Algorithm 1 t-SVD for third order tensors

Input: $\mathcal{M} \in \mathbb{R}^{n_1 \times n_2 \times n_3}$

Output: $\mathcal{U} \in \mathbb{R}^{n_1 \times n_1 \times n_3}$, $\mathcal{S} \in \mathbb{R}^{n_1 \times n_2 \times n_3}$, $\mathcal{V} \in$ $\mathbb{R}^{n_2 \times n_2 \times n_3}$

$$\mathfrak{D} \leftarrow \mathrm{fft}(\mathfrak{M}, [\], 3)$$

for i = 1 to n_3 do

$$[\mathbf{U}, \mathbf{S}, \mathbf{V}] = \operatorname{syd}(\mathbf{\mathcal{D}}^{(i)})$$

$$egin{aligned} \left[\mathbf{U},\mathbf{S},\mathbf{V}
ight] &= \mathtt{svd}(\mathbf{\mathcal{D}}^{(i)}) \ \widehat{\mathbf{\mathcal{U}}}^{(i)} &= \mathbf{U}; \ \widehat{\mathbf{S}}^{(i)} &= \mathbf{S}; \ \widehat{\mathbf{\mathcal{V}}}^{(i)} &= \mathbf{V}; \end{aligned}$$

end for

$$\mathfrak{U} \leftarrow \mathrm{ifft}(\widehat{\mathfrak{U}}, [], 3); \ \mathfrak{S} \leftarrow \mathrm{ifft}(\widehat{\mathfrak{S}}, [], 3); \ \mathfrak{V} \leftarrow \mathrm{ifft}(\widehat{\mathfrak{V}}, [], 3)$$