



# The 39th Annual AAAI Conference on Artificial Intelligence

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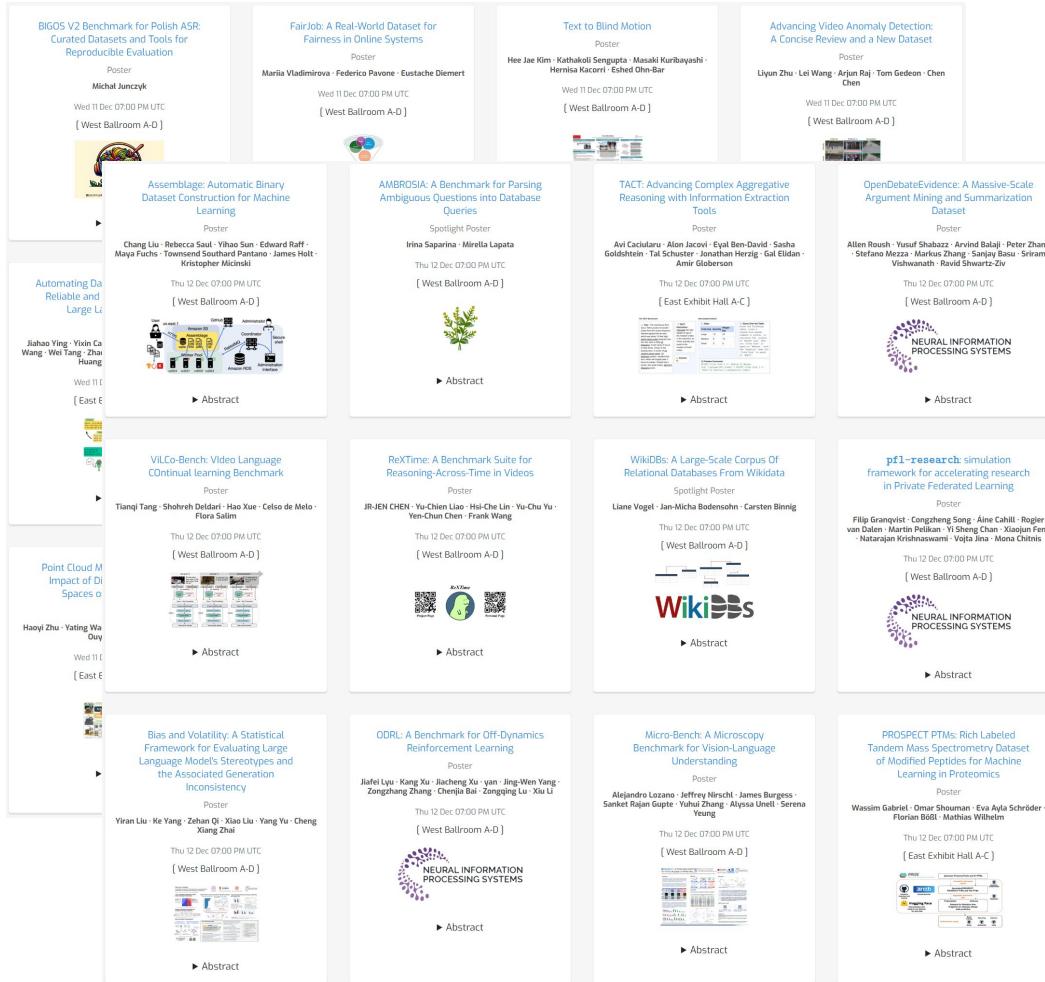


## Evaluating LLM Reasoning in the Operations Research Domain with ORQA

*Mahdi Mostajabdeh, Timothy Tin Long Yu, Samarendra Chandan Bindu Dash, Rindra Ramamonjison,  
Jabo Serge Byusa, Giuseppe Carenini, Zirui Zhou, Yong Zhang*



# Another Benchmark??



## Why ORQA?

- Expert **hand-crafted** dataset
- **Difficult questions** from a highly specialized technical domain
  - Limited exposure during training
  - Multi-step reasoning
- **Significant gap** between tested LLMs and domain experts



0.77

0.93

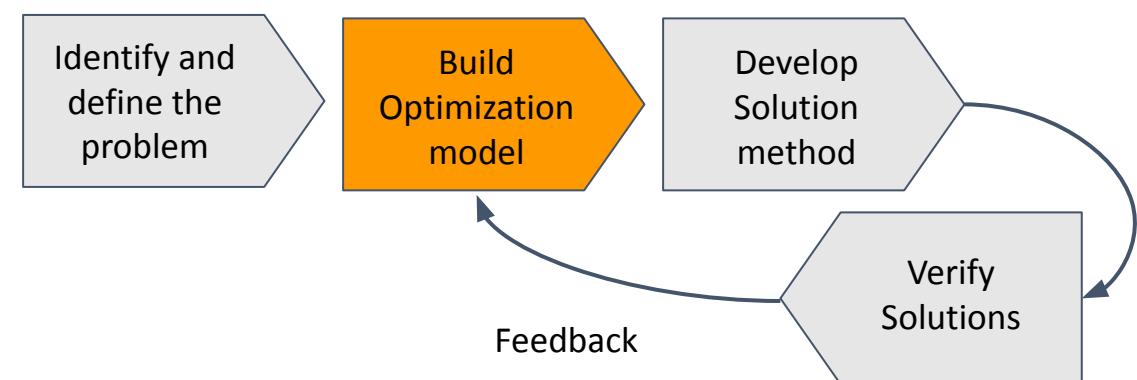
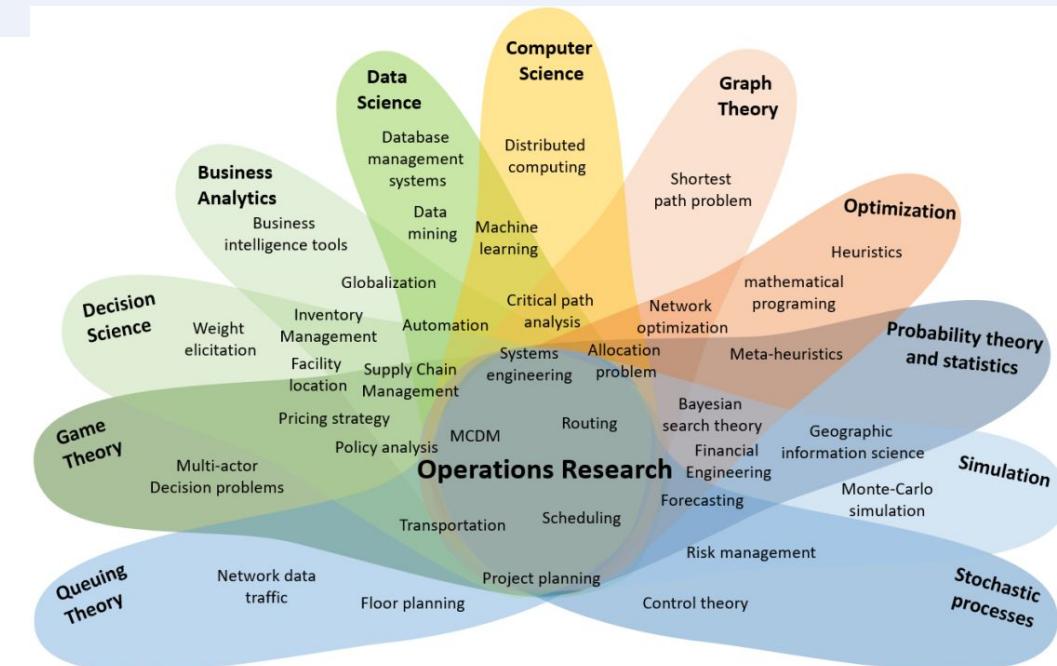
# Overview

- Background & Motivation
- What is ORQA?
- How we created ORQA
- Benchmarking LLMs
- Findings
- Future works

# Background

## The Importance of Operations Research (OR)

- **Wide-Ranging Applications:** Integral to industries like logistics, manufacturing, healthcare, finance, supply chain management, and urban planning.
- **Critical impact:** Automated decision-making, enhances efficiency, reduces costs.
- Optimization Modeling bottleneck of OR wide adaptation.
- Automating the translation of real-world problems into optimization models can revolutionize how industries use OR.
  - Lowers cost of OR projects.
  - Democratizes access to expert-level optimization
  - Expands adoption of OR

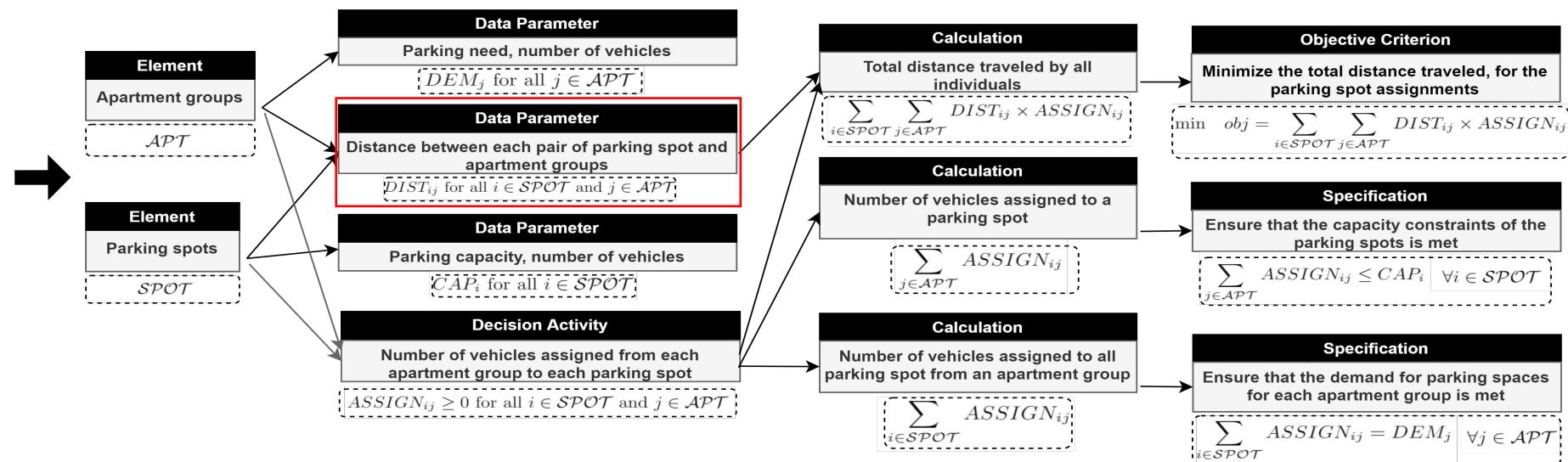


# Background - Complexity of Optimization Modeling Tasks

- **Multiple Components:**
  - **Elements:** Main entities in the problem
  - **Decision activities:** Represent choices that impact the model's outcomes.
  - **Data Parameters:** Critical data that are required to inform the model.
  - **Objective Criterion:** The goals to be maximized or minimized, such as cost, time, or profit.
  - **Constraints:** Rules and limitations that bind the model
- **Interdependencies:**
  - A change in one component (e.g., decision variables) directly affects others (e.g., constraints).
- **Implicit Components & Ambiguities:**
  - Not all model components are explicitly stated in problem descriptions and require expert insight to identify.
  - Problem owners often provide vague or ambiguous descriptions due to lack optimization expertise.

**Problem Description**

At Pine Ridge Estates, as a property management supervisor, your responsibility is to efficiently manage parking spaces for various apartment groups. Each parking spot can accommodate a certain number of vehicles, and every apartment group has its own parking needs. The primary challenge is to arrange parking in a manner that reduces the distance residents have to walk from their cars to their apartments. Remember, you have the flexibility to assign any parking spot to any apartment group.



# Motivation

## Challenges

- **Complex Reasoning Required:**
  - The interrelated nature of components demands multi-step, expert-level reasoning to build accurate models.
- **Dataset Scarcity:**
  - Operates in an underrepresented field where training data is limited, making it a rigorous testbed for LLM capabilities.
  - There are very few small optimization modeling datasets.

## What Makes ORQA Unique?

- Multi-Step Reasoning
- Expert-Level Domain Knowledge
- Complex Interactions
- Niche Technical Domain

## Impact

- **Advancing LLM Research:**
  - Provides insights into the limitations and potential improvements for LLMs in specialized domains.
- **Automation in OR:**
  - Paves the way for automating complex decision-making tasks in real-world operations research applications.

# ORQA Example

## Dataset Instance

### Problem description:

You are an operations manager in the agricultural sector. Your task is to streamline the process of getting crops from farms, processing or storing them as needed, and finally distributing them to various markets or direct consumers.

...

You also need to ensure the produce reaches markets and consumers in its best state, meets demands, and ensures a steady supply.

### Question:

What is the type of optimization model related to this problem?

### Options & answer:

A - Mixed-Integer Linear Programming

B - Linear Programming

C - Integer Linear Programming

D - Non-linear Programming

## Expert Reasoning (val. set only)

### Reasoning steps:

**Step 1:** What are the decision activities in the model?

- Amount of product to cultivate, Selecting a transportation mode (truck, rail, etc.)

**Step 2:** What is the type of values they can get?

- Continuous and integer

**Step 3:** Is there any Non-linear relationship presented in the problem?

- Constraints and objective function does not define a non-linear relation

**Step 4:** Given the variable types and linear or non-linear relationship between them, what is the optimization model type?

- There are both continuous and integer variables and there is no non-linear relation exist in the optimization problem. Therefore, the most suitable optimization model for this problem is Mixed-Integer Linear Programming (MILP).

# ORQA

## Statistics & Characteristics

- 1513 instances
- 1468 for testing; 45 for validation (ICL)
- 20 diverse application domains (e.g., healthcare, urban design, HR, petroleum)
- From each domain:
  - > 3 optimization problems
  - 60 – 90 multiple choice questions
- Standardized optimization model complexity
  - Mathematical model is within pre-defined limits (e.g., number of decision variables)

Component	$\mu$	$\sigma$
Sets	1.97	0.89
Parameters	4.08	2.19
Variables	3.14	2.29
Objectives	1.00	0.00
Constraints	4.60	3.21

# ORQA – Question Types

## 11 Question Types

- Understanding high-level problem specifications
  - Objective identification
  - Explicit constraint identification
  - Problem categorization
- Entities identification
  - Optimization type (e.g., linear, non-linear)
  - Set, decision activities, implicit constraint identification
- Relationship between Entities
  - Parameters and variables in objective / constraints
  - Meaning of calculations in objective / constraints
  - Set that a constraint is applied on

# ORQA – Question Types

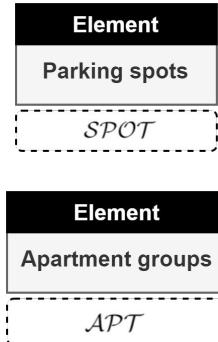
## Set that a constraint is applied on

**Question:** Which of the following system element(s) is the Parking Spot Capacity constraint applied on?

- A. Parking spots, B. Apartment group, C. Parking spots, Apartment group, vehicle count, D. Parking spots, Apartment group

**Problem Description**

At Pine Ridge Estates, as a property management supervisor, your responsibility is to efficiently manage parking spaces for various apartment groups. Each parking spot can accommodate a certain number of vehicles, and every apartment group has its own parking needs. The primary challenge is to arrange parking in a manner that reduces the distance residents have to walk from their cars to their apartments. Remember, you have the flexibility to assign any parking spot to any apartment group.



**Decision Activity**  
Number of vehicles assigned from each apartment group to each parking spot  
 $ASSIGN_{ij} \geq 0$  for all  $i \in SPOT$  and  $j \in APT$

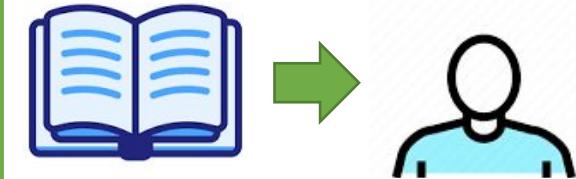
**Calculation**  
Number of vehicles assigned to a parking spot  
$$\sum_{j \in APT} ASSIGN_{ij}$$

**Specification**  
Ensure that the capacity constraints of the parking spots is met  
$$\sum_{j \in APT} ASSIGN_{ij} \leq CAP_i \quad \forall i \in SPOT$$

**A. Parking spots**

# Dataset Creation and Verification

## Selecting & Creating Optimization Problem Descriptions



1. Select optimization problem
2. Write domain-specific description focusing on diverse application domains

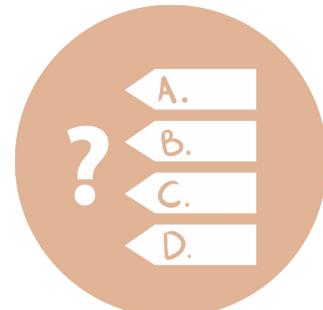
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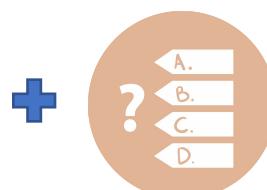
## Creating Q&A Pair



1. Reference problem description
2. Select question type
3. Create target answer
4. Create incorrect options



## Instance Verification



- ✓ Completeness
- ✓ No Ambiguity in Q&A
- ✓ Correctness in answer

- ✓ Multi-step reasoning
- ✓ Correctness in answer



# Benchmarking Results

Model	Standard (Acc)			CoT (Acc)	
	0-shot	1-shot	3-shot	0-shot	1-shot
Llama3.1-8B-I	0.588	0.615	0.618	0.563	0.324
Llama3.1-70B-I	0.702	0.721	0.735	0.689	0.292
Llama3.1-405B-I	0.723	0.753	0.772	0.695	0.360
Llama3-8B-I	0.535	0.573	0.592	0.530	0.364
Llama3-70B-I	0.676	0.716	0.710	0.671	0.448
Llama2-7B-Chat	0.368	0.375	0.403	0.368	0.282
Llama2-13B-Chat	0.409	0.437	0.454	0.432	0.313
Llama2-70B-Chat	0.526	0.552	0.589	0.518	0.372
FLAN-T5-XXL-11B	0.503	-	-	0.457	-
Falcon-7B-I	0.245	0.246	0.245	0.242	0.243
DeepSeek-M-7B-I	0.478	0.552	0.559	0.379	0.514
NuminaMath-7B	0.250	0.484	0.525	-	0.290
Mistral-7B-I-v0.1	0.467	0.475	0.483	0.460	0.407
Mistral-7B-I-v0.3	0.523	0.555	0.555	0.539	0.543
Mixtral-8x7B-I-v0.1	0.588	0.606	0.612	0.565	0.565



0.93

# Chain-of-Thought

CoT had **negative** (or negligible) impact on model performance of most models

Model	Standard (Acc)			CoT (Acc)	
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Llama3.1-8B-I	0.588	0.615	0.618	0.563	0.324
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# Detailed Reasoning Analysis

## Reasoning Analyses

### Correct Answer

**Context:** As a sales manager, you're tasked with the challenge of designing sales territories for your customers. The aim is to create regions that balance sales potential, workload, and compactness. Sales potential is estimated from past sales data of each customer. Workload is gauged by the estimated number of hours a sales representative should spend with a customer each week. Compactness is calculated by adding up the distances of all customers from the most central customer in the region. This distance is measured as a straight line based on the latitude and longitude of each customer. Your goal is to keep the maximum distance from the center of the regions as small as possible. At the same time, you need to ensure that the workload in each region doesn't exceed a set target, and that the sales potential in each region reaches a certain threshold. You also aim to keep the total distance from the centers as small as possible, with a specific weight assigned to this goal. You have a set of customers in Texas, each with their own workload, sales potential, and geographical coordinates. Your job is to design territories for these customers that meet your goals and stick to the rules.

**Question:** Under which category does the given optimization problem fall in to?

- A. Allocation problem
- B. Assortment optimization
- C. Blending problem
- D. Clustering problem

**Generated Reasoning:** Let's think step by step

The decision variables are the boundaries of the sales territories. The objective function is to minimize the total distance from the centers of the regions while ensuring that the workload in each region doesn't exceed a set target, and that the sales potential in each region reaches a certain threshold. The constraints are the workload in each region not exceeding a set target, the sales potential in each region reaching a certain threshold, and the distance from the center of the regions being as small as possible. This is a clustering problem, as we are grouping customers into regions or clusters based on their geographical coordinates, sales potential, and workload. The goal is to find the optimal way to cluster the customers to meet the objectives. Therefore, the correct answer is (D) Clustering problem.

### Incorrect Answer

**Context:** As an operations manager of Horizon International airport, you are tasked with assigning flights to the terminal gates in the most effective way to enhance the passengers' comfort and to avoid flight delays. The success of this task is integral to smooth airport operations. Every day, multiple flights are either arriving or departing, and each one must be allocated a specific gate within the terminal. Your goal is to find an assignment that decreases the total walking distance for passengers changing flights. The total walking distance is influenced by the number of passengers transferring, the layout of the terminal and the positioning of the gates. Therefore, you will need to consider both the distance between every pair of gates and the number of flight transfers happening between those specific gates. The flight schedule, including the number of flights and transfers, and the terminal layout, including the number of gates and the distance between them, are available daily. Using this information, your task is to calculate the most beneficial allocation of flights to gates, ensuring every flight has a designated gate.

**Question:** Which of the following options defines a constraint that is specified in the description of this problem?

- A. Each gate should receive at most one flight.
- B. Each flight must be assigned to at most one gate.
- C. Every arriving or departing flight must be assigned to at least one gate.
- D. Every arriving or departing flight must be assigned to one gate.

**Generated Reasoning:** Let's think step by step

the problem states that "Every day, multiple flights are either arriving or departing, and each one must be allocated a specific gate within the terminal." This implies that every arriving or departing flight must be assigned to at least one gate. Therefore, option C is a constraint that is specified in the description of this problem. Option A is incorrect because it states that each gate should receive at most one flight, which means that some gates might not receive any flights, which is not stated in the problem. Option B is also incorrect because it states that each flight must be assigned to at most one gate, which means that some flights might not be assigned to any gate, which is not stated in the problem. Option D is incorrect because it states that every arriving or departing flight must be assigned to one gate, which is a stronger statement than the constraint specified in the problem. The problem only states that each flight must be allocated a specific gate, without specifying whether it must be the only gate for that flight. The correct answer is C. Every arriving or departing flight must be assigned to at least one gate.

Pattern A	Correct Logic
Pattern B	Correct recall of knowledge
Pattern C	Correct reading comprehension

Pattern A	Incorrect Logic
Pattern B	Incorrect or insufficient knowledge
Pattern C	Incorrect reading comprehension

## Reasoning Insights (stats)

### Metric

### 0-shot 1-shot

Instances with correct answer	35.6%	33.3%
Instances where all reasoning steps are correct	15.6%	31.1%
Incorrect reasoning, correct answer	20.0%	6.7%
Incorrect answer, correct reasoning	0.0%	4.4%
Avg. number of steps per instance	7.93	4.53
Avg. accuracy of steps per instance	0.682	0.611

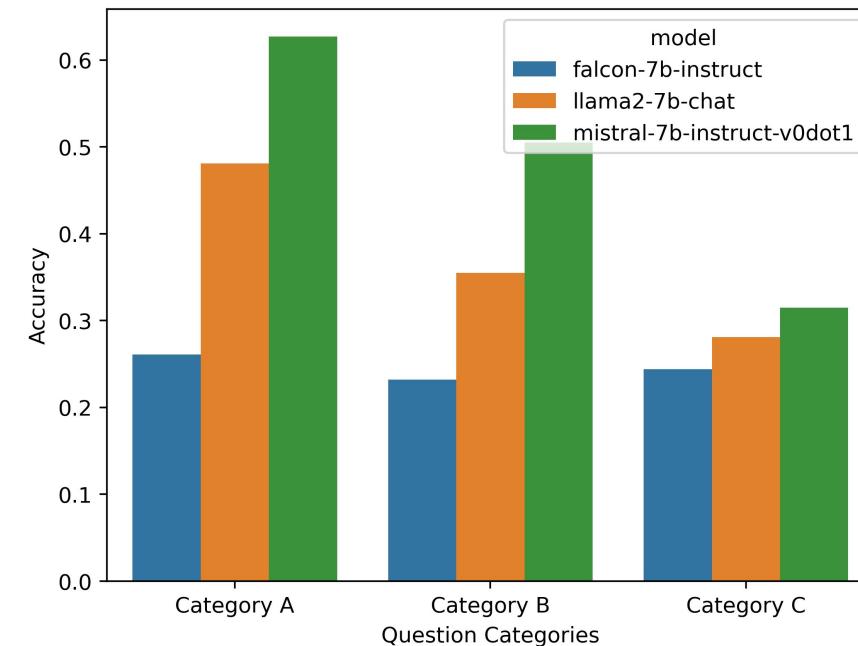
Question Category	Correct Steps	Incorrect Logic	Insufficient Knowledge	Incorrect Reading Comprehension
Category A	0.772	0.087	0.102	0.039
Category B	0.690	0.134	0.106	0.070
Category C	0.740	0.134	0.063	0.063

# Question Types (Difficulty)

## Significantly more difficult:

- Model building & understanding are significantly more difficult
- Relationships of optimization model components

llama2-7b-chat	0.58	0.42	0.46	0.41	0.35	0.31	0.35	0.31	0.31	0.25	0.24
llama2-13b-chat	0.68	0.52	0.59	0.53	0.44	0.40	0.42	0.27	0.23	0.28	0.25
llama2-70b-chat	0.74	0.64	0.66	0.61	0.59	0.51	0.62	0.34	0.31	0.44	0.36
flan-t5-xxl	0.80	0.63	0.68	0.39	0.55	0.49	0.53	0.36	0.28	0.33	0.42
falcon-7b-instruct	0.26	0.28	0.25	0.22	0.24	0.24	0.22	0.25	0.28	0.23	0.20
mistral-7b-instruct	0.67	0.56	0.66	0.59	0.47	0.46	0.52	0.34	0.31	0.36	0.25



# ICL and Trigger Prompt on Reasoning

## ICL Selection

Approach	Accuracy
Random selection	0.300
Same question type	0.313
Similar length	0.353
Similar length & same question type	0.362

Length of ICL examples has more impact on performance than question type (similarity)

## Trigger Prompts Selection

CoT Prompt (0-shot with Llama-3.1-70B-Instruct)	Average	STD	Best
Let's think step by step	0.688	0.001	0.689
Let's work by elimination	0.648	0.000	0.649
Let's reflect on each answer option like an operations research expert	0.689	0.001	0.689
Let's use step by step inductive reasoning, given the mathematical nature of the question	0.674	0.003	0.676
Let's think step by step like an operations research expert	0.685	0.000	0.685
Prompt ensembling (majority vote)	0.696	0.008	0.702

Trigger prompts and ensembling multiple runs may yield better results

# Conclusion & Future Works

<https://github.com/nl4opt/ORQA>

The screenshot shows the GitHub repository for ORQA. At the top, there are buttons for 'main' (with 1 branch and 0 tags), a search bar ('Go to file'), and a 'Code' button. Below this is a list of commits:

- mahdms Update README.md (95f4e5e · last month)
- Add files via upload (2 months ago)
- Update README.md (last month)

Below the commits is the contents of the README file:

```
Evaluating LLM Reasoning in the Operations Research Domain with ORQA

Accepted paper at AAAI 2025: arXiv Link
```

AI Gallery Notebook详情 开发者 华为云 (huaweicloud.com)

The screenshot shows the AI Gallery notebook page for 'Evaluating LLM Reasoning in Operations Research Domai...'. The page includes a diagram illustrating the relationship between Elements, Data Parameter, Decision Activities, Calculations, and Applications. The notebook was accepted by AAAI2025 and has 4 likes. It includes tabs for description, delivery, limit, version, and comments, and a 'Run in ModelArts' button.

## Future Works

- Evaluate on more models
- Expand the dataset
- Automate the reasoning analysis

ORQA □ Models more proficient at reasoning



**QwQ-32B-Preview**



**o3-mini**

# Thank you!

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