

# Computer Organization

## UNIT-1

Basic structure of Computers :-

Computer Types, Functional unit, \* Basic operational concepts, \* Bus structures.

Data Representation :-

\* Data Types, \* complements, Fixed point Representation, \* Floating point representation, other Binary Codes, Error Detection codes.

Computer Arithmetic :-

Addition and subtraction, \* Multiplication Algorithms, \* Division Algorithms, Floating point Arithmetic operations.

## UNIT-2 :-

Register Transfer language and Micro-operations:-

Register Transfer Language, Register Transfer Bus and Memory Transfers, Arithmetic Micro-operations, logic Micro-operations, shift Micro-~~op~~ operations, Arithmetic logic shift unit.

## UNIT-3:-

Basic organisation and Design :-

Instruction Codes, Computer Register Computer Instructions, Timing and control, Instruction cycle, Memory - Reference Instructions, Input-output and Interrupt, Design of Basic Computer, Design of Accumulator logic.

## UNIT-4:-

Central Processing Unit :-

General Register organization, stack organization, Instruction Formats, Addressing Modes, Data Transfer and Manipulation, program Control, Reduced Instruction set computer.

Micro programmed Control :-

Control Memory, Address sequencing, Micro program Example, Design of control.

## UNIT-5:-

The Memory System :-

Memory hierarchy, Main Memory, Auxiliary Memory, Associative Memory, Cache

Memory, Virtual Memory,

Input-output Devices :-

Peripheral Devices, Input-Output Interface,  
Asynchronous Data Transfer, Modes of Transfer,  
Priority Interrupts, Direct Memory Access.

Multiprocessors :-

Introduction, characteristic of Multi processors,  
Interconnection ~~system~~ structure, Inter processor  
Arbitration.

(1) Define Computer Architecture?

(A) Computer architecture is a set of rules & methods that describe the functionality, organization and implementation of computer systems.

The architecture of a system refers of its structure in terms of separately specified components of that system & their inter relationships.

(2) Define Computer Organization?

(A) The computer organization is concerned with the structure and behaviour of digital computers and behaviour of a computer system as seen by the user. It acts as the interface b/w hardware & software. It deals with the components of a connection in a system.

(3) Define Complements? Discuss 1's complement, 9's complements, 9's complement & 10's complement.

(A) The number derived by subtracting a number from a base number. Complements are used in the digital computers in order to simplify the subtraction operation and for the logical manipulations.

One's complement:- The one's complement of a binary number is defined as the value obtained by inverting all the bits in the binary representation of the number [swapping 0's for 1's and vice-versa].

Ex:-  $00110010 = 50$

1's complement of 50 is 11001101

Two's complement:

The two's complement of a binary number is defined as the value obtained by adding 1 to one's complement.

$$2^{\text{'s}} \text{ complement} = (\text{1's complement}) + 1$$

Ex:-  $50 = 00110010$       1's comp - 11001101

$$\begin{array}{r} 2^{\text{'s}} \text{ comp} - 1^{\text{'s}} \text{ comp} \\ + 1 \\ \hline \end{array}$$

$$\begin{array}{r}
 11001101 \\
 +1 \\
 \hline
 11001110
 \end{array}$$

9's complement :- The 9's complement of a number is calculated by subtracting each digit of the number by 9.

Ex :- 9's comp of 1423

$$\begin{array}{r}
 9999 \\
 -1423 \\
 \hline
 8576
 \end{array}$$

10's complement :- The 10's complement of a number is calculated by subtracting each digit by 9 and then adding 1 to the result.

Ex :- 10's comp of 1423 is

$$\begin{array}{r}
 9999 \\
 -1423 \\
 \hline
 8576
 \end{array}$$

$$\begin{array}{r}
 8576 \\
 +1 \\
 \hline
 8577
 \end{array}$$

## UNIT-1

### BASIC STRUCTURE OF COMPUTERS

#### Computer Types :-

Digital Computer (or) a computer is a fast calculating machine that accepts digitized coded input information process that stored information produces results as output.

\* program is a set of instructions [stored] which are stored in a memory with specified address.

\* we broadly classify computer types as follows:

(1) personal computer / desktop computer.

(2) portable notebook computer.

(3) work stations

(4) Enterprise system (or) Mainframes (or) Servers

(5) Super computers.

\* personal computer :-

processor, storage unit, visual display unit, audio video output unit, keyboard unit etc.

storage media.

\* work stations :- It is also a single user

computer system, similar to personal computer however has a more powerful processor.

micro work station Computers used for scientific or technical calculations [high end computers].

Main Frames :- [low-end computers]

Main Frame is a very large in size & is an expressive computer capable of supporting hundreds (or) even thousands of users simultaneously. Main Frame executes many programs concurrently. Generally used in applications as pay roll computation, accounting, business transactions, Engineering and Scientific Computations.

\* Super Computers :-

Super Computers are one of the fastest computer currently available.

Very expensive & are employed for specialized application that require immense amount of mathematical calculations. Generally used for weather forecasting, aircraft design, scientific simulations, (animated) graphics, fluid dynamic calculations, nuclear energy research,

electronic design and analysis of geological data.

\* Difference b/w Mainframe and Super Computer and Workstation :-

### Super Work Computer

1. Super Computers are used for large & complex mathematical computations.

2. Super Computer's speed is more than mainframe computer.

3. It can execute billions of instructions within a second.

4. largest computer

5. Heavy / high cost

6. These have Linux &

### Mainframe Computer

1. Mainframe computers are used to act as a storage for large database and serve as a maximum no. of users simultaneously.

2. Mainframe Computer's speed is comparatively less than Super Computer.

3. Millions of instructions are executed simultaneously.

4. Smaller than Super Computer size.

5. less cost than Super computer.

6. These have multiple

their operating systems. operating systems.

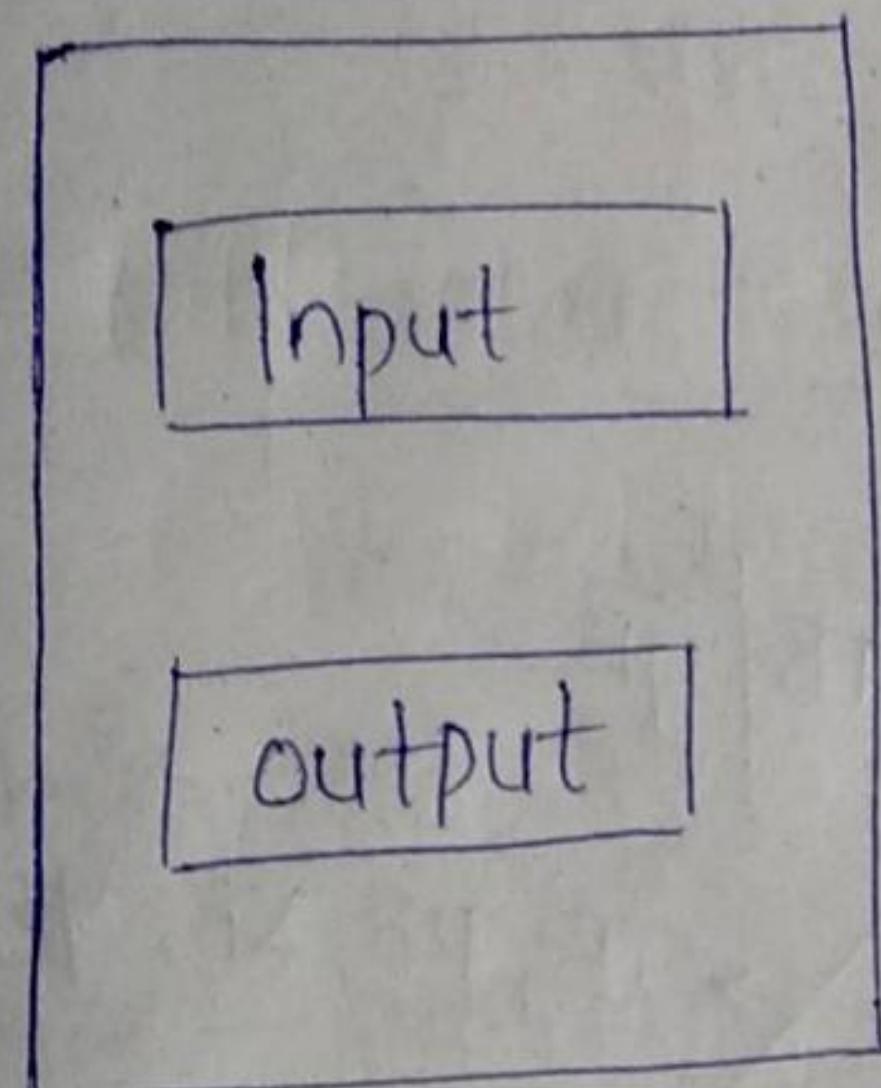
Variant

7. These are mostly purpose built for one or a few specific institutional tasks.
7. These are built to handle a large variety of tasks.
8. Seymour Cray invented the this computer.
8. Invented by IBM.
9. These can have a processing speed in the range of 100 to 900 MIPS.
9. Range of 3-4 MIPS to as high as 100 MIPS.

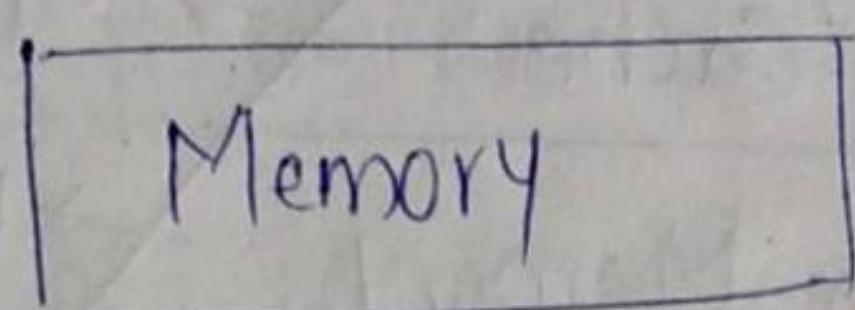
#### \* Workstation Computer :-

Desktop computer, normally more powerful than a normal pc and often dedicated to a specific task, such as an area, at a workplace, for a single worker.

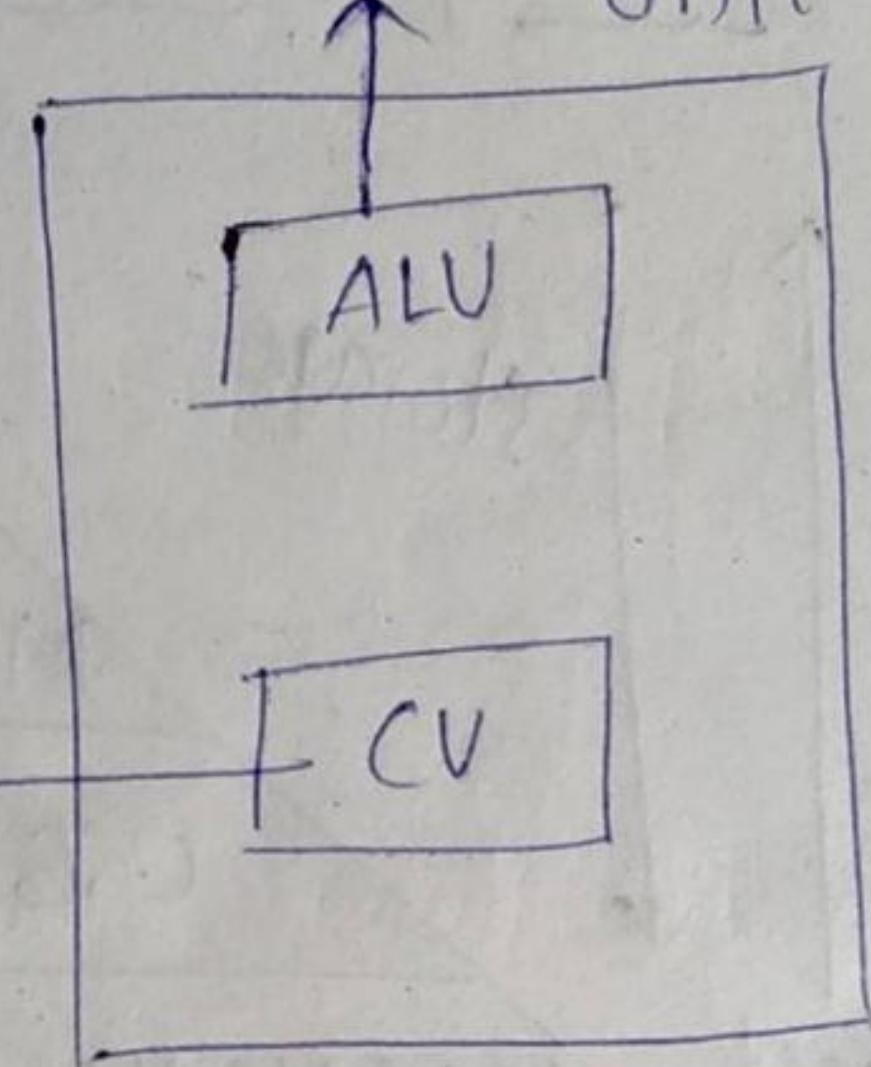
## Functional Units



I/O Unit



Control unit



processor

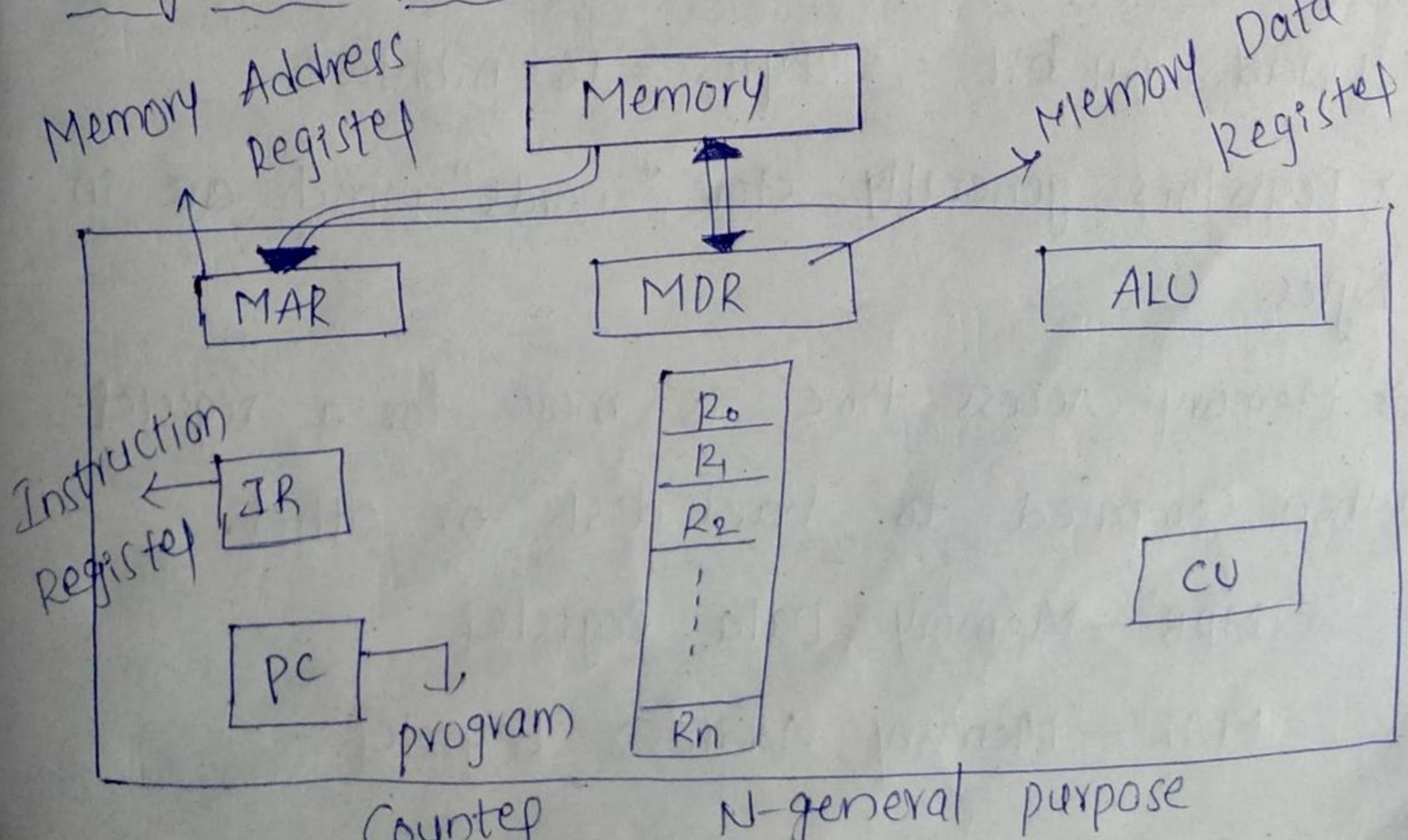
→ Address, stroage, memory & locations are same.

## \* Von-heumon Architecture :-

If the device has memory & processor then it is a computer didn't focus on input and output.

## \* Basic operational Concept :-

### N-general purpose Register :-



memory + processor

Memory Data  
Register

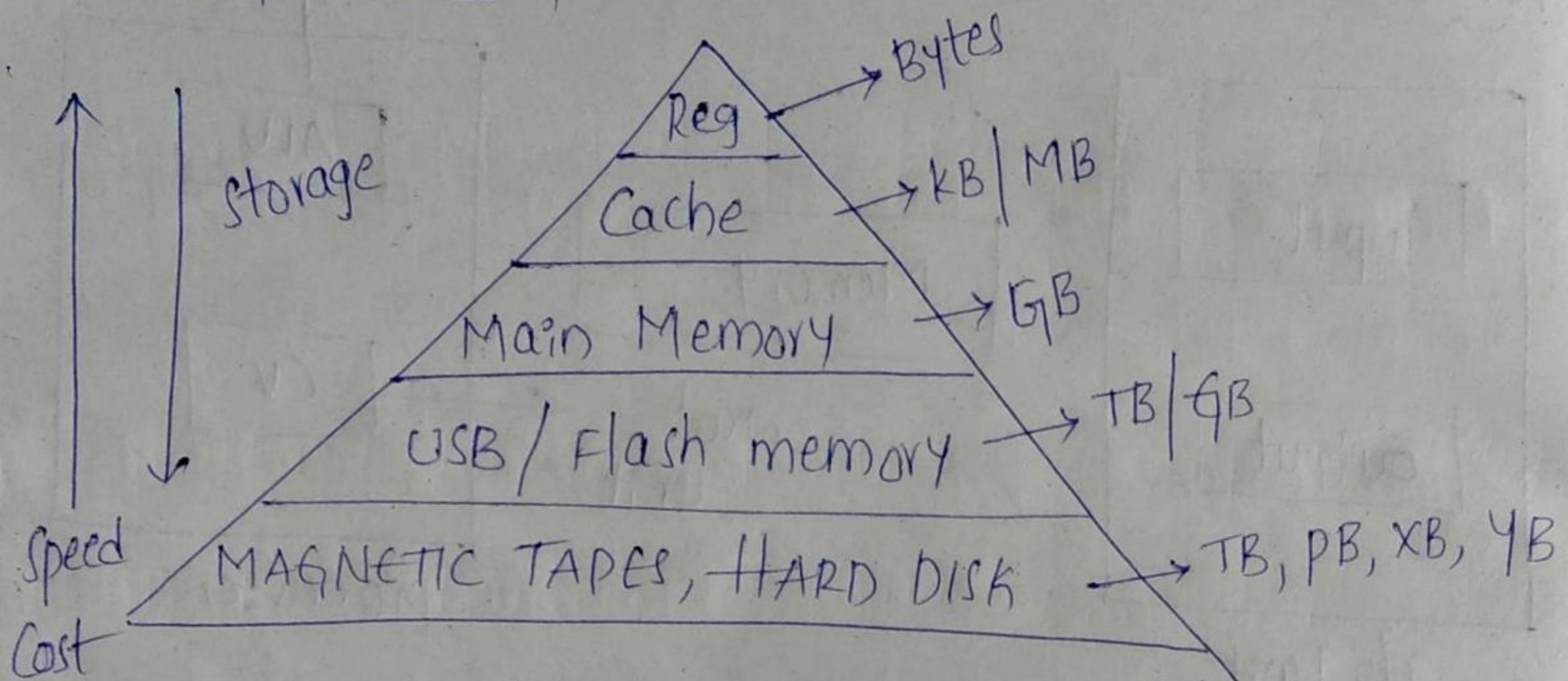
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CU

R<sub>0</sub>  
R<sub>1</sub>  
R<sub>2</sub>  
!  
R<sub>n</sub>

N-general purpose

## \* Memory Hierarchy :-



For a 32-bit processor 1 word is 8 nibble.

$$1 \text{ word} = 32 \text{ bit}$$

$$1 \text{ byte} = 8 \text{ bits}$$

$$1 \text{ nibble} = 4 \text{ bits}$$

Note :-

$$1 \text{ Byte} = 8 \text{ bits}$$

$$1 \text{ Nibble} = 4 \text{ bits}$$

32-bit processor :-

$$1 \text{ word} = 32 \text{ bit} = 4 \text{ bytes} = 8 \text{ nibbles}$$

64-bit processor :-

$$1 \text{ word} = 64 \text{ bit} = 8 \text{ bytes} = 16 \text{ nibbles.}$$

→ Registers generally store "words" which are in bytes.

→ Memory Access time is more for a register when compared to hard disk or other.

MDR - Memory Data Register

MAR - Memory Address Register.

- \* MDR is used for storing memory.
- \* MAR is used for storing Address.
- \* IR - Instruction Register :-

The address of the current executing instruction.

- \* PC - Program Counter :-

It will define the address of the next instruction which is yet to execute.

(i)

$\boxed{\text{ADD } R_0, R_1}$

(ii)

$\boxed{\begin{array}{l} \text{MOV Loc A, } R_0 \\ \text{ADD } R_0, R_1 \end{array}}$

(iii)

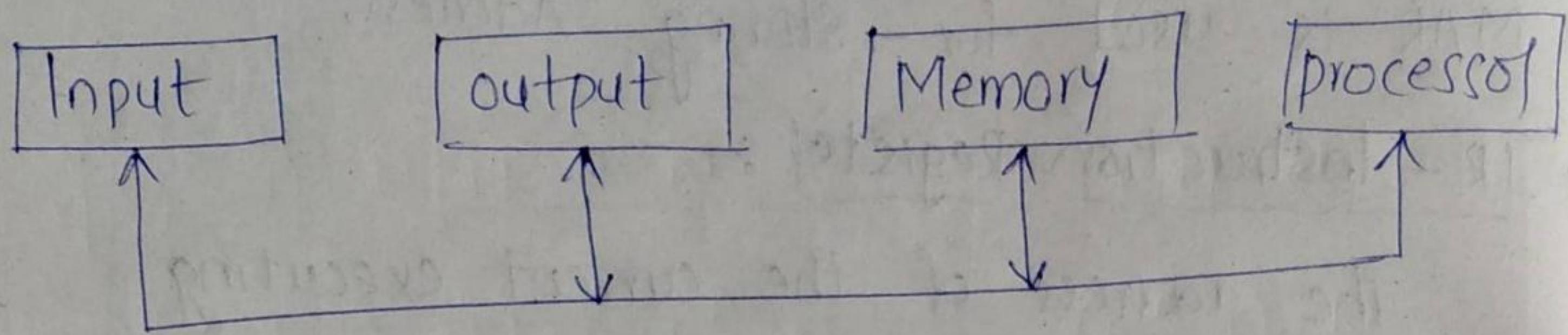
$\boxed{\begin{array}{l} \text{MOV Loc A, } R_0 \\ \text{MOV Loc B, } R_1 \\ \text{ADD } R_1, R_0 \end{array}}$

(i) Content of  $R_0$  &  $R_1$  are added, the result is stored in  $R_1$ .

(ii) Content in the location A is copied to  $R_0$  and the content of  $R_0$  &  $R_1$  are added and the result is stored in  $R_1$ .

(iii) Content in the location A is copied to the  $R_0$  & the content in the location B is copied to the  $R_1$  and the contents of both  $R_0$  and  $R_1$  are added and result is added to the  $R_0$ .

BUS :-



Single Bus :- Transfer of data in only one way.

Multi Bus :- Transfer of data in multiple ways.

#### \* Data Representation :-

Data Types :- Numbers, Alphabets, Special symbols, characters.

#### Number System :-

(1)  $r=2$ , Binary Number System

(2)  $r=10$ , Decimal Number System

(3)  $r=8$ , Octal Number System

(4)  $r=16$ , Hexa Decimal Number System.

$$*(FED)_{16} = (?)_{10}$$

$$(15 \ 14 \ 13)_{16} = (?)_{10}$$

$$15 \times 16^2 + 14 \times 16^1 + 13 \times 16^0$$

$$= 15 \times 256 + 14 \times 16 + 13$$

$$= 3,840 + 224 + 13 = (4077)_{10}$$

$$*(4077)_{10} = (\quad)_2$$

$$= (11111101101)_2$$

$$*(11111101101)_2 = (\quad)_8$$

$$(111 \underline{1101101})_2$$

$$(7755)_8$$

$$*(\underset{B}{A05\textcircled{H}1})_{16} - (\quad)_{10}$$

$$(10 \ 0 \ 5 \ 11 \ 1)_16$$

$$10 \times 16^4 + 0 \times 16^3 + 5 \times 16^2 + 11 \times 16^1 + 1 \times 16^0 = 656817$$

$$655360 + 0 + 1280 + 176 + 1 = 6,56,817$$

$$(656817)_{10}$$

$$*(656817)_{10} = (\quad)_2$$

$$(10100000011110110001)_2$$

$$(101\underline{0000011110110001})_2$$

$$(2403661)_8$$

====

$$\begin{array}{r} 2 | 4077 \\ 2 | 2038-1 \\ 2 | 1019-0 \\ 2 | 509-1 \\ 2 | 254-1 \\ 2 | 127-0 \\ 2 | 63-1 \\ 2 | 31-1 \\ 2 | 15-1 \\ 2 | 7-1 \\ 2 | 3-1 \uparrow \\ 1-1 \end{array}$$

$$\begin{array}{r} 2 | 656817 \\ 2 | 328408-1 \\ 2 | 164204-0 \\ 2 | 82102-0 \\ 2 | 41051-0 \\ 2 | 20525-1 \\ 2 | 10262-1 \\ 2 | 5131-0 \\ 2 | 2566-1 \\ 2 | 1283-1 \\ 2 | 641-1 \\ 2 | 320-1 \\ 2 | 160-0 \\ 2 | 80-0 \\ 2 | 40-0 \\ 20-0 \end{array}$$

$$\begin{array}{r} 2 | 20 \\ 2 | 10-0 \\ 2 | 5-0 \\ 2 | 2-1 \\ 1-0 \end{array} \uparrow$$

## \* Complements :-

r's

$$r : [(r^n - 1) - N] + 1 = r^n - N$$

(r-1)'s

$$(r^n - 1) - N$$

$$r=10 : [(10^n - 1) - N] + 1 = 10^n - N$$

$$(10^n - 1) - N$$

$$r=2 : [(2^n - 1) - N] + 1 = 2^n - N$$

$$(2^n - 1) - N$$

2's complement

1's complement

10's

9's

Complement

Complement

N = Number in number system

n = no. of digits in N

r = radix (or) Base

$$* (342607978)_{10} \quad n=9, \quad r=10$$

$$[(10^9 - 1) - 342607978] + 1 = 10^9 - 342607978$$

$$[999999999 - 342607978] + 1 = 1000000000 - 342607978$$

$$\underline{657392022} = 657392022$$

9's complement :-

$$(10^9 - 1) - N$$

$$999999999 - 342607978$$

$$= 657392021 + 1 = \underline{\underline{657392022}}$$

## \* Subtraction of unsigned number :-

The direct method of subtraction uses the borrow's concepts. The subtraction of 'n' digit unsigned number  $(M-N)$   $N \neq 0$  in base are can be done as follows:-

\* → Add the minend 'm' to the r's complement of the subtracted n. This performs

$$(m+r^n-N) = M-N+r^n$$

→ If  $M > N$  the sum will produce an end carry  $r^n$  which is discarded and what is left in result  $M-N$ .

→ If  $M < N$  the sum doesn't produce an end carry is equal to  $r^n-(N-M)$  which is the r's complement of  $(N-M)$ .

For example:-

$$72532 - 13250$$

The 10's complement of 13250 is

$$99999 - 13250 = 86749 + 1 = 86750$$

$$M = 72532$$

$$10\text{'s complement } N = 86750$$

$$\begin{array}{r} 72532 \\ 86750 \\ \hline 159282 \end{array}$$

discard end carry  $10^5 = 100000$

Answer - 59282

For eg:-  $M < N$  i.e.,  $13250 - 79532$

M N

Produces negative 59282

$M = 13250$

10's comp N = 27468

Sum = 40718

$$\begin{array}{r} 99999 \\ 40718 \\ \hline 59281 \\ +1 \\ \hline 59282 \end{array}$$

There is no end. carry . Answer is negative

$59282 = 10's \text{ complement of } 40718.$

### \* Binary Numbers :-

$$x = 1010100 \quad \& \quad y = 1000011$$

$$x = 1010100$$

$$2's \text{ Complement} \rightarrow y = 0111101$$

$$x-y$$

$$\text{Sum} = 10010001$$

$$\text{Discard Carry } 2^x = \frac{-10000000}{0010001}$$

## \* Fixed point Representation:-

There are two ways; we are going to represent the position of the binary point in a register.

(i) Fixed position.

(ii) Floating point Representation.

\* Fixed point method assumes that the binary point is always fixed in one position.

The two positions most widely used as

(1) A binary point in one extreme left of the register to make the stored number a fraction.

(2) A binary point in the extreme right of the register to make the stored number as an integer.

Integer Representation: +ve = 0 } sum bit  
-ve = 1

when an integer binary number is +ve the sign is represented by 0 and the

magnitude by a five binary number when an integer binary number when an integer binary number is negative the sign is represented by '1' but the rest of the number may be represented is one of three possible ways.

(1) signed magnitude Representation.

(2) signed - 1's complement

(3) signed - 2's complement

The signed magnitude representation of a negative number consists of the magnitude and a negative sign. Remaining 2, we are going to perform either 1's or 2's complement.

For example:-

$+14 = 00001110$  - 8 bit Register

left most bits are zero is 8 bit register.

$*14$  can be represent in 3 ways.

→ The signed magnitude representation of  $-14$  is obtained from  $+14$  by complementing only the sign bit  $[-14 = 10001110]$  → sign

magnitude.

→ The signed 1's complement Representation of -14 is obtained by Complementing all the bits of +14, including the sign bit

$$[-14 = 11110001]$$

→ The signed 2's complement is obtained by taking the 2's complement of the positive number, including its sign bit.

$$[-14 = 11110001 + 1 = 11110010]$$

#### \* Arithmetic Addition:-

→ The addition of 2 numbers in the signed magnitude system borrows the rules.

→ If the signs are the same, we add the magnitudes and give the sum the common sign.

→ If the signs are different, we subtract the smaller magnitude from the larger and give the result the sign of the larger.

$$\begin{array}{r}
 +6 = 00000110 \\
 +13 = 00001101 \\
 \hline
 +19 = 00010011
 \end{array}
 \quad
 \begin{array}{r}
 -6 = 11111010 \\
 +13 = 00001101 \\
 \hline
 +7 = 00000111
 \end{array}$$

$$\begin{array}{r}
 +6 = 00000110 \\
 -13 = 11110011 \\
 \hline
 -7 = 11111001
 \end{array}
 \quad
 \begin{array}{r}
 -6 = 11111010 \\
 -13 = 11110011 \\
 \hline
 -19 = 11101011
 \end{array}$$

In each and every case, we are going to perform only addition.

If there is any negative value, the total result will be the 2's complement value.

### \* Arithmetic Subtraction :-

Subtraction of two signed binary numbers when negative numbers are in 2's complement form is very simple.

→ Take the 2's complement of the subtraction (concluding the sign bit) and add it to the minuend (including the sign bit). A carry out of the sign bit

position is discarded.

→ A subtraction operation can be changed to an addition operation if the sign of the subtracted is changed.

This can be demonstrated through the relationship.

$$(\pm A) - (+B) = (\pm A) + (-B)$$

$$(\pm A) - (-B) = (\pm A) + (-B)$$

But changing a positive number to a negative number is easily done by taking its 2's complement the reverse is also true.

## \* Floating Point Representation :-

Signed +  $m^s$  = Floating point representation  
[ $m \times r^e$ ]

where  $m^s$  = mantissa

$e$  = exponent

$r$  = radix (or) base.

Ex:- Decimal number :- +6132.789 ( $r=10$ )

Floating point representation :-  $0.6132789 \times 10^4$

[ $m \times r^e$ ])

↓                            ↓  
Fraction                    exponent

+0.6132789            +04  
(m)                    (e)

Ex:- 2

Binary number :- +10011.11 ( $r=2$ )

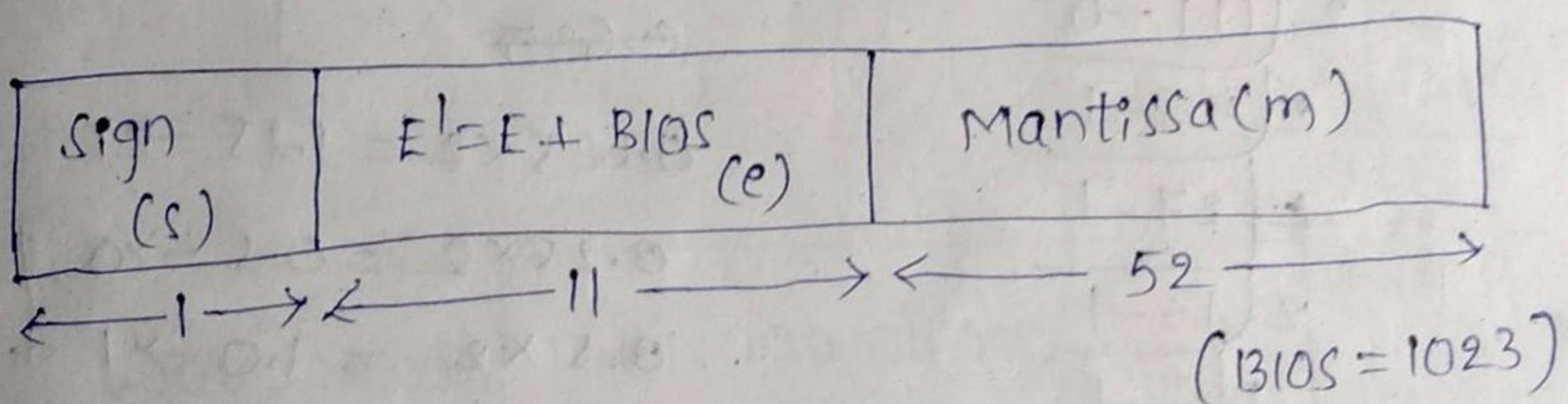
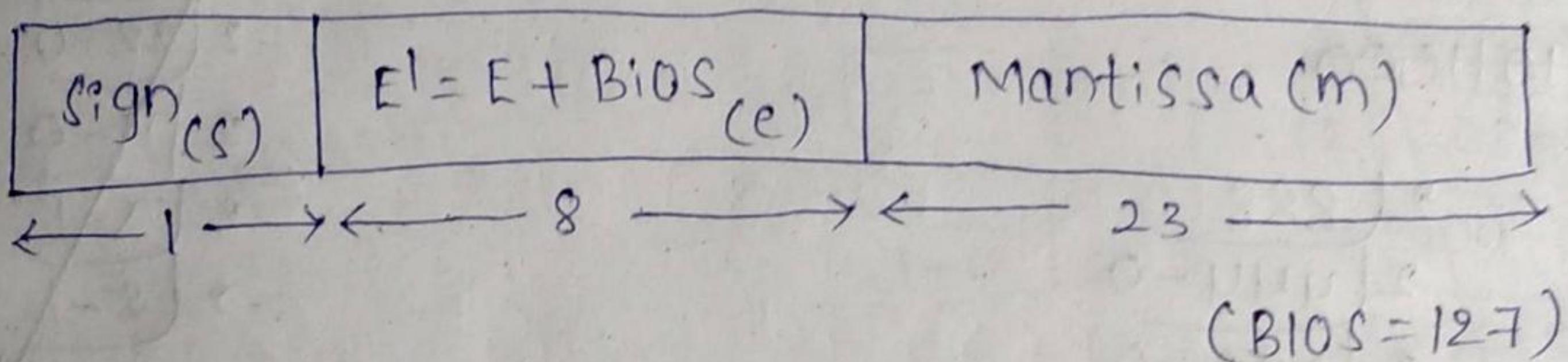
Floating point representation :-  $+0.100111 \times 2^5$

↓                            ↓  
Fraction                    exponent

+0.100111            +05  
(m)                    (e)

\* Two ways :-

1. 32 bit Floating point Representation (single precision)
2. 64 bit Floating point Representation (double precision).

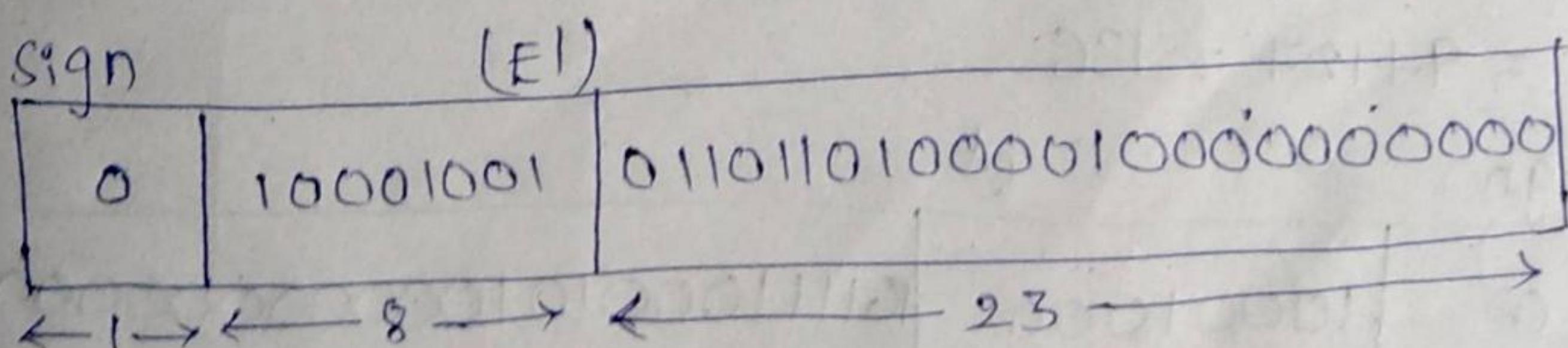


$$\text{Ex: } (1460.125)_{10} = (10110110100.001)_2$$

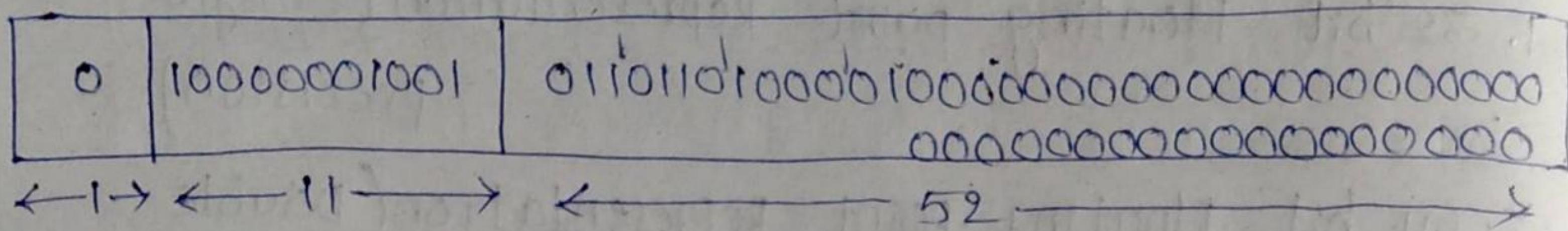
$$= 1.0110110100001 \times 2^{10} \rightarrow m \times r^e$$

$$E' = E + \text{BIOS}$$

$$= 10 + 127 = 137$$



$$E' = E + \text{BIOS} = 10 + 1023 = 1033$$



\*  $(888.625)_{10}$

~~10110000~~

$$\begin{array}{r} 2 | 888 \\ 2 | 444 - 0 \\ 2 | 222 - 0 \\ 2 | 111 - 0 \\ 2 | 55 - 1 \\ 2 | 27 - 1 \\ 2 | 13 - 1 \\ 2 | 6 - 1 \\ 2 | 3 - 0 \\ 1 - 1 \uparrow \end{array}$$

~~$$\begin{array}{r} 2 | 88 \\ 2 | 44 - 0 \\ 2 | 22 - 0 \\ 2 | 11 - 0 \\ 2 | 5 - 1 \\ 2 | 2 - 1 \\ 1 - 0 \end{array}$$~~

~~0.625~~

$$0.625 \times 2 = 1.25 \rightarrow 1$$

$$0.25 \times 2 = 0.5 \rightarrow 0$$

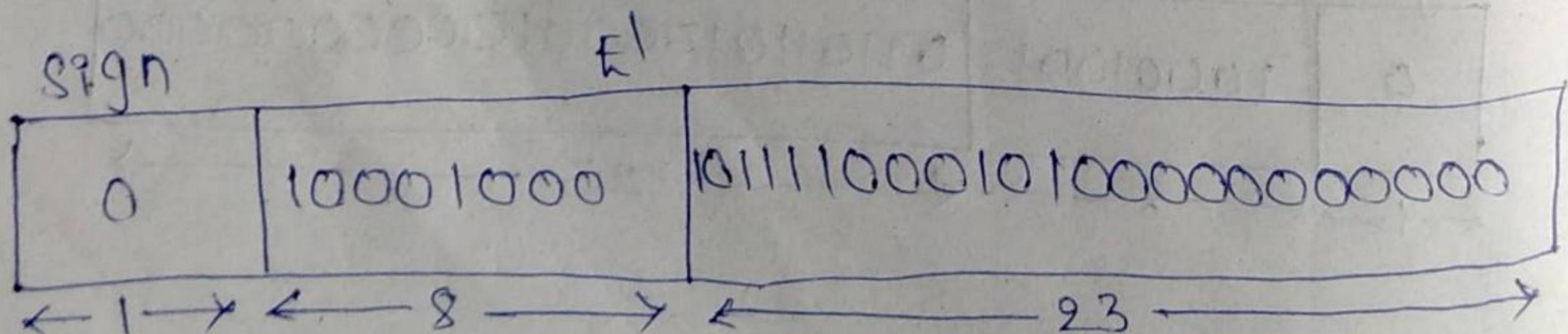
$$0.5 \times 2 = 1.0 \rightarrow 1$$

$$(888.625)_{10} = (1101111000 \cdot 101)_2$$

$$= 1.101111000101 \times 2^9$$

$$E' = E + \text{BIOS}$$

$$= 9 + 127 = 136$$

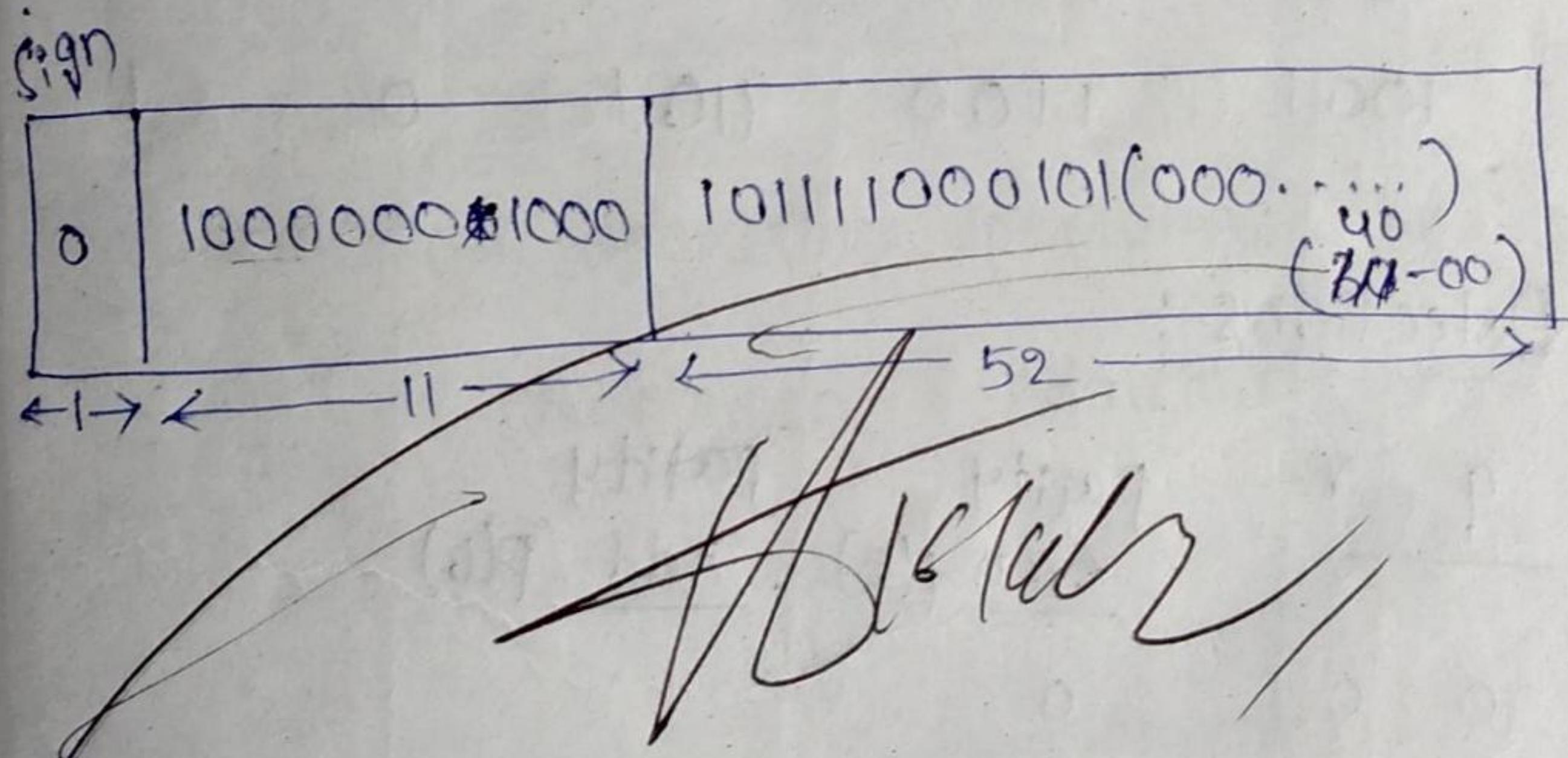


$$\begin{aligned}
 E' &= E + \text{BIOS} \\
 &= 9 + 1023 \\
 &= 1032
 \end{aligned}$$

$$\begin{array}{r}
 2 | 1032 \\
 2 | 516-0 \\
 2 | 258-0 \\
 2 | 129-0 \\
 2 | 64-1 \\
 2 | 32-0 \\
 2 | 16-0 \\
 2 | 8-0 \\
 2 | 4-0 \\
 2 | 2-0 \\
 1-0
 \end{array}$$

$$\begin{array}{r}
 2 | 136 \\
 2 | 68-0 \\
 2 | 34-0 \\
 2 | 17-0 \\
 2 | 8-1 \\
 2 | 4-0 \\
 2 | 2-0 \\
 1-0
 \end{array}$$

$$\begin{array}{r}
 2 | 1032 \\
 2 | 516-0 \\
 2 | 208-0 \\
 2 | 104-0 \\
 2 | 52-0 \\
 2 | 26-0 \\
 2 | 13-0 \\
 2 | 6-1 \\
 2 | 3-0 \\
 1-1
 \end{array}$$



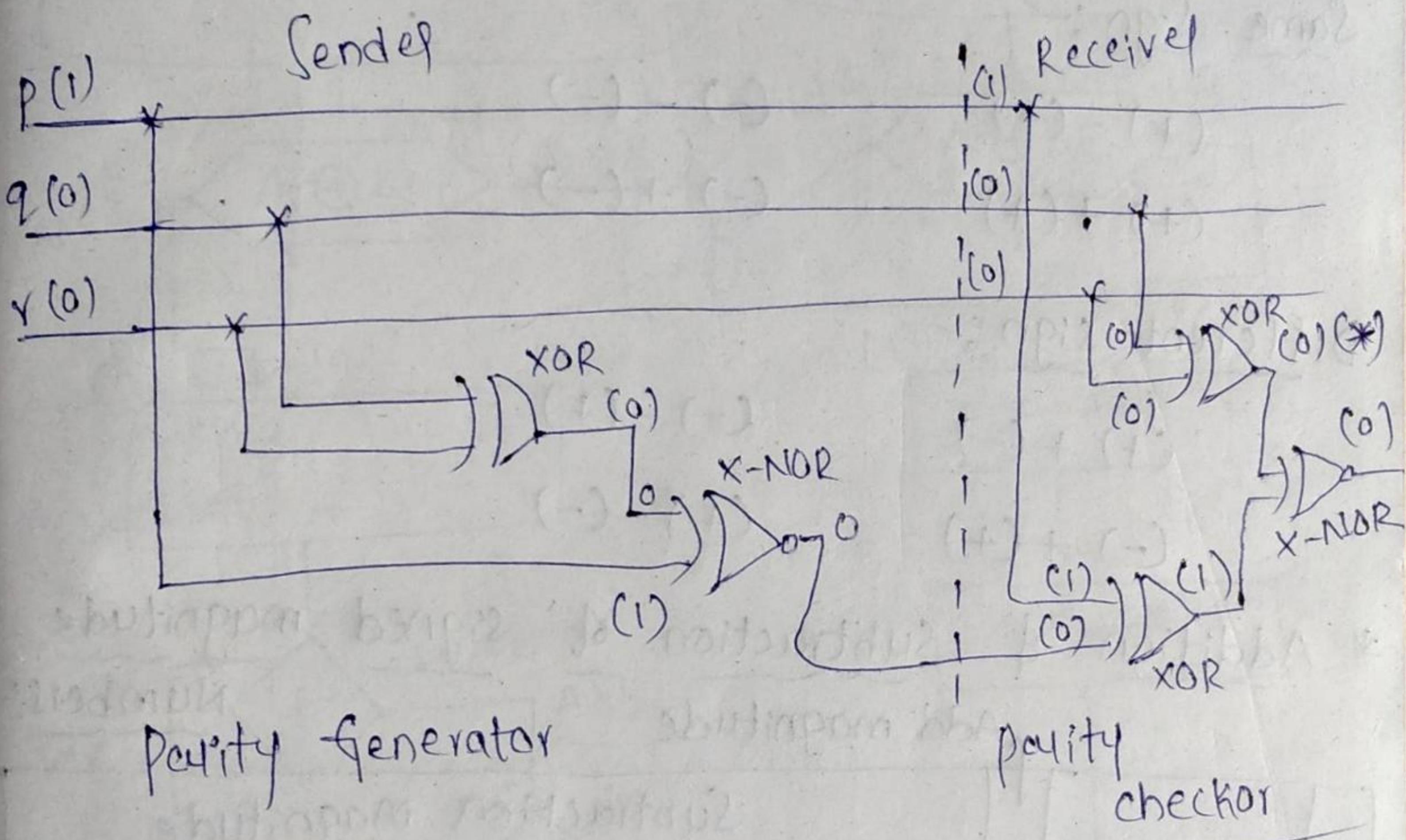
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<u>Decimal</u>	<u>Binary</u>	<u>Excess-3</u>	<u>Gray code</u>	<u>Parity Even</u>	<u>Parity odd</u>
0	0000	0011	0000	0	1
1	0001	0100	0001	1	0
2	0010	0101	0011	1	0
3	0011	0110	0010	0	1
4	0100	0111	0110	1	0
5	0101	1000	0111	0	1
6	0110	1001	0101	0	1
7	0111	1010	0100	1	0
8	1000	1011	1100	1	0
9	1001	1100	1101	0	1

### \* Error Detections :-

<u>P</u>	<u>q</u>	<u>r</u>	<u>Parity</u>	<u>Parity</u>
			<u>Even p(E)</u>	<u>odd p(O)</u>
0	0	0	0	1
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	0

- \* Odd Parity Circuit :- (1) Parity Sender (Sender)  
generator  
(2) Parity checker (Received).



- \* Subtraction operation performs by  
complement + Addition.

$$A - B = A + (\overline{B} + 1)$$

$\downarrow$   
2's complement of B.

- \* Rule 1 :- Same sign  $\rightarrow$  perform add as  
addition operation, sub as subtraction  
operation.

\* Rule 2 :- Different sign  $\rightarrow$  perform sub for Add,  
Add for sub.

Same Sign :-

$$(+)-(+)$$

$$(-)-(-)$$

$$(+)+(+)$$

$$(-)+(-)$$

Different sign :-

$$(+)+(-)$$

$$(-)-(+)$$

$$(-)+(+)$$

$$(+)-(-)$$

\* Addition & subtraction of signed magnitude Numbers:-

S.No	operation	Subtraction Magnitude		
		(i) A>B	(ii) A<B	(iii) A=B
1.	$(+A) + (+B)$	$(A+B)$	$x$	$x$
2.	$(+A) + (-B)$	$x$	$+ (A-B)$	$-(B-A)$
3.	$(-A) + (+B)$	$x$	$- (A-B)$	$+ (B-A)$
4.	$(-A) + (-B)$	$(\bar{A}+\bar{B})$	$x$	$x$
5.	$(+A) - (+B)$	$x$	$+ (A-B)$	$-(B-A)$
6.	$(+A) - (-B)$	$(A+B)$	$x$	$x$
7.	$(-A) - (+B)$	$(\bar{A}+B)$	$x$	$x$
8.	$(-A) - (-B)$	$x$	$- (A-B)$	$+ (B-A)$
				$+ (A-B)$

## Subtraction operation (-)

## All operation (+)

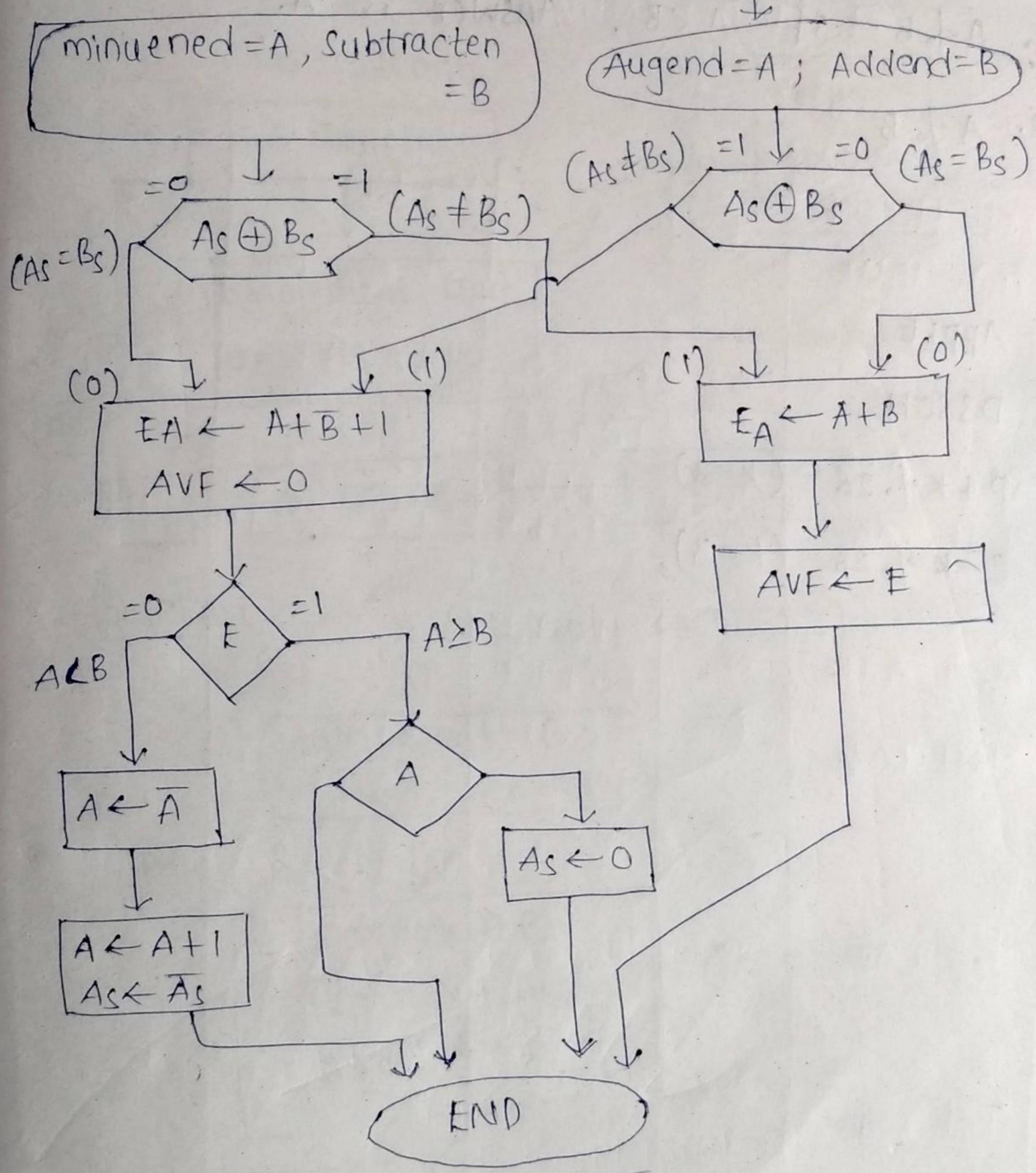


Fig:- Flowchart for add and subtract operations,,

\* Note :-

1.  $A \oplus B$  if  $A < B$ , Answer is A.

2.  $A \oplus B$

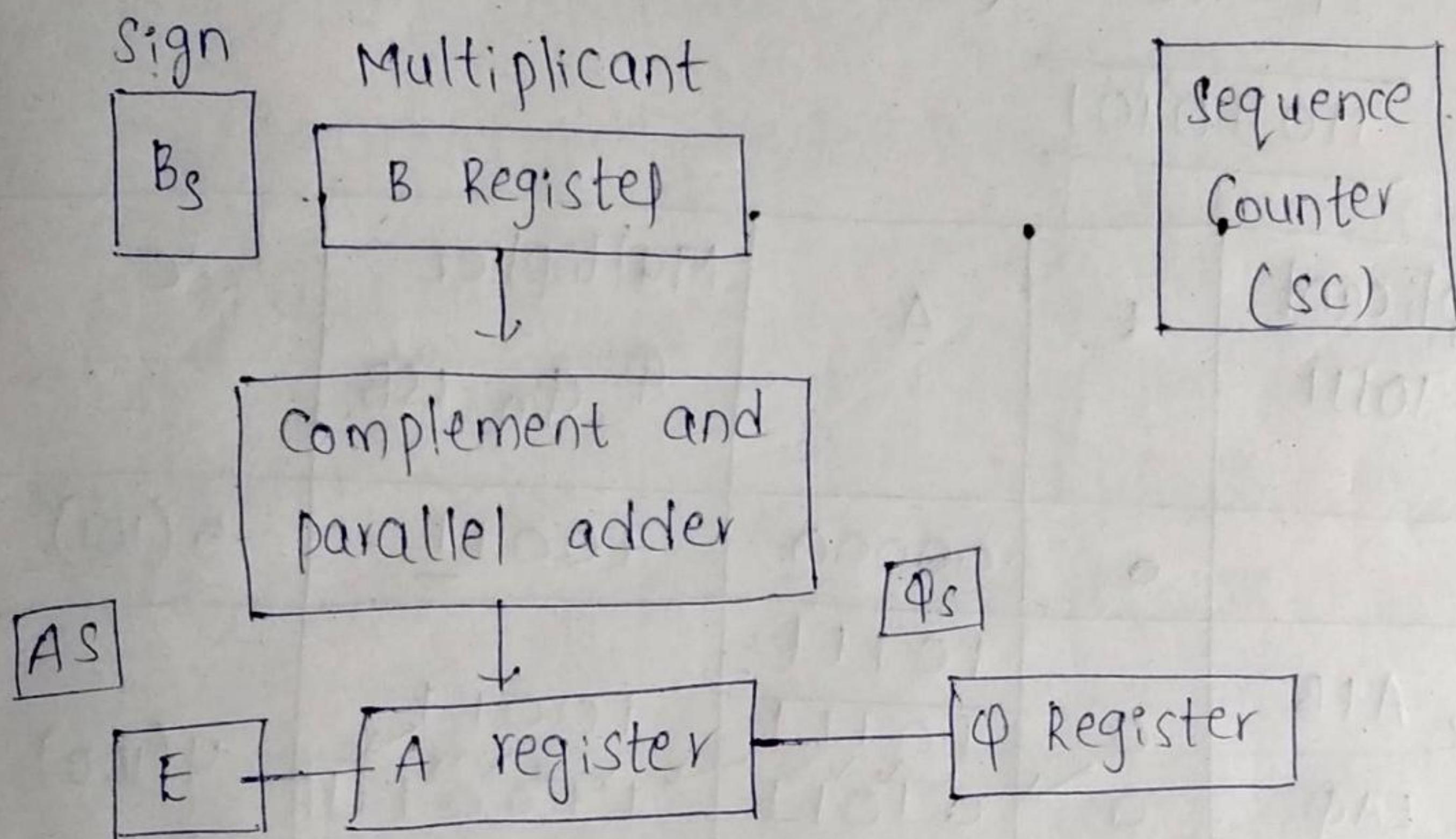
APPLE

DSSOH

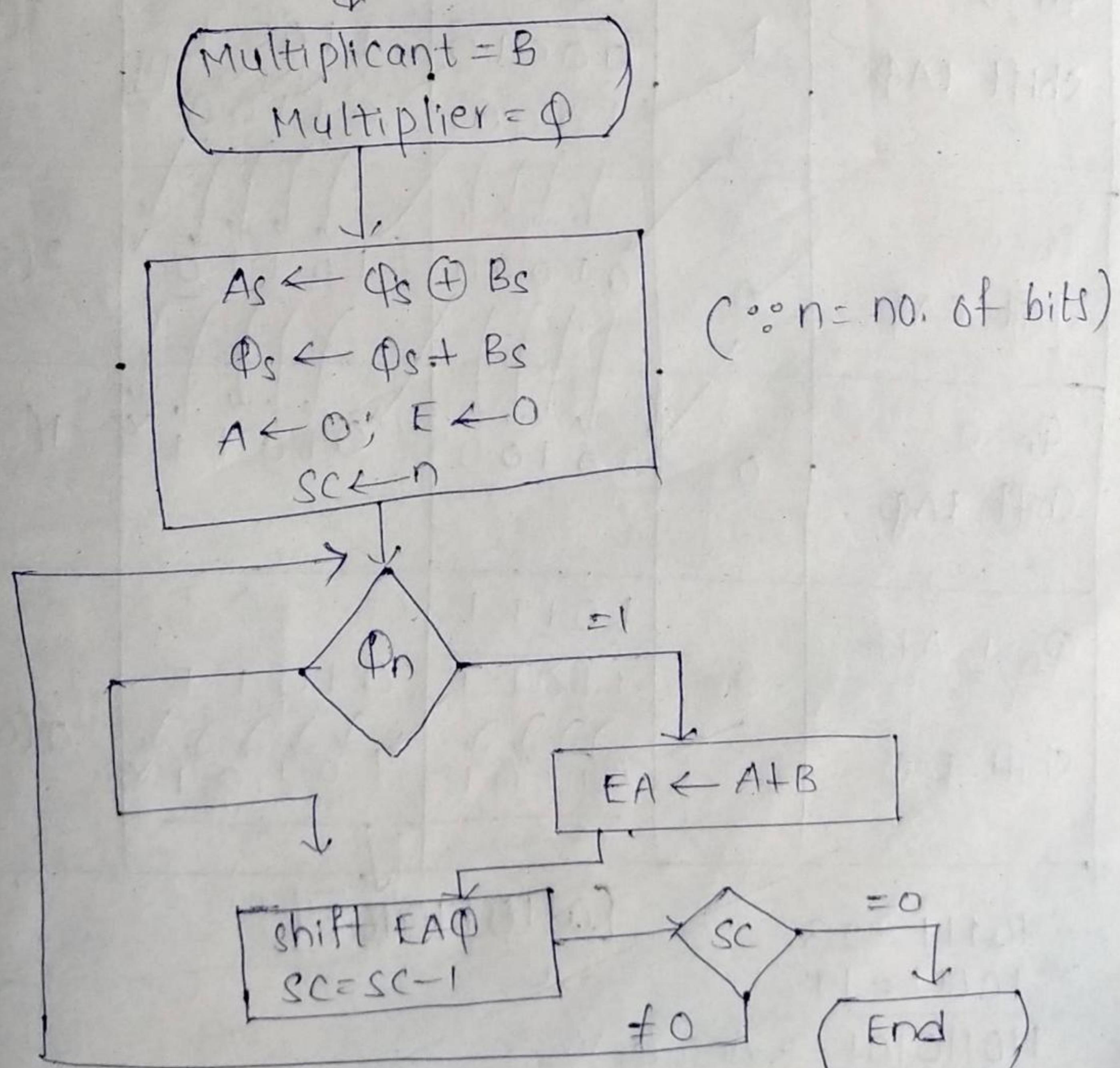
$P + K \oplus 26 \quad (k=3)$

$C - K \oplus 26 \quad (k=3),$

## \* Multiplication Algorithm with signed magnitude



## \* Flowchart :- X (Multiply operations)



\* Eg:-  $23 = 10111$  (multiplicand) = B  
 $19 = 10011$  (multiplier) = Q

110110101

Multiplicand (B) - 10111	E	A	Multiplier Q $Q_n = \text{LSB}$	sc
	0	00000	10011	5(101)
$Q_n = 1, A+B$ shift EAQ	0	10111	10011	4(100)
$Q_n = 1, A+B$ shift EAQ	1	00010	11001	3(011)
$Q_n = 0$ shift EAQ	0	01000	10110	2(010)
$Q_n = 0$ shift EAQ	0	00100	01011	1(001)
$Q_n = 1, A+B$ shift EAQ	0	10111	01011	0(000)

$10111 = 23$

$\times 10011 = 19$

$110110101 \rightarrow \text{Answer}$

[01110110101]



\* 13 \* 17

$$13 = 1101 \text{ (Multipliend)} = B$$

$$17 = 10001 \text{ (Multiplier)} = \Phi$$

$$\underline{1101 \quad 10001}$$

Multipliend  
(B)

E

A

Multiplier  
( $\Phi$ )

SC

$Q_n = \text{LSB}$

$$1101$$

0

00000

10001

5(101)

$Q_n = 1$ ,  
add "B to A"  
shift EA $\Phi$

$Q_n = 0$   
shift EA $\Phi$

$Q_n = 0$   
shift EA $\Phi$

$Q_n = 0$   
add "B to A"  
shift EA $\Phi$

$Q_n = 1$   
add "B to A"  
shift EA $\Phi$

$$1101$$

$$01101$$

$$10001$$

$$4(100)$$

$$00110$$

$$11000$$

$$3(011)$$

$$00011$$

$$01100$$

$$3(011)$$

$$00001$$

$$10110$$

$$2(010)$$

$$00000$$

$$11011$$

$$1(001)$$

$$00000$$

$$11011$$

$$1(001)$$

$$11011$$

$$11011$$

$$0(000)$$

$$11011$$

$$11011$$

$$0(000)$$

$$11011$$

$$11011$$

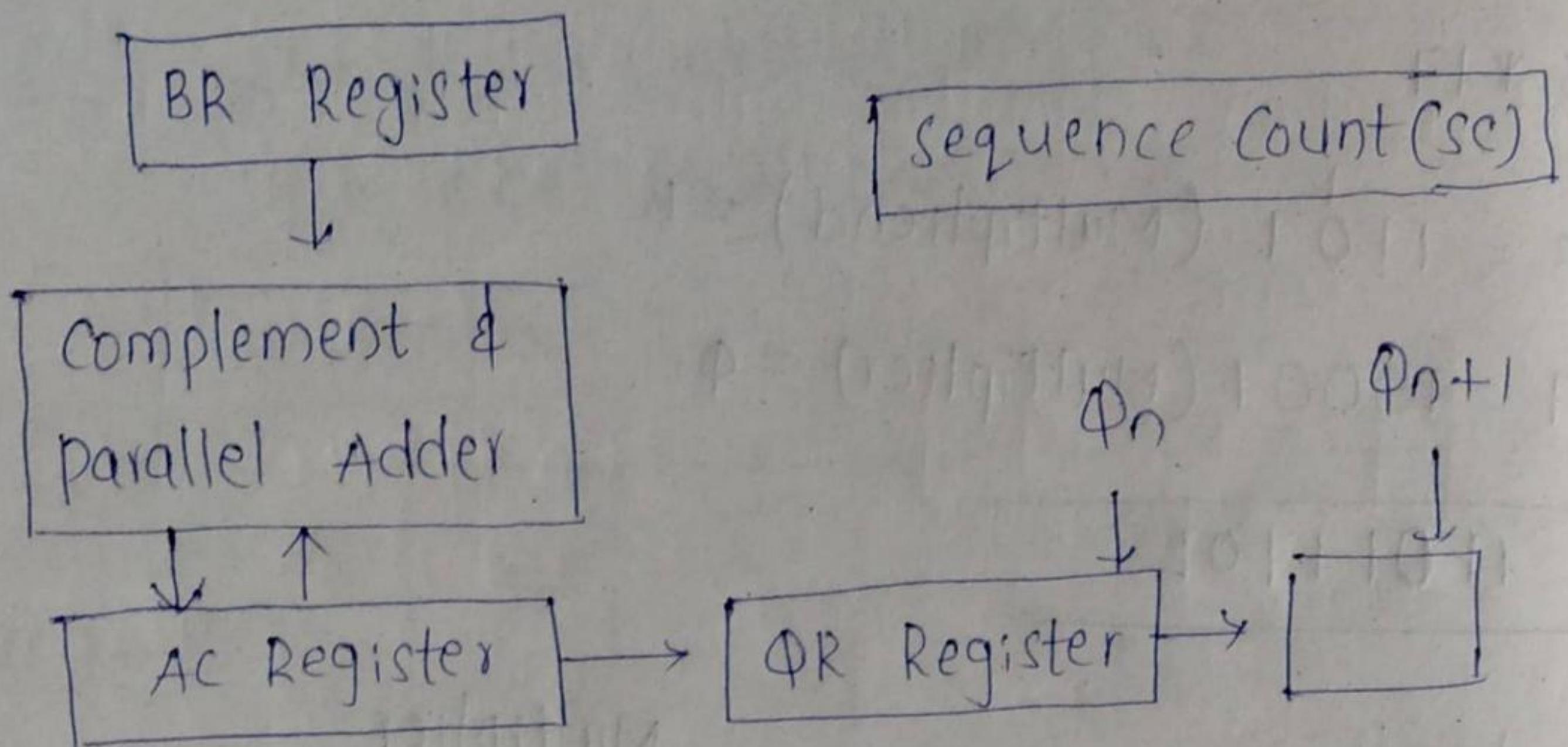
$$0(000)$$

$$11011$$

$$11011$$

$$0(000)$$

Ans(11011)



\*  $x$  (Multiply)

Multipliend = BR, Multiplier = QR

$AC \leftarrow 0$   
 $\Phi_{n+1} \leftarrow 0$   
 $SC \leftarrow n$

$n$  = no. of bits in multiplier

$= 10$

$\Phi_n \Phi_{n+1}$

$= 01$

$AC \leftarrow AC + BR$

$AC \leftarrow AC + \overline{BR} + 1$

Arithmetic shift Right  
 $(AC \& QR) \quad SC = SC - 1$

Booth's Algorithm  
 for multiplication  
 of signed 2's  
 Complement  
 Numbers.

$f_0$   
 $SC$   
 $= 0$   
 END

\*  $-9 = BR = 10111$  (2's signed complement)

$-13 = \Phi R = 10011$  (2's signed complement)

+111 (n=5) Multiplier.

$\Phi_n \Phi_{n+1}$	Multipliend $BR = 10111$ $\overline{BR} = 01000$ $\overline{BR} + 1 = 01001$	AC	Multiplier $\Phi R$	$\Phi_{n+1}$	SC
		00000	10011	0	101(5)
1 0	Subtract BR ASR (AC & $\Phi R$ )	$\begin{array}{r} 01001 \\ - 01001 \\ \hline 00000 \end{array}$	10011	0	100(4)
1 1	ASR (AC & $\Phi R$ )	$\boxed{0} 0010$	$01100$	<u>1</u>	011(3)
0 1	Add BR ASR (AC & $\Phi R$ )	$\begin{array}{r} 10111 \\ + 01001 \\ \hline 11100 \end{array}$	10111	<u>0</u>	010(2)
0 0	ASR (AC & $\Phi R$ )	11110	$01011$	<u>0</u>	001(1)
1 0	Subtract BR ASR (AC & $\Phi R$ )	$\begin{array}{r} 011001 \\ - 011001 \\ \hline 00000 \end{array}$	00000	0	000(0)

\* -11 = BR (Multiplicand) = 10101

-13 = QR (Multiplier) = 10011

10001111 (n=5)

Multiplicant

$Q_n \Phi_{n+1}$

BR = 10101

BR = 01010

BR+1 = 01011

AC

Multiplier

QR

10011

$\Phi_{n+1}$

SC  
(n=5)

00000 10011 0 5(101)

10

Subtract BR

01011  
01011 10011

ASR (AC & QR)

↓  
00101 11001 1

4(100)

11

ASR (AC & QR)

↓  
00010 11100 1

3(010)

01

$AC \leftarrow AC + BR$

10101  
10111 11100

ASR (AC & QR)

↓  
10111 11110 0

2(010)

00

ASR (AC & QR)

↓  
11101 11111 0

1(001)

10

Subtract BR

01011

ASR (AC & QR)

01000 11111

x

00100 01111 1

0(000)

\* Note :-

1. Multiplication Algorithm works for signed and unsigned numbers.

2. Where Booth's Algorithm works for 2's complement for signed magnitude numbers.

\* Division Algorithm :-

Divisor

$$B = (10001)_2$$

$$B = (17)_{10}$$

Dividend

$$A = 0111000000$$

$$A = (448)_{10}$$

$$17) \ 448 \quad \text{Quotient} \\ (26)$$

34

108

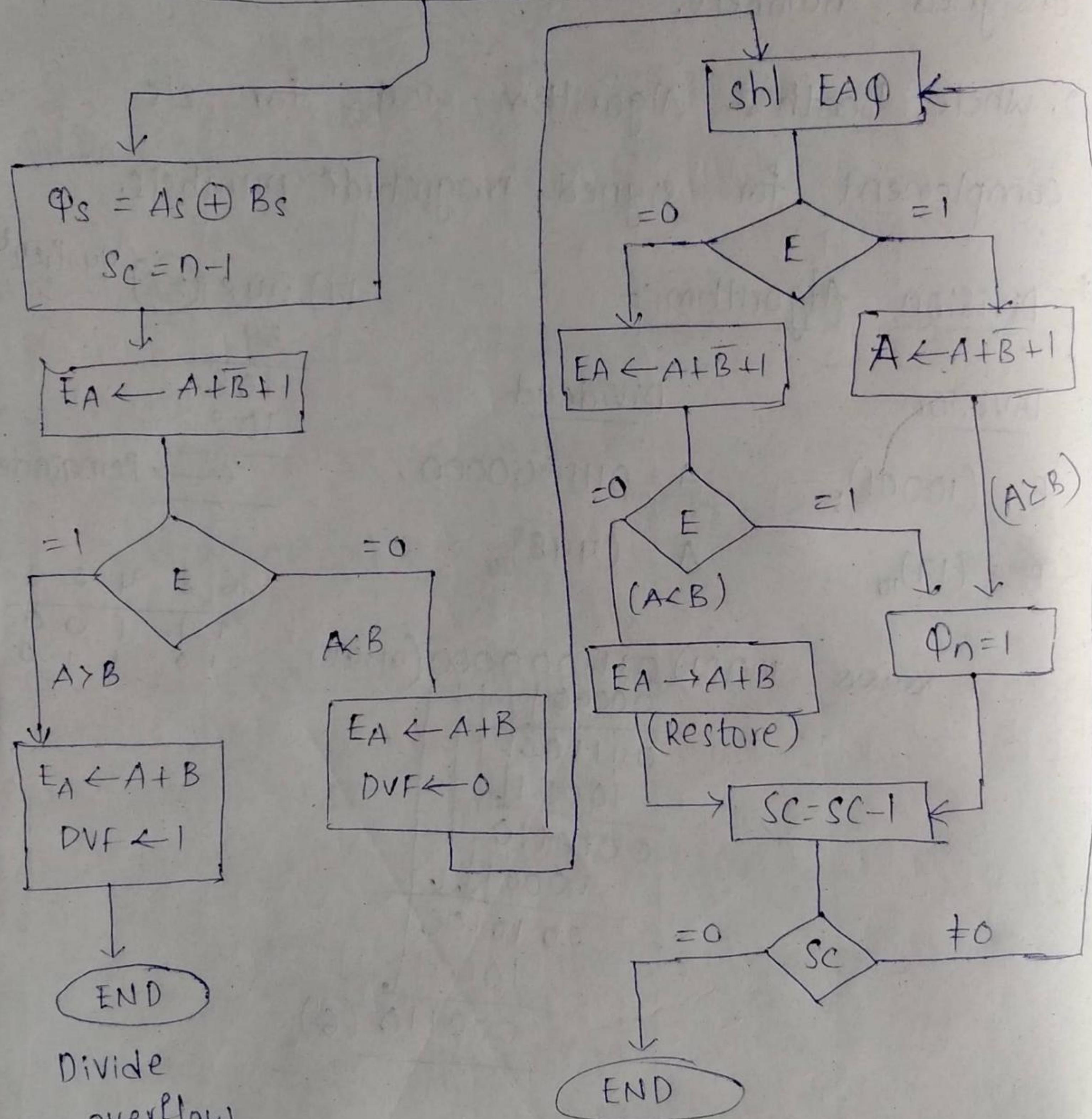
102

6 → Remainder

$$\begin{array}{r} 16 \ 8 \ 4 \ 2 \ 1 \\ \hline 1 \ 1 \ 1 \ 0 \ 0 \\ 1 \ 0 \ 1 \ 0 \ 0 \\ \hline 1 \ 1 \ 0 \ 0 \ 0 \end{array}$$

$$\begin{array}{r} 10001 ) 0111000000 ( 011010 \\ 00000 \downarrow \quad | \quad | \quad | \\ \hline 011100 \\ 10001 \downarrow \\ \hline 0010110 \\ 10001 \downarrow \\ \hline 0010100 \\ 10001 \downarrow \\ \hline 000110 \ (6) \end{array}$$

Dividend =  $A\varphi$ ; Divisor =  $B$



Divide  
overflow

\* Quotient =  $\varphi$

Remainder =  $A$

Division

$$B = 10001$$

$$\bar{B}+1 = 01111$$

Dividend =  $A\phi$

$$(A = 01110; \phi = 00000)$$

$$SC = 5$$

(No. of bits in  $\phi$ )

<u>E</u>	<u>A</u>	<u><math>\phi</math></u>	<u>SC</u>
	00 01110	00000	5(101)

Shl EA $\phi$ : -

$$\begin{array}{r} 0 \\ 0 \\ \hline \boxed{1} \end{array}$$

when E=1

het  $\phi_n = 1$

$$\begin{array}{r} 11100 \\ 01111 \\ \hline 01011 \end{array}$$

$$0000 \boxed{0}$$

$$5(101)$$

Add  $A + \bar{B} + 1$

when  $E=1$

het  $\phi_n = 1$

$$01011 \quad 00001$$

$$4(100)$$

Shl EA $\phi$  → 0

Add  $A + \bar{B} + 1$

when E=1

het  $\phi_n = 1$

$$\begin{array}{r} 10110 \\ 01111 \\ \hline 00101 \end{array}$$

$$0001 \boxed{0}$$

$$3(0011)$$

Shl EA $\phi$  → 0

Add  $A + \bar{B} + 1$  →

when E=0,

here  $\phi_n = 0$

Add  $A + B$  (Restore)

$$\begin{array}{r} 11010 \\ 01111 \\ \hline 10001 \end{array}$$

$$0011 \boxed{0}$$

$$2(010)$$

Shift 1 EA $\phi$  → 0

Add  $A + \bar{B} + 1$  →

when E=1,  $\phi_n = 1$

$$+ 10100 \quad 0110 \boxed{0}$$

$$01111 \quad 00011$$

$$1(001)$$

Shl EA $\phi$  → 0

$$\begin{array}{r} 00110 \\ 00110 \\ \hline 11011 \end{array}$$

$$1101 \boxed{0}$$

$$1101 \boxed{0}$$

Shl EAΦ → 0 00110 11010 0(000)

Add AFB+1 → 0 01111  
0 10001  
1

When E=0,

here  $\Phi_n = 0$

Add A+B(Restore) 1 10001  
00110 11010  
00110 11010

\* 444 ÷ 17

(17) 444 (26)  
34

Divisor

$B = (17)_{10}$

$B = (10001)_2$

Dividend

$A = 0110111100$

$A = (444)_{10}$

104  
102  
—  
2

~~(10001) 0110111100 (011001)~~  
~~000001 | | | |~~  
~~011011 | | | |~~  
~~10001 | | | |~~  
~~010101 | | | |~~  
~~10001 | | | |~~  
~~00011100 | | | |~~  
~~10001 | | | |~~  
~~01011 | | | |~~

16	8	4	2	1
0	1	1	0	1
1	1	0	1	1
1	0	1	0	0
			1	1
			1	1
			1	1
			1	0

$$\left. \begin{array}{l} B=10001 \\ \bar{B}=01110 \\ \bar{B}+1=01111 \end{array} \right\} \quad \begin{array}{l} \text{Divided} = A\varphi \\ A=01101 \\ \varphi=11100 \end{array}$$

$$10001) 0110111100(011010$$

$$\begin{array}{r} 00000 \\ \hline 11011 \\ 10001 \\ \hline 010101 \\ 10001 \\ \hline 0010010 \\ 10001 \\ \hline 000010 \\ 00000 \\ \hline 10 \end{array}$$

E	A	Q	SC
	01101	11100	<u>5(101)</u>

Shl EA $\varphi$	0	111011	1100 $\boxed{0}$
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Add A + $\bar{B}$ + 1	$\boxed{1}$	01111	
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When E=1		01010	11001
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Shl EA $\varphi$	0	10101	1001 $\boxed{0}$
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Add A + $\bar{B}$ + 1	$\boxed{1}$	01111	
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When E=1		00100	
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Let $\varphi_n=1$		00100	10011
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Shl EA $\varphi$	0	01001	00110
------------------	---	-------	-------

Add A + $\bar{B}$ + 1	$\boxed{0}$	01111	
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When E=0		11000	
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here $\varphi_n=0$		10001	00110
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Add A+B (Restore)	$\boxed{1}$	01001	2(010)
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1 01001 00110 2(010)

shl EAQ 0 10010 0110 0

Add A+B+1 0 01111  
0 00001

when E=1,

Let  $\Phi_n = 1$  00001 01101 1(001)

shl EAQ 0 00010 1101 0

Add A+B+1 0 01111  
0 10001

when E=0,

$\Phi_n = 0$  1 00010 11010 0(000).

Restore A+B  
(Restore) 00010 11010

\* Floating Point Representation:-

(1)  $(1259.125)_{10} \rightarrow$  Single precision

(2)  $(263.3)_{10} \rightarrow$  Double precision.

Ans).

(1)  $(1259.125)_{10} = (100111010111.001)_2$

$$= (1.00111010111001) \times 2^{10}$$

$$\Rightarrow m \times r^e$$

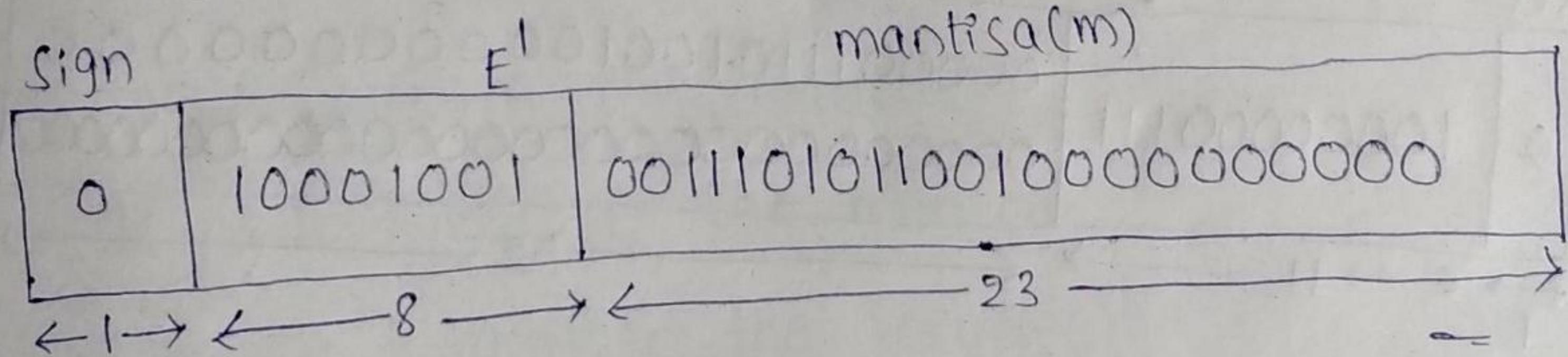
$$\begin{array}{r}
 0.125 \times 2 = 0.250 = 0. \\
 0.25 \times 2 = 0.5 = 0 \\
 0.5 \times 2 = 1 = 1
 \end{array}$$

$$\begin{array}{r}
 2 \overline{)1259} \\
 2 \overline{)629-1} \\
 2 \overline{)314-1} \\
 2 \overline{)157-0} \\
 2 \overline{)78-1} \\
 2 \overline{)39-0} \\
 2 \overline{)19-1} \\
 2 \overline{)9-1} \\
 2 \overline{)4-1} \\
 2 \overline{)2-0} \\
 1-0 \uparrow
 \end{array}$$

$$E' = E + \text{BIOS}$$

$$= 10 + 127$$

$$= 137$$



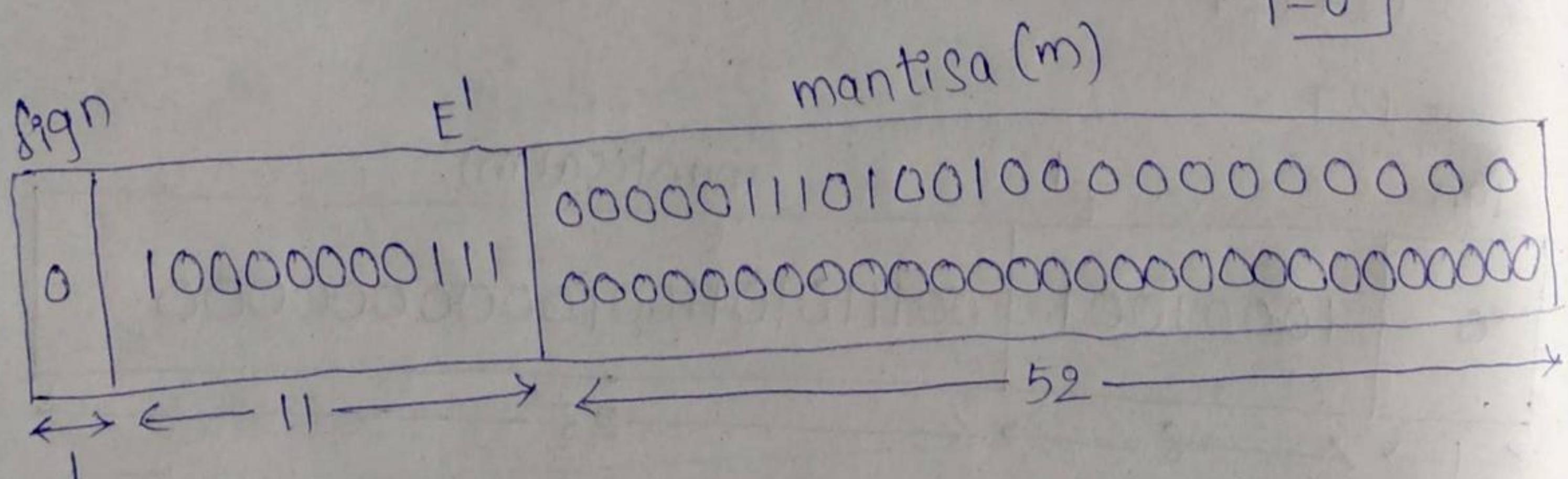
$$(2) (263.3)_{10} = (100000111.01001)_2$$

$$\begin{array}{r}
 2 \overline{)263} \\
 2 \overline{)131-1} \\
 2 \overline{)65-1} \\
 2 \overline{)32-1} \\
 2 \overline{)16-0} \\
 2 \overline{)8-0} \\
 2 \overline{)4-0} \\
 2 \overline{)2-0} \\
 1-0 \uparrow
 \end{array}$$

$0.3 \times 2 = 0.6 \rightarrow 0$   
 $0.6 \times 2 = 1.2 \rightarrow 1$   
 $0.2 \times 2 = 0.4 \rightarrow 0$   
 $0.4 \times 2 = 0.8 \rightarrow 0$   
 $0.8 \times 2 = 1.6 \rightarrow 1$   
 $0.6 \times 2 = 1.2 \rightarrow 1$

$\Rightarrow (1.0000011101001) \times 2^8$   
 $\Rightarrow m \times r^e$   
 $E' = E + 1023$   
 $= 8 + 1023$   
 $= 1031$

$$\begin{array}{r}
 2 | 1031 \\
 2 | 515-1 \\
 2 | 257-1 \\
 2 | 128-1 \\
 2 | 64-0 \\
 2 | 32-0 \\
 2 | 16-0 \\
 2 | 8-0 \\
 2 | 4-0 \\
 2 | 2-0 \\
 \hline
 & 1-0 \uparrow
 \end{array}$$



## \* Floating Point Arithmetics:

### (1) Addition:-

Steps:-

Step 1:- check for zeroes

Step 2:- Align the mantissa.

Step 3:- Add the mantissa.

Step 4:- Normalize the result

### (2) Subtraction:-

Step 1:- check for zeroes.

Step 2:- Align the mantissa.

Step 3:- Subtract the mantissa.

Step 4:- Normalize the result

### (3) Multiplication:-

Step 1 :- check for zeroes

Step 2 :- Add the exponents.

Step 3 :- Multiply the mantissa.

Step 4 :- Normalize the result.

### (4) Division:-

Step 1 :- check for zeroes.

Step 2 :- Initialize the registers & evaluate

the sign.

Step 3 :- Align the dividend.

Step 4 :- Subtract the exponents.

Step 5 :- Divide the mantas.

Step 6 :- Normalize the result.

$$* A = (0.5372400 \times 10^2)$$

$$B = (0.1580000 \times 10^{-1})$$

