:
V->number of vertices
E->number of edges
pair of vertices as edges (vertices are 1..V)
GIVES:
output of edmonds() is the maximum matching
match[i] is matched pair of i (-1 if there isn't a matched
pair)
*/
const int M=500;
struct struct_edge
{
   int v;
   struct_edge* n;
};
typedef struct_edge* edge;
struct_edge pool[M*M*2];
edge top=pool.adj[M];
int V,E,match[M],qh,qt,q[M],father[M],base[M];
bool inq[M],inb[M],ed[M][M];
void add_edge(int u,int v)
{
   top->v=v,top->n=adj[u],adj[u]=top++;
   top->v=u,top->n=adj[v],adj[v]=top++;
```

```
int LCA(int root.int u.int v)
   static bool inp[M];
   memset(inp,0,sizeof(inp));
    while(1)
        inp[u=base[u]]=true;
        if (u==root) break;
        u=father[match[u]];
    while(1)
        if (inp[v=base[v]]) return v;
        else v=father[match[v]];
void mark blossom(int lca.int u)
    while (base[u]!=lca)
        int v=match[u];
inb[base[u]]=inb[base[v]]=true;
        u=father[v]:
        if (base[u]!=lca) father[u]=v;
void blossom contraction(int s.int u.int v)
    int lca=LCA(s,u,v);
   memset(inb,0,sizeof(inb));
    mark_blossom(lca,u);
   mark_blossom(lca,v);
if (base[u]!=lca)
        father[u]=v:
    if (base[v]!=lca)
   father[v]=u;
for (int u=0; u<V; u++)
        if (inb[base[u]])
            base[u]=lca:
            if (!inq[u])
                inq[q[++qt]=u]=true;
int find_augmenting_path(int s)
   memset(inq,0,sizeof(inq));
   memset(father,-1,sizeof(father));
for (int i=0; i<V; i++) base[i]=i;
inq[q[qh=qt=0]=s]=true;</pre>
    while (qh<=qt)
        int u=q[qh++];
        for (edge e=adj[u]; e; e=e->n)
            if (base[u]!=base[v]&&match[u]!=v)
    if ((v==s)||(match[v]!=-1 &&
                      father[match[v]]!=-1))
                     blossom_contraction(s,u,v);
                 else if (father[v]==-1)
                     father[v]=u;
if (match[v]==-1)
                     else if (!inq[match[v]])
                         inq[q[++qt]=match[v]]=true;
       }
    return -1;
int augment_path(int s,int t)
    int u=t,v,w;
    while (u!=-1)
        v=father[u];
```

```
w=match[v];
    match[v]=u;
    match[u]=v;
    "match[u]=v;
}
return t!=-1;
int edmonds()//Gives number of matchings
{
    int matchc=0;
    memset(match,-1,sizeof(match));
    for (int u=0; u<V; u++)
        if (match[u]==-1)
            matchc+=augment_path(u,find_augmenting_path(u));
    return matchc;
}
//To add edge add_edge(u-1,v-1);
    ed[u-1][v-1]=ed[v-1][u-1]=true;</pre>
```

4.7 euler-path

```
int main() {
   int n:
   vector<vector<int>> g(n, vector<int>(n));
   // reading the graph in the adjacency matrix
   vector<int> deg(n);
   for (int i = 0; i < n; ++i) {
    for (int j = 0; j < n; ++j)
        deg[i] += g[i][j];
   int first = 0;
   while (first < n && !deg[first])</pre>
        ++first;
   if (first == n) {
        cout << -1;
        return 0:
    int v1 = -1, v2 = -1;
   bool bad = false;
for (int i = 0: i < n: ++i) {</pre>
        if (deg[i] & 1) {
            if (v1 == -1)
            v1 = i;
else if (v2 == -1)
                 v2 = i:
            else
                 bad = true;
   if (v1 != -1)
   ++g[v1][v2], ++g[v2][v1];
stack<int> st:
   st.push(first);
   vector<int> res:
   while (!st.empty()) {
        int v = st.top();
        for (i = 0; i < n; ++i)
            if (g[v][i])
        if (i == n) {
            res.push_back(v);
            st.pop();
        } else {
            --g[v][i]:
            --g[i][v];
            st.push(i);
   if (v1 != -1) {
        for (size_t i = 0; i + 1 < res.size(); ++i) {</pre>
            if ((res[i] == v1 && res[i + 1] == v2) ||
(res[i] == v2 && res[i + 1] == v1)) {
                 vector<int> res2;
for (size_t j = i + 1; j < res.size(); ++j)</pre>
                     res2.push_back(res[j]);
                 for (size_t j = 1; j <= i; ++j)</pre>
                     res2.push_back(res[j]);
                 res = res^{1}2;
                 break:
```

```
}
}
for (int i = 0; i < n; ++i) {
    for (int j = 0; j < n; ++j) {
        if (g[i][j])
            bad = true;
    }
}
if (bad) {
    cout << -1;
} else {
    for (int x : res)
        cout << x << " ";
}
}</pre>
```

```
4.8
      hopcraft-karp
/** Source: https://iq.opengenus.org/hopcroft-karp-algorithm/
  A class to represent Bipartite graph for
// Hopcroft Karp implementation
class BGraph{
   // m and n are number of vertices on left
    // and right sides of Bipartite Graph
   // adj[u] stores adjacents of left side
   // vertex 'u'. The value of u ranges from 1 to m.
   // 0 is used for dummy vertex
   std::list<int> *adj;
   // pointers for hopcroftKarp()
    int *pair_u, *pair_v, *dist;
public:
   BGraph(int m, int n); // Constructor
   void addEdge(int u, int v); // To add edge
   // Returns true if there is an augmenting path
   // Adds augmenting path if there is one beginning
   // with u
   bool dfs(int u);
   // Returns size of maximum matching
   int hopcroftKarpAlgorithm();
// Returns size of maximum matching
int BGraph::hopcroftKarpAlgorithm(){
   // pair_u[u] stores pair of u in matching on left side of
Bipartite Graph.
   // If u doesn't have any pair, then pair_u[u] is NIL
   pair_u = new int[m + 1];
   // pair_v[v] stores pair of v in matching on right side of
        Biparite Graph.
    // If v doesn't have any pair, then pair_u[v] is NIL
   pair_v = new int[n + 1];
// dist[u] stores distance of left side vertices
   dist = new int[m + 1];
   // Initialize NIL as pair of all vertices
   for (int u = 0; u <= m; u++)
   pair_u[u] = NIL;

for (int v = 0; v <= n; v++)

pair_v[v] = NIL;
    // Initialize result
   int result = 0;
   // Keep updating the result while there is an
   // augmenting path possible.
   while (bfs()){
       // Find a free vertex to check for a matching
       for (int u = 1; u <= m; u++)
           // If current vertex is free and there is
           // an augmenting path from current vertex
           // then increment the result
           if (pair_u[u] == NIL && dfs(u))
               result++;
   return result:
// Returns true if there is an augmenting path available, else returns false
bool BGraph::bfs(){
   std::queue<int> q; //an integer queue for bfs
```

```
// First layer of vertices (set distance as 0)
   for (int u = 1; u \le m; u++){
        // If this is a free vertex, add it to queue
       if (pair_u[u] == NIL){
           // u is not matched so distance is 0
           dist[u] = 0;
           q.push(u):
        // Else set distance as infinite so that this vertex is
            considered next time for availability
           dist[u] = INF:
   // Initialize distance to NIL as infinite
   dist[NIL] = INF;
   // q is going to contain vertices of left side only.
   while (!q.empty()){
        // dequeue a vertex
        int u = q.front();
       q.pop();
// If this node is not NIL and can provide a shorter
    path to NIL then
        if (dist[u] < dist[NIL]){</pre>
           // Get all the adjacent vertices of the dequeued
           vertex u
std::list<int>::iterator it;
           for (it = adj[u].begin(); it != adj[u].end(); ++it){
               // If pair of v is not considered so far
               // i.e. (v, pair_v[v]) is not yet explored edge.
if (dist[pair_v[v]] == INF){
                   // Consider the pair and push it to queue
                   dist[pair_v[v]] = dist[u] + 1;
                   q.push(pair_v[v]);
       }
    // If we could come back to NIL using alternating path of
        distinct
   // vertices then there is an augmenting path available
   return (dist[NIL] != INF);
  Returns true if there is an augmenting path beginning with
free vertex u
bool BGraph::dfs(int u){
   if (u != NIL){
   std::list<int>::iterator it:
        for (it = adj[u].begin(); it != adj[u].end(); ++it){
           // Adjacent vertex of u
           int v = *it;
           // Follow the distances set by BFS search
           if (dist[pair_v[v]] == dist[u] + 1){
               // If dfs for pair of v also returnn true then
               if (dfs(pair_v[v]) == true){ // new matching
                    possible, store the matching
                   pair_v[v] = u;
                   pair_u[u] = v;
                   return true:
           }
        // If there is no augmenting path beginning with u then.
       dist[u] = INF;
       return false:
   return true:
   Constructor for initialization
BGraph::BGraph(int m, int n){
   this->n = n:
   adj = new std::list<int>[m + 1];
// function to add edge from u to v
void BGraph::addEdge(int u, int v){
   adi[u].push back(v): // Add v to us list.
```

4.9 hungerian-algorithm

```
class HungarianAlgorithm{
   int N,inf,n,max_match;
    int *1x,*1y,*xy,*yx,*slack,*slackx,*prev;
   int **cost;
bool *S,*T;
   void init_labels(){
        for(int x=0; x<n; x++) lx[x]=0;
        for(int y=0; y<n; y++) ly[y]=0;
        for (int x = 0: x < n: x++)
            for (int y = 0; y < n; y++)
                lx[x] = max(lx[x], cost[x][y]);
   void update_labels(){
        int x, y, delta = inf; //init delta as infinity
        for (y = 0; y < n; y++) //calculate delta using slack
            if (!T[y])
        delta = min(delta, slack[y]);
for (x = 0; x < n; x++) //update X labels</pre>
            if (S[x]) lx[x] = delta;
        for (y = 0; y < n; y++) //update Y labels
   if (T[y]) ly[y] += delta;</pre>
        for (y = 0; y < n; y++) //update slack array if (!T[y])
                 slack[v] -= delta;
   void add_to_tree(int x, int prevx)
//x - current vertex, prevx - vertex from X before x in the
     alternating path,
//so we add edges (prevx, xy[x]), (xy[x], x){
        S[x] = true; //add x to S
        prev[x] = prevx; //we need this when augmenting
        for (int y = 0; y < n; y++) //update slacks, because we add new vertex to S
            if (lx[x] + ly[y] - cost[x][y] < slack[y]){</pre>
                slack[y] = lx[x] + ly[y] - cost[x][y];
                slackx[y] = x;
   void augment() //main function of the algorithm{
        if (max_match == n) return; //check wether matching is
             already perfect
        int x, y, root; //just counters and root vertex
int q[N], wr = 0, rd = 0; //q - queue for bfs, wr,rd -
              write and read
//pos in queue
        //memset(S, false, sizeof(S)); //init set S
        for(int i=0;i<n;i++) S[i]=false;
//memset(T, false, sizeof(T)); //init set T</pre>
        for(int i=0;i<n;i++) T[i]=false;</pre>
        //memset(prev, -1, sizeof(prev)); //init set prev - for
              the alternating tree
        for(int i=0;i<n;i++) prev[i]=-1;</pre>
        for (x = 0; x < n; x++) //finding root of the tree{
            if (xy[x] == -1){
                q[wr++] = root = x;
                prev[x] = -2;
                S[x] = true;
                break:
       for (y = 0; y < n; y++) //initializing slack array{
    slack[y] = lx[root] + ly[y] - cost[root][y];
    slackx[y] = root;</pre>
        while (true) //main cycle{
            while (rd < wr) //building tree with bfs cycle{</pre>
                x = q[rd++]; //current vertex from X part
                 for (y = 0; y < n; y++) //iterate through all</pre>
                     edges in equality graph{
if (cost[x][y] == lx[x] + ly[y] && !T[y]){
                         if (yx[y] == -1) break; //an exposed
    vertex in Y found, so
//augmenting path exists!
                         T[y] = true; //else just add y to T,
                         q[wr++] = yx[y]; //add vertex yx[y],
                               which is matched
```

```
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```

```
//with y, to the queue
                                                    add_to_tree(yx[y], x); //add edges (x,y)
                                                                and (y,yx[y]) to the tree
                                   if (y < n) break; //augmenting path found!
                         if (y < n) break; //augmenting path found!
update_labels(); //augmenting path not found, so</pre>
                                     improve labeling
                          wr = rd = 0;
                         for (y = 0; y < n; y++){

//in this cycle we add edges that were added to
                                              the equality graph as a
//result of improving the labeling, we add edge (slackx[y], y)
           to the tree if
 //and only if !T[y] \&\& slack[y] == 0, also with this edge we
           add another one
//(y, yx[y]) or augment the matching, if y was exposed
if (!T[y] && slack[y] == 0){
                                           if (yx[y] == -1) //exposed vertex in Y found
                                                       - augmenting path exists!{
                                                    x = slackx[v];
                                                    break;
                                                    T[y] = true; //else just add y to T,
                                                    if (!S[yx[y]]){
                                                             q[wr++] = yx[y]; //add vertex yx[y],
                                                                         which is matched with
//v, to the queue
                                                             add_to_tree(yx[y], slackx[y]); //and
                                                                         add edges (x,y) and (y,
//vx[v]) to the tree
                                  }
                          if (y < n) break; //augmenting path found!</pre>
                 if (y < n) //we found augmenting path!{</pre>
                          max_match++; //increment matching
//in this cycle we inverse edges along augmenting path
                         for (int cx = x, cy = y, ty; cx != -2; cx = prev[cx], cy = ty){
                                   ty = xy[cx];
                                  yx[cy] = cx;
                                   xy[cx] = cv;
                          augment(); //recall function, go to step 1 of the
                                     algorithm
         }//end of augment() function
        HungarianAlgorithm(int vv,int inf=1000000000){
                 N=vv;
                 n=N;
                 max_match=0;
this->inf=inf;
               this > III - III;
| x = new int[N]; | x = n
                  slackx=new int[N];//slackx[y] such a vertex, that
                             l(slackx[y]) + l(y) - \dot{w}(slackx[y], y) = slack[y]
                  prev=new int[N];//array for memorizing alternating paths
                 S=new bool[N];
T=new bool[N];//sets S and T in algorithm
                  cost=new int*[N];//cost matrix
                  for(int i=0; i<N; i++){</pre>
                         cost[i]=new int[N]:
         HungarianAlgorithm(){
  delete []lx;
  delete []ly;
  delete []xy;
```

```
delete []yx;
    delete []slack;
delete []slackx;
delete []prev;
    delete []$;
    delete []T;
    int i;
    for(i=0; i<N; i++){</pre>
        delete [](cost[i]);
    delete []cost:
void setCost(int i,int j,int c){
    cost[i][j]=c;
int* matching(bool first=true){
    int *ans;
    ans=new int[N];
    for(int i=0;i<N;i++){</pre>
        if(first) ans[i]=xy[i];
        else ans[i]=yx[i];
    return ans;
int hungarian(){
    int ret = 0; //weight of the optimal matching
    max_match = 0; //number of vertices in current matching
    for(int x=0;x<n;x++) xy[x]=-1;</pre>
    for(int y=0;y<n;y++) yx[y]=-1;
init_labels(); //step 0</pre>
    augment(); //steps 1-3
    for (int x = 0; x < n; x++) //forming answer there
        ret += cost[x][xy[x]];
    return ret;
```

max-flow-dinic

```
#include<bits/stdc++.h>
#include<vector>
using namespace std:
#define MAX 100
#define HUGE_FLOW 1000000000
#define BEGIN 1
#define DEFAULT LEVEL 0
struct FlowEdge {
   int v, u;
long long cap, flow = 0;
   struct Dinic {
    const long long flow_inf = 1e18;
    vector<FlowEdge> edges:
    vector<vector<int>> adi:
    int n, m = 0;
   int s, t;
vector<int> level, ptr;
   queue<int> q;
Dinic(int n, int s, int t) : n(n), s(s), t(t) {
       adj.resize(n);
       level.resize(n);
       ptr.resize(n);
   void add_edge(int v, int u, long long cap) {
       edges.emplace_back(v, u, cap);
       edges.emplace_back(u, v, 0);
       adj[v].push_back(m);
       adj[u].push_back(m + 1);
       m += 2;
    bool bfs() {
       while (!q.empty()) {
           int v = q.front();
           q.pop();
           for (int id : adj[v]) {
               if (edges[id].cap - edges[id].flow < 1)</pre>
                   continue:
               if (level[edges[id].u] != -1)
```

```
continue;
level[edges[id].u] = level[v] + 1:
              q.push(edges[id].u);
       return level[t] != -1;
   long long dfs(int v, long long pushed) {
       if (pushed == 0)
          return 0:
       if (v == t)
          return pushed;
       for (int& cid = ptr[v]; cid < (int)adj[v].size();</pre>
            cid++) {
          int id = adj[v][cid];
          int u = edges[id].u;
          if (level[v] + 1 != level[u] || edges[id].cap -
                edges[id].flow < 1)
          long long tr = dfs(u, min(pushed, edges[id].cap -
               edges[id].flow));
           if (tr == 0)
              continue
          edges[id].flow += tr;
          edges[id ^ 1].flow -= tr;
          return tr:
       return 0;
   long long flow() {
   long long f = 0;
       while (true) {
          fill(level.begin(), level.end(), -1);
          level[s] = 0;
          q.push(s);
          if (!bfs())
          fill(ptr.begin(), ptr.end(), 0);
          while (long long pushed = dfs(s, flow_inf)) {
              f += pushed;
       return f;
int main(){
   return 0;
```

4.11 min-cost-max-flow

```
struct Edge{
   int from, to, capacity, cost;
vector<vector<int>> adj, cost, capacity;
const int INF = 1e9;
void shortest_paths(int n, int v0, vector<int>& d,
    vector<int>& p) {
   d.assign(n, INF);
   vector<bool> inq(n, false);
   queue<int> q;
   q.push(v0);
   p.assign(n, -1);
   while (!q.empty()) {
       int u = q.front();
       q.pop();
       inq[u] = false;
       for (int v : adj[u]) {
          if (capacity[u][v] > 0 && d[v] > d[u] + cost[u][v])
              d[v] = d[u] + cost[u][v];
              p[v] = u;
              if (!inq[v]) {
                  inq[v] = true;
                  q.push(v);
```

```
int min_cost_flow(int N, vector<Edge> edges, int K, int s, int
     t) {
    adj.assign(N, vector<int>());
   cost.assign(N, vector<int>(N, 0));
capacity.assign(N, vector<int>(N, 0));
   for (Edge e : edges) {
   adj[e.from].push_back(e.to);
         adj[e.to].push_back(e.from);
        cost[e.from][e.to] = e.cost;
cost[e.to][e.from] = -e.cost;
         capacity[e.from][e.to] = e.capacity;
    int flow = 0:
    int cost = 0:
    vector<int> d, p;
   while (flow < K) {
    shortest_paths(N, s, d, p);
    if (d[t] == INF)</pre>
         // find max flow on that path
         int f = K - flow;
         int cur = t;
         while (cur != s) {
            f = min(f, capacity[p[cur]][cur]);
             cur = p[curl:
        // apply flow
flow += f;
         cost += f * d[t]:
         cur = t:
         while (cur != s)
             capacity[p[cur]][cur] -= f;
             capacity[cur][p[cur]] += f;
             cur = p[cur];
    if (flow < K)
        return -1:
    else
        return cost;
```

4.12 online-bridge

```
vector<int> par. dsu 2ecc. dsu cc. dsu cc size:
int bridges;
int lca_iteration;
vector<int> last_visit;
void init(int n) {
   par.resize(n);
   dsu_2ecc.resize(n);
   dsu cc.resize(n):
    dsu_cc_size.resize(n);
    lca_iteration = 0;
    last_visit.assign(n, 0);
   for (int i=0; i<n; ++i) {
    dsu_2ecc[i] = i;
        dsu_cc[i] = i;
       dsu_cc_size[i] = 1;
par[i] = -1;
   bridges = 0:
int find_2ecc(int v) {
   if (v == -1)
    return dsu_2ecc[v] == v ? v : dsu_2ecc[v] =
        find 2ecc(dsu 2ecc[v]):
int find_cc(int v) {
   v = find_2ecc(v);
   return dsu_cc[v] == v ? v : dsu_cc[v] = find_cc(dsu_cc[v]);
void make root(int v) {
   v = find_2ecc(v);
   int root = v;
int child = -1;
   while (v != -1)
       int p = find_2ecc(par[v]);
```

```
par[v] = child;
       dsu_cc[v] = root;
child = v;
v = p;
   dsu_cc_size[root] = dsu_cc_size[child];
void merge_path (int a, int b) {
   ++lca_iteration;
vector<int> path_a, path_b;
   int lca = -1;
   while (lca = -1) {
       if (a != -1) {
           a = find 2ecc(a):
           path_a.push_back(a);
           if (last_visit[a] == lca_iteration){
               lca = a;
               break:
           last_visit[a] = lca_iteration;
           a = par[a];
        if (b != -1) {
           b = find_2ecc(b);
           path_b.push_back(b);
           if (last_visit[b] == lca_iteration){
               break;
           last_visit[b] = lca_iteration;
           b = par[b]:
   for (int v : path_a) {
       dsu_2ecc[v] = lca;
       if (v == lca)
           break:
        --bridges;
   for (int v : path_b) {
        dsu_2ecc[v] = 1ca;
       if (v == 1ca)
           break:
        --bridges:
void add_edge(int a, int b) {
   a = find_2ecc(a);
   b = find_2ecc(b);
   if (a == b) return;
    int ca = find_cc(a);
   int cb = find_cc(b);
   if (ca != cb) {
        ++bridges;
       if (dsu_cc_size[ca] > dsu_cc_size[cb]) {
           swap(a, b);
           swap(ca, cb);
       make_root(a);
       par[a] = dsu_cc[a] = b;
       dsu_cc_size[cb] += dsu_cc_size[a];
       merge_path(a, b);
4.13 scc + 2 Sat
namespace SCC { //Everything 0-indexed.
const int N = 2e6+7; int which[N], vis[N], cc;
vector<int> adj[N], adjr[N]; vector<int> order;
void addEdge(int u, int v) {
 adj[u].push_back(v); adjr[v].push_back(u);
 if (vis[u]) return; vis[u] = true;
 for(int v: adj[u]) dfs1(v); order.push_back(u);
void dfs2(int u, int id) {
```

```
if(vis[u]) return; vis[u] = true;
for(int v: adjr[u]) dfs2(v, id); which[u] = id;
int last = 0:
void findSCC(int n) {
cc=0,last=n; order.clear(); fill(vis, vis+n, 0);
for(int i=0; i<n; i++) if(!vis[i]) dfs1(i);
reverse(order.begin(), order.end());</pre>
 fill(vis, vis+n, 0);
for (int u: order) {
   if (vis[u]) continue; dfs2(u, cc); ++cc;
void clear() {
for (int i=0; i<last; i++)
adj[i].clear(), adjr[i].clear();</pre>
struct TwoSat {
int n; int vars = 0; vector<bool> ans;
TwoSat(int n) : n(n), ans(n) {
   SCC::clear(); vars = 2*n;
 void implies(int x, int y) {
   SCC::addEdge(x, y); SCC::addEdge(y^1, x^1);
 void OR(int x, int y) {
   SCC::addEdge(x^1, y); SCC::addEdge(y^1, x);
 void XOR(int x, int y) {
   implies(x, y^1); implies(x^1, y);
 void atmostOne(vector<int> v) {
   int k = v.size();
   for (int i=0; i<k; i++) {
  if (i+1<k) implies(vars+2*i, vars+2*i+2);
  implies(v[i], vars+2*i);</pre>
      if (i>0) implies(v[i], vars+2*i-1);
   vars += 2*k;
 bool solve() {
   SCC::findSCC(vars); ans.resize(vars/2);
   for (int i=0; i<vars; i+=2) {</pre>
      if (SCC::which[i]==SCC::which[i+1])return 0;
      if (i<2*n)</pre>
        ans[i/2] = SCC::which[i]>SCC::which[i+1];
   return true;
```

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15 Math

5.1 combination-generator

```
bool next combination(vector<int>& a, int n) {
    int k = (int)a.size();
    for (int i = k - 1; i >= 0; i--) {
   if (a[i] < n - k + i + 1) {
             a[i]++:
             for (int j = i + 1; j < k; j++)
    a[j] = a[j - 1] + 1;
return true;
        }
    return false;
vector<int> ans:
void gen(int n, int k, int idx, bool rev) {
  if (k > n || k < 0)</pre>
    if (!n) {
         for (int i = 0; i < idx; ++i) {
             if (ans[i])
                  cout << i + 1;
         cout << "\n";
         return;
    ans[idx] = rev:
    gen(n-1, k-rev, idx + 1, false);
```

```
ans[idx] = !rev;
gen(n - 1, k - !rev, idx + 1, true);
}
void all_combinations(int n, int k) {
    ans.resize(n);
    gen(n, k, 0, false);
}
5.2 continued-fractions
```

```
auto fraction(int p, int q) {
    vector<int> a;
    while(q) {
        a.push_back(p / q);
        tie(p, q) = make_pair(q, p % q);
    }
    return a;
}
auto convergents(vector<int> a) {
    vector<int> p = {0, 1};
    vector<int> q = {1, 0};
    for(auto it: a) {
        p.push_back(p[p.size() - 1] * it + p[p.size() - 2]);
        q.push_back(q[q.size() - 1] * it + q[q.size() - 2]);
    }
    return make_pair(p, q);
}
```

5.3 crt anachor

```
/// Chinese remainder theorem (special case): find z st z%m1 = r1, z%m2 = r2.

/// z is unique modulo M = lcm(m1, m2). Returns (z, M). On failure, M = -1.

PLL CRT(LL m1, LL r1, LL m2, LL r2) {
    LL s, t;
    LL g = egcd(m1, m2, s, t);
    if (r1%g != r2%g) return PLL(0, -1);
    LL M = m1*m2;
    LL ss = ((s*r2)\%m2)*m1;
    LL tt = ((t*r1)\%m1)*m2;
    LL ans = ((ss+tt)\%M+M)\%M;
    return PLL(ans/g, M/g);
}

// expected: 23 105

// 11 12

PLL ans = CRT({3,5,7}, {2,3,2});
cout << ans.first << " " << ans.second << endl;
ans = CRT({4,6}, {3,5});
cout << ans.first << " " << ans.second << endl;
cout << ans.first << " " << ans.second << endl;
```

5.4 discrete-root

```
#define MAX 100000
int prime[MAX+1],Phi[MAX+1];
vector<int> pr;
void sieve(){
    for (int i=2: i <= N: ++i) {
        if (prime[i] == 0) {
            prime[i] = i;
            pr.push_back(i);
        for (int j=0; j < (int)pr.size() && pr[j] <= prime[i]</pre>
             && i*pr[j] <= N; ++j) {
            prime[i * pr[j]] = pr[j];
   }
void PhiWithSieve(){
    int i;
   for(i=2; i<=MAX; i++){
    if(prime[i]==i){</pre>
            Phi[i]=i-1:
        else if((i/prime[i])%prime[i]==0){
            Phi[i]=Phi[i/prime[i]]*prime[i];
        else{
            Phi[i]=Phi[i/prime[i]]*(prime[i]-1);
```

```
int powmod (int a, int b, int p) {
   int res = 1:
   while (b)
       if (b & 1)
           res = int (res * 111 * a % p), --b;
           a = int (a * 111 * a % p), b >>= 1;
   return res;
int PrimitiveRoot(int p){
   vector<int>fact;
   int phi=Phi[p];
   int n=phi;
   while (n>1) {
       if(prime[n]==n){
           fact.push_back(n);
           n=1:
       else{
           int f=prime[n];
while(n%f==0){
              n=n/f;
           fact.push_back(f);
   int res;
   for(res=p-1; res>1; --res){
    for(n=0; n<fact.size(); n++){</pre>
           if(powmod(res,phi/fact[n],p)==1){
               break;
       if(n>=fact.size()) return res;
   return -1;
int DiscreteLog(int a, int b, int m) {
   a %= m, b %= m:
   int n = sqrt(m) + 1
   map<int, int> vals;
   for (int p = 1; p <= n; ++p)
       vals[powmod(a,(int) (111* p * n) %m , m)] = p;
   for (int q = 0; q <= n; ++q) {
       int cur = (powmod(a, q, m) * 111 * b) % m;
       if (vals.count(cur))
           int ans = vals[cur] * n - q:
           return ans:
   return -1;
vector<int> DiscreteRoot(int n.int a.int k){
   int g = PrimitiveRoot(n);
   vector<int> ans:
   int any_ans = DiscreteLog(powmod(g,k,n),a,n);
   if (anv ans == -1)
       return ans:
   int delta = (n-1) / gcd(k, n-1);
   for (int cur = any_ans % delta; cur < n-1; cur += delta)</pre>
       ans.push_back(powmod(g, cur, n));
   sort(ans.begin(), ans.end());
   return ans:
5.5 fast-fourier-transform
```

```
^= bit;
        if(i < j)
            swap(a[i], a[j]);
   for(int len = 2; len <= n; len <<= 1){
   double ang = 2*PI/len*(invert ? -1 : 1);</pre>
        cd wlen(cos(ang), sin(ang));
        for(int i = 0; i < n; i += len){
            cd w(1);
            for(int' j = 0; j < len/2; j++){
   cd u = a[i+j], v = a[i+j+len/2]*w;</pre>
                a[i+j] = u+v;
                a[i+i+len/2] = u-v:
                w *= wlen;
       }
   if(invert){
        for(cd &x: a)
            x /= n;
vector<int> multiply(vector<int> const& a, vector<int>
    vector<cd> fa(a.begin(), a.end());
    vector<cd> fb(b.begin(), b.end());
    int n = 1;
    while(n < a.size()+b.size())</pre>
        n <<= 1:
    fa.resize(n):
    fb.resize(n)
    fft(fa, false)
   fft(fb, false);
for(int i = 0; i < n; i++)</pre>
       fa[i] *= fb[i];
    fft(fa, true);
    vector<int> result(n);
   for(int i = 0; i < n; i++)
  result[i] = round(fa[i].real());</pre>
    return result;
 *Number Theoretic Transformation
ll int gcd(ll int a,ll int b){
    if(b==0) return a;
    else return gcd(b,a%b);
ll int egcd(ll int a, ll int b, ll int & x, ll int & y) {
   if (a == 0) {
        x = 0;
        y = 1;
        return b:
    11 int x1, y1;
   ll int d = egcd(b % a, a, x1, y1);
   x = v1 - (b / a) * x1:
   v = x\bar{1};
    return d;
11 int ModuloInverse(ll int a,ll int n){
    ll int x,y;
   x=gcd(a,n);
    a=a/x;
   n=n/x:
   11 int res = egcd(a,n,x,y);
    x=(x%n+n)%n;
    return x;
const int mod = 998244353
const int root = 15311432
const int root_1 = 469870224;
const int root_pw = 1 << 23;</pre>
void fft(vector<int> & a, bool invert) {
    int n = a.size();
   for (int i = 1, j = 0; i < n; i++) {
        int bit = n >> 1;
        for (; j & bit; bit >>= 1)
j ^= bit;
        j ^= l
j ^= bit;
        if (i < j)
```

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```
swap(a[i], a[j]);
   for (int len = 2; len <= n; len <<= 1) {
        int wlen = invert ? root_1 : root;
        for (int i = len; i < root_pw; i <<= 1)
            wlen = (int)(1LL * wlen * wlen % mod):
        for (int i = 0; i < n; i += len) {
            int w = 1;
            for (int j = 0; j < len / 2; j++) {
  int u = a[i+j], v = (int)(1LL * a[i+j+len/2] * w</pre>
                     % mod);
                a[i+j] = u + v < mod ? u + v : u + v - mod;
                a[i+j+len/2] = u - v >= 0 ? u - v : u - v + mod;
                w = (int)(1LL * w * wlen % mod);
   if (invert) {
        int n_1 = (int) ModuloInverse(n, mod);
        for (int & x : a)
            x = (int)(1LL * x * n 1 \% mod):
vector<int> multiply(vector<int> const& a, vector<int>
   vector<int> fa(a.begin(), a.end());
vector<int> fb(b.begin(), b.end());
    int n = 1:
   while(n < a.size()+b.size())</pre>
       n <<= 1;
    fa.resize(n);
   fb.resize(n);
   fft(fa, false);
   fft(fb, false);
   for(int i = 0; i < n; i++)
    fa[i] = (int) (1LL*fa[i]*fb[i]%mod);</pre>
    fft(fa, true);
   vector<int> result(n);
   for(int i = 0; i < n; i++)
        result[i] = fa[i];
    return result;
```

5.6 fast-walsh-hadamard

```
typedef long long ftype;
void fwht_xor(ftype *data, int dim,bool invert) {
    for (int len = 1; 2 * len <= dim; len <<= 1) {
        for (int i = 0; i < dim; i += 2 * len) {
            for (int j = 0; j < len; j++) {
   ftype a = data[i + j];</pre>
                ftype b = data[i + j + len];
data[i + j] = (a + b);
                data[i + j + len] = (a - b);
   if(invert){
        for(int i=0:i<dim:i++){</pre>
            data[i]=data[i]/dim;
void fwht_and(ftype *P, int dim,bool inverse){
   for (int len = 1; 2 * len <= dim; len <<= 1) {
        for (int i = 0; i < dim; i += 2 * len) {
            for (int j = 0; j < len; j++) {
   ftype u = P[i + j];</pre>
                ftype v = P[i + len + j];
                if (!inverse) {
                    P[i + j] = v;
                    P[i + len + j] = (u + v) \% mod;
                    P[i + j] = (mod-u + v)\%mod;
                    P[i + len + i] = u:
```

```
15.7 find-root
double sqrt_newton(double n) {
   const double eps = 1E-15;
   double x = 1;
   for (;;) {
       double nx = (x + n / x) / 2;
       if (abs(x - nx) < eps)
   return x;
int isqrt_newton(int n) {
   bool decréased = false;
   for (;;) {
       int nx = (x + n / x) >> 1;
       if (x == nx \mid | nx > x && decreased)
           break
       decreased = nx < x;
       x = nx;
```

5.8 integer-factorization

return x;

```
long long pollards_p_minus_1(long long n) {
  int B = 10;
   long long g = 1;
   while (B <= 1000000 && g < n) {
       long long a = 2 + rand() \% (n - 3);
        g = gcd(a, n);
        if (g > 1)
           return g;
        // compute a^M
       for (int p : primes) {
           if (p >= B)
               continue;
           long long p_power = 1;
           while (p_power * p <= B)</pre>
               p_power *= p;
           a = power(a, p_power, n);
           g = gcd(a - 1, n);
           if (g > 1 && g < n)
               return g;
       Ď *= 2:
   return 1:
long long mult(long long a, long long b, long long mod) {
   long long result = 0;
   while (b) {
       if (b & 1)
          result = (result + a) % mod;
       a = (a + a) \% mod;
       b >>= 1:
   return result;
long long f(long long x, long long c, long long mod) {
   return (mult(x, x, mod) + c) % mod;
long long rho(long long n, long long x0=2, long long c=1) {
   long long x = x0;
   long long y = x0;
   long long g = 1;
   while (g == 1) {
       x = f(x, c, n);
       y = f(y, c, n);
       y = f(y, c, n);
       g = gcd(abs(x - y), n);
long long brent(long long n, long long x0=2, long long c=1) {
```

```
long long x = x0;
long long g = 1;
long long q = 1;
long long xs, y;
int m = 128;
int \bar{1} = 1;
while (g == 1) {
    for (int i = 1; i < 1; i++)
       x = f(x, c, n);
    int k = 0;
    while (k < 1 && g == 1) {
    xs = x:
        for (int i = 0; i < m && i < 1 - k; i++) {
           x = f(x, c, n);
            q = mult(q, abs(y - x), n);
       g = gcd(q, n);
        k += m;
if (g == n) {
    do {
       xs = f(xs, c, n);
        g = gcd(abs(xs - y), n);
    } while (g == 1);
return g;
```

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5.9 integration-simpson

```
const int N = 1000 * 1000; // number of steps (already
    multiplied by 2)
double simpson_integration(double a, double b){
    double h = (b - a) / N;
    double s = f(a) + f(b); // a = x_0 and b = x_2n
    for (int i = 1; i <= N - 1; ++i) { // Refer to final
        Simpson's formula
        double x = a + h * i;
        s += f(x) * ((i & 1) ? 4 : 2);
    }
    s *= h / 3;
    return s;
}</pre>
```

5.10 linear-diophantine-equation-gray-code

```
int gcd(int a, int b, int& x, int& y) {
   if (b == 0) {
      x = 1;
       y = 0;
      return a;
   int x1, y1;
   int d = gcd(b, a % b, x1, y1);
   x = y1;
   y = x1 - y1 * (a / b);
   return d:
bool find_any_solution(int a, int b, int c, int &x0, int &y0,
    int &g) {
   g = gc\bar{d}(abs(a), abs(b), x0, y0);
   if (c % g) {
      return false;
   x0 *= c / g;
   y0 *= c / g;
   if (a < 0) x0 = -x0:
   if (b < 0) v0 = -v0;
void shift_solution(int & x, int & y, int a, int b, int cnt) {
  x += cnt * b;
   y -= cnt * a;
int find_all_solutions(int a, int b, int c, int minx, int
    maxx, int miny, int maxy) {
   int x, y, g;
   if (!find_any_solution(a, b, c, x, y, g))
```

```
return 0:
   a /= g;
   b /= g;
   int sign_a = a > 0 ? +1 : -1;
   int sign_b = b > 0 ? +1 : -1;
   shift_solution(x, y, a, b, (minx - x) / b);
   if (x < minx)
       shift_solution(x, y, a, b, sign_b);
   if (x > maxx)
       return 0;
   int lx1 = x;
   shift_solution(x, y, a, b, (maxx - x) / b);
   if (x > maxx)
       shift_solution(x, y, a, b, -sign_b);
   shift_solution(x, y, a, b, -(miny - y) / a);
   if (y < miny)</pre>
       shift_solution(x, y, a, b, -sign_a);
   if (y > maxy)
       řeturn 0;
   int 1x2 = x:
   shift_solution(x, y, a, b, -(maxy - y) / a);
   if (y > maxy)
       shift_solution(x, y, a, b, sign_a);
   int rx2 = x;
   if (1x2 > rx2)
       swap(1x2, rx2);
   int lx = max(lx1, lx2);
   int rx = min(rx1, rx2);
   if (lx > rx)
       return 0;
   return (rx - lx) / abs(b) + 1;
int g (int n) {
   return n ^ (n >> 1);
int rev_g (int g) {
  int n = 0;
 for (; g; g >>= 1)
n = g;
 return n:
```

5.11 linear-equation-system

```
const double EPS = 1e-9:
const int INF = 2; // it doesn't actually have to be infinity
     or a big number
int gauss (vector < vector <double> > a, vector <double> & ans) {
    int n = (int) a.size();
int m = (int) a[0].size() - 1;
    vector<int> where (m, -1);
    for (int col=0, row=0; col<m && row<n; ++col) {</pre>
        int sel = row;
        for (int i=row; i<n; ++i)
    if (abs (a[i][col]) > abs (a[sel][col]))
                 sel = i
        if (abs (a[sel][col]) < EPS)</pre>
             continue;
         for (int i=col; i<=m; ++i)
   swap (a[sel][i], a[row][i]);</pre>
         where[col] = row;
        for (int i=0; i<n; ++i)
             if (i != row) {
                  double c = a[i][col] / a[row][col];
                 for (int j=col; j<=m; ++j)
a[i][j] -= a[row][j] * c;
        ++row;
    ans.assign (m, 0);
    for (int i=0; i<m; ++i)
    if (where[i] != -1)</pre>
             ans[i] = a[where[i]][m] / a[where[i]][i];
    for (int i=0; i<n; ++i) {
         double sum = 0;
        for (int j=0; j<m; ++j)
   sum += ans[j] * a[i][j];</pre>
         if (abs (sum - a[i][m]) > EPS)
             return 0;
```

```
for (int i=0: i<m: ++i)
         if (where[i] == -1)
    return INF; return 1;
|5.12\>\>\>\> matrix-determinant
const double EPS = 1E-9:
vector < vector<double> > a (n, vector<double> (n));
double det = 1;
for (int i=0; i<n; ++i) {</pre>
    int k = i:
    for (int j=i+1; j<n; ++j)
  if (abs (a[j][i]) > abs (a[k][i]))
    if (abs (a[k][i]) < EPS) {</pre>
         det = 0;
         break;
    swap (a[i], a[k]);
    if (i != k)
det = -det:
     det *= a[i][i];
    for (int j=i+1; j<n; ++j)
    a[i][j] /= a[i][i];</pre>
    for (int j=0; j<n; ++j)
if (j != i && abs (a[j][i]) > EPS)
              for (int k=i+1; k<n; ++k)
a[j][k] -= a[i][k] * a[j][i];
cout << det:
```

5.13 matrix-rank

```
const double EPS = 1E-9:
int compute_rank(vector<vector<double>> A) {
   int n = A.size();
   int m = A[0].size();
   int rank = 0;
   vector<bool> row_selected(n, false);
   for (int i = 0; i < m; ++i) {
       int j;
       for (j = 0; j < n; ++j) {
           if (!row_selected[j] && abs(A[j][i]) > EPS)
       if (j != n) {
    ++rank;
           row_selected[j] = true;
           for (int p = \tilde{i} + 1; p < m; ++p)
                A[j][p] /= A[j][i];
           for (int k = 0; k < n; ++k)
               if (k != j && abs(A[k][i]) > EPS) {
                   for (int p = i + 1; p < m; ++p)
A[k][p] -= A[j][p] * A[k][i];
       }
   return rank;
```

5.14 primality-test

```
using u64 = uint64_t;
using u128 = __uint128_t;
u64 binpower(u64 base, u64 e, u64 mod) {
    u64 result = 1;
    base %= mod;
    while (e) {
        if (e & 1)
            result = (u128)result * base % mod;
        base = (u128)base * base % mod;
        e >>= 1;
    }
    return result;
}
bool check_composite(u64 n, u64 a, u64 d, int s) {
```

```
u64 x = binpower(a, d, n);
if (x == 1 | | x == n - 1)
       return false;
   for (int r = 1; r < s; r++) {
       x = (u128)x * x % n;
       if (x == n - 1)
           return false;
   return true;
bool MillerRabin(u64 n) { // returns true if n is prime, else
    returns false.
   if (n < 2)
       return false:
    int r = 0;
   u64 d = n - 1
   while ((d & 1) == 0) {
       d >>= 1;
       r++;
   for (int a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37})
        if (n == a)
           return true:
        if (check_composite(n, a, d, r))
           return false:
   return true:
bool probablyPrimeFermat(int n, int iter=5) {
   if (n < 4)
       return n == 2 || n == 3;
   for (int i = 0; i < iter; i++) {
   int a = 2 + rand() % (n - 3);
        if (binpower(a, n-1, n) != 1)
           return false:
   return true;
```

5.15 prime counting function

```
///Source: Zahin vai's Library
#include<bits/stdc++.h>
using namespace std;
typedef long long LL;
#define MAXN 500
#define MAXN 100010
#define MAX 1000010
#define 11 long long int
#define chkbit(ar, i) (((ar[(i) >> 6]) & (1 << (((i) >> 1) &
     31))))
#define setbit(ar, i) (((ar[(i) >> 6]) |= (1 << (((i) >> 1) &
     31))))
#define isprime(x) (( (x) && ((x)&1) && (!chkbit(ar, (x)))) ||
     ((x) = 2)
namespace pcf{
    long long dp [MAXN] [MAXM];
    unsigned int ar[(MAX>>6)+5] = \{0\}:
    int len=0, primes[MAXP], counter[MAX];
    void Sieve(){
        setbit(ar,0), setbit(ar,1);
for (int i=3;(i*i)<MAX;i++,i++){
             if(!chkbit(ar, i)){
                 for(int j=(i*i);j<MAX;j+=k) setbit(ar,j);</pre>
        for(int i=1;i<MAX;i++){</pre>
             counter[i]=counter[i - 1];
             if(isprime(i)) primes[len++]=i, counter[i]++;
    void init(){
        Sieve();
        for(int n=0;n<MAXN;n++){</pre>
             for(int m=0;m<MAXM;m++){</pre>
                 if(!n) dp[n][m]=m;
                 else dp[\bar{n}][m] = dp[n-1][m] - dp[n-1][m/primes[n-1]];
```

```
11 phi(11 m, int n){
        if(n==0) return m;
if(primes[n-1]>=m) return 1;
        if(m<MAXM && n<MAXN) return dp[n][m];</pre>
        return phi(m,n-1) - phi(m/primes[n-1],n-1);
    11 Lehmer(long long m){
   if(m<MAX) return counter[m];</pre>
         ll w,res=0;
        int i,a,s,c,x,y;
s=sqrt(0.9+m), y=c=cbrt(0.9+m);
         a=counter[y], res=phi(m,a)+a-1;
for(i=a;primes[i]<=s;i++)</pre>
              res=res-Lehmer(m/primes[i])+Lehmer(primes[i])-1;
         return res:
    }
///Solves https://old.yosupo.jp/problem/counting_primes
int main() {
    pcf::init();
     long long n;
    cin>>n:
    cout<<pcf::Lehmer(n)<<endl;</pre>
```

6 String

6.1 aho-corasick

```
const int K = 26;
struct Vertex {
    int next[K];
    bool leaf = false;
int p = -1;
    char pch;
    int link = -1;
    int go[K];
    Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
vector<Vertex> t(1);
void add_string(string const& s) {
    int \overline{v} = 0;
    for (char ch : s) {
       int c = ch - 'a';
if (t[v].next[c] == -1) {
    t[v].next[c] = t.size();
            t.emplace_back(v, ch);
        v = t[v].next[c]:
    t[v].leaf = true;
int go(int v, char ch);
int get_link(int v) {
    if (t[v].link == -1)
        if (v == 0 || t[v].p == 0)
           t[v].link = 0;
            t[v].link = go(get_link(t[v].p), t[v].pch);
    return t[v].link;
int go(int v, char ch) {
    int c = ch - 'a';
if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)
            t[v].go[c] = t[v].next[c];
            t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
    return t[v].go[c];
```

6.2 manacher

```
int main(){
   char s[MAX]:
   vector<int> d1(n):
   for (int i = 0, l = 0, r = -1; i < n; i++){
        int k = (i > r) ? 1 : min(d1[l + r - i], r - i + 1);
        while (0 \le i - k \&\& i + k \le n \&\& s[i - k] == s[i + k])
       d1[i] = k--;
if (i + k > r){
l = i - k;
           r = \bar{i} + \bar{k}
    vector<int> d2(n);
   for (int i = 0, l = 0, r = -1; i < n; i++){
        int k = (i > r) ? 0 : min(d2[1 + r - i + 1], r - i + 1);
        while (0 <= i - k - 1 && i + k < n && s[i - k - 1] ==
            s[i + k])
        d2[i] = k--:
       if^{(i+k)r}
           l = i - k - 1;

r = i + k;
   return 0;
```

6.3 palindromic tree

```
struct node -
    int next[26];
    int len;
int sufflink;
    int num;
int len;
char s[MAXN]
node tree[MAXN];
int num;// node 1 - root with len -1, node 2 - root with len 0
int suff;// max suffix palindrome
long long ans;
bool addLetter(int pos) {
  int cur = suff, curlen = 0;
  int let = s[pos] - 'a';
    while (true) {
         curlen = tree[cur].len;
         if (pos - 1 - curlen >= 0 && s[pos - 1 - curlen] ==
              s[pos])
         cur = tree[cur].sufflink;
    if (tree[cur].next[let])
         suff = tree[cur].next[let];
         return false:
    num++:
    suff = num:
    tree[num].len = tree[cur].len + 2;
    tree[cur].next[let] = num;
    if (tree[num].len == 1) {
         tree[num].sufflink = 2;
tree[num].num = 1;
         return true;
    while (true) {
         cur = tree[cur].sufflink:
         curlen = tree[cur].len;
         if (pos - 1 - curlen >= 0 && s[pos - 1 - curlen] ==
              s[pos]) {
            tree[num].sufflink = tree[cur].next[let];
             break:
    tree[num].num = 1 + tree[tree[num].sufflink].num;
 void initTree() {
    num = 2: suff = 2: // memset tree must
    tree[1].len = -1; tree[1].sufflink = 1;
```

```
tree[2].len = 0; tree[2].sufflink = 1;
}
int main() {
    gets(s);
    len = strlen(s);
    initTree();
    for (int i = 0; i < len; i++) {
        addLetter(i);
        ans += tree[suff].num;
    }
    cout << ans << endl;
    return 0;
}</pre>
```

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```
6.4 suffix array da
sa => ith smallest suffix of the string
rak => rak[i] indicates the position of suffix(i) in the
height => height[i] indicates the LCP of i-1 and i th suffix
        LCP of suffix(i) & suffix(i) = { L = rak[i]. R = rak[i]
        , min(height[L+1, R]);}*/
const int maxn = 5e5+5;
int wa[maxn], wb[maxn], wv[maxn], wc[maxn];
int r[maxn],sa[maxn],rak[maxn]
      height[maxn], dp[maxn] [22], jump[maxn], SIGMA = 0;
int cmp(int *r,int a,int b,int 1) {return r[a] == r[b] &&
      r[a+1] == r[b+1];
void da(int *r,int *sa,int n,int m){
    int i,j,p,*x=wa,*y=wb,*t;
    for( i=0;i<m;i++) wc[i]=0;

for( i=0;i<m;i++) wc[x[i]=r[i]] ++;

for( i=1;i<m;i++) wc[i] += wc[i-1];

for( i= n-1;i>=0;i--)sa[--wc[x[i]]] = i;
   for( i= n-1;i>=0;i--)sa[--wc[x[i]]] = 1;
for( j= 1,p=1;p<n;j*=2,m=p){
    for(p=0,i=n-j;i<n;i++)y[p++] = i;
    for(i=0;i<n;i++)if(sa[i] >= j) y[p++] = sa[i] - j;
    for(i=0;i<n;i++)wv[i] = x[y[i]];
    for(i=0;i<n;i++)wc[i] = 0;
    for(i=0;i<n;i++) wc[w[i]] ++;
    for(i=1;i<m;i++)wc[i] += wc[i-1];
    for(i=n-1;i>=0;i--)sa[--wc[wv[i]]] = y[i];
    for(i+w = w = w = n = 1 y[sa[0]] = 0.i=1:i<n:i++) x[sa</pre>
          for(t=x,x=y,y=t,p=1,x[sa[0]] = 0,i=1;i < n;i++) x[sa[i]] =
                 cmp(y,sa[i-1],sa[i],j) ? p-1:p++;
void calheight(int *r,int *sa,int n){
    int i,j,k=0;
for(i=1;i<=n;i++) rak[sa[i]] = i;</pre>
    for(i=0;i<n;height[rak[i++]] = k )</pre>
          for(k?k--:0, j=sa[rak[i]-1]; r[i+k] == r[j+k]; k ++);
void initRMQ(int n){
    for(int i= 0;i<=n;i++) dp[i][0] = height[i];</pre>
    for(int j = 1; (1<<j) <= n; j ++ ){
  for(int i = 0; i + (1<<j) - 1 <= n; i ++ ) {
               dp[i][j] = min(dp[i][j-1], dp[i +
                      (ĭ<<(i-1))][i-1]);
    for(int i = 1;i <= n;i ++ ) {
          int k = 0;
          while((1 << (k+1)) <= i) k++;</pre>
          jump[i] = k;
int askRMQ(int L,int R){
    int k = jump[R-L+1];
return min(dp[L][k], dp[R - (1<<k) + 1][k]);</pre>
int main(){
    scanf("%s",s);
    int n = strlen(s);

for(int i = 0; i < n; i ++) {

   r[i] = s[i]-'a' + 1;
          SIGMA = max(SIGMA, r[i]):
```

```
r[n] = 0:
da(r.sa.n+1.SIGMA + 1): // don't forget SIGMA + 1. It will
    ruin you.
calheight(r,sa,n);
```

```
6.5 suffix-automaton
class SuffixAutomaton{
bool complete;
int last;
set<char> alphabet;
struct state{
    int len, link, endpos, first_pos,snas,height;
    long long substrings, sublen;
bool is_clone;
    map<char, int> next;
vector<int> inv_link;
    state(int leng=0,int li=0){
        len=leng;
        link=li;
         first_pos=-1;
        substrings=0;
         sublen=0: // length of all substrings
        endpos=1;
snas=0; // shortest_non_appearing_string
        is_clone=false;
height=0;
vector<state> st;
void process(int node){
    map<char, int> ::iterator mit;
st[node].substrings=1;
    st[node].snas=st.size();
if((int) st[node].next.size()<(int) alphabet.size())</pre>
        st[node].snas=1;
    for(mit=st[node].next.begin(); mit!=st[node].next.end();
        if(st[mit->second].substrings==0) process(mit->second); fin
st[node].height=max(st[node].height,1+st[mit->second].height); ret
st[node].substrings=st[node].substrings;
         st[node].sublen=st[node].sublen
         +st[mit->second].sublen+st[mit->second].substrings;
         st[node].snas=min(st[node].snas,
                                        1+st[mit->second].snas);
    if(st[node].link!=-1){
        st[st[node].link].inv_link.push_back(node);
void set_suffix_links(int node){
    int i;
    for(i=0; i<st[node].inv_link.size(); i++){
    set_suffix_links(st[node].inv_link[i]);
    st[node].endpos=st[node].endpos+st[st[node].inv_link[i]] endpos+st[ixAutomaton(set<char> &alpha){
void output_all_occurrences(int v, int P_length, vector<int>
     &pos){
    if (!st[v].is_clone)
    pos.push_back(st[v].first_pos - P_length + 1);
for (int u : st[v].inv_link)
        output_all_occurrences(u, P_length, pos);
void kth_smallest(int node,int k,vector<char> &str){
    if(k==0) return;
map<char, int> ::iterator mit;
    for(mit=st[node].next.begin(); mit!=st[node].next.end();
         if(st[mit->second].substrings<k)</pre>
              k=k-st[mit->second].substrings:
             str.push_back(mit->first);
             kth_smallest(mit->second,k-1,str);
```

```
int find_occurrence_index(int node,int index,vector<char>
    &str){
   if(index==str.size()) return node;
   if(!st[node].next.count(str[index])) return -1;
        find_occurrence_index(st[node].next[str[index]],index+1.str);
void klen_smallest(int node,int k,vector<char> &str){
   if(k==0) return;
map<char, int> ::iterator mit;
   for(mit=st[node].next.begin(); mit!=st[node].next.end();
       if (st[mit->second].height>=k-1){
          str.push_back(mit->first);
          klen smallest(mit->second.k-1.str):
void minimum non existing string(int node.vector<char> &str){
   map<char, int> ::iterator mit;
   set<char>::iterator sit:
   for(mit=st[node].next.begin(),sit=alphabet.begin();
        sit!=alphabet.end(); ++sit,++mit){
       if(mit==st[node].next.end()||mit->first!=(*sit)){
          str.push_back(*sit);
          return:
       else if(st[node].snas==1+st[mit->second].snas){
          str.push_back(*sit);
          minimum_non_existing_string(mit->second,str);
void find_substrings(int node,int index,vector<char>
   if(index==str.size()) return;
   if(st[node].next.count(str[index])){
   else{
       sub_info.push_back(make_pair(0,0));
void check(){
   if(!complete){
       process(0);
       set_suffix_links(0);
       int i;
complete=true;
       st.push_back(state(0,-1));
       last=0:
       complete=false:
       set char :: iterator sit;
       for(sit=alpha.begin(); sit!=alpha.end(); sit++){
          alphabet.insert(*sit);
       st[0].endpos=0;
   void sa_extend(char c){
       int cur = st.size();
       st.push_back(state(st[last].len + 1));
       st[cur].first_pos=st[cur].len-1;
      st[cdr].first_pos-st[cdr].fer 1,
int p = last;
while (p != -1 && !st[p].next.count(c)){
    st[p].next[c] = cur;
          p = st[p].link;
       if (p == -1){
          st[cur].link = 0:
       else{
          int q = st[p].next[c];
```

```
if (st[p].len + 1 == st[q].len){}
                                                                                       st[cur].link = q;
                                                                                  else{
                                                                                      int clone = st.size();
st.push_back(state(st[p].len + 1,st[q].link));
st[clone].next = st[q].next;
                                                                                       st[clone].iext = st[q].in
st[clone].is_clone=true;
st[clone].endpos=0;
                                                                                       st[clone].first_pos=st[q].first_pos;
while (p != -1 && st[p].next[c] == q){
                                                                                           st[p].next[c] = clone;
                                                                                           p = st[p].link;
                                                                                       st[q].link = st[cur].link = clone;
                                                                              last = cur;
                                                                              complete=false;
                                                                           SuffixAutomaton(){
                                                                              for (i=0; i<st.size(); i++){
    st[i].next.clear();
    st[i].inv_link.clear();</pre>
                                                                              st.clear():
                                                                              alphabet.clear();
                                                                          void kth_smallest(int k,vector<char> &str){
                                                                              check():
                                                                              kth_smallest(0,k,str);
                                                                          int FindFirstOccurrenceIndex(vector<char> &str){
                                                                              check():
                                                                              int ind=find_occurrence_index(0,0,str);
                                                                              else return st[ind].first_pos+1-(int) str.size();
st[node].next.count(str[index]]/1
find_substrings(st[node].next[str[index]],index+1,str,sub_infb);d FindAllOccurrenceIndex(vector<char> &str,vector<int>
                                                                               &pos){
                                                                              check();
                                                                              int ind=find_occurrence_index(0,0,str);
                                                                              if(ind!=-1) output_all_occurrences(ind,str.size(),pos);
                                                                          int Occurrences(vector<char> &str){
                                                                              check();
                                                                              int ind=find occurrence index(0.0.str):
                                                                              if(ind==0) return 1;
                                                                              else if(ind==-1) return 0;
                                                                              else return st[ind].endpos;
                                                                          void klen_smallest(int k,vector<char> &str){
                                                                              check()
                                                                              if(st[0].height>=k) klen_smallest(0,k,str);
                                                                          void minimum_non_existing_string(vector<char> &str){
                                                                              check();
                                                                              int ind=find occurrence index(0.0.str):
                                                                              if(ind!=-1) minimum_non_existing_string(ind,str);
                                                                          long long cyclic_occurrence(vector<char> &str){
                                                                              check();
int i,j,len;
                                                                              long long ans=0;
                                                                              int n=str.size();
                                                                              set<int> S;
set<int>::iterator it:
                                                                              for(i=0,j=0,len=0; i<n*2-1; i++){
   if(st[j].next.count(str[i%n])){</pre>
                                                                                       len++
                                                                                       j=st[j].next[str[i%n]];
                                                                                   else{
                                                                                       while(j!=-1&&(!st[j].next.count(str[i%n]))){
                                                                                           i=st[i].link:
                                                                                       if(j!=-1){
```

6.6 z-algorithm

```
vector<int> z_function(string s) {
   int n = (int) s.length();
   vector<int> z(n);
   for (int i = 1, l = 0, r = 0; i < n; ++i) {</pre>
```

```
if (i <= r)
    z[i] = min (r - i + 1, z[i - 1]);
while (i + z[i] < n && s[z[i]] == s[i + z[i]])
    ++z[i];
if (i + z[i] - 1 > r)
    l = i, r = i + z[i] - 1;
}
return z;
```

7 header

```
#define FastIO ios::sync_with_stdio(false);
    cin.tie(0);cout.tie(0)

#include <ext/pb_ds/assoc_container.hpp> // Common file
using namespace __gnu_pbds;

/*
find_by_order(k) --> returns iterator to the kth largest
    element counting from 0
order_of_key(val) --> returns the number of items in a set
    that are strictly smaller than our item

*/
typedef tree<
int,
null_type,
less<int>,
```