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How to Think Like a Computer Scientist





Learning with Python 3 (RLE)

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by Peter Wentworth, Jeffrey Elkner, Allen B. Downey, and Chris Meyers

(based on 2nd edition by Jeffrey Elkner, Allen B. Downey, and Chris Meyers)

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Source for this RLE version: https://code.launchpad.net/~thinkcspy-rle-team/thinkcspy/thinkcspy3-<u>rle</u>

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Index — How to Think Like a Computer Scientist: Learning with Python 3 How to Think Like a Computer Scientist: Learning with Python 3 » index Index Symbols | A | B | C | D | E | F | G | H | I | I | K | L | M | N | O | P | Q | R | S | T | U | V | W **Symbols** 3n + 1 sequence Α abbreviated assignment animation rate abecedarian series argument, [1] abstract data type (ADT) argv <u>accumulator</u> assignment, [1] algorithm, [1], [2], [3] <u>tuple</u> deterministic assignment statement, [1], [2] <u>aliases</u>, [1], [2] assignment token alternative execution attribute, [1], [2], [3], [4], [5] ambiguity В baked animation boolean expression, [1] bar chart boolean function, [1] boolean value, [1] base case, [1] branch, [1] binary operator binary search break statement binary tree **breakpoint** bind bug, [1] blit builtin scope block, [1] <u>bump</u> body, [1], [2], [3] **bytecode** C call graph composition, [1], [2] canvas, [1] (of functions) composition of functions cargo chained conditional, [1] compound data type, [1], [2] compound statement, [1] character chatterbox function **body** child <u>header</u> child class computation pattern

concatenate

condition, [1]

conditional

concatenation, [1]

chunking, [1]

class attribute

<u>class</u>, [1]

client

<u>clone</u> , [1]	<u>chained</u>
collection, [1]	conditional branching
command line	conditional execution
command line argument	conditional statement, [1
command prompt	conditionals
comment, [1]	<u>nested</u>
<u>comments</u>	constant time
comparison of strings	<u>constructor</u>
comparison operator, [1]	continue statement, [1]
compile, [1]	control flow, [1]
	<u>copy</u>
	<u>deep</u>
	<u>shallow</u>
	<u>counter</u>
	counting pattern
	cursor, [1]
D	
data structure, [1]	<u>delimiter, [1], [2]</u>
<u>recursive</u>	deterministic algorithm
data type, [1]	development plan, [1]
dead code, [1]	dictionary, [1]
debugging, [1], [2]	dir function
decrement	directory, [1]
deep copy	<u>docstring</u> , [1], [2]
deep equality, [1]	dot notation, [1]
default value, [1]	dot operator, [1]
<u>definite iteration</u>	<u>dot product</u>
definition	Doyle, Arthur Conan
function, [1]	
<u>recursive</u>	
del statement, [1]	
_	
E	
<u>element</u> , [1], [2]	<u>equality</u>
<u>elif</u>	<u>deep</u>
<u>else</u>	<u>shallow</u>
<u>embedded reference</u>	escape sequence, [1]
<u>encapsulate</u>	<u>eureka traversal</u>
<u>encapsulation</u>	<u>evaluate</u>
<u>encode</u>	event, [1]
<u>enumerate</u>	<u>exception</u> , [1], [2], [3]
	<u>handling</u>
	<u>executable</u>
	expression, [1], [2]
	<u>boolean</u>

fractal
Cesaro torn square
<u>Sierpinski triangle</u>
frame
frame rate
fruitful function, [1]
fully qualified name
function, [1], [2], [3]
<u>argument</u>
<u>composition</u>
<u>len</u>
<u>parameter</u>
<u>pure</u>
function call
function composition, [1]
function definition, [1], [2]
function type
functional programming style
fundamental ambiguity theorem
generic data structure
global scope
<u>5.024.200 pc</u>
<u>header line</u>
<u>help</u>
<u>helper</u>
high-level language, [1]
Holmes, Sherlock
Homes, Sheriock
initialization (of a variable)
<u>initializer method</u>
input
input dialog
instance, [1], [2]
instance, 111, 121
int, [1], [2]
integer
integer division, [1]
<u>Intel</u>
<u>interface</u>
interpret, [1]

index, [1], [2], [3] negative indexing ([]) infinite loop, [1] infinite recursion, [1] infix inheritance	invariant invoke, [1] is operator item, [1], [2] item assignment iteration, [1], [2]
J join	justification
K key, [1] key-value pair, [1]	keyword, [1]
L leaf len function length function (len) level lifetime, [1] linear linear search linear time link linked list linked queue Linux	list, [1], [2] append nested, [1] list index list traversal, [1] literalness local scope local variable, [1], [2] logarithm logical operator, [1], [2] loop, [1] loop body, [1] loop variable, [1] low-level language, [1]
M Make Way for Ducklings mapping type, [1] matrix, [1] McCloskey, Robert memo, [1] Merge algorithm meta-notation, [1] method, [1], [2], [3]	middle-test loop mode modifier, [1], [2], [3] module, [1], [2], [3] modulus operator, [1] mutable, [1], [2] mutable data type, [1], [2]
N namespace, [1] naming collision natural language, [1] negative index	nesting newline, [1] Newton's method node

nested conditionals	non-volatile memory
<u>nested list</u> , [1], [2]	None, [1]
nested loop	<u>normalized</u>
0	
object, [1], [2], [3]	operations on strings
object code	operator, [1]
object-oriented language	<u>comparison</u>
object-oriented programming, [1]	<u>in</u>
objects and values	logical, [1]
operand, [1]	modulus
	operator overloading
	optional parameter, [1] order of operations
	order of operations
P	
parameter, [1], [2]	prefix notation
<u>optional</u>	<u>preorder</u>
<u>parent</u>	print function
<u>parent class</u>	priority queue
parse, [1], [2]	Priority Queue
<u>pass statement</u>	<u>probe</u>
<u>path</u>	problem solving
<u>pattern</u>	program, [1], [2]
pattern of computation	program development
<u>Pentium</u>	program tracing
pixel	programming language
poetry	<u>promise</u> , [1], [2]
poll, [1]	prompt
polymorphic	<u>prose</u>
portability	provider
portable	pure function, [1]
post-test loop	PyGame PyGame
postfix	<u>PyScripter</u>
<u>postorder</u> <u>pre-test loop</u>	single stepping
precondition	Python shell
<u>precondition</u>	
Q	
<u>queue</u>	queueing policy
<u>Queue</u>	
R	
raise	recursive definition, [1]
random numbers	redundancy
range	refactor
<u>range</u>	<u>relactor</u>

range function, [1]	<u>refactoring code</u>
reassignment, [1]	return statement, [1]
<u>rectangle</u>	<u>return value, [1]</u>
recursion, [1]	<u>root</u>
infinite	rules of precedence, [1]
recursive call, [1]	runtime error, [1], [2], [3]
recursive data structure	
S	
<u>safe language</u>	<u>state</u>
scaffolding, [1], [2]	state snapshot, [1]
scalar multiplication	statement, [1]
scope	<u>assignment</u>
<u>builtin</u>	<u>continue</u>
global	del, [1]
<u>local</u>	if
script	import, [1]
semantic error, [1]	pass
semantics, [1]	<u>return</u>
<u>sequence</u> , [1], [2]	statement block
shallow copy	statement: break
shallow equality, [1]	step size
short-circuit evaluation, [1]	str, [1]
shuffle	string
siblings	string comparison
side effect, [1]	(>, <, >=, <=, !=)
single-step	string formatting
singleton	string module
slice, [1], [2]	string operations
slicing ([:])	string slice
socket	strings and lists
source code	style
<u>split</u>	<u>subexpression</u>
<u>sprite</u>	sublist, [1]
stack diagram	subscript operator
	<u>substring</u>
	surface, [1]
	syntax, [1]
	syntax error, [1]
Т	
<u>tab</u> , [1]	<u>traverse</u>
table	trichotomy
temporary variable, [1]	triple quoted string
terminating condition	truncation
test suite	try except
Test-driven development	try except finally
	,,

test-driven development (TDD) <u>tuple</u>, [1] text file, [1] assignment token, [1], [2] return value tuple assignment <u>trace</u> <u>traceback</u> turtle module tracing a program two-dimensional table traversal, [1] type conversion type conversion, [1] type converter functions U underscore character unit tests unit testing unreachable code V value, [1], [2], [3] <u>veneer</u> <u>boolean</u> volatile memory variable, [1] local, [1] temporary variable name W while loop <u>wrapper</u> while statement wrapping code in a function, [1] <u>whitespace</u>

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Foreword

By David Beazley

As an educator, researcher, and book author, I am delighted to see the completion of this book. Python is a fun and extremely easy-to-use programming language that has steadily gained in popularity over the last few years. Developed over ten years ago by Guido van Rossum, Python's simple syntax and overall feel is largely derived from ABC, a teaching language that was developed in the 1980's. However, Python was also created to solve real problems and it borrows a wide variety of features from programming languages such as C++, Java, Modula-3, and Scheme. Because of this, one of Python's most remarkable features is its broad appeal to professional software developers, scientists, researchers, artists, and educators.

Despite Python's appeal to many different communities, you may still wonder why Python? or why teach programming with Python? Answering these questions is no simple task—especially when popular opinion is on the side of more masochistic alternatives such as C++ and Java. However, I think the most direct answer is that programming in Python is simply a lot of fun and more productive.

When I teach computer science courses, I want to cover important concepts in addition to making the material interesting and engaging to students. Unfortunately, there is a tendency for introductory programming courses to focus far too much attention on mathematical abstraction and for students to become frustrated with annoying problems related to low-level details of syntax, compilation, and the enforcement of seemingly arcane rules. Although such abstraction and formalism is important to professional software engineers and students who plan to continue their study of computer science, taking such an approach in an introductory course mostly succeeds in making computer science boring. When I teach a course, I don't want to have a room of uninspired students. I would much rather see them trying to solve interesting problems by exploring different ideas, taking unconventional approaches, breaking the rules, and learning from their mistakes. In doing so, I don't want to waste half of the semester trying to sort out obscure syntax problems, unintelligible compiler error messages, or the several hundred ways that a program might generate a general protection fault.

One of the reasons why I like Python is that it provides a really nice balance between the practical and the conceptual. Since Python is interpreted, beginners can pick up the language and start doing neat things almost immediately without getting lost in the problems of compilation and linking. Furthermore, Python comes with a large library of modules that can be used to do all sorts of tasks ranging from web-programming to graphics. Having such a practical focus is a great way to engage students and it allows them to complete significant projects. However, Python can also serve as an excellent foundation for introducing important computer science concepts. Since Python fully supports procedures and classes, students can be gradually introduced to topics such as procedural abstraction, data structures, and object-oriented programming — all of which are applicable to later courses on Java or C++. Python even borrows a number of features from functional programming languages and can be used to introduce concepts that would be covered in more detail in courses on Scheme and Lisp.

In reading Jeffrey's preface, I am struck by his comments that Python allowed him to see a higher level of success and a lower level of frustration and that he was able to move faster with better results.

Although these comments refer to his introductory course, I sometimes use Python for these exact same reasons in advanced graduate level computer science courses at the University of Chicago. In these courses, I am constantly faced with the daunting task of covering a lot of difficult course material in a blistering nine week quarter. Although it is certainly possible for me to inflict a lot of pain and suffering by using a language like C++, I have often found this approach to be counterproductive—especially when the course is about a topic unrelated to just programming. I find that using Python allows me to better focus on the actual topic at hand while allowing students to complete substantial class projects.

Although Python is still a young and evolving language, I believe that it has a bright future in education. This book is an important step in that direction. David Beazley University of Chicago Author of the *Python Essential Reference*

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Preface

By Jeffrey Elkner

This book owes its existence to the collaboration made possible by the Internet and the free software movement. Its three authors—a college professor, a high school teacher, and a professional programmer—never met face to face to work on it, but we have been able to collaborate closely, aided by many other folks who have taken the time and energy to send us their feedback.

We think this book is a testament to the benefits and future possibilities of this kind of collaboration, the framework for which has been put in place by Richard Stallman and the Free Software Foundation.

How and why I came to use Python

In 1999, the College Board's Advanced Placement (AP) Computer Science exam was given in C++ for the first time. As in many high schools throughout the country, the decision to change languages had a direct impact on the computer science curriculum at Yorktown High School in Arlington, Virginia, where I teach. Up to this point, Pascal was the language of instruction in both our first-year and AP courses. In keeping with past practice of giving students two years of exposure to the same language, we made the decision to switch to C++ in the first year course for the 1997-98 school year so that we would be in step with the College Board's change for the AP course the following year.

Two years later, I was convinced that C++ was a poor choice to use for introducing students to computer science. While it is certainly a very powerful programming language, it is also an extremely difficult language to learn and teach. I found myself constantly fighting with C++'s difficult syntax and multiple ways of doing things, and I was losing many students unnecessarily as a result. Convinced there had to be a better language choice for our first-year class, I went looking for an alternative to C++.

I needed a language that would run on the machines in our GNU/Linux lab as well as on the Windows and Macintosh platforms most students have at home. I wanted it to be free software, so that students could use it at home regardless of their income. I wanted a language that was used by professional programmers, and one that had an active developer community around it. It had to support both procedural and object-oriented programming. And most importantly, it had to be easy to learn and teach. When I investigated the choices with these goals in mind, Python stood out as the best candidate for the job.

I asked one of Yorktown's talented students, Matt Ahrens, to give Python a try. In two months he not only learned the language but wrote an application called pyTicket that enabled our staff to report technology problems via the Web. I knew that Matt could not have finished an application of that scale in so short a time in C++, and this accomplishment, combined with Matt's positive assessment of Python, suggested that Python was the solution I was looking for.

Finding a textbook

Having decided to use Python in both of my introductory computer science classes the following year, the most pressing problem was the lack of an available textbook.

Free documents came to the rescue. Earlier in the year, Richard Stallman had introduced me to Allen

Downey. Both of us had written to Richard expressing an interest in developing free educational materials. Allen had already written a first-year computer science textbook, *How to Think Like a Computer Scientist*. When I read this book, I knew immediately that I wanted to use it in my class. It was the clearest and most helpful computer science text I had seen. It emphasized the processes of thought involved in programming rather than the features of a particular language. Reading it immediately made me a better teacher.

How to Think Like a Computer Scientist was not just an excellent book, but it had been released under the GNU public license, which meant it could be used freely and modified to meet the needs of its user. Once I decided to use Python, it occurred to me that I could translate Allen's original Java version of the book into the new language. While I would not have been able to write a textbook on my own, having Allen's book to work from made it possible for me to do so, at the same time demonstrating that the cooperative development model used so well in software could also work for educational materials.

Working on this book for the last two years has been rewarding for both my students and me, and my students played a big part in the process. Since I could make instant changes whenever someone found a spelling error or difficult passage, I encouraged them to look for mistakes in the book by giving them a bonus point each time they made a suggestion that resulted in a change in the text. This had the double benefit of encouraging them to read the text more carefully and of getting the text thoroughly reviewed by its most important critics, students using it to learn computer science.

For the second half of the book on object-oriented programming, I knew that someone with more real programming experience than I had would be needed to do it right. The book sat in an unfinished state for the better part of a year until the open source community once again provided the needed means for its completion.

I received an email from Chris Meyers expressing interest in the book. Chris is a professional programmer who started teaching a programming course last year using Python at Lane Community College in Eugene, Oregon. The prospect of teaching the course had led Chris to the book, and he started helping out with it immediately. By the end of the school year he had created a companion project on our Website at http://openbookproject.net called *Python for Fun* and was working with some of my most advanced students as a master teacher, guiding them beyond where I could take them.

Introducing programming with Python

The process of translating and using *How to Think Like a Computer Scientist* for the past two years has confirmed Python's suitability for teaching beginning students. Python greatly simplifies programming examples and makes important programming ideas easier to teach.

The first example from the text illustrates this point. It is the traditional hello, world program, which in the Java version of the book looks like this:

```
class Hello {
  public static void main (String[] args) {
    System.out.println ("Hello, world.");
  }
}
```

in the Python version it becomes:

print("Hello, World!")

Even though this is a trivial example, the advantages of Python stand out. Yorktown's Computer Science I course has no prerequisites, so many of the students seeing this example are looking at their first program. Some of them are undoubtedly a little nervous, having heard that computer programming is difficult to learn. The Java version has always forced me to choose between two unsatisfying options: either to explain the *class Hello*, *public static void main*, *String[] args*, {, and }, statements and risk confusing or intimidating some of the students right at the start, or to tell them, Just don't worry about all of that stuff now; we will talk about it later, and risk the same thing. The educational objectives at this point in the course are to introduce students to the idea of a programming statement and to get them to write their first program, thereby introducing them to the programming environment. The Python program has exactly what is needed to do these things, and nothing more.

Comparing the explanatory text of the program in each version of the book further illustrates what this means to the beginning student. There are seven paragraphs of explanation of Hello, world! in the Java version; in the Python version, there are only a few sentences. More importantly, the missing six paragraphs do not deal with the big ideas in computer programming but with the minutia of Java syntax. I found this same thing happening throughout the book. Whole paragraphs simply disappear from the Python version of the text because Python's much clearer syntax renders them unnecessary.

Using a very high-level language like Python allows a teacher to postpone talking about low-level details of the machine until students have the background that they need to better make sense of the details. It thus creates the ability to put first things first pedagogically. One of the best examples of this is the way in which Python handles variables. In Java a variable is a name for a place that holds a value if it is a built-in type, and a reference to an object if it is not. Explaining this distinction requires a discussion of how the computer stores data. Thus, the idea of a variable is bound up with the hardware of the machine. The powerful and fundamental concept of a variable is already difficult enough for beginning students (in both computer science and algebra). Bytes and addresses do not help the matter. In Python a variable is a name that refers to a thing. This is a far more intuitive concept for beginning students and is much closer to the meaning of variable that they learned in their math courses. I had much less difficulty teaching variables this year than I did in the past, and I spent less time helping students with problems using them.

Another example of how Python aids in the teaching and learning of programming is in its syntax for functions. My students have always had a great deal of difficulty understanding functions. The main problem centers around the difference between a function definition and a function call, and the related distinction between a parameter and an argument. Python comes to the rescue with syntax that is nothing short of beautiful. Function definitions begin with the keyword def, so I simply tell my students, When you define a function, begin with def, followed by the name of the function that you are defining; when you call a function, simply call (type) out its name. Parameters go with definitions; arguments go with calls. There are no return types, parameter types, or reference and value parameters to get in the way, so I am now able to teach functions in less than half the time that it previously took me, with better comprehension.

Using Python improved the effectiveness of our computer science program for all students. I saw a higher general level of success and a lower level of frustration than I experienced teaching with either C++ or Java. I moved faster with better results. More students left the course with the ability to create meaningful programs and with the positive attitude toward the experience of programming that this engenders.

Building a community

I have received email from all over the globe from people using this book to learn or to teach programming. A user community has begun to emerge, and many people have been contributing to the project by sending in materials for the companion Website at http://openbookproject.net/pybiblio.

With the continued growth of Python, I expect the growth in the user community to continue and accelerate. The emergence of this user community and the possibility it suggests for similar collaboration among educators have been the most exciting parts of working on this project for me. By working together, we can increase the quality of materials available for our use and save valuable time. I invite you to join our community and look forward to hearing from you. Please write to me at jeff@elkner.net.

Jeffrey Elkner Governor's Career and Technical Academy in Arlington Arlington, Virginia

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The Rhodes Local Edition (RLE) (Version of October, 2011)

By Peter Wentworth

We switched from Java to Python in our introductory courses in 2010. So far we think the results look positive. More time will tell.

This predecessor to this book was a great starting point for us, especially because of the liberal permission to change things. Having our own in-house course notes or handouts allows us to adapt and stay fresh, rearrange, see what works, and it gives us agility. We can also ensure that every student in the course gets a copy of the handouts — something that doesn't always happen if we prescribe costly textbooks.

Many thanks to all the contributors and the authors for making their hard work available to the Python community and to our students.

A colleague and friend, Peter Warren, once made the remark that learning introductory programming is as much about the environment as it is about the programming language.

I'm a big fan of IDEs (Integrated Development Environments). I want help to be integrated into my editor, as a first-class citizen, available at the press of a button. I want syntax highlighting. I want immediate syntax checking, and sensible autocompletion.

I'm especially keen on having a single-stepping debugger and breakpoints with code inspection built in. We're trying to build a conceptual model of program execution in the student's mind, so I find most helpful for teaching to have the call stack and variables explicitly visible, and to be able to immediately inspect the result of executing a statement.

My philosophy, then, is not to look for a language to teach, but to look for a combination of IDE and language that are packaged together, and evaluated as a whole.

I've made some quite deep changes to the original book to reflect this (and various other opinionated views that I hold), and I have no doubt that more changes will follow as we bed down our course.

Here are some of the key things I've approached differently:

- Our local situation demands that we have a large number of service course students in an introductory course of just 3 or 4 weeks, and then we get another semester of teaching with those going into our mainstream program. So the book is in two parts: we'll do the first five chapters in the big "get your toes wet" course, and the rest of the material in a separate semester.
- We're using Python 3. It is cleaner, more object oriented, and has fewer ad-hoc irregularities than earlier versions of Python.
- We're using PyScripter as our IDE, on Windows. And it is hardwired into parts of these notes, with screenshots, etc.
- I've dropped GASP.
- For graphics we start with the Turtle module. As things move along, we use PyGame for more

advanced graphics.

- I've introduced some event-driven programming using the turtle.
- I have tried to push more object-oriented notions earlier, without asking students to synthesize objects or write their own classes. So, for example, in the chapter about the turtle, we create multiple instances of turtles, talk about their attributes and state (colour, position, etc), and favour method-call style to move them around, i.e. tess.forward(100)). Similarly, when we use random numbers, we avoid the "hidden singleton generator" in the random module we rather create an instance of a generator, and invoke methods on the instance.
- The ease of constructing lists and the <u>for</u> loop seem to be winners in Python, so rather than use the traditional command-line <u>input</u> for data, I've favoured using loops and lists right up front, like this:

```
friends = ["Amy", "Joe", "Bill"]
for f in friends:
    invitation = "Hi " + f + ". Please come to my party on Saturday!"
    print(invitation)
```

This also means that I bumped range up for early exposure. I envisage that over time we'll see more opportunities to exploit "early lists, early iteration" in its most simple form.

• I dumped doctest: it is a bit too quirky for my liking. For example, it fails a test if the spacing between list elements is not precisely the same as the output string, or if Python prints a string with single quotes, but you wrote up the test case with double quotes. Cases like this also confused students (and instructors) quite badly:

```
def addlist(xs):
    """
    >>> xs = [2,3,4]
    >>> addList(xs)
    9
    """
    return
```

If you can explain the difference in scope rules and lifetimes between the parameter xs and the doctest variable xs elegantly, please let me know. Yes, I know doctest creates its own scope behind our back, but it is exactly this black magic that we're trying to avoid. From the usual indentation rules, also looks like the doctests are nested inside the function scope, but they are not. Students thought that the parameter had been given its value by the assignment to xs in the doctest!

I also think that keeping the test suite separate from the functions under test leads to a cleaner relationship between caller and callee, and gives a better chance of getting argument passing / parameter concepts taught accurately.

There is a good unit testing module in Python, (and PyScripter offers integrated support for it, and automated generation of skeleton test modules), but it looked too advanced for beginners, because it requires multi-module concepts.

So I've favoured my own test scaffolding in Chapter 6 (about 10 lines of code) that the students must insert into whatever file they're working on.

- I've played down command-line input / process / output where possible. Many of our students have never seen a command-line shell, and it is arguably quite intimidating.
- We've gone back to a more "classic / static" approach to writing our own classes and objects. Python (in company with languages like Javascript, Ruby, Perl, PHP, etc.) don't really emphasize notions of "sealed" classes or "private" members, or even "sealed instances".

So one teaching approach is to allocate each instance as an empty container, and subsequently allow the external clients of the class to poke new members (methods or attributes) into different instances as they wish to. It is a very dynamic approach, but perhaps not one that encourages thinking in abstractions, layers, contracts, decoupling, etc. It might even be the kind of thing that one could write one of those "x,y,z ... considered harmful" papers about.

In our more conservative approach, we put an initializer into every class, we determine at object instantiation time what members we want, and we initialize the instances from within the class. So we've moved closer in philosophy to C# / Java on this one.

- We're moving towards introducing more algorithms earlier into the course. Python is an efficient teaching language we can make fast progress. But the gains we make there we'd like to invest into deeper problem solving, and more complex algorithms with the basics, rather than cover "more Python features". Some of these changes have started to find their way in this version, and I'm sure we'll see more in future.
- We're interested in issues around teaching and learning. Some research indicates that "intellectual playfulness" is important. The study referenced in the Odds-and-ends workbook at the end just didn't seem to have anywhere sensible to go in the book, yet I wanted it included. It is quite likely that we'll allow more issues like this to creep into the book, to try to make it more than just about programming in Python.

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Contributor List

To paraphrase the philosophy of the Free Software Foundation, this book is free like free speech, but not necessarily free like free pizza. It came about because of a collaboration that would not have been possible without the GNU Free Documentation License. So we would like to thank the Free Software Foundation for developing this license and, of course, making it available to us.

We would also like to thank the more than 100 sharp-eyed and thoughtful readers who have sent us suggestions and corrections over the past few years. In the spirit of free software, we decided to express our gratitude in the form of a contributor list. Unfortunately, this list is not complete, but we are doing our best to keep it up to date. It was also getting too large to include everyone who sends in a typo or two. You have our gratitude, and you have the personal satisfaction of making a book you found useful better for you and everyone else who uses it. New additions to the list for the 2nd edition will be those who have made on-going contributions.

If you have a chance to look through the list, you should realize that each person here has spared you and all subsequent readers from the confusion of a technical error or a less-than-transparent explanation, just by sending us a note.

Impossible as it may seem after so many corrections, there may still be errors in this book. If you should stumble across one, we hope you will take a minute to contact us. The email address is jeff@elkner.net. Substantial changes made due to your suggestions will add you to the next version of the contributor list (unless you ask to be omitted). Thank you!

Second Edition

- An email from Mike MacHenry set me straight on tail recursion. He not only pointed out an error in the presentation, but suggested how to correct it.
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First Edition

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1. The way of the program

The goal of this book is to teach you to think like a computer scientist. This way of thinking combines some of the best features of mathematics, engineering, and natural science. Like mathematicians, computer scientists use formal languages to denote ideas (specifically computations). Like engineers, they design things, assembling components into systems and evaluating tradeoffs among alternatives. Like scientists, they observe the behavior of complex systems, form hypotheses, and test predictions.

The single most important skill for a computer scientist is problem solving. Problem solving means the ability to formulate problems, think creatively about solutions, and express a solution clearly and accurately. As it turns out, the process of learning to program is an excellent opportunity to practice problem-solving skills. That's why this chapter is called, The way of the program.

On one level, you will be learning to program, a useful skill by itself. On another level, you will use programming as a means to an end. As we go along, that end will become clearer.

1.1. The Python programming language

The programming language you will be learning is Python. Python is an example of a high-level language; other high-level languages you might have heard of are C++, PHP, and Java.

As you might infer from the name high-level language, there are also low-level languages, sometimes referred to as machine languages or assembly languages. Loosely speaking, computers can only execute programs written in low-level languages. Thus, programs written in a high-level language have to be processed before they can run. This extra processing takes some time, which is a small disadvantage of high-level languages.

But the advantages are enormous. First, it is much easier to program in a high-level language. Programs written in a high-level language take less time to write, they are shorter and easier to read, and they are more likely to be correct. Second, high-level languages are portable, meaning that they can run on different kinds of computers with few or no modifications. Low-level programs can run on only one kind of computer and have to be rewritten to run on another.

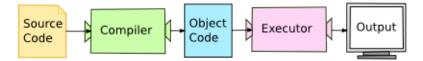
Due to these advantages, almost all programs are written in high-level languages. Low-level languages are used only for a few specialized applications.

Two kinds of programs process high-level languages into low-level languages: interpreters and compilers. An interpreter reads a high-level program and executes it, meaning that it does what the program says. It processes the program a little at a time, alternately reading lines and performing computations.



A compiler reads the program and translates it completely before the program starts running. In this

case, the high-level program is called the source code, and the translated program is called the object code or the executable. Once a program is compiled, you can execute it repeatedly without further translation.



Many modern languages use both processes. They are first compiled into a lower level language, called bytecode, and then interpreted by a program called a virtual machine. Python uses both processes, but because of the way programmers interact with it, it is usually considered an interpreted language.

There are two ways to use the Python interpreter: *immediate mode* and *script mode*. In immediate mode, you type Python expressions into the Python Interpreter window, and the interpreter immediately shows the result:

```
Python Interpreter

*** Python 3.1.2 (r312:79149, Mar 21 2010, 00:41:52) [MSC v.1500 32 bit (Intel)] on win32. ***

>>> 2+2
4
>>> |
```

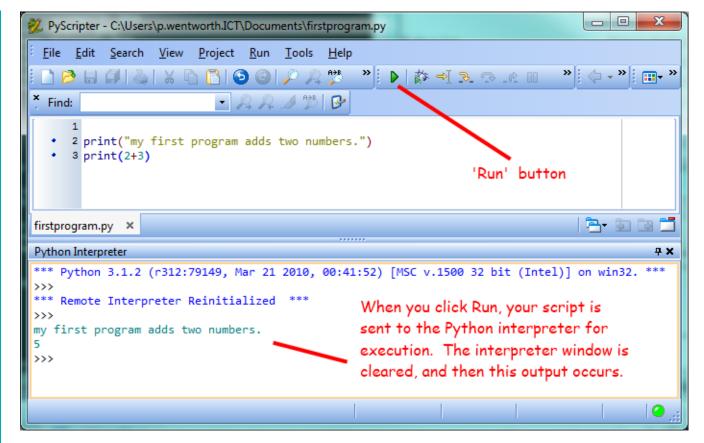
The >>> is called the Python prompt. The interpreter uses the prompt to indicate that it is ready for instructions. We typed 2 + 2, and the interpreter evaluated our expression, and replied 4, and on the next line it gave a new prompt, indicating that it is ready for more input.

Alternatively, you can write a program in a file and use the interpreter to execute the contents of the file. Such a file is called a script.

In this Rhodes Local Edition of the textbook, we use a program development environment called PyScripter. (It is available at http://code.google.com/p/pyscripter.) There are various other development environments. If you're using one of the others, you might be better off working with the authors' original book rather than this edition.

For example, we created a file named firstprogram.py using PyScripter. By convention, files that contain Python programs have names that end with .py

To execute the program, we can click the Run button in PyScripter:



Most programs are more interesting than this one.

Working directly in the interpreter is convenient for testing short bits of code because you get immediate feedback. Think of it as scratch paper used to help you work out problems. Anything longer than a few lines should be put into a script.

1.2. What is a program?

A program is a sequence of instructions that specifies how to perform a computation. The computation might be something mathematical, such as solving a system of equations or finding the roots of a polynomial, but it can also be a symbolic computation, such as searching and replacing text in a document or (strangely enough) compiling a program.

The details look different in different languages, but a few basic instructions appear in just about every language:

input

Get data from the keyboard, a file, or some other device.

output

Display data on the screen or send data to a file or other device.

math

Perform basic mathematical operations like addition and multiplication.

conditional execution

Check for certain conditions and execute the appropriate sequence of statements.

repetition

Perform some action repeatedly, usually with some variation.

Believe it or not, that's pretty much all there is to it. Every program you've ever used, no matter how complicated, is made up of instructions that look more or less like these. Thus, we can describe programming as the process of breaking a large, complex task into smaller and smaller subtasks until the subtasks are simple enough to be performed with sequences of these basic instructions.

That may be a little vague, but we will come back to this topic later when we talk about algorithms.

1.3. What is debugging?

Programming is a complex process, and because it is done by human beings, it often leads to errors. Programming errors are called bugs and the process of tracking them down and correcting them is called debugging. Use of the term *bug* to describe small engineering difficulties dates back to at least 1889, when Thomas Edison had a bug with his phonograph.

Three kinds of errors can occur in a program: <u>syntax errors</u>, <u>runtime errors</u>, and <u>semantic errors</u>. It is useful to distinguish between them in order to track them down more quickly.

1.4. Syntax errors

Python can only execute a program if the program is syntactically correct; otherwise, the process fails and returns an error message. Syntax refers to the structure of a program and the rules about that structure. For example, in English, a sentence must begin with a capital letter and end with a period. this sentence contains a syntax error. So does this one

For most readers, a few syntax errors are not a significant problem, which is why we can read the poetry of e. e. cummings without problems. Python is not so forgiving. If there is a single syntax error anywhere in your program, Python will display an error message and quit, and you will not be able to run your program. During the first few weeks of your programming career, you will probably spend a lot of time tracking down syntax errors. As you gain experience, though, you will make fewer errors and find them faster.

1.5. Runtime errors

The second type of error is a runtime error, so called because the error does not appear until you run the program. These errors are also called exceptions because they usually indicate that something exceptional (and bad) has happened.

Runtime errors are rare in the simple programs you will see in the first few chapters, so it might be a while before you encounter one.

1.6. Semantic errors

The third type of error is the semantic error. If there is a semantic error in your program, it will run successfully, in the sense that the computer will not generate any error messages, but it will not do the right thing. It will do something else. Specifically, it will do what you told it to do.

The problem is that the program you wrote is not the program you wanted to write. The meaning of the program (its semantics) is wrong. Identifying semantic errors can be tricky because it requires you to work backward by looking at the output of the program and trying to figure out what it is doing.

1.7. Experimental debugging

One of the most important skills you will acquire is debugging. Although it can be frustrating, debugging is one of the most intellectually rich, challenging, and interesting parts of programming.

In some ways, debugging is like detective work. You are confronted with clues, and you have to infer the processes and events that led to the results you see.

Debugging is also like an experimental science. Once you have an idea what is going wrong, you modify your program and try again. If your hypothesis was correct, then you can predict the result of the modification, and you take a step closer to a working program. If your hypothesis was wrong, you have to come up with a new one. As Sherlock Holmes pointed out, When you have eliminated the impossible, whatever remains, however improbable, must be the truth. (A. Conan Doyle, *The Sign of Four*)

For some people, programming and debugging are the same thing. That is, programming is the process of gradually debugging a program until it does what you want. The idea is that you should start with a program that does *something* and make small modifications, debugging them as you go, so that you always have a working program.

For example, Linux is an operating system kernel that contains millions of lines of code, but it started out as a simple program Linus Torvalds used to explore the Intel 80386 chip. According to Larry Greenfield, one of Linus's earlier projects was a program that would switch between displaying AAAA and BBBB. This later evolved to Linux (*The Linux Users' Guide* Beta Version 1).

Later chapters will make more suggestions about debugging and other programming practices.

1.8. Formal and natural languages

Natural languages are the languages that people speak, such as English, Spanish, and French. They were not designed by people (although people try to impose some order on them); they evolved naturally.

Formal languages are languages that are designed by people for specific applications. For example, the notation that mathematicians use is a formal language that is particularly good at denoting relationships among numbers and symbols. Chemists use a formal language to represent the chemical structure of molecules. And most importantly:

Programming languages are formal languages that have been designed to express computations.

Formal languages tend to have strict rules about syntax. For example, 3+3=6 is a syntactically correct mathematical statement, but 3=+6 is not. H_2O is a syntactically correct chemical name, but 2Zz is not.

Syntax rules come in two flavors, pertaining to tokens and structure. Tokens are the basic elements of the language, such as words, numbers, and chemical elements. One of the problems with 3=+6\$ is that \$\\$ is not a legal token in mathematics (at least as far as we know). Similarly, $_2$ Zz is not legal because there is no element with the abbreviation $_{Zz}$.

The second type of syntax rule pertains to the structure of a statement— that is, the way the tokens are arranged. The statement 3=+6\$ is structurally illegal because you can't place a plus sign

immediately after an equal sign. Similarly, molecular formulas have to have subscripts after the element name, not before.

When you read a sentence in English or a statement in a formal language, you have to figure out what the structure of the sentence is (although in a natural language you do this subconsciously). This process is called parsing.

For example, when you hear the sentence, "The other shoe fell", you understand that the other shoe is the subject and fell is the verb. Once you have parsed a sentence, you can figure out what it means, or the semantics of the sentence. Assuming that you know what a shoe is and what it means to fall, you will understand the general implication of this sentence.

Although formal and natural languages have many features in common — tokens, structure, syntax, and semantics — there are many differences:

ambiguity

Natural languages are full of ambiguity, which people deal with by using contextual clues and other information. Formal languages are designed to be nearly or completely unambiguous, which means that any statement has exactly one meaning, regardless of context.

redundancy

In order to make up for ambiguity and reduce misunderstandings, natural languages employ lots of redundancy. As a result, they are often verbose. Formal languages are less redundant and more concise.

literalness

Formal languages mean exactly what they say. On the other hand, natural languages are full of idiom and metaphor. If someone says, "The other shoe fell", there is probably no shoe and nothing falling. You'll need to find the original joke to understand the idiomatic meaning of the other shoe falling. *Yahoo! Answers* thinks it knows!

People who grow up speaking a natural language—everyone—often have a hard time adjusting to formal languages. In some ways, the difference between formal and natural language is like the difference between poetry and prose, but more so:

poetry

Words are used for their sounds as well as for their meaning, and the whole poem together creates an effect or emotional response. Ambiguity is not only common but often deliberate.

prose

The literal meaning of words is more important, and the structure contributes more meaning. Prose is more amenable to analysis than poetry but still often ambiguous.

program

The meaning of a computer program is unambiguous and literal, and can be understood entirely by analysis of the tokens and structure.

Here are some suggestions for reading programs (and other formal languages). First, remember that formal languages are much more dense than natural languages, so it takes longer to read them. Also, the structure is very important, so it is usually not a good idea to read from top to bottom, left to right. Instead, learn to parse the program in your head, identifying the tokens and interpreting the structure. Finally, the details matter. Little things like spelling errors and bad punctuation, which you

can get away with in natural languages, can make a big difference in a formal language.

1.9. The first program

Traditionally, the first program written in a new language is called *Hello, World!* because all it does is display the words, Hello, World! In Python, the script looks like this: (For scripts, we'll show line numbers to the left of the Python statements.)

```
print("Hello, World!")
```

This is an example of using the print function, which doesn't actually print anything on paper. It displays a value on the screen. In this case, the result shown is

```
Hello, World!
```

The quotation marks in the program mark the beginning and end of the value; they don't appear in the result.

Some people judge the quality of a programming language by the simplicity of the Hello, World! program. By this standard, Python does about as well as possible.

1.10. Comments

As programs get bigger and more complicated, they get more difficult to read. Formal languages are dense, and it is often difficult to look at a piece of code and figure out what it is doing, or why.

For this reason, it is a good idea to add notes to your programs to explain in natural language what the program is doing.

A comment in a computer program is text that is intended only for the human reader – it is completely ignored by the interpreter.

In Python, the # token starts a comment. The rest of the line is ignored. Here is a new version of *Hello, World!*.

You'll also notice that we've left a blank line in the program. Blank lines are also ignored by the interpreter, but comments and blank lines can make your programs much easier for humans to parse. Use them liberally!

1.11. Glossary

algorithm

A general process for solving a category of problems.

bug

An error in a program.

bytecode

An intermediate language between source code and object code. Many modern languages first compile source code into bytecode and then interpret the bytecode with a program called a *virtual machine*.

comment

Information in a program that is meant for other programmers (or anyone reading the source code) and has no effect on the execution of the program.

compile

To translate a program written in a high-level language into a low-level language all at once, in preparation for later execution.

debugging

The process of finding and removing any of the three kinds of programming errors.

exception

Another name for a runtime error.

executable

Another name for object code that is ready to be executed.

formal language

Any one of the languages that people have designed for specific purposes, such as representing mathematical ideas or computer programs; all programming languages are formal languages.

high-level language

A programming language like Python that is designed to be easy for humans to read and write.

immediate mode

A style of using Python where we type expressions at the command prompt, and the results are shown immediately. Contrast with script, and see the entry under Python shell.

interpret

To execute a program in a high-level language by translating it one line at a time.

low-level language

A programming language that is designed to be easy for a computer to execute; also called machine language or assembly language.

natural language

Any one of the languages that people speak that evolved naturally.

object code

The output of the compiler after it translates the program.

parse

To examine a program and analyze the syntactic structure.

portability

A property of a program that can run on more than one kind of computer.

print function

A function used in a program or script that causes the Python interpreter to display a value on its output device.

problem solving

The process of formulating a problem, finding a solution, and expressing the solution.

program

a sequence of instructions that specifies to a computer actions and computations to be performed.

Python shell

An interactive user interface to the Python interpreter. The user of a Python shell types commands at the prompt (>>>), and presses the return key to send these commands immediately to the interpreter for processing. The word *shell* comes from Unix. In the PyScripter used in this RLE version of the book, the Interpreter Window is where we'd do the immediate mode interaction.

runtime error

An error that does not occur until the program has started to execute but that prevents the program from continuing.

script

A program stored in a file (usually one that will be interpreted).

semantic error

An error in a program that makes it do something other than what the programmer intended.

semantics

The meaning of a program.

source code

A program in a high-level language before being compiled.

syntax

The structure of a program.

syntax error

An error in a program that makes it impossible to parse — and therefore impossible to interpret.

token

One of the basic elements of the syntactic structure of a program, analogous to a word in a natural language.

1.12. Exercises

- 1. Write an English sentence with understandable semantics but incorrect syntax. Write another English sentence which has correct syntax but has semantic errors.
- 2. Using the Python interpreter, type 1 + 2 and then hit return. Python evaluates this expression,

displays the result, and then shows another prompt. $\underline{*}$ is the *multiplication operator*, and $\underline{**}$ is the *exponentiation operator*. Experiment by entering different expressions and recording what is displayed by the Python interpreter.

3. Type 1 2 and then hit return. Python tries to evaluate the expression, but it can't because the expression is not syntactically legal. Instead, it shows the error message:

```
File "<interactive input>", line 1
1 2
^
SyntaxError: invalid syntax
```

In many cases, Python indicates where the syntax error occurred, but it is not always right, and it doesn't give you much information about what is wrong.

So, for the most part, the burden is on you to learn the syntax rules.

In this case, Python is complaining because there is no operator between the numbers.

See if you can find a few more examples of things that will produce error messages when you enter them at the Python prompt. Write down what you enter at the prompt and the last line of the error message that Python reports back to you.

- 4. Type print('hello'). Python executes this, which has the effect of printing the letters h-e-l-l-o. Notice that the quotation marks that you used to enclose the string are not part of the output. Now type "hello" and describe your result. Make notes of when you see the quotation marks and when you don't.
- 5. Type cheese without the quotation marks. The output will look something like this:

```
Traceback (most recent call last):
   File "<interactive input>", line 1, in ?
NameError: name 'cheese' is not defined
```

This is a run-time error; specifically, it is a NameError, and even more specifically, it is an error because the name *cheese* is not defined. If you don't know what that means yet, you will soon.

6. Type 6 + 4 * 9 at the Python prompt and hit enter. Record what happens.

Now create a python script with the following contents:

```
1 6 + 4 * 9
```

What happens when you run this script? Now change the script contents to:

```
1 print(6 + 4 * 9)
```

and run it again.

What happened this time?

Whenever an *expression* is typed at the Python prompt, it is evaluated and the result is *automatically* shown on the line below. (Like on your calculator, if you type this expression you'll get the result 42.)

A script is different, however. Evaluations of expressions are not automatically displayed, so it is necessary to use the print function to make the answer show up.

It is hardly ever necessary to use the print function in immediate mode / at the command prompt.

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2. Variables, expressions and statements

2.1. Values and data types

A value is one of the fundamental things — like a letter or a number — that a program manipulates. The values we have seen so far are $\frac{1}{2}$ (the result when we added $\frac{1}{2}$ + $\frac{1}{2}$), and "Hello, World!".

These values are classified into different classes, or data types: 4 is an *integer*, and "Hello, World!" is a *string*, so-called because it contains a string of letters. You (and the interpreter) can identify strings because they are enclosed in quotation marks.

If you are not sure what class a value falls into, Python has a function called type which can tell you.

```
>>> type("Hello, World!")
<class 'str'>
>>> type(17)
<class 'int'>
```

Not surprisingly, strings belong to the class str and integers belong to the class int. Less obviously, numbers with a decimal point belong to a class called float, because these numbers are represented in a format called *floating-point*. At this stage, you can treat the words *class* and *type* interchangeably. We'll come back to a deeper understanding of what a class is in later chapters.

```
>>> type(3.2)
<class 'float'>
```

What about values like "17" and "3.2"? They look like numbers, but they are in quotation marks like strings.

```
>>> type("17")
<class 'str'>
>>> type("3.2")
<class 'str'>
```

They're strings!

Strings in Python can be enclosed in either single quotes (') or double quotes ("), or three of each (''' or """)

```
>>> type('This is a string.')
<class 'str'>
>>> type("And so is this.")
<class 'str'>
>>> type("""and this.""")
<class 'str'>
>>> type('''and even this...''')
<class 'str'>
```

Double quoted strings can contain single quotes inside them, as in "Bruce's beard", and single quoted strings can have double quotes inside them, as in 'The knights who say "Ni!"'.

Strings enclosed with three occurrences of either quote symbol are called triple quoted strings. They can contain either single or double quotes:

```
>>> print('''"Oh no", she exclaimed, "Ben's bike is broken!"''')
"Oh no", she exclaimed, "Ben's bike is broken!"
>>>
```

Triple quoted strings can even span multiple lines:

```
>>> message = """This message will
... span several
... lines."""
>>> print(message)
This message will
span several
lines.
>>>
```

Python doesn't care whether you use single or double quotes or the three-of-a-kind quotes to surround your strings: once it has parsed the text of your program or command, the way it stores the value is identical in all cases, and the surrounding quotes are not part of the value. But when the interpreter wants to display a string, it has to decide which quotes to use to make it look like a string.

```
>>> 'This is a string.'
'This is a string.'
>>> """And so is this."""
'And so is this.'
```

So the Python language designers usually chose to surround their strings by single quotes. What do think would happen if the string already contained single quotes?

When you type a large integer, you might be tempted to use commas between groups of three digits, as in 42,000. This is not a legal integer in Python, but it does mean something else, which is legal:

```
>>> 42000
42000
>>> 42,000
(42,0)
```

Well, that's not what we expected at all! Because of the comma, Python chose to treat this as a *pair* of values. We'll come back to learn about pairs later. But, for the moment, remember not to put commas or spaces in your integers, no matter how big they are. Also revisit what we said in the previous chapter: formal languages are strict, the notation is concise, and even the smallest change might mean something quite different from what you intended.

2.2. Variables

One of the most powerful features of a programming language is the ability to manipulate variables. A variable is a name that refers to a value.

The assignment statement creates new variables and gives them values:

```
>>> message = "What's up, Doc?"
>>> n = 17
>>> pi = 3.14159
```

This example makes three assignments. The first assigns the string value "What's up, Doc?" to a new variable named message. The second gives the integer 17 to n, and the third assigns the floating-point number 3.14159 to a variable called pi.

The assignment token, $\frac{1}{2}$, should not be confused with *equals*, which uses the token ==. The assignment statement links a *name*, on the left hand side of the operator, with a *value*, on the right hand side. This is why you will get an error if you enter:

```
Tip

When reading or writing code, say to yourself "n is assigned 17" or "n gets the value 17".

Don't say "n equals 17".
```

A common way to represent variables on paper is to write the name with an arrow pointing to the variable's value. This kind of figure is called a state snapshot because it shows what state each of the variables is in at a particular instant in time. (Think of it as the variable's state of mind). This diagram shows the result of executing the assignment statements:

```
message → "What's up, Doc?"

n → 17

pi → 3.14159
```

If you ask the interpreter to evaluate a variable, it will produce the value that is currently linked to the variable:

```
>>> message
'What's up, Doc?'
>>> n
17
>>> pi
3.14159
```

In each case the result is the value of the variable. Variables also have types; again, we can ask the interpreter what they are.

```
>>> type(message)
<class 'str'>
>>> type(n)
<class 'int'>
>>> type(pi)
<class 'float'>
```

The type of a variable is the type of the value it currently refers to.

We use variables in a program to "remember" things, like the current score at the football game. But variables are *variable*. This means they can change over time, just like the scoreboard at a football game. You can assign a value to a variable, and later assign a different value to the same variable. (*This is different from maths. In maths, if you give* `x` the value 3, it cannot change to link to a different value half-way through your calculations!)

```
>>> day = "Thursday"
```

```
>>> day
'Thursday'
>>> day = "Friday"
>>> day
'Friday'
>>> day = 21
>>> day
```

You'll notice we changed the value of *day* three times, and on the third assignment we even gave it a value that was of a different type.

A great deal of programming is about having the computer remember things, e.g. *The number of missed calls on your phone*, and then arranging to update or change the variable when you miss another call.

2.3. Variable names and keywords

Variable names can be arbitrarily long. They can contain both letters and digits, but they have to begin with a letter or an underscore. Although it is legal to use uppercase letters, by convention we don't. If you do, remember that case matters. Bruce and bruce are different variables.

The underscore character (_) can appear in a name. It is often used in names with multiple words, such as my_name or price_of_tea_in_china.

There are some situations in which names beginning with an underscore have special meaning, so a safe rule for beginners is to start all names with a letter.

If you give a variable an illegal name, you get a syntax error:

```
>>> 76trombones = "big parade"
SyntaxError: invalid syntax
>>> more$ = 1000000
SyntaxError: invalid syntax
>>> class = "Computer Science 101"
SyntaxError: invalid syntax
```

76trombones is illegal because it does not begin with a letter. more\$ is illegal because it contains an illegal character, the dollar sign. But what's wrong with class?

It turns out that class is one of the Python keywords. Keywords define the language's syntax rules and structure, and they cannot be used as variable names.

Python has thirty-something keywords (and every now and again improvements to Python introduce or eliminate one or two):

and	as	assert	break	class	continue
def	del	elif	else	except	exec
finally	for	from	global	if	import
in	is	lambda	nonlocal	not	or
pass	raise	return	try	while	with
yield	True	False	None		

You might want to keep this list handy. If the interpreter complains about one of your variable names and you don't know why, see if it is on this list.

Programmers generally choose names for their variables that are meaningful to the human readers of the program — they help the programmer document, or remember, what the variable is used for.

Caution

Beginners sometimes confuse "meaningful to the human readers" with "meaningful to the computer". So they'll wrongly think that because they've called some variable average or pi, it will somehow magically calculate an average, or magically know that the variable pi should have a value like 3.14159. No! The computer doesn't understand what you intend the variable to mean.

So you'll find some instructors who deliberately don't choose meaningful names when they teach beginners — not because we don't think it is a good habit, but because we're trying to reinforce the message that you — the programmer — must write the program code to calculate the average, and you must write an assignment statement to give the variable pi the value you want it to have.

2.4. Statements

A statement is an instruction that the Python interpreter can execute. We have only seen the assignment statement so far. Some other kinds of statements that we'll see shortly are while statements, for statements, if statements, and import statements. (There are other kinds too!)

When you type a statement on the command line, Python executes it. Statements don't produce any result.

2.5. Evaluating expressions

An expression is a combination of values, variables, operators, and calls to functions. If you type an expression at the Python prompt, the interpreter evaluates it and displays the result:

```
>>> 1 + 1
2
>>> len("hello")
5
```

In this example len is a built-in Python function that returns the number of characters in a string. We've previously seen the print and the type functions, so this is our third example of a function!

The evaluation of an expression produces a value, which is why expressions can appear on the right hand side of assignment statements. A value all by itself is a simple expression, and so is a variable.

```
>>> 17
17
>>> y = 3.14
>>> x = len("hello")
>>> x
5
>>> y
3.14
```

2.6. Operators and operands

Operators are special tokens that represent computations like addition, multiplication and division.

The values the operator uses are called operands.

The following are all legal Python expressions whose meaning is more or less clear:

```
20+32 hour-1 hour*60+minute minute/60 5**2 (5+9)*(15-7)
```

The tokens \pm , -, and \pm , and the use of parenthesis for grouping, mean in Python what they mean in mathematics. The asterisk (*) is the token for multiplication, and \pm is the token for exponentiation.

```
>>> 2 ** 3
8
>>> 3 ** 2
9
```

When a variable name appears in the place of an operand, it is replaced with its value before the operation is performed.

Addition, subtraction, multiplication, and exponentiation all do what you expect.

Example: so let us convert 645 minutes into hours:

```
>>> minutes = 645
>>> hours = minutes/60
>>> hours
10.75
```

Oops! In Python 3, the division operator / always yields a floating point result. What we might have wanted to know was how many whole hours there are, and how many minutes remain. Python gives us two different flavours of the division operator. The second, called integer division uses the token //. It always truncates its result down to the next smallest integer (to the left on the number line).

```
>>> 7 / 4
1.75
>>> 7 // 4
1
>>> minutes = 645
>>> hours = minutes//60
>>> hours
10
```

Take care that you choose the correct falvour of the division operator. If you're working with expressions where you need floating point values, use the division operator that does the division accurately.

2.7. Type converter functions

Here we'll look at three more Python functions, *int*, *float* and *str*, which will (attempt to) convert their arguments into types *int*, *float* and *str* respectively. We call these type converter functions.

The *int* function can take a floating point number or a string, and turn it into an int. For floating point numbers, it *discards* the decimal portion of the number – a process we call *truncation towards zero* on the number line. Let us see this in action:

```
>>> int(3.14)
3
>>> int(3.9999)  # This doesn't round to the closest int!
```

```
3
>>> int(3.0)
3
>>> int(-3.999)  # Note that the result is closer to zero
-3
>>> int(minutes/60)
10
>>> int("2345")  # parse a string to produce an int
2345
>>> int(17)  # even works if arg is already an int
17
>>> int("23 bottles")
```

```
Traceback (most recent call last):
File "<interactive input>", line 1, in <module>
ValueError: invalid literal for int() with base 10: '23 bottles'
```

The last case shows that a string has to be a syntactically legal number, otherwise you'll get one of those pesky runtime errors.

The type converter *float* can turn an integer, a float, or a syntactically legal string into a float.

```
>>> float(17)
17.0
>>> float("123.45")
123.45
```

The type converter str turns its argument into a string:

```
>>> str(17)
'17'
>>> str(123.45)
'123.45'
```

2.8. Order of operations

When more than one operator appears in an expression, the order of evaluation depends on the rules of precedence. Python follows the same precedence rules for its mathematical operators that mathematics does. The acronym PEMDAS is a useful way to remember the order of operations:

- Parentheses have the highest precedence and can be used to force an expression to evaluate in the order you want. Since expressions in parentheses are evaluated first, 2 * (3-1) is 4, and (1+1)**(5-2) is 8. You can also use parentheses to make an expression easier to read, as in (minute * 100) / 60, even though it doesn't change the result.
- 2. Exponentiation has the next highest precedence, so 2^{**1+1} is 3 and not 4, and 3^{*1**3} is 3 and not 27.
- 3. Multiplication and both Division operators have the same precedence, which is higher than Addition and Subtraction, which also have the same precedence. So 2*3-1 yields 5 rather than 4, and 5-2*2 is 1, not 6.
- 4. Operators with the *same* precedence are evaluated from left-to-right. In algebra we say they are *left-associative*. So in the expression 6-3+2, the subtraction happens first, yielding 3. We then add 2 to get the result 5. If the operations had been evaluated from right to left, the result would have been 6-(3+2), which is 1. (The acronym PEDMAS could mislead you to thinking that

division has higher precedence than multiplication, and addition is done ahead of subtraction – don't be misled. Subtraction and addition are at the same precedence, and the left-to-right rule applies.)

• Due to some historical quirk, an exception to the left-to-right left-associative rule is the exponentiation operator **, so a useful hint is to always use parentheses to force exactly the order you want when exponentiation is involved:

```
>>> 2 ** 3 ** 2  # the right-most ** operator gets done first!
512
>>> (2 ** 3) ** 2  # Use parentheses to force the order you want!
64
```

The immediate mode command prompt of Python is great for exploring and experimenting with expressions like this.

2.9. Operations on strings

In general, you cannot perform mathematical operations on strings, even if the strings look like numbers. The following are illegal (assuming that message has type string):

```
message-1 "Hello"/123 message*"Hello" "15"+2
```

Interestingly, the <u>+</u> operator does work with strings, but for strings, the <u>+</u> operator represents concatenation, not addition. Concatenation means joining the two operands by linking them end-to-end. For example:

```
fruit = "banana"
baked_good = " nut bread"
print(fruit + baked_good)
```

The output of this program is banana nut bread. The space before the word nut is part of the string, and is necessary to produce the space between the concatenated strings.

The * operator also works on strings; it performs repetition. For example, 'Fun'*3 is 'FunFunFun'. One of the operands has to be a string; the other has to be an integer.

On one hand, this interpretation of + and * makes sense by analogy with addition and multiplication. Just as 4*3 is equivalent to 4+4+4, we expect "Fun"*3 to be the same as "Fun"+"Fun"+"Fun", and it is. On the other hand, there is a significant way in which string concatenation and repetition are different from integer addition and multiplication. Can you think of a property that addition and multiplication have that string concatenation and repetition do not?

2.10. Input

There is a built-in function in Python for getting input from the user:

```
n = input("Please enter your name: ")
```

A sample run of this script in PyScripter would pop up a dialog window like this:



The user of the program can enter the name and click OK, and when this happens the text that has been entered is returned from the *input* function, and in this case assigned to the variable n.

Even if you asked the user to enter their age, you would get back a string like "17". It would be your job, as the programmer, to convert that string into a int or a float, using the *int* or *float* converter functions we saw earlier.

2.11. Composition

So far, we have looked at the elements of a program — variables, expressions, statements, and function calls — in isolation, without talking about how to combine them.

One of the most useful features of programming languages is their ability to take small building blocks and compose them into larger chunks.

For example, we know how to get the user to enter some input, we know how to convert the string we get into a float, we know how to write a complex expression, and we know how to print values. Let's put these together in a small four-step program that asks the user to input a value for the radius of a circle, and then computes the area of the circle from the formula

Area =
$$\pi r^2$$

Firstly, we'll do the four steps one at a time:

```
response = input("What is your radius? ")
r = float(response)
area = 3.14159 * r**2
print("The area is ", area)
```

Now let's compose the first two lines into a single line of code, and compose the second two lines into another line of code.

```
r = float( input("What is your radius? ") )
print("The area is ", 3.14159 * r**2)
```

If we really wanted to be tricky, we could write it all in one statement:

```
print("The area is ", 3.14159*float(input("What is your radius?"))**2)
```

Such compact code may not be most understandable for humans, but it does illustrate how we can

compose bigger chunks from our building blocks.

If you're ever in doubt about whether to compose code or fragment it into smaller steps, try to make it as simple as you can for the human to follow. My choice would be the first case above, with four separate steps.

2.12. Glossary

assignment statement

A statement that assigns a value to a name (variable). To the left of the assignment operator, \equiv , is a name. To the right of the assignment token is an expression which is evaluated by the Python interpreter and then assigned to the name. The difference between the left and right hand sides of the assignment statement is often confusing to new programmers. In the following assignment:

$$n = n + 1$$

n plays a very different role on each side of the . On the right it is a *value* and makes up part of the *expression* which will be evaluated by the Python interpreter before assigning it to the name on the left.

assignment token

is Python's assignment token, which should not be confused with the mathematical comparison operator using the same symbol.

comment

Information in a program that is meant for other programmers (or anyone reading the source code) and has no effect on the execution of the program.

composition

The ability to combine simple expressions and statements into compound statements and expressions in order to represent complex computations concisely.

concatenate

To join two strings end-to-end.

data type

A set of values. The type of a value determines how it can be used in expressions. So far, the types you have seen are integers (int), floating-point numbers (float), and strings (str).

evaluate

To simplify an expression by performing the operations in order to yield a single value.

expression

A combination of variables, operators, and values that represents a single result value.

float

A Python data type which stores *floating-point* numbers. Floating-point numbers are stored internally in two parts: a *base* and an *exponent*. When printed in the standard format, they look like decimal numbers. Beware of rounding errors when you use floats, and remember that they are only approximate values.

int

A Python data type that holds positive and negative whole numbers.

integer division

An operation that divides one integer by another and yields an integer. Integer division yields only the whole number of times that the numerator is divisible by the denominator and discards any remainder.

keyword

A reserved word that is used by the compiler to parse program; you cannot use keywords like if, def. and while as variable names.

operand

One of the values on which an operator operates.

operator

A special symbol that represents a simple computation like addition, multiplication, or string concatenation.

rules of precedence

The set of rules governing the order in which expressions involving multiple operators and operands are evaluated.

state snapshot

A graphical representation of a set of variables and the values to which they refer, taken at a particular instant during the program's execution.

statement

An instruction that the Python interpreter can execute. So far we have only seen the assignment statement, but we will soon meet the import statement and the for statement.

str

A Python data type that holds a string of characters.

value

A number or string (or other things to be named later) that can be stored in a variable or computed in an expression.

variable

A name that refers to a value.

variable name

A name given to a variable. Variable names in Python consist of a sequence of letters (a..z, A..Z, and _) and digits (0..9) that begins with a letter. In best programming practice, variable names should be chosen so that they describe their use in the program, making the program *self* documenting.

2.13. Exercises

- 1. Take the sentence: All work and no play makes Jack a dull boy. Store each word in a separate variable, then print out the sentence on one line using print.
- 2. Add parenthesis to the expression 6 * 1 2 to change its value from 4 to -6.

- 3. Place a comment before a line of code that previously worked, and record what happens when you rerun the program.
- 4. Start the Python interpreter and enter bruce + 4 at the prompt. This will give you an error:

```
NameError: name 'bruce' is not defined
```

Assign a value to bruce so that bruce + 4 evaluates to 10.

5. The formula for computing the final amount if one is earning compound interest is given on Wikipedia as

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

Where,

- P = principal amount (initial investment)
- r = annual nominal interest rate (as a decimal)
- n = number of times the interest is compounded per year
- t = number of years

Write a Python program that assigns the principal amount of R10000 to variable p, assign to n the value 12, and assign to r the interest rate of 8%. Then have the program prompt the user for the number of months t that the money will be compounded for. Calculate and print the final amount after t months.

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3. Hello, little turtles!

There are many *modules* in Python that provide very powerful features that we can use in our own programs. Some of these can send email, or fetch web pages. The one we'll look at in this chapter allows us to create turtles and get them to draw shapes and patterns.

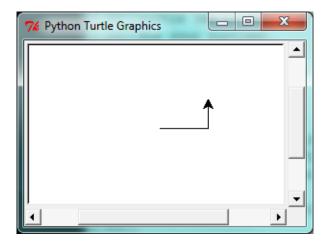
The turtles are fun, but the real purpose of the chapter is to teach ourselves a little more Python, and to develop our theme of computational thinking, or thinking like a computer scientist. Most of the Python covered here will be explored in more depth later.

3.1. Our first turtle program

Let's write a couple of lines of Python program to create a new turtle and start drawing a rectangle. (We'll call the variable that refers to our first turtle alex, but you can choose another name if you follow the naming rules from the previous chapter).

```
import turtle
1
                              # allows us to use turtles
2
    wn = turtle.Screen()
                              # creates a playground for turtles
    alex = turtle.Turtle()
3
                              # create a turtle, assign to alex
4
    alex.forward(50)
5
                              # tell alex to move forward by 50 units
6
    alex.left(90)
                              # tell alex to turn by 90 degrees
7
    alex.forward(30)
                              # complete the second side of a rectangle
8
                              # Wait for user to close window
    wn.mainloop()
```

When we run this program, a new window pops up:



Here are a couple of things you'll need to understand about this program.

The first line tells Python to load a module named turtle. That module brings us two new types that we can use: the Turtle type, and the Screen type. The dot notation turtle. Turtle means "The Turtle type that is defined within the turtle module". (Remember that Python is case sensitive, so the module name, with a lowercase t, is different from the type Turtle.)

We then create and open what it calls a screen (we would perfer to call it a window), which we assign to variable wn. Every window contains a canvas, which is the area inside the window on which we can draw.

In line 3 we create a turtle. The variable *aLex* is made to refer to this turtle. These first three lines set us up, ready for doing some useful things.

In lines 5-7, we instruct the object alex to move, and to turn. We do this by invoking, or activating, alex's methods — these are the instructions that all turtles know how to respond to.

The last line plays a part too: the wn variable refers to the window shown above. When we invoke its mainLoop method, it enters a state where it waits for events (like keypresses, or mouse movement and clicks). The program will terminate when the user closes the window.

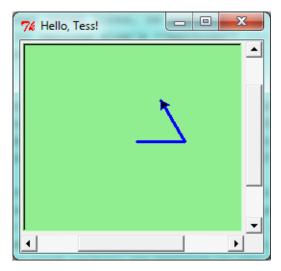
An object can have various methods — things it can do — and it can also have attributes — (sometimes called *properties*). For example, each turtle has a *color* attribute. The method invocation <code>alex.color("red")</code> will make alex red, and drawing will be red too. (Note the word *color* is spelled the American way!)

The colour of the turtle, the width of its pen, the position of the turtle within the window, which way it is facing, and so on are all part of its current state. Similarly, the window object has a background colour, and some text in the title bar, and a size and position on the screen. These are all part of the state of the window object.

Quite a number of methods exist that allow us to modify the turtle and the window objects. We'll just show a couple. In this program we've only commented those lines that are different from the previous example (and we've used a different variable name for this turtle):

```
1
      import turtle
2
      wn = turtle.Screen()
3
      wn.bgcolor("lightgreen")
                                      # set the window background colour
      wn.bgcolor("lightgreen") # set the window backgr
wn.title("Hello, Tess!") # set the window title
4
5
      tess = turtle.Turtle()
6
      tess.color("blue")
7
                                      # tell tess to change her color
8
                                      # tell tess to set her pen width
      tess.pensize(3)
9
      tess.forward(50)
10
11
      tess.left(120)
12
      tess.forward(50)
13
14
      wn.mainloop()
```

When we run this program, this new window pops up, and will remain on the screen until we close it.



Extend this program ...

- Modify this program so that before it creates the window, it prompts the user to enter the desired background colour. It should store the user's responses in a variable, and modify the colour of the window according to the user's wishes. (Hint: you can find a list of permitted colour names at http://www.tcl.tk/man/tcl8.4/TkCmd/colors.htm. It includes some quite unusual ones, like "peach puff" and "HotPink".)
- 2. Do similar changes to allow the user, at runtime, to set tess' colour.
- 3. Do the same for the width of tess' pen. *Hint:* your dialog with the user will return a string, but tess' pensize method expects its argument to be an int. So you'll need to convert the string to an int before you pass it to pensize.

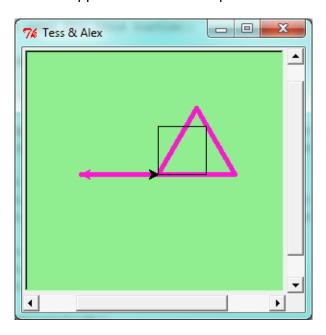
3.2. Instances — a herd of turtles

Just like we can have many different integers in a program, we can have many turtles. Each of them is called an instance. Each instance has its own attributes and methods — so alex might draw with a thin black pen and be at some position, while tess might be going in her own direction with a fat pink pen.

```
import turtle
1
                                   # Set up the window and its attributes
2
      wn = turtle.Screen()
3
     wn.bgcolor("lightgreen")
4
     wn.title("Tess & Alex")
5
6
     tess = turtle.Turtle()
                                   # create tess and set some attributes
     tess.color("hotpink")
7
8
     tess.pensize(5)
9
10
      alex = turtle.Turtle()
                                   # create alex
11
12
                                   # Make tess draw equilateral triangle
     tess.forward(80)
13
      tess.left(120)
14
      tess.forward(80)
15
      tess.left(120)
16
      tess.forward(80)
17
     tess.left(120)
                                   # complete the triangle
18
19
     tess.right(180)
                                   # turn tess around
20
     tess.forward(80)
                                   # and move her away from the origin
21
22
      alex.forward(50)
                                   # make alex draw a square
```

```
alex.left(90)
24
      alex.forward(50)
      alex.left(90)
25
      alex.forward(50)
26
27
      alex.left(90)
28
      alex.forward(50)
29
      alex.left(90)
30
31
      wn.mainloop()
```

Here is what happens when alex completes his rectangle, and tess completes her triangle:



Here are some *How to think like a computer scientist* observations:

- There are 360 degrees in a full circle. If you add up all the turns that a turtle makes, *no matter what steps occurred between the turns*, you can easily figure out if they add up to some multiple of 360. This should convince you that alex is facing in exactly the same direction as he was when he was first created. (Geometry conventions have 0 degrees facing East, and that is the case here too!)
- We could have left out the last turn for alex, but that would not have been as satisfying. If you're asked to draw a closed shape like a square or a rectangle, it is a good idea to complete all the turns and to leave the turtle back where it started, facing the same direction as it started in. This makes reasoning about the program and composing chunks of code into bigger programs easier for us humans!
- We did the same with tess: she drew her triangle, and turned through a full 360 degress. Then we turned her around and moved her aside. Even the blank line 18 is a hint about how the programmer's *mental chunking* is working: in big terms, tess' movements were chunked as "draw the triangle" (lines 12–17) and then "move away from the origin" (lines 19 and 20).
- One of the key uses for comments is to record your mental chunking, and big ideas. They're not always explicit in the code.
- And, uh-huh, two turtles may not be enough for a herd, but you get the idea!

3.3. The for loop

When we drew the square, it was quite tedious. We had to move then turn, move then turn, etc. etc.

four times. If we were drawing a hexagon, or an octogon, or a polygon with 42 sides, it would have been a nightmare.

So a basic building block of all programs is to be able to repeat some code, over and over again.

Python's for loop solves this for us. Let's say we have some friends, and we'd like to send them each an email inviting them to our party. We'll we don't quite know how to send email yet, so for the moment we'll just print a message for each friend:

```
for f in ["Joe", "Amy", "Brad", "Angelina", "Zuki", "Thandi", "Paris"]:
   invite = "Hi " + f + ". Please come to my party on Saturday!"
   print(invite)
# more code can follow here ...
```

When we run this, the output looks like this:

```
Hi Joe. Please come to my party on Saturday!
Hi Amy. Please come to my party on Saturday!
Hi Brad. Please come to my party on Saturday!
Hi Angelina. Please come to my party on Saturday!
Hi Zuki. Please come to my party on Saturday!
Hi Thandi. Please come to my party on Saturday!
Hi Paris. Please come to my party on Saturday!
```

- f in this for statement is called the loop variable. We could have chosen another variable name instead.
- Lines 2 and 3 are the loop body. The loop body is always indented. The indentation determines exactly what statements are "in the body of the loop".
- On each *iteration* or *pass* of the loop, first a check is done to see if there are still more items to be processed. If there are none left (this is called the terminating condition of the loop), the loop has finished. Program execution continues at the next statement after the loop body, (e.g. in this case the next statement below the comment in line 4).
- If there are items still to be processed, the loop variable is updated to refer to the next item in the list. This means, in this case, that the loop body is executed here 7 times, and each time *f* will refer to a different friend.
- At the end of each execution of the body of the loop, Python returns to the for statement, to see if there are more items to be handled, and to assign the next one to f.

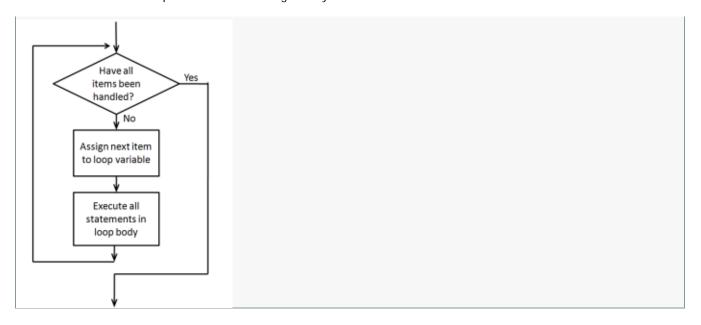
3.4. Flow of Execution of the for loop

As a program executes, the interpreter always keeps track of which statement is about to be executed. We call this the control flow, of the flow of execution of the program. When humans execute programs, they often use their finger to point to each statement in turn. So you could think of control flow as "Python's moving finger".

Control flow until now has been strictly top to bottom, one statement at a time. The <u>for</u> loop changes this.

Flowchart of a for loop

Control flow is often easy to visualize and understand if we draw a flowchart. This shows the exact steps and logic of how the <u>for</u> statement executes.



3.5. The loop simplifies our turtle program

To draw a square we'd like to do the same thing four times — move the turtle, and turn. We previously used 8 lines to have alex draw the four sides of a square. This does exactly the same, but using just three lines:

```
for i in [0,1,2,3]:
alex.forward(50)
alex.left(90)
```

Some observations:

- While "saving some lines of code" might be convenient, it is not the big deal here. What is much more important is that we've found a "repeating pattern" of statements, and reorganized our program to repeat the pattern. Finding the chunks and somehow getting our programs arranged around those chunks is a vital skill in *How to think like a computer scientist*.
- The values [0,1,2,3] were provided to make the loop body execute 4 times. We could have used any four values, but these are the conventional ones to use. In fact, they are so popular that Python gives us special built-in range objects:

```
for i in range(4):
    # Executes the body with i = 0, then 1, then 2, then 3
for x in range(10):
    # sets x to each of ... [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

- Computer scientists like to count from 0!
- range can deliver a sequence of values to the loop variable in the for loop. They start at 0, and in these cases do not include the 4 or the 10.
- Our little trick earlier to make sure that alex did the final turn to complete 360 degrees has paid off: if we had not done that, then we would not have been able to use a loop for the fourth side of the square. It would have become a "special case", different from the other sides. When

possible, we'd much prefer to make our code fit a general pattern, rather than have to create a special case.

So to repeat something four times, a good Python programmer would do this:

```
for i in range(4):
alex.forward(50)
alex.left(90)
```

By now you should be able to see how to change our previous program so that tess can also use a for loop to draw her equilateral triangle.

What would happen if we made this change?

```
for c in ["yellow", "red", "purple", "blue"]:
    alex.color(c)
    alex.forward(50)
    alex.left(90)
```

A variable can also be assigned a value that is a list. So lists can also be used in situations other than the for loop. The code above could be rewritten like this:

```
# Assign a list to a variable
clrs = ["yellow", "red", "purple", "blue"]
for c in clrs:
    alex.color(c)
    alex.forward(50)
    alex.left(90)
```

3.6. A few more turtle methods and tricks

Turtle methods can use negative angles or distances. So tess.foward(-100) will move tess backwards, and tess.left(-30) turns her to the right. Additionally, because there are 360 degrees in a circle, turning 30 to the left will get you facing in the same direction as turning 330 to the right! (The on-screen animation will differ, though — you will be able to tell if tess is turning clockwise or counter-clockwise!)

This suggests that we don't need both a left and a right turn method — we could be minimalists, and just have one method. There is also a *backward* method. (If you are very nerdy, you might enjoy saying alex.backward(-100) to move alex forward!)

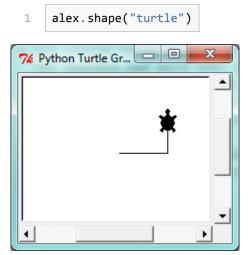
Part of *thinking like a scientist* is to understand more of the structure and rich relationships in your field. So revising a few basic facts about geometry and number lines, like we're done here is a good start if we're going to play with turtles.

A turtle's pen can be picked up or put down. This allows us to move a turtle to a different place without drawing a line. The methods are

```
alex.penup()
alex.forward(100) # this moves alex, but no line is drawn
```

```
3 alex.pendown()
```

Every turtle can have its own shape. The ones available "out of the box" are arrow, blank, circle, classic, square, triangle, turtle.



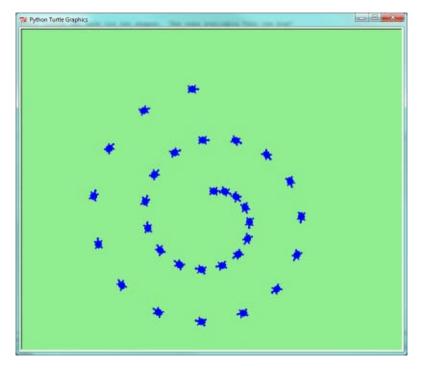
You can speed up or slow down the turtle's animation speed. (Animation controls how quickly the turtle turns and moves forward). Speed settings can be set between 1 (slowest) to 10 (fastest). But if you set the speed to 0, it has a special meaning — turn off animation and go as fast as possible.

```
1 alex.speed(10)
```

A turtle can "stamp" its footprint onto the canvas, and this will remain after the turtle has moved somewhere else. Stamping works, even when the pen is up.

Let's do an example that shows off some of these new features:

```
import turtle
1
    wn = turtle.Screen()
    wn.bgcolor("lightgreen")
    tess = turtle.Turtle()
5
    tess.shape("turtle")
    tess.color("blue")
6
7
8
    tess.penup()
                                # this is new
9
    size = 20
10
    for i in range(30):
11
                                # leave an impression on the canvas
       tess.stamp()
12
       size = size + 3
                                # increase the size on every iteration
13
       tess.forward(size)
                               # move tess along
14
       tess.right(24)
                                # and turn her
15
    wn.mainloop()
16
```



Be careful now! How many times was the body of the loop executed? How many turtle images do you see on the screen? All except one of the shapes you see on the screen here are footprints created by stamp. But the program still only has *one* turtle instance — can you figure out which one here is the real tess? (Hint: if you're not sure, write a new line of code after the <u>for</u> loop to change tess' colour, or to put her pen down and draw a line, or to change her shape, etc.)

3.7. Glossary

attribute

Some state or value that belongs to a particular object. For example, tess has a color.

canvas

A surface within a window where drawing takes place.

control flow

See *flow of execution* in the next chapter.

for loop

A statement in Python for convenient repetition of statements in the *body* of the loop.

loop body

Any number of statements nested inside a loop. The nesting is indicated by the fact that the statements are indented under the for loop statement.

loop variable

A variable used as part of a for loop. It is assigned a different value on each iteration of the loop.

instance

An object of a certain type, or class. tess and alex are different instances of the class Turtle.

method

A function that is attached to an object. Invoking or activating the method causes the object to respond in some way, e.g. forward is the method when we say tess.forward(100).

invoke

An object has methods. We use the verb invoke to mean *activate the method*. Invoking a method is done by putting parentheses after the method name, with some possible arguments. So tess.forward() is an invocation of the forward method.

module

A file containing Python definitions and statements intended for use in other Python programs. The contents of a module are made available to the other program by using the *import* statement.

object



A "thing" to which a variable can refer. This could be a screen window, or one of the turtles you have created.

range

A built-in function in Python for generating sequences of integers. It is especially useful when we need to write a for loop that executes a fixed number of times.

terminating condition

A condition that occurs which causes a loop to stop repeating its body. In the <u>for</u> loops we saw in this chapter, the terminating condition has been when there are no more elements to assign to the loop variable.

3.8. Exercises

- 1. Write a program that prints We like Python's turtles! 1000 times.
- 2. Give three attributes of your cellphone object. Give three methods of your cellphone.
- 3. Write a program that uses a for loop to print

```
One of the months of the year is January
One of the months of the year is February
... etc
```

- 4. Assume you have the assignment xs = [12, 10, 32, 3, 66, 17, 42, 99, 20]
 - a. Write a loop that prints each of the numbers on a new line.
 - b. Write a loop that prints each number and its square on a new line.
 - c. Write a loop that adds all the numbers from the list into a variable called *total*. You should set the *total* variable to have the value 0 before you start adding them up, and print the value in total after the loop has completed.
 - d. Print the product of all the numbers in the list. (product means all multiplied together)
- 5. Use for loops to make a turtle draw these regular polygons (regular means all sides the same lengths, all angles the same):
 - An equilateral triangle
 - A square
 - A hexagon (six sides)
 - An octagon (eight sides)
- 6. A drunk student makes a random turn and then takes 100 steps forward, makes another random turn, takes another 100 steps, turns another random amount, etc. A social science student records the angle of each turn before the next 100 steps are taken. Her experimental

- data is [160, -43, 270, -97, -43, 200, -940, 17, -86]. (Positive angles are counter-clockwise.) Use a turtle to draw the path taken by our drunk friend.
- 7. Enhance your program above to also tell us what the drunk student's heading is after he has finished stumbling around. (Assume he begins at heading 0).
- 8. If you were going to draw a regular polygon with 18 sides, what angle would you need to turn the turtle at each corner?
- 9. At the interactive prompt, anticipate what each of the following lines will do, and then record what happens. Score yourself, giving yourself one point for each one you anticipate correctly:

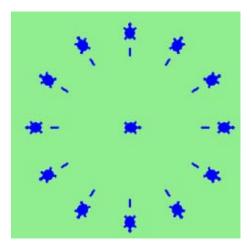
```
>>> import turtle
>>> wn = turtle.Screen()
>>> tess = turtle.Turtle()
>>> tess.right(90)
>>> tess.left(3600)
>>> tess.right(-90)
>>> tess.speed(10)
>>> tess.speed(10)
>>> tess.left(3600)
>>> tess.left(3600)
>>> tess.speed(0)
>>> tess.speed(0)
>>> tess.speed(0)
>>> tess.speed(0)
```

10. Write a program to draw a shape like this:



Hints:

- Try this on a piece of paper, moving and turning your cellphone as if it was a turtle. Watch how many complete rotations your cellphone makes before you complete the star. Since each full rotation is 360 degrees, you can figure out the total number of degrees that your phone was rotated through. If you divide that by 5, because there are five points to the star, you'll know how many degrees to turn the turtle at each point.
- You can hide a turtle behind its invisibility cloak if you don't want it shown. It will still
 draw its lines if its pen is down. The method is invoked as tess.showturtle() makes the turtle visible again.
- 11. Write a program to draw a face of a clock that looks something like this:



- 12. Create a turtle, and assign it to a variable. When you ask for its type, what do you get?
- 13. What is the collective noun for turtles? (Hint: they don't come in *herds*.)
- 14. What the collective noun for pythons? Is a python a viper? Is a python venomous?

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4. Functions

4.1. Functions

In Python, a function is a named sequence of statements that belong together. Their primary purpose is to help us organize programs into chunks that match how we think about the problem.

The syntax for a function definition is:

```
def NAME( PARAMETERS ):
   STATEMENTS
```

You can make up any names you want for the functions you create, except that you can't use a name that is a Python keyword, and the names must follow the rules for legal identifiers. The parameters specifies what information, if any, you have to provide in order to use the new function.

There can be any number of statements inside the function, but they have to be indented from the def. In the examples in this book, we will use the standard indentation of four spaces. Function definitions are the second of several compound statements we will see, all of which have the same pattern:

- 1. A header line which begins with a keyword and ends with a colon.
- 2. A body consisting of one or more Python statements, each indented the same amount 4 spaces is the Python standard - from the header line.

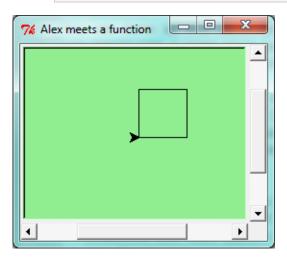
We've already seen the for loop which follows this pattern.

In a function definition, the keyword in the header is def, which is followed by the name of the function and some parameters enclosed in parentheses. The parameter list may be empty, or it may contain any number of parameters separated from one another by commas. In either case, the parentheses are required.

Suppose we're working with turtles, and a common operation we need is to draw squares. "Draw a square* is an abstraction, or a mental chunk, of a number of smaller steps. So let's write a function to capture the pattern of this "building block":

```
1
      import turtle
2
3
     def draw_square(t, sz):
         """Make turtle t draw a square of sz."""
4
5
6
         for i in range(4):
7
             t.forward(sz)
8
             t.left(90)
9
10
11
     wn = turtle.Screen()
                                 # Set up the window and its attributes
     wn.bgcolor("lightgreen")
12
     wn.title("Alex meets a function")
13
```

```
alex = turtle.Turtle() # create alex
draw_square(alex, 50) # Call the function to draw the square
wn.mainloop()
```



This function is named draw_square. It has two parameters — one to tell the function which turtle to move around, and the other to tell it the size of the square we want drawn. Make sure you know where the body of the function ends — it depends on the indentation, and the blank lines don't count for this purpose!

docstrings

If the first thing after the function header is a triple-quoted string, it is called a docstring and gets special treatment in Python and in some of the programming tools. For example, when using PyScripter, when you type a function name it will pop up a tooltip showing the parameters of the function, and the text from the docstring.

Another way to retrieve this information is to use the interactive interpreter, and enter the expression <function_name>.__doc__, which will retrieve the docstring for the function. So the string you write as documentation at the start of a function is retrievable by python tools *at runtime*. This is different from comments in your code, which are completely eliminated when the program is parsed.

By convention, Python programmers use docstrings for the key documentation of their functions.

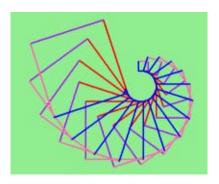
Defining a new function does not make the function run. To do that we need a function call. We've already seen how to call some built-in functions like print, range and int. Function calls contain the name of the function being executed followed by a list of values, called *arguments*, which are assigned to the parameters in the function definition. So in the second last line of the program, we call the function, and pass alex as the turtle to be manipulated, and 50 as the size of the square we want.

Once we've defined a function, we can call it as often as we like, and its statements will be executed each time we call it. And we could use it to get any of our turtles to draw a square. In the next example, we've changed the draw_square function a little, and we get tess to draw 15 squares, with some variations.

```
import turtle

def draw_multicolour_square(t, sz):
    """Make turtle t draw a multi-colour square of sz."""
for i in ['red','purple','hotpink','blue']:
```

```
t.color(i)
 7
               t.forward(sz)
 8
               t.left(90)
9
10
     wn = turtle.Screen()
                                     # Set up the window and its attributes
11
     wn.bgcolor("lightgreen")
12
13
     tess = turtle.Turtle()
                                      # create tess and set some attributes
14
     tess.pensize(3)
15
16
     size = 20
                                      # size of the smallest square
     for i in range(15):
17
18
          draw_multicolour_square(tess, size)
         size = size + 10  # increase the size for next time
tess.forward(10)  # move tess along a little
tess.right(18)  # and give her some extra turn
19
20
21
22
23
     wn.mainloop()
```



4.2. Functions can call other functions

Let's assume now we want a function to draw a rectangle. We need to be able to call the function with different arguments for width and height. And, unlike the case of the square, we cannot repeat the same thing 4 times, because the four sides are not equal.

So we eventually come up with this rather nice code that can draw a rectangle.

```
def draw_rectangle(t, w, h):
    """Get turtle t to draw a rectangle of width w and height h."""
    for i in range(2):
        t.forward(w)
        t.left(90)
        t.forward(h)
        t.left(90)
```

The parameter names are deliberately chosen as single letters to ensure they're not misunderstood. In real programs, once you've had more experience, we will insist on better variable names than this. But the point is that the program doesn't "understand" that you're drawing a rectangle, or that the parameters represent the width and the height. Concepts like rectangle, width, and height are the meaning we humans have, not concepts that the program or the computer understands.

Thinking like a scientist involves looking for patterns and relationships. In the code above, we've done that to some extent. We did not just draw four sides. Instead, we spotted that we could draw the rectangle as two halves, and used a loop to repeat that pattern twice.

But now we might spot that a square is a special kind of rectangle. We already have a function that draws a rectangle, so we can use that to draw our square.

```
def draw_square(tx, sz):  # a new version of draw_square
draw_rectangle(tx, sz, sz)
```

There are some points worth noting here:

- · Functions can call other functions.
- Rewriting draw_square like this captures the relationship that we've spotted.
- A caller of this function might say *draw_square(tess, 50)*. The parameters of this function, tx and sz, are assigned the values of the tess object, and the int 50 respectively.
- In the body of the function they are just like any other variable.
- When the call is made to <code>draw_rectangle</code>, the values in variables <code>tx</code> and <code>sz</code> are fetched first, then the call happens. So as we enter the top of function <code>draw_rectangle</code>, its variable <code>t</code> is assigned the tess object, and <code>w</code> and <code>h</code> in that function are both given the value 50.

So far, it may not be clear why it is worth the trouble to create all of these new functions. Actually, there are a lot of reasons, but this example demonstrates two:

- 1. Creating a new function gives you an opportunity to name a group of statements. Functions can simplify a program by hiding a complex computation behind a single command. The function (including its name) can capture your mental chunking, or *abstraction*, of the problem.
- 2. Creating a new function can make a program smaller by eliminating repetitive code.

As you might expect, you have to create a function before you can execute it. In other words, the function definition has to be executed before the first time it is called.

4.3. Flow of execution

In order to ensure that a function is defined before its first use, you have to know the order in which statements are executed, which is called the flow of execution. We've already talked about this a little in the previous chapter.

Execution always begins at the first statement of the program. Statements are executed one at a time, in order from top to bottom.

Function definitions do not alter the flow of execution of the program, but remember that statements inside the function are not executed until the function is called. Although it is not common, you can define one function inside another. In this case, the inner definition isn't executed until the outer function is called.

Function calls are like a detour in the flow of execution. Instead of going to the next statement, the flow jumps to the first line of the called function, executes all the statements there, and then comes back to pick up where it left off.

That sounds simple enough, until you remember that one function can call another. While in the middle of one function, the program might have to execute the statements in another function. But while executing that new function, the program might have to execute yet another function!

Fortunately, Python is adept at keeping track of where it is, so each time a function completes, the program picks up where it left off in the function that called it. When it gets to the end of the program, it terminates.

What's the moral of this sordid tale? When you read a program, don't read from top to bottom. Instead, follow the flow of execution.

Watch the flow of execution in action

In PyScripter, you can watch the flow of execution by "single-stepping" through any program. PyScripter will highlight each line of code just before it is about to be executed.

PyScripter also lets you hover the mouse over any variable in the program, and it will pop up the current value of that variable. So this makes it easy to inspect the "state snapshot" of the program — the current values that are assigned to the program's variables.

This is a powerful mechanism for building a deep and thorough understanding of what is happening at each step of the way. Learn to use the single-stepping feature well, and be mentally proactive: as you work through the code, challenge yourself before each step: "What changes will this line make to any variables in the program?" and "Where will flow of execution go next?"

Let us go back and see how this works with the program above that draws 15 multicolour squares. First, we're going to add one line of magic below the import statement — not strictly necessary, but it will make our lives much simpler, because it prevents stepping into the module containing the turtle code.

```
import turtle
__import__('turtle').__traceable__ = False
```

Now we're ready to begin. Put the mouse cursor on the line of the program where we create the turtle screen, and press the *F4* key. This will run the Python program up to, but not including, the line where you have the cursor. Your program will "break" now, and provide a highlight on the next line to be executed, something like this:

```
1 import turtle
  2 __import__('turtle').__traceable__ = False
   4 def drawMulticolouredSquare(t, sz): # Make turtle t draw a square of sz
         for i in ['red', 'purple', 'hotpink', 'blue']:
             t.color(i)
             t.forward(sz)
             t.left(90)
p 10 wn = turtle.Screen()
                                        # Set up the window and its attributes

    11 wn.bgcolor("lightgreen")

    12 wn.title("Tess dances")

  13
14 tess = turtle.Turtle()
                                       # create tess and set some attributes

    15 tess.speed(10)

    16 tess.pensize(3)

  17
• 18 size = 20
                                        # size of the smallest square

    19 for i in range(15):

        drawMulticolou.ca.

size = size + 10

toss forward(10)
        drawMulticolouredSquare(tess, size)
• 21
                                       # increase the size for next time
• 22
                                      # move tess along a little
                                       # and give her some extra turn
• 23
        tess.right(18)
  24

    25 wn.exitonclick()
```

At this point you can press the *F7* key (*step into*) repeatedly to single step through the code. Observe as you execute lines 10, 11, 12, ... how the turtle window gets created, how its canvas colour is changed, how the title gets changed, how the turtle is created on the canvas, and then how the flow of execution gets into the loop, and from there into the function, and into the function's loop, and then repeatedly

through the body of that loop.

While you do this, also hover your mouse over some of the variables in the program, and confirm that their values match your conceptual model of what is happening.

After a few loops, when you're about to execute line 20 and you're starting to get bored, you can use the key *F8* to "step over" the function you are calling. This executes all the statements in the function, but without having to step through each one. You always have the choice to either "go for the detail", or to "take the high-level view" and execute the function as a single chunk.

There are some other options, including one that allow you to *resume* execution without further stepping. Find them under the *Run* menu of PyScripter.

4.4. Functions that return values

Most functions require arguments, values that control how the function does its job. For example, if you want to find the absolute value of a number, you have to indicate what the number is. Python has a built-in function for computing the absolute value:

```
>>> abs(5)
5
>>> abs(-5)
5
```

In this example, the arguments to the abs function are 5 and -5.

Some functions take more than one argument. For example the built-in function pow takes two arguments, the base and the exponent. Inside the function, the values that are passed get assigned to variables called parameters.

```
>>> pow(2, 3)
8
>>> pow(7, 4)
2401
```

Another built-in function that takes more than one argument is max.

```
>>> max(7, 11)
11
>>> max(4, 1, 17, 2, 12)
17
>>> max(3 * 11, 5**3, 512 - 9, 1024**0)
503
```

max can be sent any number of arguments, separated by commas, and will return the maximum value sent. The arguments can be either simple values or expressions. In the last example, 503 is returned, since it is larger than 33, 125, and 1.

Furthermore, functions like range, int, abs all return values that can be used to build more complex expressions.

So an important difference between these functions and one like draw_square was not executed because we wanted it to compute a value — on the contrary, we wrote draw_square because we wanted it to execute a sequence of steps that caused the turtle to draw.

Functions that return values are called fruitful functions in this course. In many other languages, a

chunk that doesn't return a value is called a procedure, but we will stick here with the Python way of also calling it a function, or if we want to stress it, a *non-fruitful* function. (Would the term *barren function* be easier?)

How do we write our own fruitful function? In the exercises at the end of chapter 2 we saw the standard formula for compound interest, which we'll now write as a fruitful function:

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

Where,

- P = principal amount (initial investment)
- r = annual nominal interest rate (as a decimal)
- n = number of times the interest is compounded per year
- t = number of years

```
1
    def final_amt(p, r, n, t):
2
3
         Apply the compound interest formula to p
4
           to produce the final amount.
5
6
7
        a = p * (1 + r/n) ** (n*t)
8
                        # This is new, and makes the function fruitful.
9
10
    # now that we have the function above, let us call it.
    toInvest = float(input("How much do you want to invest?"))
11
12
    fnl = final_amt(toInvest, 0.08, 12, 5)
    print("At the end of the period you'll have R", fnl)
```

- The return statement is followed an expression which is evaluated. Its result is returned to the caller as the "fruit" of calling this function.
- We prompted the user for the principal amount. The type of toInvest is a string, but we need a number before we can work with it. Because it is money, and could have decimal places, we've used the float type converter function to parse the string and return a float.
- Notice how we entered the arguments for 8% interest, compounded 12 times per year, for 5 years.
- · When we run this, we get the output

At the end of the period you'll have R 14898.457083

This is a bit messy with all these decimal places, but remember that Python doesn't understand that you're working with money: it just does the calculation to the best of its ability, without rounding. Later we'll show you how to format the string that is printed in such a way that it does get nicely rounded to two decimal places before printing.

• The line toInvest = float(input("How much do you want to invest?")) also shows yet another example of composition — we can call a function like float, and its arguments can be the results of other function calls (like input) that we've called along the way.

Notice something else very important here. The name of the variable we pass as an argument — toInvest — has nothing to do with the name of the parameter — p. It is as if p = toInvest is executed when $final_amt$ is called. It doesn't matter what the value was named in the caller, in $final_amt$ it's

name is p.

These short variable names are getting quite tricky, so perhaps you'd prefer one of these versions instead:

```
1
    def final_amt_v2(principalAmount, nominalPercentageRate,
2
                                       numTimesPerYear, years):
3
        a = principalAmount * (1 + nominalPercentageRate /
                            numTimesPerYear) ** (numTimesPerYear*years)
4
5
        return a
7
   def final_amt_v3(amt, rate, compounded, years):
8
        a = amt * (1 + rate/compounded) ** (componded*years)
9
        return a
```

They all do the same thing. Use your judgement to write code that can be best understood by other humans! Short variable names are more economical and sometimes make code easier to read: $E = mc^2$ would not be nearly so memorable if Einstein had used longer variable names! If you do prefer short names, make sure you also have some comments to enlighten the reader about what the variables are used for.

4.5. Variables and parameters are local

When you create a local variable inside a function, it only exists inside the function, and you cannot use it outside. For example, consider again this function:

```
def final_amt(p, r, n, t):
    a = p * (1 + r/n) ** (n*t)
    return a
```

If we try to use a, outside the function, we'll get an error:

```
>>> a
NameError: name 'a' is not defined
```

The variable a is local to final_amt, and is not visible outside the function.

Additionally, a only exists while the function is being executed — we call this its lifetime. When the execution of the function terminates, the local variables are destroyed.

Parameters are also local, and act like local variables. For example, the lifetimes of p, r, n, t begin when $final_amt$ is called, and the lifetime ends when the function completes its execution.

So it is not possible for a function to set some local variable to a value, complete its execution, and then when it is called again next time, recover the local variable. Each call of the function creates new local variables, and their lifetimes expire when the function returns to the caller.

4.6. Turtles Revisited

Now that we have fruitful functions, we can focus our attention on reorganizing our code so that it fits more nicely into our mental chunks. This process of rearrangement is called refactoring the code.

Two things we're always going to want to do when working with turtles is to create the window for the turtle, and to create one or more turtles. We could write some functions to make these tasks easier in future:

```
1
    def make_window(colr, ttle):
2
3
          Set up the window with the given background colour and title.
4
          Returns the new window.
5
        w = turtle.Screen()
6
7
        w.bgcolor(colr)
8
        w.title(ttle)
9
        return w
10
11
    def make_turtle(colr, sz):
12
13
14
          Set up a turtle with the given colour and pensize.
15
          Returns the new turtle.
16
17
        t = turtle.Turtle()
18
        t.color(colr)
19
        t.pensize(sz)
20
        return t
21
22
    wn = make_window("lightgreen", "Tess and Alex dancing")
23
    tess = make_turtle("hotpink", 5)
24
    alex = make_turtle("black", 1)
25
    dave = make_turtle("yellow", 2)
26
```

The trick about refactoring code is to see which things you are likely to want to change each time you call the function: these should become the parameters, or changeable bits, of the functions you write.

4.7. Glossary

argument

A value provided to a function when the function is called. This value is assigned to the corresponding parameter in the function. The argument can be the result of an expression which may involve operators, operands and calls to other fruitful functions.

body

The second part of a compound statement. The body consists of a sequence of statements all indented the same amount from the beginning of the header. The standard amount of indentation used within the Python community is 4 spaces.

compound statement

A statement that consists of two parts:

- 1. header which begins with a keyword determining the statement type, and ends with a colon.
- 2. body containing one or more statements indented the same amount from the header.

The syntax of a compound statement looks like this:

```
keyword expression:
```

statement ...

docstring

If the first thing in a function body is a string (or, we'll see later, in other situations too) that is attached to the function as its __doc__ attribute, and can be used by tools like PyScripter.

flow of execution

The order in which statements are executed during a program run.

frame

A box in a stack diagram that represents a function call. It contains the local variables and parameters of the function.

function

A named sequence of statements that performs some useful operation. Functions may or may not take parameters and may or may not produce a result.

function call

A statement that executes a function. It consists of the name of the function followed by a list of arguments enclosed in parentheses.

function composition

Using the output from one function call as the input to another.

function definition

A statement that creates a new function, specifying its name, parameters, and the statements it executes.

fruitful function

A function that returns a value when it is called.

header line

The first part of a compound statement. A header line begins with a keyword and ends with a colon (:)

import statement

A statement which permits functions and variables defined in another Python module to be brought into the environment of another script. To use the features of the turtle, we need to first import the turtle module.

lifetime

Variables and objects have lifetimes — they are created at some point during program execution, and will be destroyed at some time.

local variable

A variable defined inside a function. A local variable can only be used inside its function. Parameters of a function are also a special kind of local variable.

parameter

A name used inside a function to refer to the value which was passed to it as an argument.

refactor

A fancy word to describe reorganizing your program code, usually to make it more understandable. Typically, we have a program that is already working, then we go back to "tidy it up". It often involves choosing better variable names, or spotting repeated patterns and moving that code into a function.

stack diagram

A graphical representation of a stack of functions, their variables, and the values to which they refer.

traceback

A list of the functions that are executing, printed when a runtime error occurs. A traceback is also commonly referred to as a *stack trace*, since it lists the functions in the order in which they are stored in the <u>runtime stack</u>.

4.8. Exercises

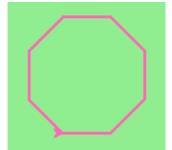
1. Write a non-fruitful function to draw a square. Use it in a program to draw the image shown below. Assume each side is 20 units. (Hint: notice that the turtle has already moved away from the ending point of the last square when the program ends.)



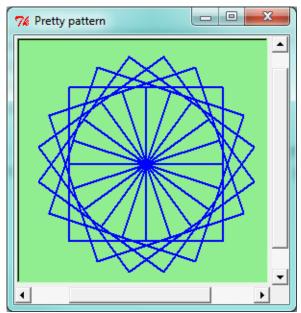
2. Write a program to draw this. Assume the innermost square is 20 units per side, and each successive square is 20 units bigger, per side, than the one inside it.



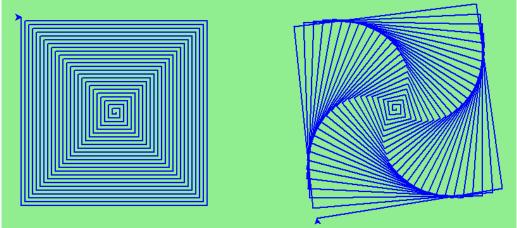
3. Write a non-fruitful function draw_poly(t, n, sz) which makes a turtle draw a regular polygon. When called with draw poly(tess, 8, 50), it will draw a shape like this:



4. Draw this pretty pattern.



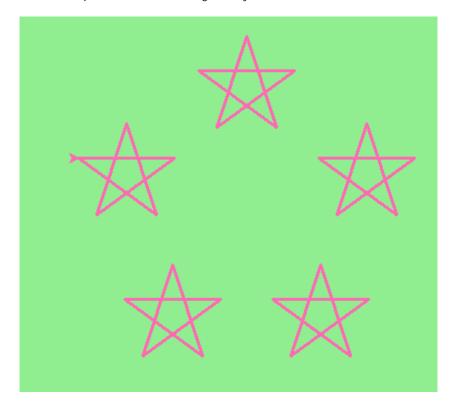
5. The two spirals in this picture differ only by the turn angle. Draw both.



- 6. Write a non-fruitful function draw_equitriangle(t, sz) which calls draw_poly from the previous question to have its turtle draw a equilateral triangle.
- 7. Write a fruitful function $sum_to(n)$ that returns the sum of all integer numbers up to and including n. So $sum_to(10)$ would be 1+2+3...+10 which would return the value 55.
- 8. Write a function $area_{of_circle(r)}$ which returns the area of a circle of radius r.
- 9. Write a non-fruitful function to draw a star, where the length of each side is 100 units. (Hint: You should turn the turtle by 144 degrees at each point.)



10. Extend your program above. Draw five stars, but between each, pick up the pen, move forward by 350 units, turn right by 144, put the pen down, and draw the next star. You'll get something like this:



What would it look like if you didn't pick up the pen?

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5. Conditionals

5.1. The modulus operator

The modulus operator works on integers (and integer expressions) and gives the remainder when the first number is divided by the second. In Python, the modulus operator is a percent sign (%). The syntax is the same as for other operators:

```
>>> q = 7 // 3  # This is integer division operator
>>> print(q)
2
>>> r = 7 % 3
>>> print(r)
1
```

So 7 divided by 3 is 2 with a remainder of 1.

The modulus operator turns out to be surprisingly useful. For example, you can check whether one number is divisible by another—if x % y is zero, then x is divisible by y.

Also, you can extract the right-most digit or digits from a number. For example, \times % 10 yields the right-most digit of x (in base 10). Similarly x % 100 yields the last two digits.

It is also extremely useful for doing conversions, say from seconds, to hours, minutes and seconds. So let's write a program to ask the user to enter some seconds, and we'll convert them into hours, minutes, and remaining seconds.

5.2. Boolean values and expressions

The Python type for storing true and false values is called <u>bool</u>, named after the British mathematician, George Boole. He created *Boolean algebra*, which is the basis of all modern computer arithmetic.

There are only two boolean values, True and False. Capitalization is important, since true and false are not boolean values.

```
>>> type(True)
<class 'bool'>
>>> type(true)
```

```
Traceback (most recent call last):
   File "<interactive input>", line 1, in <module>
NameError: name 'true' is not defined
```

A boolean expression is an expression that evaluates to a boolean value. The operator == compares two values and produces a boolean value:

```
>>> 5 == 5
True
>>> 5 == 6
False
```

In the first statement, the two operands are equal, so the expression evaluates to True; in the second statement, 5 is not equal to 6, so we get False.

The == operator is one of six common comparison operators; the others are:

```
x != y  # x is not equal to y
x > y  # x is greater than y
x < y  # x is less than y
x >= y  # x is greater than or equal to y
x <= y  # x is less than or equal to y</pre>
```

Although these operations are probably familiar to you, the Python symbols are different from the mathematical symbols. A common error is to use a single equal sign (=) instead of a double equal sign (==). Remember that = is an assignment operator and == is a comparison operator. Also, there is no such thing as =< or =>.

5.3. Logical operators

There are three logical operators: and, or, and not. The semantics (meaning) of these operators is similar to their meaning in English. For example, x > 0 and x < 10 is true only if x is greater than 0 and at the same time, x is less than 10.

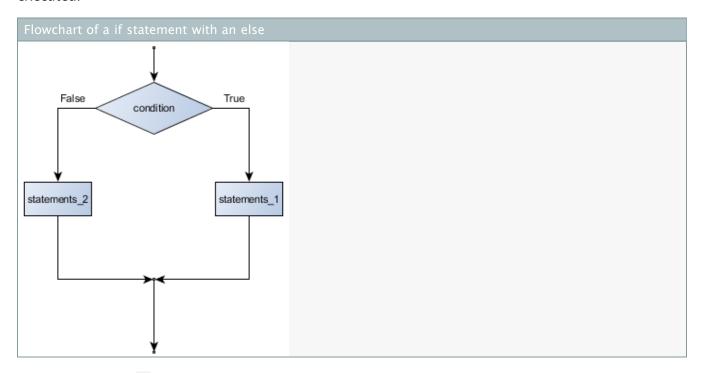
n % 2 == 0 or n % 3 == 0 is true if *either* of the conditions is true, that is, if the number is divisible by 2 or divisible by 3.

Finally, the <u>not</u> operator negates a boolean expression, so $\underline{not(x > y)}$ is true if $\underline{(x > y)}$ is false, that is, if x is less than or equal to y.

5.4. Conditional execution

In order to write useful programs, we almost always need the ability to check conditions and change the behavior of the program accordingly. Conditional statements give us this ability. The simplest form is the if statement:

The boolean expression after the if statement is called the condition. If it is true, then all the indented statements get executed. If not, then all the statements indented under the else clause get executed.



The syntax for an if statement looks like this:

```
if BOOLEAN EXPRESSION:
STATEMENTS_1 # executed if condition evaluates to True
else:
STATEMENTS_2 # executed if condition evaluates to False
```

As with the function definition from the last chapter and other compound statements like <u>for</u>, the <u>if</u> statement consists of a header line and a body. The header line begins with the keyword <u>if</u> followed by a *boolean expression* and ends with a colon (:).

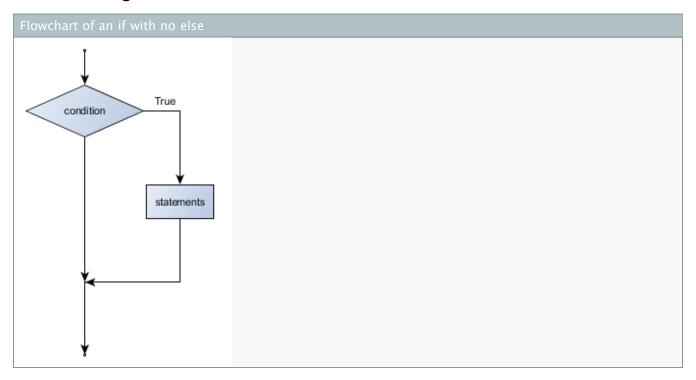
The indented statements that follow are called a block. The first unindented statement marks the end of the block.

Each of the statements inside the first block of statements are executed in order if the boolean expression evaluates to True. The entire first block of statements is skipped if the boolean expression evaluates to False, and instead all the statements under the else clause are executed.

There is no limit on the number of statements that can appear under the two clauses of an if statement, but there has to be at least one statement in each block. Occasionally, it is useful to have a section with no statements (usually as a place keeper, or scaffolding, for code you haven't written yet). In that case, you can use the pass statement, which does nothing except act as a placeholder.

```
if True: # This is always true
pass # so this is always executed, but it does nothing
else:
pass
```

5.5. Omitting the *else* clause



Another form of the <u>if</u> statement is one in which the <u>else</u> clause is omitted entirely. In this case, when the condition evaluates to True, the statements are executed, otherwise the flow of execution continues to the statement after the <u>if</u>.

```
if x < 0:
    print("The negative number ", x, " is not valid here.")
    x = 42
    print("I've decided to use the number 42 instead.")

print("The square root of ", x, "is", math.sqrt(x))</pre>
```

In this case, the print function that outputs the square root is the one after the <u>if</u> – not because we left a blank line, but because of the way the code is indented. Note too that the function call math.sqrt(x) will give an error unless you have an <u>import math</u> statement, usually placed near the top of your script.

Python terminology

Python documentation sometimes uses the term suite of statements to mean what we have called a *block* here. They mean the same thing, and since most other languages and computer scientists use the word *block*, we'll stick with that.

Notice too that <u>else</u> is not a statement. The <u>if</u> statement has two *clauses*, one of which is the (optional) else clause.

5.6. Chained conditionals

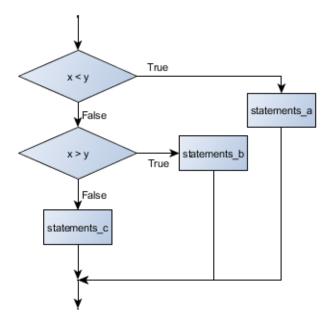
Sometimes there are more than two possibilities and we need more than two branches. One way to express a computation like that is a chained conditional:

```
if x < y:
    STATEMENTS_A

elif x > y:
    STATEMENTS_B

else:
    STATEMENTS_C
```

Flowchart of this chained conditional



elif is an abbreviation of else if. Again, exactly one branch will be executed. There is no limit of the number of elif statements but only a single (and optional) final else statement is allowed and it must be the last branch in the statement:

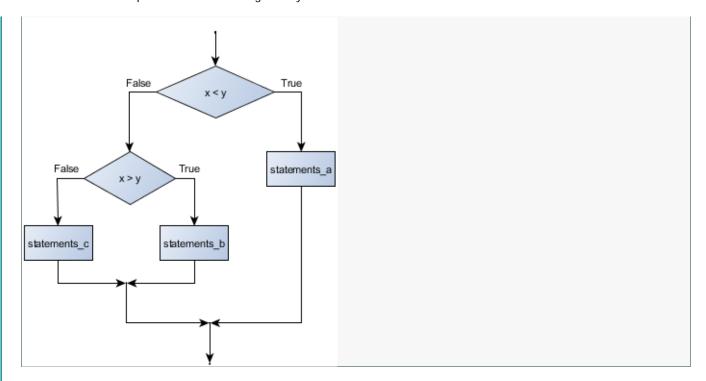
```
if choice == 'a':
    function_a()
elif choice == 'b':
    function_b()
elif choice == 'c':
    function_c()
else:
    print("Invalid choice.")
```

Each condition is checked in order. If the first is false, the next is checked, and so on. If one of them is true, the corresponding branch executes, and the statement ends. Even if more than one condition is true, only the first true branch executes.

5.7. Nested conditionals

One conditional can also be nested within another. (It is the same theme of composibility, again!) We could have written the previous example as follows:

Flowchart of this nested conditional



```
if x < y:
    STATEMENTS_A
else:
    if x > y:
        STATEMENTS_B
else:
    STATEMENTS_C
```

The outer conditional contains two branches. The second branch contains another <u>if</u> statement, which has two branches of its own. Those two branches could contain conditional statements as well.

Although the indentation of the statements makes the structure apparent, nested conditionals very quickly become difficult to read. In general, it is a good idea to avoid them when you can.

Logical operators often provide a way to simplify nested conditional statements. For example, we can rewrite the following code using a single conditional:

```
if 0 < x:  # assume x is an int here
if x < 10:
    print("x is a positive single digit.")</pre>
```

The print function is called only if we make it past both the conditionals, so we can use the and operator:

```
if 0 < x and x < 10:
    print("x is a positive single digit.")</pre>
```

5.8. The return statement

The <u>return</u> statement, with or without a value, depending on whether the function is fruitful or not, allows you to terminate the execution of a function before you reach the end. One reason to use it is if you detect an error condition:

```
def print_square_root(x):
    if x <= 0:
        print("Positive numbers only, please.")
    return

result = x**0.5
print("The square root of", x, "is", result)</pre>
```

The function print_square_root has a parameter named x. The first thing it does is check whether x is less than or equal to 0, in which case it displays an error message and then uses return to exit the function. The flow of execution immediately returns to the caller, and the remaining lines of the function are not executed.

5.9. Type conversion

We've had a first look at this in an earlier chapter. Seeing it again won't hurt!

Many Python types comes with a built-in function that attempts to convert values of another type into its own type. The <u>int(ARGUMENT)</u> function, for example, takes any value and converts it to an integer, if possible, or complains otherwise:

```
>>> int("32")
32
>>> int("Hello")
ValueError: invalid literal for int() with base 10: 'Hello'
```

int can also convert floating-point values to integers, but remember that it truncates the fractional part:

```
>>> int(-2.3)
-2
>>> int(3.99999)
3
>>> int("42")
42
>>> int(1.0)
1
```

The float (ARGUMENT) function converts integers and strings to floating-point numbers:

```
>>> float(32)
32.0
>>> float("3.14159")
3.14159
>>> float(1)
1.0
```

It may seem odd that Python distinguishes the integer value 1 from the floating-point value 1.0. They may represent the same number, but they belong to different types. The reason is that they are represented differently inside the computer.

The str(ARGUMENT) function converts any argument given to it to type string:

```
>>> str(32)
'32'
>>> str(3.14149)
'3.14149'
>>> str(True)
'True'
>>> str(true)
Traceback (most recent call last):
  File "<interactive input>", line 1, in <module>
NameError: name 'true' is not defined
```

str(ARGUMENT) will work with any value and convert it into a string. As mentioned earlier, True is boolean value; true is not.

5.10. A Turtle Bar Chart

The turtle has a lot more power than we've seen so far. If you want to see the full documentation, look at http://docs.python.org/library/turtle.html, or within PyScripter, use Help and search for the turtle module.

Here are a couple of new tricks for our turtles:

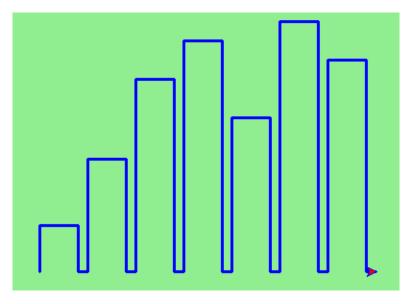
- We can get a turtle to display text on the canvas at the turtle's current position. The method is alex.write("Hello").
- One can fill a shape (circle, semicircle, triangle, etc.) with a fill colour. It is a two-step process. First you call the method alex.begin_fill(), then you draw the shape, then call alex.end_fill().
- We've previously set the color of our turtle we can now also set it's fillcolour, which need not be the same as the turtle and the pen colour. We use alex.color("blue", "red") to set the turtle to draw in blue, and fill in red.

Ok, so can we get tess to draw a bar chart? Let us start with some data to be charted,

```
xs = [48, 117, 200, 240, 160, 260, 220]
```

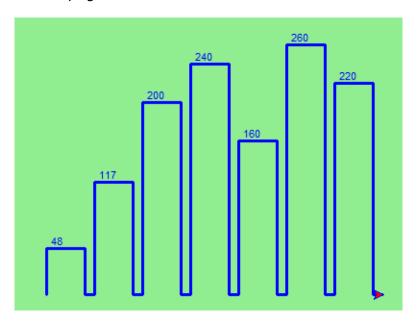
Corresponding to each data measurement, we'll draw a simple rectangle of that height, with a fixed width.

```
def draw_bar(t, height):
 1
 2
          """ Get turtle t to draw one bar, of height. """
 3
         t.left(90)
         t.forward(height) # Draw up the Left side
4
 5
         t.right(90)
                                 # width of bar, along the top
 6
         t.forward(40)
 7
         t.right(90)
         t.forward(height) # And down again!
t.left(90) # put the turtle facing the way we found it.
t forward(10) # logge small aga after each han
8
9
10
         t.forward(10)
                                 # leave small gap after each bar
11
12
    for v in xs:
13
                                  # assume xs and tess are ready
         draw_bar(tess, v)
14
```



Ok, not fantasically impressive, but it is a nice start! The important thing here was the mental chunking, or how we broke the problem into smaller pieces. Our chunk is to draw one bar, and we wrote a function to do that. Then, for the whole chart, we repeatedly called our function.

Next, at the top of each bar, we'll print the value of the data. We'll do this in the body of draw_bar, by adding t.write(' ' + str(height))) as the new third line of the body. We've put a little space in front of the number, and turned the number into a string. Without this extra space we tend to cramp our text awkwardly against the bar to the left. The result looks a lot better now:

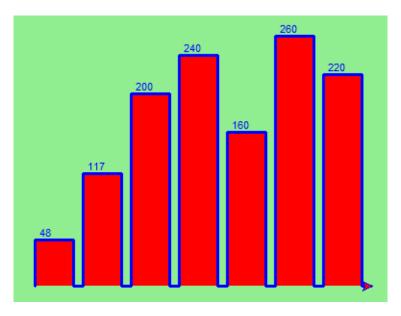


And now we'll add two lines to fill each bar. Our final program now looks like this:

```
def draw_bar(t, height):
1
         """ Get turtle t to draw one bar, of height.
2
3
                                     # added this line
        t.begin_fill()
4
        t.left(90)
5
        t.forward(height)
6
        t.write('
                   '+ str(height))
7
        t.right(90)
8
        t.forward(40)
9
        t.right(90)
10
        t.forward(height)
```

```
11
         t.left(90)
12
         t.end_fill()
                                  # added this line
13
         t.forward(10)
14
15
     wn = turtle.Screen()
                                  # Set up the window and its attributes
16
    wn.bgcolor("lightgreen")
17
18
    tess = turtle.Turtle()
                                  # create tess and set some attributes
19
     tess.color("blue", "red")
20
    tess.pensize(3)
21
22
    xs = [48, 117, 200, 240, 160, 260, 220]
23
24
     for a in xs:
25
         draw_bar(tess, a)
26
27
     wn.mainloop()
```

It produces the following, which is more satisfying:



Mmm. Perhaps the bars should not be joined to each other at the bottom. We'll need to pick up the pen while making the gap between the bars. We'll leave that as an exercise for you!

5.11. Glossary

block

A group of consecutive statements with the same indentation.

body

The block of statements in a compound statement that follows the header.

boolean expression

An expression that is either true or false.

boolean value

There are exactly two boolean values: True and False. Boolean values result when a boolean expression is evaluated by the Python interepreter. They have type bool.

branch

One of the possible paths of the flow of execution determined by conditional execution.

chained conditional

A conditional branch with more than two possible flows of execution. In Python chained conditionals are written with if ... else statements.

comparison operator

One of the operators that compares two values: ==, !=, >, <, >=, and <=.

condition

The boolean expression in a conditional statement that determines which branch is executed.

conditional statement

A statement that controls the flow of execution depending on some condition. In Python the keywords if, elif, and else are used for conditional statements.

logical operator

One of the operators that combines boolean expressions: and, or, and not.

modulus operator

An operator, denoted with a percent sign (%), that works on integers and yields the remainder when one number is divided by another.

nesting

One program structure within another, such as a conditional statement inside a branch of another conditional statement.

prompt

A visual cue that tells the user to input data.

type conversion

An explicit function call that takes a value of one type and computes a corresponding value of another type.

wrapping code in a function

The process of adding a function header and parameters to a sequence of program statements is often refered to as "wrapping the code in a function". This process is very useful whenever the program statements in question are going to be used multiple times. It is even more useful when it allows the programmer to express their mental chunking, and how they've broken a complex problem into pieces.

5.12. Exercises

1. Evaluate the following numerical expressions in your head, then use the Python interpreter to check your results:

- 1. >>> 5 % 2
- 2. >>> 9 % 5
- 3. >>> 15 % 12
- 4. >>> 12 % 15
- 5. >>> 6 % 6
- 6. >>> 0 % 7

What happened with the last example? Why? If you were able to correctly anticipate the computer's response in all but the last one, it is time to move on. If not, take time now to make up examples of your own. Explore the modulus operator until you are confident you understand how it works.

- 2. You look at the clock and it is exactly 2pm. You set an alarm to go off in 51 hours. At what time does the alarm go off?
- 3. Write a Python program to solve the general version of the above problem. Ask the user for the time now (in hours), and ask for the number of hours to wait. Your program should output what the time will be on the clock when the alarm goes off.
- 4. Assume the days of the week are numbered 0,1,2,3,4,5,6 from Sunday to Saturday. Write a function which is given the day number, and it returns the day name (a string).
- 5. You go on a wonderful holiday (perhaps to jail, if you don't like happy exercises) leaving on day number 3 (a Wednesday). You return home after 137 sleeps. Write a general version of the program which asks for the starting day number, and the length of your stay, and it will tell you the name of day of the week you will return on.
- 6. Give the logical opposites of these conditions

```
1. a > b
```

2. a >= b

3. a >= 18 and day == 3

4. a >= 18 and day != 3

- 7. What do these expressions evaluate to?
 - 1. 3 == 3
 - 2. 3 != 3
 - 3. 3 >= 4
 - 4. not (3 < 4)
- 8. Write a function which is given an exam mark, and it returns a string the grade for that mark according to this scheme:

Mark	Grade
>= 75	First
[70-75)	Upper Second
[60-70)	Second
[50-60)	Third
[45-50)	F1 Supp
[40-45)	F2
< 40	F3

The square and round brackets denote closed and open intervals. A closed interval includes the number, and open interval excludes it. So 39.99999 gets grade F3, but 40 gets grade F2. Assume

```
xs = [83, 75, 74.9, 70, 69.9, 65, 60, 59.9, 55, 50,
49.9, 45, 44.9, 40, 39.9, 2, 0
```

Test your function by printing the mark and the grade for all the elements in this list.

- 9. Modify the turtle bar chart program so that the pen is up for the small gaps between each bar.
- 10. Modify the turtle bar chart program so that the bar for any value of 200 or more is filled with red, values between [100 and 200) are filled with yellow, and bars representing values less than 100 are filled with green.
- 11. In the turtle bar chart program, what do you expect to happen if one or more of the data values in the list is negative? Try it out. Change the program so that when it prints the text value for the negative bars, it puts the text below the bottom of the bar.
- 12. Write a function <u>find_hypot</u> which, given the length of two sides of a right-angled triangle, returns the length of the hypotenuse. (Hint: x ** 0.5 will return the square root.)
- 13. Write a function is_rightangled which, given the length of three sides of a triangle, will determine whether the triangle is right-angled. Assume that the third argument to the function is always the longest side. It will return True if the triangle is right-angled, or False otherwise.

Hint: floating point arithmetic is not always exactly accurate, so it is not safe to test floating point numbers for equality. If a good programmer wants to know whether $\frac{1}{x}$ is equal or close enough to $\frac{1}{y}$, they would probably code it up as

```
if abs(x-y) < 0.000001: # if x is approximately equal to y
...</pre>
```

14. Extend the above program so that the sides can be given to the function in any order.

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6. Fruitful functions

6.1. Return values

The built-in functions we have used, such as abs, pow, int, max, and range, have produced results. Calling each of these functions generates a value, which we usually assign to a variable or use as part of an expression.

```
biggest = max(3, 7, 2, 5)
x = abs(3 - 11) + 10
```

We also wrote our own function to return the final amount for a compound interest calculation.

In this chapter, we are going to write more functions that return values, which we will call fruitful functions, for want of a better name. The first example is area, which returns the area of a circle with the given radius:

```
1
    def area(radius):
2
        b = 3.14159 * radius**2
3
        return b
```

We have seen the return statement before, but in a fruitful function the return statement includes a return value. This statement means: evaluate the return expression, and then return it immediately as the result (the fruit) of this function. The expression provided can be arbitrarily complicated, so we could have written this function like this:

```
1
    def area(radius):
       return 3.14159 * radius * radius
```

On the other hand, temporary variables like b above often make debugging easier.

Sometimes it is useful to have multiple return statements, one in each branch of a conditional. We have already seen the built-in abs, now we see how to write our own:

```
def absolute value(x):
1
2
        if x < 0:
3
            return -x
4
        else:
5
            return x
```

Another way to write the above function is to leave out the else and just follow the if condition by the second return statement.

```
def absolute_value(x):
    if x < 0:
        return -x
    return x</pre>
```

Think about this version and convince yourself it works the same as the first one.

Code that appears after a return statement, or any other place the flow of execution can never reach, is called dead code, or unreachable code.

In a fruitful function, it is a good idea to ensure that every possible path through the program hits a return statement. The following version of absolute value fails to do this:

```
def bad_absolute_value(x):
    if x < 0:
        return -x
    elif x > 0:
        return x
```

This version is not correct because if x happens to be 0, neither condition is true, and the function ends without hitting a return statement. In this case, the return value is a special value called None:

```
>>> print(bad_absolute_value(0))
None
```

All Python functions return None whenever they do not return another value.

It is also possible to use a return statement in the middle of a for loop, in which case control immediately returns from the function. Let us assume that we want a function which looks through a list of words. It should return the first 2-letter word. If there is not one, it should return the empty string:

```
def find_first_2_letter_word(xs):
    for wd in xs:
        if len(wd) == 2:
            return wd
    return ''
```

```
>>> find_first_2_letter_word(['This', 'is', 'a', 'dead', 'parrot'])
'is'
>>> find_first_2_letter_word(["I", "like", "cheese"])
''
```

Single-step through this code and convince yourself that in the first test case that we've provided, the function returns while processing the second element in the list: it does not have to traverse the whole list.

6.2. Program development

At this point, you should be able to look at complete functions and tell what they do. Also, if you have been doing the exercises, you have written some small functions. As you write larger functions, you

might start to have more difficulty, especially with runtime and semantic errors.

To deal with increasingly complex programs, we are going to suggest a technique called incremental development. The goal of incremental development is to avoid long debugging sessions by adding and testing only a small amount of code at a time.

As an example, suppose you want to find the distance between two points, given by the coordinates (x_1, y_1) and (x_2, y_2) . By the Pythagorean theorem, the distance is:

distance =
$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

The first step is to consider what a distance function should look like in Python. In other words, what are the inputs (parameters) and what is the output (return value)?

In this case, the two points are the inputs, which we can represent using four parameters. The return value is the distance, which is a floating-point value.

Already we can write an outline of the function that captures our thinking so far:

```
def distance(x1, y1, x2, y2):
    return 0.0
```

Obviously, this version of the function doesn't compute distances; it always returns zero. But it is syntactically correct, and it will run, which means that we can test it before we make it more complicated.

To test the new function, we call it with sample values:

```
>>> distance(1, 2, 4, 6)
0.0
```

We chose these values so that the horizontal distance equals 3 and the vertical distance equals 4; that way, the result is 5 (the hypotenuse of a 3-4-5 triangle). When testing a function, it is useful to know the right answer.

At this point we have confirmed that the function is syntactically correct, and we can start adding lines of code. After each incremental change, we test the function again. If an error occurs at any point, we know where it must be — in the last line we added.

A logical first step in the computation is to find the differences $x_2 - x_1$ and $y_2 - y_1$. We will store those values in temporary variables named dx and dy.

```
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    return 0.0
```

If we call the function with the arguments shown above, when the flow of execution gets to the return statement, dx should be 3 and dy should be 4. We can check that this is the case in PyScripter by putting the cursor on the return statement, and running the program to break execution when it gets to the cursor (using the F4 key). Then we inspect the variables dx and dy by hovering the mouse above

them, to confirm that the function is getting the right parameters and performing the first computation correctly. If not, there are only a few lines to check.

Next we compute the sum of squares of dx and dy:

```
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    dsquared = dx*dx + dy*dy
    return 0.0
```

Again, we could run the program at this stage and check the value of dsquared (which should be 25).

Finally, using the fractional exponent 0.5 to find the square root, we compute and return the result:

If that works correctly, you are done. Otherwise, you might want to inspect the value of result before the return statement.

When you start out, you might add only a line or two of code at a time. As you gain more experience, you might find yourself writing and debugging bigger conceptual chunks. Either way, stepping through your code one line at a time and veryifying that each step matches your expectations can save you a lot of debugging time. As you improve your programming skills you should find yourself managing bigger and bigger chunks: this is very similar to the way we learnt to read letters, syllables, words, phrases, sentences, paragraphs, etc., or the way we learn to chunk music — from indvidual notes to chords, bars, phrases, and so on.

The key aspects of the process are:

- 1. Start with a working skeleton program and make small incremental changes. At any point, if there is an error, you will know exactly where it is.
- 2. Use temporary variables to hold intermediate values so that you can easily inspect and check them
- 3. Once the program is working, relax, sit back, and play around with your options. (There is interesting research that links "playfulness" to better understanding, better learning, more enjoyment, and a more positive mindset about what you can achieve so spend some time fiddling around!) You might want to consolidate multiple statements into one bigger compound expression, or rename the variables you've used, or see if you can make the function shorter. A good guideline is to aim for making code as easy as possible for others to read.

Here is another version of the function. It makes use of a square root function that is in the math module (we'll learn about modules shortly). Which do you prefer? Which looks "closer" to the Pythagorean formula we started out with?

```
1 import math
```

```
def distance(x1, y1, x2, y2):
    return math.sqrt( (x2-x1)**2 + (y2-y1)**2 )
```

```
>>> distance(1, 2, 4, 6) 5.0
```

6.3. Debugging with print

Another powerful technique for debugging (an alternative to single-stepping and inspection of program variables), is to insert extra print functions in carefully selected places in your code. Then, by inspecting the output of the program, you can check whether the algorithm is doing what you expect it to. Be clear about the following, however:

- You must have a clear solution to the problem, and must know what should happen before you can debug a program. Work on *solving* the problem on a piece of paper (perhaps using a flowchart to record the steps you take) *before* you concern yourself with writing code. Writing a program doesn't solve the problem it simply *automates* the manual steps you would take. So first make sure you have a pen-and-paper manual solution that works. Programming then is about making those manual steps happen automatically.
- Do not write chatterbox functions. A chatterbox is a fruitful function that, in addition to its primary task, also asks the user for input, or prints output, when it would be more useful if it simply shut up and did its work quietly.

For example, we've seen built-in functions like <u>range</u>, <u>max</u> and <u>abs</u>. None of these would be useful building blocks for other programs if they prompted the user for input, or printed their results while they performed their tasks.

So a good tip is to avoid calling print and input functions inside fruitful functions, unless the primary purpose of your function is to perform input and output. The one exception to this rule might be to temporarily sprinkle some calls to print into your code to help debug and understand what is happening when the code runs, but these will then be removed once you get things working.

6.4. Composition

As you should expect by now, you can call one function from within another. This ability is called composition.

As an example, we'll write a function that takes two points, the center of the circle and a point on the perimeter, and computes the area of the circle.

Assume that the center point is stored in the variables xc and yc, and the perimeter point is in xp and yp. The first step is to find the radius of the circle, which is the distance between the two points. Fortunately, we've just written a function, distance, that does just that, so now all we have to do is use it:

```
1 radius = distance(xc, yc, xp, yp)
```

The second step is to find the area of a circle with that radius and return it. Again we will use one of our earlier functions:

```
result = area(radius)
return result
```

Wrapping that up in a function, we get:

```
def area2(xc, yc, xp, yp):
    radius = distance(xc, yc, xp, yp)
    result = area(radius)
    return result
```

We called this function area2 to distinguish it from the area function defined earlier. There can only be one function with a given name within a module.

The temporary variables <u>radius</u> and <u>result</u> are useful for development, debugging, and single-stepping through the code to inspect what is happening, but once the program is working, we can make it more concise by composing the function calls:

```
def area2(xc, yc, xp, yp):
    return area(distance(xc, yc, xp, yp))
```

6.5. Boolean functions

Functions can return boolean values, which is often convenient for hiding complicated tests inside functions. For example:

```
def is_divisible(x, y):
    if x % y == 0:
        return True
    else:
        return False
```

The name of this function is <u>is_divisible</u>. It is common to give boolean functions names that sound like yes/no questions. <u>is_divisible</u> returns either True or False to indicate whether the x is or is not divisible by y.

We can make the function more concise by taking advantage of the fact that the condition of the <u>if</u> statement is itself a boolean expression. We can return it directly, avoiding the <u>if</u> statement altogether:

```
def is_divisible(x, y):
    return x % y == 0
```

This session shows the new function in action:

```
>>> is_divisible(6, 4)
False
>>> is_divisible(6, 3)
True
```

Boolean functions are often used in conditional statements:

```
if is_divisible(x, y):
    ... # do something ...
else:
    ... # do something else ...
```

It might be tempting to write something like:

```
if is_divisible(x, y) == True:
```

but the extra comparison is unnecessary.

6.6. Programming with style

Readability is very important to programmers, since in practice programs are read and modified far more often then they are written. All the code examples in this book will be consistent with the *Python Enhancement Proposal 8* (PEP 8), a style guide developed by the Python community.

We'll have more to say about style as our programs become more complex, but a few pointers will be helpful already:

- use 4 spaces for indentation
- imports should go at the top of the file
- · separate function definitions with two blank lines
- keep function definitions together
- keep top level statements, including function calls, together at the bottom of the program

6.7. Unit testing

It is a common best practice in software development these days to include automatic unit testing of source code. Unit testing provides a way to automatically verify that individual pieces of code, such as functions, are working properly. This makes it possible to change the implementation of a function at a later time and quickly test that it still does what it was intended to do.

Unit testing also forces the programmer to think about the different cases that the function needs to handle. You also only have to type the tests once into the script, rather than having to keep entering the same test data over and over as you develop your code.

Extra code in your program which is there because it makes debugging or testing easier is called scaffolding.

A collection of tests for some code is called its test suite.

There are a few different preferred ways to do unit testing in Python — but at this stage we're going to

ignore what the Python community usually does, and we're going to start with two functions that we'll write ourselves. We'll use these for writing our unit tests.



Let's start with the <u>absolute_value</u> function that we wrote earlier in this chapter. Recall that we wrote a few different versions, the last of which was incorrect, and had a bug. Would tests have caught this bug?

First we plan our tests. We'd like to know if the function returns the correct value when its argument is negative, or when its argument is positive, or when its argument is zero. When planning your tests, you'll always want to think carefully about the "edge" cases — here, an argument of 0 to absolute_value is on the edge of where the function behaviour changes, and as we saw at the beginning of the chapter, it is an easy spot for the programmer to make a mistake! So it is a good case to include in our test suite.

We're going to write a helper function for checking the results of one test. It takes two arguments — the actual value that was returned from the computation, and the value we expected to get. It compares these, and will either print a message telling us that the test passed, or it will print a message to inform us that the test failed. The first two lines of the body (after the function's docstring) can be copied to your own code as they are here: they import a module called sys, and extract the caller's line number from the stack frame. This allows us to print the line number of the test, which will help when we want to fix any tests that fail.

```
1
    def test(actual, expected):
2
         """ Compare the actual to the expected value,
3
            and print a suitable message.
4
5
        import sys
6
        linenum = sys._getframe(1).f_lineno # get the caller's line number.
7
        if (expected == actual):
8
            msg = "Test on line {0} passed.".format(linenum)
9
10
            msg = ("Test on line {0} failed. Expected '{1}', but got '{2}'."
11
                                         . format(linenum, expected, actual))
12
        print(msg)
```

There is also some slightly tricky string formatting using the <u>format</u> method which we will gloss over for the moment, and cover in detail in a future chapter. But with this function written, we can proceed to construct our test suite:

```
def test_suite():
1
         """ Run the suite of tests for code in this module (this file).
2
3
        test(absolute_value(17), 17)
4
5
        test(absolute_value(-17), 17)
6
        test(absolute_value(0), 0)
7
        test(absolute_value(3.14), 3.14)
8
        test(absolute_value(-3.14), 3.14)
9
10
    test suite()
                         # and here is the call to run the tests
```

Here you'll see that we've constructed five tests in our test suite. We could run this against the first or second versions (the correct versions) of absolute_value, and we'd get output similar to the following:

```
Test on line 24 passed.
Test on line 25 passed.
Test on line 26 passed.
Test on line 27 passed.
Test on line 28 passed.
```

But let's say you change the function to an incorrect version like this:

```
def absolute_value(n): # Buggy version
    """ Compute the absolute value of n """
    if n < 0:
        return 1
    elif n > 0:
        return n
```

Can you find at least two mistakes in this code? Running our test suite we get:

```
Test on line 24 passed.
Test on line 25 failed. Expected '17', but got '1'.
Test on line 26 failed. Expected '0', but got 'None'.
Test on line 27 passed.
Test on line 28 failed. Expected '3.14', but got '1'.
```

These are three examples of failing tests.

6.8. Glossary

boolean function

A function that returns a boolean value. The only possible values of the bool type are False and True.

chatterbox function

A function which interacts with the user (using <u>input</u> or <u>print</u>) when it should not. Silent functions that just convert their input arguments into their output results are usually the most useful ones.

composition (of functions)

Calling one function from within the body of another, or using the return value of one function as an argument to the call of another.

dead code

Part of a program that can never be executed, often because it appears after a return statement.

fruitful function

A function that yields a return value instead of None.

incremental development

A program development plan intended to simplify debugging by adding and testing only a small amount of code at a time.

None

A special Python value. One use in Python is that it is returned by functions that do not execute a return statement with a return argument.

return value

The value provided as the result of a function call.

scaffolding

Code that is used during program development to assist with development and debugging. The unit test code that we added in this chapter are examples of scaffolding.

temporary variable

A variable used to store an intermediate value in a complex calculation.

test suite

A collection of tests for some code you have written.

unit testing

An automatic procedure used to validate that individual units of code are working properly.

6.9. Exercises

All of the exercises below should be added to a single file. In that file, you should also add the <u>test</u> and <u>test_suite</u> scaffolding functions shown above, and then, as you work through the exercises, add the new tests to your test suite. (If you open the online version of the textbook, you can easily cut and paste the tests and the fragments of code into your Python editor.)

After completing each exercise, confirm that all the tests pass.

1. The four compass points can be abbreviated by single-letter strings as "N", "E", "S", and "W". Write a function turn_clockwise that takes one of these four compass points as its parameter, and returns the next compass point in the clockwise direction. Here are some tests that should pass:

```
test(turn_clockwise("N"), "E")
test(turn_clockwise("W"), "N")
```

You might ask "What if the argument to the function is some other value?" For all other cases, the function should return the value None:

```
test(turn_clockwise(42), None)
test(turn_clockwise("rubbish"), None)
```

2. Write a function day_name that converts an integer number 0 to 6 into the name of a day. Assume day 0 is "Sunday". Once again, return None if the arguments to the function are not valid. Here are some tests that should pass:

```
test(day_name(3), "Wednesday")
test(day_name(6), "Saturday")
test(day_name(42), None)
```

3. Write the inverse function day_num which is given a day name, and returns its number:

```
test(day_num("Friday"), 5)
test(day_num("Sunday"), 0)
test(day_num(day_name(3)), 3)
test(day_name(day_num("Thursday")), "Thursday")
```

Once again, if this function is given an invalid argument, it should return None:

```
test(day_num("Halloween"), None);
```

4. Write a function that helps answer questions like "Today is Wednesday. I leave on holiday in 19 days time. What day will that be?" So the function must take a day name and a delta argument — the number of days to add — and should return the resulting day name:

```
test(day_add("Monday", 4), "Friday")
test(day_add("Tuesday", 0), "Tuesday")
test(day_add("Tuesday", 14), "Tuesday")
test(day_add("Sunday", 100), "Tuesday")
```

Hint: use the first two functions written above to help you write this one.

5. Can your day_add function already work with negative deltas? For example, -1 would be yesterday, or -7 would be a week ago:

```
test(day_add("Sunday", -1), "Saturday")
test(day_add("Sunday", -7), "Sunday")
test(day_add("Tuesday", -100), "Sunday")
```

If your function already works, explain why. If it does not work, make it work.

Hint: Play with some cases of using the modulus function % (introduced at the beginning of the previous chapter). Specifically, explore what happens to \times % 7 when x is negative.

6. Write a function days_in_month which takes the name of a month, and returns the number of days in the month. Ignore leap years:

```
test(days_in_month("February"), 28)
test(days_in_month("December"), 31)
```

If the function is given invalid arguments, it should return None.

7. Write a function <u>to_secs</u> that converts hours, minutes and seconds to a total number of seconds. Here are some tests that should pass:

```
test(to_secs(2, 30, 10), 9010)
test(to_secs(2, 0, 0), 7200)
test(to_secs(0, 2, 0), 120)
test(to_secs(0, 0, 42), 42)
test(to_secs(0, -10, 10), -590)
```

8. Extend to_secs so that it can cope with real values as inputs. It should always return an integer number of seconds (truncated towards zero):

```
test(to_secs(2.5, 0, 10.71), 9010)
test(to_secs(2.433,0,0), 8758)
```

- 9. Write three functions that are the "inverses" of to_secs:
 - 1. hours_in returns the whole integer number of hours represented by a total number of seconds.
 - 2. <u>minutes_in</u> returns the whole integer number of left over minutes in a total number of seconds, once the hours have been taken out.
 - 3. seconds in returns the left over seconds represented by a total number of seconds.

You may assume that the total number of seconds passed to these functions is an integer. Here

are some test cases:

```
test(hours_in(9010), 2)
test(minutes_in(9010), 30)
test(seconds_in(9010), 10)
```

10. Which of these tests fail? Explain why.

```
test(3 % 4, 0)
test(3 % 4, 3)
test(3 / 4, 0)
test(3 // 4, 0)
test(3+4 * 2, 14)
test(4-2+2, 0)
test(len("hello, world!"), 13)
```

11. Write a compare function that returns 1 if a > b, 0 if a == b, and -1 if a < b

```
test(compare(5, 4), 1)
test(compare(7, 7), 0)
test(compare(2, 3), -1)
test(compare(42, 1), 1)
```

12. Write a function called <u>hypotenuse</u> that returns the length of the hypotenuse of a right triangle given the lengths of the two legs as parameters:

```
test(hypotenuse(3, 4), 5.0)
test(hypotenuse(12, 5), 13.0)
test(hypotenuse(24, 7), 25.0)
test(hypotenuse(9, 12), 15.0)
```

13. Write a function slope(x1, y1, x2, y2) that returns the slope of the line through the points (x1, y1) and (x2, y2). Be sure your implementation of slope can pass the following tests:

```
test(slope(5, 3, 4, 2), 1.0)
test(slope(1, 2, 3, 2), 0.0)
test(slope(1, 2, 3, 3), 0.5)
test(slope(2, 4, 1, 2), 2.0)
```

Then use a call to slope in a new function named intercept(x1, y1, x2, y2) that returns the y-intercept of the line through the points (x1, y1) and (x2, y2)

```
test(intercept(1, 6, 3, 12), 3.0)
test(intercept(6, 1, 1, 6), 7.0)
test(intercept(4, 6, 12, 8), 5.0)
```

14. Write a function called $is_{even(n)}$ that takes an integer as an argument and returns True if the argument is an even number and False if it is odd.

Add your own tests to the test suite.

15. Now write the function $is_odd(n)$ that returns True when n is odd and False otherwise. Include unit tests for this function too.

Finally, modify it so that it uses a call to <u>is_even</u> to determine if its argument is an odd integer, and ensure that its test still pass.

16. Write a function is_factor(f, n) that passes these tests:

```
test(is_factor(3, 12), True)
test(is_factor(5, 12), False)
test(is_factor(7, 14), True)
test(is_factor(7, 15), False)
test(is_factor(1, 15), True)
test(is_factor(15, 15), True)
test(is_factor(25, 15), False)
```

An important role of unit tests is that they can also act as unambiguous "specifications" of what is expected. These test cases answer the question *Do we treat 1 and 15 as factors of 15?*

17. Write is_multiple to satisfy these unit tests:

```
test(is_multiple(12, 3), True)
test(is_multiple(12, 4), True)
test(is_multiple(12, 5), False)
test(is_multiple(12, 6), True)
test(is_multiple(12, 7), False)
```

Can you find a way to use is_factor in your definition of is_multiple?

18. Write the function f2c(t) designed to return the integer value of the nearest degree Celsius for given tempurature in Fahrenheit. (hint: you may want to make use of the built-in function, round. Try printing round. __doc__ in a Python shell or looking up help for the round function, and experimenting with it until you are comfortable with how it works.)

```
test(f2c(212), 100)  # boiling point of water

test(f2c(32), 0)  # freezing point of water

test(f2c(-40), -40)  # Wow, what an interesting case!

test(f2c(36), 2)

test(f2c(37), 3)

test(f2c(38), 3)

test(f2c(39), 4)
```

19. Now do the opposite: write the function c2f which converts Celcius to Fahrenheit:

```
test(c2f(0), 32)
test(c2f(100), 212)
test(c2f(-40), -40)
test(c2f(12), 54)
test(c2f(18), 64)
test(c2f(-48), -54)
```

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7. Iteration

Computers are often used to automate repetitive tasks. Repeating identical or similar tasks without making errors is something that computers do well and people do poorly.

Repeated execution of a set of statements is called iteration. Because iteration is so common, Python provides several language features to make it easier. We've already seen the for statement in chapter 3. This the the form of iteration you'll likely be using most often. But in this chapter we've going to look at the while statement — another way to have your program do iteration, useful in slightly different circumstances.

Before we do that, let's just review a few ideas...

7.1. Reassignment

As we have mentioned previously, it is legal to make more than one assignment to the same variable. A new assignment makes an existing variable refer to a new value (and stop referring to the old value).

```
bruce = 5
print(bruce)
bruce = 7
print(bruce)
```

The output of this program is:

```
7
```

because the first time bruce is printed, its value is 5, and the second time, its value is 7.

Here is what reassignment looks like in a state snapshot:



With reassignment it is especially important to distinguish between an assignment statement and a boolean expression that tests for equality. Because Python uses the equal token (=) for assignment, it is tempting to interpret a statement like a = b as a boolean test. Unlike mathematics, it is not! Remember that the Python token for the equality operator is ==.

Note too that an equality test is symmetric, but assignment is not. For example, if a == 7 then 7 == a. But in Python, the statement a = 7 is legal and 7 = a is not.

Furthermore, in mathematics, a statement of equality is always true. If a == b now, then a will always equal b. In Python, an assignment statement can make two variables equal, but because of the possibility of reassignment, they don't have to stay that way:

```
b = a
         # after executing this line, a and b are now equal
         # after executing this line, a and b are no longer equal
```

The third line changes the value of a but does not change the value of b, so they are no longer equal. (In some programming languages, a different symbol is used for assignment, such as <- or :=, to avoid confusion. Python chose to use the tokens = for assignment, and == for equality. This is a popular choice also found in languages like C, C++, Java, and C#.)

7.2. Updating variables

When an assignment statement is executed, the right-hand-side expression (i.e. the expression that comes after the assignment token) is evaluated first. Then the result of that evaluation is written into the variable on the left hand side, thereby changing it.

One of the most common forms of reassignment is an update, where the new value of the variable depends on its old value.

Line 2 means get the current value of n, multiply it by three and add one, and put the answer back into n as its new value. So after executing the two lines above, n will have the value 16.

If you try to get the value of a variable that doesn't exist yet, you'll get an error:

```
>>> w = x + 1
Traceback (most recent call last):
  File "<interactive input>", line 1, in
NameError: name 'x' is not defined
```

Before you can update a variable, you have to initialize it, usually with a simple assignment:

```
>>> x = 0
>>> x = x + 1
```

This second statement — updating a variable by adding 1 to it — is very common. It is called an increment of the variable; subtracting 1 is called a decrement. Sometimes programmers also talk about bumping a variable, which means the same as incrementing it by 1.

7.3. The for loop revisited

Recall that the <u>for</u> loop processes each item in a list. Each item in turn is (re-)assigned to the loop variable, and the body of the loop is executed. We saw this example in an earlier chapter:

```
for f in ["Joe", "Amy", "Brad", "Angelina", "Zuki", "Thandi", "Paris"]:
    invitation = "Hi " + f + ". Please come to my party on Saturday!"
    print(invitation)
```

Running through all the items in a list is called traversing the list, or traversal.

Let us write a function now to sum up all the elements in a list of numbers. Do this by hand first, and try to isolate exactly what steps you take. You'll find you need to keep some "running total" of the sum so far, either on a piece of paper, or in your head. Remembering things from one step to the next is precisely why we have variables in a program: so we'll need some variable to remember the "running total". It should be initialized with a value of zero, and then we need to traverse the items in the list. For each item, we'll want to update the running total by adding the next number to it.

```
1
     def mysum(xs):
            " Sum all the numbers in the list xs, and return the total. """
2
         running_total = 0
4
         for x in xs:
5
             running_total = running_total + x
         return running_total
8
     #add tests like these to your test suite ...
    test(mysum([1, 2, 3, 4]), 10)
test(mysum([1.25, 2.5, 1.75]), 5.5)
10
11
     test(mysum([1, -2, 3]), 2)
     test(mysum([ ]), 0)
12
     test(mysum(range(11)), 55)
                                    # 11 is not in the list.
```

7.4. The while statement

Here is a fragment of code that demonstrates the use of the while statement:

```
def sum to(n):
2
        """ Return the sum of 1+2+3 ... n """
3
        ss = 0
4
        while v <= n:
5
            ss = ss + v
           v = v + 1
8
        return ss
10
    # for your test suite
11
    test(sum_to(4), 10)
    test(sum_to(1000), 500500)
12
```

You can almost read the while statement as if it were English. It means, While \underline{v} is less than or equal to \underline{n} , continue executing the body of the loop. Within the body, each time, increment \underline{v} . When \underline{v} passes \underline{n} , return your accumulated sum.

More formally, here is precise flow of execution for a while statement:

- 1. Evaluate the condition, yielding False or True.
- 2. If the condition is false, exit the while statement and continue execution at the next statement.
- 3. If the condition is true, execute each of the statements in the body and then go back to step 1.

The body consists of all of the statements below the header with the same indentation.

This type of flow is called a loop because the third step loops back around to the top. Notice that if the condition is false the first time through the loop, the statements inside the loop are never executed.

The body of the loop should change the value of one or more variables so that eventually the condition becomes false and the loop terminates. Otherwise the loop will repeat forever, which is called an infinite loop. An endless source of amusement for computer scientists is the observation that the directions on shampoo, lather, rinse, repeat, are an infinite loop.

In the case here, we can prove that the loop terminates because we know that the value of \underline{n} is finite, and we can see that the value of \underline{v} increments each time through the loop, so eventually it will have to exceed \underline{n} . In other cases, it is not so easy to tell.

What you will notice here is that the while loop is more work for you — the programmer — than the equivalent for loop. When using a while loop one has to control the loop variable yourself: give it an initial value, test for completion, and then make sure you change something in the body so that the loop terminates. By comparison, here is an alternative function that uses for instead:

```
1  def sum_to(n):
2    """ Return the sum of 1+2+3 ... n """
3    ss = 0
4    for v in range(n+1):
5        ss = ss + v
6    return ss
```

Notice the slightly tricky call to the <u>range</u> function — we had to add one onto \underline{n} , because <u>range</u> generates its list up to but not including the value you give it. It would be easy to make a programming mistake and overlook this, but because we've made the investment of writing some unit tests, our test suite would have caught our error.

So why have two kinds of loop if for looks easier? This next example shows a case where we need the extra power that we get from the while loop.

7.5. The 3n + 1 sequence

Let's look at a simple sequence that has fascinated and foxed mathematicians for many years. They still cannot answer even quite simple questions about this.

The "computational rule" for creating the sequence is to start from some given \underline{n} , and to generate the next term of the sequence from \underline{n} , either by halving \underline{n} , (whenever \underline{n} is even), or else by multiplying it by three and adding 1. The sequence terminates when \underline{n} reaches 1.

This Python function captures that algorithm:

```
1
    def seq3np1(n):
2
        """ Print the 3n+1 sequence from n,
        terminating when it reaches 1.
3
4
5
        while n != 1:
            print(n, end=', ')
6
            if n % 2 == 0:
                                # n is even
8
               n = n // 2
9
            else:
                                # n is odd
               n = n * 3 + 1
10
        print(n, end='.\n')
11
```

Notice first that the print function has an extra argument <code>end=', '</code>. This tells the <code>print</code> function to follow the printed string with whatever the programmer chooses (in this case, a comma followed by a space), instead of ending the line. So each time something is printed in the loop, it is printed on the same line, with the output separated by commas. The call to <code>print(n, end='.\n')</code> when the loop terminates will then print the final value of <code>n</code> followed by a period and a newline character. (You'll cover the <code>\n</code> (newline character) in the next chapter).

The condition for this loop is n = 1, so the loop will continue running until n is 1, which will make the condition false.

Each time through the loop, the program outputs the value of \underline{n} and then checks whether it is even or odd. If it is even, the value of \underline{n} is divided by 2 using integer division. If it is odd, the value is replaced by $\underline{n * 3 + 1}$. Here are some examples:

Since \underline{n} sometimes increases and sometimes decreases, there is no obvious proof that \underline{n} will ever reach 1, or that the program terminates. For some particular values of \underline{n} , we can prove termination. For example, if the starting value is a power of two, then the value of \underline{n} will be even each time through the loop until it reaches 1. The previous example ends with such a sequence, starting with 16.

You might like to have some fun and see if you can find a small starting number that needs more than a hundred steps before it terminates.

Particular values aside, the interesting question was first posed by a German mathematician called Lothar Collatz: the Collatz conjecture (also known as the 3n + 1 conjecture, is that this sequence terminates for all positive values of n. So far, no one has been able to prove it or disprove it!

Think carefully about what would be needed for a proof or disproof of the conjecture "All positive integers will eventually converge to 1". With fast computers we have been able to test every integer up to very large values, and so far, they all eventually end up at 1. But this doesn't mean that there might not be some as-yet untested number which does not reduce to 1.

You'll notice that if you don't stop when you reach one the sequence gets into its own loop: 1, 4, 2, 1, 4, 2, 1, 4 ... So another possibility is that there might be other cycles that we just haven't found.

Wikipedia has an informative article about the Collatz conjecture. The sequence also goes under a number of other names (Hailstone sequence, Wonderous numbers, etc.), and you'll find out just how many integers have already been tested by computer, and found to always converge!

```
Choosing between for and while
```

Use a for loop if you know, before you start looping, the maximum number of times that you'll need to execute the body. For example, if you're traversing a list of elements, you know that the maximum number of loop iterations you can possibly need is "all the elements in the list". Or if you need to print the 12 times table, we know right away how many times the loop will need to run.

So any problem like "iterate this weather model for 1000 cycles", or "search this list of words", "find all prime numbers up to 10000" suggest that a for loop is best.

By contrast, if you are required to repeat some computation until some condition is met, and you cannot calculate in advance when this will happen, as we did in this 3n + 1 problem, you'll need a while loop.

We call the first case definite iteration — we have some definite bounds for what is needed. The latter case is called indefinite iteration — we're not sure how many iterations we'll need — we cannot even establish an upper bound!

7.6. Tracing a program

To write effective computer programs a programmer needs to develop the ability to trace the execution of a computer program. Tracing involves becoming the computer and following the flow of execution through a sample program run, recording the state of all variables and any output the program generates after each instruction is executed.

To understand this process, let's trace the call to seq3np1(3) from the previous section. At the start of the trace, we have a local variable, n (the parameter), with an initial value of 3. Since 3 is not equal to 1, the while loop body is executed. 3 is printed and $\frac{3}{2} = 0$ is evaluated. Since it evaluates to False, the else branch is executed and $\frac{3}{2} + 1$ is evaluated and assigned to n.

To keep track of all this as you hand trace a program, make a column heading on a piece of paper for each variable created as the program runs and another one for output. Our trace so far would look something like this:

Since 10 != 1 evaluates to True, the loop body is again executed, and 10 is printed. 10 % 2 == 0 is true, so the if branch is executed and n becomes 5. By the end of the trace we have:

Tracing can be a bit tedious and error prone (that's why we get computers to do this stuff in the first place!), but it is an essential skill for a programmer to have. From this trace we can learn a lot about the way our code works. We can observe that as soon as n becomes a power of 2, for example, the program will require $\log_2(n)$ executions of the loop body to complete. We can also see that the final 1 will not be printed as output within the body of the loop, which is why we put the special print function at the end.

Tracing a program is, of course, related to single-stepping through your code and being able to inspect the variables. Using the computer to single-step for you is less error prone and more convenient. Also, as your programs get more complex, they might execute many millions of steps before they get to the code that you're really interested in, so manual tracing becomes impossible. Being able to set a breakpoint where you need one is far more powerful. So we strongly encourage you to invest time in learning using to use your programming environment (PyScripter, in these notes) to full effect.

There are also some great visualization tools becoming available to help you trace and understand small fragments of Python code. The one we recommend is at http://netserv.ict.ru.ac.za/python3_viz

We've cautioned against chatterbox functions, but used them here. As we learn a bit more Python, we'll be able to show you how to generate a list of values to hold the sequence, rather than having the function print them. Doing

this would remove the need to have all these pesky print functions in the middle of our logic, and will make the function more useful.

7.7. Counting digits

The following function counts the number of decimal digits in a positive integer:

```
def num_digits(n):
    count = 0
    while n != 0:
        count = count + 1
        n = n // 10
    return count
```

A call to print(num_digits(710)) will display 3. Trace the execution of this function call (perhaps using the single step function in PyScripter, or the Python visualizer, or on some paper) to convince yourself that it works.

This function demonstrates an important pattern of computation called a counter. The variable count is initialized
to 0 and then incremented each time the loop body is executed. When the loop exits, count contains the result —
the total number of times the loop body was executed, which is the same as the number of digits.

If we wanted to only count digits that are either 0 or 5, adding a conditional before incrementing the counter will do the trick:

```
def num_zero_and_five_digits(n):
    count = 0
    while n > 0:
        digit = n % 10
        if digit == 0 or digit == 5:
            count = count + 1
        n = n // 10
    return count
```

Confirm that test(num_zero_and_five_digits(1055030250), 7) passes.

Notice, however, that test(num_digits(0), 1) fails. Explain why. Do you think this is a bug in the code, or a bug in the specifications, or our expectations, or the tests?

7.8. Abbreviated assignment

Incrementing a variable is so common that Python provides an abbreviated syntax for it:

```
>>> count = 0
>>> count += 1
>>> count
1
>>> count += 1
>>> count += 1
>>> count
2
```

 $\frac{\text{count } += 1}{\text{out }}$ is an abreviation for $\frac{\text{count } = \text{count } + 1}{\text{count }}$. We pronouce the operator as "plus-equals". The increment value does not have to be 1:

```
>>> n = 2
>>> n += 5
>>> n
7
```

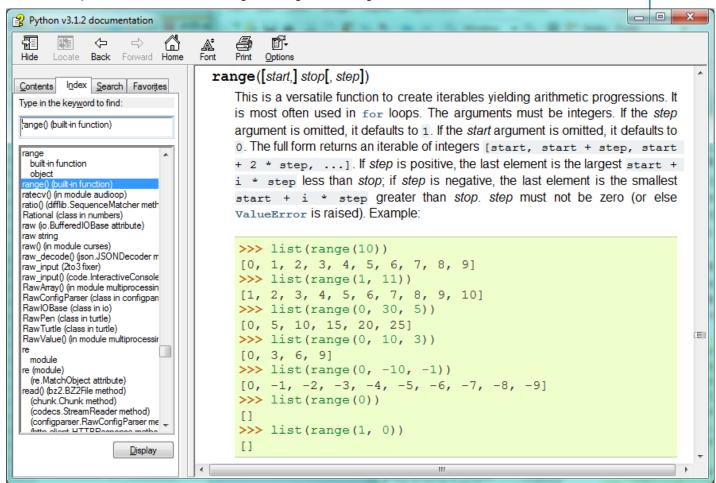
There are similar abbreviations for -=, *=, /=, //= and %=:

```
>>> n = 2
>>> n *= 5
>>> n
10
>>> n -= 4
>>> n
```

```
6
>>> n //= 2
>>> n
3
>>> n %= 2
>>> n
1
```

7.9. Help and meta-notation

Python comes with extensive documentation for all its built-in functions, and its libraries. Different systems have different ways of accessing this help. In PyScripter, click on the *Help* menu item, and select *Python Manuals*. Then search for help on the built-in function range. You'll get something like this...



Notice the square brackets in the description of the arguments. These are examples of meta-notation — notation that describes Python syntax, but is not part of it. The square brackets in this documentation mean that the argument is *optional* — the programmer can omit it. So what this first line of help tells us is that <u>range</u> must always have a <u>stop</u> argument, but it may have an optional <u>start</u> argument (which must be followed by a comma if it is present), and it can also have an optional <u>step</u> argument, preceded by a comma if it is present.

The examples from help show that range can have either 1, 2 or 3 arguments. The list can start at any starting value, and go up or down in increments other than 1. The documentation here also says that the arguments must be integers.

Other meta-notation you'll frequently encounter is the use of bold and italics. The bold means that these are tokens — keywords or symbols — typed into your Python code exactly as they are, whereas the italic terms stand for "something of this type". So the syntax description

for variable in list:

means you can substitute any legal variable and any legal list when you write your Python code.

This (simplified) description of the print function, shows another example of meta-notation in which the ellipses

(...) mean that you can have as many objects as you like (even zero), separated by commas:

```
print( [object, ... ] )
```

Meta-notation gives us a concise and powerful way to describe the pattern of some syntax or feature.

7.10. Tables

One of the things loops are good for is generating tabular data. Before computers were readily available, people had to calculate logarithms, sines and cosines, and other mathematical functions by hand. To make that easier, mathematics books contained long tables listing the values of these functions. Creating the tables was slow and boring, and they tended to be full of errors.

When computers appeared on the scene, one of the initial reactions was, "This is great! We can use the computers to generate the tables, so there will be no errors." That turned out to be true (mostly) but shortsighted. Soon thereafter, computers and calculators were so pervasive that the tables became obsolete.

Well, almost. For some operations, computers use tables of values to get an approximate answer and then perform computations to improve the approximation. In some cases, there have been errors in the underlying tables, most famously in the table the Intel Pentium processor chip used to perform floating-point division.

Although a log table is not as useful as it once was, it still makes a good example of iteration. The following program outputs a sequence of values in the left column and 2 raised to the power of that value in the right column:

```
for x in range(13): # generate numbers 0 to 12
print(x, '\t', 2**x)
```

The string '\t' represents a tab character. The backslash character in '\t' indicates the beginning of an escape sequence. Escape sequences are used to represent invisible characters like tabs and newlines. The sequence \n represents a newline.

An escape sequence can appear anywhere in a string; in this example, the tab escape sequence is the only thing in the string. How do you think you represent a backslash in a string?

As characters and strings are displayed on the screen, an invisible marker called the cursor keeps track of where the next character will go. After a print function, the cursor normally goes to the beginning of the next line.

The tab character shifts the cursor to the right until it reaches one of the tab stops. Tabs are useful for making columns of text line up, as in the output of the previous program:

```
0
         1
1
         2
2
         4
3
         8
4
         16
         32
6
         64
7
         128
8
         256
9
         512
10
         1024
         2048
11
         4096
12
```

Because of the tab characters between the columns, the position of the second column does not depend on the number of digits in the first column.

7.11. Two-dimensional tables

A two-dimensional table is a table where you read the value at the intersection of a row and a column. A multiplication table is a good example. Let's say you want to print a multiplication table for the values from 1 to 6.

A good way to start is to write a loop that prints the multiples of 2, all on one line:

```
for i in range(1, 7):
    print(2 * i, end=' ')
print()
```

Here we've used the range function, but made it start its sequence at 1. As the loop executes, the value of \underline{i} changes from 1 to 6. When all the elements of the range have been assigned to \underline{i} , the loop terminates. Each time through the loop, it displays the value of 2 * i, followed by three spaces.

Again, the extra end=' ' argument in the print function suppresses the newline, and uses three spaces instead. After the loop completes, the second call to print finishes the current line, and starts a new line.

The output of the program is:

```
2 4 6 8 10 12
```

So far, so good. The next step is to encapsulate and generalize.

7.12. Encapsulation and generalization

Encapsulation is the process of wrapping a piece of code in a function, allowing you to take advantage of all the things functions are good for. You have already seen some examples of encapsulation, including <u>is_divisible</u> in a previous chapter.

Generalization means taking something specific, such as printing the multiples of 2, and making it more general, such as printing the multiples of any integer.

This function encapsulates the previous loop and generalizes it to print multiples of n:

```
def print_multiples(n):
    for i in range(1, 7):
        print(n * i, end=' ')
    print()
```

To encapsulate, all we had to do was add the first line, which declares the name of the function and the parameter list. To generalize, all we had to do was replace the value 2 with the parameter n.

If we call this function with the argument 2, we get the same output as before. With the argument 3, the output is:

```
3 6 9 12 15 18
```

With the argument 4, the output is:

```
4 8 12 16 20 24
```

By now you can probably guess how to print a multiplication table — by calling print_multiples repeatedly with different arguments. In fact, we can use another loop:

```
for i in range(1, 7):
    print_multiples(i)
```

Notice how similar this loop is to the one inside <u>print_multiples</u>. All we did was replace the <u>print</u> function with a function call.

The output of this program is a multiplication table:

```
1
        2
                3
                        4
                                5
                                        6
2
                                        12
                        8
                                10
                6
3
                        12
        6
                9
                                15
                                        18
4
        8
                12
                        16
                                20
                                        24
5
        10
                15
                        20
                                25
                                        30
6
                                        36
```

7.13. More encapsulation

To demonstrate encapsulation again, let's take the code from the last section and wrap it up in a function:

```
def print_mult_table():
    for i in range(1, 7):
        print_multiples(i)
```

This process is a common development plan. We develop code by writing lines of code outside any function, or typing them in to the interpreter. When we get the code working, we extract it and wrap it up in a function.

This development plan is particularly useful if you don't know how to divide the program into functions when you start writing. This approach lets you design as you go along.

7.14. Local variables

You might be wondering how we can use the same variable, i, in both print_multiples and print_mult_table.
Doesn't it cause problems when one of the functions changes the value of the variable?

The answer is no, because the i in print_multiples and the i in print_mult_table are not the same variable.

Variables created inside a function definition are local; you can't access a local variable from outside its home function. That means you are free to have multiple variables with the same name as long as they are not in the same function.

Python examines all the statements in a function – if any of them assign a value to a variable, that is the clue that Python uses to make the variable a local variable.

The stack diagram for this program shows that the two variables named \underline{i} are not the same variable. They can refer to different values, and changing one does not affect the other.

```
print_mult_table \begin{bmatrix} & & & 1 \\ & & & & 2 \\ & & & & 3 \end{bmatrix}
print_multiples \begin{bmatrix} & & & & 1 \\ & & & & & 1 \\ & & & & & & 1 \end{bmatrix}
```

The value of \underline{i} in $\underline{print_mult_table}$ goes from 1 to 6. In the diagram it happens to be 3. The next time through the loop it will be 4. Each time through the loop, $\underline{print_mult_table}$ calls $\underline{print_multiples}$ with the current value of \underline{i} as an argument. That value gets assigned to the parameter \underline{n} .

Inside print_multiples, the value of i goes from 1 to 6. In the diagram, it happens to be 2. Changing this variable has no effect on the value of i in print_mult_table.

It is common and perfectly legal to have different local variables with the same name. In particular, names like \underline{i} and \underline{j} are used frequently as loop variables. If you avoid using them in one function just because you used them somewhere else, you will probably make the program harder to read.

The visualizer at http://netserv.ict.ru.ac.za/python3_viz/ shows very clearly how the two variables \underline{i} are distinct variables, and how they have independent values. (The visualizer has a limit of showing 100 steps, though — not quite enough to run this particular example all the way to the end.)

7.15. The break statement

The break statement is used to immediately leave the body of its loop. The next statement to be executed is the first one after the body:

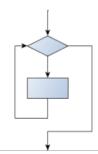
```
for i in [12, 16, 17, 24, 29]:
    if i % 2 == 1: # if the number is odd
        break # immediately exit the loop
print(i)
print("done")
```

This prints:

```
12
16
done
```

he pre-test loop - standard loop behaviour

for and while loops do their tests at the start, before executing any part of the body. They're called pre-test loops, because the test happens before (pre) the body. break and return are our tools for adapting this standard behaviour.



7.16. Other flavours of loops

Sometimes we'd like to have the middle-test loop with the exit test in the middle of the body, rather than at the beginning or at the end. Or a post-test loop that puts its exit test as the last thing in the body. Other languages have different syntax amd keywords for these different flavours, but Python just uses a combination of while and if condition: break to get the job done.

A typical example is a problem where the user has to input numbers to be summed. To indicate that there are no more inputs, the user enters a special value, often the value -1, or the empty string. This needs a middle-exit loop pattern: input the next number, then test whether to exit, or else process the number:



```
total = 0
while True:
    response = input("Enter the next number. (Leave blank to end)")
if response == "":
    break
total += int(response)
print("The total of the numbers you entered is ", total)
```

Convince yourself that this fits the middle-exit loop flowchart: line 3 does some useful work, lines 4 and 5 can exit the loop, and if they don't line 6 does more useful work before the next iteration starts.

The while bool-expr: uses the boolean expression to determine whether to iterate again. True is a trivial boolean expression, so while True: means always do the loop body again. This is a language idiom — a convention that most programmers will recognize immediately. Since the expression on line 2 will never terminate the loop, (it is a dummy test) the programmer must arrange to break (or return) out of the loop body elsewhere, in some other way (i.e. in lines 4 and 5 in this sample). A clever compiler or interpreter will understand that line 2 is a fake test that must always succeed, so it won't even generate a test, and our flowchart never even put the diamond-shape

dummy test box at the top of the loop!

Similarly, by just moving the <u>if condition</u>: <u>break</u> to the end of the loop body we create a pattern for a post-test loop. Post-test loops are used when you want to be sure that the loop body always executes at least once (because the first test only happens at the end of the execution of the first loop body). This is useful, for example, if we want to play an interactive game against the user — we always want to play at least one game:

```
while True:
    play_the_game_once()
    response = input("Play again? (yes or no)")
    if response != "yes":
        break
print("Goodbye!")
```

Hint: think about where you want the exit test to happer

Once you've recognized that you need a loop to repeat something, think about its terminating condition — when will I want to stop iterating? Then figure out whether you need to do the test before starting the first (and every other) iteration, or at the end of the first (and every other) iteration, or perhaps in the middle of each iteration. Iteractive programs that require input from the user or read from files often need to exit their loops in the middle or at the end of an iteration, when it becomes clear that there is no more data to process, or the user doesn't want to play our game anymore.

7.17. An example

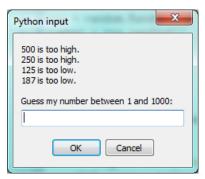
The following program implements a simple guessing game:

```
import random
    rng = random.Random()
                                   # We cover random numbers in chapter 10
2
                                    # so you can peek ahead.
    number = rng.randrange(1, 1000) # Get random number between [1 and 1000).
4
5
    guesses = 0
    msg = ""
6
    while True:
8
9
        guess = int(input(msg + "\nGuess my number between 1 and 1000: "))
10
        guesses += 1
        if guess > number:
11
            msg += str(guess) + " is too high.\n"
12
13
        elif guess < number:</pre>
           msg += str(guess) + " is too low.\n"
14
15
        else:
17
    input("\n\nGreat, you got it in {0} guesses!\n\n" .format(guesses))
```

This program makes use of the mathematical law of trichotomy (given real numbers a and b, exactly one of these three must be true: a > b, a < b, or a == b).

At line 18 there is a call to the input function, but we don't do anything with the result, not even assign it to a variable. This is legal in Python. Here it has the effect of popping up the input dialog window and waiting for the user to respond before the program terminates. Programmers often use the trick of doing some extra input at the end of a script, just to keep the window open.

Also notice the use of the msg variable, initially an empty string, on lines 6, 12 and 14. Each time through the loop we extend the message being displayed: this allows us to display the program's feedback right at the same place as we're asking for the next guess.



7.18. The continue statement

This is a control flow statement that causes the program to immediately skip the processing of the rest of the body of the loop, *for the current iteration*. But the loop still carries on running for its remaining iterations:

```
for i in [12, 16, 17, 24, 29, 30]:
    if i % 2 == 1:  # if the number is odd
        continue  # don't process it
    print(i)
    print("done")
```

This prints:

```
12
16
24
30
done
```

7.19. More generalization

As another example of generalization, imagine you wanted a program that would print a multiplication table of any size, not just the six-by-six table. You could add a parameter to print_mult_table:

```
def print_mult_table(high):
    for i in range(1, high+1):
        print_multiples(i)
```

We replaced the value 1 with the expression high+1. If we call print_mult_table with the argument 7, it displays:

```
1
       2
               3
                      4
                                      6
2
       4
               6
                      8
                              10
                                      12
3
               9
       6
                      12
                              15
                                      18
4
       8
               12
                      16
                              20
                                      24
5
       10
               15
                      20
                              25
                                      30
6
               18
                      24
                              30
                                      36
       12
       14
               21
                      28
                              35
                                      42
```

This is fine, except that we probably want the table to be square — with the same number of rows and columns. To do that, we add another parameter to print_multiples to specify how many columns the table should have.

Just to be annoying, we call this parameter high, demonstrating that different functions can have parameters with the same name (just like local variables). Here's the whole program:

```
def print_multiples(n, high):
    for i in range(1, high+1):
        print(n * i, end=' ')
    print()

def print_mult_table(high):
    for i in range(1, high+1):
        print_multiples(i, high)
```

Notice that when we added a new parameter, we had to change the first line of the function (the function heading), and we also had to change the place where the function is called in print_mult_table.

Now, when we call print_mult_table(7):

```
2
               3
                                               7
1
        4
                       8
                                       12
                                               14
                               10
3
               9
                       12
                                       18
                                               21
        6
                               15
4
        8
               12
                       16
                               20
                                       24
                                               28
5
        10
               15
                       20
                               25
                                       30
                                               35
6
        12
               18
                       24
                               30
                                       36
                                               42
7
                                               49
        14
                21
                        28
                                       42
```

When you generalize a function appropriately, you often get a program with capabilities you didn't plan. For example, you might notice that, because ab = ba, all the entries in the table appear twice. You could save ink by printing only half the table. To do that, you only have to change one line of print_mult_table. Change

```
print_multiples(i, high+1)
```

to

```
print_multiples(i, i+1)
```

and you get:

```
1
       4
3
       6
4
       8
              12
                      16
5
       10
                      20
                              25
               15
6
       12
               18
                      24
                              30
                                     36
                                             49
```

7.20. Functions

A few times now, we have mentioned all the things functions are good for. By now, you might be wondering what exactly those things are. Here are some of them:

- 1. Capturing your mental chunking. Breaking your complex tasks into sub-tasks, and giving the sub-tasks a meaningful name is a powerful mental technique. Look back at the example that illustrated the post-test loop: we assumed that we had a function called play_the_game_once. This chunking allowed us to put aside the details of the particular game is it a card game, or noughts and crosses, or a role playing game and simply focus on one isolated part of our program logic letting the player choose whether they want to play again.
- 2. Dividing a long program into functions allows you to separate parts of the program, debug them in isolation, and then compose them into a whole.
- 3. Functions facilitate the use of iteration.
- 4. Well-designed functions are often useful for many programs. Once you write and debug one, you can reuse it.

7.21. Paired Data

We've already seen lists of names and lists of numbers in Python. We're going to peek ahead in the textbook a little, and show a more advanced way of representing our data. Making a pair of things in Python is as simple as putting them into parentheses, like this:

```
1 year_born = ("Paris Hilton", 1981)
```

We can put many pairs into a list of pairs:

3

```
celebs = [("Brad Pitt", 1963), ("Jack Nicholson", 1937), ("Justin Bieber", 1994)]
```

Here is a quick sample of things we can do with structured data like this. First, print all the celebs:

```
print(celebs)
print(len(celebs))

[('Brad Pitt', 1963), ('Jack Nicholson', 1937), ('Justin Bieber', 1994)]
```

Notice that the celebs list has just 3 elements, each of them pairs.

Now print the names of those celebs born before 1980:

```
for (nm, yr) in celebs:

if yr < 1980:

print(nm)
```

```
Brad Pitt
Jack Nicholson
```

There is a new feature in the <u>for</u> loop: instead of using a single loop control variable, we've put a pair of variable names, <u>nm</u> and <u>yr</u> there instead. The loop is executed three times – once for each pair, and on each iteration both the variables are assigned values from the celeb that is being handled.

7.22. Nested Loops for Nested Data

Now we'll come up with an even more adventurous list of structured data. In this case, we have a list of students. Each student has a name which is paired up with another list of subjects that they are enrolled for:

```
students = [
    ("John", ["CompSci", "Physics"]),
    ("Vusi", ["Maths", "CompSci", "Stats"]),
    ("Jess", ["CompSci", "Accounting", "Economics", "Management"]),
    ("Sarah", ["InfSys", "Accounting", "Economics", "CommLaw"]),
    ("Zuki", ["Sociology", "Economics", "Law", "Stats", "Music"])]
```

Here we've assigned a list of five elements to the variable *students*. Let's print out each student name, and the number of subjects they are enrolled for:

```
# print all students with a count of their courses.
for (name, subjects) in students:
    print(name, "takes", len(subjects), "courses")
```

Python agreeably responds with the following output:

```
John takes 2 courses
Vusi takes 3 courses
Jess takes 4 courses
Sarah takes 4 courses
Zuki takes 5 courses
```

Now we'd like to ask how many students are taking CompSci. This needs a counter, and for each student we need a second loop that tests each of the subjects in turn:

```
# Count how many students are taking CompSci
counter = 0
```

```
The number of students taking CompSci is 3
```

You should set up a list of your own data that interests you — perhaps a list of your CDs, each containing a list of song titles on the CD, or a list of movie titles, each with a list of movie stars who acted in the movie. You could then ask questions like "Which movies starred Angelina Jolie?"

7.23. Newton's method for finding square roots

Loops are often used in programs that compute numerical results by starting with an approximate answer and iteratively improving it.

For example, before we had calculators or computers, people needed to calculate square roots manually. Newton used a particularly good method (there is some evidence that this method was known many years before). Suppose that you want to know the square root of n. If you start with almost any approximation, you can compute a better approximation (closer to the actual answer) with the following formula:

```
better = (approx + n/approx)/2
```

Repeat this calculation a few times using your calculator. Can you see why each iteration brings your estimate a little closer? One of the amazing properties of this particular algorithm is how quickly it converges to an accurate answer — a great advantage for doing it manually.

By using a loop and repeating this formula until the better approximation gets close enough to the previous one, we can write a function for computing the square root. (In fact, this is how your calculator finds square roots — it may have a slightly different formula and method, but it is also based on repeatedly improving its guesses.)

This is an example of an *indefinite* iteration problem: we cannot predict in advance how many times we'll want to improve our guess — we just want to keep getting closer and closer. Our stopping condition for the loop will be when our old guess and our improved guess are "close enough" to each other.

Ideally, we'd like the old and new guess to be exactly equal to each other when we stop. But exact equality is a tricky notion in computer arithmetic when real numbers are involved. Because real numbers are not represented absolutely accurately (after all, a number like pi or the square root of two has an infinite number of decimal places because it is irrational), we need to formulate the stopping test for the loop by asking "is a close enough to b"? This stopping condition can be coded like this:

```
if abs(a-b) < 0.001: # make this smaller for better accuracy break
```

Notice that we take the absolute value of the difference between a and b!

This problem is also a good example of when a middle-exit loop is appropriate:

```
1
     def sqrt(n):
2
        approx = n/2.0
                            # start with some or other auess at the answer
         while True:
             better = (approx + n/approx)/2.0
5
             if abs(approx - better) < 0.001:</pre>
6
                 break;
             approx = better
8
         return better
    # test cases
10
11
    print(sqrt(25.0))
12
     print(sqrt(49.0))
13
    print(sqrt(81.0))
```

The output is:

5.000000000002

7.0

9.0

See if you can improve the approximations by changing the stopping condition. Also, step through the algorithm (perhaps by hand, using your calculator) to see how many iterations were needed before it achieved this level of accuracy for *sqrt(5)*.

7.24. Algorithms

Newton's method is an example of an algorithm: it is a mechanical process for solving a category of problems (in this case, computing square roots).

Some kinds of knowledge are not algorithmic. For example, learning dates from history or your multiplication tables involves memorization of specific solutions.

But the techniques you learned for addition with carrying, subtraction with borrowing, and long division are all algorithms. Or if you are an avid Sudoku puzzle solver, you might have some specific set of steps that you always follow.

One of the characteristics of algorithms is that they do not require any intelligence to carry out. They are mechanical processes in which each step follows from the last according to a simple set of rules. And they're designed to solve a general class or category of problems, not just a single problem.

Understanding that hard problems can be solved by step-by-step algorithmic processes (and having technology to execute these algorithms for us) is one of the major breakthroughs that has had enormous benefits. So while the execution of the algorithm may be boring and may require no intelligence, algorithmic or computational thinking — i.e. using algorithms and automation as the basis for approaching problems — is rapidly transforming our society. Some claim that this shift towards algorithmic thinking and processes is going to have even more impact on our society than the invention of the printing press. And the process of designing algorithms is interesting, intellectually challenging, and a central part of what we call programming.

Some of the things that people do naturally, without difficulty or conscious thought, are the hardest to express algorithmically. Understanding natural language is a good example. We all do it, but so far no one has been able to explain *how* we do it, at least not in the form of a step-by-step mechanical algorithm.

7.25. Glossary

algorithm

A step-by-step process for solving a category of problems.

body

The statements inside a loop.

breakpoint

A place in your program code where program execution will pause (or break), allowing you to inspect the state of the program's variables, or single-step through individual statements, executing them one at a time.

bump

Programmer slang. Synonym for increment.

counter

A variable used to count something, usually initialized to zero and incremented in the body of a loop.

cursor

An invisible marker that keeps track of where the next character will be printed.

decrement

Decrease by 1.

definite iteration

A loop where we have an upper bound on the number of times the body will be executed. Definite iteration is usually best coded as a for loop.

development plan

A process for developing a program. In this chapter, we demonstrated a style of development based on developing code to do simple, specific things and then encapsulating and generalizing.

encapsulate

To divide a large complex program into components (like functions) and isolate the components from each other (by using local variables, for example).

escape sequence

An escape character, \setminus , followed by one or more printable characters used to designate a nonprintable character.

generalize

To replace something unnecessarily specific (like a constant value) with something appropriately general (like a variable or parameter). Generalization makes code more versatile, more likely to be reused, and sometimes even easier to write.

increment

Both as a noun and as a verb, increment means to increase by 1.

infinite loop

A loop in which the terminating condition is never satisfied.

indefinite iteration

A loop where we just need to keep going until some condition is met. A while statement is used for this case.

initialization (of a variable)

To initialize a variable is to give it an initial value. Since in Python variables don't exist until they are assigned values, they are initialized when they are created. In other programming languages this is not the case, and variables can be created without being initialized, in which case they have either default or *garbage* values.

iteration

Repeated execution of a set of programming statements.

loop

A statement or group of statements that execute repeatedly until a terminating condition is satisfied.

loop variable

A variable used as part of the terminating condition of a loop.

meta-notation

Extra symbols or notation that helps describe other notation. Here we introduced square brackets, ellipses, italics, and bold as meta-notation to help describe optional, repeatable, substitutable and fixed parts of the Python syntax.

middle-test loop

A loop that executes some of the body, then tests for the exit condition, and then may execute some more of the body. We don't have a special Python construct for this case, but can use while and break together.

nested loop

A loop inside the body of another loop.

newline

A special character that causes the cursor to move to the beginning of the next line.

post-test loop

A loop that executes the body, then tests for the exit condition. We don't have a special Python construct for this, but can use while and break together.

pre-test loop

A loop that tests before deciding whether the execute its body. for and while are both pre-test loops.

reassignment

Making more than one assignment to the same variable during the execution of a program.

single-step

A mode of interpreter execution where you are able to execute your program one step at a time, and inspect the consequences of that step. Useful for debugging and building your internal mental model of what is going on.

tab

A special character that causes the cursor to move to the next tab stop on the current line.

trichotomy

Given any real numbers a and b, exactly one of the following relations holds: a < b, a > b, or a == b. Thus when you can establish that two of the relations are false, you can assume the remaining one is true.

trace

To follow the flow of execution of a program by hand, recording the change of state of the variables and any output produced.

7.26. Exercises

This chapter showed us how to sum a list of items, and how to count items. The counting example also had an if statement that let us only count some selected items. In the previous chapter we also showed a function find_first_2_letter_word that allowed us an "early exit" from inside a loop by using return when some condition occurred. We now also have break to exit a loop (but not the enclosing function, and continue to abandon the current iteration of the loop without ending the loop.

Composition of list traversal, summing, counting, testing conditions and early exit is a rich collection of building blocks that can be combined in powerful ways to create many functions that are all slightly different.

The first six questions are typical functions you should be able to write using only these building blocks.

- 1. Write a function to count how many odd numbers are in a list.
- 2. Sum up all the even numbers in a list.
- 3. Sum up all the negative numbers in a list.
- 4. Count how many words in a list have length 5.
- 5. Sum all the elements in a list up to but not including the first even number. (Write your unit tests. What if there is no even number?)
- 6. Count how many words occur in a list up to and including the first occurrence of the word "sam". (Write your unit tests for this case too. What if "sam" does not occur?)
- 7. Add a print function to Newton's <u>sqrt</u> function that prints out <u>better</u> each time it is calculated. Call your modified function with 25 as an argument and record the results.
- 8. Trace the execution of the last version of print_mult_table and figure out how it works.
- 9. Write a function print_triangular_numbers(n) that prints out the first n triangular numbers. A call to print_triangular_numbers(5) would produce the following output:

```
1 1
2 3
3 6
4 10
5 15
```

(hint: use a web search to find out what a triangular number is.)

10. Write a function, is_prime, which takes a single integer argument and returns True when the argument is a prime number and False otherwise. Add tests for cases like this:

```
test(is_prime(11), True)
test(is_prime(35), False)
test(is_prime(19911129), True)
```

The last case could represent your birth date. Were you born on a prime day? In a class of 100 students, how

many do you think would have prime birth dates?

- 11. Revisit the drunk student problem from the exercises in chapter 3. This time, the drunk student makes a turn, and then takes some steps forward, and repeats this. Our social science student now records *pairs* of data: the angle of each turn, and the number of steps taken after the turn. Her experimental data is [(160, 20), (-43, 10), (270, 8), (-43, 12)]. Use a turtle to draw the path taken by our drunk friend.
- 12. Many interesting shapes can be drawn by the turtle by giving a list of pairs like we did above, where the first item of the pair is the angle to turn, and the second item is the distance to move forward. Set up a list of pairs so that the turtle draws a house with a cross through the centre, as show here. This should be done without going over any of the lines / edges more than once, and without lifting your pen.



13. Not all shapes like the one above can be drawn without lifting your pen, or going over an edge more than once. Which of these can be drawn?



Now read Wikipedia's article(http://en.wikipedia.org/wiki/Eulerian_path) about Eulerian paths. Learn how to tell immediately by inspection whether it is possible to find a solution or not. If the path is possible, you'll also know where to put your pen to start drawing, and where you should end up!

14. What will num_digits(0">num_digits(-24) result in an infinite loop? (hint: -1//10 evaluates to -1) Modify num_digits so that it works correctly with any integer value. Add these tests:

```
test(num_digits(0), 1)
test(num_digits(-12345), 5)
```

15. Write a function num_even_digits(n) that counts the number of even digits in n. These tests should pass:

```
test(num_even_digits(123456), 3)
test(num_even_digits(2468), 4)
test(num_even_digits(1357), 0)
test(num_even_digits(0), 1)
```

16. Write a function sum_of_squares(xs) that computes the sum of the squares of the numbers in the list xs. For example, sum_of_squares([2, 3, 4]) should return 4+9+16 which is 29:

```
test(sum_of_squares([2, 3, 4]), 29)
test(sum_of_squares([]), 0)
test(sum_of_squares([2, -3, 4]), 29)
```

17. You and your friend are in a team to write a two-player game, human against computer, such as Tic-Tac-Toe / Noughts and Crosses. Your friend will write the logic to play one round of the game, while you will write the logic to allow many rounds of play, keep score, decide who plays, first, etc. The two of you negotiate on how the two parts of the program will fit together, and you come up with this simple scaffolding (which your friend will improve later):

```
# your friend will complete this function

def play_once(human_plays_first):

"""

Must play one round of the game. If the parameter
is True, the human gets to play first, else the
computer gets to play first. When the round ends,
```

```
the return value of the function is one of
8
           -1 (human wins), 0 (game drawn), 1 (computer wins).
9
10
        # This is all dummy scaffolding code right at the moment...
                                       # see ch 10 for details
11
        import random
12
        rng = random.Random()
13
        # pick a random result between -1 and 1.
14
        result = rng.randrange(-1,2)
        print("Human plays first={0}, winner={1} "
15
16
                           .format(human_plays_first, result))
17
        return result
```

- a. Write the main program which repeatedly calls this function to play the game, and after each round it announces the outcome as "I win!", "You win!", or "Game drawn!". It then asks the player "Do you want to play again?" and either plays again, or says "Goodbye", and terminates.
- b. Keep score of how many wins each player has had, and how many draws there have been. After each round of play, also announce the scores.
- c. Add logic so that the players take turns to play first.
- d. Compute the percentage of wins for the human, out of all games played. Also announce this at the end of each round.
- e. Draw a flowchart of your logic.

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8. Strings

8.1. A compound data type

So far we have seen built-in types like int, float, bool, str and we've seen lists and pairs. Strings, lists, and pairs are qualitatively different from the others because they are made up of smaller pieces. In the case of strings, they're made up of smaller strings each containing one character.

Types that comprise smaller pieces are called compound data types. Depending on what we are doing, we may want to treat a compound data type as a single thing, or we may want to access its parts. This ambiguity is useful.

8.2. Working with strings as single things

We previously saw that each turtle instance has its own attributes and a number of methods that can be applied to the instance. For example, we could set the turtle's color, and we wrote tess.turn(90).

Just like a turtle, a strings is also an object. So each string instance has its own attributes and methods.

For example:

```
>>> ss = "Hello, World!"
>>> tt = ss.upper()
>>> tt
'HELLO, WORLD!'
```

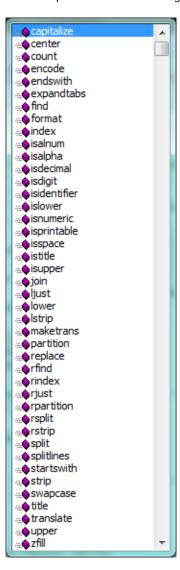
upper is a method that can be invoked on any string object to create a new string, in which all the characters are in uppercase. (The original string ss remains unchanged.)

There are also methods like *Lower*, *capitalize*, and *swapcase* that do other interesting stuff.

To learn what methods are available, you can consult the Help documentation, look for the string module, and read the documentation. Or, if you're a bit lazier, simply type the following into a PyScripter script:

```
1 ss = "Hello, World!"
2 tt = ss.
```

When you type the period to select one of the methods of ss, PyScripter will pop up a selection window showing all the methods (there are around 70 of them — thank goodness we'll only use a few of those!) that could be used on your string.



When you type the name of the method, some further help about it's parameter and return type, and its docstring, will be displayed. This is a good example of a tool — PyScripter — using the meta-information — the docstrings — provided by the module programmers.

8.3. Working with the parts of a string

The indexing operator (Python uses square brackets to enclose the index) selects a single character substring from a string:

```
>>> fruit = "banana"
>>> m = fruit[1]
>>> print(m)
```

The expression fruit[1] selects character number 1 from fruit, and creates a new string containing just this one character. The variable m refers to the result. When we display m, we could get a surprise:

```
a
```

Computer scientists always start counting from zero! The letter at subscript position zero of "banana" is b. So at position [1] we have the letter a.

If you want the zero-eth letter of a string, you just put 0, or any expression with the value 0, in the brackets:

```
>>> m = fruit[0]
>>> print(m)
b
```

The expression in brackets is called an index. An index specifies a member of an ordered collection, in this case the collection of characters in the string. The index *indicates* which one you want, hence the name. It can be any integer expression.

Note that indexing returns a *string* — Python has no special type for a single character. It is just a string of length 1.

We've also seen lists previously. The same indexing notation works to extract elements from a list:

```
>>> prime_nums = [2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31]
>>> prime_nums[4]
11
>>> friends = ["Joe", "Amy", "Brad", "Angelina", "Zuki", "Thandi", "Paris"]
>>> friends[3]
'Angelina'
```

8.4. Length

The 1en function, when applied to a string, returns the number of characters in a string:

```
>>> fruit = "banana"
>>> len(fruit)
6
```

To get the last letter of a string, you might be tempted to try something like this:

```
sz = len(fruit)
last = fruit[sz] # ERROR!
```

That won't work. It causes the runtime error IndexError: string index out of range. The reason is that there is no letter at index position 6 in "banana". Since we started counting at zero, the six indexes are numbered 0 to 5. To get the last character, we have to subtract 1 from <u>length</u>:

```
sz = len(fruit)
last = fruit[sz-1]
```

Alternatively, we can use negative indices, which count backward from the end of the string. The expression fruit[-1] yields the last letter, fruit[-2] yields the second to last, and so on.

As you might have guessed, indexing with a negative index also works like this for lists.

We won't use negative indexes in the rest of these notes — not many computer languages use this idiom, and you'll probably be better off avoiding it. But there is plenty of Python code out on the Internet that will use this trick, so it is best to know that it exists.

8.5. Traversal and the for loop

A lot of computations involve processing a string one character at a time. Often they start at the beginning, select each character in turn, do something to it, and continue until the end. This pattern of processing is called a traversal. One way to encode a traversal is with a while statement:

```
ix = 0
while ix < len(fruit):
    letter = fruit[ix]
print(letter)
ix += 1</pre>
```

This loop traverses the string and displays each letter on a line by itself. The loop condition is ix < len(fruit), so when ix is equal to the length of the string, the condition is false, and the body of the loop is not executed. The last character accessed is the one with the index len(fruit)-1, which is the last character in the string.

But we've previously seen how the for loop can easily iterate over lists: for also works for strings:

```
for c in fruit:
print(c)
```

Each time through the loop, the next character in the string is assigned to the variable c. The loop continues until no characters are left.

The following example shows how to use concatenation and a <u>for</u> loop to generate an abecedarian series. Abecedarian refers to a series or list in which the elements appear in alphabetical order. For example, in Robert McCloskey's book *Make Way for Ducklings*, the names of the ducklings are Jack, Kack, Lack, Mack, Nack, Ouack, Pack, and Quack. This loop outputs these names in order:

```
prefixes = "JKLMNOPQ"
suffix = "ack"

for p in prefixes:
    print(p + suffix)
```

The output of this program is:

```
Jack
Kack
Lack
Mack
Nack
Oack
Pack
Qack
```

Of course, that's not quite right because Ouack and Quack are misspelled. You'll fix this as an exercise below.

8.6. Slices

A *substring* of a string is obtained by taking a slice. Similarly, we can slice a list to refer to some sublist of the items in the list:

```
>>> s = "Peter, Paul, and Mary"
>>> print(s[0:5])
Peter
>>> print(s[7:11])
Paul
>>> print(s[17:21])
Mary
>>> friends = ["Joe", "Amy", "Brad", "Angelina", "Zuki", "Thandi", "Paris"]
>>> print(friends[2:4])
['Brad', 'Angelina']
```

The operator [n:m] returns the part of the string from the n'th character to the m'th character, including the first but excluding the last. This behavior makes sense if you imagine the indices pointing *between* the characters, as in the following diagram:

```
fruit --> " b a n a n a "
```

Now if you imagine this as a piece of paper, the slice operator [n:m] cuts the paper at the n and m positions.

Two tricks are added to this: if you omit the first index (before the colon), the slice starts at the beginning of the string (or list). If you omit the second index, the slice extends to the end of the string (or list). Thus:

```
>>> fruit = "banana"
>>> fruit[:3]
'ban'
>>> fruit[3:]
'ana'
```

What do you think s[:] means? What about friends[4:]?

8.7. String comparison

The comparison operators work on strings. To see if two strings are equal:

```
if word == "banana":
    print("Yes, we have no bananas!")
```

Other comparison operations are useful for putting words in Lexicographical order:

```
if word < "banana":
    print("Your word, " + word + ", comes before banana.")</pre>
```

```
elif word > "banana":
    print("Your word, " + word + ", comes after banana.")
else:
    print("Yes, we have no bananas!")
```

This is similar to the alphabetical order you would use with a dictionary, except that all the uppercase letters come before all the lowercase letters. As a result:

```
Your word, Zebra, comes before banana.
```

A common way to address this problem is to convert strings to a standard format, such as all lowercase, before performing the comparison. A more difficult problem is making the program realize that zebras are not fruit.

8.8. Strings are immutable

It is tempting to use the [] operator on the left side of an assignment, with the intention of changing a character in a string. For example:

```
greeting = "Hello, world!"
greeting[0] = 'J' # ERROR!
print(greeting)
```

Instead of producing the output <code>Jello</code>, <code>world!</code>, this code produces the runtime error <code>TypeError: 'str'</code> object does not support item assignment.

Strings are immutable, which means you can't change an existing string. The best you can do is create a new string that is a variation on the original:

```
greeting = "Hello, world!"
newGreeting = 'J' + greeting[1:]
print(newGreeting)
```

The solution here is to concatenate a new first letter onto a slice of greeting. This operation has no effect on the original string.

8.9. The in and not in operators

The in operator tests if one string is a substring of another:

```
>>> 'p' in 'apple'
True
>>> 'i' in 'apple'
False
>>> 'ap' in 'apple'
True
>>> 'pa' in 'apple'
False
```

Note that a string is a substring of itself, and the empty string is a substring of any other string. (Also note that computer scientists like to think about these edge cases quite carefully!)

```
>>> 'a' in 'a'
True
>>> 'apple' in 'apple'
True
>>> '' in 'a'
True
>>> '' in 'apple'
True
```

The not in operator returns the logical opposite results of in:

```
>>> 'x' not in 'apple'
True
```

Combining the \underline{in} operator with string concatenation using $\underline{+}$, we can write a function that removes all the vowels from a string:

```
1
    def remove vowels(s):
     vowels = "aeiouAEIOU"
2
3
       s_without_vowels = ""
4
       for x in s:
5
            if x not in vowels:
6
                s_without_vowels += x
7
        return s_without_vowels
8
9
    test(remove_vowels("compsci"), "cmpsc")
    test(remove_vowels("aAbEefIijOopUus"), "bfjps")
10
```

8.10. A find function

What does the following function do?

```
def find(strng, ch):
 1
 2
 3
             Find and return the index of ch in strng.
 4
             Return -1 if ch does not occur in strng.
 5
 6
           ix = 0
 7
         while ix < len(strng):</pre>
 8
              if strng[ix] == ch:
 9
                     return ix
10
                ix += 1
11
           return -1
12
      test(find("Compsci", "p"), 3)
test(find("Compsci", "C"), 0)
test(find("Compsci", "i"), 6)
test(find("Compsci", "x"), -1)
13
14
15
```

In a sense, <u>find</u> is the opposite of the indexing operator. Instead of taking an index and extracting the corresponding character, it takes a character and finds the index where that character appears. If the character is not found, the function returns -1.

This is another example where we see a return statement inside a loop. If strng[ix] == ch, the

function returns immediately, breaking out of the loop prematurely.

If the character doesn't appear in the string, then the program exits the loop normally and returns -1.

This pattern of computation is sometimes called a *eureka traversal* or "short-circuit evaluation", because as soon as we find what we are looking for, we can cry "Eureka!", take the short-circuit, and stop looking.

8.11. Looping and counting

The following program counts the number of times the letter a appears in a string, and is another example of the counter pattern introduced in <u>Counting digits</u>:

```
def count_a(text):
    count = 0
    for c in text:
        if c == 'a':
            count += 1
    return(count)

test(count_a("banana"), 3)
```

8.12. Optional parameters

To find the locations of the second or third occurrence of a character in a string, we can modify the find function, adding a third parameter for the starting postion in the search string:

```
1
    def find2(strng, ch, start):
2
       ix = start
3
        while ix < len(strng):</pre>
4
           if strng[ix] == ch:
5
                return ix
6
            ix += 1
7
        return -1
8
    test(find2('banana', 'a', 2), 3)
```

The call find2('banana', 'a', 2) now returns 3, the index of the first occurrence of 'a' in 'banana' after index 2. What does find2('banana', 'n', 3) return? If you said, 4, there is a good chance you understand how find2 works.

Better still, we can combine find and find2 using an optional parameter:

```
def find(strng, ch, start=0):
    ix = start
    while ix < len(strng):
        if strng[ix] == ch:
            return ix
        ix += 1
    return -1</pre>
```

When a function has an optional parameter, the caller may provide a matching argument. If the third

argument is provided to find, it gets assigned to start. But if the caller leaves the argument out, then start is given a default value indicated by the assignment start=0 in the function definition.

So the call find('banana', 'a', 2) to this version of find behaves just like find2, while in the call find('banana', 'a'), start will be set to the default value of 0.

Adding another optional parameter to <u>find</u> makes it search from a starting position, up to but not including the end position:

```
def find(strng, ch, start=0, end=None):
1
2
        ix = start
3
        if end == None:
           end = len(strng)
4
5
        while ix < end:</pre>
           if strng[ix] == ch:
6
7
                return ix
8
            ix += 1
        return -1
```

The optional value for end is interesting: we give it a default value None if the caller does not supply any argument. In the body of the function we test what end is, and if the caller did not supply any argument, we reassign end to be the length of the string. If the caller has supplied an argument for end, however, the caller's value will be used in the loop.

The semantics of start and end in this function are precisely the same as they are in the range function.

Here are some test cases that should pass:

```
ss = "Python strings have some interesting methods."
test(find(ss, 's'), 7)
test(find(ss, 's', 7), 7)
test(find(ss, 's', 8), 13)
test(find(ss, 's', 8, 13), -1)
test(find(ss, '.'), len(ss)-1)
```

8.13. The built-in find method

Now that we've done all this work to write a powerful find function, we can let on that strings already have their own built-in``find`` method. It can do everything that our one can do, and more!

```
test(ss.find('s'), 7)
test(ss.find('s', 7), 7)
test(ss.find('s', 8), 13)
test(ss.find('s', 8, 13), -1)
test(ss.find('.'), len(ss)-1)
```

The built-in find method is more general than our version. It can find substrings, not just single characters:

```
>>> "banana".find("nan")
2
```

```
>>> "banana".find("na", 3)
4
```

Usually we'd prefer to use the methods that Python provides rather than reinvent our own equivalents. But many of the built-in functions and methods make good teaching exercises, and the underlying techniques you learn are your building blocks to becoming a proficient programmer.

8.14. The split method

One of the most useful methods on strings is the split method: it splits a single multi-word string into a list of individual words, removing all the whitespace between them. (Whitespace means any tabs, newlines, or spaces.) This allows us to read input as a single string, and split it into words.

```
>>> ss = 'Well I never did said Alice'
>>> wds = ss.split()
>>> wds
['Well', 'I', 'never', 'did', 'said', 'Alice']
```

8.15. Cleaning up your strings

We'll often work with strings that contain punctuation, or tab and newline characters, especially, as we'll see in a future chapter, when we read our text from files or from the Internet. But if we're writing a program, say, to count word frequencies or check the spelling of each word, we'd prefer to strip off these unwanted characters.

We'll show just one example of how to strip punctuation from a string. Remember that strings are immutable, so we cannot change the string with the punctuation — we need to traverse the original string and create a new string, omitting any punctuation:

Setting up that first assignment is messy and error-prone. Fortunately, the Python string module already does it for us. So we will make a slight improvement to this program — we'll import the string module and use its definition:

```
import string
 1
 2
 3
     def remove_punctuation(s):
 4
       s without punct =
 5
       for letter in s:
            if letter not in string.punctuation:
 7
                s without punct += letter
 8
        return s_without_punct
9
     test(remove_punctuation('"Well, I never did!", said Alice.'),
10
                                "Well I never did said Alice")
11
     test(remove_punctuation("Are you very, very, sure?"),
12
```

```
13 "Are you very very sure")
```

Composing together this function and the split method from the previous section makes a useful combination — we'll clean out the punctuation, and split will clean out the newlines and tabs while turning the string into a list of words:

```
my story = '''
1
    Pythons are constrictors, which means that they will 'squeeze' the life
3
    out of their prey. They coil themselves around their prey and with
4
    each breath the creature takes the snake will squeeze a little tighter
    until they stop breathing completely. Once the heart stops the prey
5
    is swallowed whole. The entire animal is digested in the snake's
7
    stomach except for fur or feathers. What do you think happens to the fur,
8
    feathers, beaks, and eggshells? The 'extra stuff' gets passed out as ---
    you guessed it --- snake POOP! '''
9
10
11
    wds = remove_punctuation(my_story).split()
12
    print(wds)
```

The output:

```
['Pythons', 'are', 'constrictors', ..., 'it', 'snake', 'POOP']
```

There are other useful functions in the string module, other ways to classify characters, and other methods on string instances, but this book isn't intended to be a reference manual. On the other hand, the *Python Library Reference* is. Along with a wealth of other documentation, it's available from the Python website, http://www.python.org.

8.16. The format method for strings

The easiest and most powerful way to format a string in Python 3 is to use the *format* method. To see how this works, let's start with a few examples:

```
s1 = "His name is {0}!".format("Arthur")
1
2
     print(s1)
3
     name = "Alice"
4
5
     s2 = "I am {0} and I am {1} years old.".format(name, age)
7
     print(s2)
8
9
     n1 = 4
10
     n2 = 5
     s3 = "2**10 = \{0\} \text{ and } \{1\} * \{2\} = \{3:f\}".format(2**10, n1, n2, n1 * n2)
11
12
     print(s3)
```

Running the script produces:

```
His name is Arthur!
I am Alice and I am 10 years old.
2**10 = 1024 and 4 * 5 = 20.000000
```

The key idea is that one provides a formatter string which contains placeholder fields, ... {0} ...

{1} ... {2} ... etc. The format method of a string uses the numbers as indexes into its arguments, and substitutes the appropriate argument into each placeholder field.

Each of the placeholders can also contain a format specification — it is always introduced by the symbol. This can control things like

- whether the field is aligned left <, centered ^, or right >
- the width allocated to the field within the result string (a number like 10)
- the type of conversion (we'll initially only force conversion to float, f, as we did in line 11 of the code above, or perhaps we'll ask integer numbers to be converted to hexadecimal using x)
- if the type conversion is a float, you can also specify how many decimal places are wanted (typically, .2f is useful for working with currencies to two decimal places.)

Let's do a few simple and common examples that should be enough for most needs. If you need to do anything more esoteric, use *help* and read all the gory details.

```
n1 = "Paris"
1
    n2 = "Whitney"
2
3
    n3 = "Hilton"
4
5
    print("Ppi to three decimal places is {0:.3f}".format(3.1415926))
    print("123456789 123456789 123456789 123456789 123456789 123456789")
7
    print("|||{0:<15}|||{1:^15}|||{2:>15}|||Born in {3}|||"
                                                .format(n1,n2,n3,1981))
    print("The decimal value {0} converts to hex value {0:x}"
9
10
                                                .format(123456))
```

This script produces the output:

```
The value of pi to three decimal places is 3.142
123456789 123456789 123456789 123456789
|||Paris ||| Whitney ||| Hilton|||Born in 1981|||
The decimal value 123456 converts to hex value 1e240
```

You can have multiple placeholders indexing the same argument, or perhaps even have extra arguments that are not referenced at all:

```
letter = '''
Dear {0} {2}.
  {0}, I have an interesting money-making proposition for you!
If you deposit $10 million into my bank account, I can
double your money ...
'''
print(letter.format("Paris", "Whitney", "Hilton"))
print(letter.format("Bill", "Henry", "Gates"))
```

This produces the following:

```
Dear Paris Hilton.
Paris, I have an interesting money-making proposition for you!
If you deposit $10 million into my bank account, I can double your money ...

Dear Bill Gates.
```

```
Bill, I have an interesting money-making proposition for you! If you deposit $10 million into my bank account I can, double your money ...
```

As you might expect, you'll get an index error if your placeholders refer to arguments that you do not provide:

```
>>> "hello {3}".format("Dave")
Traceback (most recent call last):
  File "<interactive input>", line 1, in <module>
IndexError: tuple index out of range
```

The following example illustrates the real utility of string formatting. First, we'll try to print a table without using string formatting:

This program prints out a table of various powers of the numbers from 1 to 10. (This assumes that the tab width is 8. You might see something even worse than this if you tab width is set to 4.) In its current form it relies on the tab character (\t) to align the columns of values, but this breaks down when the values in the table get larger than the tab width:

```
i**2
              i**3
                     i**5
                           i**10 i**20
i
             1
1
      1
                     1
                           1
                                  1
2
       4
              8
                     32
                           1024
                                  1048576
3
      9
             27
                     243
                          59049 3486784401
                    1024 1048576 1099511627776
4
      16
             64
5
             125
                     3125 9765625
                                         95367431640625
6
      36
             216
                    7776
                           60466176
                                        3656158440062976
7
      49
             343
                    16807
                           282475249
                                         79792266297612001
8
      64
             512
                     32768
                           1073741824
                                        1152921504606846976
9
      81
             729
                     59049
                            3486784401
                                          12157665459056928801
                     100000 10000000000
                                          10000000000000000000000
10
      100
              1000
```

One possible solution would be to change the tab width, but the first column already has more space than it needs. The best solution would be to set the width of each column independently. As you may have guessed by now, string formatting provides a much nicer solution. We can also right-justify each field:

```
layout = "{0:>4}{1:>6}{2:>6}{3:>8}{4:>13}{5:>24}"

print(layout.format('i', 'i**2', 'i**3', 'i**5', 'i**10', 'i**20'))
for i in range(1, 11):
    print(layout.format(i, i**2, i**3, i**5, i**10, i**20))
```

Running this version produces the following (much more satisfying) output:

```
i**2 i**3
                 i**5
                             i**10
                                                    i**20
i
1
     1
          1
                  1
                               1
                                                        1
2
     4
           8
                  32
                             1024
                                                  1048576
3
     9
          27
                 243
                             59049
                                               3486784401
```

4 16 64 1024 1048576 1099511627776 5 25 125 3125 9765625 95367431640625 6 36 216 7776 60466176 3656158440062976 7 49 343 16807 282475249 79792266297612001 8 64 512 32768 1073741824 1152921504606846976 9 81 729 59049 3486784401 12157665459056928801 10 100 1000 1000000 1000000000000000000000000000000000000						
6 36 216 7776 60466176 3656158440062976 7 49 343 16807 282475249 79792266297612001 8 64 512 32768 1073741824 1152921504606846976 9 81 729 59049 3486784401 12157665459056928801	4	16	64	1024	1048576	1099511627776
7 49 343 16807 282475249 79792266297612001 8 64 512 32768 1073741824 1152921504606846976 9 81 729 59049 3486784401 12157665459056928801	5	25	125	3125	9765625	95367431640625
8 64 512 32768 1073741824 1152921504606846976 9 81 729 59049 3486784401 12157665459056928801	6	36	216	7776	60466176	3656158440062976
9 81 729 59049 3486784401 12157665459056928801	7	49	343	16807	282475249	79792266297612001
	8	64	512	32768	1073741824	1152921504606846976
10 100 1000 100000 10000000000 100000000	9	81	729	59049	3486784401	12157665459056928801
	10	100	1000	100000	10000000000	1000000000000000000000

8.17. Summary

This chapter introduced a lot of new ideas. The following summary may prove helpful in remembering what you learned.

indexing ([])

Access a single character in a string using its position (starting from 0). Example: 'This'[2] evaluates to 'i'.

length function (len)

Returns the number of characters in a string. Example: len('happy') evaluates to 5.

for loop traversal (for)

Traversing a string means accessing each character in the string, one at a time. For example, the following for loop:

```
for ix in 'Example':
    ...
```

executes the body of the loop 7 times with different values of ix each time.

slicing ([:])

A *slice* is a substring of a string. Example: 'bananas and cream'[3:6] evaluates to ana (so does 'bananas and cream'[1:4]).

```
string comparison (>, <, >=, <=, ==, !=)
```

The six common comparision operators work with strings, evaluating according to <code>Lexicographical</code> order. Examples: <code>'apple' < 'banana'</code> evaluates to <code>True</code>. <code>'Zeta' < 'Appricot'</code> evaluates to <code>False</code>. <code>'Zebra' <= 'aardvark'</code> evaluates to <code>True</code> because all upper case letters precede lower case letters.

in and not in operator (in, not in)

The in operator tests whether one string is contained inside another string. Examples: 'heck' in "I'll be checking for you." evaluates to True. 'cheese' in "I'll be checking for you." evaluates to False.

8.18. Glossary

compound data type

A data type in which the values are made up of components, or elements, that are themselves values.

default value

The value given to an optional parameter if no argument for it is provided in the function call.

docstring

A string constant on the first line of a function or module definition (and as we will see later, in class and method definitions as well). Docstrings provide a convinient way to associate documentation with code. Docstrings are also used by programming tools to provide interactive help.

dot notation

Use of the dot operator, ., to access methods and attributes of an object.

immutable

A compound data type whose elements can not be assigned new values.

index

A variable or value used to select a member of an ordered collection, such as a character from a string, or an element from a list.

optional parameter

A parameter written in a function header with an assignment to a default value which it will receive if no corresponding argument is given for it in the function call.

short-circuit evaluation

A style of programming that shortcuts extra work as soon as the outcome is know with certainty. In this chapter our <u>find</u> function returned as soon as it found what it was looking for: it didn't traverse all the rest of the items in the string.

slice

A part of a string (substring) specified by a range of indices. More generally, a subsequence of any sequence type in Python can be created using the slice operator (sequence[start:stop]).

traverse

To iterate through the elements of a collection, performing a similar operation on each.

whitespace

Any of the characters that move the cursor without printing visible characters. The constant string.whitespace contains all the white-space characters.

8.19. Exercises

We suggest you create a single file containing the test scaffolding from our previous chapters, and put all functions that require tests into that file.

1. What is the result of each of the following:

```
>>> 'Python'[1]
>>> "Strings are sequences of characters."[5]
>>> len("wonderful")
>>> 'Mystery'[:4]
>>> 'p' in 'Pineapple'
>>> 'apple' in 'Pineapple'
>>> 'pear' not in 'Pineapple'
>>> 'apple' > 'pineapple'
>>> 'pineapple' < 'Peach'</pre>
```

2. Modify:

```
prefixes = "JKLMNOPQ"
suffix = "ack"

for letter in prefixes:
    print(letter + suffix)
```

so that Ouack and Quack are spelled correctly.

3. Encapsulate

```
fruit = "banana"
count = 0
for char in fruit:
    if char == 'a':
        count += 1
print(count)
```

in a function named count_letters, and generalize it so that it accepts the string and the letter
as arguments. Make the function return the number of characters, rather than print the answer.
The caller should do the printing.

- 4. Now rewrite the <u>count_letters</u> function so that instead of traversing the string, it repeatedly calls the <u>find</u> method, with the optional third parameter to locate new occurences of the letter being counted.
- 5. Assign to a variable in your program a triple-quoted string that contains your favourite paragraph of text perhaps a poem, a speech, instructions to bake a cake, some inspirational verses, etc.

Write a function which removes all punctuation from the string, breaks the string into a list of words, and counts the number of words in your text that contain the letter 'e'. Your program should print an analysis of the text like this:

```
Your text contains 243 words, of which 109 (44.8%) contain an 'e'.
```

- 6. Print out a neatly formatted multiplication table, up to 12×12 .
- 7. Write a function that reverses its string argument, and satisfies these tests:

```
test(reverse('happy'), 'yppah')
test(reverse('Python'), 'nohtyP')
test(reverse(''), '')
test(reverse('a'), 'a')
```

8. Write a function that mirrors its argument:

```
test(mirror('good'), 'gooddoog')
test(mirror('Python'), 'PythonnohtyP')
test(mirror(''), '')
test(mirror('a'), 'aa')
```

9. Write a function that removes all occurrences of a given letter from a string:

```
test(remove_letter('a', 'apple'), 'pple')
test(remove_letter('a', 'banana'), 'bnn')
test(remove_letter('z', 'banana'), 'banana')
test(remove_letter('i', 'Mississippi'), 'Msssspp')
test(remove_letter('b', ''), '')
test(remove_letter('b', 'c'), 'c')
```

10. Write a function that recognizes palindromes. (Hint: use your <u>reverse</u> function to make this easy!):

```
test(is_palindrome('abba'), True)
test(is_palindrome('abab'), False)
test(is_palindrome('tenet'), True)
test(is_palindrome('banana'), False)
test(is_palindrome('straw warts'), True)
test(is_palindrome('a'), True)
#test(is_palindrome(''), ??) # Is an empty string a palindrome?
```

11. Write a function that counts how many times a substring occurs in a string:

```
test(count('is', 'Mississippi'), 2)
test(count('an', 'banana'), 2)
test(count('ana', 'banana'), 2)
test(count('nana', 'banana'), 1)
test(count('nanan', 'banana'), 0)
test(count('aaa', 'aaaaaa'), 4)
```

12. Write a function that removes the first occurrence of a string from another string:

```
test(remove('an', 'banana'), 'bana')
test(remove('cyc', 'bicycle'), 'bile')
test(remove('iss', 'Mississippi'), 'Missippi')
test(remove('egg', 'bicycle'), 'bicycle')
```

13. Write a function that removes all occurrences of a string from another string:

```
test(remove_all('an', 'banana'), 'ba')
test(remove_all('cyc', 'bicycle'), 'bile')
test(remove_all('iss', 'Mississippi'), 'Mippi')
test(remove_all('eggs', 'bicycle'), 'bicycle')
```

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9. Tuples

9.1. Tuples are used for grouping data

We've seen earlier that we can group together pairs of values by putting them into parentheses. Recall this example:

```
>>> year born = ("Paris Hilton", 1981)
```

This is an example of a data structure — a mechanism for grouping and organizing data to make it easier to use.

The pair is an example of a tuple. Generalizing this, a tuple can be used to group any number of items into a single compound value. Syntactically, a tuple is a comma-separated sequence of values. Although it is not necessary, it is conventional to enclose tuples in parentheses:

```
>>> julia = ("Julia", "Roberts", 1967,
                  "Duplicity", 2009, "Actress", "Atlanta, Georgia")
```

Tuples are useful for representing what other languages often call records — some related information that belongs together, like your student record. There is no description of what each of these fields means, but we can guess. A tuple lets us "chunk" together related information and use it as a single thing.

Tuples support the same sequence operations as strings. The index operator selects an element from a tuple.

```
>>> julia[2]
```

But if we try to use item assignment to modify one of the elements of the tuple, we get an error:

```
>>> julia[0] = 'X'
TypeError: 'tuple' object does not support item assignment
```

So like strings, tuples are immutable. Once Python has created a tuple in memory, it cannot be changed.

Of course, even if we can't modify the elements of a tuple, we can always make the julia variable reference a new tuple holding different information. To construct the new tuple, it is convenient that we can slice parts of the old tuple and join up the bits to make the new tuple. So if julia has a new recent film, we could change her variable to reference a new tuple that used some information from the old one:

```
>>> julia = julia[:3] + ("Eat Pray Love", 2010) + julia[5:]
>>> julia
('Julia', 'Roberts', 1967, 'Eat Pray Love', 2010, 'Actress', 'Atlanta, Georgia')
```

To create a tuple with a single element (but you're probably not likely to do that too often), we have to include the final comma, because without the final comma, Python treats the (5) below as an integer in parentheses:

```
>>> tup = (5,)
>>> type(tup)
<class 'tuple'>
>>> x = (5)
>>> type(x)
<class 'int'>
```

9.2. Tuple assignment

Python has a very powerful tuple assignment feature that allows a tuple of variables on the left of an assignment to be assigned values from a tuple on the right of the assignment. (We already saw this used for pairs, but it generalizes.)

```
(name, surname, b_year, movie, m_year, profession, b_place) = julia
```

This does the equivalent of seven assignment statements, all on one easy line. One requirement is that the number of variables on the left must match the number of elements in the tuple.

Once in a while, it is useful to swap the values of two variables. With conventional assignment statements, we have to use a temporary variable. For example, to swap a and b:

```
1 temp = a
2 a = b
3 b = temp
```

Tuple assignment solves this problem neatly:

```
1 (a, b) = (b, a)
```

The left side is a tuple of variables; the right side is a tuple of values. Each value is assigned to its respective variable. All the expressions on the right side are evaluated before any of the assignments. This feature makes tuple assignment quite versatile.

Naturally, the number of variables on the left and the number of values on the right have to be the same:

```
>>> (a, b, c, d) = (1, 2, 3)
ValueError: need more than 3 values to unpack
```

9.3. Tuples as return values

Functions can always only return a single value, but by making that value a tuple, we can effectively group together as many values as we like, and return them together. This is very useful — we often want to know some batsman's highest and lowest score, or we want to find the mean and the standard deviation, or we want to know the year, the month, and the day, or if we're doing some

some ecological modelling we may want to know the number of rabbits and the number of wolves on an island at a given time.

For example, we could write a function that returns both the area and the circumference of a circle of radius r:

```
def f(r):
    """ Return (circumference, area) of a circle of radius r """
    c = 2 * math.pi * r
    a = math.pi * r * r
    return (c, a)
```

9.4. Composability of Data Structures

We saw in an earlier chapter that we could make a list of pairs, and we had an example where one of the items in the tuple was itself a list:

```
students = [
    ("John", ["CompSci", "Physics"]),
    ("Vusi", ["Maths", "CompSci", "Stats"]),
    ("Jess", ["CompSci", "Accounting", "Economics", "Management"]),
    ("Sarah", ["InfSys", "Accounting", "Economics", "CommLaw"]),
    ("Zuki", ["Sociology", "Economics", "Law", "Stats", "Music"])]
```

Tuples items can themselves be other tuples. For example, we could improve the information about our movie stars to hold the full date of birth rather than just the year, and we could have a list of some of her movies and dates that they were made, and so on:

Notice in this case the tuple has just five elements – but each of those in turn can be another tuple, a list, a string, or any other kind of Python value.

9.5. Glossary

data structure

An organization of data for the purpose of making it easier to use.

immutable data type

A data type which cannot be modified. Assignments to elements or slices (sub-parts) of immutable types cause a runtime error.

mutable data type

A data type which can be modified. All mutable types are compound types. Lists and dictionaries (coming soon) are mutable data types; strings and tuples are not.

tuple

An immutable data type that contains related elements. Tuples are used to group together related data, such as a person's name, their age, and their gender.

tuple assignment

An assignment to all of the elements in a tuple using a single assignment statement. Tuple assignment occurs *simultaneously* rather than in sequence, making it useful for swapping values.

9.6. Exercises

- 1. We've said nothing in this chapter about whether you can pass tuples as arguments to a function. Construct a small Python example to test whether this is possible, and write up your findings.
- 2. Is a pair a generalization of a tuple, or is a tuple a generalization of a pair?
- 3. Is a pair a kind of tuple, or is a tuple a kind of pair?

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10. Event-Driven Programming

Most programs and devices like your cellphone respond to *events* — things that happen. For example, you might move your mouse, and the computer responds. Or you click a button, and the program does something interesting. In this chapter we'll touch very briefly on how event-driven programming works.

10.1. Keypress events

Here's a program with some new features. Copy it into your workspace, run it. When the turtle window opens, press the arrow keys and make tess move about!

```
1
     import turtle
 2
                                             # determine the window size
     turtle.setup(400,500)
     wn = turtle.Screen()
                                            # get a reference to the window
     wn.title("Handling keypresses!")  # Change the window title
wn.bgcolor("lightgreen")  # Set the background color
     tess = turtle.Turtle()
                                            # Create our favorite turtle
 8
 9
     # The next four functions are our "event handlers".
10
     def h1():
11
       tess.forward(30)
12
     def h2():
13
14
       tess.left(45)
15
     def h3():
16
17
       tess.right(45)
18
19
     def h4():
                                            # Close down the turtle window
20
         wn.bye()
21
22
     # These lines "wire up" keypresses to the handlers we've defined.
     wn.onkey(h1, "Up")
23
     wn.onkey(h2, "Left")
24
     wn.onkey(h3, "Right")
wn.onkey(h4, "q")
25
26
27
28
     # Now we need to tell the window to start listening for events,
29
     # If any of the keys that we're monitoring is pressed, its
30
     # handler will be called.
31
     wn.listen()
     wn.mainloop()
```

Here are some points to note:

- You need the call to the window's <u>listen</u> method at line 31, otherwise it won't notice your keypresses.
- We named our handler functions h1, h2 and so on, but you can choose better names. The handlers can be arbitrarily complex functions that call other functions, etc.
- Pressing the g key on the keyboard calls function h4 (because we bound the g key to h4 on line

- 26). While executing h4, the window's bye method (line 24) closes the turtle window, which causes the window's mainloop call (line 31) to end its execution. Since we did not write any more statements after line 32, this means that our program has completed everything, so it too will terminate.
- You can refer to keys on the keyboard by their character code (as we did in line 26), or by their symbolic names. Some of the symbolic names you can try are Cancel (the Break key), BackSpace, Tab, Return(the Enter key), Shift_L (any Shift key), Control_L (any Control key), Alt_L (any Alt key), Pause, Caps_Lock, Escape, Prior (Page Up), Next (Page Down), End, Home, Left, Up, Right, Down, Print, Insert, Delete, F1, F2, F3, F4, F5, F6, F7, F8, F9, F10, F11, F12, Num_Lock, and Scroll_Lock.

10.2. Mouse events

A mouse event is a bit different from a keypress event because its handler needs two parameters to receive x,y coordinate information telling us where the mouse was when the event occurred.

```
import turtle
 1
 2
 3
     turtle.setup(400,500)
     wn = turtle.Screen()
 4
     wn.title("How to handle mouse clicks on the window!")
     wn.bgcolor("lightgreen")
 8
     tess = turtle.Turtle()
 9
     tess.color("purple")
10
     tess.pensize(3)
    tess.shape("circle")
11
12
13
    def h1(x, y):
14
       tess.goto(x, y)
15
16
     wn.onclick(h1) # Wire up a click on the window.
17
     wn.mainloop()
```

There is a new turtle method used at line 14 — this allows us to move the turtle to an *absolute* coordinate position. (Most of the examples that we've seen so far move the turtle *relative* to where it currently is). So what this program does is move the turtle (and draw a line) to wherever the mouse is clicked. Try it out!

If we add this line before line 14, we'll learn a useful debugging trick too:

```
wn.title("Got click at coords {0}, {1}".format(x, y))
```

Because we can easily change the text in the window's title bar, it is a useful place to display occasional debugging or status information. (Of course, this is not the real purpose of the window title!)

But there is more!

Not only can the window receive mouse events: individual turtles can also have their own handlers for mouse clicks. The turtle that "receives" the click event will be the one under the mouse. So we'll create two turtles. Each will bind a handler to its onclick event. And the two handlers can do different things for their turtles.

```
import turtle
2
3
                                       # determine the window size
    turtle.setup(400,500)
4
    wn = turtle.Screen()
                                      # get a reference to the window
    wn.title("Handling mouse clicks!") # Change the window title
    wn.bgcolor("lightgreen") # Set the background color
7
   tess = turtle.Turtle()
                                     # Create two turtles
    tess.color("purple")
    alex = turtle.Turtle()
                                     # and move them apart
    alex.color("blue")
10
11
    alex.forward(100)
12
13
    def handler_for_tess(x, y):
        wn.title("Tess clicked at {0}, {1}".format(x, y))
14
        tess.left(42)
15
16
        tess.forward(30)
17
18
    def handler_for_alex(x, y):
19
        wn.title("Alex clicked at {0}, {1}".format(x, y))
20
        alex.right(84)
21
        alex.forward(50)
22
23
    tess.onclick(handler_for_tess)
24
    alex.onclick(handler_for_alex)
25
26
    wn.mainloop()
```

Run this, click on the turtles, see what happens!

10.3. Automatic events from a timer

Alarm clocks, kitchen timers, and thermonuclear bombs in James Bond movies are set to create an "automatic" event after a certain interval. The turtle module in Python has a timer that can cause an event when its time is up.

```
1
     import turtle
 2
 3
     turtle.setup(400,500)
     wn = turtle.Screen()
     wn.title("Using a timer")
     wn.bgcolor("lightgreen")
 8
    tess = turtle.Turtle()
     tess.color("purple")
9
10
    tess.pensize(3)
11
12
     def h1():
        tess.forward(100)
13
14
        tess.left(56)
15
16
     wn.ontimer(h1, 2000)
17
     wn.mainloop()
```

On line 16 the timer is started and set to explode in 2000 milliseconds (2 seconds). When the event does occur, the handler is called, and tess springs into action.

Unfortunately, when one sets a timer, it only goes off once. So a common idiom, or style, is to restart the timer inside the handler. In this way the timer will keep on giving new events. Try this program:

```
1 import turtle
```

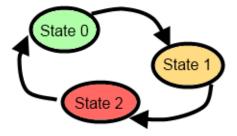
```
3
     turtle.setup(400,500)
     wn = turtle.Screen()
 4
     wn.title("Using a timer to get events!")
     wn.bgcolor("lightgreen")
 8
     tess = turtle.Turtle()
9
     tess.color("purple")
10
11
     def h1():
12
         tess.forward(100)
         tess.left(56)
13
14
         wn.ontimer(h1, 60)
15
16
     h1()
17
     wn.mainloop()
```

10.4. An example: state machines

A state machine is a system that can be in one of a few different *states*. We draw a state diagram to represent the machine, where each state is drawn as a circle or an ellipse. Certain events occur which cause the system to leave one state and *transition* into a different state. These *state transitions* are usually drawn as an arrow on the diagram.

This idea is not new: when you first turn on your cellphone, it goes into a state which we could call "Awaiting PIN". When the correct PIN is entered, it transitions into a different state — say "Ready". Then you could lock the phone, and it would enter a "Locked" state, and so on.

A simple state machine that we encounter often is a traffic light. Here is a state diagram which shows that the machine continually cycles through three different states, which we've numbered 0, 1 and 2.



We're going to build a program that uses a turtle to simulate the traffic lights. There are three lessons here. The first shows off some different ways to use our turtles. The second demonstrates how we would program a state machine in Python, by using a variable to keep track of the current state, and a number of different if statements to inspect the current state, and take the actions as we change to a different state. The third lesson is to use events from the keyboard to trigger the state changes.

Copy and run this program. Make sure you understand what each line does, consulting the documentation as you need to.

```
import turtle  # Tess becomes a traffic light.

turtle.setup(400,500)
wn = turtle.Screen()
wn.title("Tess becomes a traffic light!")
wn.bgcolor("lightgreen")
tess = turtle.Turtle()
```

```
9
10
     def draw_housing():
        ''' Draw a nice housing to hold the traffic lights '''
11
12
        tess.pensize(3)
        tess.color('black', 'darkgrey')
13
14
        tess.begin fill()
15
        tess.forward(80)
16
        tess.left(90)
17
        tess.forward(200)
18
        tess.circle(40, 180)
        tess.forward(200)
19
20
        tess.left(90)
21
        tess.end fill()
22
23
24
     draw housing()
25
26
     tess.penup()
     # Position Tess onto the place where the green light should be
27
28
    tess.forward(40)
29
    tess.left(90)
30
    tess.forward(50)
31
     # Turn tess into a big green circle
32
    tess.shape('circle')
33
    tess.shapesize(3)
34
    tess.fillcolor('green')
35
36
     # A traffic light is a kind of state machine with three states,
37
     # Green, Orange, Red. We number these states 0, 1, 2
38
     # When the machine changes state, we change tess' position and
39
     # her fillcolor.
40
41
     # This variable holds the current state of the machine
42
     state_num = 0
43
44
45
     def advance_state_machine():
46
         global state num
47
         if state num == 0:
                                  # transition from state 0 to state 1
             tess.forward(70)
48
49
            tess.fillcolor('orange')
            state_num = 1
50
        elif state_num == 1:
                                  # transition from state 1 to state 2
51
52
            tess.forward(70)
53
            tess.fillcolor('red')
54
             state num = 2
55
                                  # transition from state 2 to state 0
       else:
56
            tess.back(140)
57
             tess.fillcolor('green')
58
             state_num = 0
59
     # bind the event handler to the space key.
60
61
     wn.onkey(advance_state_machine, "space")
62
                                      # listen for events
63
     wn.listen()
64
     wn.mainloop()
```

The new Python statement is at line 46. The global keyword tells Python not to create a new local variable for state_num (in spite of the fact that the function assigns to this variable at lines 50, 54, and 58). Instead, in this function, state_num always refers to the variable that was created at line 42.

What the code in advance_state_machine does is advance from whatever the current state is, to the next state. On the state change we move tess to her new position, change her color, and, of course,

we assign to state num the number of the new state we've just entered.

Each time the space bar is pressed, the event handler causes the traffic light machine to move to its new state.

10.5. Glossary

bind

We bind a function (or associate it) with an event, meaning that when the event occurs, the function is called to handle it.

event

Something that happens "outside" the normal control flow of your program, usually from some user action. Typical events are mouse operations and keypresses. We've also seen that a timer can be primed to create an event.

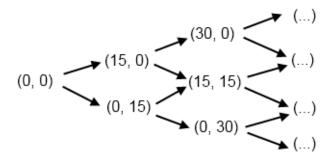
handler

A function that is called in response to an event.

10.6. Exercises

- 1. Add some new key bindings to the first sample program:
 - Pressing keys 'R', 'G' or 'B' should change tess' color to Red, Green or Blue.
 - Pressing keys '+' or '-' should increase or decrease the width of tess' pen. Ensure that the pen size stays between 1 and 20 (inclusive).
 - Handle some other keys to change some attributes of tess, or attributes of the window, or to give her new behaviour that can be controlled from the keyboard.
- 2. Change the traffic light program so that changes occur automatically, driven by a timer.
- 3. In an earlier chapter we saw two turtle methods, hideturtle and show a turtle. This suggests that we could take a different approach to the traffic lights program. Modify the program so that we create three separate turtles for each of the green, orange and red lights, and instead of moving tess to different positions and changing her color, we just make one of the three turtles visible at any time. Once you've made the changes, sit back and ponder some deep thoughts: you've got two programs, both seem to do the same thing. Is one approach somehow preferable to the other? Which one more closely resembles reality i.e. the traffic lights in your town?
- 4. Now that you've got a traffic light program with different turtles for each light, perhaps the visibility / invisibility trick wasn't such a great idea. If you watch the traffic lights, they turn on and off but when they're off they are still there, perhaps just a darker color. Modify the program now so that the lights don't disappear: they are either on, or off. But when they're off, they're still visible.
- 5. Your traffic light controller program has been patented, and you're about to become seriously rich. But your new client needs a change. They want four states in their state machine: Green, then Green and Orange together, then Orange only, and then Red. Additionally, they want different times spent in each state. The machine should spend 3 seconds in the Green state, followed by one second in the Green+Orange state, then one second in the Orange state, and then 2 seconds in the Red state. Change the logic in the state machine.
- 6. If you don't know how tennis scoring works, ask a friend or consult Wikipedia. A single game in

tennis between player A and player B always has a score. We want to think about the "state of the score" as a state machine. The game starts in state (0, 0), meaning neither player has any score yet. We'll assume the first element in this pair is the score for player A. If player A wins the first point, the score becomes (15, 0). If B wins the first point, the state becomes (0, 15). Below are the first few states and transitions for a state diagram. In this diagram, each state has two possible outcomes (A wins the next point, or B does), and the uppermost arrow is always the transition that happens when A wins the point. Complete the diagram, showing all transitions and all states. (Hint: there are twenty states, if you include the duece state, the advantage states, and the "A wins" and "B wins" states in your diagram.)



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11. Lists

A list is an ordered collection of values. The values that make up a list are called its elements, or its items. We will use the term *element* or *item* to mean the same thing. Lists are similar to strings, which are ordered collections of characters, except that the elements of a list can be any type. Lists and strings — and other collections that maintain the order of their items — are called sequences.

11.1. List values

There are several ways to create a new list; the simplest is to enclose the elements in square brackets ([and]):

```
ps = [10, 20, 30, 40]
qs = ["spam", "bungee", "swallow"]
```

The first example is a list of four integers. The second is a list of three strings. The elements of a list don't have to be the same type. The following list contains a string, a float, an integer, and (amazingly) another list:

```
zs = ["hello", 2.0, 5, [10, 20]]
```

A list within another list is said to be nested.

Finally, a list with no elements is called an empty list, and is denoted [].

We have already seen that we can assign list values to variables or pass lists as parameters to functions:

```
>>> vocabulary = ["apple", "cheese", "dog"]
>>> numbers = [17, 123]
>>> an_empty_list = []
>>> print(vocabulary, numbers, an_empty_list)
['apple', 'cheese', 'dog'] [17, 123] []
```

11.2. Accessing elements

The syntax for accessing the elements of a list is the same as the syntax for accessing the characters of a string—the index operator ([] - not to be confused with an empty list). The expression inside the brackets specifies the index. Remember that the indices start at 0:

```
>>> numbers[0]
17
```

Any integer expression can be used as an index:

```
>>> numbers[9-8]
5
>>> numbers[1.0]
Traceback (most recent call last):
  File "<interactive input>", line 1, in <module>
TypeError: list indices must be integers, not float
```

If you try to access or assign to an element that does not exist, you get a runtime error:

```
>>> numbers[2]
Traceback (most recent call last):
  File "<interactive input>", line 1, in <module>
IndexError: list index out of range
```

It is common to use a loop variable as a list index.

```
horsemen = ["war", "famine", "pestilence", "death"]

for i in [0, 1, 2, 3]:
    print(horsemen[i])
```

Each time through the loop, the variable i is used as an index into the list, printing the i'th element. This pattern of computation is called a list traversal.

The above sample doesn't need or use the index i for anything besides getting the items from the list, so this more direct version — where the *for* loop gets the items — might be preferred:

```
horsemen = ["war", "famine", "pestilence", "death"]

for h in horsemen:
    print(h)
```

11.3. List length

The function <u>len</u> returns the length of a list, which is equal to the number of its elements. If you are going to use an integer index to access the list, it is a good idea to use this value as the upper bound of a loop instead of a constant. That way, if the size of the list changes, you won't have to go through the program changing all the loops; they will work correctly for any size list:

```
horsemen = ["war", "famine", "pestilence", "death"]

for i in range(len(horsemen)):
    print(horsemen[i])
```

The last time the body of the loop is executed, \underline{i} is $\underline{len(horsemen)}$ - 1, which is the index of the last element. (But the version without the index looks even better now!)

Although a list can contain another list, the nested list still counts as a single element in its parent list. The length of this list is 4:

```
>>> len(['car makers', 1, ['Ford', 'Toyota', 'BMW'], [1, 2, 3]])
4
```

11.4. List membership

in and not in are boolean operators that test membership in a sequence. We used them previously with strings, but they also work with lists and other sequences:

```
>>> horsemen = ['war', 'famine', 'pestilence', 'death']
>>> 'pestilence' in horsemen
True
>>> 'debauchery' in horsemen
False
>>> 'debauchery' not in horsemen
True
```

Using this produces a more elegant version of the nested loop program we previously used to count the number of students doing Computer Science in the section <u>Nested Loops for Nested Data</u>:

```
1
        students = [
              ("John", ["CompSci", "Physics"]),
("Vusi", ["Maths", "CompSci", "Stats"]),
("Jess", ["CompSci", "Accounting", "Economics", "Management"]),
("Sarah", ["InfSys", "Accounting", "Economics", "CommLaw"]),
("Zuki", ["Sociology", "Economics", "Law", "Stats", "Music"])]
 2
 3
 4
 5
 6
 7
 8
        # Count how many students are taking CompSci
 9
       counter = 0
10
       for (name, subjects) in students:
          if "CompSci" in subjects:
11
12
                         counter += 1
13
        print("The number of students taking CompSci is", counter)
14
```

11.5. List operations

The + operator concatenates lists:

```
>>> a = [1, 2, 3]
>>> b = [4, 5, 6]
>>> c = a + b
>>> c
[1, 2, 3, 4, 5, 6]
```

Similarly, the * operator repeats a list a given number of times:

```
>>> [0] * 4
[0, 0, 0, 0]
>>> [1, 2, 3] * 3
[1, 2, 3, 1, 2, 3, 1, 2, 3]
```

The first example repeats [0] four times. The second example repeats the list [1, 2, 3] three times.

11.6. List slices

The slice operations we saw previously with strings lets us work with sublists:

```
>>> a_list = ['a', 'b', 'c', 'd', 'e', 'f']
>>> a_list[1:3]
['b', 'c']
>>> a_list[:4]
['a', 'b', 'c', 'd']
>>> a_list[3:]
['d', 'e', 'f']
>>> a_list[:]
['a', 'b', 'c', 'd', 'e', 'f']
```

11.7. Lists are mutable

Unlike strings, lists are mutable, which means we can change their elements. Using the bracket operator on the left side of an assignment, we can update one of the elements:

```
>>> fruit = ["banana", "apple", "quince"]
>>> fruit[0] = "pear"
>>> fruit[2] = "orange"
>>> fruit
['pear', 'apple', 'orange']
```

The bracket operator applied to a list can appear anywhere in an expression. When it appears on the left side of an assignment, it changes one of the elements in the list, so the first element of <u>fruit</u> has been changed from <u>'banana'</u> to <u>'pear'</u>, and the last from <u>'quince'</u> to <u>'orange'</u>. An assignment to an element of a list is called item assignment. Item assignment does not work for strings:

```
>>> my_string = 'TEST'
>>> my_string[2] = 'X'
Traceback (most recent call last):
   File "<interactive input>", line 1, in <module>
TypeError: 'str' object does not support item assignment
```

but it does for lists:

```
>>> my_list = ['T', 'E', 'S', 'T']
>>> my_list[2] = 'X'
>>> my_list
['T', 'E', 'X', 'T']
```

With the slice operator we can update a whole sublist at once:

```
>>> a_list = ['a', 'b', 'c', 'd', 'e', 'f']
>>> a_list[1:3] = ['x', 'y']
>>> a_list
['a', 'x', 'y', 'd', 'e', 'f']
```

We can also remove elements from a list by assigning the empty list to them:

```
>>> a_list = ['a', 'b', 'c', 'd', 'e', 'f']
>>> a_list[1:3] = []
>>> a_list
['a', 'd', 'e', 'f']
```

And we can add elements to a list by squeezing them into an empty slice at the desired location:

```
>>> a_list = ['a', 'd', 'f']
```

```
>>> a_list[1:1] = ['b', 'c']
>>> a_list
['a', 'b', 'c', 'd', 'f']
>>> a_list[4:4] = ['e']
>>> a_list
['a', 'b', 'c', 'd', 'e', 'f']
```

11.8. List deletion

Using slices to delete list elements can be error-prone. Python provides an alternative that is more readable. The del statement removes an element from a list:

```
>>> a = ['one', 'two', 'three']
>>> del a[1]
>>> a
['one', 'three']
```

As you might expect, del causes a runtime error if the index is out of range.

You can also use del with a slice to delete a sublist:

```
>>> a_list = ['a', 'b', 'c', 'd', 'e', 'f']
>>> del a_list[1:5]
>>> a_list
['a', 'f']
```

As usual, the sublist selected by slice contains all the elements up to, but not including, the second index.

11.9. Objects and references

If we execute these assignment statements,

we know that a and b will refer to a string ojbect with the letters "banana". But we don't know yet whether they point to the *same* string object.

There are two possible ways the Python interpreter could arrange its memory:

```
a → "banana" a b → "banana" b
```

In one case, a and b refer to two different objects that have the same value. In the second case, they refer to the same object.

We can test whether two names refer to the same object using the *is* operator:

```
>>> a is b
True
```

This tells us that both a and b refer to the same object, and that it is the second of the two state

snapshots that accurately describes the relationship.

Since strings are *immutable*, Python optimizes resources by making two names that refer to the same string value refer to the same object.

This is not the case with lists:

```
>>> a = [1, 2, 3]
>>> b = [1, 2, 3]
>>> a == b
True
>>> a is b
False
```

The state snapshot here looks like this:

```
a \longrightarrow [1, 2, 3]b \longrightarrow [1, 2, 3]
```

a and b have the same value but do not refer to the same object.

11.10. Aliasing

Since variables refer to objects, if we assign one variable to another, both variables refer to the same object:

```
>>> a = [1, 2, 3]
>>> b = a
>>> a is b
True
```

In this case, the state snapshot looks like this:

```
a [1, 2, 3]
```

Because the same list has two different names, a and b, we say that it is aliased. Changes made with one alias affect the other:

```
>>> b[0] = 5
>>> a
[5, 2, 3]
```

Although this behavior can be useful, it is sometimes unexpected or undesirable. In general, it is safer to avoid aliasing when you are working with mutable objects(i.e. lists at this point in our textbook, but we'll meet more mutable objects as we cover classes and objects, dictionaries and sets). Of course, for immutable objects (i.e. strings, tuples), there's no problem – it is just not possible to change something and get a surprise when you access an alias name. That's why Python is free to alias strings (and any other immutable kinds of data) when it sees an opportunity to economize.

11.11. Cloning lists

If we want to modify a list and also keep a copy of the original, we need to be able to make a copy of the list itself, not just the reference. This process is sometimes called cloning, to avoid the ambiguity of the word copy.

The easiest way to clone a list is to use the slice operator:

```
>>> a = [1, 2, 3]
>>> b = a[:]
>>> b
[1, 2, 3]
```

Taking any slice of a creates a new list. In this case the slice happens to consist of the whole list. So now the relationship is like this:

```
a \longrightarrow [1, 2, 3]b \longrightarrow [1, 2, 3]
```

Now we are free to make changes to b without worrying that we'll inadvertently be changing a:

```
>>> b[0] = 5
>>> a
[1, 2, 3]
```

11.12. Lists and for loops

The for loop also works with lists, as we've already seen. The generalized syntax of a for loop is:

```
for VARIABLE in LIST:
BODY
```

So, as we've seen

```
friends = ["Joe", "Amy", "Brad", "Angelina", "Zuki", "Thandi", "Paris"]
for friend in friends:
    print(friend)
```

It almost reads like English: For (every) friend in (the list of) friends, print (the name of the) friend.

Any list expression can be used in a for loop:

```
for number in range(20):
    if number % 3 == 0:
        print(number)

for fruit in ["banana", "apple", "quince"]:
    print("I like to eat " + fruit + "s!")
```

The first example prints all the multiples of 3 between 0 and 19. The second example expresses enthusiasm for various fruits.

Since lists are mutable, we often want to traverse a list, changing each of its elements. The following

squares all the numbers in the list xs:

Take a moment to think about range(len(xs)) until you understand how it works.

In this example we are interested in both the *value* of an item, (we want to square that value), and its *index* (so that we can assign the new value to that position). This pattern is common enough that Python provides a nicer way to implement it:

```
1     xs = [1, 2, 3, 4, 5]
2     for (i, val) in enumerate(xs):
        xs[i] = val**2
```

enumerate generates pairs of both (index, value) during the list traversal. Try this next example to see more clearly how enumerate works:

```
for (i, v) in enumerate(['banana', 'apple', 'pear', 'lemon']):
    print(i, v)
```

```
0 banana
1 apple
2 pear
3 lemon
```

11.13. List parameters

Passing a list as an argument actually passes a reference to the list, not a copy or clone of the list. So parameter passing creates an alias for you: the caller has one variable referencing the list, and the called function has an alias, but there is only one underlying list object. For example, the function below takes a list as an argument and multiplies each element in the list by 2:

```
def double_stuff(a_list):
    """ Overwrite each element in a_list with double its value. """
    for (idx, val) in enumerate(a_list):
        a_list[idx] = 2 * val
```

If we add the following onto our script:

```
things = [2, 5, 9]
double_stuff(things)
print(things)
```

When we run it we'll get:

```
[4, 10, 18]
```

In the function above, the parameter a_list and the variable things are aliases for the same object. So before any changes to the elements in the list, the state snapshot looks like this:

```
__main__ a_list
double_stuff things [2,5,9]
```

Since the list object is shared by two frames, we drew it between them.

If a function modifies the items of a list parameter, the caller sees the change.

```
Use the Python visualizer!
```

We've already mentioned the Python visualizer at http://netserv.ict.ru.ac.za/python3_viz. It is a very useful tool for building a good understanding of references, aliases, assignments, and passing arguments to functions. Pay special attention to cases where you clone a list or have two separate lists, and cases where there is only one underlying list, but more than one variable is aliased to reference the list.

11.14. List methods

The dot operator can also be used to access built-in methods of list objects. We'll start with the most useful method for adding something onto the end of an existing list...

```
>>> mylist = []
>>> mylist.append(5)
>>> mylist.append(27)
>>> mylist.append(3)
>>> mylist.append(12)
>>> mylist
[5, 27, 3, 12]
>>>
```

append is a list method which adds the argument passed to it to the end of the list. We'll use it heavily when we're creating new lists. Continuing with this example, we show several other list methods:

```
>>> mylist.insert(1, 12) # insert 12 at pos 1, shift other items up
>>> mylist
[5, 12, 27, 3, 12]
>>> mylist.count(12)
                         # how many times is 12 in mylist?
>>> mylist.extend([5, 9, 5, 11]) # put whole list onto end of mylist
>>> mylist
[5, 12, 27, 3, 12, 5, 9, 5, 11])
>>> mylist.index(9)
                                  # find index of first 9 in mylist
>>> mylist.reverse()
>>> mylist
[11, 5, 9, 5, 12, 3, 27, 12, 5]
>>> mylist.sort()
>>> mylist
[3, 5, 5, 5, 9, 11, 12, 12, 27]
>>> mylist.remove(12)
                                 # remove the first 12 in the list
```

```
>>> mylist
[3, 5, 5, 5, 9, 11, 12, 27]
>>>
```

Experiment and play with the list methods shown here, and read their documentation until you feel confident that you understand how they work.

11.15. Pure functions and modifiers

Functions which take lists as arguments and change them during execution are called modifiers and the changes they make are called side effects.

A pure function does not produce side effects. It communicates with the calling program only through parameters, which it does not modify, and a return value. Here is double_stuff written as a pure function:

```
def double stuff(a list):
2
         """ Return a new list in which contains
3
            doubles of the elements in a_list.
4
5
        new_list = []
6
        for value in a_list:
7
            new_elem = 2 * value
8
            new_list.append(new_elem)
9
10
        return new_list
```

This version of <u>double_stuff</u> does not change its arguments:

```
>>> things = [2, 5, 9]
>>> xs = double_stuff(things)
>>> things
[2, 5, 9]
>>> xs
[4, 10, 18]
```

An early rule we saw for assignment said "first evaluate the right hand side, then assign the resulting value to the variable". So it is quite safe to assign the function result to the same variable that was passed to the function:

```
>>> things = [2, 5, 9]
>>> things = double_stuff(things)
>>> things
[4, 10, 18]
```

Which style is better?

Anything that can be done with modifiers can also be done with pure functions. In fact, some programming languages only allow pure functions. There is some evidence that programs that use pure functions are faster to develop and less error-prone than programs that use modifiers. Nevertheless, modifiers are convenient at times, and in some cases, functional programs are less efficient.

In general, we recommend that you write pure functions whenever it is reasonable to do so and resort to modifiers only if there is a compelling advantage. This approach might be called a *functional programming style*.

11.16. Functions that produce lists

The pure version of double_stuff above made use of an important pattern for your toolbox. Whenever you need to write a function that creates and returns a list, the pattern is usually:

```
initialize a result variable to be an empty list loop
create a new element
append it to result
return the result
```

Let us show another use of this pattern. Assume you already have a function $is_prime(x)$ that can test if x is prime. Write a function to return a list of all prime numbers less than n:

```
def primes_lessthan(n):
    ''' Return a list of all prime numbers less than n. '''
    result = []
    for i in range(2, n):
        if is_prime(i):
            result.append(i)
    return result
```

11.17. Strings and lists

Two of the most useful methods on strings involve conversion to and from lists of substrings. The <u>split</u> method (which we've already seen) breaks a string into a list of words. By default, any number of whitespace characters is considered a word boundary:

```
>>> song = "The rain in Spain..."
>>> wds = song.split()
>>> wds
['The', 'rain', 'in', 'Spain...']
```

An optional argument called a delimiter can be used to specify which string to use as the boundary marker between substrings. The following example uses the string at as the delimiter:

```
>>> song.split('ai')
['The r', 'n in Sp', 'n...']
```

Notice that the delimiter doesn't appear in the result.

The inverse of the split method is join. You choose a desired separator string, (often called the *glue*) and join the list with the glue between each of the elements:

```
>>> glue = ';'
>>> s = glue.join(wds)
>>> s
'The;rain;in;Spain...'
```

The list that you glue together (wds in this example) is not modified. Also, as these next examples show, you can use empty glue or multi-character strings as glue:

```
>>> ' --- ' . join(wds)
'The --- rain --- in --- Spain...'
>>> '' . join(wds)
'TheraininSpain...'
```

11.18. list and range

Python has a built-in type conversion function called <u>list</u> that tries to turn whatever you give it into a list.

```
>>> xs = list("Crunchy Frog")
>>> xs
['C', 'r', 'u', 'n', 'c', 'h', 'y', ' ', 'F', 'r', 'o', 'g']
>>> ''.join(xs)
'Crunchy Frog'
```

One particular feature of range is that it doesn't instantly compute all its values: it "puts off" the computation, and does it on demand, or "lazily". We'll say that it gives a promise to produce the values when they are needed. This is very convenient if your computation short-circuits a search and returns early, as in this case:

```
def f(n):
1
2
        """ Find the first positive integer between 101 and less
3
           than n that is divisible by 21
4
5
       for i in range(101, n):
6
         if (i % 21 == 0):
7
               return i
8
9
10
    test(f(110), 105)
    test(f(1000000000), 105)
11
```

In the second test, if range were to eagerly go about building a list with all those elements, you would soon exhaust your computer's available memory and crash the program. But it is cleverer than that! This computation works just fine, because the range object is just a promise to produce the elements if and when they are needed. Once the condition in the *if* becomes true, no further elements are generated, and the function returns. (Note: Before Python 3, range was not lazy. If you use an earlier versions of Python, YMMV!)

```
YMMV: Your Mileage May Vary
```

The acronym YMMV stands for *your mileage may vary*. American car advertisements often quoted fuel consumption figures for cars, e.g. that they would get 28 miles per gallon. But this always had to be accompanied by legal small-print warning the reader that they might not get the same. The term YMMV is now used idiomatically to mean "your results may differ", e.g. *The battery life on this phone is 3 days, but YMMV*.

You'll sometimes find the lazy range wrapped in a call to <u>list</u>. This forces Python to turn the lazy promise into an actual list:

```
>>> range(10) # create a Lazy promise
```

```
range(0, 10)
>>> list(range(10)) # Call in the promise, to produce a list.
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

11.19. Nested lists

A nested list is a list that appears as an element in another list. In this list, the element with index 3 is a nested list:

```
>>> nested = ["hello", 2.0, 5, [10, 20]]
```

If we print(nested[3]), we get [10, 20]. To extract an element from the nested list, we can proceed in two steps:

```
>>> elem = nested[3]
>>> elem[0]
10
```

Or we can combine them:

```
>>> nested[3][1]
20
```

Bracket operators evaluate from left to right, so this expression gets the three-'th element of nested and extracts the one-'th element from it.

11.20. Matrices

Nested lists are often used to represent matrices. For example, the matrix:

```
1 2 3
4 5 6
7 8 9
```

might be represented as:

```
>>> mx = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
```

mx is a list with three elements, where each element is a row of the matrix. We can select an entire row from the matrix in the usual way:

```
>>> mx[1]
[4, 5, 6]
```

Or we can extract a single element from the matrix using the double-index form:

```
>>> mx[1][2]
6
```

The first index selects the row, and the second index selects the column. Although this way of representing matrices is common, it is not the only possibility. A small variation is to use a list of

columns instead of a list of rows. Later we will see a more radical alternative using a dictionary.

11.21. Glossary

aliases

Multiple variables that contain references to the same object.

clone

To create a new object that has the same value as an existing object. Copying a reference to an object creates an alias but doesn't clone the object.

delimiter

A character or string used to indicate where a string should be split.

element

One of the values in a list (or other sequence). The bracket operator selects elements of a list. Also called *item*.

index

An integer value that indicates the position of an item in a list. Indexes start from 0.

item

See element.

list

A collection of values, each in a fixed position within the list. Like other types str, int, float, etc.
there is also a list type-converter function that tries to turn whatever argument you give it into a list.

list traversal

The sequential accessing of each element in a list.

modifier

A function which changes its arguments inside the function body. Only mutable types can be changed by modifiers.

mutable data type

A data type in which the elements can be modified. All mutable types are compound types. Lists are mutable data types; strings are not.

nested list

A list that is an element of another list.

object

A thing to which a variable can refer.

pattern

A sequence of statements, or a style of coding something that has general applicability in a number of different situations. Part of becoming a mature Computer Scientist is to learn and establish the patterns and algorithms that form your toolkit. Patterns often correspond to your "mental chunking".

promise

An object that promises to do some work or deliver some values if they're eventually needed, but it lazily puts off doing the work immediately. Calling range produces a promise.

pure function

A function which has no side effects. Pure functions only make changes to the calling program through their return values.

sequence

Any of the data types that consist of an ordered collection of elements, with each element identified by an index.

side effect

A change in the state of a program made by calling a function. Side effects can only be produced by modifiers.

step size

The interval between successive elements of a linear sequence. The third (and optional argument) to the range function is called the step size. If not specified, it defaults to 1.

11.22. Exercises

1. What is the Python interpreter's response to the following?

```
>>> list(range(10, 0, -2))
```

The three arguments to the *range* function are *start*, *stop*, and *step*, respectively. In this example, <u>start</u> is greater than <u>stop</u>. What happens if <u>start</u> < <u>stop</u> and <u>step</u> < <u>0</u>? Write a rule for the relationships among start, stop, and step.

Consider this fragment of code:

```
import turtle

tess = turtle.Turtle()
alex = tess
alex.color("hotpink")
```

Does this fragment create one or two turtle instances? Does setting the colour of alex also change the colour of tess? Explain in detail.

3. Draw a state snapshot for a and b before and after the third line of the following python code is executed:

```
a = [1, 2, 3]
b = a[:]
b[0] = 5
```

4. What will be the output of the following program?

```
this = ['I', 'am', 'not', 'a', 'crook']
that = ['I', 'am', 'not', 'a', 'crook']
```

```
print("Test 1: {0}".format(this is that))
that = this
print("Test 2: {0}".format(this is that))
```

Provide a detailed explaination of the results.

5. Lists can be used to represent mathematical *vectors*. In this exercise and several that follow you will write functions to perform standard operations on vectors. Create a script named <u>vectors.py</u> and write Python code to pass the tests in each case.

Write a function add_vectors(u, v) that takes two lists of numbers of the same length, and returns a new list containing the sums of the corresponding elements of each:

```
test(add_vectors([1, 1], [1, 1]), [2, 2])
test(add_vectors([1, 2], [1, 4]), [2, 6])
test(add_vectors([1, 2, 1], [1, 4, 3]), [2, 6, 4])
```

6. Write a function $scalar_mult(s, v)$ that takes a number, s, and a list, v and returns the $scalar_multiple$ of v by s. :

```
test(scalar_mult(5, [1, 2]), [5, 10])
test(scalar_mult(3, [1, 0, -1]), [3, 0, -3])
test(scalar_mult(7, [3, 0, 5, 11, 2]), [21, 0, 35, 77, 14])
```

7. Write a function $dot_{product}(u, v)$ that takes two lists of numbers of the same length, and returns the sum of the products of the corresponding elements of each (the <u>dot_product</u>).

```
test(dot_product([1, 1], [1, 1]), 2)
test(dot_product([1, 2], [1, 4]), 9)
test(dot_product([1, 2, 1], [1, 4, 3]), 12)
```

- 8. Extra challenge for the mathematically inclined: Write a function cross_product(u, v) that takes
 two lists of numbers of length 3 and returns their cross product. You should write your own
 tests.
- 9. Describe the relationship between ''.join(song.split()) and song in the fragment of code below. Are they the same for all strings assigned to song? When would they be different?:

```
song = "The rain in Spain..."
```

10. Write a function replace(s, old, new) that replaces all occurences of old with new in a string s:

```
test(replace('Mississippi', 'i', 'I'), 'MIssIssIppI')

s = 'I love spom! Spom is my favorite food. Spom, spom, yum!'

test(replace(s, 'om', 'am'),
    'I love spam! Spam is my favorite food. Spam, spam, yum!')

test(replace(s, 'o', 'a'),
```

```
8 'I lave spam! Spam is my favarite faad. Spam, spam, yum!')
```

Hint: use the split and join methods.

11. Cut and paste the following functions to a script called segtools.py.

```
1
     def make_empty(seq): pass
     def insert_at_end(val, seq): pass
 2
     def insert_in_front(val, seq): pass
     def index_of(val, seq, start=0): pass
     def remove_at(index, seq): pass
     def remove_val(val, seq): pass
     def remove_all(val, seq): pass
     def count(val, seq): pass
     def reverse(seq): pass
10
     def sort_sequence(seq): pass
11
12
     def testsuite():
13
         test(make_empty([1, 2, 3, 4]), [])
        test(make_empty(('a', 'b', 'c')), ())
14
15
         test(make_empty("No, not me!"),
16
        test(insert_at_end(5, [1, 3, 4, 6]), [1, 3, 4, 6, 5])
test(insert_at_end('x', 'abc'), 'abcx')
17
18
19
         test(insert_at_end(5, (1, 3, 4, 6)), (1, 3, 4, 6, 5))
20
21
         test(insert_in_front(5, [1, 3, 4, 6]), [5, 1, 3, 4, 6])
22
         test(insert_in_front(5, (1, 3, 4, 6)), (5, 1, 3, 4, 6))
23
         test(insert_in_front('x', 'abc'),
                                                   'xabc')
24
25
         test(index_of(9, [1, 7, 11, 9, 10]), 3)
         test(index_of(5, (1, 2, 4, 5, 6, 10, 5, 5)), 3)
26
        test(index_of(5, (1, 2, 4, 5, 6, 10, 5, 5), 4), 6)
test(index_of('y', 'happy birthday'), 4)
27
28
29
         test(ndex_of('banana',['apple','banana','cherry','date']),1)
30
         test(index_of(5, [2, 3, 4]), -1)
         test(index_of('b', ['apple', 'banana', 'cherry', 'date']),-1)
31
32
33
         test(remove_at(3, [1, 7, 11, 9, 10]), [1, 7, 11, 10])
         test(remove_at(5, (1,4,6,7,0,9,3,5)), (1,4,6,7,0,3,5))
34
35
         test(remove_at(2, "Yomrktown"), 'Yorktown')
36
         test(remove_val(11, [1, 7, 11, 9, 10]), [1, 7, 9, 10])
37
         test(remove_val(15, (1, 15, 11, 4, 9)), (1, 11, 4, 9))
38
        39
40
41
42
         test(remove_all(11, [1,7,11,9,11,10,2,11]),[1,7,9,10,2])
         test(remove_all('i', 'Mississippi'), 'Msssspp')
43
44
45
         test(count(5, (1, 5, 3, 7, 5, 8, 5)), 3)
46
         test(count('s', 'Mississippi'), 4)
47
         test(count((1, 2), [1, 5, (1, 2), 7, (1, 2), 8, 5]), 2)
48
49
         test(reverse([1, 2, 3, 4, 5]), [5, 4, 3, 2, 1])
         test(reverse(('shoe','my','buckle',2,1)),
50
51
                         (1,2,'buckle','my','shoe'))
         test(reverse('Python'), 'nohtyP')
52
53
54
         test(sort_sequence([3, 4, 6, 7, 8, 2]), [2, 3, 4, 6, 7, 8])
55
         test(sort_sequence((3, 4, 6, 7, 8, 2)), (2, 3, 4, 6, 7, 8))
         test(sort_sequence("nothappy"), 'ahnoppty')
56
```

As usual, add your test function and work on each of these one at a time until they pass all the tests.

But do you really want to do this?

Disclaimer. These exercises illustrate nicely that the sequence abstraction is general, (because slicing, indexing, and concatenation are so general), so it is possible to write general functions that work over all sequence types. A nice lesson indeed about generalization!

Another view is that tuples are different from lists and strings precisely because you want to think about them very differently. It usually doesn't make sense to sort the fields of the <code>julia</code> tuple we saw in the chapter on tuples, or to cut bits out or insert bits into the middle, <code>even if Python lets you do so!</code> Tuple fields get their meaning from their position in the tuple. Don't mess with that.

Use lists for "many things of the same type", like an enrollment of many students for a course.

Use tuples for "fields of different types that make up a compound record".

12. Suppose you want to swap around the values in two variables. You decide to factor this out into a reusable function, and write this code:

```
def swap(x, y):
                         # incorrect version
         print("before swap statement: x:", x, "y:", y)
 2
         (x, y) = (y, x)
 3
         print("after swap statement: x:", x, "y:", y)
 4
 5
    a = ["This", "is", "fun"]
 6
 7
    b = [2,3,4]
 8
    print("before swap function call: a:", a, "b:", b)
9
     swap(a, b)
10
     print("after swap function call: a:", a, "b:", b)
```

Run this program and describe the results. Oops! So it didn't do what you intended! Explain why not. Using a Python visualizer like the one at http://netserv.ict.ru.ac.za/python3_viz may help you build a good conceptual model of what is going on. What will be the values of a and b after the call to swap?

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12. Modules

A module is a file containing Python definitions and statements intended for use in other Python programs. There are many Python modules that come with Python as part of the standard library. We have seen at least two of these already, the turtle module and the string module.

We have also shown you how to access help. The help system contains a listing of all the standard modules that are available with Python. Play with help!

12.1. Random numbers

We often want to use random numbers in programs: here are a few typical uses:

- To play a game of chance where the computer needs to throw some dice, pick a number, or flip a coin,
- To shuffle a deck of playing cards randomly,
- To randomly allow a new enemy spaceship to appear and shoot at you,
- To simulate possible rainfall when we make a computerized model for estimating the environmental impact of builing a dam,
- For encrypting your banking session on the Internet.

Python provides a module random that helps with tasks like this. You can look it up using help, but here are the key things we'll do with it:

```
1
    import random
    # create a black box object that generates random numbers
3
    rng = random.Random()
    dice_throw = rng.randrange(1,7) # return an int, one of 1,2,3,4,5,6
    delay_in_seconds = rng.random() * 5.0
```

The randrange method call generates generates an integer between its lower and upper argument, using the same semantics as range — so the lower bound is included, but the upper bound is excluded. All the values have an equal probability of occurring (i.e. the results are uniformly distributed). Like range, randrange can also take an optional step argument. So let's assume we needed a random odd number less than 100, we could say:

```
r odd = rng.randrange(1, 100, 2)
```

Other methods can also generate other distributions e.g. a bell-shaped, or "normal" distribution might be more appropriate for estimating seasonal rainfall, or the concentration of a compound in the body after taking a dose of medicine.

The random() method returns a floating point number in the interval [0.0, 1.0) — the square bracket

means "closed interval on the left" and the round parenthesis means "open interval on the right". In other words, 0.0 is possible, but all returned numbers will be strictly less than 1.0. It is usual to *scale* the results after calling this method, to get them into an interval suitable for your application. In the case shown here, we've converted the result of the method call to a number in the interval [0.0, 5.0). Once more, these are uniformly distributed numbers — numbers close to 0 are just as likely to occur as numbers close to 0.5, or numbers close to 1.0.

This example shows how to shuffle a list. (*shuffle* cannot work directly with a lazy promise, so notice that we had to convert the range object using the list type converter first.)

```
cards = list(range(52)) # generate ints [0 .. 51]

representing a pack of cards.

rng.shuffle(cards) # shuffle the pack
```

12.1.1. Repeatability and Testing

Random number generators are based on a deterministic algorithm — repeatable and predictable. So they're called pseudo-random generators — they are not genuinely random. They start with a *seed* value. Each time you ask for another random number, you'll get one based on the current seed attribute, and the state of the seed (which is one of the attributes of the generator) will be updated.

For debugging and for writing unit tests, it is convenient to have repeatability — programs that do the same thing every time they are run. We can arrange this by forcing the random number generator to be initialized with a known seed every time. (Often this is only wanted during testing — playing a game of cards where the shuffled deck was always in the same order as last time you played would get boring very rapidly!)

```
drng = random.Random(123) # create generator with known starting state
```

This alternative way of creating a random number generator gives an explicit seed value to the object. Without this argument, the system probably uses something based on the time. So grabbing some random numbers from drng today will give you precisely the same random sequence as it will tomorrow!

12.1.2. Picking balls from bags, throwing dice, shuffling a pack of cards

Here is an example to generate a list containing n random into between a lower and an upper bound:

```
1
    import random
2
3
    def make random ints(num, lower bound, upper bound):
4
5
         Generate a list containing num random ints between lower bound
6
         and upper_bound. upper_bound is an open bound.
7
8
       result = []
9
       rng = random.Random()
10
        for i in range(num):
11
          result.append(rng.randrange(lower_bound, upper_bound))
12
```

```
>>> make_random_ints(5, 1, 13) # pick 5 random month numbers
[8, 1, 8, 5, 6]
```

Notice that we got a duplicate in the result. Often this is wanted, e.g. if we throw a die five times, we would expect some duplicates.

But what if you don't want duplicates? If you wanted 5 distinct months, then this algorithm is wrong. In this case a good algorithm is to generate the list of possibilities, shuffle it, and slice off the number of elements you want:

```
xs = list(range(1,13)) # make list 1..12. There are no duplicates
random.shuffle(xs) # shuffle the list
result = xs[:5] # take the first five elements.
```

In statistics courses, the first case — allowing duplicates — is usually described as pulling balls out of a bag *with replacement* — you put the drawn ball back in each time, so it can occur again. The latter case, with no duplicates, is usually described as pulling balls out of the bag *without replacement*. Once the ball is drawn, it doesn't go back to be drawn again. TV lotto games work like this.

The second "shuffle and slice" algorithm would not be so great if you only wanted a few elements, but from a very large domain. Suppose I wanted five numbers between one and ten million, without duplicates. Generating a list of ten million items, shuffling it, and then slicing off the first five would be a performance disaster! So let us have another try:

```
import random
 1
 2
 3
     def make_random_ints_no_dups(num, lower_bound, upper_bound):
 4
 5
         Generate a list containing num random ints between
 6
         Lower_bound and upper_bound. upper_bound is an open bound.
 7
         The result list cannot contain duplicates.
 8
9
        result = []
10
        rng = random.Random()
11
        for i in range(num):
12
           while True:
13
                candidate = rng.randrange(lower bound, upper bound)
14
                if candidate not in result:
15
                    break:
16
17
            result.append(candidate)
       return result
18
19
20
     xs = make_random_ints_no_dups(5, 1, 10000000)
21
     print(xs)
```

This agreeably produces 5 random numbers, without duplicates:

```
[3344629, 1735163, 9433892, 1081511, 4923270]
```

Even this function has its pitfalls. Can you spot what is going to happen in this case?

```
1 xs = make_random_ints_no_dups(10, 1, 6)
```

12.2. The time module

As we start to work with more sophisticated algorithms and bigger programs, at natural concern is "is our code efficient?" One way to experiment is to time how long various operations take. The time module has a function called clock that is recommended for this purpose. Whenever clock is called, it returns a floating point number representing how many seconds have elapsed since your program started running.

The way to use it is to call clock and assign the result to a variable, say t0, just before you start executing the code you want to measure. Then after execution, call clock again, (this time we'll save the result in variable t1). The difference t1-t0 is the time elapsed, and is a measure of how fast your program is running.

Let's try a small example. Python has a built-in <u>sum</u> function that can sum the elements in a list. We can also write our own. How do we think they would compare for speed? We'll try to do the summation of a list [0, 1, 2 ...] in both cases, and compare the results:

```
import time
1
2
3
    def do_my_sum(xs):
4
       sum = 0
5
       for v in xs:
6
            sum += v
7
        return sum
8
9
    sz = 10000000
                         # lets have 10 million elements in the list
10
    testdata = range(sz)
11
12
    t0 = time.clock()
    my_result = do_my_sum(testdata)
13
14
    t1 = time.clock()
    print("my_result = {0} (time taken = {1:.4f} seconds)"
15
                                         .format(my result, t1-t0))
16
17
18
    t2 = time.clock()
19
    their_result = sum(testdata)
20
    t3 = time.clock()
21
    print("their_result = {0} (time taken = {1:.4f} seconds)"
22
                                      .format(their_result, t3-t2))
```

On a reasonably modest laptop, we get these results:

```
my_sum = 49999995000000 (time taken = 1.5567 seconds)
their_sum = 49999995000000 (time taken = 0.9897 seconds)
```

So our function runs about 57% slower than their built-in one. And summing up ten million elements in under a second is not too shabby!

12.3. The math module

The math module contains the kinds of mathematical functions you'd typically find on your calculator (sin, cos, sqrt, asin, Log, Log10) and some mathematical constants like pi and e:

```
>>> import math
```

```
>>> math.pi
                           # constant attribute for pi
3.141592653589793
                           # constant natural log base
>>> math.e
2.718281828459045
>>> math.sqrt(2.0)
                           # square root function
1.4142135623730951
>>> math.radians(90)
                           # convert 90 degrees to radians
1.5707963267948966
>>> math.sin(math.radians(90)) # find sin of 90 degrees.
>>> math.asin(1.0) * 2
                           # Double arcsin of 1.0 to get pi
3.141592653589793
```

Like almost all other programming languages, angles are expressed in *radians* rather than degrees. There are two functions <u>radians</u> and <u>degrees</u> to convert between the two popular ways of measuring angles.

Notice another difference between this module and our use of random and turtle: in random and turtle we create objects and we call methods on the object. This is because objects have *state* — a turtle has a colour, a position, a heading, etc., and every random number generator has a seed value that determines its next result.

Mathematical functions are "pure" and don't have any state — calculating the square root of 2.0 doesn't depend on any kind of state or history about what happened in the past. So the functions are not methods of an object — they are simply functions that are grouped together in a module called *math*.

12.4. Creating your own modules

All we need to do to create our own modules is to save our script as a file with a .py extension on the filename. Suppose, for example, this script is saved as a file named seqtools.py:

```
def remove_at(pos, seq):
    return seq[:pos] + seq[pos+1:]
```

We can now use our module, both in scripts we write, or in the interactive Python interpreter. To do so, we must first *import* the module.

```
>>> import seqtools
>>> s = "A string!"
>>> seqtools.remove_at(4, s)
'A sting!'
```

We do not include the .py file extension when importing. Python expects the file names of Python modules to end in .py, so the file extention is not included in the import statement.

The use of modules makes it possible to break up very large programs into managable sized parts, and to keep related parts together.

12.5. Namespaces

A namespace is a collection of identifiers that belong to a module, or to a function, (and as we will see soon, in classes too). Generally, we like a namespace to hold "related" things, e.g. all the math

functions, or all the typical things we'd do with random numbers.

Each module has its own namespace, so we can use the same identifier name in multiple modules without causing an identification problem.

```
# module1.py
question = "What is the meaning of Life, the Universe, and Everything?"
answer = 42

# module2.py
question = "What is your quest?"
answer = "To seek the holy grail."
```

We can now import both modules and access question and answer in each:

```
import module1
import module2

print(module1.question)
print(module2.question)
print(module1.answer)
print(module2.answer)
```

will output the following:

```
What is the meaning of Life, the Universe, and Everything?
What is your quest?
42
To seek the holy grail.
```

Functions also have their own namespaces:

```
def f():
1
2
        n = 7
3
        print("printing n inside of f:", n)
4
5
    def g():
6
        n = 42
7
        print("printing n inside of g:", n)
8
9
    n = 11
    print("printing n before calling f:", n)
10
11
    f()
12
    print("printing n after calling f:", n)
13
    g()
    print("printing n after calling g:", n)
```

Running this program produces the following output:

```
printing n before calling f: 11
printing n inside of f: 7
printing n after calling f: 11
```

```
printing n inside of g: 42
printing n after calling g: 11
```

The three n's here do not collide since they are each in a different namespace — they are three names for three different variables, just like there might be three different instances of people, all called "Bruce".

Namespaces permit several programmers to work on the same project without having naming collisions.

How are namespaces, files and modules related?

Python has a convenient and simplifying one-to-one mapping, one module per file, giving rise to one namespace. Also, Python takes the module name from the file name, and this becomes the name of the namespace. math.py is a filename, the module is called math, and its namespace is math. So in Python the concepts are more or less interchangeable.

But you will encounter other languages (e.g. C#), that allow one module to span multiple files, or one file to have multiple namespaces, or many files to all share the same namespace. So the name of the file doesn't need to be the same as the namespace.

So a good idea is to try to keep the concepts distinct in your mind.

Files and directories organize *where* things are stored in our computer. On the other hand, namespaces and modules are a programming concept: they help us organize how we want to group related functions and attributes. They are not about "where" to store things, and should not have to coincide with the file and directory structures.

So in Python, if you rename the file <u>math.py</u>, its module name also changes, your <u>import</u> statements would need to change, and your code that refers to functions or attributes inside that namespace would also need to change.

In other languages this is not necessarily the case. So don't blur the concepts, just because Python blurs them!

12.6. Scope and lookup rules

The scope of an identifier is the region of program code in which the identifier can be accessed, or used.

There are three important scopes in Python:

- Local scope refers to identifiers declared within a function. These identifiers are kept in the namespace that belongs to the function, and each function has its own namespace.
- Global scope refers to all the identifiers declared within the current module, or file.
- Built-in scope refers to all the identifiers built into Python those like <u>range</u> and <u>min</u> that can be used without having to import anything, and are (almost) always available.

Python (like most other computer languages) uses precedence rules: the same name could occur in more than one of these scopes, but the innermost, or local scope, will always take precedence over the global scope, and the global scope always gets used in preference to the built-in scope. Let's start with a simple example:

```
def range(n):
    return 123*n
print(range(10))
```

What gets printed? We've defined our own function called range, so there is now a potential ambiguity. When we use range, do we mean our own one, or the built-in one? Using the scope lookup rules determines this: our own range function, not the built-in one, is called, because our function range is in the global namespace, which takes precedence over the built-in names.

So although names likes range and min are built-in, they can be "hidden" from your use if you choose to define your own variables or functions that reuse those names. (It is a confusing practice to redefine built-in names — so to be a good programmer you need to understand the scope rules and understand that you can do nasty things that will cause confusion, and then you avoid doing them!)

Now, a slightly more complex example:

This prints 17 10 3. The reason is that the two variables m and n in lines 1 and 2 are outside the function in the global namespace. Inside the function, new variables called n and m are created just for the duration of the execution of f. These are created in the local namespace of function f. Within the body of f, the scope lookup rules determine that we use the local variables f and f and f arguments to the print function refer to the original variables on lines 1 and 2, and these have not been changed in any way by executing function f.

Notice too that the def puts name f into the global namespace here. So it can be called on line 7.

What is the scope of the variable \underline{n} on line 1? Its scope — the region in which it is visible — is lines 1, 2, 6, 7. It is hidden from view in lines 3,4,5 because of the local variable \underline{n} .

12.7. Attributes and the dot operator

Variables defined inside a module are called attributes of the module. We've seen that objects have attributes too: for example, most objects have a __doc__ attribute, some functions have a __annotations__ attribute. Attributes are accessed by using the dot operator (.). The question attribute of module1 and module2 are accessed using module1.question and module2.question.

Modules contain functions as well as attributes, and the dot operator is used to access them in the same way. seqtools.remove_at refers to the remove_at function in the seqtools module.

When we use a dotted name, we often refer to it as a fully qualified name, because we're saying exactly which question attribute we mean.

12.8. Three import statement variants

Here are three different ways to import names into the current namespace, and to use them:

```
import math
  x = math.sqrt(10)
```

Here just the single identifier math is added to the current namespace. If you want to access one of the functions in the module, you need to use the dot notation to get to it.

Here is a different arrangement:

```
from math import cos, sin, sqrt x = sqrt(10)
```

The names are added directly to the current namespace, and can be used without qualification. The name math is not itself imported, so trying to use the qualified form math.sqrt would give an error.

Then we have a convenient shorthand:

```
from math import * # import all the identifiers from math,

# adding them to the current namespace.

x = sqrt(10) # Use them without qualification.
```

Of these three, the first method is generally preferred, even though it means a little more typing each time. (But hey, with nice editors that do auto-completion, and fast fingers, that's a small price!)

Finally, observe this case:

```
def area(radius):
    import math
    return math.pi * r * r

x = math.sqrt(10)  # this gives an error
```

Here we imported <u>math</u>, but we imported it into the local namespace of <u>area</u>. So the name is usable within the function body, but not in the enclosing script, because it is not in the global namespace.

12.9. Turn your unit tester into a module

Near the end of Chapter 6 we introduced unit testing, and our own <u>test</u> function, and you've had to copy this into each module for which you wrote tests. Now we can put that definition into a module of its own, say my_own_unit_tester.py, and simply use one line in each new script instead:

```
1 from my_own_unit_tester import test
```

12.10. Glossary

argv

argv is short for argument vector and is a variable in the sys module which stores a list of command line arguments passed to a program at run time.

attribute

A variable defined inside a module (or class or instance – as we will see later). Module attributes are accessed by using the dot operator (.).

command line

The sequence of characters read into the *command interpreter* in a *command line interface* (see the Wikipedia article on <u>command line interface</u> for more information).

command line argument

A value passed to a program along with the program's invocation at the *command prompt* of a command line interface (CLI).

command prompt

A string displayed by a command line interface indicating that commands can be entered.

continue statement

A statement that causes the current iteration of a loop to be skipped. The flow of execution goes back to the top of the loop, evaluates the condition, and proceeds accordingly, so further execution of the loop body may still take place.

dot operator

The dot operator () permits access to attributes and functions of a module (or attributes and methods of a class or instance – as we have seen elsewhere).

import statement

A statement which makes the objects contained in a module available for use within another module. There are two forms for the import statement. Using hypothetical modules named $\frac{\text{mymod1}}{\text{mymod2}}$ each containing functions $\frac{1}{1}$ and $\frac{1}{1}$, and variables $\frac{1}{1}$ and $\frac{1}{1}$, examples of these two forms include:

```
import mymod1
from mymod2 import f1, f2, v1, v2
```

The second form brings the imported objects into the namespace of the importing module, while the first form preserves a seperate namespace for the imported module, requiring mymod1.v1 to access the v1 variable from that module.

method

Function-like attribute of an object. Methods are *invoked* (called) on an object using the dot operator. For example:

```
>>> s = "this is a string."
>>> s.upper()
'THIS IS A STRING.'
>>>
```

We say that the method, upper is invoked on the string, \underline{s} . \underline{s} is implicitely the first argument to upper.

module

A file containing Python definitions and statements intended for use in other Python programs. The contents of a module are made available to the other program by using the import statement.

namespace

A syntactic container providing a context for names so that the same name can reside in different namespaces without ambiguity. In Python, modules, classes, functions and methods all form namespaces.

naming collision

A situation in which two or more names in a given namespace cannot be unambiguously resolved. Using

```
1 import string
```

instead of

```
1 from string import *
```

prevents naming collisions.

standard library

A library is a collection of software used as tools in the development of other software. The standard library of a programming language is the set of such tools that are distributed with the core programming language. Python comes with an extensive standard library.

12.11. Exercises

- 1. Open help for the calendar module.
 - a. Try the following:

```
import calendar
cal = calendar.TextCalendar()  # create an instance
cal.pryear(2011)  # What happens here?
```

- b. Observe that the week starts on Monday. An adventurous CompSci student believes that it is better mental chunking to have his week start on Thursday, because then there are only two working days to the weekend, and every week has a break in the middle. Read the documentation for TextCalendar, and see how you can help him print a calendar that suits his needs.
- c. Find a function to print just the month in which your birthday occurs this year.
- d. Try this:

```
d = calendar.LocaleTextCalendar(6, "SPANISH")
d.pryear(2011)
```

Try a few other languages, including one that doesn't work, and see what happens.

e. Experiment with calendar.isleap. What does it expect as an argument? What does it return as a result? What kind of a function is this?

Make detailed notes about what you learned from these exercises.

- 2. Open help for the math module.
 - a. How many functions are in the math module?
 - b. What does math.ceil do? What about math.floor?(hint: both floor and ceil expect floating point arguments.)
 - c. Describe how we have been computing the same value as math.sqrt without using the math module.
 - d. What are the two data contstants in the math module?

Record detailed notes of your investigation in this exercise.

- 3. Investigate the copy module. What does deepcopy do? In which exercises from last chapter would deepcopy have come in handy?
- 4. Create a module named mymodule1.py. Add attributes mymodule2.py. Add attributes mymodule2.py. Add attributes mymage set to 0, and year set to the year you were born. Now create a file named mamespace_test.py. Import both of the modules above and write the following statement:

```
print( (mymodule2.myage - mymodule1.myage) ==
(mymodule2.year - mymodule1.year) )
```

When you will run namespace_test.py you will see either True or False as output depending on whether or not you've already had your birthday this year.

5. Add the following statement to mymodule1.py, mymodule2.py, and namespace_test.py from the previous exercise:

```
print("My name is", __name__)
```

Run namespace_test.py. What happens? Why? Now add the following to the bottom of mymodule1.py:

```
if __name__ == '__main__':
    print("This won't run if I'm imported.")
```

Run mymodule1.py and namespace_test.py again. In which case do you see the new print statement?

6. In a Python shell / interactive interpreter, try the following:

```
>>> import this
```

What does Tim Peters have to say about namespaces?

7. Give the Python interpreter's response to each of the following from a continuous interpreter session:

```
>>> s = "If we took the bones out, it wouldn't be crunchy, would it?"
>>> s.split()
>>> type(s.split())
>>> s.split('o')
>>> s.split('i')
>>> '0'.join(s.split('o'))
```

Be sure you understand why you get each result. Then apply what you have learned to fill in the body of the function below using the split and join methods of str objects:

Your solution should pass the tests.

8. Create a module named wordtools.py with our test scaffolding in place.

Now add functions to these tests pass:

```
test(cleanword('what?'), 'what')
test(cleanword('"now!"'), 'now')
test(cleanword('?+="w-o-r-d!,@$()"'), 'word')
test(has_dashdash('distance--but'), True)
test(has_dashdash('several'), False)
test(has_dashdash('spoke--'), True)
test(has_dashdash('distance--but'), True)
test(has_dashdash('-yo-yo-'), False)
test(extract_words('Now is the time! "Now", is the time? Yes, now.'),
      ['now', 'is', 'the', 'time', 'now', 'is', 'the', 'time', 'yes', 'now'])
test(extract words('she tried to curtsey as she spoke--fancy'),
      ['she', 'tried', 'to', 'curtsey', 'as', 'she', 'spoke', 'fancy'])
test(wordcount('now', ['now','is','time','is','now','is','is']), 2)
test(wordcount('is', ['now','is','time','is','now','the','is']), 3)
test(wordcount('time', ['now','is','time','is','now','is','is']), 1)
test(wordcount('frog', ['now','is','time','is','now','is','is']), 0)
test(wordset(['now', 'is', 'time', 'is', 'now', 'is', 'is']),
test(longestword(['a', 'apple', 'pear', 'grape']), 5)
test(longestword(['a', 'am', 'I', 'be']), 2)
```

```
test(longestword(['this', 'supercalifragilisticexpialidocious']), 34)
test(longestword([]), 0)

Save this module so you can use the tools it contains in future programs.

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13. Files

13.1. About files

While a program is running, its data is stored in *random access memory* (RAM). RAM is fast and inexpensive, but it is also volatile, which means that when the program ends, or the computer shuts down, data in RAM disappears. To make data available the next time you turn on your computer and start your program, you have to write it to a non-volatile storage medium, such a hard drive, usb drive, or CD-RW.

Data on non-volatile storage media is stored in named locations on the media called files. By reading and writing files, programs can save information between program runs.

Working with files is a lot like working with a notebook. To use a notebook, you have to open it. When you're done, you have to close it. While the notebook is open, you can either write to it or read from it. In either case, you know where you are in the notebook. You can read the whole notebook in its natural order or you can skip around.

All of this applies to files as well. To open a file, you specify its name and indicate whether you want to read or write.

13.2. Writing our first file

Let's begin with a simple program that writes three lines of text into a file:

```
myfile = open('test.txt', 'w')
myfile.write("My first file written from Python\n")
myfile.write("----\n")
myfile.write("Hello, world!\n")
myfile.close()
```

Opening a file creates what we call a file handle. In this example, the variable myfile refers to the new handle object. Our program calls methods on the handle, and this makes changes to the actual file which is usually located on our disk.

On line 1, the open function takes two arguments. The first is the name of the file, and the second is the mode. Mode 'w' means that we are opening the file for writing.

If there is no file named test.txt on the disk, it will be created. If there already is one, it will be replaced by the file we are writing.

To put data in the file we invoke the write method on the handle, shown in lines 2, 3 and 4 above. In bigger programs, lines 2-4 will usually be replaced by a loop that writes many more lines into the file.

Closing the file handle (line 5) tells the system that we are done writing and makes the disk file available for reading by other programs (or by our own program).

A handle is somewhat like a TV remote control

We're all familiar with a remote control for a TV. You perform operations on the remote control — switch channels, change the volume, etc. But the real action happens on the TV. So, by simple analogy, we'd call the remote control your *handle* to the underlying TV.

Sometimes we want to emphasize the difference — the file handle is not the same as the file, and the remote control is not the same as the TV. But at other times we prefer to treat them as a single mental chunk, or abstraction, and we'll just say "close the file", or "flip the TV channel".

13.3. Reading a file line-at-a-time

Now that the file exists on our disk, we can open it, this time for reading, and read all the lines in the file, one at a time. This time, the mode argument is 'r' for reading:

```
1
    mynewhandle = open('test.txt', 'r')
2
    while True
                                         # keep reading forever
        theline = mynewhandle.readline() # try to read next line
3
        if len(theline) == 0:
4
                                          # if there are no more lines
5
            break
                                               leave the loop
6
7
        # Now process the line we've just read
8
        print(theline, end='')
9
10
    mynewhandle.close()
```

This is a handy pattern for our toolbox. In bigger programs, we'd squeeze more extensive logic into the body of the loop at line 8 — for example, if each line of the file contained the name and email address of one of our friends, perhaps we'd split the line into some pieces and call a function to send the friend a party invitation.

On line 8 we suppress the newline character that <pri>print</print usually appends to our strings. Why? This is because the string already has its own newline: the <pre>readline method in line 3 returns everything up to and including the newline character. This also explains the end-of-file detection logic: when there are no more lines to be read from the file, readline returns an empty string — one that does not even have a newline at the end, hence it's length is 0.

Bump your head first ..

In our sample case here, we have three lines in the file, yet we enter the loop *four* times. In Python, you only learn that the file has no more lines by bumping your head against the end of file, i.e. when you try to read a line that doesn't exist. In some other programming languages (e.g. Pascal), things are different: there you read three lines, but you have what is called *look ahead* — after reading the third line you already know that there are no more lines in the file. You're not even allowed to try to read the fourth line.

So the templates for working line-at-a-time in Pascal and Python are subtly different! When you transfer your Python skills to your next computer language, be sure to ask how you'll know when the file has ended: is the style in the language "try, and when you bump your head you'll know", or is it "look ahead"?

If we try to open a file that doesn't exist, we get an error:

```
>>> mynewhandle = open('wharrah.txt', 'r')
IOError: [Errno 2] No such file or directory: 'wharrah.txt'
```

13.4. Turning a file into a list of lines

It is often useful to fetch data from a disk file and turn it into a list of lines. Suppose we have a file containing our friends and their email addresses, one per line in the file. But we'd like the lines sorted into alphabetical order. A good plan is to read everything into a list of lines, then sort the list, and then write the sorted list back to another file:

```
f = open('friends.txt', 'r')
xs = f.readlines()
f.close()

xs.sort()

g = open('sortedfriends.txt', 'w')
for v in xs:
    g.write(v)
g.close()
```

The readlines method in line 2 reads all the lines and returns a list of the strings.

We could have used the template from the previous section to read each line one-at-a-time, and to build up the list ourselves, but it is a lot easier to use the method that the Python implementors gave us!

13.5. Reading the whole file at once

Another way of working with text files is to read the complete contents of the file into a string, and then to use our string-processing skills to work with the contents.

We'd normally use this method of processing files if we were not interested in the line structure of the file. For example, we've seen the split method on strings which can break a string into words. So here is how we might count the number of words in a file:

```
f = open('somefile.txt')
content = f.read()
f.close()

words = content.split()
print("There are {0} words in the file.".format(len(words)))
```

You will notice here that we left out the 'r' mode in line 1. By default, if you don't supply the mode, Python opens the file for reading.

13.6. Working with binary files

Files that hold photographs, videos, zip files, executable programs, etc. are called binary files: they're not organized into lines, and cannot be opened with a normal text editor. Python works just as easily with binary files, but when you read from the file you're going to get bytes back rather than a string.

Here we'll copy one binary file to another:

```
f = open('somefile.zip', 'rb')
1
2
    g = open('thecopy.zip', 'wb')
3
4
    while True:
5
        buf = f.read(1024)
6
        if len(buf) == 0:
7
             break
8
        g.write(buf)
9
10
    f.close()
11
    g.close()
```

There are a few new things here. In lines 1 and 2 we added a 'b' to the mode to tell Python that the files are binary rather than text files. In line 5, we see read can take an argument which tells it how many bytes to attempt to read from the file. Here we chose to read and write up to 1024 bytes on each iteration of the loop. When we get back an empty buffer from our attempt to read, we know we can break out of the loop and close both the files.

If you set a breakpoint at line 6, (or print type(buf) there) you'll see that the type of buf is bytes. We don't do any detailed work with bytes objects in this textbook.

13.7. An example

Many useful line-processing programs will read a text file line-at-a-time and do some minor processing as they write the lines to an output file. They might number the lines in the output file, or insert extra blank lines after every 60 lines to make it convenient for printing on sheets of paper, or extract some specific columns only from each line in the source file, or only print lines that contain a specific substring. We call this kind of program a filter.

Here is a filter that copies one file to another, omitting any lines that begin with #:

```
1
      def filter(oldfile, newfile):
2
         infile = open(oldfile, 'r')
3
         outfile = open(newfile, 'w')
4
         while True:
5
             text = infile.readline()
6
             if len(text) == 0:
7
                break
8
             if text[0] == '#':
9
                continue
10
11
             # put any more processing logic here
             outfile.write(text)
12
13
14
         infile.close()
15
         outfile.close()
```

The continue statement at line 9 skips over the remaining lines in the current iteration of the loop, but the loop will still iterate. This style looks a bit contrived here, but it is often useful to say "get the lines we're not concerned with out of the way early, so that we have cleaner more focussed logic in the meaty part of the loop that might be written around line 11."

Thus, if text is the empty string, the loop exits. If the first character of text is a hash mark, the flow of execution goes to the top of the loop, ready to start processing the next line. Only if both conditions fail do we fall through to do the processing at line 11, in this example, writing the line into the new file.

Let's consider one more case: suppose your original file contained empty lines. At line 6 above, would this program find the first empty line in the file, and terminate immediately? No! Recall that readline always includes the newline character in the string it returns. It is only when we try to read *beyond* the end of the file that we get back the empty string of length 0.

13.8. Directories

Files on non-volatile storage media are organized by a set of rules known as a file system. File systems are made up of files and directories, which are containers for both files and other directories.

When you create a new file by opening it and writing, the new file goes in the current directory (wherever you were when you ran the program). Similarly, when you open a file for reading, Python looks for it in the current directory.

If you want to open a file somewhere else, you have to specify the path to the file, which is the name of the directory (or folder) where the file is located:

```
>>> wordsfile = open('/usr/share/dict/words', 'r')
>>> wordlist = wordsfile.readlines()
>>> print(wordlist[:6])
['\n', 'A\n', "A's\n", 'AOL\n', "AOL\s\n", 'Aachen\n']
```

This (unix) example opens a file named words that resides in a directory named dict, which resides in share, which resides in usr, which resides in the top-level directory of the system, called /. It then reads in each line into a list using readlines, and prints out the first 5 elements from that list.

A Windows path might be "c:/temp/words.txt" or "c:\\temp\\words.txt". Because backslashes are used to escape things like newlines and tabs, you need to write two backslashes in a literal string to get one! So the length of these two strings is the same!

You cannot use $\overline{/}$ or $\overline{\backslash}$ as part of a filename; they are reserved as a delimiter between directory and filenames.

The file /usr/share/dict/words should exist on unix-based systems, and contains a list of words in alphabetical order.

13.9. What about fetching something from the web?

The Python libraries are pretty messy in places. But here is a very simple example that copies the contents at some web URL to a local file.

```
import urllib.request

url = 'http://xml.resource.org/public/rfc/txt/rfc793.txt'

destination_filename = 'rfc793.txt'

urllib.request.urlretrieve(url, destination_filename)
```

The <u>urlretrieve</u> function — just one call — could be used to download any kind of content from the Internet.

We'll need to get a few things right before this works:

- The resource we're trying to fetch must exist! Check this using a browser.
- We'll need permission to write to the destination filename, and the file will be created in the "current directory" i.e. the same folder that the Python program is saved in.
- If we are behind a proxy server that requires authentication, (as some students are), this may require some more special handling to work around our proxy. Use a local resource for the purpose of this demonstration!

Here is a slightly different example. Rather than save the web resource to our local disk, we read it directly into a string, and return it:

```
1
    import urllib.request
2
3
    def retrieve page(url):
        ''' Retrieve the contents of a web page.
5
            The contents is converted to a string before returning it.
6
7
        my socket = urllib.request.urlopen(url)
8
        dta = str(my_socket.readall())
9
        my socket.close()
10
        return dta
11
12
    the_text = retrieve_page("http://xml.resource.org/public/rfc/txt/rfc793.txt")
13
    print(the_text)
```

Opening the remote url returns what we call a socket. This is a handle to our end of the connection between our program and the remote web server. We can call read, write, and close methods on the socket object in much the same way as we can work with a file handle.

13.10. Glossary

delimiter

A sequence of one or more characters used to specify the boundary between separate parts of text.

directory

A named collection of files, also called a folder. Directories can contain files and other directories, which are referred to as *subdirectories* of the directory that contains them.

file

A named entity, usually stored on a hard drive, floppy disk, or CD-ROM, that contains a stream of characters.

file system

A method for naming, accessing, and organizing files and the data they contain.

handle

An object in our program that is connected to an underlying resource (e.g. a file). The file handle lets our program manipulate / read/ write / close the actual file that is on our disk.

fully qualified name

A name that is prefixed by some namespace identifier and the dot operator, or by an instance object, e.g. math.sqrt or tess.forward(10).

mode

A distinct method of operation within a computer program. Files in Python can be openned in one of three modes: read ('r'), write ('w'), and append ('a').

non-volatile memory

Memory that can maintain its state without power. Hard drives, flash drives, and rewritable compact disks (CD-RW) are each examples of non-volatile memory.

path

A sequence of directory names that specifies the exact location of a file.

text file

A file that contains printable characters organized into lines separated by newline characters.

socket

One end of a connection allowing one to read and write information to or from another computer.

volatile memory

Memory which requires an electrical current to maintain state. The *main memory* or RAM of a computer is volatile. Information stored in RAM is lost when the computer is turned off.

13.11. Exercises

- 1. Write a program that reads a file and writes out a new file with the lines in reversed order (i.e. the first line in the old file becomes the last one in the new file.)
- 2. Write a program that reads a file and prints only those lines that contain the substring snake.
- 3. Write a program that reads a text file and produces an output file which is a copy of the file, except the first five columns of each line contain a four digit line number, followed by a space. Start numbering the first line in the output file at 1. Ensure that every line number is formatted to the same width in the output file. Use one of your Python programs as test data for this exercise: your output should be a printed and numbered listing of the Python program.
- 4. Write a program that undoes the numbering of the previous exercise: it should read a file with numbered lines and produce another file without line numbers.

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14. List Algorithms

This chapter is a bit different from what we've done so far: rather than introduce more new Python syntax and features, we're going to focus on the program development process, and some algorithms that work with lists.

As in all parts of this book, our expectation is that you, the reader, will copy our code into your Python environment, play and experiment, and work along with us.

14.1. Test-driven development

Early in our Fruitful functions chapter we introduced the idea of incremental development, where we added small fragments of code to slowly build up the whole, so that we could easily find problems early. Later in that same chapter we introduced unit testing and gave code for our testing framework so that we could capture, in code, appropriate tests for the functions we were writing.

Test-driven development (TDD) is a software development practice which takes these practices one step further. The key idea is that automated tests should be written first. This technique is called test-driven because — if we are to believe the extremists — non-testing code should only be written when there is a failing test to make pass.

We can still retain our mode of working in small incremental steps, but now we'll define and express those steps in terms of a sequence of increasingly sophisticated unit tests that demand more from our code at each stage.

We'll turn our attention to some standard algorithms that process lists now, but as we proceed through this chapter we'll attempt to do so in the spirit envisaged by TDD.

14.2. The linear search algorithm

We'd like to know the index where a specific item occurs within in a list of items. Specifically, we'll return the index of the item if it is found, or we'll return -1 if the item doesn't occur in the list. Let us start with some tests:

```
friends = ["Joe", "Amy", "Brad", "Angelina", "Zuki", "Thandi", "Paris"]
   test(search_linear(friends, 'Amy'), 1)
   test(search_linear(friends, 'Joe'), 0)
test(search_linear(friends, 'Paris'), 6)
4
     test(search linear(friends, 'Bill'), -1)
```

Motivated by the fact that our tests don't even run, let alone pass, we now write the function:

```
def search_linear(xs, target):
       ''' Find and return the index of target in sequence xs '''
3
        for (i, v) in enumerate(xs):
           if v == target:
```

```
5 return i
6 return -1
```

There are a some points to learn here: We've seen a similar algorithm in section 8.10 when we searched for a character in a string. There we used a while loop, here we've used a for loop, coupled with enumerate to extract the (i, v) pair on each iteration. There are other variants — for example, we could have used range and made the loop run only over the indexes, or we could have used the idiom of returning None when the item was not found in the list. But the essential similarity in all these variations is that we test every item in the list in turn, from first to last, using the pattern of the short-circuit eureka traversal that we introduced in section 8.10 — that we return from the function as soon as we find the target that we're looking for.

Searching all items of a sequence from first to last is called a linear search. Each time we check whether v == target we'll call it a probe. We like to count probes as a measure of how efficient our algorithm is, and this will be a good enough indication of how long our algorithm will take to execute.

Linear searching is characterized by the fact that the number of probes needed to find some target depends directly on the length of the list. So if the list becomes ten times bigger, we can expect to wait ten times longer when searching for things. Notice too, that if we're searching for a target that is not present in the list, we'll have to go all the way to the end before we can return the negative value. So this case needs N probes, where N is the length of the list. However, if we're searching for a target that does exist in the list, we could be lucky and find it immediately in position 0, or we might have to look further, perhaps even all the way to the last item. On average, when the target is present, we're going to need to go about halfway through the list, or N/2 probes.

We say that this search has linear performance (linear meaning *straight Line*) because, if we were to measure the search times for different sizes of lists (N), and then plot a graph of time-to-search against N, we'd get a more-or-less straight line graph.

Analysis like this is pretty meaningless for small lists — the computer is quick enough not to bother if the list only has a handful of items. So generally, we're interested in the scalability of our algorithms — how do they perform if we throw bigger problems at them. Would this search be a sensible one to use if we had a million or ten million items (perhaps the catalog of books in your local library) in our list? What happens for really large datasets, e.g. how does Google search so brilliantly well?

14.3. A more realistic problem

As children learn to read, there are expectations that their vocabulary will grow. So a child of age 14 is expected to know more words than a child of age 8. When prescribing reading books for a grade, an important question might be "which words in this book are not in the expected vocabulary at this level?"

Let us assume we can read a vocabulary of words into our program, and read the text of a book, and split it into words. Let us write some tests for what we need to do next. Test data can usually be very small, even if we intend to finally use our program for larger cases:

Notice we were a bit lazy, and used <u>split</u> to create our list of words — it is easier than typing out the list, and very convenient if you want to input a sentence into the program and turn it into a list of words.

We now need to implement the function for which we've written tests, and we'll make use of our linear search. The basic strategy is to run through each of the words in the book, look it up in the vocabulary, and if it is not in the vocabulary, save it into a new resulting list which we return from the function:

```
def find_unknown_words(vocab, wds):
    """ Return a List of words in wds that do not occur in vocab """
    result = []
    for w in wds:
        if (search_linear(vocab, w) < 0):
            result.append(w)
    return result</pre>
```

We can happily report now that the tests all pass.

Now let us look at the scalability. We have more realistic vocabulary in a text file, so let us read in the file (as a single string) and split it into a list of words. For convenience, we'll create a function to do this for us, and test it on a file we happen to have available:

```
1
    def load words from file(filename):
         """ Read words from filename, return list of words. """
2
3
        f = open(filename, 'r')
4
        file content = f.read()
5
        f.close()
        wds = file_content.split()
6
7
        return wds
8
9
    bigger_vocab = load_words_from("vocab.txt")
    print("There are {0} words in the vocab, starting with\n {1} "
10
                   .format(len(bigger_vocab), bigger_vocab[:6]))
11
```

Python responds with:

```
There are 19469 words in the vocab, starting with ['a', 'aback', 'abacus', 'abandon', 'abandoned', 'abandonment']
```

So we've got a more sensible size vocabulary. Now let us load up a book. Loading a book is much like loading words from a file, but we're going to do a little extra black magic. Books are full of punctuation, and have mixtures of lowercase and uppercase letters. We need to clean up the contents of the book. This will involve removing punctuation, and converting everything to the same case (lowercase, because our vocabulary is all in lowercase). So we'll want a more sophisticated way of converting text to words.

There is a powerful translate method available for strings. The idea is that one sets up desired substitutions — for every character, we can give a corresponding replacement character. The translate method will apply these replacements throughout the whole string. So here we go:

```
1
     def text_to_words(the_text):
 2
         """ return a list of words with all punctuation removed,
 3
            and all in lowercase
 4
 5
 6
        my_substitutions = the_text.maketrans(
 7
          # if you find any of these
 8
          'ABCDEFGHIJKLMNOPQRSTUVWXYZ,.!?"-*+/>()0123456789[]:;\'',
 9
          # replace it by these
10
          'abcdefghijklmnopqrstuvwxyz
                                                                 ')
11
12
        # Translate the text now.
13
        cleaned_text = the_text.translate(my_substitutions)
14
        wds = cleaned_text.split()
15
         return wds
```

The translation turns all uppercase characters into lowercase, and all punctuation characters and digits into spaces. Then, of course, split will get rid of the spaces as it breaks the text into a list of words. The tests pass.

Now we're ready to read in our book:

```
1
     def get_words_in_book(filename):
         """ Read a book from filename, and return a list of its words.
2
        f = open(filename, 'r')
3
4
        content = f.read()
5
        f.close()
6
        wds = text to words(content)
7
        return wds
8
9
     book words = get words in book("AliceInWonderland.txt")
10
     print("There are \{0\} words in the book, starting with n\{1\}".
11
               format(len(book_words), book_words[:100]))
```

Python prints the following (all on one line, we've cheated a bit for the textbook):

```
There are 27336 words in the book, starting with
['alice', 's', 'adventures', 'in', 'wonderland', 'lewis', 'carroll',
    'chapter', 'i', 'down', 'the', 'rabbit', 'hole', 'alice', 'was',
    'beginning', 'to', 'get', 'very', 'tired', 'of', 'sitting', 'by',
    'her', 'sister', 'on', 'the', 'bank', 'and', 'of', 'having',
    'nothing', 'to', 'do', 'once', 'or', 'twice', 'she', 'had',
    'peeped', 'into', 'the', 'book', 'her', 'sister', 'was', 'reading',
    'but', 'it', 'had', 'no', 'pictures', 'or', 'conversations', 'in',
    'it', 'and', 'what', 'is', 'the', 'use', 'of', 'a', 'book',
    'thought', 'alice', 'without', 'pictures', 'or', 'conversation',
    'so', 'she', 'was', 'considering', 'in', 'her', 'own', 'mind',
    'as', 'well', 'as', 'she', 'could', 'for', 'the', 'hot', 'day',
    'made', 'her', 'feel', 'very', 'sleepy', 'and', 'stupid',
    'whether', 'the', 'pleasure', 'of', 'making', 'a']
```

Well now we have all the pieces ready. Let us see what words in this book are not in the vocabulary:

```
>>> missing_words = find_unknown_words(bigger_vocab, book_words)
```

We wait a considerable time now, something like a minute, before Python finally works its way through this, and prints a list of 3398 words in the book that are not in the vocabulary. Mmm... This is not particularly scaleable. For a vocabularly that is twenty times larger (you'll often find school dictionaries with 300 000 words, for example), and longer books, this is going to be slow. So let us make some timing measurements while we think about how we can improve this in the next section.

```
import time

t0 = time.clock()
missing_words = find_unknown_words(bigger_vocab, book_words)
t1 = time.clock()
print("There are {0} unknown words.".format(len(missing_words)))
print("That took {0:.4f} seconds.".format(t1-t0))
```

We get the results and some timing that we can refer back to later:

```
There are 3398 unknown words.
That took 49.8014 seconds.
```

14.4. Binary Search

If you think about what we've just done, it is not how we work in real life. If you were given a vocabulary and asked to tell if some word was present, you'd probably start in the middle. You can do this because the vocabulary is ordered — so you can probe some word in the middle, and immediately realize that your target was before (or perhaps after) the one you had probed. Applying this principle repeatedly leads us to a very much better algorithm for searching in a list of items that are already ordered. (Note that if the items are not ordered, you have little choice other than to look through all of them. But, if we know the items are in order, we can improve our searching technique).

Lets start with some tests. Remember, the list needs to be sorted:

```
xs = [2,3,5,7,11,13,17,23,29,31,37,43,47,53]
test(search_binary(xs, 20), -1)
test(search_binary(xs, 99), -1)
test(search_binary(xs, 1), -1)
for (i, v) in enumerate(xs):
    test(search_binary(xs, v), i)
```

Even our test cases are interesting this time: notice that we start with items not in the list and look at boundary conditions — in the middle of the list, less that all items in the list, bigger than the biggest. Then we use a loop to use every list item as a target, and to confirm that our binary search returns the corresponding index of that item in the list.

It is useful to think about having a *region-of-interest* (roi) within the list being searched. This roi will be the portion of the list in which it is still possible that our target might be found. Our algorithm will start with the roi set to all the items in the list. On the first probe in the middle of the roi, there are three possible outcomes: either we find the target, or we learn that we can discard the top half of the roi, or we learn that we can discard the bottom half of the roi. And we keep doing this repeatedly, until we find our target, or until we end up with no more items in our region of interest. We can code this as follows:

```
1
    def search_binary(xs, target):
2
         """ Find and return the index of key in sequence xs """
3
        1b = 0
4
        ub = len(xs)
5
        while True:
6
            if lb == ub: # if region of interest (roi) becomes empty
7
               return -1
8
9
            # next probe should be in the middle of the roi
10
            mid_index = (1b + ub) // 2
11
12
            # fetch the item at that position
13
            item_at_mid = xs[mid_index]
14
            # print("Roi[{0}:{1}](size={2}), probed='{3}', target='{4}'"
15
16
                    .format(lb, ub, ub-lb, item at mid, target))
17
18
            # how does the probed item compare to the target?
19
            if item at mid == target:
                                      # found it!
20
                return mid_index
21
            if item_at_mid < target:</pre>
22
                lb = mid_index + 1  # use upper half of roi next time
23
            else:
24
                                     # use lower half of roi next time
                ub = mid_index
```

The region of interest is represented by two variables, a lower bound <u>lb</u> and an upper bound <u>ub</u>. It is important to be precise about what values these indexes have. We'll make <u>lb</u> hold the index of the first item in the roi, and make <u>ub</u> hold the index just *beyond* the last item of interest. So these semantics are similar to a Python slice semantics: the region of interest is exactly the slice <u>xs[lb:ub]</u>. (The algorithm never actually takes any array slices!)

With this code in place, our tests pass. Great. Now if we substitute a call to this search algorithm instead of calling the search_linear in find_unknown_words, can we improve our performance? Let's do that, and again run this test:

```
t0 = time.clock()
missing_words = find_unknown_words(bigger_vocab, book_words)
t1 = time.clock()
print("There are {0} unknown words.".format(len(missing_words)))
print("That took {0:.4f} seconds.".format(t1-t0))
```

What a spectacular difference! More than 200 times faster!

```
There are 3398 unknown words.
That took 0.2262 seconds.
```

Why is this binary search so much faster than the linear search? If we uncomment the print statement on lines 15 and 16, we'll get a trace of the probes done during a search. Let's go ahead, and try that:

```
>>> search_binary(bigger_vocab, "magic")
Roi[0:19469](size=19469), probed='known', target='magic'
Roi[9735:19469](size=9734), probed='retailer', target='magic'
Roi[9735:14602](size=4867), probed='overthrow', target='magic'
Roi[9735:12168](size=2433), probed='mission', target='magic'
Roi[9735:10951](size=1216), probed='magnificent', target='magic'
Roi[9735:10343](size=608), probed='liken', target='magic'
```

```
Roi[10040:10343](size=303), probed='looks', target='magic'
Roi[10192:10343](size=151), probed='lump', target='magic'
Roi[10268:10343](size=75), probed='machete', target='magic'
Roi[10306:10343](size=37), probed='mafia', target='magic'
Roi[10325:10343](size=18), probed='magnanimous', target='magic'
Roi[10325:10334](size=9), probed='magical', target='magic'
Roi[10325:10329](size=4), probed= maggot', target='magic'
Roi[10328:10329](size=1), probed='magic', target='magic'
```

Here we see that finding the target word "magic" needed just 14 probes before it was found at index 10328. The important thing is that each probe more or less halves the remaining region of interest. By contrast, the linear search would have needed 10329 probes.

The word *binary* means *two*. Binary search gets its name from the fact that each probe splits the list into two pieces and discards the one half from the region of interst.

The beauty of the algorithm is that we could double the size of the vocabulary, and it would only need one more probe! And after another doubling, just another one probe. So as the vocabulary gets bigger, this algorithm's performance becomes even more impressive.

Can we put a formula to this? If our list size is N, what is the most number of probes k we could need? The maths is a bit easier if we turn the question around: how big a list N could we deal with if we were only allowed to make k probes?

With 1 probe, we can only search a list of size 1. With two probes we could cope with lists up to size 3 – (test the middle item with the first probe, then test either the left or right sublist with the remaining probe). With one more probe, we could cope with 7 items (the middle item, and two sublists of size 3). With four probes, we can search 15 items, and 5 probes lets us search up to 31 items. So the general relationship is given by the formula

$$N = 2^k - 1$$

where k is the number of probes we're allowed to make, and N is the maximum size of the list that can be searched in that many probes. This function is *exponential* in k – because k occurs as the exponent. If we wanted to turn the formula around and solve for k in terms of N, we need to move the constant 1 to the other side, and take a log (base 2) on each side. (The log is the inverse of an exponent.) So the formula for k in terms of N is now:

$$k = \lceil \log_2(N+1) \rceil$$

The square-only-on-top brackets are called *ceiling brackets*: this means that you must round the number up to the next whole integer.

Let us try this on a calculator, or in Python, which is the mother of all calculators: suppose I have 1000 elements to be searched, what is the maximum number of probes I'll need? (There is a pesky +1 in the formula, so let us not forget to add it on...):

```
>>> from math import log
>>> log(1000 + 1, 2)
9.967226258835993
```

Telling us that we'll need 9.96 probes maximum, to search 1000 items is not quite what we want. We forgot to take the ceiling. The ceil function in the math module does exactly this. So more accurately,

now:

This tells us that searching 1000 items needs 10 probes. (Well technically, with 10 probes we can search exactly 1023 items, but the easy and useful stuff to remember here are that "1000 items needs 10 probes, a million needs 20 probes, and a billion items only needs 30 probes").

You will rarely encounter algorithms that scale to large datasets as beautifully as binary search does!

14.5. Removing adjacent duplicates from a list

We often want to get the unique elements in a list, i.e. produce a new list in which each different element occurs just once. Consider our case of looking for words in Alice in Wonderland that are not in our vocabulary. We had a report that there are 3398 such words, but there are duplicates in that list. In fact, the word "alice" occurs 398 times in the book, and it is not in our vocabulary! How should we remove these duplicates?

A good approach is to sort the list, then remove all adjacent duplicates. Let us start with removing adjacent duplicates

The algorithm is easy and efficient. We simply have to remember the most recent item that was inserted into the result, and avoid inserting it again:

```
1
     def remove adjacent dups(xs):
         """ Return a new list in which all adjacent
2
3
            duplicates from xs have been removed.
4
5
         result = []
6
         most_recent_elem = None
7
         for e in xs:
8
            if e != most_recent_elem:
9
                 result.append(e)
10
                 most_recent_elem = e
11
12
         return result
```

The amount of work done in this algorithm is linear — each item in xs causes the loop to execute exactly once, and there are no nested loops. So doubling the number of elements in xs should cause this program to run twice as long: the relationship between the size of the list and the time to run will be graphed as a straight (linear) line.

Let us go back now to our analysis of *Alice in Wonderland*. Before checking the words in the book against the vocabulary, we'll sort those words into order, and eliminate duplicates. So our new code looks like this:

Almost magically, we get the following output:

```
There are 27336 words in the book. Only 2570 are unique.
The first 100 words are
['_i_', 'a', 'abide', 'able', 'about', 'above', 'absence', 'absurd',
'acceptance', 'accident', 'accidentally', 'account', 'accounting',
'accounts', 'accusation', 'accustomed', 'ache', 'across', 'act',
'actually', 'ada', 'added', 'adding', 'addressed', 'addressing',
'adjourn', 'adoption', 'advance', 'advantage', 'adventures',
'advice', 'advisable', 'advise', 'affair', 'affectionately',
'afford', 'afore', 'afraid', 'after', 'afterwards', 'again',
'against', 'age', 'ago', 'agony', 'agree', 'ah', 'ahem', 'air',
'airs', 'alarm', 'alarmed', 'alas', 'alice', 'alive', 'all',
'allow', 'almost', 'alone', 'along', 'aloud', 'already', 'also',
'altered', 'alternately', 'altogether', 'always', 'am', 'ambition',
'among', 'an', 'ancient', 'and', 'anger', 'angrily', 'angry',
'animal', 'animals', 'ann', 'annoy', 'annoyed', 'another',
'answer', 'answered', 'answers', 'antipathies', 'anxious',
'anxiously', 'any', 'anything', 'anywhere', 'appealed', 'appear',
'appearance', 'appeared', 'appearing', 'applause', 'apple',
'apples', 'arch']
```

It should surprise you that Lewis Carroll was able to write a classic piece of literature using only 2570 different words!

14.6. Merging sorted lists

Suppose we have two sorted lists. Devise an algorithm to merge them together into a single sorted list.

A simple but inefficient algorithm could be to simply append the two lists together, and sort the result:

```
newlist = (xs + ys)
newlist.sort()
```

But this doesn't take advantage of the fact that the two lists are already sorted, and is going to have poor scaleability and performance for very large lists.

Lets get some tests together first:

```
1 xs = [1,3,5,7,9,11,13,15,17,19]
```

Here is our merge algorithm:

```
1
     def merge(xs, ys):
         """ merge sorted lists xs and ys. Return a sorted result """
 2
 3
        result = []
 4
        xi = 0
 5
        yi = 0
 6
 7
        while True:
            if xi >= len(xs): # if xs list is finished,
 8
9
                result.extend(ys[yi:]) # add remaining items from ys
10
                return result; # and we're done.
11
            if yi >= len(ys):
12
                                     # Same again, but swap roles
13
                result.extend(xs[xi:])
14
                return result;
15
16
            # Both lists still have items, copy smaller item to result.
17
            if xs[xi] <= ys[yi]:</pre>
18
                result.append(xs[xi])
19
                xi += 1
20
            else:
21
                result.append(ys[yi])
22
                yi += 1
```

The algorithm works as follows: we create a result list, and keep two indexes, one into each list (lines 3–5). On each iteration of the loop, whichever list item is smaller is copied to the result list, and that list's index is advanced. As soon as either index reaches the end of its list, we copy all the remaining items from the other list into the result, which we return.

14.7. Alice in Wonderland, again!

Underlying the algorithm for merging sorted lists is a deep pattern of computation that is widely reusable. The pattern essence is "Run through the lists always processing the smallest remaining items from each, with these cases to consider:"

- What should we do when either list has no more items?
- What should we do if the smallest items from each list are equal to each other?
- What should we do if the smallest item in the first list is smaller than the smallest one the second list?
- · What should we do in the remaining case?

Lets assume we have two sorted lists. Exercise your algorithmic skills by adapting the merging algorithm pattern for each of these cases:

Return only those items that are present in both lists.

- Return only those items that are present in the first list, but not in the second.
- Return only those items that are present in the second list, but not in the first.
- Return items that are present in either the first or the second list.
- Return items from the first list that are not eliminated by a matching element in the second list. In this case, an item in the second list "knocks out" just one matching item in the first list. This operation is sometimes called *bagdiff*. For example bagdiff([5,7,11,11,12,13], [7,8,11]) would return [5,11,11,12,13]

In the previous section we sorted the words from the book, and elimated duplicates. Our vocabulary is also sorted. So third case above — find all items in the second list that are not in the first list, would be another way to implement find_unknown_words. Instead of searching for every word in the dictionary (either by linear or binary search), why not use a variant of the merge to return the words that occur in the book, but not in the vocabulary.

```
1
     def find_unknowns_merge_pattern(vocab, wds):
         """ Both the vocab and wds must be sorted. Return a new
2
3
            list of words from wds that do not occur in vocab.
4
5
6
         result = []
7
         xi = 0
8
         yi = 0
9
         while True:
10
11
            if xi >= len(vocab):
12
                 result.extend(wds[yi:])
13
                 return result
14
15
            if yi >= len(wds):
16
                 return result
17
             if vocab[xi] == wds[yi]: # good, word exists in vocab
18
19
                yi += 1
20
             elif vocab[xi] < wds[yi]: # move past this vocab word,</pre>
21
22
                xi += 1
23
24
             else:
                                       # got word that is not in vocab
25
                 result.append(wds[yi])
26
                 yi += 1
```

Now we put it all together:

```
all_words = get_words_in_book("AliceInWonderland.txt")
t0 = time.clock()
all_words.sort()
book_words = remove_adjacent_dups(all_words)
missing_words = find_unknowns_merge_pattern(bigger_vocab, book_words)
t1 = time.clock()
print("There are {0} unknown words.".format(len(missing_words)))
print("That took {0:.4f} seconds.".format(t1-t0))
```

Even more stunning performance here:

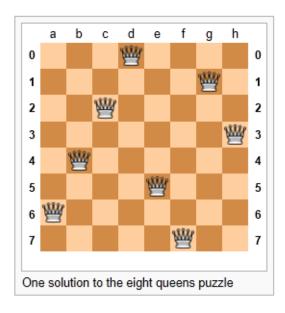
```
There are 828 unknown words.
That took 0.0410 seconds.
```

Let's review what we've done. We started with a word-by-word linear lookup in the vocabulary that ran in about 50 seconds. We implemented a clever binary search, and got that down to 0.22 seconds, more than 200 times faster. But then we did something even better: we sorted the words from the book, eliminated duplicates, and used a merging pattern to find words from the book that were not in the dictionary. This was about five times faster than even the binary lookup algorithm. At the end of the chapter our algorithm is more than a 1000 times faster than our first attempt!

That is what we can call a good day at the office!

14.8. Eight queens puzzle, part 1

As told by Wikipedia, "The eight queens puzzle is the problem of placing eight chess queens on an 8x8 chessboard so that no two queens attack each other. Thus, a solution requires that no two queens share the same row, column, or diagonal."



Please try this yourself, and find a few more solutions by hand.

We'd like to write a program to find solutions to the this puzzle. In fact, the puzzle generalizes to placing N queens on an NxN board, so we're going to think about the general case, not just the 8x8 case. Perhaps we can find solutions for 12 queens on a 12x12 board, or 20 queens on a 20x20 board.

How do we approach a complex problem like this? A good starting point is to think about our *data structures* — how exactly do we plan to represent the state of the chessboard and its queens in our program? Once we have some handle on what our puzzle is going to look like in memory, we can begin to think about the functions and logic we'll need to solve the puzzle, i.e. how do we put another queen onto the board somewhere, and to check whether it clashes with any of the queens already on the board.

The steps of finding a good representation, and then finding a good algorithm to operate on the data cannot always be done independently of each other. As you think about the operations you require, you may want to change or reorganize the data somewhat to make it easier to do the operations you need.

This relationship between algorithms and data was elegantly expressed in the title of a book Algorithms + Data Structures = Programs, written by one of the pioneers in Computer Science, Niklaus Wirth, the inventor of Pascal.

Let's brainstorm some ideas about how a chessboard and queens could be represented in memory.

• A two dimensional matrix (a list of 8 lists, each containing 8 squares) is one possibility. At each square of the board would like to know whether it contains a queen or not — just two possible states for each square — so perhaps each element in the lists could be True or False, or, more simply, 0 or 1.

Our state for the solution above could then have this data representation:

You should also be able to see how the empty board would be represented, and you should start to imagine what operations or changes you'd need to make to the data to place another queen somewhere on the board.

• Another idea might be to keep a list of coordinates of where the queens are. Using the notation in the illustration, for example, we could represent the state of that solution as:

```
bd2 = [ 'a6', 'b4', 'c2', 'd0', 'e5', 'f7', 'g1', 'h3' ]
```

• We could make other tweaks to this — perhaps each element in this list should rather be a tuple, with integer coordinates for both axes. And being good computer scientists, we'd probably start numbering each axis from 0 instead of at 1. Now our representation could be:

```
bd3 = [(0,6), (1,4), (2,2), (3,0), (4,5), (5,7), (6,1), (7,3)]
```

• Looking at this representation, we can't help but notice that the first coordinates are 0,1,2,3,4,5,6,7 and they correspond exactly to the index position of the pairs in the list. So we could discard them, and come up with this really compact alternative representation of the solution:

```
1 bd4 = [6, 4, 2, 0, 5, 7, 1, 3]
```

This will be what we'll use, let's see where that takes us.

This representation is not genera

We've come up with a great representation. But will it work for other puzzles? Our list representation has the constraint that one can only put one queen in each column. But that is a puzzle constraint anyway — no two queens are allowed to share the same column. So

puzzle and data representation are well matched.

But if we were trying to solve a different puzzle on a chessboard, perhaps play a game of checkers, where many pieces could occupy the same column, our representation would not work.

Let us now take some grand insight into the problem. Do you think it is a coincidence that there are no repeated numbers in the solution? The solution [6,4,2,0,5,7,1,3] contains the numbers 0,1,2,3,4,5,6,7, but none are duplicated! Could other solutions contain duplicate numbers, or not?

A little thinking should convince you that there can never be duplicate numbers in a solution: the numbers represent the row on which the queen is placed, and because we are never permitted to put two queens in the same row, no solution will ever have duplicate row numbers in it.

Our key insight

In our representation, any solution to the N queens problem must therefore be a permutation of the numbers [0..N-1].

Note that not all permutations are solutions. For example, [0,1,2,3,4,5,6,7] has all queens on the same diagonal.

Wow, we seem to be making progress on this problem merely by thinking, rather than coding!

Our algorithm should start taking shape now. We can start with the list [0..N-1], generate various permutations of that list, and check each permutation to see if it has any clashes (queens that are on the same diagonal). If it has no clashes, it is a solution, and we can print it.

Let us be precise and clear on this issue: if we only use permutations of the rows, and we're using our compact representation, no queens can clash on either rows or columns, and we don't even have to concern ourselves with those cases. So the only clashes we need to test for are clashes on the diagonals.

It sounds like a useful function will be one that can test if two queens share a diagonal. Each queen is on some (x,y) position. So does the queen at (5,2) share a diagonal with the one at (2,0)? Does (5,2) clash with (3,0)?

```
test(share_diagonal(5,2,2,0), False)
test(share_diagonal(5,2,3,0), True)
test(share_diagonal(5,2,4,3), True)
test(share_diagonal(5,2,4,1), True)
```

A little geometry will help us here. A diagonal has a slope of either 1 or -1. The question we really want to ask is *is their distance between them the same in the x and the y direction?* If it is, they share a diagonal. Because diagonals can be to the left or right, it will make sense for this program to use the absolute distance in each direction:

```
def share_diagonal(x0, y0, x1, y1):

""" Is (x0, y0) on a shared diagonal with (x1, y1)? """

dy = abs(y1 - y0)  # calc the absolute y distance
dx = abs(x1 - x0)  # calc the absolute x distance
return dx == dy  # they clash if dx == dy
```

If you copy the code and run it, you'll be happy to learn that the tests pass!

Now let's consider how we construct a solution by hand. We'll put a queen somewhere in the first column, then place one in the second column, only if it does not clash with the one already on the board. And then we'll put a third one on, checking it against the two queens already to its left. When we consider the queen on column 6, we'll need to check for clashes against those in all the columns to its left, i.e. in columns 0,1,2,3,4,5.

So the next building block is a function that, given a partially completed puzzle, can check whether the queen at column c clashes with any of the queens to its left, at columns 0,1,2,...c-1:

```
1
    # solutions should not have any clashes
2
      test(col_clashes([6,4,2,0,5], 4), False)
3
      test(col_clashes([6,4,2,0,5,7,1,3], 7), False)
4
    # Now some test cases that should mostly clash
5
     test(col_clashes([0,1], 1), True)
     test(col_clashes([5,6], 1), True)
7
      test(col_clashes([6,5], 1), True)
8
     test(col_clashes([0,6,4,3], 3), True)
      test(col_clashes([5,0,7], 2), True)
9
      test(col_clashes([2,0,1,3], 1), False)
10
11
      test(col_clashes([2,0,1,3], 2), True)
```

Here is our function that makes them all pass:

```
1
    def col_clashes(bs, c):
2
        """ Return True if the queen at column c clashes
3
            with any queen to its left.
4
5
       for i in range(c): # look at all columns to the left of c
6
             if share_diagonal(i, bs[i], c, bs[c]):
7
                 return True
8
9
       return False
                             # no clashes - col c has a safe placement.
```

Finally, we're going to give our program one of our permutations — i.e. all queens placed somewhere, one on each row, one on each column. But does the permutation have any diagonal clashes?

```
test(has_clashes([6,4,2,0,5,7,1,3]), False) # solution from above test(has_clashes([4,6,2,0,5,7,1,3]), True) # swap rows of first two test(has_clashes([0,1,2,3]), True) # try small 4x4 board test(has_clashes([2,0,3,1]), False) # solution to 4x4 case
```

And the code to make the tests pass:

```
def has_clashes(the_board):
    """ Determine whether we have any queens clashing on the diagonals.
    We're assuming here that the_board is a permutation of column
    numbers, so we're not explicitly checking row or column clashes.

for col in range(1,len(the_board)):
    if col_clashes(the_board, col):
        return True
```

return False

Summary of what we've done so far: we now have a powerful function called has_clashes that can tell if a configuration is a solution to the queens puzzle. Let's get on now with generating lots of permutations and finding solutions!

14.9. Eight queens puzzle, part 2

This is the fun, easy part. We could try to find all permutations of [0,1,2,3,4,5,6,7] — that might be algorithmically challenging, and would be a *brute force* way of tackling the problem. We just try everything, and find all possible solutions.

Of course we know there are N! permutations of N things, so we can get an early idea of how long it would take to search all of them for all solutions. Not too long at all, actually – 8! is only 40320 different cases to check out. This is vastly better than starting with 64 places to put eight queens. If you do the sums for how many ways can you choose 8 of the 64 squares for your queens, the formula (called *N choose k* where you're choosing k=8 squares of the available N=64) yieds a whopping 4426165368, obtained from $(64! / (8! \times 56!))$.

So our earlier key insight — that we only need to consider permutations — has reduced what we call the *problem space* from about 4.4 billion cases to just 40320!

We're not even going to explore all those, however. When we introduced the random number module, we learnt that it had a <u>shuffle</u> method that randomly permuted a list of items. So we're going to write a "random" algorithm to find solutions to the N queens problem. We'll begin with the permutation [0,1,2,3,4,5,6,7] and we'll repeatedly shuffle the list, and test each to see if it works! Along the way we'll count how many attempts we need before we find each solution, and we'll find 10 solutions (we could hit the same solution more than once, because shuffle is random!):

```
1
    def main():
2
        import random
3
        rng = random.Random() # instantiate a generator
4
        bd = list(range(8))
5
                               # generate the initial permutation
6
        numFound = 0
7
        tries = 0
8
        while numFound < 10:
9
           rng.shuffle(bd)
10
           tries += 1
           if not has_clashes(bd):
11
               print('Found solution {0} in {1} tries.'.format(bd, tries))
12
13
               tries = 0
14
               numFound += 1
15
16
    main()
```

Almost magically, and at great speed, we get this:

```
Found solution [3, 6, 2, 7, 1, 4, 0, 5] in 693 tries.
Found solution [5, 7, 1, 3, 0, 6, 4, 2] in 82 tries.
Found solution [3, 0, 4, 7, 1, 6, 2, 5] in 747 tries.
Found solution [1, 6, 4, 7, 0, 3, 5, 2] in 428 tries.
Found solution [6, 1, 3, 0, 7, 4, 2, 5] in 376 tries.
Found solution [3, 0, 4, 7, 5, 2, 6, 1] in 204 tries.
```

```
Found solution [4, 1, 7, 0, 3, 6, 2, 5] in 98 tries.

Found solution [3, 5, 0, 4, 1, 7, 2, 6] in 64 tries.

Found solution [5, 1, 6, 0, 3, 7, 4, 2] in 177 tries.

Found solution [1, 6, 2, 5, 7, 4, 0, 3] in 478 tries.
```

Here is an interesting fact about this algorithm. There are know to be 92 solutions to this puzzle, and we know there are 40320 permutations, all in all. So on average, you probably need to try 40320/92 shuffles which is about 438, before you stumble across a solution. The number of tries we printed looks like our experimental data agrees quite nicely with our theory!

14.10. Glossary

binary search

A famous algorithm that searches for a target in a sorted list. Each probe in the list allows us to discard half the remaining items, so the algorithm is very efficient.

linear

Relating to a straight line. Here, we talk about graphing how the time taken by an algorithm depends on the size of the data it is processing. Linear algorithms have straight-line graphs that can describe this relationship.

linear search

A search that probes each item in a list or sequence, from first, until it finds what it is looking for. It is used for searching for a target in unordered lists of items.

Merge algorithm

An efficient algorithm that merges two already sorted lists, to produce a sorted list result. The merge algorithm is really a pattern of computation that can be adapted and reused for various other scenarios, such as finding words that are in a book, but not in a vocabulary.

probe

Each time we take a look when searching for an item is called a probe. In our chapter on *Iteration* we also played a guessing game where the computer tried to guess the user's secret number. Each of those tries would also be called a probe.

test-driven development (TDD)

A software development practice which arrives at a desired feature through a series of small, iterative steps motivated by automated tests which are *written first* that express increasing refinements of the desired feature. (see the Wikipedia article on <u>Test-driven development</u> for more information.)

14.11. Exercises

- 1. The section in this chapter called <u>Alice in Wonderland, again!</u> started with the observation that the merge algorithm uses a pattern that can be reused in other situations. Adapt the merge algorithm to write each of these functions, as was suggested there:
 - a. Return only those items that are present in both lists.
 - b. Return only those items that are present in the first list, but not in the second.
 - c. Return only those items that are present in the second list, but not in the first.
 - d. Return items that are present in either the first or the second list.
 - e. Return items from the first list that are not eliminated by a matching element

in the second list. In this case, an item in the second list "knocks out" just one matching item in the first list. This operation is sometimes called *bagdiff*. For example bagdiff([5,7,11,11,11,12,13], [7,8,11]) would return [5,11,11,12,13]

- 2. Modify the queens program to solve some boards of size 4, 12, and 16. What is the maximum size puzzle you can usually solve in under a minute?
- 3. Adapt the queens program so that we keep a list of solutions that have already printed, so that we don't print the same solution more than once.
- 4. Chess boards are symmetric: if we have a solution to the queens problem, its mirror solution either flipping the board on the X or in the Y axis, is also a solution. And giving the board a 90 degree, 180 degree, or 270 degree rotation is also a solution. In some sense, solutions that are just mirror images or rotations of other solutions in the same family are less interesting than the unique "core cases". Of the 92 solutions for the 8 queens problem, there are only 12 unique families if you take rotations and mirror images into account. Wikipedia has some fascinating stuff about this.
 - a. Write a function to mirror a solution in the Y axis,
 - b. Write a function to mirror a solution in the X axis,
 - c. Write a function to rotate a solution by 90 degrees anti-clockwise, and use this to provide 180 and 270 degree rotations too.
 - d. Write a function which is given a solution, and it generates the family of symmetries for that solution. For example, the symmetries of [0,4,7,5,2,6,1,3] are

```
[[0,4,7,5,2,6,1,3],[7,1,3,0,6,4,2,5],
[4,6,1,5,2,0,3,7],[2,5,3,1,7,4,6,0],
[3,1,6,2,5,7,4,0],[0,6,4,7,1,3,5,2],
[7,3,0,2,5,1,6,4],[5,2,4,6,0,3,1,7]]
```

- e. Now adapt the queens program so it won't list solutions that are in the same family. It only prints solutions from unique families.
- 5. Every week a computer scientist buys four lotto tickets. He always choses the same prime numbers, with the hope that he ever hits the jackpot, he will be able to go on TV and tell everyone his secret and this will suddenly create widespread public interest in prime numbers. He represents his weekly tickets in Python as a list of lists:

Complete these exercises.

- a. Each lotto draw takes six random balls, numbered from 1 to 49. Write a function to return a lotto draw.
- b. Write a function that returns compares a single ticket and a draw, and returns the number of correct picks on that ticket:

```
test(lotto_match([42,4,7,11,1,13], [2,5,7,11,13,17]), 3)
```

c. Write a function that takes a list of tickets and a draw, and returns a list telling how many picks were correct on each ticket:

```
test(lotto_matches([42,4,7,11,1,13], my_tickets), [1,2,3,1])
```

d. Write a function that takes a list of integers, and returns the number of primes in the list:

```
test(primes_in([42, 4, 7, 11, 1, 13]), 3)
```

e. Write a function to discover whether the computer scientist has missed any prime numbers in his selection of the four tickets. Return a list of all primes that he has missed:

```
test(prime_misses(my_tickets), [3, 29, 47])
```

- f. Write a function that repeatedly makes a new draw, and compares the draw to the four tickets.
 - Count how many draws are needed until one of the computer scientist's tickets has at least 3 correct picks. Try the experiment twenty times, and average out the number of draws needed.
 - ii. How many draws are needed, on average, before he gets at least 4 picks correct?
 - iii. How many draws are needed, on average, before he gets at least 5 correct? (Hint: this might take a while. It would be nice if you could print some dots, like a progress bar, to show when each of the 20 experiments has completed.)

Notice that we have difficulty constructing test cases here, because our random numbers are not deterministic. Automated testing only really works if you already know what the answer should be!

6. Read Alice in Wonderland. You can read the plain text version we have with this textbook, or if you have e-book reader software on your PC, or a Kindle, iPhone, Android, etc. you'll be able to find a suitable version for your device at http://www.gutenberg.org/. They also have html and pdf versions, with pictures, and thousands of other classic books!

How to Think Like a Computer Scientist: Learning with Python 3 »

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15. Classes and Objects – the Basics

15.1. Object-oriented programming

Python is an object-oriented programming language, which means that it provides features that support object-oriented programming (OOP).

Object-oriented programming has its roots in the 1960s, but it wasn't until the mid 1980s that it became the main programming paradigm used in the creation of new software. It was developed as a way to handle the rapidly increasing size and complexity of software systems, and to make it easier to modify these large and complex systems over time.

Up to now, most of the programs we have been writing use a procedural programming paradigm. In procedural programming the focus is on writing functions or *procedures* which operate on data. In object-oriented programming the focus is on the creation of objects which contain both data and functionality together. (We have seen turtle objects, string objects, and random number generators, to name a few places where we've already worked with objects.)

Usually, each object definition corresponds to some object or concept in the real world, and the functions that operate on that object correspond to the ways real-world objects interact.

15.2. User-defined compound data types

We've already seen classes like str, int, float and Turtle. We are now ready to create our own userdefined class: the Point.

Consider the concept of a mathematical point. In two dimensions, a point is two numbers (coordinates) that are treated collectively as a single object. Points are often written in parentheses with a comma separating the coordinates. For example, (0, 0) represents the origin, and (x, y)represents the point x units to the right and y units up from the origin.

Some of the typical operations that one associates with points might be calculating the distance of a point from the origin, or from another point, or finding a midpoint of two points, or asking if a point falls within a given rectangle or circle. We'll shortly see how we can organize these together with the data.

A natural way to represent a point in Python is with two numeric values. The question, then, is how to group these two values into a compound object. The quick and dirty solution is to use a tuple, and for some applications that might be a good choice.

An alternative is to define a new class. This approach involves a bit more effort, but it has advantages that will be apparent soon. We'll want our points to each have an \bar{x} and a \bar{y} attribute, so our first class definition looks like this:

```
class Point:
    """ Point class represents and manipulates x,y coords.
```

```
def __init__(self):
    """ Create a new point at the origin """
self.x = 0
self.y = 0
```

Class definitions can appear anywhere in a program, but they are usually near the beginning (after the <u>import</u> statements). Some programmers and languages prefer to put every class in a module of its own — we won't do that here. The syntax rules for a class definition are the same as for other compound statements. There is a header which begins with the keyword, <u>class</u>, followed by the name of the class, and ending with a colon. You'll know where the class ends by looking at the indentation.

If the first line after the class header is a string, it becomes the docstring of the class, and will be recognized by various tools. (This is also the way docstrings work in functions.)

Every class should have a method with the special name <u>__init__</u>. This initializer method is automatically called whenever a new instance of <u>Point</u> is created. It gives the programmer the opportunity to set up the attributes required within the new instance by giving them their initial state / values. The <u>self</u> parameter (you could choose any other name, but nobody ever does!) is automatically set to reference the newly created object that needs to be initialized.

So let's use our new Point class now...

```
p = Point()  # Instantiate an object of type Point
q = Point()  # and make a second point

print(p.x, p.y, q.x, q.y) # Each point object has its own x and y
```

This program prints:

```
0 0 0 0
```

because during the initialization of the objects, we created two attributes called x and y for each, and gave them both the value 0.

This should look familiar — we've used classes before to create more than one object:

```
from turtle import Turtle

tess = Turtle()  # Instantiate objects of type Turtle
alex = Turtle()
```

The variables p and q are assigned references to two new <u>Point</u> objects. A function like <u>Turtle</u> or <u>Point</u> that creates a new object instance is called a constructor, and every class automatically provides a constructor function which is named the same as the class.

It may be helpful to think of a class as a *factory* for making objects. The class itself isn't an instance of a point, but it contains the machinery to make point instances. Every time you call the constructor, you're asking the factory to make you a new object. As the object comes off the production line, its initialization method is executed to get the object properly set up with it's factory default settings.

The combined process of "make me a new object" and "get its settings initialized to the factory

default settings" is called instantiation.

15.3. Attributes

Like real world objects, object instances have both attributes and methods.

We can modify the attributes in an instance using dot notation:

```
>>> p.x = 3
>>> p.y = 4
```

Both modules and instances create their own namespaces, and the syntax for accessing names contained in each, called attributes, is the same. In this case the attribute we are selecting is a data item from an instance.

The following state diagram shows the result of these assignments:

```
p -> x -> 3
y -> 4
```

The variable p refers to a Point object, which contains two attributes. Each attribute refers to a number.

We can access the value of an attribute using the same syntax:

```
>>> print(p.y)
4
>>> x = p.x
>>> print(x)
3
```

The expression p.x means, "Go to the object p refers to and get the value of x". In this case, we assign that value to a variable named x. There is no conflict between the variable x (in the global namespace here) and the attribute x (in the namespace belonging to the instance). The purpose of dot notation is to fully qualify which variable you are referring to unambiguously.

You can use dot notation as part of any expression, so the following statements are legal:

```
print('(x={0}, y={1})'.format(p.x, p.y))
distance_squared_from_origin = p.x * p.x + p.y * p.y
```

The first line outputs (x=3, y=4). The second line calculates the value 25.

15.4. Improving our initializer

To create a point at position (7, 6) currently needs three lines of code:

```
1 p = Point()
2 p.x = 7
p.y = 6
```

We can make our class constructor more general by putting extra parameters into the init

method, as shown in this example:

```
class Point:
""" Point class represents and manipulates x,y coords. """

def __init__(self, x=0, y=0):
    """ Create a new point at x, y """
    self.x = x
    self.y = y

# Other statements outside the class continue below here.
```

The \overline{x} and \overline{y} parameters here are both optional. If the caller does not supply arguments, they'll get the default values of 0. Here is our improved class in action:

```
>>> p = Point(4, 2)

>>> q = Point(6, 3)

>>> r = Point() # r represents the origin (0, 0)

>>> print(p.x, q.y, r.x)

4 3 0
```

Technically speaking ..

If we are really fussy, we would argue that the <u>__init__</u> method's docstring is inaccurate. <u>__init__</u> doesn't *create* the object (i.e. set aside memory for it), — it just initializes the object to its factory-default settings after its creation.

But tools like PyScripter understand that instantiation — creation and initialization — happen together, and they choose to display the *initializer's* docstring as the tooltip to guide the programmer when you call the class constructor.

So we're writing the docstring so that it makes the most sense when it pops up to help the programmer who is using our <u>Point</u> class:

```
class Point:

""" Point class represents and manipulates x,y coords. """

def __init__(self, x=0, y=0):

""" Create a new point at x, y """

self.x = x
self.y = y

10 # Other statements outside the class continue below here.

11

12 q = Point(

x=0, y=0
Create a new point at x, y
```

15.5. Adding other methods to our class

The key advantage of using a class like Point rather than a simple tuple (6, 7) now becomes apparent. We can add methods to the Point class that are sensible operations for points, but which may not be appropriate for other tuples like (25, 12) which might represent, say, a day and a month, e.g. Christmas day. So being able to calculate the distance from the origin is sensible for points, but not for (day, month) data. For (day, month) data, we'd like different operations, perhaps to find what day of the week it will fall on in 2020.

Creating a class like <u>Point</u> brings an exceptional amount of "organizational power" to our programs, and to our thinking. We can group together the sensible operations, and the kinds of data they apply to, and each instance of the class can have its own state.

A method behaves like a function but it is invoked on a specific instance, e.g. tess.right(90). Like a data attribute, methods are accessed using dot notation.

Let's add another method, distance_from_origin, to see better how methods work:

```
1
     class Point:
2
         """ Create a new Point, at coordinates x, y """
3
       def __init__(selt, x=0, y-0,.
""" Create a new point at x, y """
4
5
6
             self.x = x
7
             self.y = y
8
9
         def distance_from_origin(self):
             """ Compute my distance from the origin """
10
11
             return ((self.x ** 2) + (self.y ** 2)) ** 0.5
```

Let's create a few point instances, look at their attributes, and call our new method on them:

```
>>> p = Point(3, 4)
>>> p.x
3
>>> p.y
4
>>> p.distance_from_origin()
5.0
>>> q = Point(5, 12)
>>> q.x
5
>>> q.y
12
>>> q.distance_from_origin()
13.0
>>> r = Point()
>>> r.x
0
>>> r.y
0
>>> r.distance_from_origin()
0.0
```

When defining a method, the first parameter refers to the instance being manipulated. As already noted, it is customary to name this parameter self.

Notice that the caller of distance_from_origin does not explicitly supply an argument to match the self parameter — this is done for you, behind your back.

15.6. Instances as arguments and parameters

You can pass an object as an argument in the usual way. We've already seen this in some of the turtle examples, where we passed the turtle to some function like draw_bar in the chapter titled Conditionals, so that the function could control and use whatever turtle instance we passed to it.

Be aware that your variable only holds a reference to an object, so passing tess into a function creates

an alias: both the caller and the called function now have a reference, but there is only one turtle!

Here is a simple function involving our new Point objects:

```
def print_point(pt):
    print('({0}, {1})'.format(pt.x, pt.y))
```

print_point takes a point as an argument and formats the output in whichever way we choose. If you call print_point(p) with point p as defined previously, the output is (3, 4).

15.7. Converting an instance to a string

Most object-oriented programmers probably would not do what we've just done in print_point. When we're working with classes and objects, a preferred alternative is to add a new method to the class. And we don't like chatterbox methods that call print. A better approach is to have a method so that every instance can produce a string representation of itself. Let's initially call it to_string:

```
class Point:
    # ...

def to_string(self):
    return '({0}, {1})'.format(self.x, self.y)
```

Now we can say:

```
>>> p = Point(3, 4)
>>> print(p.to_string())
(3, 4)
```

But, you ask, don't we already have an str type converter that can turn our object into a string? Yes! And doesn't print automatically use this when printing things? Yes again! But these automatic mechanisms do not yet do exactly what we want:

```
>>> str(p)
'<__main__.Point object at 0x01F9AA10>'
>>> print(p)
'<__main__.Point object at 0x01F9AA10>'
```

Python has a clever trick up its sleeve to fix this. If we call our new method <u>str</u> instead of <u>to_string</u>, the Python interpreter will use our code whenever it needs to convert a <u>Point</u> to a string. Let's re-do this again, now:

```
class Point:

# ...

def __str__(self): # all we have done is renamed the method
return '({0}, {1})'.format(self.x, self.y)
```

and now things are looking great!

```
>>> str(p) # python now uses the __str__ method that we wrote.
```

```
(3, 4)
>>> print(p)
(3, 4)
```

15.8. Instances as return values

Functions and methods can return instances. For example, given two Point objects, find their midpoint. First we'll write this as a regular function:

```
def midpoint(p1, p2):
    """ Return the midpoint of points p1 and p2 """
    mx = (p1.x + p2.x)/2
    my = (p1.y + p2.y)/2
    return Point(mx, my)
```

The function creates and returns a new Point object:

```
>>> p = Point(3, 4)
>>> q = Point(5, 12)
>>> r = midpoint(p, q)
>>> r
(4.0, 8.0)
```

Now let us do this as a method instead. Suppose you have a point object, and wish to find the midpoint halfway between it and some other target point:

```
class Point:
    # ...

def halfway(self, target):
    """ Return the halfway point between myself and the target """
    mx = (self.x + target.x)/2
    my = (self.y + target.y)/2
    return Point(mx, my)
```

This method is identical to the function, aside from some renaming. It's usage might be like this:

```
>>> p = Point(3, 4)
>>> q = Point(5, 12)
>>> r = p.halfway(q)
>>> r
(4.0, 8.0)
```

While this example assigns each point to a variable, this need not be done. Just as function calls are composable, method calls and object instantiation are also composable, leading to this alternative that uses no variables:

```
>>> print(Point(3, 4).halfway(Point(5, 12)))
(4.0, 8.0)
```

15.9. A change of perspective

The original syntax for a function call, print_time(current_time), suggests that the function is the

active agent. It says something like, "Hey, print_time! Here's an object for you to print."

In object-oriented programming, the objects are considered the active agents. An invocation like current_time.print_time() says "Hey current_time! Please print yourself!"

In our early introduction to turtles, we used an object-oriented style, so that we said tess.forward(100), which asks the turtle to move itself forward by the given number of steps.

This change in perspective might be more polite, but it may not initially be obvious that it is useful. But sometimes shifting responsibility from the functions onto the objects makes it possible to write more versatile functions, and makes it easier to maintain and reuse code.

The most important advantage of the object-oriented style is that it fits our mental chunking and real-life experience more accurately. In real life our cook method is part of our microwave oven — we don't have a cook function sitting in the corner of the kitchen, into which we pass the microwave! Similarly, we use the cellphone's own methods to send an sms, or to change its state to silent. The functionality of real-world objects tends to be tightly bound up inside the objects themselves. OOP allows us to accurately mirror this when we organize our programs.

15.10. Objects can have state

Objects are most useful when we also need to keep some state that is updated from time to time. Consider a turtle object. Its state consists of things like its position, its heading, its color, and its shape. A method like left(90) updates the turtle's heading, forward changes its position, and so on.

For a bank account object, a main component of the state would be the current balance, and perhaps a log of all transactions. The methods would allow us to query the current balance, deposit new funds, or make a payment. Making a payment would include an amount, and a description, so that this could be added to the transaction log. We'd also want a method to show the transaction log.

15.11. Glossary

attribute

One of the named data items that makes up an instance.

class

A user-defined compound type. A class can also be thought of as a template for the objects that are instances of it. (The iPhone is a class. By December 2010, estimates are that 50 million instances had been sold!)

constructor

Every class has a "factory", called by the same name as the class, for making new instances. If the class has an *initializer method*, this method is used to get the attributes (i.e. the state) of the new object properly set up.

initializer method

A special method in Python (called <u>__init__</u>) that is invoked automatically to set a newly created object's attributes to their initial (factory-default) state.

instance

An object whose type is of some class. Instance and object are used interchangeably.

instantiate

To create an instance of a class, and to run its initializer.

method

A function that is defined inside a class definition and is invoked on instances of that class.

object

A compound data type that is often used to model a thing or concept in the real world. It bundles together the data and the operations that are relevant for that kind of data. Instance and object are used interchangeably.

object-oriented programming

A powerful style of programming in which data and the operations that manipulate it are organized into classes and methods.

object-oriented language

A language that provides features, such as user-defined classes and inheritance, that facilitate object-oriented programming.

15.12. Exercises

- 1. Rewrite the distance function from the chapter titled *fruitful functions* so that it takes two Points as parameters instead of four numbers.
- 2. Add a method $reflect_x$ to Point which returns a new Point, one which is the reflection of the point about the x-axis. For example, Point(3, 5). $reflect_x()$ is (3, -5)
- 3. Add a method slope_from_origin which returns the slope of the line joining the origin to the point. For example,

```
>>> Point(4, 10).slope_from_origin()
2.5
```

What cases will cause your method to fail?

4. The equation of a straight line is "y = ax + b", (or perhaps "y = mx + c"). The coefficients a and b completely describe the line. Write a method in the Point class so that if a point instance is given another point, it will compute the equation of the straight line joining the two points. It must return the two coefficients as a tuple of two values. For example,

```
>>> print(Point(4, 11).get_line_to(Point(6, 15)))
>>> (2, 3)
```

This tells us that the equation of the line joining the two points is "y = 2x + 3". When will your method fail?

5. Given four points that fall on the circumference of a circle, find the midpoint of the circle. When will you function fail?

Hint: You must know how to solve the geometry problem before you think of going anywhere near programming. You cannot program a solution to a problem if you don't understand what you want the computer to do!

6. Create a new class, SMS_store. The class will instantiate SMS_store objects, like your inbox or your outbox on your cellphone:

```
my_inbox = SMS_store()
```

This store can hold multiple SMS messages (i.e. its internal state will just be a list of messages). Each message will be represented as a tuple:

```
(has_been_viewed, from_number, time_arrived, text_of_SMS)
```

Your inbox object should provide these methods:

```
my_inbox.add_new_arrival(from_number, time_arrived, text_of_SMS)
 # Makes new SMS tuple, inserts it after other messages
 # in the store. When creating this message, its
 # has been viewed status is set False.
my_inbox.message_count()
 # returns the number of sms messages in my inbox
my_inbox.get_unread_indexes()
 # returns list of indexes of all not-yet-viewed SMS messages
my_inbox.get_message(i)
 # return (from_number, time_arrived, text_of_sms) for message[i]
 # Also change its state to "has been viewed".
 # If there is no message at position i, return None
my inbox.delete(i)
                       # delete the message at index i
my_inbox.clear()
                      # delete all messages from inbox
```

Write the class, create a message store object, write tests for these methods, and implement the methods.

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16. Classes and Objects - Digging a little deeper

16.1. Rectangles

Let's say that we want a class to represent a rectangle which is located somewhere in the XY plane. The question is, what information do we have to provide in order to specify such a rectangle? To keep things simple, assume that the rectangle is oriented either vertically or horizontally, never at an angle.

There are a few possibilities: we could specify the center of the rectangle (two coordinates) and its size (width and height); or we could specify one of the corners and the size; or we could specify two opposing corners. A conventional choice is to specify the upper-left corner of the rectangle, and the

Again, we'll define a new class, and provide it with an initializer and a string converter method:

```
1
     class Rectangle:
         """ A class to manufacture rectangle objects """
2
3
        def __init__(self, posn, w, n):
    """ Initialize rectangle at posn, with width w, height h """
4
5
6
             self.corner = posn
7
             self.width = w
8
             self.height = h
9
10
         def __str__(self):
11
           return "({0}, {1}, {2})"
12
                        .format(self.corner, self.width, self.height)
13
14
     box = Rectangle(Point(0, 0), 100, 200)
15
     bomb = Rectangle(Point(100, 80), 5, 10) # in my video game
     print("box: ", box)
16
     print("bomb: ", bomb)
```

To specify the upper-left corner, we have embedded a Point object (as we used it in the previous chapter) within our new Rectangle object! We create two new Rectangle objects, and then print them producing:

```
box: ((0, 0), 100, 200)
bomb: ((100, 80), 5, 10)
```

The dot operator composes. The expression box.corner.x means, Go to the object that box refers to and select its attribute named corner; then go to that object and select its attribute named x.

The figure shows the state of this object:

```
width --> 100.0
 height -> 200.0
                   x -> 0.0
comer -
                   y -> 0.0
```

16.2. Objects are mutable

We can change the state of an object by making an assignment to one of its attributes. For example, to grow the size of a rectangle without changing its position, we could modify the values of width and height:

```
box.width += 50
box.height += 100
```

Of course, we'd probably like to provide a method to encapsulate this inside the class. We will also provide another method to move the position of the rectangle elsewhere:

```
class Rectangle:
2
        # ...
3
4
        def grow(self, delta_width, delta_height):
             """ Grow (or shrink) this object by the deltas """
5
            self.width += delta_width
6
7
            self.height += delta_height
8
9
        def move(self, dx, dy):
            """ Move this object by the deltas """
10
11
            self.corner.x += dx
            self.corner.y += dy
12
```

Let us try this:

```
>>> r = Rectangle(Point(10,5), 100, 50)
>>> print(r)
((10, 5), 100, 50)
>>> r.grow(25, -10)
>>> print(r)
((10, 5), 125, 40)
>>> r.move(-10, 10)
print(r)
((0, 15), 125, 40)
```

16.3. Sameness

The meaning of the word *same* seems perfectly clear until you give it some thought, and then you realize there is more to it than you expected.

For example, if you say, Chris and I have the same car, you mean that his car and yours are the same make and model, but that they are two different cars. If you say, Chris and I have the same mother, you mean that his mother and yours are the same person.

When you talk about objects, there is a similar ambiguity. For example, if two Points are the same, does that mean they contain the same data (coordinates) or that they are actually the same object?

We've already seen the <u>is</u> operator in the chapter on lists, where we talked about aliases: it allows us to find out if two references refer to the same object:

```
>>> p1 = Point(3, 4)
>>> p2 = Point(3, 4)
>>> p1 is p2
```

```
False
```

Even though p1 and p2 contain the same coordinates, they are not the same object. If we assign p1 to p3, then the two variables are aliases of the same object:

```
>>> p3 = p1
>>> p1 is p3
True
```

This type of equality is called shallow equality because it compares only the references, not the contents of the objects.

To compare the contents of the objects — deep equality — we can write a function called same coordinates:

```
def same_coordinates(p1, p2):
    return (p1.x == p2.x) and (p1.y == p2.y)
```

Now if we create two different objects that contain the same data, we can use same_point to find out if they represent points with the same coordinates.

```
>>> p1 = Point(3, 4)
>>> p2 = Point(3, 4)
>>> same_coordinates(p1, p2)
True
```

Of course, if the two variables refer to the same object, they have both shallow and deep equality.

Reware of --

"When I use a word," Humpty Dumpty said, in a rather scornful tone, "it means just what I choose it to mean — neither more nor less." *Alice in Wonderland*

Python has a powerful feature that allows a designer of a class to decide what an operation like == or < should mean. (We've just shown how we can control how our own objects are converted to strings, so we've already made a start!) We'll cover more detail later. But sometimes the implementors will attach shallow equality semantics, and sometimes deep equality, as shown in this little experiment:

```
p = Point(4, 2)
s = Point(4, 2)
print("== on Points returns", p == s)
# by default, == on Point objects does a shallow equality test

a = [2,3]
b = [2,3]
print("== on lists returns", a == b)
# but by default, == does a deep equality test on lists
```

This outputs:

```
== on Points returns False
== on lists returns True
```

So we conclude that even though the two lists (or tuples, etc.) are distinct objects with different memory addresses, for lists the == operator tests for deep equality, while in the case of points it makes a shallow

test.

16.4. Copying

Aliasing can make a program difficult to read because changes made in one place might have unexpected effects in another place. It is hard to keep track of all the variables that might refer to a given object.

Copying an object is often an alternative to aliasing. The copy module contains a function called copy that can duplicate any object:

```
>>> import copy
>>> p1 = Point(3, 4)
>>> p2 = copy.copy(p1)
>>> p1 is p2
False
>>> same_coordinates(p1, p2)
True
```

Once we import the <u>copy</u> module, we can use the <u>copy</u> function to make a new <u>Point</u>. p1 and p2 are not the same point, but they contain the same data.

To copy a simple object like a <u>Point</u>, which doesn't contain any embedded objects, <u>copy</u> is sufficient. This is called shallow copying.

For something like a <u>Rectangle</u>, which contains a reference to a <u>Point</u>, <u>copy</u> doesn't do quite the right thing. It copies the reference to the <u>Point</u> object, so both the old <u>Rectangle</u> and the new one refer to a single <u>Point</u>.

If we create a box, b1, in the usual way and then make a copy, b2, using copy, the resulting state diagram looks like this:



This is almost certainly not what we want. In this case, invoking grow on one of the Rectangles would not affect the other, but invoking move on either would affect both! This behavior is confusing and error-prone. The shallow copy has created an alias to the Point that represents the corner.

Fortunately, the <u>copy</u> module contains a function named <u>deepcopy</u> that copies not only the object but also any embedded objects. You will not be surprised to learn that this operation is called a deep copy.

```
>>> b2 = copy.deepcopy(b1)
```

Now b1 and b2 are completely separate objects.

16.5. Glossary

deep copy

To copy the contents of an object as well as any embedded objects, and any objects embedded in them, and so on; implemented by the deepcopy function in the copy module.

deep equality

Equality of values, or two references that point to objects that have the same value.

shallow copy

To copy the contents of an object, including any references to embedded objects; implemented by the copy function in the copy module.

shallow equality

Equality of references, or two references that point to the same object.

16.6. Exercises

1. Add a method area to the Rectangle class that returns the area of any instance:

```
r = Rectangle(Point(0, 0), 10, 5)
test(r.area(), 50)
```

2. Write a perimeter method in the Rectangle class so that we can find the perimeter of any rectangle instance:

```
r = Rectangle(Point(0, 0), 10, 5)
test(r.perimeter(), 30)
```

3. Write a flip method in the Rectangle class that swaps the width and the height of any rectangle instance:

```
r = Rectangle(Point(100, 50), 10, 5)
test(r.width, 10)
test(r.height, 5)
r.flip()
test(r.width, 5)
test(r.height, 10)
```

4. Write a new method in the Rectangle class to test if a Point falls within the rectangle. For this exercise, assume that a rectangle at (0,0) with width 10 and height 5 has *open* upper bounds on the width and height, i.e. it stretches in the x direction from [0 to 10), where 0 is included but 10 is excluded, and from [0 to 5) in the y direction. So it does not contain the point (10, 2). These tests should pass:

```
r = Rectangle(Point(0, 0), 10, 5)
test(r.contains(Point(0, 0)), True)
test(r.contains(Point(3, 3)), True)
test(r.contains(Point(3, 7)), False)
test(r.contains(Point(3, 5)), False)
test(r.contains(Point(3, 4.99999)), True)
test(r.contains(Point(-3, -3)), False)
```

5. In games, we often put a rectangular "bounding box" around our sprites. (A sprite is an object that can move about in the game, as we will see shortly.) We can then do *collision detection* between, say, bombs and spaceships, by comparing whether their rectangles overlap anywhere.

Write a function to determine whether two rectangles collide. *Hint: this might be quite a tough exercise! Think carefully about all the cases before you code.*

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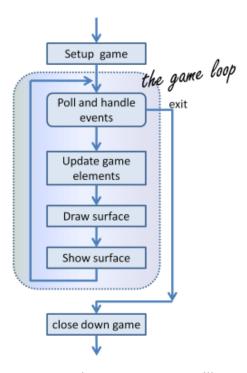
17. PyGame

PyGame is a package that is not part of the standard Python distribution, so if you do not already have it installed (i.e. import pygame fails), download and install a suitable version from http://pygame.org/download.shtml. These notes are based on PyGame 1.9.1, the most recent version at the time of writing.

PyGame comes with a substantial set of tutorials, examples, and help, so there is ample opportunity to stretch yourself on the code. You may need to look around a bit to find these resources, though: if you've installed PyGame on a Windows machine, for example, they'll end up in a folder like C:\Python31\Lib\site-packages\pygame\ where you will find directories for *docs* and *examples*.

17.1. The game loop

The structure of the games we'll consider always follows this fixed pattern:



In every game, in the *setup* section we'll create a window, load and prepare some content, and then enter the game loop. The game loop continuously does four main things:

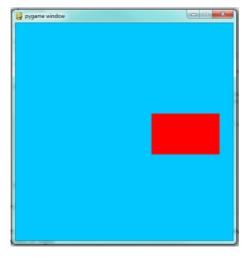
- it polls for events i.e. asks the system whether events have occurred and responds appropriately,
- it updates whatever internal data structures or objects need changing,
- it draws the current state of the game into a (non-visible) surface,
- it puts the just-drawn surface on display.

```
import pygame

def main():
    """ Set up the game and run the main game loop """
    pygame.init() # prepare the pygame module for use
```

```
surfaceSz = 480  # Desired physical surface size, in pixels.
8
        # Create surface of (width, height), and its window.
9
        main_surface = pygame.display.set_mode((surfaceSz, surfaceSz))
10
        # set up some data to describe a small rectangle and its color
11
        small_rect = (300, 200, 150, 90)
12
                                        # A color is a mix of (Red, Green, Blue)
13
        some_color = (255, 0, 0)
14
15
        while True:
            ev = pygame.event.poll() # look for any event
17
            if ev.type == pygame.QUIT: # window close button clicked?
                                       # ... Leave game Loop
18
                break
19
20
            # Update your game objects and data structures here...
21
22
            # We draw everything from scratch on each frame.
            # So first fill everything with the background color
23
24
            main_surface.fill((0, 200, 255))
25
            # Overpaint a smaller rectangle on the main surface
26
27
            main_surface.fill(some_color, small_rect)
28
29
            # Now the surface is ready, tell pygame to display it!
30
            pygame.display.flip()
31
32
        pygame.quit()
                          # once we leave the loop, close the window.
33
    main()
34
```

This program pops up a window which stays there until we close it:



PyGame does all its drawing onto rectangular *surfaces*. After initializing PyGame at line 5, we create a window holding our main surface. The main loop of the game extends from line 15 to 30, with the following key bits of logic:

- First (line 16) we poll to fetch the next event that might be ready for us. This step will always be followed by some conditional statements that will determine whether any event that we're interested in has happened. Polling for the event consumes it, as far as PyGame is concerned, so we only get one chance to fetch and use each event. On line 17 we test whether the type of the event is the predefined constant called pygame.QUIT. This is the event that we'll see when the user clicks the close button on the PyGame window. In response to this event, we leave the loop.
- Once we've left the loop, the code at line 32 closes window, and we'll return from function main. Your program could go on to do other things, or reinitialize pygame and create another window, but it will usually just end too.
- There are different kinds of events key presses, mouse motion, mouse clicks, joystick

movement, and so on. It is usual that we test and handle all these cases with new code squeezed in before line 19. The general idea is "handle events first, then worry about the other stuff".

- At line 20 we'd update objects or data for example, if we wanted to vary the color, position, or size of the rectangle we're about to draw, we'd re-assign some color, and small rect here.
- A modern way to write games (now that we have fast computers and fast graphics cards) is to redraw everything from scratch on every iteration of the game loop. So the first thing we do at line 24 is fill the entire surface with a background color. The fill method of a surface takes two arguments the color to use for filling, and the rectangle to be filled. But the second argument is optional, and if it is left out the entire surface is filled.
- In line 27 we fill a second rectangle, this time using some_color. The placement and size of the rectangle are given by the tuple small_rect, a 4-element tuple (x, y, width, height).
- It is important to understand that the origin of the PyGame's surface is at the top left corner (unlike the turtle module that puts it's origin in the middle of the screen). So, if you wanted the rectangle closer to the top of the window, you need to make its y coordinate smaller.
- If your graphics display hardware tries to read from memory at the same time as the program is writing to that memory, they will interfere with each other, causing video noise and flicker. To get around this, PyGame keeps two buffers in the main surface the *back buffer* that the program draws to, while the *front buffer* is being shown to the user. Each time the program has fully prepared its back buffer, it flips the back/front role of the two buffers. So the drawing on lines 24 and 27 does does not change what is seen on the screen until we flip the buffers, on line 30.

17.2. Displaying images and text

To draw an image on the main surface, we load the image, say a beach ball, into its own new surface. The main surface has a blit method that copies pixels from the beach ball surface into its own surface. When we call blit, we can specify where the beach ball should be placed on the main surface. The term blit is widely used in computer graphics, and means to make a fast copy of pixels from one area of memory to another.

So in the setup section, before we enter the game loop, we'd load the image, like this:

```
ball = pygame.image.load("ball.png")
```

and after line 28 in the program above, we'd add this code to display our image at position (100,120):

```
main_surface.blit(ball, (100, 120))
```

To display text, we need do do three things. Before we enter the game loop, we instantiate a font object:

```
# Instantiate 16 point Courier font to draw text.
my_font = pygame.font.SysFont('Courier', 16)
```

and after line 28, again, we use the font's <u>render</u> method to create a new surface containing the pixels of the drawn text, and then, as in the case for images, we blit our new surface onto the main surface. Notice that <u>render</u> takes two extra parameters — the second tells it whether to carefully smooth edges of the text while drawing (this process is called <u>anti-aliasing</u>), and the second is the color that we

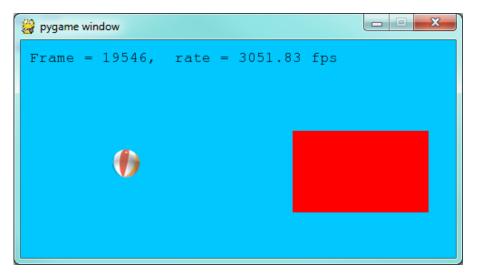
want the text text be. Here we've used (0,0,0) which is black:

```
the_text = my_font.render('Hello, world!', True, (0,0,0))
surface.blit(the_text, (10, 10))
```

We'll demonstrate these two new features by counting the frames — the iterations of the game loop — and keeping some timing information. On each frame, we'll display the frame count, and the frame rate. We will only update the frame rate after every 500 frames, when we'll look at the timing interval and can do the calculations.

```
import pygame
 1
                          # for graphics
 2
     import time
 3
4
     def main():
 5
 6
         pygame.init()
                         # prepare the PyGame module for use
 7
         main_surface = pygame.display.set_mode((480, 240))
8
9
         # Load an image to draw. Substitute your own.
10
         # PyGame handles gif, jpg, png, etc. image types.
         ball = pygame.image.load("ball.png")
11
12
13
         # Create a font for rendering text
14
         my_font = pygame.font.SysFont('Courier', 16)
15
16
         frame_count = 0
17
         frame_rate = 0
         t0 = time.clock()
18
19
20
         while True:
21
22
             # look for an event from keyboard, mouse, joystick, etc.
23
             ev = pygame.event.poll()
                                         # window close button clicked?
24
             if ev.type == pygame.QUIT:
25
                 break
                                          # Leave game Loop
26
27
             # do other bits of logic for the game here
28
             frame_count += 1
29
             if frame_count % 500 == 0:
30
                t1 = time.clock()
31
                 frame_rate = 500 / (t1-t0)
32
                t0 = t1
33
             # Completely redraw the surface, starting with background
35
             main_surface.fill((0, 200, 255))
36
37
             # Put a red rectangle somewhere on the surface
38
             main_surface.fill((255,0,0), (300, 100, 150, 90))
39
             # Copy our image to the surface, at this (x,y) posn
40
41
             main_surface.blit(ball, (100, 120))
42
43
             # Make a new surface with an image of the text
             the_text = my_font.render('Frame = {0}, rate = {1:.2f} fps'
44
45
                       .format(frame_count, frame_rate), True, (0,0,0))
46
             # Copy the text surface to the main surface
47
             main_surface.blit(the_text, (10, 10))
48
49
             # Now that everything is drawn, put it on display!
50
             pygame.display.flip()
51
52
         pygame.quit()
53
54
55
     main()
```

The frame rate is close to ridiculous — a lot faster than one's eye can process frames. (Commercial video games usually plan their action for 60 frames per second (fps).) Of course, our rate will drop once we start doing something a little more strenuous inside our game loop.



17.3. Drawing a board for the N queens puzzle

In section <u>Fight queens puzzle, part 1</u> we solved our N queens puzzle. For the 8x8 board, one of the solutions was the list [6,4,2,0,5,7,1,3]. Let's now use PyGame to draw that chessboard with its queens.

We begin with a background of black and red squares for the board. Perhaps we could create an image that we could load and draw, but that approach would need different background images for different size boards. Just drawing our own red and black rectangles of the appropriate size sounds like much more fun!

```
1
    def draw board(the board):
        """ Draw a chess board with queens, from the board. """
 3
 4
        pygame.init()
 5
        colors = [(255,0,0), (0,0,0)] # set up colors [red, black]
 6
        n = len(the_board)
7
                                # this is an NxN chess board.
        surfaceSz = 480
8
                                # Proposed physical surface size.
        sq sz = surfaceSz // n # sq sz is length of a square.
9
10
        surfaceSz = n * sq_sz
                                # Adjust to exactly fit n squares.
11
        # Create the surface of (width, height), and its window.
12
13
        surface = pygame.display.set_mode((surfaceSz, surfaceSz))
```

Here we precompute sq_sz, the integer size that each square will be, so that we can fit the squares nicely into the available window. So if we'd like the board to be 480x480, and we're drawing an 8x8 chessboard, then each square will need to have a size of 60 units. But we notice that a 7x7 board cannot fit nicely into 480 — we're going to get some ugly border that our squares don't fill exactly. So we recompute the surface size to exactly fit our squares before we create the window.

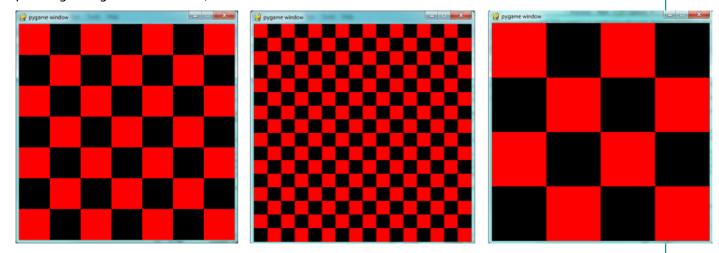
Now let's draw the squares, in the game loop. We'll need a nested loop: the outer loop will run over the rows of the chessboard, the inner loop over the columns:

```
# Draw a fresh background (a blank chess board)
for row in range(n): # Draw each row of the board.
```

```
c_indx = row % 2  # Change starting color on each row
for col in range(n):  # Run through cols drawing squares
the_square = (col*sq_sz, row*sq_sz, sq_sz, sq_sz)
surface.fill(colors[c_indx], the_square)
# now flip the color index for the next square
c_indx = (c_indx + 1) % 2
```

There are two important ideas in this code: firstly, we compute the rectangle to be filled from the row and col loop variables, multiplying them by the size of the square to get their position. And, of course, each square is a fixed width and height. So the square represents the rectangle to be filled on the current iteration of the loop. The second idea is that we have to alternate colors on every square. In the earlier setup code we created a list containing two colors, here we manipulate c indx (which will always either have the value 0 or 1) to start each row on a color that is different from the previous row's starting color, and to switch colors each time a square is filled.

This (together with the other fragments not shown to flip the surface onto the display) leads to the pleasing backgrounds like this, for different size boards:

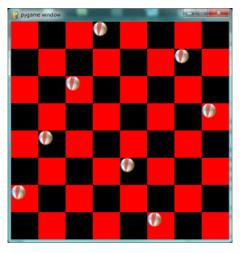


Now, on to drawing the queens! Recall that our solution [6,4,2,0,5,7,1,3] means that in column 0 of the board we want a queen at row 6, at column 1 we want a queen at row 4, and so on. So we need a loop running over each queen:

```
for (col, row) in enumerate(the_board):
# draw a queen at col, row...
```

In this chapter we already have a beach ball image, so we'll use that for our queens. In the setup code before our game loop, we load the ball image (as we did before), and in the body of the loop, we add the line:

```
surface.blit(ball, (col * sq_sz, row * sq_sz))
```



We're getting there, but those queens need to be centred in their squares! Our problem arises from the fact that both the ball and the rectangle have their upper left corner as their reference points. If we're going to centre this ball in the square, we need to give it an extra offset in both the x and y direction. (Since the ball is round and the square is square, the offset in the two directions will be the same, so we'll just compute a single offset value, and use it in both directions.)

The offset we need is half the (size of the square less the size of the ball). So we'll precompute this in the game's setup section, after we've loaded the ball and determined the square size:

```
ball_offset = (sq_sz - ball.get_width()) // 2
```

Now we touch up the drawing code for the ball and we're done:

```
surface.blit(ball, (col * sq_sz + ball_offset, row * q_sz + ball_offset))
```

We might just want to think about what would happen if the ball was bigger than the square. In that case, <u>ball_offset</u> would become negative. So it would still be centered in the square – it would just spill over the boundaries, or perhaps obscure the square entirely!

Here is the complete program:

```
import pygame
1
 2
 3
    def draw board(the board):
         """ Draw a chess board with queens, as determined by the the_board. """
 4
 5
 6
        pygame.init()
 7
        colors = [(255,0,0), (0,0,0)] # set up colors [red, black]
8
        n = len(the_board)
9
                                 # this is an NxN chess board.
10
        surfaceSz = 480
                                 # Proposed physical surface size.
11
        sq sz = surfaceSz // n # sq sz is length of a square.
12
        surfaceSz = n * sq_sz
                                 # Adjust to exactly fit n squares.
13
        # Create the surface of (width, height), and its window.
14
        surface = pygame.display.set_mode((surfaceSz, surfaceSz))
15
16
17
        ball = pygame.image.load("ball.png")
18
19
        # Use an extra offset to centre the ball in its square.
20
        # If the square is too small, offset becomes negative,
21
         # but it will still be centered :-)
```

```
ball_offset = (sq_sz-ball.get_width()) // 2
22
23
24
         while True:
25
26
             # Look for an event from keyboard, mouse, etc.
27
             ev = pygame.event.poll()
28
             if ev.type == pygame.QUIT:
29
                 break:
30
31
             # Draw a fresh background (a blank chess board)
             for row in range(n): # Draw each row of the board.
                 c_indx = row % 2  # Alternate starting color
for col in range(n):  # Run through cols drawing squares
33
34
                     the_square = (col*sq_sz, row*sq_sz, sq_sz, sq_sz)
35
36
                     surface.fill(colors[c_indx], the_square)
37
                     # now flip the color index for the next square
38
                     c_{indx} = (c_{indx} + 1) % 2
39
40
             # Now that squares are drawn, draw the queens.
             for (col, row) in enumerate(the_board):
41
42
               surface.blit(ball,
43
                        (col*sq_sz+ball_offset,row*sq_sz+ball_offset))
44
45
             pygame.display.flip()
46
47
         pygame.quit()
48
49
50
    if __name__ == '__main_
51
         draw_board([0, 5, 3, 1, 6, 4, 2])
                                                # 7 x 7 to test window size
52
         draw_board([6, 4, 2, 0, 5, 7, 1, 3])
53
         draw_board([9, 6, 0, 3, 10, 7, 2, 4, 12, 8, 11, 5, 1]) # 13 x 13
         draw_board([11, 4, 8, 12, 2, 7, 3, 15, 0, 14, 10, 6, 13, 1, 5, 9])
54
```

There is one more thing worth reviewing here. The conditional statement on line 50 tests whether the name of the currently executing program is __main__. This allows us to distinguish whether this module is being run as a main program, or whether it has been imported elsewhere, and used as a module. If we run this module in Python, the test cases in lines 51–54 will be executed. However, if we import this module into another program (i.e. our N queens solver from earlier) the condition at line 50 will be false, and the statements on lines 51–54 won't run.

In the section *Eight queens puzzle*, part 2 our main program looked like this:

```
def main():
1
2
3
         bd = list(range(8)) # generate the initial permutation
4
        numFound = 0
5
        tries = 0
6
        while numFound < 10:</pre>
7
           random.shuffle(bd)
8
           tries += 1
9
           if not has_clashes(bd):
10
                print('Found solution {0} in {1} tries.'.format(bd, tries))
                tries = 0
11
12
                numFound += 1
13
14
     main()
```

Now we just need two changes. At the top of that program, we import the module that we've been working on here (assume we called it draw_queens). (You'll have to ensure that the two modules are saved in the same folder.) Then after line 10 here we add a call to draw the solution that we've just discovered:

```
draw_queens.draw_board(bd)
```

And that gives a very satisfying combination of program that can search for solutions to the N queens problem, and when it finds each, it pops up the board showing the solution.

17.4. Sprites

A sprite is an object that can move about in a game, and has internal behaviour and state of its own. For example, a spaceship would be a sprite, the player would be a sprite, and bullets and bombs would all be sprites.

Object oriented programming (OOP) is ideally suited to a situation like this: each object can have its own attributes and internal state, and a couple of methods. Let's have some fun with our N queens board. Instead of placing the queen in her final position, we'd like to drop her in from the top of the board, and let her fall into position, perhaps bouncing along the way.

The first encapsulation we need is to turn each of our queens into an object. We'll keep a list of all the active sprites (i.e. a list of queen objects), and arrange two new things in our game loop:

- After handling events, but before drawing, call an <u>update</u> method on every sprite. This will give each sprite a chance to modify its internal state in some way perhaps change its image, or change its position, or rotate itself, or make itself grow a bit bigger or a bit smaller.
- Once all the sprites have updated themselves, the game loop can begin drawing first the background, and then call a draw method on each sprite in turn, and delegate (hand off) the task of drawing to the object itself. This is in line with the OOP idea that we don't say "Hey, draw, show this queen!", but we prefer to say "Hey, queen, draw youself!".

We start with a simple object, no movement or animation yet, just scaffolding, to see how to fit all the pieces together:

```
class Queen_sprite:
1
3
        def __init__(self, img, target_posn):
             """ Create and initialize a queen for this
4
5
                target position on the board
6
7
            self.image = img
8
            self.target_posn = target_posn
            self.posn = target_posn
10
        def update(self):
11
12
            return
                                  # do nothing for the moment.
13
14
        def draw(self, target_surface):
15
            target_surface.blit(self.image, self.posn)
```

We've given the sprite three attributes: an image to be drawn, a target position, and a current position. If we're going to move the spite about, the current position may need to be different from the target, which is where we want the queen finally to end up. In this code at this time we've done nothing in the <u>update</u> method, and our <u>draw</u> method (which can probably remain this simple in future) simply draws itself at its current position on the surface that is provided by the caller.

With its class definition in place, we now instantiate our N queens, put them into a list of sprites, and arrange for the game loop to call the <u>update</u> and <u>draw</u> methods on each frame. The new bits of code, and the revised game loop look like this:

```
all_sprites = [] # Keep a list of all sprites in the game
 2
 3
         # Create a sprite object for each queen, and populate our list.
 4
        for (col, row) in enumerate(the board):
 5
            a queen = Queen sprite(ball,
                       (col*sq_sz+ball_offset, row*sq_sz+ball_offset))
 6
 7
            all_sprites.append(a_queen)
8
9
        while True:
10
            # look for an event from keyboard, mouse, etc.
            ev = pygame.event.poll()
12
            if ev.type == pygame.QUIT:
13
                break;
14
            # Ask every sprite to update itself.
15
16
            for sprite in all sprites:
17
                sprite.update()
18
            # Draw a fresh background (a blank chess board)
19
20
            # ... same as before ...
21
            # Ask every sprite to draw itself.
22
23
            for sprite in all_sprites:
24
                sprite.draw(surface)
25
26
            pygame.display.flip()
```

This works just like it did before, but our extra work in making objects for the queens has prepared the way for some more ambitious extensions.

Let us begin with a falling queen object. At any instant, it will have a velocity i.e. a speed, in a certain direction. (We are only working with movement in the y direction, but use your imagination!) So in the object's update method, we want to change its current position by its velocity. If our N queens board is floating in space, velocity would stay constant, but hey, here on Earth we have gravity! Gravity changes the velocity on each time interval, so we'll want a ball that speeds up as it falls further. Gravity will be constant for all queens, so we won't keep it in the instances — we'll just make it a variable in our module. We'll make one other change too: we will start every queen at the top of the board, so that it can fall towards its target position. With these changes, we now get the following:

```
1
    gravity = 0.0001
3
    class Queen_sprite:
4
5
        def __init__(self, img, target_posn):
            self.image = img
6
 7
            self.target_posn = target_posn
8
            (x, y) = target_posn
9
            self.posn = (x, 0)
                                  # start ball at top of its column
                                # with zero initial velocity
10
            self.y velocity = 0
11
12
        def update(self):
            self.y_velocity += gravity # gravity changes velocity
13
            (x, y) = self.posn
15
            new_y_pos = y + self.y_velocity # velocity moves the ball
16
            self.posn = (x, new_y_pos)
                                            # to this new position.
17
        def draw(self, target_surface):
                                            # same as before.
18
19
            target_surface.blit(self.image, self.posn)
```

Making these changes gives us a new chessboard in which each queen starts at the top of its column, and speeds up, until it drops off the bottom of the board and disappears forever. A good start — we have movement!

The next step is to get the ball to bounce when it reaches its own target position. It is pretty easy to bounce something — you just change the sign of its velocity, and it will move at the same speed in the opposite direction. Of course, if it is travelling up towards the top of the board it will be slowed down by gravity. (Gravity always sucks down!) And you'll find it bounces all the way up to where it began from, reaches zero velocity, and starts falling all over again. So we'll have bouncing balls that never settle.

A realistic way to settle the object is to lose some energy (probably to friction) each time it bounces — so instead of simply reversing the sign of the velocity, we multiply it by some fractional factor — say – 0.65. This means the ball only retains 65% of its energy on each bounce, so it will, as in real life, stop bouncing after a short while, and settle on its "ground".

The only changes are in the update method, which now looks like this:

```
1
    def update(self):
2
        self.y_velocity += gravity
        (x, y) = self.posn
3
        new_y_pos = y + self.y_velocity
5
        (target_x, target_y) = self.target_posn # unpack the position
                                                # how far to our floor?
6
        dist_to_go = target_y - new_y_pos
7
                                                 # Are we under floor?
8
        if dist_to_go < 0:</pre>
9
            self.y_velocity = -0.65 * self.y_velocity # bounce
10
            new_y_pos = target_y + dist_to_go  # move back above floor
11
12
        self.posn = (x, new_y_pos)
                                                # set our new position.
```

Heh, heh! We're not going to show animated screenshots, so copy the code into your Python environment and see for yourself.

17.5. Events

The only kind of event we're handled so far has been the QUIT event. But we can also detect keydown and keyup events, mouse motion, and mousebutton down or up events. Consult the PyGame documentation and follow the link to Event.

When your program polls for and receives an event object from PyGame, its event type will determine what secondary information is available. Each event object carries a *dictionary* (which you may only cover in due course in these notes). The dictionary holds certain *keys* and *values* that make sense for the type of event.

For example, if the type of event is MOUSEMOTION, we'll be able to find the mouse position and information about the state of the mouse buttons in the dictionary attached to the event. Similarly, if the event is KEYDOWN, we can learn from the dictionary whick key went down, and whether any modifier keys (shift, control, alt, etc.) are also down. You also get events when the game window becomes active (i.e. gets focus) or loses focus.

The event object with type NOEVENT is returned if there are no events waiting. Events can be printed, allowing you to experiment and play around. So dropping these lines of code into the game loop directly after polling for any event is quite informative:

```
if ev.type != NOEVENT: # only print if it is interesting!
print(ev)
```

With this is place, hit the space bar and the escape key, and watch the events you get. Click your three

mouse buttons. Move your mouse over the window. (This causes a vast cascade of events, so you may also need to filter those out of the printing.) You'll get output that looks something like this:

```
<Event(17-VideoExpose {})>
<Event(1-ActiveEvent {'state': 1, 'gain': 0})>
<Event(2-KeyDown {'scancode': 57, 'key': 32, 'unicode': ' ', 'mod': 0})>
<Event(3-KeyUp {'scancode': 57, 'key': 32, 'mod': 0})>
<Event(2-KeyDown {'scancode': 1, 'key': 27, 'unicode': '\x1b', 'mod': 0})>
<Event(3-KeyUp {'scancode': 1, 'key': 27, 'mod': 0})>
<Event(4-MouseMotion {'buttons': (0, 0, 0), 'pos': (323, 194), 'rel': (-3, -1)})>
<Event(4-MouseMotion {'buttons': (0, 0, 0), 'pos': (322, 193), 'rel': (-1, -1)})>
<Event(4-MouseMotion {'buttons': (0, 0, 0), 'pos': (321, 192), 'rel': (-1, -1)})>
<Event(4-MouseMotion {'buttons': (0, 0, 0), 'pos': (319, 192), 'rel': (-2, 0)})>
<Event(5-MouseButtonDown {'button': 1, 'pos': (319, 192)})>
<Event(6-MouseButtonUp {'button': 1, 'pos': (319, 192)})>
<Event(4-MouseMotion {'buttons': (0, 0, 0), 'pos': (319, 191), 'rel': (0, -1)})>
                                                'pos': (319, 191)})>
<Event(5-MouseButtonDown {'button': 2, 'pos': (319, 191)})>
<Event(5-MouseButtonDown {'button': 5, 'pos': (319, 191)})>
<Event(6-MouseButtonUp {'button': 5, 'pos': (319, 191)})>
<Event(6-MouseButtonUp {'button': 2, 'pos': (319, 191)})>
<Event(5-MouseButtonDown {'button': 3, 'pos': (319, 191)})>
<Event(6-MouseButtonUp {'button': 3, 'pos': (319, 191)})>
<Event(1-ActiveEvent {'state': 1, 'gain': 0})>
<Event(12-Quit {})>
```

So let us now make these changes to the code near the top of our game loop:

```
while True:
 2
3
        # look for an event from keyboard, mouse, etc.
4
        ev = pygame.event.poll()
5
        if ev.type == pygame.QUIT:
6
            break;
7
        if ev.type == pygame.KEYDOWN:
8
           key = ev.dict['key']
9
            if key == 27:
                                          # on Escape key
10
                                          # Leave the game Loop
                break
11
            if key == ord('r'):
                colors[0] = (255, 0, 0) # change to red + black
12
13
            elif key == ord('g'):
            colors[0] = (0, 255, 0)
elif key == ord('b'):
                                          # change to green + black
15
                colors[0] = (0, 0, 255) # change to blue + black
16
17
        if ev.type == pygame.MOUSEBUTTONDOWN: # mouse gone down?
18
19
            posn_of_click = ev.dict['pos'] # get the coordinates
20
            print(posn of click)
                                              # just print them
```

Lines 7-16 show typical processing for a KEYDOWN event — if a key has gone down, we test which key it is, and take some action. With this in place, we have another way to quit our queens program — by hitting the escape key. Also, we can use keys to change the color of the board that is drawn.

Finally, at line 20, we respond (pretty lamely) to the mouse button going down.

As a final exercise in this section, we'll write a better response handler to mouse clicks. What we will do is figure out if the user has clicked the mouse on one of our sprites. If there is a sprite under the mouse when the click occurs, we'll send the click to the sprite and let it respond in some sensible way.

We'll begin with some code that finds out which sprite is under the clicked position, perhaps none! We add a method to the class, contains_point, which returns True if the point is within the rectangle of

the sprite:

```
def contains point(self, pt):
          """ Return True if my sprite rectangle contains point pt """
3
          (my_x, my_y) = self.posn
          my_width = self.image.get_width()
          my_height = self.image.get_height()
6
          (x, y) = pt
7
          return ( x \ge my_x and x < my_x + my_width and
8
                   y >= my_y and y < my_y + my_height)</pre>
```

Now in the game loop, once we've seen the mouse event, we determine which queen, if any, should be told to respond to the event:

```
1
    if ev.type == pygame.MOUSEBUTTONDOWN:
        posn_of_click = ev.dict['pos']
2
        for sprite in all sprites:
4
            if sprite.contains_point(posn_of_click):
5
                sprite.handle_click()
6
                break
```

And the final thing is to write a new method called handle_click in the Queen_sprite class. When a sprite is clicked, we'll just add some velocity in the up direction, i.e. kick it back into the air.

```
1
   def handle_click(self):
       self.y_velocity += -0.3 # kick it up
```

With these changes we have a playable game! See if you can keep all the balls on the move, not allowing any one to settle!

17.6. A wave of animation

Many games have sprites that are animated: they crouch, jump and shoot. How do they do that?

Consider this sequence of 10 images: if we display them in quick succession, Duke will wave at us. (Duke is a friendly visitor from the kingdom of Javaland.)





















A compound image containing smaller patches which are intended for animation is called a sprite sheet. Download this sprite sheet by right-clicking in your browser and saving it in your working directory with the name duke sprintesheet.png.

The sprite sheet has been quite carefully prepared: each of the 10 patches are spaced exactly 50 pixels apart. So, assuming we want to draw patch number 4 (numbering from 0), we want to draw only the rectangle that starts at x position 200, and is 50 pixels wide, within the sprite sheet. Here we've shown the patches and highlighted the patch we want to draw.





















The blit method we've been using — for copying pixels from one surface to another — can copy a sub-rectangle of the source surface. So the grand idea here is that each time we draw Duke, we won't blit the whole sprite sheet. Instead we'll provide an extra rectangle argument that determines which portion of the sprite sheet will be blitted.

We're going to add new code in this section to our existing N queens drawing game. What we want is to put some instances of Duke on the chessboard somewhere. If the user clicks on one of them, we'll get him to respond by waving back, for one cycle of his animation.

But before we do that, we need another change. Up until now, our game loop has been running at really fast frame rates that are unpredictable. So we've chosen some *magic numbers* for gravity and for bouncing and kicking the ball on the basis of trial-and-error. If we're going to start animating more sprites, we need to tame our game loop to operate at a fixed, known frame rate. This will allow us to plan our animation better.

PyGame gives us the tools to do this in just two lines of code. In the setup section of the game, we instantiate a new Clock object:

```
my_clock = pygame.time.Clock()
```

and right at the bottom of the game loop, we call a method on this object that limits the frame rate to whatever we specify. So let's plan our game and animation for 60 frames per second, by adding this line at the bottom of our game loop:

```
my_clock.tick(60) # Waste time so that frame rate becomes 60 fps
```

You'll find that you have to go back and adjust the numbers for gravity and kicking the ball now, to match this much slower frame rate. When we plan an animation so that it only works sensibly at a fixed frame rate, we say that we've *baked* the animation. In this case we're baking our animations for 60 frames per second.

To fit into the existing framework that we already have for our queens board, we want to create a Duke_sprite class that has all the same methods as the Queens_sprite class. Then we can add one or more Duke instances onto our list of all_sprites, and our existing game loop will then call methods of the Duke instance. Let us start with skeleton scaffolding for the new class:

```
1
     class Duke_sprite:
 2
 3
         def __init__(self, img, target_posn):
 4
             self.image = img
             self.posn = target_posn
 5
 6
 7
         def update(self):
8
             return
9
10
         def draw(self, target_surface):
11
             return
12
         def handle_click(self):
13
14
             return
15
         def contains_point(self, pt):
16
17
             # use code from Queens_sprite
18
             return
```

The only changes we'll need to the existing game are all in the setup section. We load up the new sprite sheet and instantiate a couple of instances of Duke, at the positions we want on the chessboard. So before entering the game loop, we add this code:

```
1
     # Load the sprite sheet
 2
    duke sprite sheet = pygame.image.load("duke spritesheet.png")
 3
4
    # Instantiate two duke instances, put them on the chessboard
5
    duke1 = Duke_sprite(duke_sprite_sheet,(sq_sz*2, 0))
    duke2 = Duke_sprite(duke_sprite_sheet,(sq_sz*5, sq_sz))
    # Add them to the list of sprites which our game loop manages
8
9
    all_sprites.append(duke1)
10
    all_sprites.append(duke2)
```

Now the game loop will test if each instance has been clicked, will call the click handler for that instance. It will also call update and draw for all sprites. All the remaining changes we need to make will be made in the methods of the Duke_sprite class.

Let's begin with drawing one of the patches. We'll introduce a new attribute curr_patch_num into the class. It holds a value between 0 and 9, and determines which patch to draw. So the job of the draw method is to compute the sub-rectangle of the patch to be drawn, and to blit only that portion of the spritesheet:

Now on to getting the animation to work. We need to arrange logic in update so that if we're busy animating, we change the curr_patch_num every so often, and we also decide when to bring Duke back to his rest position, and stop the animation. An important issue is that the game loop frame rate — in our case 60 fps — is not the same as the animation rate — the rate at which we want to change Duke's animation patches. So we'll plan Duke wave's animation cycle for a duration of 1 second. In other words, we want to play out Duke's 10 animation patches over 60 calls to update. (This is how the baking of the animation takes place!) So we'll keep another animation frame counter in the class, which will be zero when we're not animating, and each call to update will increment the counter up to 59, and then back to 0. We can then divide that animation counter by 6, to set the curr_patch_num variable to select the patch we want to show.

```
def update(self):
    if self.anim_frame_count > 0:
        self.anim_frame_count = (self.anim_frame_count + 1 ) % 60
        self.curr_patch_num = self.anim_frame_count // 6
```

Notice that if anim_frame_count is zero, i.e. Duke is at rest, nothing happens here. But if we start the counter running, it will count up to 59 before settling back to zero. Notice also, that because anim_frame_count can only be a value between 0 and 59, the curr_patch_num will always stay between 0 and 9. Just what we require!

Now how do we trigger the animation, and start it running? On the mouse click.

```
def handle_click(self):
```

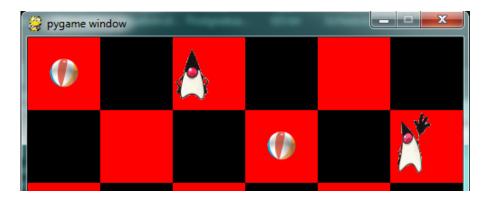
```
if self.anim_frame_count == 0:
self.anim_frame_count = 5
```

Two things of interest here. We only start the animation if Duke is at rest. Clicks on Duke while he is already waving get ignored. And when we do start the animation, we set the counter to 5 — this means that on the very next call to update the counter becomes 6, and the image changes. If we had set the counter to 1, we would have needed to wait for 5 more calls to update before anything happened — a slight lag, but enough to make things feel sluggish.

The final touch-up is to initialize our two new attributes when we instantiate the class. Here is the code for the whole class now:

```
class Duke_sprite:
1
        def __init__(self, img, target_posn):
3
4
            self.image = img
5
            self.posn = target_posn
            self.anim_frame_count = 0
6
7
            self.curr_patch_num = 0
8
9
        def update(self):
10
            if self.anim_frame_count > 0:
               self.anim_frame_count = (self.anim_frame_count + 1 ) % 60
11
               self.curr_patch_num = self.anim_frame_count // 6
12
13
        def draw(self, target_surface):
14
15
            patch_rect = (self.curr_patch_num * 50, 0,
16
                           50, self.image.get_height())
17
            target_surface.blit(self.image, self.posn, patch_rect)
18
19
        def contains_point(self, pt):
              """ Return True if my sprite rectangle contains pt """
20
             (my_x, my_y) = self.posn
21
22
             my_width = self.image.get_width()
             my_height = self.image.get_height()
23
24
             (x, y) = pt
25
             return ( x >= my_x and x < my_x + my_width and
26
                      y >= my_y and y < my_y + my_height)
27
28
        def handle click(self):
29
             if self.anim frame count == 0:
                self.anim_frame_count = 5
```

Now we have two extra Duke instances on our chessboard, and clicking on either causes that instance to wave.



17.7. Aliens – a case study

Find the example games with the PyGame package, (On a windows system, something like

C:\Python3\Lib\site-packages\pygame\examples) and play the Aliens game. Then read the code, in an editor or Python environment that shows line numbers.

It does a number of much more advanced things that we do, and relies on the PyGame framework for more of its logic. Here are some of the points that you'll notice:

- The frame rate is deliberately constrained near the bottom of the game loop at line 311. If you change that number you can make the game very slow or unplayably fast!
- There are different kinds of sprites: Explosions, Shots, Bombs, Aliens and a Player. Some of these have more than one image by swapping the images, we get animation of the sprites, i.e. the Alien spacecraft lights change, and this is done at line 112.
- Different kinds of objects are referenced in different groups of sprites, and PyGame helps maintain these. This lets the program check for collisions between, say, the list of shots fired by the player, and the list of spaceships that are attacking. PyGame does a lot of the hard work for you.
- Unlike our game, objects in the Aliens game have a limited lifetime, and have to get killed. For example, if you shoot, a Shot object is created if it reaches the top of the screen without expoding against anything, it has to be removed from the game. Lines 141–142 do this. Similarly, when a falling bomb gets close to the ground (line 156), it instantiates a new Explosion sprite, and the bomb kills itself.
- There are random timings that add to the fun when to spawn the next Alien, when an Alien drops the next bomb, etc.
- The game plays sounds too: a less-than-relaxing loop sound, plus sounds for the shots and explosions.

17.8. Reflections

Object oriented programming is a good organizational tool for software. In the examples in this chapter, we've started to use (and hopefully appreciate) these benefits. Here we had N queens each with its own state, falling to its own floor level, bouncing, getting kicked, etc. We might have managed without the organizational power of objects — perhaps we could have kept lists of velocities for each queen, and lists of target positions, and so on — our code would likely have been much more complicated, ugly, and a lot poorer!

17.9. Glossary

animation rate

The rate at which we play back successive patches to create the illusion of movement. In the sample we considered in this chapter, we played Duke's 10 patches over the duration of one second. Not the same as the frame rate.

baked animation

An animation that is designed to look good at a predetermined fixed frame rate. This reduces the amount of computation that needs to be done when the game is running. High-end commercial games usually bake their animations.

blit

A verb used in computer graphics, meaning to make a fast copy of an image or pixels from a sub-rectangle of one image or surface to another surface or image.

frame rate

The rate at which the game loop executes and updates the display.

game loop

A loop that drives the logic of a game. It will usually poll for events, then update each of the objects in the game, then get everything drawn, and then put the newly drawn frame on display.

pixel

A single picture element, or dot, from which images are made.

poll

To ask whether something like a keypress or mouse movement has happened. Game loops usually poll to discover what events have occured. This is different from event-driven programs like the ones seen in the chapter titled "Events". In those cases, the button click or keypress event triggers the call of a handler function in your program, but this happens behind your back.

sprite

An active agent or element in a game, with its own state, position and behaviour.

surface

This is PyGame's term for what the Turtle module calls a *canvas*. A surface is a rectangle of pixels used for displaying shapes and images.

17.10. Exercises

- 1. Have fun with Python, and with PyGame.
- 2. We deliberately left a bug in the code for animating Duke. If you click on one of the chessboard squares to the right of Duke, he waves anyway. Why? Find a one-line fix for the bug.
- 3. Search Google for "sprite sheet playing cards". Create a list [0..51] to represent an encoding of the 52 cards in a deck. Shuffle the cards, slice off the top five as your hand in a poker deal. Display the hand you have been dealt.
- 4. So the Aliens game is in outer space, without gravity. Shots fly away forever, and bombs don't speed up when they fall. Add some gravity to the game. Decide if you're going to allow your own shots to fall back on your head and kill you.
- 5. Those pesky Aliens seem to pass right through each other! Change the game so that they collide, and destroy each other in a mighty explosion.

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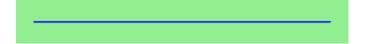
18. Recursion

18.1. Drawing Fractals

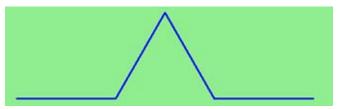
Recursion means "defining something in terms of itself" usually at some smaller scale, perhaps multiple times, to achieve your objective. For example, we might say "A human being is someone whose mother is a human being."

For our purposes, a fractal is drawing which also has self-similar structure, where it can be defined in terms of itself.

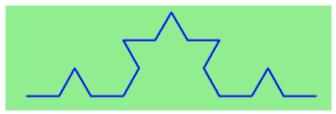
Let us start by looking at the famous Koch fractal. An order 0 Koch fractal is simply a straight line of a given size.



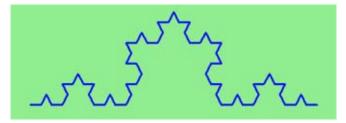
An order 1 Koch fractal is obtained like this: instead of drawing just one line, draw instead four smaller segments, in the pattern shown here:



Now what would happen if we repeated this Koch pattern again on each of the order 1 segments? We'd get this order 2 Koch fractal:



Repeating our pattern again gets us an order 3 Koch fractal:



Now let us think about it the other way around. To draw a Koch fractal of order 3, we can simply draw four order 2 Koch fractals. But each of these in turn needs four order 1 Koch fractals, and each of those in turn needs four order 0 fractals. Ultimately, the only drawing that will take place is at order 0. This is very simple to code up in Python:

```
def koch(t, order, size):
 1
 2
 3
           Make turtle t draw a Koch fractal of 'order' and 'size'.
 4
          Leave the turtle facing the same direction.
 5
 6
        if order == 0:
                                # The base case is just a straight line
 8
            t.forward(size)
 9
        else:
            koch(t, order-1, size/3) # go 1/3 of the way
10
            t.left(60)
11
            koch(t, order-1, size/3)
12
13
            t.right(120)
14
            koch(t, order-1, size/3)
15
            t.left(60)
            koch(t, order-1, size/3)
16
```

The key thing that is new here is that if order is not zero, koch calls itself recursively to get its job done.

Let's make a simple observation and tighten up this code. Remember that turning right by 120 is the same as turning left by -120. So with a bit of clever rearrangement, we can use a loop instead of lines 10-16:

```
def koch(t, order, size):
    if order == 0:
        t.forward(size)

else:
    for angle in [60, -120, 60, 0]:
        koch(t, order-1, size/3)
        t.left(angle)
```

The final turn is 0 degrees — so it has no effect. But it has allowed us to find a pattern and reduce seven lines of code to three, which will make things easier for our next observations.

Recursion, the high-level view

One way to think about this is to convince yourself that the function works correctly when you call it for an order 0 fractal. Then do a mental *leap of faith*, saying *"the fairy godmother* (or Python, if you can think of Python as your fairy godmother) *knows how to handle the recursive level 0 calls for me on lines* 11, 13, 15, and 17, so I don't need to think about that detail!" All I need to focus on is how to draw an order 1 fractal *if I can assume the order 0 one is already working*.

You're practicing mental abstraction — ignoring the subproblem while you solve the big problem.

If this mode of thinking works (and you should practice it!), then take it to the next level. Aha! now can I see that it will work when called for order 2 *under the assumption that it is already working for level 1*.

And, in general, if I can assume the order n-1 case works, can I just solve the level n problem?

Students of mathematics who have played with proofs of induction should see some very strong similarities here.

Recursion, the low-level operational view

Another way of trying to understand recursion is to get rid of it! If we had separate functions to draw a level 3 fractal, a level 2 fractal, a level 1 fractal and a level 0 fractal, we could simplify the above code, quite mechanically, to a situation where there was no longer any recursion, like this:

```
def koch_0(t, size):
 2
           t.forward(size)
 3
        def koch_1(t, size):
 5
           for angle in [60, -120, 60, 0]:
 6
               koch_0(t, size/3)
 7
               t.left(angle)
 8
 9
       def koch_2(t, size):
           for angle in [60, -120, 60, 0]:
10
11
               koch_1(t, size/3)
12
               t.left(angle)
13
14
       def koch_3(t, size):
15
            for angle in [60, -120, 60, 0]:
16
               koch_2(t, size/3)
               t.left(angle)
17
```

This trick of "unrolling" the recursion gives us an operational view of what happens. You can trace the program into koch_3, and from there, into koch_2, and then into koch_1, etc., all the way down the different layers of the recursion.

This might be a useful hint to build your understanding. The mental goal is, however, to be able to do the abstraction!

18.2. Recursive data structures

All of the Python data types we have seen can be grouped inside lists and tuples in a variety of ways. Lists and tuples can also be nested, providing a myriad possibilities for organizing data. The organization of data for the purpose of making it easier to use is called a data structure.

It's election time and we are helping to compute the votes as they come in. Votes arriving from individual wards, precincts, municipalities, counties, and states are sometimes reported as a sum total of votes and sometimes as a list of subtotals of votes. After considering how best to store the tallies, we decide to use a *nested number list*, which we define as follows:

A *nested number list* is a list whose elements are either:

- a. numbers
- b. nested number lists

Notice that the term, *nested number list* is used in its own definition. Recursive definitions like this are quite common in mathematics and computer science. They provide a concise and powerful way to describe recursive data structures that are partially composed of smaller and simpler instances of themselves. The definition is not circular, since at some point we will reach a list that does not have any lists as elements.

Now suppose our job is to write a function that will sum all of the values in a nested number list. Python has a built-in function which finds the sum of a sequence of numbers:

```
>>> sum([1, 2, 8])
11
```

For our *nested number list*, however, sum will not work:

```
>>> sum([1, 2, [11, 13], 8])
Traceback (most recent call last):
```

```
File "<interactive input>", line 1, in <module>
TypeError: unsupported operand type(s) for +: 'int' and 'list'
>>>
```

The problem is that the third element of this list, [11, 13], is itself a list, so it cannot just be added to 1, 2, and 8.

18.3. Recursion

To sum all the numbers in our recursive nested number list we need to traverse the list, visiting each of the elements within its nested structure, adding any numeric elements to our sum, and *repeating this process* with any elements which are lists.

Modern programming languages generally support recursion, which means that functions can *call themselves* within their definitions. Thanks to recursion, the Python code needed to sum the values of a nested number list is surprisingly short:

```
1
    def r_sum(nested_num_list):
2
       tot = 0
3
       for element in nested num list:
4
            if type(element) == type([]):
5
                tot += r_sum(element)
6
            else:
7
                tot += element
8
        return tot
```

The body of r_sum consists mainly of a for loop that traverses nested_num_list. If element is a numerical value (the else branch), it is simply added to tot. If element is a list, then r_sum is called again, with the element as an argument. The statement inside the function definition in which the function calls itself is known as the recursive call.

Recursion is truly one of the most beautiful and elegant tools in computer science.

A slightly more complicated problem is finding the largest value in our nested number list:

```
1
     def r_max(nxs):
 2
 3
           Find the maximum in a recursive structure of lists
 4
           within other lists.
 5
           Precondition: No lists or sublists are empty.
 6
 7
         largest = None
 8
         first time = True
9
         for e in nxs:
10
             if type(e) == type([]):
                  val = r max(e)
11
12
13
                  val = e
14
             if first_time or val > largest:
15
                  largest = val
16
                  first_time = False
17
18
         return largest
19
     test(r_max([2, 9, [1, 13], 8, 6]), 13)
test(r_max([2, [[100, 7], 90], [1, 13], 8, 6]), 100)
20
21
22
     test(r_max([[[13, 7], 90], 2, [1, 100], 8, 6]), 100)
     test(r_max(["joe", ["sam", "ben"]]), "sam")
23
```

Tests are included to provide examples of r_max at work.

The added twist to this problem is finding a value for initializing largest. We can't just use nxs[0], since that may be either a element or a list. To solve this problem (at every recursive call) we initialize a boolean flag. When we've found the value of interest, we check to see whether this is the initializing (first) value for largest, or a value that could potentially change largest.

The two examples above each have a base case which does not lead to a recursive call: the case where the element is a number and not a list. Without a base case, you'll have infinite recursion, and your program will not work. Python stops after reaching a maximum recursion depth and returns a runtime error. See how this happens, by running this little script which we will call *infinite_recursion.py*:

```
def recursion_depth(number):
    print("{0}, ".format(number), end='')
    recursion_depth(number + 1)

recursion_depth(0)
```

After watching the messages flash by, you will be presented with the end of a long traceback that ends with a message like the following:

```
RuntimeError: maximum recursion depth exceeded ...
```

We would certainly never want something like this to happen to a user of one of our programs, so before finishing the recursion discussion, let's see how errors, any kinds of errors, are handled in Python.

18.4. Case study: Fibonacci numbers

The famous Fibonacci sequence 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 134, ... was devised by Fibonacci (1170–1250), who used this to model the breeding of (pairs) of rabbits. If, in generation 7 you had 21 pairs in total, of which 13 were adults, then next generation the adults will all have bred new children, and the previous children will have grown up to become adults. So in generation 8 you'll have 13+21=34, of which 21 are adults.

This *model* to explain rabbit breeding made the simplifying assumption that rabbits never died. Scientists often make (unrealistic) simplifying assumptions and restrictions to make some headway with the problem.

If we number the terms of the sequence from 0, we can describe each term recursively as the sum of the previous two terms:

```
fib(0) = 0

fib(1) = 1

fib(n) = fib(n-1) + fib(n-2) for n >= 2
```

This translates very directly into some Python:

```
def fib(n):
    if n <= 1:
        return n
    t = fib(n-1) + fib(n-2)</pre>
```

```
5 return t
```

This is a particularly inefficient algorithm, and we'll show one way of fixing it when we learn about dictionaries:

```
import time
t0 = time.clock()
n = 35
result = fib(n)
t1 = time.clock()
print('fib({0}) = {1}, ({2:.2f} secs)'.format(n, result, t1-t0))
```

We get the correct result, but an exploding amount of work!

```
fib(35) = 9227465, (10.54 secs)
```

18.5. Example with recursive directories and files

The following program lists the contents of a directory and all its subdirectories.

```
1
     import os
 2
 3
     def get_dirlist(path):
 4
 5
          Return a sorted list of all entries in path.
          This returns just the names, not the full path to the names.
 6
 7
 8
        dirlist = os.listdir(path)
9
        dirlist.sort()
10
         return dirlist
11
    def print_files(path, prefix = ""):
12
13
         """ Print recursive listing of contents of path """
         if prefix == "": # detect outermost call, print a heading
14
15
            print('Folder listing for', path)
16
            prefix = "| "
17
        dirlist = get_dirlist(path)
18
19
        for f in dirlist:
20
            print(prefix+f)
                                            # print the line
            fullE = os.path.join(path, f) # turn name into full path
21
            if os.path.isdir(fullE):
22
                                             # if a directory, recurse.
23
                print_files(fullE, prefix + " ")
```

Calling the function print_files with some folder name will produce output similar to this:

```
Folder listing for c:\python31\Lib\site-packages\pygame\examples
| __init__.py
| aacircle.py
| aliens.py
| arraydemo.py
| blend_fill.py
| blit_blends.py
| camera.py
| chimp.py
| cursors.py
| data
```

```
| | alien1.png
| | alien2.png
| | alien3.png
...
```

18.6. Glossary

base case

A branch of the conditional statement in a recursive function that does not give rise to further recursive calls.

infinite recursion

A function that calls itself recursively without ever reaching any base case. Eventually, infinite recursion causes a runtime error.

recursion

The process of calling a function that is already executing.

recursive call

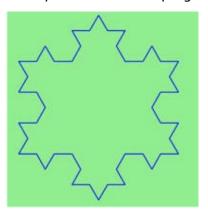
The statement that calls an already executing function. Recursion can also be indirect — function f can call g which calls h, and h could make a call back to f.

recursive definition

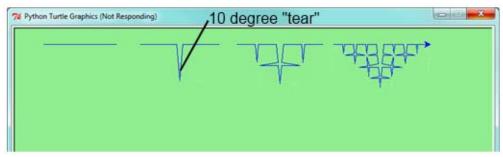
A definition which defines something in terms of itself. To be useful it must include *base cases* which are not recursive. In this way it differs from a *circular definition*. Recursive definitions often provide an elegant way to express complex data structures, like a directory that can contain other directories, or a menu that can contain other menus.

18.7. Exercises

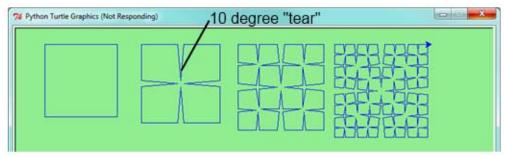
1. Modify the Koch fractal program so that it draws a Koch snowflake, like this:



2. a. Draw a Cesaro torn line fractal, of the order given by the user. We show four different lines of orders 0,1,2,3. In this example, the angle of the tear is 10 degrees.



b. Four lines make a square. Use the code in part a) to draw cesaro squares. Varying the angle gives interesting effects — experiment a bit, or perhaps let the user input the angle of the tear.



- c. (For the mathematically inclined). In the squares shown here, the higher-order drawings become a little larger. (Look at the bottom lines of each square they're not aligned.) This is because we just halved the drawn part of the line for each recursive subproblem. So we've "grown" the overall square by the width of the tear(s). Can you solve the geometry problem so that the total size of the subproblem case (including the tear) remains exactly the same size as the original?
- 3. A Sierpinski triangle of order 0 is an equilateral triangle. An order 1 triangle can be drawn by drawing 3 smaller triangles (shown slightly disconnected here, just to help our understanding). Higher order 2 and 3 triangles are also shown. Draw Sierpinski triangles of any order input by the user.

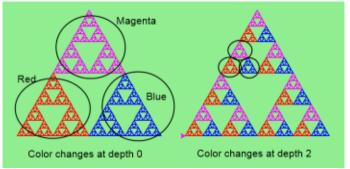








4. Adapt the above program to change the color of its three sub-triangles at some depth of recursion. The illustration below shows two cases: on the left, the color is changed at depth 0 (the outmost level of recursion), on the right, at depth 2. If the user supplies a negative depth, the color never changes. (Hint: add a new optional parameter colorChangeDepth (which defaults to -1), and make this one smaller on each recursive subcall. Then, in the section of code before you recurse, test whether the parameter is zero, and change color.)



5. Write a function, recursive_min, that returns the smallest value in a nested number list. Assume there are no empty lists or sublists:

```
test(recursive_min([2, 9, [1, 13], 8, 6]), 1)
test(recursive_min([2, [[100, 1], 90], [10, 13], 8, 6]), 1)
test(recursive_min([2, [[13, -7], 90], [1, 100], 8, 6]), -7)
test(recursive_min([[[-13, 7], 90], 2, [1, 100], 8, 6]), -13)
```

6. Write a function count that returns the number of occurences of target in a nested list:

7. Write a function flatten that returns a simple list containing all the values in a nested list:

- 8. Rewrite the fibonacci algorithm without using recursion. Can you find bigger terms of the sequence? Can you find fib(200)?
- 9. Use help to find out what sys.getrecursionlimit() and sys.setrecursionlimit(n) do. Create several experiments similar to what was done in infinite_recursion.py to test your understanding of how these module functions work.
- 10. Write a program that walks a directory structure (as in the last section of this chapter), but instead of printing filenames, it returns a list of all the full paths of files in the directory or the subdirectories. (Don't include directories in this list just files.) For example, the output list might have elements like this:

```
['C:\Python31\Lib\site-packages\pygame\docs\ref\mask.html',
    'C:\Python31\Lib\site-packages\pygame\docs\ref\midi.html',
    ...
    'C:\Python31\Lib\site-packages\pygame\examples\aliens.py',
    ...
    'C:\Python31\Lib\site-packages\pygame\examples\data\boom.wav',
    ...
]
```

11. Write a program named litter.py that creates an empty file named trash.txt in each

subdirectory of a directory tree given the root of the tree as an argument (or the current directory as a default). Now write a program named cleanup.py that removes all these files. *Hint:* Use the program from the example in the last section of this chapter as a basis for these two recursive programs. Because you're going to destroy files on your disks, you better get this right, or you risk losing files you care about. So excellent advice is that initially you should fake the deletion of the files — just print the full path names of each file that you intend to delete. Once you're happy that your logic is correct, and you can see that you're not deleting the wrong things, you can replace the print statement with the real thing.

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19. Exceptions

19.1. Catching exceptions

Whenever a runtime error occurs, it creates an exception object. The program stops running at this point and Python prints out the traceback, which ends with a message describing the exception that occurred.

For example, dividing by zero creates an exception:

```
>>> print(55/0)
Traceback (most recent call last):
 File "<interactive input>", line 1, in <module>
ZeroDivisionError: integer division or modulo by zero
>>>
```

So does accessing a non-existent list item:

```
>>> a = []
>>> print(a[5])
Traceback (most recent call last):
 File "<interactive input>", line 1, in <module>
IndexError: list index out of range
>>>
```

Or trying to make an item assignment on a tuple:

```
>>> tup = ('a', 'b', 'd', 'd')
>>> tup[2] = 'c'
Traceback (most recent call last):
 File "<interactive input>", line 1, in <module>
TypeError: 'tuple' object does not support item assignment
>>>
```

In each case, the error message on the last line has two parts: the type of error before the colon, and specifics about the error after the colon.

Sometimes we want to execute an operation that might cause an exception, but we don't want the program to stop. We can handle the exception using the try statement to "wrap" a region of code.

For example, we might prompt the user for the name of a file and then try to open it. If the file doesn't exist, we don't want the program to crash; we want to handle the exception:

```
filename = input('Enter a file name: ')
1
2
3
        f = open(filename, 'r')
4
    except:
        print('There is no file named', filename)
```

The try statement has three separate clauses, or parts, introduced by the keywords try ... except ...

finally. The finally clause can be omitted, so we'll consider the two-clause version of the try statement first.

The <u>try</u> statement executes and monitors the statements in the first block. If no exceptions occur, it skips the block under the <u>except</u> clause. If any exception occurs, it executes the statements in the except clause and then continues.

We could encapsulate this capability in a function: exists which takes a filename and returns true if the file exists, false if it doesn't:

```
def exists(filename):
    try:
        f = open(filename)
        f.close()
        return True
    except:
        return False
```

A template to test if a file exists, without using exceptions

The function we've just shown is not one we'd recommend. It opens and closes the file, which is semantically different from asking "does it exist?". How? Firstly, it might update some timestamps on the file. Secondly, it might tell you that there is no such file if some other program already happens to have the file open, or if your permissions settings don't allow you to open the file.

Python provides a module called <u>os.path</u> (this is the first time we've seen a dotted module name with two namespace components). It provides a number of useful functions to work with paths, files and directories, so you should check out the help.

```
import os.path

this is the preferred way to check if a file exists.
if os.path.isfile("c:/temp/testdata.txt"):
...
```

You can use multiple except clauses to handle different kinds of exceptions (see the Errors and Exceptions lesson from Python creator Guido van Rossum's Python Tutorial for a more complete discussion of exceptions). So your program could do one thing if the file does not exist, but do something else if the file was in use by another program.

19.2. Raising your own exceptions

Can your program deliberately cause its own exceptions? If your program detects an error condition, you can raise an exception. Here is an example that gets input from the user and checks that the number is non-negative:

```
def get_age():
    age = int(input('Please enter your age: '))
    if age < 0:
        # Create a new instance of an exception
        myError = ValueError('{0} is not a valid age'.format(age))
    raise myError</pre>
```

```
7 return age
```

Line 4 creates an exception object, in this case, a ValueError object, which encapsulates your specific information about the error. The raise statement on line 5 carries this object out as a kind of "return value", and immediately exits from the function, and its caller, and its caller, until it encounters a try ... except that can handle the exception. We call this "unwinding the call stack".

<u>ValueError</u> is one of the built-in exception types which most closely matches the kind of error we want to raise. The complete listing of built-in exceptions is found in the <u>Built-in Exceptions</u> section of the <u>Python Library Reference</u>, again by Python's creator, Guido van Rossum.

If the function that called get_age (or its caller, or their caller, ...) handles the error, then the program can carry on running; otherwise, Python prints the traceback and exits:

```
>>> get_age()
Please enter your age: 42
42
>>> get_age()
Please enter your age: -2
Traceback (most recent call last):
  File "<interactive input>", line 1, in <module>
  File "learn_exceptions.py", line 4, in get_age
    raise ValueError('{0} is not a valid age'.format(age))
ValueError: -2 is not a valid age
>>>
```

The error message includes the exception type and the additional information that was provided when the exception object was first created.

It is often the case that lines 4 and 5 (creating the exception object, then raising the exception) are combined into a single statement, but there are really two different and independent things happening, so perhaps it makes sense to keep the two steps separate when we first learn to work with exceptions. Here we show it all in a single statement:

```
raise ValueError('{0} is not a valid age'.format(age))
```

19.3. Revisiting an earlier example

Using exception handling, we can now modify our recursion_depth example from the previous chapter so that it stops when it reaches the maximum recursion depth allowed:

```
def recursion_depth(number):
    print("Recursion depth number", number)
    try:
        recursion_depth(number + 1)
    except:
        print("I cannot go any deeper into this wormhole.")
recursion_depth(0)
```

Run this version and observe the results.

19.4. The finally clause of the try statement

A common programming pattern is to grab a resource of some kind — e.g. we create a window for turtles to draw on, or we dial up a connection to our internet service provider, or we may open a file for writing. Then we perform some computation which may raise an exception, or may work without any problems.

Whatever happens, we want to "clean up" the resources we grabbed — e.g. close the window, disconnect our dial-up connection, or close the file. The <u>finally</u> clause of the <u>try</u> statement is the way to do just this. Consider this (somewhat contrived) example:

```
1
      import turtle, time
2
3
     def show_poly():
         try:
4
                                     # Grab/create a resource, eg a window
5
             win = turtle.Screen()
6
             tess = turtle.Turtle()
7
8
             # This dialog could be cancelled,
9
             # or the conversion to int might fail.
             n = int(input("How many sides do you want in your polygon?"))
10
11
             angle = 360 / n
12
             for i in range(n):
                                     # Draw the polygon
13
                 tess.forward(10)
14
                 tess.left(angle)
15
             time.sleep(3)
                                    # make program wait a few seconds
       finally:
16
17
                                     # close the turtle's window.
             win.bye()
18
19
20
      show_poly()
21
      show_poly()
22
     show poly()
```

In lines 19–21, show_poly is called three times. Each one creates a new window for its turtle, and draws a polygon with the number of sides input by the user. But what if the user enters a string that cannot be converted to an int? What if they close the dialog? We'll get an exception, but even though we've had an exception, we still want to close the turtle's window. Lines 16–17 does this for us. Whether we complete the statements in the try clause successfully or not, the finally block will always be executed.

Notice that the exception is still unhandled — only an except clause can handle an exception, so your program will still crash. But at least it's turtle window will be closed before it crashes!

19.5. Glossary

exception

An error that occurs at runtime.

handle an exception

To prevent an exception from causing your program to crash, by wrapping the block of code in a try / except construct.

immutable data type

A data type which cannot be modified. Assignments to elements or slices (sub-parts)

of immutable types cause a runtime error.

mutable data type

A data type which can be modified. All mutable types are compound types. Lists and dictionaries (see next chapter) are mutable data types; strings and tuples are not.

raise

To create a deliberate exception by using the raise statement.

19.6. Exercises

1. Write a function named readposint that uses the input dialog to prompt the user for a positive integer and then checks the input to confirm that it meets the requirements. It should be able to handle inputs that cannot be converted to int, as well as negative ints, and edge cases (e.g. when the user closes the dialog, or does not enter anything at all.)

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20. Dictionaries

All of the compound data types we have studied in detail so far — strings, lists, and tuples — are sequence types, which use integers as indices to access the values they contain within them.

Dictionaries are yet another kind of compound type. They are Python's built-in mapping type. They map keys, which can be any immutable type, to values, which can be any type, just like the values of a list or tuple.

As an example, we will create a dictionary to translate English words into Spanish. For this dictionary, the keys are strings.

One way to create a dictionary is to start with the empty dictionary and add key-value pairs. The empty dictionary is denoted {}:

```
>>> eng2sp = {}
>>> eng2sp['one'] = 'uno'
>>> eng2sp['two'] = 'dos'
```

The first assignment creates a dictionary named eng2sp; the other assignments add new key-value pairs to the dictionary. We can print the current value of the dictionary in the usual way:

```
>>> print(eng2sp)
{'two': 'dos', 'one': 'uno'}
```

The key-value pairs of the dictionary are seperated by commas. Each pair contains a key and a value separated by a colon.

The order of the pairs may not be what you expected. Python uses complex algorithms, designed for very fast access, to determine where the key-value pairs are stored in a dictionary. For our purposes we can think of this ordering as unpredicatable.

Another way to create a dictionary is to provide a list of key-value pairs using the same syntax as the previous output:

```
>>> eng2sp = {'one': 'uno', 'two': 'dos', 'three': 'tres'}
```

It doesn't matter what order we write the pairs. The values in a dictionary are accessed with keys, not with indices, so there is no need to care about ordering.

Here is how we use a key to look up the corresponding value:

```
>>> print(eng2sp['two'])
'dos'
```

The key 'two' yields the value 'dos'.

Lists, tuples, and strings have been called *sequences*, because their items occur in order. The dictionary is the first compound type that we've seen that is not a sequence, so we can't index or slice a dictionary.

20.1. Dictionary operations

The del statement removes a key-value pair from a dictionary. For example, the following dictionary contains the names of various fruits and the number of each fruit in stock:

```
>>> inventory={'apples':430,'bananas':312,'oranges':525,'pears':217}
>>> print(inventory)
{'pears': 217, 'apples': 430, 'oranges': 525, 'bananas': 312}
```

If someone buys all of the pears, we can remove the entry from the dictionary:

```
>>> del inventory['pears']
>>> print(inventory)
{'apples': 430, 'oranges': 525, 'bananas': 312}
```

Or if we're expecting more pears soon, we might just change the value associated with pears:

```
>>> inventory['pears'] = 0
>>> print(inventory)
{'pears': 0, 'apples': 430, 'oranges': 525, 'bananas': 312}
```

A new shipment of bananas arriving could be handled like this:

```
>>> inventory['bananas'] += 200
>>> print(inventory)
{'pears': 0, 'apples': 430, 'oranges': 525, 'bananas': 512}
```

The len function also works on dictionaries; it returns the number of key-value pairs:

```
>>> len(inventory)
4
```

20.2. Dictionary methods

Dictionaries have a number of useful built-in methods.

The keys method returns what Python 3 calls a view of its underlying keys. A view object has some similarities to the range object we saw earlier — it is a lazy promise, to deliver its elements when they're needed by the rest of the program. We can iterate over the view, or turn the view into a list like this:

```
for k in eng2sp.keys(): # the order of the k's is not defined
    print("Got key", k, "which maps to value", eng2sp[k])

ks = list(eng2sp.keys())
    print(ks)
```

This produces this output:

```
Got key three which maps to value tres
Got key two which maps to value dos
```

```
Got key one which maps to value uno ['three', 'two', 'one']
```

It is so common to iterate over the keys in a dictionary that you can omit the keys method call in the for loop — iterating over a dictionary implicitly iterates over its keys:

```
for k in eng2sp:
    print("Got key", k)
```

As we saw earlier with strings and lists, dictionary methods use dot notation, which specifies the name of the method to the right of the dot and the name of the object on which to apply the method immediately to the left of the dot. The parentheses indicate that this method takes no parameters.

A method call is called an invocation; in this case, we would say that we are invoking the keys method on the object eng2sp. As we will see in a few chapters when we talk about object oriented programming, the object on which a method is invoked is actually the first argument to the method.

The values method is similar; it returns a view object which can be turned into a list:

```
>>> list(eng2sp.values())
['tres', 'dos', 'uno']
```

The <u>items</u> method also returns a view, which promises a list of tuples — one tuple for each key-value pair:

```
>>> list(eng2sp.items())
[('three', 'tres'), ('two', 'dos'), ('one', 'uno')]
```

Tuples are often useful for getting both the key and the value at the same time while you are looping:

```
for (k,v) in eng2sp.items():
    print("Got",k,"that maps to",v)
```

This produces:

```
Got three that maps to tres
Got two that maps to dos
Got one that maps to uno
```

The in and not in operators can test if a key is in the dictionary:

```
>>> 'one' in eng2sp
True
>>> 'six' in eng2sp
False
>>> 'tres' in eng2sp # note that 'in' tests keys, not values.
False
```

This method can be very useful, since looking up a non-existent key in a dictionary causes a runtime error:

```
>>> eng2esp['dog']
```

```
Traceback (most recent call last):
    ...
KeyError: 'dog'
>>>
```

20.3. Aliasing and copying

As in the case of lists, because dictionaries are mutable, you need to be aware of aliasing. Whenever two variables refer to the same object, changes to one affect the other.

If you want to modify a dictionary and keep a copy of the original, use the <u>copy</u> method. For example, opposites is a dictionary that contains pairs of opposites:

```
>>> opposites = {'up': 'down', 'right': 'wrong', 'true': 'false'}
>>> alias = opposites
>>> copy = opposites.copy()
```

alias and opposites refer to the same object; copy refers to a fresh copy of the same dictionary. If we modify alias, opposites is also changed:

```
>>> alias['right'] = 'left'
>>> opposites['right']
'left'
```

If we modify copy, opposites is unchanged:

```
>>> copy['right'] = 'privilege'
>>> opposites['right']
'left'
```

20.4. Sparse matrices

We previously used a list of lists to represent a matrix. That is a good choice for a matrix with mostly nonzero values, but consider a <u>sparse matrix</u> like this one:

```
0 0 0 1 0
0 0 0 0 0
0 2 0 0 0
0 0 0 0 0
0 0 0 3 0
```

The list representation contains a lot of zeroes:

An alternative is to use a dictionary. For the keys, we can use tuples that contain the row and column numbers. Here is the dictionary representation of the same matrix:

```
>>> matrix = {(0, 3): 1, (2, 1): 2, (4, 3): 3}
```

We only need three key-value pairs, one for each nonzero element of the matrix. Each key is a tuple,

and each value is an integer.

To access an element of the matrix, we could use the [] operator:

```
>>> matrix[(0, 3)]
1
```

Notice that the syntax for the dictionary representation is not the same as the syntax for the nested list representation. Instead of two integer indices, we use one index, which is a tuple of integers.

There is one problem. If we specify an element that is zero, we get an error, because there is no entry in the dictionary with that key:

```
>>> matrix[(1, 3)]
KeyError: (1, 3)
```

The get method solves this problem:

```
>>> matrix.get((0, 3), 0)
1
```

The first argument is the key; the second argument is the value get should return if the key is not in the dictionary:

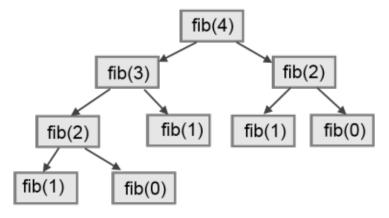
```
>>> matrix.get((1, 3), 0)
0
```

get definitely improves the semantics of accessing a sparse matrix. Shame about the syntax.

20.5. Memos

If you played around with the fibo function from the chapter on recursion, you might have noticed that the bigger the argument you provide, the longer the function takes to run. Furthermore, the run time increases very quickly. On one of our machines, fib(20) finishes instantly, fib(30) takes about a second, and fib(40) takes roughly forever.

To understand why, consider this call graph for fib with n = 4:



A call graph shows some function frames (instances when the function has been invoked), with lines connecting each frame to the frames of the functions it calls. At the top of the graph, $\frac{fib}{f}$ with $\frac{fi$

Count how many times fib(0) and fib(1) are called. This is an inefficient solution to the problem, and it gets far worse as the argument gets bigger.

A good solution is to keep track of values that have already been computed by storing them in a dictionary. A previously computed value that is stored for later use is called a memo. Here is an implementation of fib using memos:

```
1
    previous = \{0: 0, 1: 1\}
3
   def fib(n):
4
       if n in previous:
5
           return previous[n]
6
       else:
7
           new value = fib(n-1) + fib(n-2)
           previous[n] = new_value
8
9
           return new_value
```

The dictionary named previous keeps track of the Fibonacci numbers we already know. We start with only two pairs: 0 maps to 1; and 1 maps to 1.

Whenever fib is called, it checks the dictionary to determine if it contains the result. If it's there, the function can return immediately without making any more recursive calls. If not, it has to compute the new value. The new value is added to the dictionary before the function returns.

Using this version of fib, our machines can compute fib(100) in an eyeblink.

```
>>> fib(100)
354224848179261915075
```

20.6. Counting letters

In the exercises in Chapter 8 we wrote a function that counted the number of occurrences of a letter in a string. A more general version of this problem is to form a frequency table of the letters in the string, that is, how many times each letter appears.

Such a frequency table might be useful for compressing a text file. Because different letters appear with different frequencies, we can compress a file by using shorter codes for common letters and longer codes for letters that appear less frequently.

Dictionaries provide an elegant way to generate a frequency table:

```
>>> letter_counts = {}
>>> for letter in "Mississippi":
... letter_counts[letter] = letter_counts.get (letter, 0) + 1
...
>>> letter_counts
{'M': 1, 's': 4, 'p': 2, 'i': 4}
```

We start with an empty dictionary. For each letter in the string, we find the current count (possibly zero) and increment it. At the end, the dictionary contains pairs of letters and their frequencies.

It might be more appealing to display the frequency table in alphabetical order. We can do that with the items and sort methods:

```
>>> letter_items = list(letter_counts.items())
```

```
>>> letter_items.sort()
>>> print(letter_items)
[('M', 1), ('i', 4), ('p', 2), ('s', 4)]
```

Notice in the first line we had to call the type conversion function <u>list</u>. That turns the promise we get from <u>items</u> into a list, a step that is needed before we can use the list's <u>sort</u> method.

20.7. Glossary

call graph

A graph consisting of nodes which represent function frames (or invocations), and directed edges (lines with arrows) showing which frames gave rise to other frames.

dictionary

A collection of key-value pairs that maps from keys to values. The keys can be any immutable type, and the values can be any type.

key

A data item that is *mapped to* a value in a dictionary. Keys are used to look up values in a dictionary.

key-value pair

One of the pairs of items in a dictionary. Values are looked up in a dictionary by key.

mapping type

A mapping type is a data type comprised of a collection of keys and associated values. Python's only built-in mapping type is the dictionary. Dictionaries implement the <u>associative array</u> abstract data type.

memo

Temporary storage of precomputed values to avoid duplicating the same computation.

20.8. Exercises

1. Write a program that reads a string and returns a table of the letters of the alphabet in alphabetical order which occur in the string together with the number of times each letter occurs. Case should be ignored. A sample output of the program when the user enters the data

ThiS is String with Upper and lower case Letters

would look this this:

```
a 2
c 1
d 1
e 5
g 1
h 2
i 4
l 2
n 2
o 1
p 2
r 4
s 5
```

```
t 5
u 1
w 2
$
```

2. Give the Python interpreter's response to each of the following from a continuous interpreter session:

```
>>> d = {'apples': 15, 'bananas': 35, 'grapes': 12}
>>> d['oranges'] = 20
>>> len(d)

>>> 'grapes' in d

>>> d['pears']

>>> d.get('pears', 0)

>>> fruits = d.keys()
>>> fruits.sort()
>>> print(fruits)

>>> del d['apples']
>>> 'apples' in d
```

Be sure you understand why you get each result. Then apply what you have learned to fill in the body of the function below:

```
def add_fruit(inventory, fruit, quantity=0):
 1
 2
         pass
 3
 4
    # make these tests work...
    new_inventory = {}
 5
6
    add_fruit(new_inventory, 'strawberries', 10)
 7
    test('strawberries' in new_inventory, True)
    test(new_inventory['strawberries'], 10)
8
9
    add_fruit(new_inventory, 'strawberries', 25)
    test(new_inventory['strawberries'], 35)
10
```

3. Write a program called alice_words.py that creates a text file named alice_words.txt containing an alphabetical listing of all the words, and the number of times each occurs, in the text version of Alice's Adventures in WonderLand. (You can obtain a free plain text version of the book, along with many others, from http://www.gutenberg.org.) The first 10 lines of your output file should look something like this:

about 94 above 3 absence 1
ahsence 1
absence
absurd 2

How many times does the word, alice, occur in the book?

4. What is the longest word in Alice in Wonderland? How many characters does it have?

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21. Even more OOP

21.1. MyTime

As another example of a user-defined type, we'll define a class called MyTime that records the time of day. We'll provide an __init__ method to ensure that every instance is created with appropriate attributes and initialization. The class definition looks like this:

```
class MyTime:

def __init__(self, hrs=0, mins=0, secs=0):
    """ Create a MyTime object initialized to hrs, mins, secs """
    self.hours = hrs
    self.minutes = mins
    self.seconds = secs
```

We can instantiate a new MyTime object:

```
1 tim1 = MyTime(11, 59, 30)
```

The state diagram for the object looks like this:

```
tim1 → hours → 11
minutes → 59
seconds → 30
```

We'll leave it as an exercise for the readers to add a <u>str</u> method so that MyTime objects can print themselves decently.

21.2. Pure functions

In the next few sections, we'll write two versions of a function called add_time, which calculates the sum of two MyTime objects. They will demonstrate two kinds of functions: pure functions and modifiers.

The following is a rough version of add time:

```
def add_time(t1, t2):
    h = t1.hours + t2.hours
    m = t1.minutes + t2.minutes
    s = t1.seconds + t2.seconds
    sum_t = MyTime(h, m, s)
    return sum_t
```

The function creates a new MyTime object and returns a reference to the new object. This is called a

pure function because it does not modify any of the objects passed to it as parameters and it has no side effects, such as updating global variables, displaying a value, or getting user input.

Here is an example of how to use this function. We'll create two MyTime objects: current_time, which contains the current time; and bread_time, which contains the amount of time it takes for a breadmaker to make bread. Then we'll use add time to figure out when the bread will be done.

```
>>> current_time = MyTime(9, 14, 30)
>>> bread_time = MyTime(3, 35, 0)
>>> done_time = add_time(current_time, bread_time)
>>> print(done_time)
12:49:30
```

The output of this program is 12:49:30, which is correct. On the other hand, there are cases where the result is not correct. Can you think of one?

The problem is that this function does not deal with cases where the number of seconds or minutes adds up to more than sixty. When that happens, we have to carry the extra seconds into the minutes column or the extra minutes into the hours column.

Here's a better version of the function:

```
def add_time(t1, t2):
 1
 2
 3
        h = t1.hours + t2.hours
 4
        m = t1.minutes + t2.minutes
 5
        s = t1.seconds + t2.seconds
 6
 7
        if s >= 60:
 8
            s -= 60
 9
            m += 1
10
11
        if m >= 60:
12
            m -= 60
13
            h += 1
14
15
        sum_t = MyTime(h, m, s)
16
        return sum t
```

This function is starting to get bigger, and still doesn't work for all possible cases. Later we will suggest an alternative approach that yields better code.

21.3. Modifiers

There are times when it is useful for a function to modify one or more of the objects it gets as parameters. Usually, the caller keeps a reference to the objects it passes, so any changes the function makes are visible to the caller. Functions that work this way are called modifiers.

increment, which adds a given number of seconds to a MyTime object, would be written most naturally as a modifier. A rough draft of the function looks like this:

```
def increment(t, secs):
    t.seconds += secs

if t.seconds >= 60:
```

```
t.seconds -= 60
t.minutes += 1

if t.minutes >= 60:
t.minutes -= 60
t.hours += 1
```

The first line performs the basic operation; the remainder deals with the special cases we saw before.

Is this function correct? What happens if the parameter <u>seconds</u> is much greater than sixty? In that case, it is not enough to carry once; we have to keep doing it until <u>seconds</u> is less than sixty. One solution is to replace the <u>if</u> statements with <u>while</u> statements:

```
def increment(t, seconds):
1
2
        t.seconds += seconds
3
4
        while t.seconds >= 60:
5
            t.seconds -= 60
6
            t.minutes += 1
8
        while t.minutes >= 60:
9
            t.minutes -= 60
10
            t.hours += 1
```

This function is now correct when seconds is not negative, and when hours does not exceed 23, but it is not a particularly good solution.

21.4. Converting increment to a method

Once again, OOP programmers would prefer to put functions that work with MyTime objects into the MyTime class, so let's convert increment to a method. To save space, we will leave out previously defined methods, but you should keep them in your version:

```
1
     class MyTime:
2
        #previous method definitions here...
3
4
        def increment(self, seconds):
5
            self.seconds += seconds
6
7
            while self.seconds >= 60:
8
                self.seconds -= 60
9
                self.minutes += 1
10
            while self.minutes >= 60:
11
12
                self.minutes -= 60
13
                self.hours += 1
```

The transformation is purely mechanical – we move the definition into the class definition and (optionally) change the name of the first parameter to self, to fit with Python style conventions.

Now we can invoke increment using the syntax for invoking a method.

```
current_time.increment(500)
```

Again, the object on which the method is invoked gets assigned to the first parameter, self. The second parameter, seconds gets the value 500.

21.5. An "Aha!" insight

Often a high-level insight into the problem can make the programming much easier.

In this case, the insight is that a MyTime object is really a three-digit number in base 60! The second component is the ones column, the minute component is the sixties column, and the hour component is the thirty-six hundreds column.

When we wrote add_time and increment, we were effectively doing addition in base 60, which is why we had to carry from one column to the next.

This observation suggests another approach to the whole problem — we can convert a MyTime object into a single number and take advantage of the fact that the computer knows how to do arithmetic with numbers. The following method is added to the MyTime class to convert any instance into a corresponding number of seconds:

```
class MyTime:
    # ...

def to_seconds(self):
    """ Return the number of seconds represented
    by this instance
    """
return self.hours * 3600 + self.minutes * 60 + self.seconds
```

Now, all we need is a way to convert from an integer back to a MyTime object. Supposing we have tsecs seconds, some integer division and mod operators can do this for us:

```
hrs = tsecs // 3600
leftoversecs = tsecs % 3600
mins = leftoversecs // 60
secs = leftoversecs % 60
```

You might have to think a bit to convince yourself that this technique to convert from one base to another is correct.

In OOP we're really trying to wrap together the data and the operations that apply to it. So we'd like to have this logic inside the MyTime class. A good solution is to rewrite the class initializer so that it can cope with initial values of seconds or minutes that are outside the normalized values. (A normalized time would be something like 3 hours 12 minutes and 20 seconds. The same time, but unnormalized could be 2 hours 70 minutes and 140 seconds.)

Let's rewrite a more powerful initializer for MyTime:

```
class MyTime:
    # ...

def __init__(self, hrs=0, mins=0, secs=0):
    """ Create a new MyTime object initialized to hrs, mins, secs.
```

```
The values of mins and secs may be outside the range 0-59,
7
               but the resulting MyTime object will be normalized.
8
9
10
           # calculate total seconds to represent
11
           totalsecs = hrs*3600 + mins*60 + secs
12
           self.hours = totalsecs // 3600
                                               # split in h, m, s
13
           leftoversecs = totalsecs % 3600
14
           self.minutes = leftoversecs // 60
15
           self.seconds = leftoversecs % 60
```

Now we can rewrite add time like this:

```
def add_time(t1, t2):
    secs = t1.to_seconds() + t2.to_seconds()
    return MyTime(0, 0, secs)
```

This version is much shorter than the original, and it is much easier to demonstrate or reason that it is correct.

21.6. Generalization

In some ways, converting from base 60 to base 10 and back is harder than just dealing with times. Base conversion is more abstract; our intuition for dealing with times is better.

But if we have the insight to treat times as base 60 numbers and make the investment of writing the conversions, we get a program that is shorter, easier to read and debug, and more reliable.

It is also easier to add features later. For example, imagine subtracting two MyTime objects to find the duration between them. The naive approach would be to implement subtraction with borrowing. Using the conversion functions would be easier and more likely to be correct.

Ironically, sometimes making a problem harder (or more general) makes the programming easier, because there are fewer special cases and fewer opportunities for error.

Specialization versus Generalization

Computer Scientists are generally fond of specializing their types, while mathematicians often take the opposite approach, and generalize everything.

What do we mean by this?

If you ask a mathematician to solve a problem involving weekdays, days of the century, playing cards, time, or dominoes, their most likely response is to observe that all these objects can be represented by integers. Playing cards, for example, can be numbered from 0 to 51. Days within the century can be numbered. Mathematicians will say "These things are enumerable — the elements can be uniquely numbered (and we can reverse this numbering to get back to the original concept). So let's number them, and confine our thinking to integers. Luckily, we have powerful techniques and a good understanding of integers, and so our abstractions — the way we tackle and simplify these problems — is to try to reduce them to problems about integers."

Computer Scientists tend to do the opposite. We will argue that there are many integer operations that are simply not meaningful for dominoes, or for days of the century. So we'll often define new specialized types, like MyTime, because we can restrict, control, and specialize the operations that are possible.

Object-oriented programming is particularly popular because it gives us a good way to bundle methods and specialized data into a new type.

Both approaches are powerful problem-solving techniques. Often it may help to try to think about the problem from both points of view — "What would happen if I tried to reduce everything to very few primitive types?", versus "What would happen if this thing had its own specialized type?"

21.7. Another example

The after function should compare two times, and tell us whether the first time is strictly after the second, e.g.

```
>>> t1 = MyTime(10, 55, 12)
>>> t2 = MyTime(10, 48, 22)
>>> after(t1, t2) # is t1 after t2?
True
```

This is slightly more complicated because it operates on two MyTime objects, not just one. But we'd prefer to write it as a method anyway — in this case, a method on the first argument:

```
1
     class MyTime:
2
         #previous method definitions here...
3
4
         def after(self, time2):
             """ Return True if I am strictly greater than time2 """
5
6
             if self.hours > time2.hours:
7
                 return True
8
             if self.hours < time2.hours:</pre>
9
                 return False
10
11
             if self.minutes > time2.minutes:
12
                 return True
13
             if self.minutes < time2.minutes:</pre>
14
                 return False
15
             if self.seconds > time2.seconds:
16
                 return True
17
18
             return False
```

We invoke this method on one object and pass the other as an argument:

```
if current_time.after(done_time):
   print("The bread will be done before it starts!")
```

You can almost read the invocation like English: If the current time is after the done time, then...

The logic of the if statements deserve special attention here. Lines 11–18 will only be reached if the two hour fields are the same. Similarly, the test at line 16 is only executed if both times have the same hours and the same minutes.

Could we make this easier by using our "Aha!" insight and extra work from earlier, and reducing both times to integers? Yes, with spectacular results!

```
1 class MyTime:
```

```
#previous method definitions here...

def after(self, time2):
    """ Return True if I am strictly greater than time2 """
    return self.to_seconds() > time2.to_seconds()
```

This is a great way to code this: if you want to tell if the first time is after the second time, turn them both into integers and compare the integers.

21.8. Operator overloading

Some languages, including Python, make it possible to have different meanings for the same operator when applied to different types. For example, $\frac{1}{2}$ in Python means quite different things for integers and for strings. This feature is called operator overloading.

It is especially useful when programmers can also overload the operators for their own user-defined types.

For example, to override the addition operator +, we can provide a method named __add__:

```
class MyTime:
    # previously defined methods here...

def __add__(self, other):
    return MyTime(0, 0, self.to_seconds() + other.to_seconds())
```

As usual, the first parameter is the object on which the method is invoked. The second parameter is conveniently named other to distinguish it from self. To add two MyTime objects, we create and return a new MyTime object that contains their sum.

Now, when we apply the + operator to MyTime objects, Python invokes the __add__ method that we have written:

```
>>> t1 = MyTime(1, 15, 42)
>>> t2 = MyTime(3, 50, 30)
>>> t3 = t1 + t2
>>> print(t3)
05:06:12
```

The expression t1 + t2 is equivalent to $t1._add_(t2)$, but obviously more elegant. As an exercise, add a method $_sub_(self, other)$ that overloads the subtraction operator, and try it out.

For the next couple of exercises we'll go back to the Point class defined in our first chapter about objects, and overload some of its operators. Firstly, adding two points adds their respective (x, y) coordinates:

```
class Point:
    # previously defined methods here...

def __add__(self, other):
    return Point(self.x + other.x, self.y + other.y)
```

There are several ways to override the behavior of the multiplication operator: by defining a method

```
named __mul__, or __rmul__, or both.
```

If the left operand of * is a Point, Python invokes __mul__, which assumes that the other operand is also a Point. It computes the dot product of the two Points, defined according to the rules of linear algebra:

```
def __mul__(self, other):
    return self.x * other.x + self.y * other.y
```

If the left operand of * is a primitive type and the right operand is a Point, Python invokes __rmul__, which performs scalar multiplication:

```
def __rmul__(self, other):
    return Point(other * self.x, other * self.y)
```

The result is a new <u>Point</u> whose coordinates are a multiple of the original coordinates. If <u>other</u> is a type that cannot be multiplied by a floating-point number, then <u>__rmul__</u> will yield an error.

This example demonstrates both kinds of multiplication:

```
>>> p1 = Point(3, 4)
>>> p2 = Point(5, 7)
>>> print(p1 * p2)
43
>>> print(2 * p2)
(10, 14)
```

What happens if we try to evaluate p2 * 2? Since the first parameter is a Point, Python invokes __mul__ with 2 as the second argument. Inside __mul__, the program tries to access the x coordinate of other, which fails because an integer has no attributes:

```
>>> print(p2 * 2)
AttributeError: 'int' object has no attribute 'x'
```

Unfortunately, the error message is a bit opaque. This example demonstrates some of the difficulties of object-oriented programming. Sometimes it is hard enough just to figure out what code is running.

21.9. Polymorphism

Most of the methods we have written only work for a specific type. When you create a new object, you write methods that operate on that type.

But there are certain operations that you will want to apply to many types, such as the arithmetic operations in the previous sections. If many types support the same set of operations, you can write functions that work on any of those types.

For example, the multadd operation (which is common in linear algebra) takes three parameters; it multiplies the first two and then adds the third. We can write it in Python like this:

```
def multadd (x, y, z):
```

```
return x * y + z
```

This function will work for any values of x and y that can be multiplied and for any value of z that can be added to the product.

We can invoke it with numeric values:

```
>>> multadd (3, 2, 1)
7
```

Or with Points:

```
>>> p1 = Point(3, 4)
>>> p2 = Point(5, 7)
>>> print(multadd (2, p1, p2))
(11, 15)
>>> print(multadd (p1, p2, 1))
44
```

In the first case, the <u>Point</u> is multiplied by a scalar and then added to another <u>Point</u>. In the second case, the dot product yields a numeric value, so the third parameter also has to be a numeric value.

A function like this that can take arguments with different types is called polymorphic.

As another example, consider the function ``front_and_back``, which prints a list twice, forward and backward:

```
def front_and_back(front):
    import copy

back = copy.copy(front)
back.reverse()
print(str(front) + str(back))
```

Because the <u>reverse</u> method is a modifier, we make a copy of the list before reversing it. That way, this function doesn't modify the list it gets as a parameter.

Here's an example that applies front_and_back to a list:

```
>>> myList = [1, 2, 3, 4]
>>> front_and_back(myList)
[1, 2, 3, 4][4, 3, 2, 1]
```

Of course, we intended to apply this function to lists, so it is not surprising that it works. What would be surprising is if we could apply it to a Point.

To determine whether a function can be applied to a new type, we apply Python's fundamental rule of polymorphism, called the duck typing rule: *If all of the operations inside the function can be applied to the type, the function can be applied to the type.* The operations in the front_and_back function include copy, reverse, and print.

Not all programming languages define polymorphism in this way. Look up *duck typing*, and see if you can figure out why it has this name.

copy works on any object, and we have already written a __str__ method for Point objects, so all we

need is a reverse method in the Point class:

```
def reverse(self):
    (self.x , self.y) = (self.y, self.x)
```

Then we can pass Points to front and back:

```
>>> p = Point(3, 4)
>>> front_and_back(p)
(3, 4)(4, 3)
```

The most interesting polymorphism is the unintentional kind, where you discover that a function you have already written can be applied to a type for which you never planned.

21.10. Glossary

dot product

An operation defined in linear algebra that multiplies two Points and yields a numeric value.

functional programming style

A style of program design in which the majority of functions are pure.

modifier

A function or method that changes one or more of the objects it receives as parameters. Most modifiers are void.

normalized

Data is said to be normalized if it fits into some reduced range or set of rules. We usually normalize our angles to values in the range [0..360). We normalize minutes and seconds to be values in the range [0..60). And we'd be surprised if the local store advertised its cold drinks at "One dollar, two hundred and fifty cents".

operator overloading

Extending built-in operators (\pm , -, *, >, <, etc.) so that they do different things for different types of arguments. We've seen early in the book how \pm is overloaded for numbers and strings, and here we've shown how to further overload it for user-defined types.

polymorphic

A function that can operate on more than one type. Notice the subtle distinction: overloading has different functions (all with the same name) for different types, whereas a polymorphic function is a single function that can work for a range of types.

pure function

A function that does not modify any of the objects it receives as parameters. Most pure functions are fruitful.

scalar multiplication

An operation defined in linear algebra that multiplies each of the coordinates of a Point by a numeric value.

21.11. Exercises

1. Write a boolean function between that takes two MyTime objects, t1 and t2, as arguments, and returns True if the invoking object falls between the two times. Assume t1 <= t2, and make the test closed at the lower bound and open at the upper bound, i.e. return True if

$$t1 \le obj < t2$$

- 2. Turn the above function into a method in the MyTime class.
- 3. Overload the necessary operator(s) so that instead of having to write

```
if t1.after(t2): ...
```

we can use the more convenient

```
if t1 > t2: ...
```

- 4. Rewrite increment as a method that uses our "Aha" insight.
- 5. Create some test cases for the <u>increment</u> method. Consider specifically the case where the number of seconds to add to the time is negative. Fix up <u>increment</u> so that it handles this case if it does not do so already. (You may assume that you will never subtract more seconds than are in the time object.)
- 6. Can physical time be negative, or must time always move in the forward direction? Some serious physicists think this is not such a dumb question. See what you can find on the Internet about this.

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22. Collections of objects

22.1. Composition

By now, you have seen several examples of composition. One of the first examples was using a method invocation as part of an expression. Another example is the nested structure of statements; you can put an if statement within a while loop, within another if statement, and so on.

Having seen this pattern, and having learned about lists and objects, you should not be surprised to learn that you can create lists of objects. You can also create objects that contain lists (as attributes); you can create lists that contain lists; you can create objects that contain objects; and so on.

In this chapter and the next, we will look at some examples of these combinations, using <u>Card</u> objects as an example.

22.2. Card objects

If you are not familiar with common playing cards, now would be a good time to get a deck, or else this chapter might not make much sense. There are fifty-two cards in a deck, each of which belongs to one of four suits and one of thirteen ranks. The suits are Spades, Hearts, Diamonds, and Clubs (in descending order in bridge). The ranks are Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, and King. Depending on the game that you are playing, the rank of Ace may be higher than King or lower than 2. The rank is sometimes called the face-value of the card.

If we want to define a new object to represent a playing card, it is obvious what the attributes should be: rank and suit. It is not as obvious what type the attributes should be. One possibility is to use strings containing words like "Spade" for suits and "Queen" for ranks. One problem with this implementation is that it would not be easy to compare cards to see which had a higher rank or suit.

An alternative is to use integers to encode the ranks and suits. By encode, we do not mean what some people think, which is to encrypt or translate into a secret code. What a computer scientist means by encode is to define a mapping between a sequence of numbers and the items I want to represent. For example:

```
      Spades
      --> 3

      Hearts
      --> 2

      Diamonds
      --> 1

      Clubs
      --> 0
```

An obvious feature of this mapping is that the suits map to integers in order, so we can compare suits by comparing integers. The mapping for ranks is fairly obvious; each of the numerical ranks maps to the corresponding integer, and for face cards:

```
Jack --> 11
Queen --> 12
King --> 13
```

The reason we are using mathematical notation for these mappings is that they are not part of the Python program. They are part of the program design, but they never appear explicitly in the code. The class definition for the Card type looks like this:

```
class Card:
    def __init__(self, suit=0, rank=0):
        self.suit = suit
        self.rank = rank
```

As usual, we provide an initialization method that takes an optional parameter for each attribute.

To create some objects, representing say the 3 of Clubs and the Jack of Diamonds, use these commands:

```
three_of_clubs = Card(0, 3)
card1 = Card(1, 11)
```

In the first case above, for example, the first argument, 0, represents the suit Clubs.

22.3. Class attributes and the str method

In order to print Card objects in a way that people can easily read, we want to map the integer codes onto words. A natural way to do that is with lists of strings. We assign these lists to class attributes at the top of the class definition:

```
1
   class Card:
      2
3
4
5
6
      def __init__(self, suit=0, rank=0):
7
          self.suit = suit
8
          self.rank = rank
9
      def __str__(self):
10
          return (self.ranks[self.rank] + " of " + self.suits[self.suit])
11
```

A class attribute is defined outside of any method, and it can be accessed from any of the methods in the class.

Inside __str__, we can use suits and ranks to map the numerical values of suit and rank to strings. For example, the expression self.suits[self.suit] means use the attribute suit from the object self as an index into the class attribute named suits, and select the appropriate string.

The reason for the "narf" in the first element in ranks is to act as a place keeper for the zero-eth element of the list, which will never be used. The only valid ranks are 1 to 13. This wasted item is not entirely necessary. We could have started at 0, as usual, but it is less confusing to encode the rank 2 as integer 2, 3 as 3, and so on.

With the methods we have so far, we can create and print cards:

```
>>> card1 = Card(1, 11)
>>> print(card1)
Jack of Diamonds
```

Class attributes like <u>suits</u> are shared by all <u>Card</u> objects. The advantage of this is that we can use any <u>Card</u> object to access the class attributes:

```
>>> card2 = Card(1, 3)
>>> print(card2)
3 of Diamonds
>>> print(card2.suits[1])
Diamonds
```

Because every <u>Card</u> instance references the same class attribute, we have an aliasing situation. The disadvantage is that if we modify a class attribute, it affects every instance of the class. For example, if we decide that Jack of Diamonds should really be called Jack of Swirly Whales, we could do this:

```
>>> card1.suits[1] = "Swirly Whales"
>>> print(card1)
Jack of Swirly Whales
```

The problem is that all of the Diamonds just became Swirly Whales:

```
>>> print(card2)
3 of Swirly Whales
```

It is usually not a good idea to modify class attributes.

22.4. Comparing cards

For primitive types, there are six relational operators (\langle , \rangle , ==, etc.) that compare values and determine when one is greater than, less than, or equal to another. If you want your own types to be comparable using the syntax of these relational operators, you need to define six corresponding special methods in your class.

We'd like to start with a single method named cmp that houses the logic of ordering. By convention, a comparison method takes two parameters, self and other, and returns 1 if the first object is greater, -1 if the second object is greater, and 0 if they are equal to each other.

Some types are completely ordered, which means that you can compare any two elements and tell which is bigger. For example, the integers and the floating-point numbers are completely ordered. Some types are unordered, which means that there is no meaningful way to say that one element is bigger than another. For example, the fruits are unordered, which is why you cannot compare apples and oranges, and you cannot meaningfully order a collection of images, or a collection of cellphones.

Playing cards are partially ordered, which means that sometimes you can compare cards and sometimes not. For example, you know that the 3 of Clubs is higher than the 2 of Clubs, and the 3 of Diamonds is higher than the 3 of Clubs. But which is better, the 3 of Clubs or the 2 of Diamonds? One has a higher rank, but the other has a higher suit.

In order to make cards comparable, you have to decide which is more important, rank or suit. To be honest, the choice is arbitrary. For the sake of choosing, we will say that suit is more important, because a new deck of cards comes sorted with all the Clubs together, followed by all the Diamonds, and so on.

With that decided, we can write cmp:

```
def cmp(self, other):
        # check the suits
3
        if self.suit > other.suit: return 1
4
        if self.suit < other.suit: return -1</pre>
5
        # suits are the same... check ranks
        if self.rank > other.rank: return 1
6
7
        if self.rank < other.rank: return -1</pre>
8
        # ranks are the same... it's a tie
9
        return 0
```

In this ordering, Aces appear lower than Deuces (2s).

Now, we can define the six special methods that do the overloading of each of the relational operators for us:

```
def __eq__(self, other):
1
2
         return self.cmp(other) == 0
3
4
     def __le__(self, other):
5
         return self.cmp(other) <= 0</pre>
6
7
     def __ge__(self, other):
8
         return self.cmp(other) >= 0
9
10
     def __gt__(self, other):
11
         return self.cmp(other) > 0
12
     def __lt__(self, other):
13
14
         return self.cmp(other) < 0</pre>
15
16
     def __ne__(self, other):
17
         return self.cmp(other) != 0
```

With this machinery in place, the relational operators now work as we'd like them to:

```
>>> card1 = Card(1, 11)
>>> card2 = Card(1, 3)
>>> card3 = Card(1, 11)
>>> card1 < card2
False
>>> card1 == card3
True
```

22.5. Decks

Now that we have objects to represent <u>Cards</u>, the next logical step is to define a class to represent a <u>Deck</u>. Of course, a deck is made up of cards, so each <u>Deck</u> object will contain a list of cards as an attribute. Many card games will need at least two different decks — a red deck and a blue deck.

The following is a class definition for the Deck class. The initialization method creates the attribute cards and generates the standard pack of fifty-two cards:

```
1 class Deck:
```

```
def __init__(self):
    self.cards = []
for suit in range(4):
    for rank in range(1, 14):
        self.cards.append(Card(suit, rank))
```

The easiest way to populate the deck is with a nested loop. The outer loop enumerates the suits from 0 to 3. The inner loop enumerates the ranks from 1 to 13. Since the outer loop iterates four times, and the inner loop iterates thirteen times, the total number of times the body is executed is fifty-two (thirteen times four). Each iteration creates a new instance of <u>Card</u> with the current suit and rank, and appends that card to the <u>cards</u> list.

With this in place, we can instantiate some decks:

```
redDeck = Deck()
blueDeck = Deck()
```

22.6. Printing the deck

As usual, when we define a new type we want a method that prints the contents of an instance. To print a Deck, we traverse the list and print each Card:

Here, and from now on, the ellipsis (...) indicates that we have omitted the other methods in the class.

As an alternative to print_deck, we could write a __str_ is that it is more flexible. Rather than just printing the contents of the object, it generates a string representation that other parts of the program can manipulate before printing, or store for later use.

Here is a version of <u>str</u> that returns a string representation of a <u>Deck</u>. To add a bit of pizzazz, it arranges the cards in a cascade where each card is indented one space more than the previous card:

```
class Deck:
    ...

def __str__(self):
    s = ""

for i in range(len(self.cards)):
    s = s + " " * i + str(self.cards[i]) + "\n"
    return s
```

This example demonstrates several features. First, instead of traversing self.cards and assigning each card to a variable, we are using i as a loop variable and an index into the list of cards.

Second, we are using the string multiplication operator to indent each card by one more space than

the last. The expression " " * i yields a number of spaces equal to the current value of i.

Third, instead of using the print command to print the cards, we use the str function. Passing an object as an argument to str is equivalent to invoking the __str_ method on the object.

Finally, we are using the variable s as an accumulator. Initially, s is the empty string. Each time through the loop, a new string is generated and concatenated with the old value of s to get the new value. When the loop ends, s contains the complete string representation of the Deck, which looks like this:

```
>>> redDeck = Deck()
>>> print(redDeck)
Ace of Clubs
 2 of Clubs
 3 of Clubs
  4 of Clubs
    5 of Clubs
      6 of Clubs
       7 of Clubs
        8 of Clubs
         9 of Clubs
          10 of Clubs
           Jack of Clubs
             Queen of Clubs
             King of Clubs
              Ace of Diamonds
               2 of Diamonds
```

And so on. Even though the result appears on 52 lines, it is one long string that contains newlines.

22.7. Shuffling the deck

If a deck is perfectly shuffled, then any card is equally likely to appear anywhere in the deck, and any location in the deck is equally likely to contain any card.

To shuffle the deck, we will use the randrange function from the random module. With two integer arguments, a and b, randrange chooses a random integer in the range a $\langle = x \rangle \langle b \rangle$. Since the upper bound is strictly less than b, we can use the length of a list as the second parameter, and we are guaranteed to get a legal index. For example, if rng has already been instantiated as a random number source, this expression chooses the index of a random card in a deck:

```
rng.randrange(0, len(self.cards))
```

An easy way to shuffle the deck is by traversing the cards and swapping each card with a randomly chosen one. It is possible that the card will be swapped with itself, but that is fine. In fact, if we precluded that possibility, the order of the cards would be less than entirely random:

```
class Deck:
    ...

def shuffle(self):
    import random
    rng = random.Random()  # create a random generator
    num_cards = len(self.cards)
    for i in range(num_cards):
```

```
j = rng.randrange(i, num_cards)
(self.cards[i], self.cards[j]) = (self.cards[j], self.cards[i])
```

Rather than assume that there are fifty-two cards in the deck, we get the actual length of the list and store it in num_cards.

For each card in the deck, we choose a random card from among the cards that haven't been shuffled yet. Then we swap the current card (\underline{i}) with the selected card (\underline{j}). To swap the cards we use a tuple assignment:

```
(self.cards[i], self.cards[j]) = (self.cards[j], self.cards[i])
```

While this is a good shuffling method, a random number generator object also has a shuffle method that can shuffle elements in a list, in place. So we could rewrite this function to use the one provided for us:

```
class Deck:
def shuffle(self):
    import random
rng = random.Random()  # create a random generator
rng.shuffle(self.cards)  # use its shuffle method
```

22.8. Removing and dealing cards

Another method that would be useful for the Deck class is remove, which takes a card as a parameter, removes it, and returns True if the card was in the deck and False otherwise:

```
class Deck:

def remove(self, card):

if card in self.cards:

self.cards.remove(card)

return True

else:

return False
```

The <u>in</u> operator returns True if the first operand is in the second. If the first operand is an object, Python uses the object's <u>eq</u> method to determine equality with items in the list. Since the <u>eq</u> we provided in the <u>Card</u> class checks for deep equality, the <u>remove</u> method checks for deep equality.

To deal cards, we want to remove and return the top card. The list method pop provides a convenient way to do that:

```
class Deck:
    def pop(self):
    return self.cards.pop()
```

Actually, pop removes the *last* card in the list, so we are in effect dealing from the bottom of the deck.

One more operation that we are likely to want is the boolean function <u>is_empty</u>, which returns True if the deck contains no cards:

```
class Deck:
def is_empty(self):
return len(self.cards) == 0
```

22.9. Glossary

encode

To represent one type of value using another type of value by constructing a mapping between them.

class attribute

A variable that is defined inside a class definition but outside any method. Class attributes are accessible from any method in the class and are shared by all instances of the class.

accumulator

A variable used in a loop to accumulate a series of values, such as by concatenating them onto a string or adding them to a running sum.

22.10. Exercises

1. Modify cmp so that Aces are ranked higher than Kings.

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23. Inheritance

23.1. Inheritance

The language feature most often associated with object-oriented programming is inheritance. Inheritance is the ability to define a new class that is a modified version of an existing class.

The primary advantage of this feature is that you can add new methods to a class without modifying the existing class. It is called inheritance because the new class inherits all of the methods of the existing class. Extending this metaphor, the existing class is sometimes called the parent class. The new class may be called the child class or sometimes subclass.

Inheritance is a powerful feature. Some programs that would be complicated without inheritance can be written concisely and simply with it. Also, inheritance can facilitate code reuse, since you can customize the behavior of parent classes without having to modify them. In some cases, the inheritance structure reflects the natural structure of the problem, which makes the program easier to understand.

On the other hand, inheritance can make programs difficult to read. When a method is invoked, it is sometimes not clear where to find its definition. The relevant code may be scattered among several modules. Also, many of the things that can be done using inheritance can be done as elegantly (or more so) without it. If the natural structure of the problem does not lend itself to inheritance, this style of programming can do more harm than good.

In this chapter we will demonstrate the use of inheritance as part of a program that plays the card game Old Maid. One of our goals is to write code that could be reused to implement other card games.

23.2. A hand of cards

For almost any card game, we need to represent a hand of cards. A hand is similar to a deck, of course. Both are made up of a set of cards, and both require operations like adding and removing cards. Also, we might like the ability to shuffle both decks and hands.

A hand is also different from a deck. Depending on the game being played, we might want to perform some operations on hands that don't make sense for a deck. For example, in poker we might classify a hand (straight, flush, etc.) or compare it with another hand. In bridge, we might want to compute a score for a hand in order to make a bid.

This situation suggests the use of inheritance. If Hand is a subclass of Deck, it will have all the methods of Deck, and new methods can be added.

In the class definition, the name of the parent class appears in parentheses:

```
class Hand(Deck):
```

This statement indicates that the new Hand class inherits from the existing Deck class.

The Hand constructor initializes the attributes for the hand, which are name and cards. The string name identifies this hand, probably by the name of the player that holds it. The name is an optional parameter with the empty string as a default value. cards is the list of cards in the hand, initialized to the empty list:

```
class Hand(Deck):
    def __init__(self, name=""):
        self.cards = []
        self.name = name
```

For just about any card game, it is necessary to add and remove cards from the deck. Removing cards is already taken care of, since Hand inherits remove from Deck. But we have to write add:

Again, the ellipsis indicates that we have omitted other methods. The list append method adds the new card to the end of the list of cards.

23.3. Dealing cards

Now that we have a Hand class, we want to deal cards from the Deck into hands. It is not immediately obvious whether this method should go in the Hand class or in the Deck class, but since it operates on a single deck and (possibly) several hands, it is more natural to put it in Deck.

deal should be fairly general, since different games will have different requirements. We may want to deal out the entire deck at once or add one card to each hand.

deal takes two parameters, a list (or tuple) of hands and the total number of cards to deal. If there are not enough cards in the deck, the method deals out all of the cards and stops:

```
1
    class Deck :
2
3
       def deal(self, hands, num_cards=999):
4
          num_hands = len(hands)
5
           for i in range(num_cards):
6
               if self.is_empty(): break # break if out of cards
7
               card = self.pop() # take the top card
8
               hand = hands[i % num_hands] # whose turn is next?
9
               hand.add(card)
                                          # add the card to the hand
```

The second parameter, num_cards, is optional; the default is a large number, which effectively means that all of the cards in the deck will get dealt.

The loop variable <u>i</u> goes from 0 to <u>num_cards-1</u>. Each time through the loop, a card is removed from the deck using the list method pop, which removes and returns the last item in the list.

The modulus operator (%) allows us to deal cards in a round robin (one card at a time to each hand). When i is equal to the number of hands in the list, the expression i % num_hands wraps around to the beginning of the list (index 0).

23.4. Printing a Hand

```
>>> deck = Deck()
>>> deck.shuffle()
>>> hand = Hand("frank")
>>> deck.deal([hand], 5)
>>> print(hand)
Hand frank contains
2 of Spades
3 of Spades
4 of Spades
Ace of Hearts
9 of Clubs
```

It's not a great hand, but it has the makings of a straight flush.

Although it is convenient to inherit the existing methods, there is additional information in a Hand object we might want to include when we print one. To do that, we can provide a __str__ method in the Hand class that overrides the one in the Deck class:

```
class Hand(Deck)

def __str__(self):
    s = "Hand " + self.name
    if self.is_empty():
        s = s + " is empty\n"
    else:
        s = s + " contains\n"
    return s + Deck.__str__(self)
```

Initially, \underline{s} is a string that identifies the hand. If the hand is empty, the program appends the words $\underline{i}\underline{s}$ empty and returns \underline{s} .

Otherwise, the program appends the word <u>contains</u> and the string representation of the <u>Deck</u>, computed by invoking the <u>__str__</u> method in the <u>Deck</u> class on <u>self</u>.

It may seem odd to send <u>self</u>, which refers to the current <u>Hand</u>, to a <u>Deck</u> method, until you remember that a <u>Hand</u> is a kind of <u>Deck</u>. <u>Hand</u> objects can do everything <u>Deck</u> objects can, so it is legal to send a <u>Hand</u> to a <u>Deck</u> method.

In general, it is always legal to use an instance of a subclass in place of an instance of a parent class.

23.5. The CardGame class

The CardGame class takes care of some basic chores common to all games, such as creating the deck and shuffling it:

```
class CardGame:
def __init__(self):
    self.deck = Deck()
    self.deck.shuffle()
```

This is the first case we have seen where the initialization method performs a significant computation, beyond initializing attributes.

To implement specific games, we can inherit from CardGame and add features for the new game. As an example, we'll write a simulation of Old Maid.

The object of Old Maid is to get rid of cards in your hand. You do this by matching cards by rank and color. For example, the 4 of Clubs matches the 4 of Spades since both suits are black. The Jack of Hearts matches the Jack of Diamonds since both are red.

To begin the game, the Queen of Clubs is removed from the deck so that the Queen of Spades has no match. The fifty-one remaining cards are dealt to the players in a round robin. After the deal, all players match and discard as many cards as possible.

When no more matches can be made, play begins. In turn, each player picks a card (without looking) from the closest neighbor to the left who still has cards. If the chosen card matches a card in the player's hand, the pair is removed. Otherwise, the card is added to the player's hand. Eventually all possible matches are made, leaving only the Queen of Spades in the loser's hand.

In our computer simulation of the game, the computer plays all hands. Unfortunately, some nuances of the real game are lost. In a real game, the player with the Old Maid goes to some effort to get their neighbor to pick that card, by displaying it a little more prominently, or perhaps failing to display it more prominently, or even failing to fail to display that card more prominently. The computer simply picks a neighbor's card at random.

23.6. OldMaidHand class

A hand for playing Old Maid requires some abilities beyond the general abilities of a Hand. We will define a new class, OldMaidHand, that inherits from Hand and provides an additional method called remove_matches:

```
class OldMaidHand(Hand):
1
2
      def remove matches(self):
3
            count = 0
            original_cards = self.cards[:]
4
5
            for card in original_cards:
6
                match = Card(3 - card.suit, card.rank)
7
                if match in self.cards:
8
                    self.cards.remove(card)
9
                    self.cards.remove(match)
10
                    print("Hand {0}: {1} matches {2}"
11
                            .format(self.name, card, match))
                    count = count + 1
12
13
            return count
```

We start by making a copy of the list of cards, so that we can traverse the copy while removing cards from the original. Since self.cards is modified in the loop, we don't want to use it to control the traversal. Python can get quite confused if it is traversing a list that is changing!

For each card in the hand, we figure out what the matching card is and go looking for it. The match card has the same rank and the other suit of the same color. The expression 3 - card.suit turns a Club (suit 0) into a Spade (suit 3) and a Diamond (suit 1) into a Heart (suit 2). You should satisfy yourself that the opposite operations also work. If the match card is also in the hand, both cards are removed.

The following example demonstrates how to use remove matches:

```
>>> game = CardGame()
>>> hand = OldMaidHand("frank")
>>> game.deck.deal([hand], 13)
>>> print(hand)
Hand frank contains
Ace of Spades
 2 of Diamonds
 7 of Spades
  8 of Clubs
   6 of Hearts
    8 of Spades
     7 of Clubs
      Queen of Clubs
       7 of Diamonds
        5 of Clubs
         Jack of Diamonds
          10 of Diamonds
           10 of Hearts
>>> hand.remove_matches()
Hand frank: 7 of Spades matches 7 of Clubs
Hand frank: 8 of Spades matches 8 of Clubs
Hand frank: 10 of Diamonds matches 10 of Hearts
>>> print(hand)
Hand frank contains
Ace of Spades
 2 of Diamonds
 6 of Hearts
   Oueen of Clubs
   7 of Diamonds
     5 of Clubs
     Jack of Diamonds
```

Notice that there is no <u>__init__</u> method for the <u>OldMaidHand</u> class. We inherit it from <u>Hand</u>.

23.7. OldMaidGame class

Now we can turn our attention to the game itself. OldMaidGame is a subclass of CardGame with a new method called play that takes a list of players as a parameter.

Since init is inherited from CardGame, a new OldMaidGame object contains a new shuffled deck:

```
1
    class OldMaidGame(CardGame):
2
     def play(self, names):
3
            # remove Queen of Clubs
4
            self.deck.remove(Card(0,12))
5
            # make a hand for each player
7
            self.hands = []
8
            for name in names:
9
                self.hands.append(OldMaidHand(name))
10
            # deal the cards
11
12
            self.deck.deal(self.hands)
```

```
print("----- Cards have been dealt")
13
14
            self.printHands()
15
            # remove initial matches
16
            matches = self.remove_all_matches()
17
18
            print("----- Matches discarded, play begins")
19
            self.printHands()
20
21
            # play until all 50 cards are matched
22
            turn = 0
23
            numHands = len(self.hands)
24
            while matches < 25:</pre>
25
                matches = matches + self.play_one_turn(turn)
26
                turn = (turn + 1) % numHands
27
28
            print("----- Game is Over")
29
            self.printHands()
```

The writing of printHands() is left as an exercise.

Some of the steps of the game have been separated into methods. remove_all_matches traverses the list of hands and invokes remove_matches on each:

```
class OldMaidGame(CardGame):

def remove_all_matches(self):
    count = 0
    for hand in self.hands:
        count = count + hand.remove_matches()
    return count
```

count is an accumulator that adds up the number of matches in each hand and returns the total.

When the total number of matches reaches twenty-five, fifty cards have been removed from the hands, which means that only one card is left and the game is over.

The variable turn keeps track of which player's turn it is. It starts at 0 and increases by one each time; when it reaches numHands, the modulus operator wraps it back around to 0.

The method playOneTurn takes a parameter that indicates whose turn it is. The return value is the number of matches made during this turn:

```
1
     class OldMaidGame(CardGame):
2
3
         def play_one_turn(self, i):
4
              if self.hands[i].is_empty():
5
                  return 0
              neighbor = self.find_neighbor(i)
6
7
              pickedCard = self.hands[neighbor].pop()
8
              self.hands[i].add(pickedCard)
              print("Hand", self.hands[i].name, "picked", pickedCard)
count = self.hands[i].remove_matches()
9
10
11
              self.hands[i].shuffle()
12
              return count
```

If a player's hand is empty, that player is out of the game, so he or she does nothing and returns 0.

Otherwise, a turn consists of finding the first player on the left that has cards, taking one card from the neighbor, and checking for matches. Before returning, the cards in the hand are shuffled so that the next player's choice is random.

The method <u>find_neighbor</u> starts with the player to the immediate left and continues around the circle until it finds a player that still has cards:

```
class OldMaidGame(CardGame):
    ...

def find_neighbor(self, i):
    numHands = len(self.hands)

for next in range(1,numHands):
    neighbor = (i + next) % numHands
    if not self.hands[neighbor].is_empty():
        return neighbor
```

If <u>find_neighbor</u> ever went all the way around the circle without finding cards, it would return None and cause an error elsewhere in the program. Fortunately, we can prove that that will never happen (as long as the end of the game is detected correctly).

We have omitted the print_hands method. You can write that one yourself.

The following output is from a truncated form of the game where only the top fifteen cards (tens and higher) were dealt to three players. With this small deck, play stops after seven matches instead of twenty-five.

```
>>> import cards
>>> game = cards.OldMaidGame()
>>> game.play(["Allen","Jeff","Chris"])
----- Cards have been dealt
Hand Allen contains
King of Hearts
Jack of Clubs
 Queen of Spades
  King of Spades
   10 of Diamonds
Hand Jeff contains
Queen of Hearts
 Jack of Spades
 Jack of Hearts
  King of Diamonds
   Queen of Diamonds
Hand Chris contains
Jack of Diamonds
King of Clubs
 10 of Spades
  10 of Hearts
   10 of Clubs
Hand Jeff: Queen of Hearts matches Queen of Diamonds
Hand Chris: 10 of Spades matches 10 of Clubs
----- Matches discarded, play begins
Hand Allen contains
King of Hearts
Jack of Clubs
 Queen of Spades
  King of Spades
   10 of Diamonds
```

```
Hand Jeff contains
Jack of Spades
Jack of Hearts
 King of Diamonds
Hand Chris contains
Jack of Diamonds
King of Clubs
 10 of Hearts
Hand Allen picked King of Diamonds
Hand Allen: King of Hearts matches King of Diamonds
Hand Jeff picked 10 of Hearts
Hand Chris picked Jack of Clubs
Hand Allen picked Jack of Hearts
Hand Jeff picked Jack of Diamonds
Hand Chris picked Queen of Spades
Hand Allen picked Jack of Diamonds
Hand Allen: Jack of Hearts matches Jack of Diamonds
Hand Jeff picked King of Clubs
Hand Chris picked King of Spades
Hand Allen picked 10 of Hearts
Hand Allen: 10 of Diamonds matches 10 of Hearts
Hand Jeff picked Queen of Spades
Hand Chris picked Jack of Spades
Hand Chris: Jack of Clubs matches Jack of Spades
Hand Jeff picked King of Spades
Hand Jeff: King of Clubs matches King of Spades
----- Game is Over
Hand Allen is empty
Hand Jeff contains
Queen of Spades
Hand Chris is empty
```

So Jeff loses.

23.8. Glossary

inheritance

The ability to define a new class that is a modified version of a previously defined class.

parent class

The class from which a child class inherits.

child class

A new class created by inheriting from an existing class; also called a subclass.

23.9. Exercises

- 1. Add a method, print_hands, to the OldMaidGame class which traverses self.hands and prints each hand.
- 2. Define a new kind of Turtle, TurtleGTX, that comes with some extra features: it can jump forward a given distance, and it has an odometer that keeps track of how far the turtle has travelled since it came off the production line. (The parent class has a number of synonyms like fd, forward, back, backward, and bk: for this exercise, just focus on putting this functionality on the forward method.) Think carefully about how to count the distance if the turtle is asked to move

- forward by a negative amount. (We would not want to buy a second-hand turtle whose odometer reading was faked because its previous owner drove it backwards around the block too often. Try this in a car near you, and see if the car's odometer counts up or down when you reverse.)
- 3. After travelling some random distance, your turtle should break down with a flat tyre. After this happens, raise an exception whenever <u>forward</u> is called. Also provide a <u>changeTyre</u> method that can fix the flat.

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24. Linked lists

24.1. Embedded references

We have seen examples of attributes that refer to other objects, which we called embedded references. A common data structure, the linked list, takes advantage of this feature.

Linked lists are made up of nodes, where each node contains a reference to the next node in the list. In addition, each node contains a unit of data called the cargo.

A linked list is considered a recursive data structure because it has a recursive definition.

A linked list is either:

- 1. the empty list, represented by None, or
- 2. a node that contains a cargo object and a reference to a linked list.

Recursive data structures lend themselves to recursive methods.

24.2. The Node class

As usual when writing a new class, we'll start with the initialization and str methods so that we can test the basic mechanism of creating and displaying the new type:

```
1
    class Node:
2
       def __init__(self, cargo=None, next=None):
3
            self.cargo = cargo
4
            self.next = next
5
        def __str__(self):
6
            return str(self.cargo)
```

As usual, the parameters for the initialization method are optional. By default, both the cargo and the link, next, are set to None.

The string representation of a node is just the string representation of the cargo. Since any value can be passed to the str function, we can store any value in a list.

To test the implementation so far, we can create a Node and print it:

```
>>> node = Node("test")
>>> print(node)
test
```

To make it interesting, we need a list with more than one node:

```
>>> node1 = Node(1)
>>> node2 = Node(2)
>>> node3 = Node(3)
```

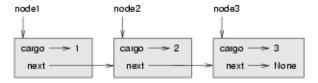
This code creates three nodes, but we don't have a list yet because the nodes are not linked. The state diagram looks like this:



To link the nodes, we have to make the first node refer to the second and the second node refer to the third:

```
>>> node1.next = node2
>>> node2.next = node3
```

The reference of the third node is None, which indicates that it is the end of the list. Now the state diagram looks like this:



Now you know how to create nodes and link them into lists. What might be less clear at this point is why.

24.3. Lists as collections

Lists are useful because they provide a way to assemble multiple objects into a single entity, sometimes called a collection. In the example, the first node of the list serves as a reference to the entire list.

To pass the list as a parameter, we only have to pass a reference to the first node. For example, the function print_list takes a single node as an argument. Starting with the head of the list, it prints each node until it gets to the end:

```
def print_list(node):
    while node != None:
        print(node, end=' ')
        node = node.next
    print()
```

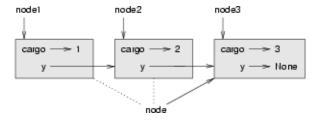
To invoke this method, we pass a reference to the first node:

```
>>> print_list(node1)
1 2 3
```

Inside print_list we have a reference to the first node of the list, but there is no variable that refers to the other nodes. We have to use the next value from each node to get to the next node.

To traverse a linked list, it is common to use a loop variable like <u>node</u> to refer to each of the nodes in succession.

This diagram shows the value of list and the values that node takes on:



24.4. Lists and recursion

It is natural to express many list operations using recursive methods. For example, the following is a recursive algorithm for printing a list backwards:

- 1. Separate the list into two pieces: the first node (called the head); and the rest (called the tail).
- 2. Print the tail backward.
- 3. Print the head.

Of course, Step 2, the recursive call, assumes that we have a way of printing a list backward. But if we assume that the recursive call works – the leap of faith – then we can convince ourselves that this algorithm works.

All we need are a base case and a way of proving that for any list, we will eventually get to the base case. Given the recursive definition of a list, a natural base case is the empty list, represented by None:

```
def print_backward(list):
    if list == None: return
    head = list
    tail = list.next
    print_backward(tail)
    print(head,end=' ')
```

The first line handles the base case by doing nothing. The next two lines split the list into head and tail. The last two lines print the list. The end argument of the print statement keeps Python from printing a newline after each node.

We invoke this method as we invoked print list:

```
>>> print_backward(node1)
3 2 1
```

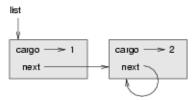
The result is a backward list.

You might wonder why print_list and print_backward are functions and not methods in the Node class. The reason is that we want to use None to represent the empty list and it is not legal to invoke a method on None. This limitation makes it awkward to write list - manipulating code in a clean object-oriented style.

Can we prove that print_backward will always terminate? In other words, will it always reach the base case? In fact, the answer is no. Some lists will make this method crash.

24.5. Infinite lists

There is nothing to prevent a node from referring back to an earlier node in the list, including itself. For example, this figure shows a list with two nodes, one of which refers to itself:



If we invoke print_list on this list, it will loop forever. If we invoke print_backward, it will recurse infinitely. This sort of behavior makes infinite lists difficult to work with.

Nevertheless, they are occasionally useful. For example, we might represent a number as a list of digits and use an infinite list to represent a repeating fraction.

Regardless, it is problematic that we cannot prove that print_list and print_backward terminate. The best we can do is the hypothetical statement, "If the list contains no loops, then these methods will terminate." This sort of claim is called a precondition. It imposes a constraint on one of the parameters and describes the behavior of the method if the constraint is satisfied. You will see more examples soon.

24.6. The fundamental ambiguity theorem

One part of print_backward might have raised an eyebrow:

```
head = list
tail = list.next
```

After the first assignment, head and list have the same type and the same value. So why did we create a new variable?

The reason is that the two variables play different roles. We think of <u>head</u> as a reference to a single node, and we think of <u>list</u> as a reference to the first node of a list. These roles are not part of the program; they are in the mind of the programmer.

In general we can't tell by looking at a program what role a variable plays. This ambiguity can be useful, but it can also make programs difficult to read. We often use variable names like node and list to document how we intend to use a variable and sometimes create additional variables to disambiguate.

We could have written print_backward without head and tail, which makes it more concise but possibly less clear:

```
def print_backward(list):
    if list == None : return
    print_backward(list.next)
    print(list,end=' ')
```

Looking at the two function calls, we have to remember that print_backward treats its argument as a collection and print treats its argument as a single object.

The fundamental ambiguity theorem describes the ambiguity that is inherent in a reference to a node:

A variable that refers to a node might treat the node as a single object or as the first in a list of nodes.

24.7. Modifying lists

There are two ways to modify a linked list. Obviously, we can change the cargo of one of the nodes, but the more interesting operations are the ones that add, remove, or reorder the nodes.

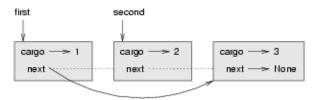
As an example, let's write a method that removes the second node in the list and returns a reference to the removed node:

```
1
    def removeSecond(list):
2
       if list == None: return
3
       first = list
4
       second = list.next
5
       # make the first node refer to the third
6
       first.next = second.next
7
        # separate the second node from the rest of the list
8
        second.next = None
9
        return second
```

Again, we are using temporary variables to make the code more readable. Here is how to use this method:

```
>>> print_list(node1)
1 2 3
>>> removed = removeSecond(node1)
>>> print_list(removed)
2
>>> print_list(node1)
1 3
```

This state diagram shows the effect of the operation:



What happens if you invoke this method and pass a list with only one element (a singleton)? What happens if you pass the empty list as an argument? Is there a precondition for this method? If so, fix the method to handle a violation of the precondition in a reasonable way.

24.8. Wrappers and helpers

It is often useful to divide a list operation into two methods. For example, to print a list backward in the conventional list format [3, 2, 1] we can use the print_backward method to print 3, 2, but we need a separate method to print the brackets and the first node. Let's call it print_backward_nicely:

```
def print_backward_nicely(list):
    print("[", end=' ')
    if list != None:
        head = list
        tail = list.next
        print_backward(tail)
```

```
print(head, end=' ')
print("]", end=' ')
```

Again, it is a good idea to check methods like this to see if they work with special cases like an empty list or a singleton.

When we use this method elsewhere in the program, we invoke print_backward_nicely directly, and it invokes print_backward_nicely acts as a wrapper, and it uses print_backward as a helper.

24.9. The LinkedList class

There are some subtle problems with the way we have been implementing lists. In a reversal of cause and effect, we'll propose an alternative implementation first and then explain what problems it solves.

First, we'll create a new class called <u>LinkedList</u>. Its attributes are an integer that contains the length of the list and a reference to the first node. <u>LinkedList</u> objects serve as handles for manipulating lists of Node objects:

```
class LinkedList:
def __init__(self):
self.length = 0
self.head = None
```

One nice thing about the <u>LinkedList</u> class is that it provides a natural place to put wrapper functions like <u>print_backward_nicely</u>, which we can make a method of the <u>LinkedList</u> class:

```
1
    class LinkedList:
2
3
        def print backward(self):
4
            print("[", end=' ')
5
            if self.head != None:
                self.head.print_backward()
6
7
            print("]", end=' ')
8
9
    class Node:
10
11
        def print_backward(self):
12
        if self.next != None:
            tail = self.next
13
            tail.print_backward()
14
15
        print(self.cargo, end='
```

Just to make things confusing, we renamed print_backward_nicely. Now there are two methods named print_backward one in the LinkedList class (the wrapper). When the wrapper invokes self.head.print_backward, it is invoking the helper, because self.head is a Node object.

Another benefit of the <u>LinkedList</u> class is that it makes it easier to add or remove the first element of a list. For example, addFirst is a method for <u>LinkedLists</u>; it takes an item of cargo as an argument and puts it at the beginning of the list:

```
class LinkedList:

def addFirst(self, cargo):
    node = Node(cargo)
    node.next = self.head
    self.head = node
    self.length = self.length + 1
```

As usual, you should check code like this to see if it handles the special cases. For example, what happens if the list is initially empty?

24.10. Invariants

Some lists are well formed; others are not. For example, if a list contains a loop, it will cause many of our methods to crash, so we might want to require that lists contain no loops. Another requirement is that the LinkedList object should be equal to the actual number of nodes in the list.

Requirements like these are called invariants because, ideally, they should be true of every object all the time. Specifying invariants for objects is a useful programming practice because it makes it easier to prove the correctness of code, check the integrity of data structures, and detect errors.

One thing that is sometimes confusing about invariants is that there are times when they are violated. For example, in the middle of addFirst, after we have added the node but before we have incremented length, the invariant is violated. This kind of violation is acceptable; in fact, it is often impossible to modify an object without violating an invariant for at least a little while. Normally, we require that every method that violates an invariant must restore the invariant.

If there is any significant stretch of code in which the invariant is violated, it is important for the comments to make that clear, so that no operations are performed that depend on the invariant.

24.11. Glossary

embedded reference

A reference stored in an attribute of an object.

linked list

A data structure that implements a collection using a sequence of linked nodes.

node

An element of a list, usually implemented as an object that contains a reference to another object of the same type.

cargo

An item of data contained in a node.

link

An embedded reference used to link one object to another.

precondition

An assertion that must be true in order for a method to work correctly.

fundamental ambiguity theorem

A reference to a list node can be treated as a single object or as the first in a list of nodes.

singleton

A linked list with a single node.

wrapper

A method that acts as a middleman between a caller and a helper method, often making the method easier or less error-prone to invoke.

helper

A method that is not invoked directly by a caller but is used by another method to perform part of an operation.

invariant

An assertion that should be true of an object at all times (except perhaps while the object is being modified).

24.12. Exercises

1. By convention, lists are often printed in brackets with commas between the elements, as in [1, 2, 3]. Modify print_list so that it generates output in this format.

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25. Stacks

25.1. Abstract data types

The data types you have seen so far are all concrete, in the sense that we have completely specified how they are implemented. For example, the Card class represents a card using two integers. As we discussed at the time, that is not the only way to represent a card; there are many alternative implementations.

An abstract data type, or ADT, specifies a set of operations (or methods) and the semantics of the operations (what they do), but it does not not specify the implementation of the operations. That's what makes it abstract.

Why is that useful?

- 1. It simplifies the task of specifying an algorithm if you can denote the operations you need without having to think at the same time about how the operations are performed.
- 2. Since there are usually many ways to implement an ADT, it might be useful to write an algorithm that can be used with any of the possible implementations.
- 3. Well-known ADTs, such as the Stack ADT in this chapter, are often implemented in standard libraries so they can be written once and used by many programmers.
- 4. The operations on ADTs provide a common high-level language for specifying and talking about algorithms.

When we talk about ADTs, we often distinguish the code that uses the ADT, called the client code, from the code that implements the ADT, called the provider code.

25.2. The Stack ADT

In this chapter, we will look at one common ADT, the stack. A stack is a collection, meaning that it is a data structure that contains multiple elements. Other collections we have seen include dictionaries and lists.

An ADT is defined by the operations that can be performed on it, which is called an interface. The interface for a stack consists of these operations:

__init__

Initialize a new empty stack.

push

Add a new item to the stack.

pop

Remove and return an item from the stack. The item that is returned is always the last one that was added.

is_empty

Check whether the stack is empty.

A stack is sometimes called a last in, first out or LIFO data structure, because the last item added is the first to be removed.

25.3. Implementing stacks with Python lists

The list operations that Python provides are similar to the operations that define a stack. The interface isn't exactly what it is supposed to be, but we can write code to translate from the Stack ADT to the built-in operations.

This code is called an implementation of the Stack ADT. In general, an implementation is a set of methods that satisfy the syntactic and semantic requirements of an interface.

Here is an implementation of the Stack ADT that uses a Python list:

```
1
    class Stack:
2
        def __init__(self):
3
            self.items = []
4
5
        def push(self, item):
6
            self.items.append(item)
7
8
        def pop(self):
9
            return self.items.pop()
10
11
        def is empty(self):
            return (self.items == [])
12
```

A Stack object contains an attribute named items that is a list of items in the stack. The initialization method sets items to the empty list.

To push a new item onto the stack, <u>push</u> appends it onto <u>items</u>. To pop an item off the stack, <u>pop</u> uses the homonymous (<u>same-named</u>) list method to remove and return the last item on the list.

Finally, to check if the stack is empty, is empty compares items to the empty list.

An implementation like this, in which the methods consist of simple invocations of existing methods, is called a veneer. In real life, veneer is a thin coating of good quality wood used in furniture-making to hide lower quality wood underneath. Computer scientists use this metaphor to describe a small piece of code that hides the details of an implementation and provides a simpler, or more standard, interface.

25.4. Pushing and popping

A stack is a generic data structure, which means that we can add any type of item to it. The following example pushes two integers and a string onto the stack:

```
>>> s = Stack()
>>> s.push(54)
>>> s.push(45)
>>> s.push("+")
```

We can use is empty and pop to remove and print all of the items on the stack:

```
while not s.is_empty():
    print(s.pop(), end=' ')
```

The output is + 45 54. In other words, we just used a stack to print the items backward! Granted, it's not the standard format for printing a list, but by using a stack, it was remarkably easy to do.

You should compare this bit of code to the implementation of print_backward in the last chapter. There is a natural parallel between the recursive version of print_backward and the stack algorithm here. The difference is that print_backward uses the runtime stack to keep track of the nodes while it traverses the list, and then prints them on the way back from the recursion. The stack algorithm does the same thing, except that is use a Stack object instead of the runtime stack.

25.5. Using a stack to evaluate postfix

In most programming languages, mathematical expressions are written with the operator between the two operands, as in $\frac{1}{2}$. This format is called infix. An alternative used by some calculators is called postfix. In postfix, the operator follows the operands, as in $\frac{1}{2}$.

The reason postfix is sometimes useful is that there is a natural way to evaluate a postfix expression using a stack:

- 1. Starting at the beginning of the expression, get one term (operator or operand) at a time.
 - If the term is an operand, push it on the stack.
 - If the term is an operator, pop two operands off the stack, perform the operation on them, and push the result back on the stack.
- 2. When you get to the end of the expression, there should be exactly one operand left on the stack. That operand is the result.

25.6. Parsing

To implement the previous algorithm, we need to be able to traverse a string and break it into operands and operators. This process is an example of parsing, and the results—the individual chunks of the string – are called tokens. You might remember these words from Chapter 1.

Python provides a <u>split</u> method in both string objects and the <u>re</u> (regular expression) module. A string's <u>split</u> method splits it into a list using a single character as a delimiter. For example:

```
>>> import string
>>> "Now is the time".split(" ")
['Now', 'is', 'the', 'time']
```

In this case, the delimiter is the space character, so the string is split at each space.

The function re.split is more powerful, allowing us to provide a regular expression instead of a delimiter. A regular expression is a way of specifying a set of strings. For example, [A-z] is the set of all letters and [0-9] is the set of all numbers. The operator negates a set, so [0-9] is the set of everything that is not a number, which is exactly the set we want to use to split up postfix expressions:

```
>>> import re
>>> re.split("([^0-9])", "123+456*/")
['123', '+', '456', '*', '', '']
```

The resulting list includes the operands 123 and 456 and the operators * and /. It also includes two empty strings that are inserted after the operands.

25.7. Evaluating postfix

To evaluate a postfix expression, we will use the parser from the previous section and the algorithm from the section before that. To keep things simple, we'll start with an evaluator that only implements the operators + and *:

```
def eval_postfix(expr):
2
         import re
3
         token list = re.split("(\lceil ^0-9 \rceil)", expr)
4
         stack = Stack()
5
         for token in token list:
             if token == '' or token == ' ':
6
7
                 continue
             if token == '+':
8
9
                 sum = stack.pop() + stack.pop()
10
                 stack.push(sum)
11
             elif token == '*':
12
                 product = stack.pop() * stack.pop()
13
                 stack.push(product)
14
15
                 stack.push(int(token))
16
         return stack.pop()
```

The first condition takes care of spaces and empty strings. The next two conditions handle operators. We assume, for now, that anything else must be an operand. Of course, it would be better to check for erroneous input and report an error message, but we'll get to that later.

Let's test it by evaluating the postfix form of (56+47)*2:

```
>>> print(eval_postfix ("56 47 + 2 *"))
206
```

That's close enough.

25.8. Clients and providers

One of the fundamental goals of an ADT is to separate the interests of the provider, who writes the code that implements the ADT, and the client, who uses the ADT. The provider only has to worry about whether the implementation is correct – in accord with the specification of the ADT – and not how it will be used.

Conversely, the client *assumes* that the implementation of the ADT is correct and doesn't worry about the details. When you are using one of Python's built-in types, you have the luxury of thinking exclusively as a client.

Of course, when you implement an ADT, you also have to write client code to test it. In that case, you play both roles, which can be confusing. You should make some effort to keep track of which role you are playing at any moment.

25.9. Glossary

abstract data type (ADT)

A data type (usually a collection of objects) that is defined by a set of operations but that can be implemented in a variety of ways.

client

A program (or the person who wrote it) that uses an ADT.

delimiter

A character that is used to separate tokens, such as punctuation in a natural language.

generic data structure

A kind of data structure that can contain data of any type.

implementation

Code that satisfies the syntactic and semantic requirements of an interface.

interface

The set of operations that define an ADT.

infix

A way of writing mathematical expressions with the operators between the operands.

parse

To read a string of characters or tokens and analyze its grammatical structure.

postfix

A way of writing mathematical expressions with the operators after the operands.

provider

The code (or the person who wrote it) that implements an ADT.

token

A set of characters that are treated as a unit for purposes of parsing, such as the words in a natural language.

veneer

A class definition that implements an ADT with method definitions that are invocations of other methods, sometimes with simple transformations. The veneer does no significant work, but it improves or standardizes the interface seen by the client.

25.10. Exercises

- 1. Apply the postfix algorithm to the expression $\frac{1}{2} + \frac{3}{3}$. This example demonstrates one of the advantages of postfix—there is no need to use parentheses to control the order of operations. To get the same result in infix, we would have to write (1 + 2) * 3.
- 2. Write a postfix expression that is equivalent to 1 + 2 * 3.

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26. Queues

This chapter presents two ADTs: the Queue and the Priority Queue. In real life, a queue is a line of customers waiting for service of some kind. In most cases, the first customer in line is the next customer to be served. There are exceptions, though. At airports, customers whose flights are leaving soon are sometimes taken from the middle of the queue. At supermarkets, a polite customer might let someone with only a few items go first.

The rule that determines who goes next is called the queueing policy. The simplest queueing policy is called FIFO, for first- in-first-out. The most general queueing policy is priority queueing, in which each customer is assigned a priority and the customer with the highest priority goes first, regardless of the order of arrival. We say this is the most general policy because the priority can be based on anything: what time a flight leaves; how many groceries the customer has; or how important the customer is. Of course, not all queueing policies are fair, but fairness is in the eye of the beholder.

The Queue ADT and the Priority Queue ADT have the same set of operations. The difference is in the semantics of the operations: a queue uses the FIFO policy; and a priority queue (as the name suggests) uses the priority queueing policy.

26.1. The Queue ADT

The Queue ADT is defined by the following operations:

__init__

Initialize a new empty queue.

insert

Add a new item to the queue.

remove

Remove and return an item from the queue. The item that is returned is the first one that was added.

is_empty

Check whether the queue is empty.

26.2. Linked Queue

The first implementation of the Queue ADT we will look at is called a linked queue because it is made up of linked Node objects. Here is the class definition:

```
1
    class Queue:
2
     def __init__(self):
3
           self.length = 0
4
           self.head = None
5
       def is_empty(self):
```

```
return (self.length == 0)
8
9
        def insert(self, cargo):
10
          node = Node(cargo)
11
            node.next = None
12
           if self.head == None:
13
               # if list is empty the new node goes first
               self.head = node
15
16
               # find the last node in the list
17
               last = self.head
               while last.next: last = last.next
18
19
               # append the new node
20
                last.next = node
21
            self.length = self.length + 1
22
23
        def remove(self):
24
           cargo = self.head.cargo
25
            self.head = self.head.next
26
            self.length = self.length - 1
27
            return cargo
```

The methods is_empty and remove are identical to the LinkedList methods is_empty and remove_first. The insert method is new and a bit more complicated.

We want to insert new items at the end of the list. If the queue is empty, we just set head to refer to the new node.

Otherwise, we traverse the list to the last node and tack the new node on the end. We can identify the last node because its next attribute is None.

There are two invariants for a properly formed <u>Queue</u> object. The value of <u>length</u> should be the number of nodes in the queue, and the last node should have <u>next</u> equal to <u>None</u>. Convince yourself that this method preserves both invariants.

26.3. Performance characteristics

Normally when we invoke a method, we are not concerned with the details of its implementation. But there is one detail we might want to know—the performance characteristics of the method. How long does it take, and how does the run time change as the number of items in the collection increases?

First look at <u>remove</u>. There are no loops or function calls here, suggesting that the runtime of this method is the same every time. Such a method is called a constant-time operation. In reality, the method might be slightly faster when the list is empty since it skips the body of the conditional, but that difference is not significant.

The performance of <u>insert</u> is very different. In the general case, we have to traverse the list to find the last element.

This traversal takes time proportional to the length of the list. Since the runtime is a linear function of the length, this method is called linear time. Compared to constant time, that's very bad.

26.4. Improved Linked Queue

We would like an implementation of the Queue ADT that can perform all operations in constant time. One way to do that is to modify the Queue class so that it maintains a reference to both the first and the last node, as shown in the figure:

The ImprovedQueue implementation looks like this:

```
class ImprovedQueue:

def __init__(self):
    self.length = 0
    self.head = None
    self.last = None

def is_empty(self):
    return (self.length == 0)
```

So far, the only change is the attribute <u>last</u>. It is used in <u>insert</u> and <u>remove</u> methods:

```
1
    class ImprovedQueue:
2
3
        def insert(self, cargo):
4
            node = Node(cargo)
5
            node.next = None
6
            if self.length == 0:
7
                # if list is empty, the new node is head and last
8
                self.head = self.last = node
9
            else:
                # find the last node
10
11
                last = self.last
12
                # append the new node
13
                last.next = node
14
                self.last = node
15
            self.length = self.length + 1
```

Since <u>last</u> keeps track of the last node, we don't have to search for it. As a result, this method is constant time.

There is a price to pay for that speed. We have to add a special case to remove to set last to None when the last node is removed:

```
class ImprovedQueue:
1
2
3
        def remove(self):
           cargo = self.head.cargo
4
5
           self.head = self.head.next
            self.length = self.length - 1
6
7
            if self.length == 0:
8
                self.last = None
9
            return cargo
```

This implementation is more complicated than the Linked Queue implementation, and it is more difficult to demonstrate that it is correct. The advantage is that we have achieved the goal – both insert and remove are constant-time operations.

26.5. Priority queue

The Priority Queue ADT has the same interface as the Queue ADT, but different semantics. Again, the interface is:

init

Initialize a new empty queue.

insert

Add a new item to the queue.

remove

Remove and return an item from the queue. The item that is returned is the one with the highest priority.

is empty

Check whether the queue is empty.

The semantic difference is that the item that is removed from the queue is not necessarily the first one that was added. Rather, it is the item in the queue that has the highest priority. What the priorities are and how they compare to each other are not specified by the Priority Queue implementation. It depends on which items are in the queue.

For example, if the items in the queue have names, we might choose them in alphabetical order. If they are bowling scores, we might go from highest to lowest, but if they are golf scores, we would go from lowest to highest. As long as we can compare the items in the queue, we can find and remove the one with the highest priority.

This implementation of Priority Queue has as an attribute a Python list that contains the items in the queue.

```
class PriorityQueue:
    def __init__(self):
        self.items = []

def is_empty(self):
    return self.items == []

def insert(self, item):
    self.items.append(item)
```

The initialization method, is_empty, and insert are all veneers on list operations. The only interesting method is remove:

```
1
    class PriorityQueue:
2
3
        def remove(self):
4
           maxi = 0
5
           for i in range(1, len(self.items)):
6
               if self.items[i] > self.items[maxi]: maxi = i
7
            item = self.items[maxi]
8
            self.items[maxi:maxi+1] = []
9
            return item
```

At the beginning of each iteration, maxi holds the index of the biggest item (highest priority) we have seen so far. Each time through the loop, the program compares the i-eth item to the champion. If the new item is bigger, the value of maxi if set to i.

When the for statement completes, maxi is the index of the biggest item. This item is removed from the list and returned.

Let's test the implementation:

```
>>> q = PriorityQueue()
>>> q.insert(11)
>>> q.insert(12)
>>> q.insert(14)
>>> q.insert(13)
>>> while not q.is_empty(): print(q.remove())
14
13
12
11
```

If the queue contains simple numbers or strings, they are removed in numerical or alphabetical order, from highest to lowest. Python can find the biggest integer or string because it can compare them using the built-in comparison operators.

If the queue contains an object type, it has to provide a <u>__gt__</u> method. When <u>remove</u> uses the <u>></u> operator to compare items, it invokes the <u>__gt__</u> for one of the items and passes the other as a parameter. As long as the <u>__gt__</u> method works correctly, the Priority Queue will work.

26.6. The Golfer class

As an example of an object with an unusual definition of priority, let's implement a class called Golfer that keeps track of the names and scores of golfers. As usual, we start by defining __init__ and __str__:

```
class Golfer:
    def __init__(self, name, score):
        self.name = name
        self.score= score

def __str__(self):
    return "{0:16}: {1}".format(self.name, self.score)
```

__str__ uses the format method to put the names and scores in neat columns.

Next we define a version of <u>_gt_</u> where the lowest score gets highest priority. As always, <u>_gt_</u> returns True if self is greater than other, and False otherwise.

```
class Golfer:
    def __gt__(self, other):
        return self.score < other.score # less is more</pre>
```

Now we are ready to test the priority queue with the Golfer class:

```
>>> tiger = Golfer("Tiger Woods", 61)
>>> phil = Golfer("Phil Mickelson", 72)
>>> hal = Golfer("Hal Sutton", 69)
>>>
```

```
>>> pq = PriorityQueue()
>>> pq.insert(tiger)
>>> pq.insert(phil)
>>> pq.insert(hal)
>>> while not pq.is_empty(): print(pq.remove())
   Tiger Woods : 61
   Hal Sutton : 69
   Phil Mickelson : 72
```

26.7. Glossary

constant time

An operation whose runtime does not depend on the size of the data structure.

FIFO

First In, First Out, a queueing policy in which the first member to arrive is the first to be removed.

linear time

An operation whose runtime is a linear function of the size of the data structure.

linked queue

An implementation of a queue using a linked list.

priority queue

A queueing policy in which each member has a priority determined by external factors. The member with the highest priority is the first to be removed.

Priority Queue

An ADT that defines the operations one might perform on a priority queue.

queue

An ordered set of objects waiting for a service of some kind.

Queue

An ADT that performs the operations one might perform on a queue.

queueing policy

The rules that determine which member of a queue is removed next.

26.8. Exercises

- 1. Write an implementation of the Queue ADT using a Python list. Compare the performance of this implementation to the ImprovedQueue for a range of queue lengths.
- 2. Write an implementation of the Priority Queue ADT using a linked list. You should keep the list sorted so that removal is a constant time operation. Compare the performance of this implementation with the Python list implementation.

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27. Trees

Like linked lists, trees are made up of nodes. A common kind of tree is a binary tree, in which each node contains a reference to two other nodes (possibly None). These references are referred to as the left and right subtrees. Like list nodes, tree nodes also contain cargo. A state diagram for a tree looks like this:

To avoid cluttering up the picture, we often omit the Nones.

The top of the tree (the node tree refers to) is called the root. In keeping with the tree metaphor, the other nodes are called branches and the nodes at the tips with null references are called leaves. It may seem odd that we draw the picture with the root at the top and the leaves at the bottom, but that is not the strangest thing.

To make things worse, computer scientists mix in another metaphor - the family tree. The top node is sometimes called a parent and the nodes it refers to are its children. Nodes with the same parent are called siblings.

Finally, there is a geometric vocabulary for talking about trees. We already mentioned left and right, but there is also up (toward the parent/root) and down (toward the children/leaves). Also, all of the nodes that are the same distance from the root comprise a level of the tree.

We probably don't need three metaphors for talking about trees, but there they are.

Like linked lists, trees are recursive data structures because they are defined recursively. A tree is either:

- 1. the empty tree, represented by None, or
- 2. a node that contains an object reference (cargo) and two tree references.

27.1. Building trees

The process of assembling a tree is similar to the process of assembling a linked list. Each constructor invocation builds a single node.

```
class Tree:
1
2
       def __init__(self, cargo, left=None, right=None):
3
           self.cargo = cargo
4
           self.left = left
           self.right = right
7
        def __str__(self):
           return str(self.cargo)
```

The cargo can be any type, but the left and right parameters should be tree nodes. left and right are optional; the default value is None.

To print a node, we just print the cargo.

One way to build a tree is from the bottom up. Allocate the child nodes first:

```
1 left = Tree(2)
2 right = Tree(3)
```

Then create the parent node and link it to the children:

```
tree = Tree(1, left, right)
```

We can write this code more concisely by nesting constructor invocations:

```
>>> tree = Tree(1, Tree(2), Tree(3))
```

Either way, the result is the tree at the beginning of the chapter.

27.2. Traversing trees

Any time you see a new data structure, your first question should be, How do I traverse it? The most natural way to traverse a tree is recursively. For example, if the tree contains integers as cargo, this function returns their sum:

```
def total(tree):
    if tree == None: return 0
    return total(tree.left) + total(tree.right) + tree.cargo
```

The base case is the empty tree, which contains no cargo, so the sum is 0. The recursive step makes two recursive calls to find the sum of the child trees. When the recursive calls complete, we add the cargo of the parent and return the total.

27.3. Expression trees

A tree is a natural way to represent the structure of an expression. Unlike other notations, it can represent the computation unambiguously. For example, the infix expression $\frac{1+2*3}{3}$ is ambiguous unless we know that the multiplication happens before the addition.

This expression tree represents the same computation:

The nodes of an expression tree can be operands like $\underline{1}$ and $\underline{2}$ or operators like $\underline{+}$ and $\underline{*}$. Operands are leaf nodes; operator nodes contain references to their operands. (All of these operators are binary, meaning they have exactly two operands.)

We can build this tree like this:

```
>>> tree = Tree('+', Tree(1), Tree('*', Tree(2), Tree(3)))
```

Looking at the figure, there is no question what the order of operations is; the multiplication happens first in order to compute the second operand of the addition.

Expression trees have many uses. The example in this chapter uses trees to translate expressions to

postfix, prefix, and infix. Similar trees are used inside compilers to parse, optimize, and translate programs.

27.4. Tree traversal

We can traverse an expression tree and print the contents like this:

```
def print_tree(tree):
    if tree == None: return
    print(tree.cargo, end=' ')
    print_tree(tree.left)
    print_tree(tree.right)
```

In other words, to print a tree, first print the contents of the root, then print the entire left subtree, and then print the entire right subtree. This way of traversing a tree is called a preorder, because the contents of the root appear *before* the contents of the children. For the previous example, the output is:

```
>>> tree = Tree('+', Tree(1), Tree('*', Tree(2), Tree(3)))
>>> print_tree(tree)
+ 1 * 2 3
```

This format is different from both postfix and infix; it is another notation called prefix, in which the operators appear before their operands.

You might suspect that if you traverse the tree in a different order, you will get the expression in a different notation. For example, if you print the subtrees first and then the root node, you get:

```
def print_tree_postorder(tree):
    if tree == None: return
    print_tree_postorder(tree.left)
    print_tree_postorder(tree.right)
    print(tree.cargo, end=' ')
```

The result, 1 2 3 * +, is in postfix! This order of traversal is called postorder.

Finally, to traverse a tree inorder, you print the left tree, then the root, and then the right tree:

```
def print_tree_inorder(tree):
    if tree == None: return
    print_tree_inorder(tree.left)
    print(tree.cargo, end=' ')
    print_tree_inorder(tree.right)
```

The result is 1 + 2 * 3, which is the expression in infix.

To be fair, we should point out that we have omitted an important complication. Sometimes when we write an expression in infix, we have to use parentheses to preserve the order of operations. So an inorder traversal is not quite sufficient to generate an infix expression.

Nevertheless, with a few improvements, the expression tree and the three recursive traversals provide a general way to translate expressions from one format to another.

If we do an inorder traversal and keep track of what level in the tree we are on, we can generate a graphical representation of a tree:

```
def print_tree_indented(tree, level=0):
    if tree == None: return
    print_tree_indented(tree.right, level+1)
    print(' '* level + str(tree.cargo))
    print_tree_indented(tree.left, level+1)
```

The parameter <u>level</u> keeps track of where we are in the tree. By default, it is initially 0. Each time we make a recursive call, we pass <u>level+1</u> because the child's level is always one greater than the parent's. Each item is indented by two spaces per level. The result for the example tree is:

```
>>> print_tree_indented(tree)
    3
    *
    2
+
    1
```

If you look at the output sideways, you see a simplified version of the original figure.

27.5. Building an expression tree

In this section, we parse infix expressions and build the corresponding expression trees. For example, the expression (3 + 7) * 9 yields the following tree:

Notice that we have simplified the diagram by leaving out the names of the attributes.

The parser we will write handles expressions that include numbers, parentheses, and the operators \pm and \pm . We assume that the input string has already been tokenized into a Python list (producing this list is left as an exercise). The token list for (3 + 7) * 9 is:

```
['(', 3, '+', 7, ')', '*', 9, 'end']
```

The end token is useful for preventing the parser from reading past the end of the list.

The first function we'll write is get_token, which takes a token list and an expected token as parameters. It compares the expected token to the first token on the list: if they match, it removes the token from the list and returns True; otherwise, it returns False:

```
def get_token(token_list, expected):
    if token_list[0] == expected:
        del token_list[0]
        return True
else:
        return False
```

Since token_list refers to a mutable object, the changes made here are visible to any other variable that refers to the same object.

The next function, get number, handles operands. If the next token in token list is a number,

get_number removes it and returns a leaf node containing the number; otherwise, it returns None.

```
def get_number(token_list):
    x = token_list[0]
    if type(x) != type(0): return None
    del token_list[0]
    return Tree (x, None, None)
```

Before continuing, we should test get_number in isolation. We assign a list of numbers to token_list, extract the first, print the result, and print what remains of the token list:

```
>>> token_list = [9, 11, 'end']
>>> x = get_number(token_list)
>>> print_tree_postorder(x)
9
>>> print(token_list)
[11, 'end']
```

The next method we need is get_product, which builds an expression tree for products. A simple product has two numbers as operands, like 3 * 7.

Here is a version of get product that handles simple products.

```
def get_product(token_list):
    a = get_number(token_list)
    if get_token(token_list, '*'):
        b = get_number(token_list)
        return Tree ('*', a, b)
else:
    return a
```

Assuming that get_number succeeds and returns a singleton tree, we assign the first operand to a. If the next character is *, we get the second number and build an expression tree with a, b, and the operator.

If the next character is anything else, then we just return the leaf node with a. Here are two examples:

```
>>> token_list = [9, '*', 11, 'end']
>>> tree = get_product(token_list)
>>> print_tree_postorder(tree)
9 11 *

>>> token_list = [9, '+', 11, 'end']
>>> tree = get_product(token_list)
>>> print_tree_postorder(tree)
9
```

The second example implies that we consider a single operand to be a kind of product. This definition of product is counterintuitive, but it turns out to be useful.

Now we have to deal with compound products, like like 3 * 5 * 13. We treat this expression as a product of products, namely 3 * (5 * 13). The resulting tree is:

With a small change in get_product, we can handle an arbitrarily long product:

```
def get_product(token_list):
    a = get_number(token_list)
    if get_token(token_list, '*'):
        b = get_product(token_list) # this Line changed
        return Tree ('*', a, b)
    else:
        return a
```

In other words, a product can be either a singleton or a tree with $\underline{*}$ at the root, a number on the left, and a product on the right. This kind of recursive definition should be starting to feel familiar.

Let's test the new version with a compound product:

```
>>> token_list = [2, '*', 3, '*', 5, '*', 7, 'end']
>>> tree = get_product(token_list)
>>> print_tree_postorder(tree)
2 3 5 7 * * *
```

Next we will add the ability to parse sums. Again, we use a slightly counterintuitive definition of sum. For us, a sum can be a tree with \pm at the root, a product on the left, and a sum on the right. Or, a sum can be just a product.

If you are willing to play along with this definition, it has a nice property: we can represent any expression (without parentheses) as a sum of products. This property is the basis of our parsing algorithm.

get_sum tries to build a tree with a product on the left and a sum on the right. But if it doesn't find a \pm , it just builds a product.

```
def get_sum(token_list):
    a = get_product(token_list)
    if get_token(token_list, '+'):
        b = get_sum(token_list)
        return Tree ('+', a, b)
    else:
    return a
```

Let's test it with 9 * 11 + 5 * 7:

```
>>> token_list = [9, '*', 11, '+', 5, '*', 7, 'end']
>>> tree = get_sum(token_list)
>>> print_tree_postorder(tree)
9 11 * 5 7 * +
```

We are almost done, but we still have to handle parentheses. Anywhere in an expression where there can be a number, there can also be an entire sum enclosed in parentheses. We just need to modify get_number to handle subexpressions:

```
def get_number(token_list):
    if get_token(token_list, '('):
        x = get_sum(token_list)  # get the subexpression
        get_token(token_list, ')')  # remove the closing parenthesis
        return x
else:
```

Let's test this code with 9 * (11 + 5) * 7:

```
>>> token_list = [9, '*', '(', 11, '+', 5, ')', '*', 7, 'end']
>>> tree = get_sum(token_list)
>>> print_tree_postorder(tree)
9 11 5 + 7 * *
```

The parser handled the parentheses correctly; the addition happens before the multiplication.

In the final version of the program, it would be a good idea to give get_number a name more descriptive of its new role.

27.6. Handling errors

Throughout the parser, we've been assuming that expressions are well-formed. For example, when we reach the end of a subexpression, we assume that the next character is a close parenthesis. If there is an error and the next character is something else, we should deal with it.

```
def get_number(token_list):
    if get_token(token_list, '('):
        x = get_sum(token_list)
    if not get_token(token_list, ')'):
        raise 'BadExpressionError', 'missing parenthesis'
    return x
else:
    # the rest of the function omitted
```

The raise statement creates an exception; in this case we create a new kind of exception, called a BadExpressionError. If the function that called get_number, or one of the other functions in the traceback, handles the exception, then the program can continue. Otherwise, Python will print an error message and quit.

27.7. The animal tree

In this section, we develop a small program that uses a tree to represent a knowledge base.

The program interacts with the user to create a tree of questions and animal names. Here is a sample run:

```
Are you thinking of an animal? y
Is it a bird? n
What is the animals name? dog
What question would distinguish a dog from a bird? Can it fly
If the animal were dog the answer would be? n

Are you thinking of an animal? y
Can it fly? n
Is it a dog? n
What is the animals name? cat
What question would distinguish a cat from a dog? Does it bark
If the animal were cat the answer would be? n
```

```
Are you thinking of an animal? y
Can it fly? n
Does it bark? y
Is it a dog? y
I rule!
Are you thinking of an animal? n
```

Here is the tree this dialog builds:

At the beginning of each round, the program starts at the top of the tree and asks the first question. Depending on the answer, it moves to the left or right child and continues until it gets to a leaf node. At that point, it makes a guess. If the guess is not correct, it asks the user for the name of the new animal and a question that distinguishes the (bad) guess from the new animal. Then it adds a node to the tree with the new question and the new animal.

Here is the code:

```
1
     def yes(ques):
 2
         ans = input(ques).lower()
 3
         return ans[0] == 'y'
 4
 5
     def animal():
 6
         # start with a singleton
 7
         root = Tree("bird")
 8
9
         # loop until the user quits
10
         while True:
11
             print
12
             if not yes("Are you thinking of an animal? "): break
13
             # walk the tree
14
15
             tree = root
16
             while tree.left != None:
17
                 prompt = tree.cargo + "? "
18
                 if yes(prompt):
19
                    tree = tree.right
20
                 else:
21
                     tree = tree.left
22
23
             # make a guess
24
             guess = tree.cargo
25
             prompt = "Is it a " + guess + "? "
26
             if yes(prompt):
27
                 print("I rule!")
28
                 continue
29
30
             # get new information
31
             prompt = "What is the animal's name? "
32
             animal = input(prompt)
33
             prompt = "What question would distinguish a {0} from a {1}? "
34
             question = input(prompt.format(animal, guess))
35
             # add new information to the tree
36
             tree.cargo = question
37
             prompt = "If the animal were {0} the answer would be? "
38
39
             if yes(prompt.format(animal)):
40
                 tree.left = Tree(guess)
41
                 tree.right = Tree(animal)
42
             else:
43
                 tree.left = Tree(animal)
44
                 tree.right = Tree(guess)
```

The function yes is a helper; it prints a prompt and then takes input from the user. If the response begins with y or Y, the function returns True.

The condition of the outer loop of animal is True, which means it will continue until the break statement executes, if the user is not thinking of an animal.

The inner while loop walks the tree from top to bottom, guided by the user's responses.

When a new node is added to the tree, the new question replaces the cargo, and the two children are the new animal and the original cargo.

One shortcoming of the program is that when it exits, it forgets everything you carefully taught it! Fixing this problem is left as an exercise.

27.8. Glossary

binary operator

An operator that takes two operands.

binary tree

A tree in which each node refers to zero, one, or two dependent nodes.

child

One of the nodes referred to by a node.

leaf

A bottom-most node in a tree, with no children.

level

The set of nodes equidistant from the root.

parent

The node that refers to a given node.

postorder

A way to traverse a tree, visiting the children of each node before the node itself.

prefix notation

A way of writing a mathematical expression with each operator appearing before its operands.

preorder

A way to traverse a tree, visiting each node before its children.

root

The topmost node in a tree, with no parent.

siblings

Nodes that share a common parent.

subexpression

An expression in parentheses that acts as a single operand in a larger expression.

27.9. Exercises

- 1. Modify print_tree_inorder so that it puts parentheses around every operator and pair of operands. Is the output correct and unambiguous? Are the parentheses always necessary?
- 2. Write a function that takes an expression string and returns a token list.
- 3. Find other places in the expression tree functions where errors can occur and add appropriate raise statements. Test your code with improperly formed expressions.
- 4. Think of various ways you might save the animal knowledge tree in a file. Implement the one you think is easiest.

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Debugging

Different kinds of errors can occur in a program, and it is useful to distinguish among them in order to track them down more quickly:

- 1. Syntax errors are produced by Python when it is translating the source code into byte code. They usually indicate that there is something wrong with the syntax of the program. Example: Omitting the colon at the end of a def statement yields the somewhat redundant message SyntaxError: invalid syntax.
- 2. Runtime errors are produced by the runtime system if something goes wrong while the program is running. Most runtime error messages include information about where the error occurred and what functions were executing. Example: An infinite recursion eventually causes a runtime error of maximum recursion depth exceeded.
- 3. Semantic errors are problems with a program that compiles and runs but doesn't do the right thing. Example: An expression may not be evaluated in the order you expect, yielding an unexpected result.

The first step in debugging is to figure out which kind of error you are dealing with. Although the following sections are organized by error type, some techniques are applicable in more than one situation.

Syntax errors

Syntax errors are usually easy to fix once you figure out what they are. Unfortunately, the error messages are often not helpful. The most common messages are SyntaxError: invalid syntax and SyntaxError: invalid token, neither of which is very informative.

On the other hand, the message does tell you where in the program the problem occurred. Actually, it tells you where Python noticed a problem, which is not necessarily where the error is. Sometimes the error is prior to the location of the error message, often on the preceding line.

If you are building the program incrementally, you should have a good idea about where the error is. It will be in the last line you added.

If you are copying code from a book, start by comparing your code to the book's code very carefully. Check every character. At the same time, remember that the book might be wrong, so if you see something that looks like a syntax error, it might be.

Here are some ways to avoid the most common syntax errors:

- 1. Make sure you are not using a Python keyword for a variable name.
- 2. Check that you have a colon at the end of the header of every compound statement, including for, while, if, and def statements.
- 3. Check that indentation is consistent. You may indent with either spaces or tabs but it's best not to mix them. Each level should be nested the same amount.
- 4. Make sure that any strings in the code have matching quotation marks.
- 5. If you have multiline strings with triple quotes (single or double), make sure you have

terminated the string properly. An unterminated string may cause an <u>invalid token</u> error at the end of your program, or it may treat the following part of the program as a string until it comes to the next string. In the second case, it might not produce an error message at all!

- 6. An unclosed bracket (, {, or [makes Python continue with the next line as part of the current statement. Generally, an error occurs almost immediately in the next line.
- 7. Check for the classic = instead of == inside a conditional.

If nothing works, move on to the next section...

I can't get my program to run no matter what I do.

If the compiler says there is an error and you don't see it, that might be because you and the compiler are not looking at the same code. Check your programming environment to make sure that the program you are editing is the one Python is trying to run. If you are not sure, try putting an obvious and deliberate syntax error at the beginning of the program. Now run (or import) it again. If the compiler doesn't find the new error, there is probably something wrong with the way your environment is set up.

If this happens, one approach is to start again with a new program like Hello, World!, and make sure you can get a known program to run. Then gradually add the pieces of the new program to the working one.

Runtime errors

Once your program is syntactically correct, Python can import it and at least start running it. What could possibly go wrong?

My program does absolutely nothing.

This problem is most common when your file consists of functions and classes but does not actually invoke anything to start execution. This may be intentional if you only plan to import this module to supply classes and functions.

If it is not intentional, make sure that you are invoking a function to start execution, or execute one from the interactive prompt. Also see the Flow of Execution section below.

My program hangs.

If a program stops and seems to be doing nothing, we say it is hanging. Often that means that it is caught in an infinite loop or an infinite recursion.

- 1. If there is a particular loop that you suspect is the problem, add a print statement immediately before the loop that says entering the loop and another immediately after that says exiting the loop.
- 2. Run the program. If you get the first message and not the second, you've got an infinite loop. Go to the Infinite Loop section below.
- 3. Most of the time, an infinite recursion will cause the program to run for a while and then produce a RuntimeError: Maximum recursion depth exceeded error. If that happens, go to the Infinite Recursion section below.
- 4. If you are not getting this error but you suspect there is a problem with a recursive method or function, you can still use the techniques in the Infinite Recursion section.

- 5. If neither of those steps works, start testing other loops and other recursive functions and methods.
- 6. If that doesn't work, then it is possible that you don't understand the flow of execution in your program. Go to the Flow of Execution section below.

Infinite Loop

If you think you have an infinite loop and you think you know what loop is causing the problem, add a print statement at the end of the loop that prints the values of the variables in the condition and the value of the condition.

For example:

```
while x > 0 and y < 0:
    # do something to x
    # do something to y

print("x: ", x)
print("y: ", y)
print("condition: ", (x > 0 and y < 0))</pre>
```

Now when you run the program, you will see three lines of output for each time through the loop. The last time through the loop, the condition should be <u>false</u>. If the loop keeps going, you will be able to see the values of \bar{x} and \bar{y} , and you might figure out why they are not being updated correctly.

In a development environment like PyScripter, one can also set a breakpoint at the start of the loop, and single-step through the loop. While you do this, inspect the values of x and y by hovering your cursor over them.

Of course, all programming and debugging require that you have a good mental model of what the algorithm ought to be doing: if you don't understand what ought to happen to \bar{x} and \bar{y} , printing or inspecting its value is of little use. Probably the best place to debug the code is away from your computer, working on your understanding of what should be happening.

Infinite Recursion

Most of the time, an infinite recursion will cause the program to run for a while and then produce a Maximum recursion depth exceeded error.

If you suspect that a function or method is causing an infinite recursion, start by checking to make sure that there is a base case. In other words, there should be some condition that will cause the function or method to return without making a recursive invocation. If not, then you need to rethink the algorithm and identify a base case.

If there is a base case but the program doesn't seem to be reaching it, add a print statement at the beginning of the function or method that prints the parameters. Now when you run the program, you will see a few lines of output every time the function or method is invoked, and you will see the parameters. If the parameters are not moving toward the base case, you will get some ideas about why not.

Once again, if you have an environment that supports easy single-stepping, breakpoints, and inspection, learn to use them well. It is our opinion that walking through code step-by-step builds

the best and most accurate mental model of how computation happens. Use it if you have it!

Flow of Execution

If you are not sure how the flow of execution is moving through your program, add <u>print</u> statements to the beginning of each function with a message like entering function <u>foo</u>, where <u>foo</u> is the name of the function.

Now when you run the program, it will print a trace of each function as it is invoked.

If you're not sure, step through the program with your debugger.

When I run the program I get an exception.

If something goes wrong during runtime, Python prints a message that includes the name of the exception, the line of the program where the problem occurred, and a traceback.

Put a breakpoint on the line causing the exception, and look around!

The traceback identifies the function that is currently running, and then the function that invoked it, and then the function that invoked *that*, and so on. In other words, it traces the path of function invocations that got you to where you are. It also includes the line number in your file where each of these calls occurs.

The first step is to examine the place in the program where the error occurred and see if you can figure out what happened. These are some of the most common runtime errors:

NameError

You are trying to use a variable that doesn't exist in the current environment. Remember that local variables are local. You cannot refer to them from outside the function where they are defined.

TypeError

There are several possible causes:

- 1. You are trying to use a value improperly. Example: indexing a string, list, or tuple with something other than an integer.
- 2. There is a mismatch between the items in a format string and the items passed for conversion. This can happen if either the number of items does not match or an invalid conversion is called for.
- 3. You are passing the wrong number of arguments to a function or method. For methods, look at the method definition and check that the first parameter is self. Then look at the method invocation; make sure you are invoking the method on an object with the right type and providing the other arguments correctly.

KeyError

You are trying to access an element of a dictionary using a key value that the dictionary does not contain.

AttributeError

You are trying to access an attribute or method that does not exist.

IndexError

The index you are using to access a list, string, or tuple is greater than its length minus one. Immediately before the site of the error, add a print statement to display the value of the index and the length of the array. Is the array the right size? Is the index the right value?

I added so many print statements I get inundated with output.

One of the problems with using print statements for debugging is that you can end up buried in output. There are two ways to proceed: simplify the output or simplify the program.

To simplify the output, you can remove or comment out print statements that aren't helping, or combine them, or format the output so it is easier to understand.

To simplify the program, there are several things you can do. First, scale down the problem the program is working on. For example, if you are sorting an array, sort a *small* array. If the program takes input from the user, give it the simplest input that causes the problem.

Second, clean up the program. Remove dead code and reorganize the program to make it as easy to read as possible. For example, if you suspect that the problem is in a deeply nested part of the program, try rewriting that part with simpler structure. If you suspect a large function, try splitting it into smaller functions and testing them separately.

Often the process of finding the minimal test case leads you to the bug. If you find that a program works in one situation but not in another, that gives you a clue about what is going on.

Similarly, rewriting a piece of code can help you find subtle bugs. If you make a change that you think doesn't affect the program, and it does, that can tip you off.

You can also wrap your debugging print statements in some condition, so that you suppress much of the output. For example, if you are trying to find an element using a binary search, and it is not working, you might code up a debugging print statement inside a conditional: if the range of candidate elements is less that 6, then print debugging information, otherwise don't print.

Similarly, breakpoints can be made conditional: you can set a breakpoint on a statement, then edit the breakpoint to say "only break if this expression becomes true".

Semantic errors

In some ways, semantic errors are the hardest to debug, because the compiler and the runtime system provide no information about what is wrong. Only you know what the program is supposed to do, and only you know that it isn't doing it.

The first step is to make a connection between the program text and the behavior you are seeing. You need a hypothesis about what the program is actually doing. One of the things that makes that hard is that computers run so fast.

You will often wish that you could slow the program down to human speed, and with some debuggers you can. But the time it takes to insert a few well-placed <u>print</u> statements is often short compared to setting up the debugger, inserting and removing breakpoints, and walking the program to where the error is occurring.

My program doesn't work.

You should ask yourself these questions:

- 1. Is there something the program was supposed to do but which doesn't seem to be happening? Find the section of the code that performs that function and make sure it is executing when you think it should.
- 2. Is something happening that shouldn't? Find code in your program that performs that function and see if it is executing when it shouldn't.
- 3. Is a section of code producing an effect that is not what you expected? Make sure that you understand the code in question, especially if it involves invocations to functions or methods in other Python modules. Read the documentation for the functions you invoke. Try them out by writing simple test cases and checking the results.

In order to program, you need to have a mental model of how programs work. If you write a program that doesn't do what you expect, very often the problem is not in the program; it's in your mental model.

The best way to correct your mental model is to break the program into its components (usually the functions and methods) and test each component independently. Once you find the discrepancy between your model and reality, you can solve the problem.

Of course, you should be building and testing components as you develop the program. If you encounter a problem, there should be only a small amount of new code that is not known to be correct.

I've got a big hairy expression and it doesn't do what I expect.

Writing complex expressions is fine as long as they are readable, but they can be hard to debug. It is often a good idea to break a complex expression into a series of assignments to temporary variables.

For example:

```
self.hands[i].addCard (self.hands[self.findNeighbor(i)].popCard())
```

This can be rewritten as:

```
neighbor = self.findNeighbor (i)
pickedCard = self.hands[neighbor].popCard()
self.hands[i].addCard (pickedCard)
```

The explicit version is easier to read because the variable names provide additional documentation, and it is easier to debug because you can check the types of the intermediate variables and display or inspect their values.

Another problem that can occur with big expressions is that the order of evaluation may not be what you expect. For example, if you are translating the expression x/2pi into Python, you might write:

```
y = x / 2 * math.pi
```

That is not correct because multiplication and division have the same precedence and are evaluated from left to right. So this expression computes (x/2)pi.

A good way to debug expressions is to add parentheses to make the order of evaluation explicit:

```
y = x / (2 * math.pi)
```

Whenever you are not sure of the order of evaluation, use parentheses. Not only will the program be correct (in the sense of doing what you intended), it will also be more readable for other people who haven't memorized the rules of precedence.

I've got a function or method that doesn't return what I expect.

If you have a <u>return</u> statement with a complex expression, you don't have a chance to print the <u>return</u> value before returning. Again, you can use a temporary variable. For example, instead of:

```
return self.hands[i].removeMatches()
```

you could write:

```
count = self.hands[i].removeMatches()
return count
```

Now you have the opportunity to display or inspect the value of count before returning.

I'm really, really stuck and I need help.

First, try getting away from the computer for a few minutes. Computers emit waves that affect the brain, causing these effects:

- 1. Frustration and/or rage.
- 2. Superstitious beliefs (the computer hates me) and magical thinking (the program only works when I wear my hat backward).
- 3. Random-walk programming (the attempt to program by writing every possible program and choosing the one that does the right thing).

If you find yourself suffering from any of these symptoms, get up and go for a walk. When you are calm, think about the program. What is it doing? What are some possible causes of that behavior? When was the last time you had a working program, and what did you do next?

Sometimes it just takes time to find a bug. We often find bugs when we are away from the computer and let our minds wander. Some of the best places to find bugs are trains, showers, and in bed, just before you fall asleep.

No, I really need help.

It happens. Even the best programmers occasionally get stuck. Sometimes you work on a program so long that you can't see the error. A fresh pair of eyes is just the thing.

Before you bring someone else in, make sure you have exhausted the techniques described here. Your program should be as simple as possible, and you should be working on the smallest input that causes the error. You should have print statements in the appropriate places (and the output they produce should be comprehensible). You should understand the problem well enough to describe it concisely.

When you bring someone in to help, be sure to give them the information they need:

- 1. If there is an error message, what is it and what part of the program does it indicate?
- 2. What was the last thing you did before this error occurred? What were the last lines of code that you wrote, or what is the new test case that fails?
- 3. What have you tried so far, and what have you learned?

Good instructors and helpers will also do something that should not offend you: they won't believe when you tell them "I'm sure all the input routines are working just fine, and that I've set up the data correctly!". They will want to validate and check things for themselves. After all, your program has a bug. Your understanding and inspection of the code have not found it yet. So you should expect to have your assumptions challenged. And as you gain skills and help others, you'll need to do the same for them.

When you find the bug, take a second to think about what you could have done to find it faster. Next time you see something similar, you will be able to find the bug more quickly.

Remember, the goal is not just to make the program work. The goal is to learn how to make the program work.

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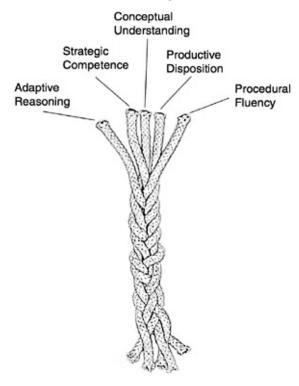
An odds-and-ends Workbook

This workbook / cookbook of recipes is still very much under construction.

The Five Strands of Proficiency

This was an important study commissioned by the President in the USA. It looked at what was needed for students to become proficient in maths.

But it is also an amazingly accurate fit for what we need for proficiency in Computer Science, or even for proficiency in playing Jazz!



- 1. Procedural Fluency: Learn the syntax. Learn to type. Learn your way around your tools. Learn and practice your scales. Learn to rearrange formulae.
- 2. Conceptual Understanding: Understand why the bits fit together like they do.
- 3. Strategic Competence: Can you see what to do next? Can you formulate this word problem into your notation? Can you take the music where you want it to go?
- 4. Adaptive Reasoning: Can you see how to change what you've learnt for this new problem?
- 5. A Productive Disposition: We need that *Can Do!* attitude!
 - a. You habitually think it is worthwhile studying this stuff.
 - b. You are diligent and disciplined enough to grind through the tough stuff, and to put in your practice hours.
 - c. You develop a sense of efficacy that you can make things happen!

Check out http://mason.gmu.edu/~isuh4/teaching/strands.htm, or Kilpatrick's book at

http://www.nap.edu/openbook.php?isbn=0309069955

Sending Email

Sometimes it is fun to do powerful things with Python — remember that part of the "productive disposition" we saw under the five threads of proficiency included *efficacy* — the sense of being able to accomplish something useful. Here is a Python example of how you can send email to someone.

```
import smtplib, email.mime.text
1
2
    me = 'joe@my.org.com'
3
                                         # put your own email here
    me = 'joe@my.org.com'  # put your own email here
fred = 'fred@his.org.com'  # and fred's email address here
     your_mail_server = 'mail.my.org.com' # Ask your system administrator
     # Create a text message containing the body of the email.
8
     # You could read this from a file, of course.
9
     msg = email.mime.text.MIMEText("""Hey Fred,
10
11
     I'm having a party, please come at 8pm.
     Bring a plate of snacks and your own drinks.
12
13
    Joe""" )
14
15
     msg['From'] = me
                                     # add headers to the message object
16
17
     msg['To'] = fred
     msg['Subject'] = 'Party on Saturday 23rd'
18
19
    # create a connection to your mail server
20
21
    svr = smtplib.SMTP(your_mail_server)
     response = svr.sendmail(me, fred, msg.as_string()) # send message
22
23
     if response != {}:
24
         print("Sending failed for ", response)
25
    else:
         print("Message sent.")
26
27
28
                                                   # close the connection
     svr.quit()
```

In the context of the course, notice how we use the two objects in this program: we create a message object on line 9, and set some attributes at lines 16-18. We then create a connection object at line 21, and ask it to send our message.

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Configuring Ubuntu for Python Development

Note: the following instructions assume that you are connected to the Internet and that you have both the main and universe package repositories enabled. All unix shell commands are assumed to be running from your home directory (\$HOME). Finally, any command that begins with sudo assums that you have administrative rights on your machine. If you do not — please ask your system administrator about installing the software you need.

What follows are instructions for setting up an Ubuntu 9.10 (Karmic) home environment for use with this book. I use Ubuntu GNU/Linux for both development and testing of the book, so it is the only system about which I can personally answer setup and configuration questions.

In the spirit of software freedom and open collaboration, please contact me if you would like to maintain a similar appendix for your own favorite system. I'd be more than happy to link to it or put it on the Open Book Project site, provided you agree to answer user feedback concerning it.

Thanks!

Jeffrey Elkner

Governor's Career and Technical Academy in Arlington Arlington, Virginia

Vim

Vim can be used very effectively for Python development, but Ubuntu only comes with the vim-tiny package installed by default, so it doesn't support color syntax highlighting or auto-indenting.

To use Vim, do the following:

1. From the unix command prompt, run:

```
$ sudo apt-get install vim-gnome
```

2. Create a file in your home directory named .vimrc that contains the following:

```
syntax enable
filetype indent on
set et
set sw=4
set smarttab
map \langle f2 \rangle : w | !python %
```

When you edit a file with a .py extension, you should now have color systax highlighting and auto indenting. Pressing the key should run your program, and bring you back to the editor when the program completes.

To learn to use vim, run the following command at a unix command prompt:

```
$ vimtutor
```

GASP

Several of the case studies use GASP (Graphics API for Students for Python), which is the only additional library needed to use this book.

To install GASP on Ubuntu 9.04 (Jaunty) or later, run the following command at a unix command prompt:

```
$ sudo apt-get install python-gasp
```

or use the synaptic package manager.

Getting GASP from Launchpad

To install the latest version of GASP into your home directory, run the following commands at a unix command prompt:

```
$ sudo apt-get install bzr
$ bzr branch lp:gasp-code
```

\$HOME environment

The following creates a useful environment in your home directory for adding your own Python libraries and executable scripts:

1. From the command prompt in your home directory, create *bin* and *Lib/python* subdirectories by running the following commands:

```
$ mkdir bin lib
$ mkdir lib/python
```

2. Add the following lines to the bottom of your .bashrc in your home directory:

```
PYTHONPATH=$HOME/lib/python
EDITOR=vim
export PYTHONPATH EDITOR
```

This will set your prefered editor to Vim, add your own *Lib/python* subdirectory for your Python libraries to your Python path, and add your own *bin* directory as a place to put executable scripts. You need to logout and log back in before your local *bin* directory will be in your <u>search</u> path.

Making a python script executable and runnable from anywhere

On unix systems, Python scripts can be made executable using the following process:

1. Add this line as the first line in the script:

```
#!/usr/bin/env python
```

2. At the unix command prompt, type the following to make <code>myscript.py</code> executable:

```
$ chmod +x myscript.py
```

3. Move myscript.py into your bin directory, and it will be runnable from anywhere.

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This book is free as in freedom, which means you have the right to modify it to suite your needs, and to redistribute your modifications so that our whole community can benefit.

That freedom lacks meaning, however, if you the tools needed to make a custom version or to contribute corrections and additions are not within your reach. This appendix attempts to put those tools in your hands.

Thanks!

Jeffrey Elkner

Governor's Career and Technical Academy in Arlington Arlington, Virginia

Getting the Source

This book is <u>marked up</u> in <u>ReStructuredText</u> using a document generation system called <u>Sphinx</u>.

The source code is located on the <u>Launchpad website</u> at http://bazaar.launchpad.net/~thinkcspy/thinkcspy/english2e/files.

The easiest way to get the source code on an Ubuntu 9.10 computer is:

- 1. run sudo apt-get install bzr on your system to install bzr.
- 2. run bzr branch lp:thinkcspy.

The last command above will download the book source from Launchpad into a directory named thinkcspy which contains the Sphinx source and configuration information needed to build the book.

Making the HTML Version

To generate the html version of the book:

- 1. run sudo apt-get install python-sphinx to install the Sphinx documentation system.
- 2. cd thinkcspy change into the thinkcspy directory containing the book source.
- 3. make html.

The last command will run sphinx and create a directory named build containing the html verion of the text.

Note: Sphinx supports building other output types as well, such as <u>PDF</u>. This requires that <u>LaTeX</u> be present on your system. Since I only personally use the html version, I will not

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attempt to document that process here.

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Some Tips, Tricks, and Common Errors

These are small summaries of ideas, tips, and commonly seen errors that might be helpful to those beginning Python.

Functions

Functions help us with our mental chunking: they allow us to group together statements for a highlevel purpose, e.g. a function to sort a list of items, a function to make the turtle draw a spiral, or a function to compute the mean and standard deviation of some measurements.

There are two kinds of functions: fruitful functions calculate and return a value, and we use them because we're primarily interested in the value they'll return. Non-fruitful functions are used because they perform actions that we want done — e.g. make a turtle draw a rectangle, or print the first thousand prime numbers. They always return None - a special dummy value.

Tip: None is not a string

Values like None, True and False are not strings: they are special values in Python, and are in the list of keywords we gave in chapter 2. Keywords are special in the language: they are part of the syntax. So we cannot create our own variable or function with a name True — we'll get a syntax error. (Built-in functions are not priviledged like keywords: we can define our own variable or function called len, but we'd be silly to do so!)

Along with the fruitful/non-fruitful division, there are two flavours of the return statement in Python - one that returns a useful value, and the other that returns nothing, or None. And if we get to the end of any function and we have not explicitly executed any return statement, Python automatically returns the value None.

Perhaps nothing — some functions exists purely to perform actions rather than to calculate and return a result.

To make functions more useful, they are given parameters. So a function to make a turtle draw a square might have two parameters — one for the turtle that needs to do the drawing, and another for the size of the square. See the first example in Chapter 4 - that function can be used with any turtle, and for any size square. So it is much more general than a function that always uses a specific turtle, say tess to draw a square of a specific size, say 30.

Understand which parts of the function will be hard-coded and unchangeable, and which parts should become parameters so that they can be customized by the caller of the function.

In math, we're familiar with functions like f(x) = 3x + 5. We already understand that when we call the

function $\underline{f(3)}$ we make some association between the parameter x and the argument 3. Try to draw parallels to argument passing in Python.

Quiz: Is the function f(z) = 3z + 5 the same as function f above?

Problems with logic and flow of control

We often want to know if some condition holds for any item in a list, e.g. "does the list have any odd numbers?" This is a common mistake:

```
def anyOdd(xs):
    ''' Return True if there is an odd number in xs, a list of integers. '''
for v in xs:
    if v % 2 == 1:
        return True
else:
        return False
```

Can we spot what's wrong here? As soon as we execute a return, we'll leave the function. So the logic of saying "If I find an odd number I can return True" is fine. However, we cannot return False after only looking at one item — we can only return False if we've been through all the items, and none of them are odd. So line 6 should not be there, and line 7 has to be outside the loop. Here is a corrected version:

```
def anyOdd(xs):
    ''' Return True if there is an odd number in xs, a list of integers. '''
for v in xs:
    if v % 2 == 1:
        return True
return False
```

This "eureka", or "short-circuit" style of returning from a function as soon as we are certain what the outcome will be was first seen in Section 8.10, in the chapter on strings.

It is preferred over this one, which also works correctly:

```
1
    def anyOdd(xs):
        ''' Return True if there is an odd number in xs, a list of integers.
2
3
       count = 0
4
       for v in xs:
5
          if v % 2 == 1:
                         # count the odd numbers
6
             count += 1
7
        if count > 0:
8
          return True
9
        else:
10
           return False
```

The performance disadvantage of this one is that it traverses the whole list, even if it knows the outcome very early on.

```
Tip: Think about the return conditions of the function
```

Do I need to look at all elements in all cases? Can I shortcut and take an early exit? Under what

```
conditions? When will I have to examine all the items in the list?
```

The code in lines 7-10 can also be tightened up. The expression count > 0 evaluates to a boolean value, either True or False. The value can be used directly in the return statement. So we could cut out that code and simply have the following:

```
1
    def anyOdd(xs):
        ''' Return True if there is an odd number in xs, a list of integers.
2
3
       count = 0
4
        for v in xs:
5
          if v % 2 == 1:
6
             count += 1
                         # count the odd numbers
7
        return count > 0  # Aha! a programmer who understands that boolean
8
                          # expressions are not just used in if statements!
```

Although this code is tighter, it is not as nice as the one that did the short-circuit return as soon as the first odd number was found.

Tip: Generalize your use of booleans

Mature programmers won't write <u>if isPrime(n) == True</u>: when they could say instead <u>if isPrime(n)</u>: Think more generally about boolean values, not just in the context of <u>if</u> or <u>while</u> statements. Like arithmetic expressions, they have their own set of operators (<u>and</u>, <u>or</u>, <u>not</u>) and values (True, False) and can be assigned to variables, put into lists, etc. A good resource for improving your use of booleans is http://en.wikibooks.org/wiki/Non-Programmer%27s_Tutorial_for_Python_3/Boolean_Expressions

Exercise time:

- How would we adapt this to make another function which returns True if *all* the numbers are odd? Can you still use a short-circuit style?
- How would we adapt it to return True if at least three of the numbers are odd? Short-circuit the traversal when the third odd number is found don't traverse the whole list unless we have to.

Local variables

Functions are called, or activated, and while they're busy they create their own stack frame which holds local variables. A local variable is one that belongs to the current activation. As soon as the function returns (whether from an explicit return statement or because Python reached the last statement), the stack frame and its local variables are all destroyed. The important consquence of this is that a function cannot use its own variables to remember any kind of state between different activations. It cannot count how many times it has been called, or remember to switch colours between red and blue UNLESS it makes use of variables that are global. Global variables will survive even after our function has exited, so they are the correct way maintain information between calls.

This fragment assumes our turtle is tess. Each time we call h2() it turns, draws, and increases the global variable sz. Python always assumes that an assignment to a variable (as in line 7) means that we want a new local variable, unless we've provided a global declaration (on line 4). So leaving out the global declaration means this does not work.

```
Tip: Local variables do not survive when vou exit the function
```

Use a Python visualizer like the one at http://netserv.ict.ru.ac.za/python3_viz to build a strong understanding of function calls, stack frames, local variables, and function returns.

Tip: Assigment in a function creates a local variable

Any assignment to a variable within a function means Python will make a local variable, unless we override with global.

Event handler functions

Our chapter on event handling showed three different kinds of events that we could handle. They each have their own subtle points that can trip us up.

- Event handlers are non-fruitful functions they don't return any values.
- They're automatically called by the Python interpreter in response to an event, so we don't get to see the code that calls them.
- A mouse-click event passes two coordinate arguments to its handler, so when we write this handler we have to provide for two parameters (usually named x and y). This is how the handler knows where the mouse click occurred.
- A keypress event handler has to be bound to the key it responds to. There is a messy extra step when using keypresses we have to remember to issue a wn.listen() before our program will receive any keypresses. But if the user presses the key 10 times, the handler will be called ten times.
- Using a timer to create a future-dated event only causes one call to the handler. If we want repeated periodic handler activations, then from within the handler we call wn.ontimer(....) to set up the next event.

String handling

There are only four *really* important operations on strings, and we'll be able to do just about anything. There are many more nice-to-have methods (we'll call them sugar coating) that can make life easier, but if we can work with the basic four operations smoothly, we'll have a great grounding.

- len(str) finds the length of a string.
- str[i] the subscript operation extracts the i'th character of the string, as a new string.
- str[i:j] the slice operation extracts a substring out of a string.
- str.find(target) returns the index where target occurs within the string, or -1 if it is not found.

So if we need to know if "snake" occurs as a substring within s, we could write

```
if s.find("snake") >= 0: ...
if "snake" in s: ... # also works, nice-to-know sugar coating!
```

It would be wrong to split the string into words unless we were asked whether the word "snake"

occurred in the string.

Suppose we're asked to read some lines of data and find function definitions, e.g.: def someFunctionName(x, y):, and we are further asked to isolate and work with the name of the function. (Let's say, print it.)

```
s = "..."

defPos = s.find("def ")

if defPos == 0:

opIndex = s.find('(')

fnname = s[4:opIndex]

print(fnname)

# somehow get the next line to work with

# Look for "def " in the line

# if it occurs at the left margin

# find the index of the open parenthesis

# slice out the function name

# and work with it.
```

One can extend these ideas:

- What if the function def was indented, and didn't start at column 0? The code would need a bit of adjustment, and we'd probably want to be sure that all the characters in front of the defpos were spaces. We would not want to do the wrong thing on data like this: `` # I def initely like Python!
- We've assumed on line 3 that we will find an open parenthesis. It may need to be checked that we did!
- We have also assumed that there was exactly one space between the keyword $\frac{def}{def}$ and the start of the function name. It will not work nicely for $\frac{def}{def}$

As we've already mentioned, there are many more "sugar-coated" methods that let us work more easily with strings. There is an rfind method, like find, that searches from the end of the string backwards. It is useful if we want to find the last occurrence of something. The lower and upper methods can do case conversion. And the split method is great for breaking a string into a list of words, or into a list of lines. We've also made extensive use in this book of the format method. In fact, if we want to practice reading the python documentation and learning some new methods on our own, the string methods are an excellent resource.

Exercises:

- Suppose any line of text can contain at most one url that starts with "http://" and ends at the next space in the line. Write a fragment of code to extract and print the full url if it is present. (Hint: read the documentation for find. It takes some extra arguments, so you can set a starting point from which it will search.)
- Suppose a string contains at most one substring "< ... >". Write a fragment of code to extract and print the portion of the string between the angle brackets.

Looping and lists

Computers are useful because they can repeat computation, accurately and fast. So loops are going to be a central feature of almost all programs you encounter.

```
Tip: Don't create unnecessary lists
```

Lists are useful if you need to keep data for later computation. But if you don't need lists, it is probably better not to generate them.

Here are two functions that both generate ten million random numbers, and return the sum of the

numbers. They both work.

```
1
    import random
2
    joe = random.Random()
3
4
    def sum1():
       ''' Build a list of random numbers, then sum them '''
5
       xs = []
6
7
       for i in range(10000000):
8
           num = joe.randrange(1000) # generate one random number
9
           xs.append(num)
                                    # save it in our list
10
       tot = sum(xs)
11
12
       return tot
13
14
    def sum2():
       ''' Sum the random numbers as we generate them '''
15
16
       tot = 0
17
       for i in range(10000000):
18
          num = joe.randrange(1000)
19
           tot += num
20
       return tot
21
22
    print(sum1())
23
    print(sum2())
```

What reasons are there for preferring the second version here? (Hint: open a tool like the Performance Monitor on your computer, and watch the memory usage. How big can you make the list before you get a fatal memory error in sum1?)

In a similar way, when working with files, we often have an option to read the whole file contents into a single string, or we can read one line at a time and process each line as we read it. Line-at-a-time is the more traditional and perhaps safer way to do things — you'll be able to work comfortably no matter how large the file is. But you may find whole-file-at-once is sometimes more convenient!

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How to Think Like a Computer Scientist: Learning with Python 3 »

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How to Think Like a Computer Scientist



Learning with Python 3 (RLE)

Version date: November 2011

by Peter Wentworth, Jeffrey Elkner, Allen B. Downey, and Chris Meyers

(based on 2nd edition by Jeffrey Elkner, Allen B. Downey, and Chris Meyers)

Corresponding author: p.wentworth@ru.ac.za

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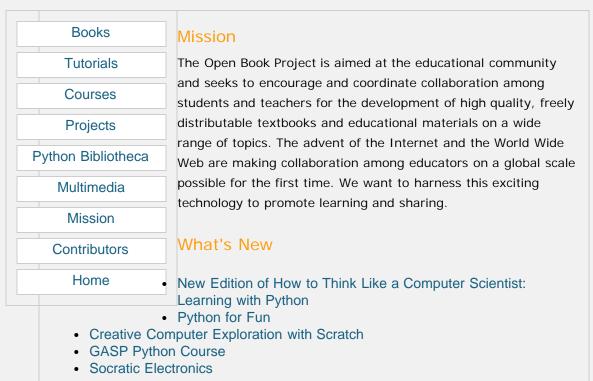
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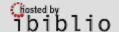


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"He that does good to another does good also to himself."

-- Seneca





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Purpose of this Collection

This collection is presentation of several small Python programs. They are aimed at intermediate programmers; people who have studied Python and are fairly comfortable with basic recursion and object oriented techniques. Each program is very short, never more than couple of pages and accompanied with a write-up.

I have found Python to be an excellent language to express algorithms clearly. Some of the ideas here originated in other programs in other languages. But in most cases developed code from scratch from just an outline of an idea. However "Lisp in Python" almost was exercise translation from McCarthy's John original "Evalquote in Lisp".

From many years of programming these are some of my favorite programs. I hope you enjoy them as

The Collection

Items with a "*" have been recently added or updated

A Simple Video Game Queues, Trees and Water Buckets Towers of Hanoi Animal Trees

Building a GUI with Tkinter Using SQL with the GUI Building a GUI with wxPython

Erlang for Python
Programmers *
Erlang Concurrency:
Logic Circuits
revisted *

Forth in Python * Lisp in Python Prolog Python in (Introduction) * Prolog **Python** in (Part 1) * Prolog in **Python** (Part 2) * Prolog **Python** in (Part 3) * Squeezing Bits. Huffman Data Compression * Natural Language **Processing**

much as I do. I look forward to hearing from readers, especially folks with suggestions for improvements, ideas for new projects, or people who are doing similar things. You can email me at mailme.html

Many thanks to Paul Carduner and Jeff Elkner for their work on this page, especially for Paul's graphic of "Psyltherin" (apologies to Harry Potter) and to the Twisted developement team for their Lore documentation generator to which all the other web pages in this collection have been recently adapted.

Chris Meyers

Classic AI. Semantic Information Retrival Unicode support in Python

Logic Circuits
Logic Circuits (more)

Simulator for Toy Computer Assembler for Toy Computer Compiler for Toy Computer

Using SQL with Python

Waves and Harmonics *

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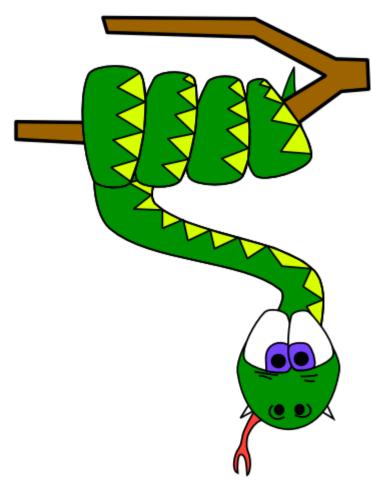
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So come on in, poke around. feel free to take whatever you find useful (everything here is free!), and if you feel the urge, get involved and contribute as well.

Happy computing!

jeff elkner arlington county public schools arlington, va

What's



New

• <u>Learning</u> Zope 3 Tools, tips, and tutorials for learning to program with Zope 3.

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