

2.2 Denote the events:

$$\begin{aligned}M &= \{ \text{problems with a motherboard} \} \\H &= \{ \text{problems with a hard drive} \}\end{aligned}$$

We have:

$$P\{M\} = 0.4, \quad P\{H\} = 0.3, \quad \text{and} \quad P\{M \cap H\} = 0.15.$$

Hence,

$$P\{M \cup H\} = P\{M\} + P\{H\} - P\{M \cap H\} = 0.4 + 0.3 - 0.15 = 0.55,$$

and

$$P\{\text{fully functioning MB and HD}\} = 1 - P\{M \cup H\} = \boxed{0.45}$$

2.4 Denote the events,

$$C = \{ \text{knows C/C++} \}, \quad F = \{ \text{knows Fortran} \}.$$

Then

$$(a) \quad P\{\bar{F}\} = 1 - P\{F\} = 1 - 0.6 = \boxed{0.4}$$

$$\begin{aligned}(b) \quad P\{\bar{F} \cap \bar{C}\} &= 1 - P\{F \cup C\} = 1 - (P\{F\} + P\{C\} - P\{F \cap C\}) \\&= 1 - (0.7 + 0.6 - 0.5) = 1 - 0.8 = \boxed{0.2}\end{aligned}$$

$$(c) \quad P\{C \setminus F\} = P\{C\} - P\{F \cap C\} = 0.7 - 0.5 = \boxed{0.2}$$

$$(d) \quad P\{F \setminus C\} = P\{F\} - P\{F \cap C\} = 0.6 - 0.5 = \boxed{0.1}$$

$$(e) \quad P\{C \mid F\} = \frac{P\{C \cap F\}}{P\{F\}} = \frac{0.5}{0.6} = \boxed{0.8333}$$

$$(f) \quad P\{F \mid C\} = \frac{P\{C \cap F\}}{P\{C\}} = \frac{0.5}{0.7} = \boxed{0.7143}$$

2.6 Let $A = \{\text{arrive on time}\}$, $W = \{\text{good weather}\}$. We have

$$P\{A \mid W\} = 0.8, \quad P\{A \mid \bar{W}\} = 0.3, \quad P\{W\} = 0.6$$

By the Law of Total Probability,

$$\begin{aligned}P\{A\} &= P\{A \mid W\}P\{W\} + P\{A \mid \bar{W}\}P\{\bar{W}\} \\&= (0.8)(0.6) + (0.3)(0.4) = \boxed{0.60}\end{aligned}$$

2.8 Let $A_1 = \{\text{1st device fails}\}$, $A_2 = \{\text{2nd device fails}\}$, $A_3 = \{\text{3rd device fails}\}$.

$$\begin{aligned}
 P\{\text{on time}\} &= P\{\text{all function}\} \\
 &= P\{\bar{A}_1 \cap \bar{A}_2 \cap \bar{A}_3\} \\
 &= P\{\bar{A}_1\} P\{\bar{A}_2\} P\{\bar{A}_3\} \quad (\text{independence}) \\
 &= (1 - 0.01)(1 - 0.02)(1 - 0.02) \quad (\text{complement rule}) \\
 &= \boxed{0.9508}
 \end{aligned}$$

2.9 $P\{\text{at least one fails}\} = 1 - P\{\text{all work}\} = 1 - (.96)(.95)(.90) = \boxed{0.1792}$.

2.10 $P\{A \cup B \cup C\} = 1 - P\{\bar{A} \cap \bar{B} \cap \bar{C}\} = 1 - P\{\bar{A}\} P\{\bar{B}\} P\{\bar{C}\}$
 $= 1 - (1 - 0.4)(1 - 0.5)(1 - 0.2) = \boxed{0.76}$

2.15 Let $A = \{\text{Error in the 1st block}\}$ and $B = \{\text{Error in the 2nd block}\}$. Then $P\{A\} = 0.2$, $P\{B\} = 0.3$, and $P\{A \cap B\} = 0.06$ by independence;
 $P\{\text{error in program}\} = P\{A \cup B\} = 0.2 + 0.3 - 0.06 = 0.44$.

Then, by the definition of conditional probability,

$$P\{A \cap B \mid A \cup B\} = \frac{P\{A \cap B\}}{P\{A \cup B\}} = \frac{0.06}{0.44} = \boxed{0.1364}$$

Or, by the Bayes Rule,

$$\begin{aligned}
 P\{A \cap B \mid A \cup B\} &= \frac{P\{A \cup B \mid A \cap B\} P\{A \cap B\}}{P\{A \cup B\}} \\
 &= \frac{(1)(0.06)}{0.44} = \boxed{0.1364}
 \end{aligned}$$

2.17 Let $D = \{\text{defective part}\}$. We are given:

$$\begin{array}{l|l}
 P\{X\} = 0.24 & P\{D|X\} = 0.05 \\
 P\{Y\} = 0.36 & P\{D|Y\} = 0.10 \\
 P\{Z\} = 0.40 & P\{D|Z\} = 0.06
 \end{array}$$

Combine the Bayes Rule and the Law of Total Probability.

$$\begin{aligned}
 P\{Z \mid D\} &= \frac{P\{D|Z\} P\{Z\}}{P\{D|X\} P\{X\} + P\{D|Y\} P\{Y\} + P\{D|Z\} P\{Z\}} \\
 &= \frac{(0.06)(0.40)}{(0.05)(0.24) + (0.10)(0.36) + (0.06)(0.40)} \\
 &= \boxed{1/3 \text{ or } 0.3333}
 \end{aligned}$$

2.19 Let $D = \{\text{defective part}\}$ and $I = \{\text{inspected electronically}\}$. By the Bayes Rule,

$$\begin{aligned}P\{I|D\} &= \frac{P\{D|I\}P\{I\}}{P\{D|I\}P\{I\} + P\{D|\bar{I}\}P\{\bar{I}\}} \\&= \frac{(1 - 0.95)(0.20)}{(1 - 0.95)(0.20) + (1 - 0.7)(1 - 0.20)} = \boxed{0.0400}\end{aligned}$$