

Custom Search

COURSES

HIRE WITH US



Program for Fibonacci numbers

The Fibonacci numbers are the numbers in the following integer sequence.

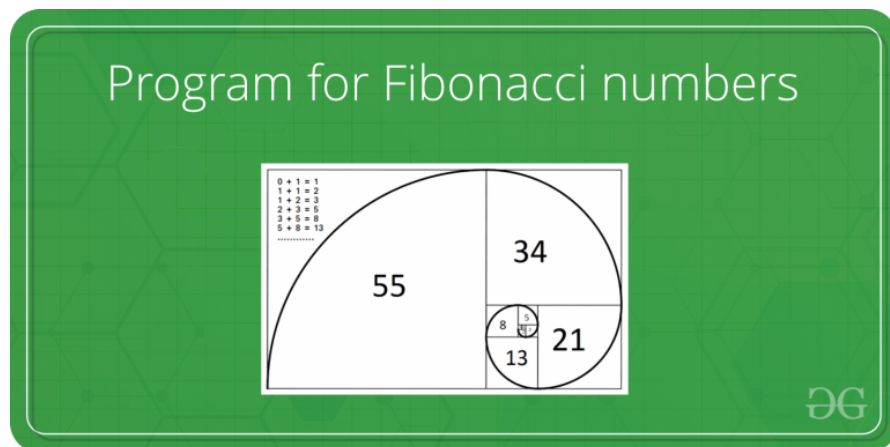
0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144,

In mathematical terms, the sequence F_n of Fibonacci numbers is defined by the recurrence relation

$$F_n = F_{n-1} + F_{n-2}$$

with seed values

$$F_0 = 0 \text{ and } F_1 = 1.$$



Given a number n , print n -th Fibonacci Number.

Examples:

Input : $n = 2$

Output : 1

Input : $n = 9$

Output : 34

Recommended: Please solve it on "[PRACTICE](#)" first, before moving on to the solution.

Write a function `int fib(int n)` that returns F_n . For example, if $n = 0$, then `fib()` should return 0. If $n = 1$, then it should return 1. For $n > 1$, it should return $F_{n-1} + F_{n-2}$

For $n = 9$

Output: 34

Following are different methods to get the n th Fibonacci number.



Get to know your we

Method 1 (Use recursion)

A simple method that is a direct recursive implementation mathematical recurrence relation given above.

C++

```
//Fibonacci Series using Recursion
#include<bits/stdc++.h>
using namespace std;

int fib(int n)
{
    if (n <= 1)
        return n;
    return fib(n-1) + fib(n-2);
}

int main ()
{
    int n = 9;
    cout << fib(n);
    getchar();
    return 0;
}

// This code is contributed
// by Akanksha Rai
```

C

```
//Fibonacci Series using Recursion
#include<stdio.h>
int fib(int n)
{
    if (n <= 1)
        return n;
    return fib(n-1) + fib(n-2);
}

int main ()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}
```

Java

```
//Fibonacci Series using Recursion
class fibonacci
{
    static int fib(int n)
    {
        if (n <= 1)
            return n;
        return fib(n-1) + fib(n-2);
    }

    public static void main (String args[])
    {
        int n = 9;
        System.out.println(fib(n));
    }
}

/* This code is contributed by Rajat Mishra */
```

Python

```
# Function for nth Fibonacci number

def Fibonacci(n):
    if n<0:
        print("Incorrect input")
    # First Fibonacci number is 0
    elif n==0:
        return 0
    # Second Fibonacci number is 1
    elif n==1:
        return 1
    else:
        return Fibonacci(n-1)+Fibonacci(n-2)

# Driver Program

print(Fibonacci(9))

#This code is contributed by Saket Modi
```

C#

```
// C# program for Fibonacci Series
// using Recursion
using System;

public class GFG
{
    public static int Fib(int n)
    {
        if (n <= 1)
        {
            return n;
        }
        else
        {
            return Fib(n - 1) + Fib(n - 2);
        }
    }

    // driver code
    public static void Main(string[] args)
    {
        int n = 9;
        Console.Write(Fib(n));
    }
}

// This code is contributed by Sam007
```

PHP

```
<?php
// Fibonacci Series
// using Recursion

// function returns
// the Fibonacci number
function fib($n)
{
    if ($n <= 1)
        return $n;
    return fib($n - 1) +
        fib($n - 2);
}

// Driver Code
$n = 9;
echo fib($n);

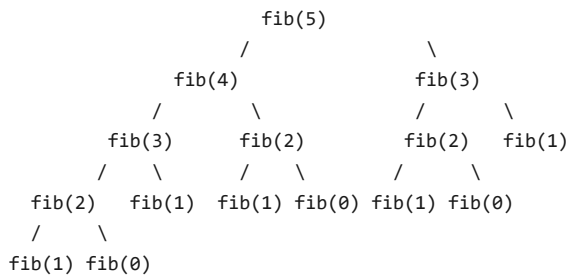
// This code is contributed by aj_36
?>
```

Output

34

Time Complexity: $T(n) = T(n-1) + T(n-2)$ which is exponential.

We can observe that this implementation does a lot of repeated work (see the following recursion tree). So this is a bad implementation for nth Fibonacci number.



Extra Space: $O(n)$ if we consider the function call stack size, otherwise $O(1)$.

Method 2 (Use Dynamic Programming)

We can avoid the repeated work done in the method 1 by storing the Fibonacci numbers calculated so far.

C

```
//Fibonacci Series using Dynamic Programming
#include<stdio.h>

int fib(int n)
{
    /* Declare an array to store Fibonacci numbers. */
    int f[n+2];    // 1 extra to handle case, n = 0
    int i;

    /* 0th and 1st number of the series are 0 and 1*/
    f[0] = 0;
    f[1] = 1;

    for (i = 2; i <= n; i++)
    {
        /* Add the previous 2 numbers in the series
           and store it */
        f[i] = f[i-1] + f[i-2];
    }

    return f[n];
}

int main ()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}
```

Java

```
// Fibonacci Series using Dynamic Programming
class fibonacci
{
    static int fib(int n)
    {
        /* Declare an array to store Fibonacci numbers. */
        int f[] = new int[n+2]; // 1 extra to handle case, n = 0
        int i;

        /* 0th and 1st number of the series are 0 and 1*/
        f[0] = 0;
        f[1] = 1;
    }
}
```

```

for (i = 2; i <= n; i++)
{
    /* Add the previous 2 numbers in the series
    and store it */
    f[i] = f[i-1] + f[i-2];
}

return f[n];
}

public static void main (String args[])
{
    int n = 9;
    System.out.println(fib(n));
}
}
/* This code is contributed by Rajat Mishra */

```

Python

```

# Fibonacci Series using Dynamic Programming
def fibonacci(n):

    # Taking 1st two fibonacci numbers as 0 and 1
    FibArray = [0, 1]

    while len(FibArray) < n + 1:
        FibArray.append(0)

    if n <= 1:
        return n
    else:
        if FibArray[n - 1] == 0:
            FibArray[n - 1] = fibonacci(n - 1)

        if FibArray[n - 2] == 0:
            FibArray[n - 2] = fibonacci(n - 2)

    FibArray[n] = FibArray[n - 2] + FibArray[n - 1]
    return FibArray[n]

print(fibonacci(9))

```

C#

```

// C# program for Fibonacci Series
// using Dynamic Programming
using System;
class fibonacci {

static int fib(int n)
{
    // Declare an array to
    // store Fibonacci numbers.
    // 1 extra to handle
    // case, n = 0
    int []f = new int[n + 2];
    int i;

    /* 0th and 1st number of the
    series are 0 and 1 */
    f[0] = 0;
    f[1] = 1;

    for (i = 2; i <= n; i++)
    {
        /* Add the previous 2 numbers
        in the series and store it */
        f[i] = f[i - 1] + f[i - 2];
    }

    return f[n];
}

// Driver Code

```

```
public static void Main ()
{
    int n = 9;
    Console.WriteLine(fib(n));
}

// This code is contributed by anuj_67.
```

PHP

```
<?php
//Fibonacci Series using Dynamic
// Programming

function fib( $n)
{
    /* Declare an array to store
    Fibonacci numbers. */

    // 1 extra to handle case,
    // n = 0
    $f = array();
    $i;

    /* 0th and 1st number of the
    series are 0 and 1*/
    $f[0] = 0;
    $f[1] = 1;

    for ($i = 2; $i <= $n; $i++)
    {
        /* Add the previous 2
        numbers in the series
        and store it */
        $f[$i] = $f[$i-1] + $f[$i-2];
    }

    return $f[$n];
}

$n = 9;
echo fib($n);

// This code is contributed by
// anuj_67.
?>
```

Output:

34

Method 3 (Space Optimized Method 2)

We can optimize the space used in method 2 by storing the previous two numbers only because that is all we need to get the next Fibonacci number in series.

C/C++

```
// Fibonacci Series using Space Optimized Method
#include<stdio.h>
int fib(int n)
{
    int a = 0, b = 1, c, i;
    if( n == 0)
        return a;
    for (i = 2; i <= n; i++)
    {
        c = a + b;
        a = b;
        b = c;
    }
}
```

```

    return b;
}

int main ()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}

```

Java

```

// Java program for Fibonacci Series using Space
// Optimized Method
class fibonacci
{
    static int fib(int n)
    {
        int a = 0, b = 1, c;
        if (n == 0)
            return a;
        for (int i = 2; i <= n; i++)
        {
            c = a + b;
            a = b;
            b = c;
        }
        return b;
    }

    public static void main (String args[])
    {
        int n = 9;
        System.out.println(fib(n));
    }
}

// This code is contributed by Mihir Joshi

```

Python

```

# Function for nth fibonacci number - Space Optimisatation
# Taking 1st two fibonacci numbers as 0 and 1

def fibonacci(n):
    a = 0
    b = 1
    if n < 0:
        print("Incorrect input")
    elif n == 0:
        return a
    elif n == 1:
        return b
    else:
        for i in range(2, n+1):
            c = a + b
            a = b
            b = c
        return b

# Driver Program

print(fibonacci(9))

#This code is contributed by Saket Modi

```

C#

```

// C# program for Fibonacci Series
// using Space Optimized Method
using System;

namespace Fib

```

```

{
    public class GFG
    {
        static int Fib(int n)
        {
            int a = 0, b = 1, c = 0;

            // To return the first Fibonacci number
            if (n == 0) return a;

            for (int i = 2; i <= n; i++)
            {
                c = a + b;
                a = b;
                b = c;
            }

            return b;
        }

        // Driver function
        public static void Main(string[] args)
        {
            int n = 9;
            Console.WriteLine("{0} ", Fib(n));
        }
    }
}

// This code is contributed by Sam007.

```

PHP

```

<?php
// PHP program for Fibonacci Series
// using Space Optimized Method

function fib( $n)
{
    $a = 0;
    $b = 1;
    $c;
    $i;
    if( $n == 0)
        return $a;
    for($i = 2; $i <= $n; $i++)
    {
        $c = $a + $b;
        $a = $b;
        $b = $c;
    }
    return $b;
}

// Driver Code
$n = 9;
echo fib($n);

// This code is contributed by anuj_67.
?>

```

Output :

34

Time Complexity: $O(n)$

Extra Space: $O(1)$

Method 4 (Using power of the matrix $\begin{Bmatrix} 1 & 1 \\ 1 & 0 \end{Bmatrix}$)

This another $O(n)$ which relies on the fact that if we n times multiply the matrix $M = \begin{Bmatrix} 1 & 1 \\ 1 & 0 \end{Bmatrix}$ to itself (in other words calculate $\text{power}(M, n)$), then we get the $(n+1)$ th Fibonacci number as the element at row and column $(0, 0)$ in the resultant matrix.

The matrix representation gives the following closed expression for the Fibonacci numbers:

$$\begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix}^n = \begin{pmatrix} F_{n+1} & F_n \\ F_n & F_{n-1} \end{pmatrix}.$$

C

```
#include <stdio.h>

/* Helper function that multiplies 2 matrices F and M of size 2*2, and
puts the multiplication result back to F[][] */
void multiply(int F[2][2], int M[2][2]);

/* Helper function that calculates F[][] raise to the power n and puts the
result in F[][]
Note that this function is designed only for fib() and won't work as general
power function */
void power(int F[2][2], int n);

int fib(int n)
{
    int F[2][2] = {{1,1},{1,0}};
    if (n == 0)
        return 0;
    power(F, n-1);

    return F[0][0];
}

void multiply(int F[2][2], int M[2][2])
{
    int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
    int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
    int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
    int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

    F[0][0] = x;
    F[0][1] = y;
    F[1][0] = z;
    F[1][1] = w;
}

void power(int F[2][2], int n)
{
    int i;
    int M[2][2] = {{1,1},{1,0}};

    // n - 1 times multiply the matrix to {{1,0},{0,1}}
    for (i = 2; i <= n; i++)
        multiply(F, M);
}

/* Driver program to test above function */
int main()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}
```

Java

```
class fibonacci
{
    static int fib(int n)
    {
        int F[][] = new int[][]{{1,1},{1,0}};
        if (n == 0)
            return 0;
        power(F, n-1);

        return F[0][0];
    }
}
```

```

/* Helper function that multiplies 2 matrices F and M of size 2*2, and
puts the multiplication result back to F[][] */
static void multiply(int F[][], int M[][])
{
    int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
    int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
    int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
    int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

    F[0][0] = x;
    F[0][1] = y;
    F[1][0] = z;
    F[1][1] = w;
}

/* Helper function that calculates F[][] raise to the power n and puts the
result in F[][]
Note that this function is designed only for fib() and won't work as general
power function */
static void power(int F[][], int n)
{
    int i;
    int M[][] = new int[][]{{1,1},{1,0}};

    // n - 1 times multiply the matrix to {{1,0},{0,1}}
    for (i = 2; i <= n; i++)
        multiply(F, M);
}

/* Driver program to test above function */
public static void main (String args[])
{
    int n = 9;
    System.out.println(fib(n));
}
}
/* This code is contributed by Rajat Mishra */

```

Python 3

```

# Helper function that multiplies
# 2 matrices F and M of size 2*2,
# and puts the multiplication
# result back to F[][]

# Helper function that calculates
# F[][] raise to the power n and
# puts the result in F[][]
# Note that this function is
# designed only for fib() and
# won't work as general
# power function
def fib(n):
    F = [[1, 1],
          [1, 0]]
    if (n == 0):
        return 0
    power(F, n - 1)

    return F[0][0]

def multiply(F, M):

    x = (F[0][0] * M[0][0] +
          F[0][1] * M[1][0])
    y = (F[0][0] * M[0][1] +
          F[0][1] * M[1][1])
    z = (F[1][0] * M[0][0] +
          F[1][1] * M[1][0])
    w = (F[1][0] * M[0][1] +
          F[1][1] * M[1][1])

    F[0][0] = x
    F[0][1] = y
    F[1][0] = z
    F[1][1] = w

def power(F, n):

```

```

M = [[1, 1],
      [1, 0]]

# n - 1 times multiply the
# matrix to {{1,0},{0,1}}
for i in range(2, n + 1):
    multiply(F, M)

# Driver Code
if __name__ == "__main__":
    n = 9
    print(fib(n))

# This code is contributed
# by ChitraNayal

```

C#

```

// C# program to find fibonacci number.
using System;

class GFG {

    static int fib(int n)
    {
        int [,]F = new int[,] {{1, 1},
                                {1, 0}};

        if (n == 0)
            return 0;
        power(F, n-1);

        return F[0,0];
    }

    /* Helper function that multiplies 2
    matrices F and M of size 2*2, and puts
    the multiplication result back to F[][] */
    static void multiply(int [,]F, int [,]M)
    {
        int x = F[0,0]*M[0,0] + F[0,1]*M[1,0];
        int y = F[0,0]*M[0,1] + F[0,1]*M[1,1];
        int z = F[1,0]*M[0,0] + F[1,1]*M[1,0];
        int w = F[1,0]*M[0,1] + F[1,1]*M[1,1];

        F[0,0] = x;
        F[0,1] = y;
        F[1,0] = z;
        F[1,1] = w;
    }

    /* Helper function that calculates F[][]
    raise to the power n and puts the result
    in F[][] Note that this function is designed
    only for fib() and won't work as general
    power function */
    static void power(int [,]F, int n)
    {
        int i;
        int [,]M = new int[,]{{1, 1},
                                {1, 0}};

        // n - 1 times multiply the matrix to
        // {{1,0},{0,1}}
        for (i = 2; i <= n; i++)
            multiply(F, M);
    }

    /* Driver program to test above function */
    public static void Main ()
    {
        int n = 9;
        Console.WriteLine(fib(n));
    }
}

// This code is contributed by anuj_67.

```

PHP

```
<?php
// PHP program for above approach
function fib($n)
{
    $F = array(array(1, 1),
                array(1, 0));
    if ($n == 0)
        return 0;
    power($F, $n - 1);

    return $F[0][0];
}

function multiply(&$F, &$M)
{
    $x = $F[0][0] * $M[0][0] +
        $F[0][1] * $M[1][0];
    $y = $F[0][0] * $M[0][1] +
        $F[0][1] * $M[1][1];
    $z = $F[1][0] * $M[0][0] +
        $F[1][1] * $M[1][0];
    $w = $F[1][0] * $M[0][1] +
        $F[1][1] * $M[1][1];

    $F[0][0] = $x;
    $F[0][1] = $y;
    $F[1][0] = $z;
    $F[1][1] = $w;
}

function power(&$F, $n)
{
    $M = array(array(1, 1),
                array(1, 0));

    // n - 1 times multiply the
    // matrix to {{1,0},{0,1}}
    for ($i = 2; $i <= $n; $i++)
        multiply($F, $M);
}

// Driver Code
$n = 9;
echo fib($n);

// This code is contributed
// by ChitraNayal
?>
```

Time Complexity: $O(n)$

Extra Space: $O(1)$

Method 5 (Optimized Method 4)

The method 4 can be optimized to work in $O(\log n)$ time complexity. We can do recursive multiplication to get $\text{power}(M, n)$ in the previous method (Similar to the optimization done in [this post](#))

C

```
#include <stdio.h>

void multiply(int F[2][2], int M[2][2]);

void power(int F[2][2], int n);

/* function that returns nth Fibonacci number */
int fib(int n)
{

```

```

int F[2][2] = {{1,1},{1,0}};
if (n == 0)
    return 0;
power(F, n-1);
return F[0][0];
}

/* Optimized version of power() in method 4 */
void power(int F[2][2], int n)
{
    if( n == 0 || n == 1)
        return;
    int M[2][2] = {{1,1},{1,0}};

    power(F, n/2);
    multiply(F, F);

    if (n%2 != 0)
        multiply(F, M);
}

void multiply(int F[2][2], int M[2][2])
{
    int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
    int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
    int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
    int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

    F[0][0] = x;
    F[0][1] = y;
    F[1][0] = z;
    F[1][1] = w;
}

/* Driver program to test above function */
int main()
{
    int n = 9;
    printf("%d", fib(9));
    getchar();
    return 0;
}

```

Java

```

//Fibonacci Series using Optimized Method
class fibonacci
{
    /* function that returns nth Fibonacci number */
    static int fib(int n)
    {
        int F[][] = new int[][]{{1,1},{1,0}};
        if (n == 0)
            return 0;
        power(F, n-1);

        return F[0][0];
    }

    static void multiply(int F[], int M[])
    {
        int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
        int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
        int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
        int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

        F[0][0] = x;
        F[0][1] = y;
        F[1][0] = z;
        F[1][1] = w;
    }

    /* Optimized version of power() in method 4 */
    static void power(int F[], int n)
    {
        if( n == 0 || n == 1)
            return;
        int M[] = new int[][]{{1,1},{1,0}};
    }
}

```

```

power(F, n/2);
multiply(F, F);

if (n%2 != 0)
    multiply(F, M);
}

/* Driver program to test above function */
public static void main (String args[])
{
    int n = 9;
    System.out.println(fib(n));
}
}
/* This code is contributed by Rajat Mishra */

```

Python 3

```

# Fibonacci Series using
# Optimized Method

# function that returns nth
# Fibonacci number
def fib(n):

    F = [[1, 1],
          [1, 0]]
    if (n == 0):
        return 0
    power(F, n - 1)

    return F[0][0]

def multiply(F, M):

    x = (F[0][0] * M[0][0] +
          F[0][1] * M[1][0])
    y = (F[0][0] * M[0][1] +
          F[0][1] * M[1][1])
    z = (F[1][0] * M[0][0] +
          F[1][1] * M[1][0])
    w = (F[1][0] * M[0][1] +
          F[1][1] * M[1][1])

    F[0][0] = x
    F[0][1] = y
    F[1][0] = z
    F[1][1] = w

# Optimized version of
# power() in method 4
def power(F, n):

    if( n == 0 or n == 1):
        return;
    M = [[1, 1],
          [1, 0]];

    power(F, n // 2)
    multiply(F, F)

    if (n % 2 != 0):
        multiply(F, M)

# Driver Code
if __name__ == "__main__":
    n = 9
    print(fib(n))

# This code is contributed
# by ChitraNayal

```

C#

```

// Fibonacci Series using
// Optimized Method

```

```

using System;

class GFG
{
    /* function that returns
    nth Fibonacci number */
    static int fib(int n)
    {
        int[,] F = new int[,]{{1, 1},
                               {1, 0}};

        if (n == 0)
            return 0;
        power(F, n - 1);

        return F[0, 0];
    }

    static void multiply(int[,] F,
                        int[,] M)
    {
        int x = F[0, 0] * M[0, 0] +
                F[0, 1] * M[1, 0];
        int y = F[0, 0] * M[0, 1] +
                F[0, 1] * M[1, 1];
        int z = F[1, 0] * M[0, 0] +
                F[1, 1] * M[1, 0];
        int w = F[1, 0] * M[0, 1] +
                F[1, 1] * M[1, 1];

        F[0, 0] = x;
        F[0, 1] = y;
        F[1, 0] = z;
        F[1, 1] = w;
    }

    /* Optimized version of
    power() in method 4 */
    static void power(int[,] F, int n)
    {
        if (n == 0 || n == 1)
            return;
        int[,] M = new int[,]{{1, 1},
                               {1, 0}};

        power(F, n / 2);
        multiply(F, F);

        if (n % 2 != 0)
            multiply(F, M);
    }

    // Driver Code
    public static void Main ()
    {
        int n = 9;
        Console.Write(fib(n));
    }
}

// This code is contributed
// by ChitraNayal

```

Time Complexity: $O(\log n)$

Extra Space: $O(\log n)$ if we consider the function call stack size, otherwise $O(1)$.

Method 6 ($O(\log n)$ Time)

Below is one more interesting recurrence formula that can be used to find n'th Fibonacci Number in $O(\log n)$ time.

If n is even then $k = n/2$:
 $F(n) = [2 * F(k-1) + F(k)] * F(k)$

If n is odd then $k = (n + 1)/2$:
 $F(n) = F(k) * F(k) + F(k-1) * F(k-1)$

How does this formula work?

The formula can be derived from above matrix equation.

$$\begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix}^n = \begin{pmatrix} F_{n+1} & F_n \\ F_n & F_{n-1} \end{pmatrix}.$$

Taking determinant on both sides, we get

$$(-1)^n = F_{n+1}F_{n-1} - F_n^2$$

Moreover, since $A^n A^m = A^{n+m}$ for any square matrix A, the following identities can be derived (they are obtained from two different coefficients of the matrix product)

$$F_m F_n + F_{m-1} F_{n-1} = F_{m+n-1}$$

By putting $n = n+1$,

$$F_m F_{n+1} + F_{m-1} F_n = F_{m+n}$$

Putting $m = n$

$$F_{2n-1} = F_n^2 + F_{n-1}^2$$

$$F_{2n} = (F_{n-1} + F_{n+1})F_n = (2F_{n-1} + F_n)F_n \text{ (Source: Wiki)}$$

To get the formula to be proved, we simply need to do following

If n is even, we can put $k = n/2$

If n is odd, we can put $k = (n+1)/2$

Below is the implementation of above idea.

C++

```
// C++ Program to find n'th fibonacci Number in
// with O(Log n) arithmetic operations
#include <bits/stdc++.h>
using namespace std;

const int MAX = 1000;

// Create an array for memoization
int f[MAX] = {0};

// Returns n'th fibonacci number using table f[]
int fib(int n)
{
    // Base cases
    if (n == 0)
        return 0;
    if (n == 1 || n == 2)
        return (f[n] = 1);

    // If fib(n) is already computed
    if (f[n])
        return f[n];

    int k = (n & 1)? (n+1)/2 : n/2;

    // Applying above formula [Note value n&1 is 1
    // if n is odd, else 0.
    f[n] = (n & 1)? (fib(k)*fib(k) + fib(k-1)*fib(k-1))
        : (2*fib(k-1) + fib(k))*fib(k);

    return f[n];
}

/* Driver program to test above function */
int main()
{
    int n = 9;
    printf("%d ", fib(n));
    return 0;
}
```

Java


```
// Java Program to find n'th fibonacci
// Number with O(Log n) arithmetic operations
import java.util.*;

class GFG {

    static int MAX = 1000;
    static int f[];

    // Returns n'th fibonacci number using
    // table f[]
    public static int fib(int n)
    {
        // Base cases
        if (n == 0)
            return 0;

        if (n == 1 || n == 2)
            return (f[n] = 1);

        // If fib(n) is already computed
        if (f[n] != 0)
            return f[n];

        int k = (n & 1) == 1 ? (n + 1) / 2
            : n / 2;

        // Applying above formula [Note value
        // n&1 is 1 if n is odd, else 0.
        f[n] = (n & 1) == 1 ? (fib(k) * fib(k) +
            fib(k - 1) * fib(k - 1))
            : (2 * fib(k - 1) + fib(k))
            * fib(k);

        return f[n];
    }

    /* Driver program to test above function */
    public static void main(String[] args)
    {
        int n = 9;
        f = new int[MAX];
        System.out.println(fib(n));
    }
}

// This code is contributed by Arnav Kr. Mandal.
```

Python

```
# Python 3 Program to find n'th fibonacci Number in
# with O(Log n) arithmetic operations
MAX = 1000

# Create an array for memoization
f = [0] * MAX

# Returns n'th fibonacci number using table f[]
def fib(n) :
    # Base cases
    if (n == 0) :
        return 0
    if (n == 1 or n == 2) :
        f[n] = 1
        return (f[n])

    # If fib(n) is already computed
    if (f[n]) :
        return f[n]

    if (n & 1) :
        k = (n + 1) // 2
    else :
        k = n // 2

    # Applying above formula [Note value n&1 is 1
    # if n is odd, else 0.
    if ((n & 1) ) :
        f[n] = (fib(k) * fib(k) + fib(k-1) * fib(k-1))
```

```

    else :
        f[n] = (2*fib(k-1) + fib(k))*fib(k)

    return f[n]

# Driver code
n = 9
print(fib(n))

# This code is contributed by Nikita Tiwari.

```

C#

```

// C# Program to find n'th
// fibonacci Number with
// O(Log n) arithmetic operations
using System;

class GFG
{
    static int MAX = 1000;
    static int[] f;

    // Returns n'th fibonacci
    // number using table f[]
    public static int fib(int n)
    {
        // Base cases
        if (n == 0)
            return 0;

        if (n == 1 || n == 2)
            return (f[n] = 1);

        // If fib(n) is already
        // computed
        if (f[n] != 0)
            return f[n];

        int k = (n & 1) == 1 ? (n + 1) / 2
                           : n / 2;

        // Applying above formula
        // [Note value n&1 is 1 if
        // n is odd, else 0.
        f[n] = (n & 1) == 1 ? (fib(k) * fib(k) +
                             fib(k - 1) * fib(k - 1))
                           : (2 * fib(k - 1) + fib(k)) *
                             fib(k);

        return f[n];
    }

    // Driver Code
    static void Main()
    {
        int n = 9;
        f = new int[MAX];
        Console.WriteLine(fib(n));
    }
}

// This code is contributed by mits

```

PHP

```

<?php
// PHP Program to find n'th
// fibonacci Number in with
// O(Log n) arithmetic operations

$MAX = 1000;

```

```
// Returns n'th fibonacci
// number using table f[]
function fib($n)
{
    global $MAX;

    // Create an array for memoization
    $f = array_fill(0, $MAX, NULL);

    // Base cases
    if ($n == 0)
        return 0;
    if ($n == 1 || $n == 2)
        return ($f[$n] = 1);

    // If fib(n) is already computed
    if ($f[$n])
        return $f[$n];

    $k = ($n & 1) ? ($n + 1) / 2 : $n / 2;

    // Applying above formula
    // [Note value n&1 is 1 if
    // n is odd, else 0.
    $f[$n] = ($n & 1) ? (fib($k) * fib($k) +
                        fib($k - 1) * fib($k - 1)) :
                (2 * fib($k - 1) + fib($k)) * fib($k);

    return $f[$n];
}

// Driver Code
$n = 9;
echo fib($n);

// This code is contributed
// by ChitraNayal
?>
```

Output :

34

Time complexity of this solution is $O(\log n)$ as we divide the problem to half in every recursive call.

Method 7

Another approach:(Using formula)

In this method we directly implement the formula for nth term in the fibonacci series.

$$F_n = \{[(\sqrt{5} + 1)/2]^n\} / \sqrt{5}$$

Reference: <http://www.maths.surrey.ac.uk/hosted-sites/R.Knott/Fibonacci/fibFormula.html>

C++

```
// C++ Program to find n'th fibonacci Number
#include<iostream>
#include<cmath>

int fib(int n) {
    double phi = (1 + sqrt(5)) / 2;
    return round(pow(phi, n) / sqrt(5));
}

// Driver Code
int main ()
{
    int n = 9;
    std::cout << fib(n) << std::endl;
    return 0;
}

//This code is contributed by Lokesh Mohanty.
```

C

```
// C Program to find n'th fibonacci Number
#include<stdio.h>
#include<math.h>
int fib(int n) {
    double phi = (1 + sqrt(5)) / 2;
    return round(pow(phi, n) / sqrt(5));
}
int main ()
{
    int n = 9;
    printf("%d", fib(n));
    return 0;
}
```

Java

```
// Java Program to find n'th fibonacci Number
import java.util.*;

class GFG {

    static int fib(int n) {
        double phi = (1 + Math.sqrt(5)) / 2;
        return (int) Math.round(Math.pow(phi, n)
                                / Math.sqrt(5));
    }

    // Driver Code
    public static void main(String[] args) {
        int n = 9;
        System.out.println(fib(n));
    }
}
// This code is contributed by PrinciRaj1992
```

C#

```
// C# Program to find n'th fibonacci Number
using System;

public class GFG
{
    static int fib(int n)
    {
        double phi = (1 + Math.Sqrt(5)) / 2;
        return (int) Math.Round(Math.Pow(phi, n)
                                / Math.Sqrt(5));
    }

    // Driver code
    public static void Main()
    {
        int n = 9;
        Console.WriteLine(fib(n));
    }
}

// This code is contributed by 29AjayKumar
```

PHP

```
<?php
// PHP Program to find n'th
// fibonacci Number

function fib($n)
{
    $phi = (1 + sqrt(5)) / 2;
    return round(pow($phi, $n) / sqrt(5));
}

// Driver Code
$n = 9;
echo fib($n) ;
```

```
// This code is contributed by Ryuga
?>
```

Output:

34

Time Complexity: $O(1)$ **Space Complexity:** $O(1)$

Program for Fibonacci numbers using Dynamic Programming | Geeksfor...



This method is contributed by Chirag Agarwal.

Related Articles:[Large Fibonacci Numbers in Java](#)

Please write comments if you find the above codes/algorithms incorrect, or find other ways to solve the same problem.

References:http://en.wikipedia.org/wiki/Fibonacci_number<http://www.ics.uci.edu/~epstein/161/960109.html>**Recommended Posts:**[C Program for Fibonacci numbers](#)[Program to print first n Fibonacci Numbers | Set 1](#)[Non Fibonacci Numbers](#)[GCD and Fibonacci Numbers](#)[Even Fibonacci Numbers Sum](#)[Sum of Fibonacci Numbers](#)[Sum of squares of Fibonacci numbers](#)[Alternate Fibonacci Numbers](#)[Prime numbers and Fibonacci](#)[Sum of Fibonacci Numbers in a range](#)[Find the sum of first N odd Fibonacci numbers](#)[The Magic of Fibonacci Numbers](#)[Interesting facts about Fibonacci numbers](#)[Sum of Fibonacci Numbers with alternate negatives](#)[Find the GCD of N Fibonacci Numbers with given Indices](#)

Improved By : [jit_t](#), [vt_m](#), [humblezero](#), [Mithun Kumar](#), [Ita_c](#), [more](#)

Article Tags : [Dynamic Programming](#) [Mathematical](#) [Amazon](#) [Bloomberg](#) [Fibonacci](#) [MakeMyTrip](#) [MAQ Software](#) [matrix-exponentiation](#)

[Modular Arithmetic](#) [series](#)

Practice Tags : [Amazon](#) [MakeMyTrip](#) [MAQ Software](#) [Bloomberg](#) [Dynamic Programming](#) [Mathematical](#) [series](#) [Fibonacci](#) [Modular Arithmetic](#)



61

☐ To-do ☐ Done

3

Based on 303 vote(s)

[Feedback/ Suggest Improvement](#)[Notes](#)[Improve Article](#)

Please write to us at contribute@geeksforgeeks.org to report any issue with the above content.

Writing code in comment? Please use ide.geeksforgeeks.org, generate link and share the link here.

[Load Comments](#)

A computer science portal for geeks

5th Floor, A-118,
Sector-136, Noida, Uttar Pradesh - 201305
feedback@geeksforgeeks.org

COMPANY

[About Us](#)
[Careers](#)
[Privacy Policy](#)
[Contact Us](#)

PRACTICE

[Courses](#)
[Company-wise](#)
[Topic-wise](#)
[How to begin?](#)

LEARN

[Algorithms](#)
[Data Structures](#)
[Languages](#)
[CS Subjects](#)
[Video Tutorials](#)

CONTRIBUTE

[Write an Article](#)
[Write Interview Experience](#)
[Internships](#)
[Videos](#)