

1. Express the wave $f(t, x) = A \sin(\omega t - kx)$ in complex notation.

Answer: In complex notation, $f(x) = \text{Re}(\tilde{f}(x))$, where $\tilde{f}(x) = \tilde{A}e^{i(\omega t - kx)}$, $\tilde{A} = Ae^{-i\pi/2}$

2. In vacuum, EM waves are transverse with \mathbf{E} and \mathbf{B} perpendicular to each other. This can be shown from
(a) Gauss law, (b) Ampere's law, (c) $\nabla \cdot \mathbf{B} = 0$, (d) Faraday-Lenz law

Answer: (b) & (d)

3. Pressure applied by EM waves incident on a surface is arises due to forces applied by the oscillating EM fields of the EM wave on electrons in the wall material. This pressure is along which force component:
(a) $q\mathbf{E}$, (b) $\frac{q}{c}\mathbf{v} \times \mathbf{B}$, (c) $q\mathbf{E} + \frac{q}{c}\mathbf{v} \times \mathbf{B}$, (d) $\mathbf{I} \times \mathbf{B}$

Answer: (b)

4. For an Ohmic conductor, on which timescale any injected volume charge dissipates i.e. flows out to the surface/edges:
(a) 0, (b) $\frac{\epsilon}{\sigma}$, (c) $\frac{\mu\epsilon}{\sigma}$, (d) $\frac{1}{\omega}$

Answer: (b)

5. Skin Effect: As we increase ω , the EM wave incident on a conductor, penetrates :
(a) deeper, (b) lesser, (c) about the same

Answer: (b)

6. Cauchy dispersion formula holds for
(a) Normal dispersion (b) Anomalous dispersion (c) General Case

Answer: (a)

7. Which frequency is not allowed in a rectangular wave guide:
(a) ω_{00} (b) ω_{10} (c) ω_{01} (d) ω_{11}

Answer: (a)

8. For reflection at conducting surface, the Fresnel equations although formally identical to the dielectric, are different due to...

Answer: For the case of conductors the equations are complex, while for dielectrics they are real (no phase factors contributing to phase difference between \mathbf{E} and \mathbf{B}).

9. Poynting vector in a dielectric is
(a) $\frac{1}{\mu_0}\mathbf{E} \times \mathbf{B}$ (b) $\frac{1}{c^2}\mathbf{D} \times \mathbf{B}$ (c) $\mathbf{E} \times \mathbf{H}$ (d) $\mathbf{D} \times \mathbf{H}$

Answer: (c)

1. **Solution:**

$$f(x) = A \sin(\omega t - kx) = A \cos(\omega t - kx - \frac{\pi}{2})$$

which is the real part of,

$$\tilde{f}(x) = A e^{i(\omega t - kx - \frac{\pi}{2})} = \tilde{A} e^{i(\omega t - kx)}, \tilde{A} = A e^{-i\pi/2}.$$

2. **Solution:** Look up lecture slides.

3. **Solution:** The electric field component of the EM waves make the charged particles move around, and these moving charges experience the Lorentz magnetic force, $F = \frac{q}{c} \mathbf{v} \times \mathbf{B}$. Since \mathbf{v} is lies on the wall, as well as \mathbf{B} has a component parallel to the wall, the charge experiences a Lorentz magnetic force in a direction normal to the wall. The sum total of this normal Lorentz magnetic force over all charges per unit area of the wall gives rise to radiation pressure.

4. **Solution:** Look up the lecture slides.

5. **Solution:** Skin depth is, $d \sim \sqrt{\frac{2}{\mu\sigma\omega}} \propto \omega^{-1/2}$.

6. **Solution:** Look up lecture slides

7. **Solution:** Recall from lecture, for the **TE** mode ω_{00} , $m = n = 0$, which gives $B_z = \text{constant}$. This immediately implies, $B_{x,y} = E_{x,y} = 0$. Thus ω_{00} cannot be sustained in a rectangular wave guide.

8. **Solution:** Look up lecture slides

9. **Solution:** Derive this as an exercise.