



CY 1020: Dynamics of Chemical Systems Basics in Electrochemistry

CY1020: Dynamics of Chemical Systems



Basics in Electrochemistry: Electrochemical principles and reactions, basic concepts of electrochemical cells, Nernst Equation, applications of EMF, conductivity of electrolyte solutions.



Books Recommended



- 1. Principles of Physical Chemistry: Puri, Sharma, Pathania
- 2. Physical Chemistry: Vol-, K L Kapoor
- 3. Physical Chemistry: P.W. Atkins



Electrochemistry

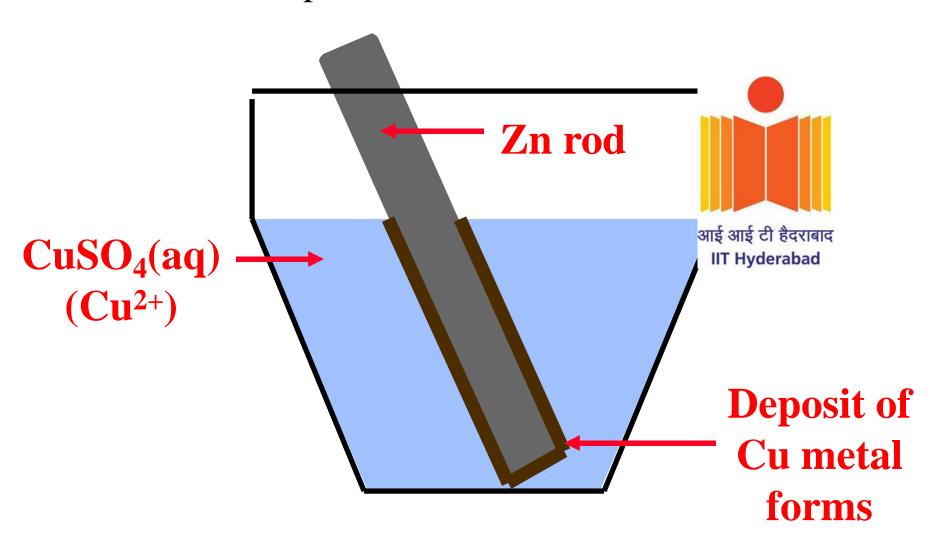


आई आई टी हैदराबाद Electrochemistry

- deals with interconversion between chemical and electrical energy
- involves redox reactions: electron transfer reactions

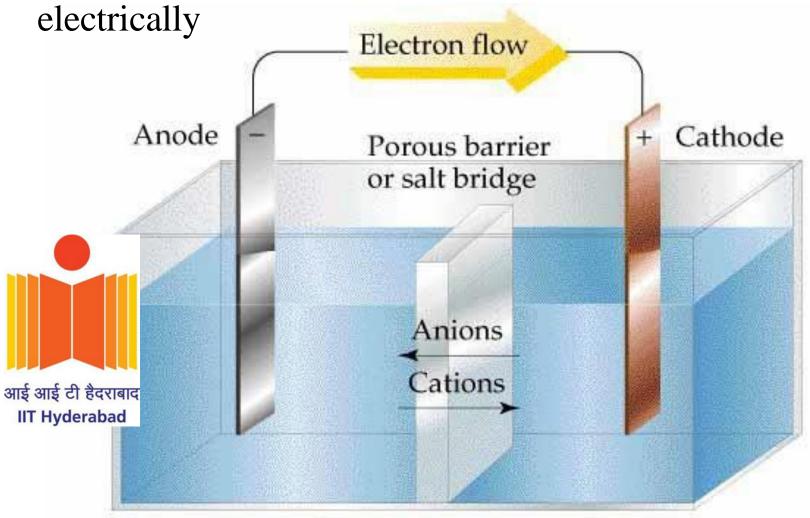
Direct Redox Reaction

 Oxidizing and reducing agents are mixed together and reaction takes place in the same vessel



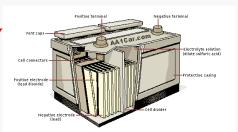
Indirect Redox Reactions

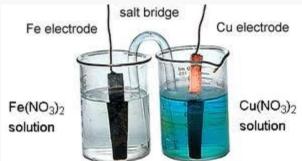
Oxidizing and reducing agents are separated but connected



Anode compartment Oxidation occurs Cathode compartment Reduction occurs

- Electrochemical cell-Voltaic Cell
 - cell in which a spontaneous redox reaction generates electricity
 - ◆ chemical energy → electrical energy
 - Ex: Battery





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- Electrolytic Cell
 - electrochemical cell in which an electric current drives a non-spontaneous redox reaction
 - electrical energy → chemical energy
 - Ex: Decomposition of water

Difference between Electrochemical (Galvanic) and Electrolytic Cell

Electrochemical Cell	Electrolytic cell
It is a device to convert chemical energy into electrical energy as a result of redox reaction taking place	energy into chemical energy to bring

It is based upon redox reaction which redox reaction The is spontaneous spontaneous The two electrodes are set up in the The two electrodes may be set up in solution of the same or different same electrolytic solution electrolytes

The electrode which is connected to The electrode on which oxidation takes place is called the anode and the negative terminal of the battery the electrode on which reduction takes place is called the cathode Dr. R. Anand

A salt bridge or a porous pot is used

in this cell

is called cathode, the cations migrate to it which gains electrons and hence reduction takes place here. The other electrode is called the anode

No salt bridge is used in this case

The Electrochemical Cells: Voltaic Pile

- Invented by Alessandro Volta in 1800
- Zinc and Copper with a cloth soaked in brine
- ❖ Technical Flaws:
 - Compressing of cloth created shorts
 - ❖Short battery life





Voltaic Pile

- Electrodes: are usually metal strips/wires connected by an electrically conducting wire.
- Salt Bridge: is a U-shaped tube that contains a gel permeated with a solution of an inert electrolyte.

 Fe electrode

 Cu electrode
- Anode: is the electrode where oxidation takes
- Cathode: is the electrode where reduction tak Fe(NO3)2
- Convention for expressing the cell: Place to the cell: Pl

Anode Half-Cell || Cathode Half-Cell Electrode | Anode Soln || Cathode Soln | Electrode Zn(s) | Zn²⁺ (1 M) || Cu²⁺ (1 M) | Cu(s)

solution

Cu(NO₃)₂ solution

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- | | represents Salt bridge
- represents Phase boundary

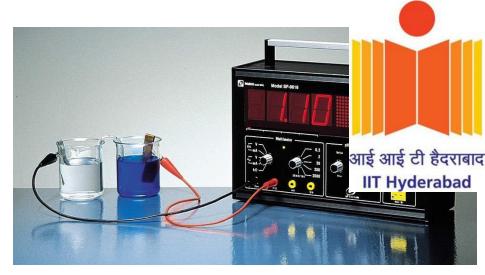
The notation for a cell involving a gas has an additional vertical line because an additional phase is present. e.g.

- Electrons flow from anode to cathode.
- Anode is placed on left by convention.

Galvanic Cells

The difference in electrical potential between the anode and cathode is called:

- cell voltage
- electromotive force (emf)
- cell potential



Cell Diagram

$$Zn (s) + Cu^{2+} (aq) \longrightarrow Cu (s) + Zn^{2+} (aq)$$

$$[Cu^{2+}] = 1 M \& [Zn^{2+}] = 1 M$$

$$Zn (s) | Zn^{2+} (1 M) || Cu^{2+} (1 M) | Cu (s)$$

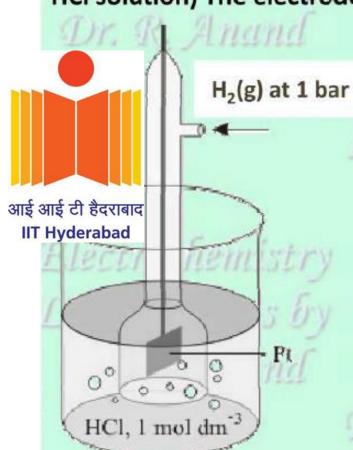
$$anode \qquad cathode$$

$$E_{cell} = E_{cathode} - E_{anode} = E_{redn} - E_{ox} E_{cell}^{\circ}$$

$$= E_{cathode}^{\circ} - E_{anode}^{\circ} = E_{redn}^{\circ} - E_{ox}^{\circ}$$

STANDARD HYDROGEN ELECTRODE

The primary reference electrode is the standard hydrogen electrode. It consists of a platinum foil that is connected to a platinum wire and sealed in a glass tube. H₂ gas at 1 atm pressure is passed through the side arm of the glass tube and bubbled through a solution of H⁺ ions of unit activity (e.g. 1N HCl solution) The electrode potential of SHE is zero at all temperatures.



It is represented as Pt, H₂ (1atm) | H⁺ (1M)

When it acts as anode the electrode reaction can be written as

$$H_2(g) \rightarrow 2H^+ + 2e^-$$

When it acts as cathode the electrode reaction can be written as

The equilibrium of hydrogen electrode is represented as

$$\frac{1}{2}$$
 H₂ (g) \rightleftharpoons H+ + e⁻

• $E^{\circ} = 0 V$ (by definition)

The electrode is reversible with respect to hydrogen ion. Since H₂ gas is non-conducting, Pt or some other metal which is not attacked by the acid and comes easily into equilibrium with H₂ is used for making electrical contact in the circuit.

Limitations 10 125 0

- It is very difficult to maintain the unit activity of hydrogen ions in solution.
- It is very difficult to pass hydrogen at 1 atm pressure uniformly.
- The deposition of impurities by adsorption on platinum foil causes hindrance in maintaining the equilibrium between hydrogen gas and hydrogen ions.
- This electrode cannot be used if some reducible ions are present in the equilibrium.
- The hydrogen electrode is readily affected by compounds of Hg, As, S and oxidizing agents like Fe³⁺, [MnO₄]⁻, Cr₂O₇²⁻ etc
- It cannot be used in solutions containing redox system
- The potential of the electrode is altered by changes in barometric pressure.
- It requires considerable volume of test solution.

Standard Electrode Potentials

- Standard Reduction Potentials, E°
 - E°_{cell} measured relative to S.H.E. (0 V)
 - electrode of interest = cathode

- Compare strengths of reducing/oxidizing agents.
 - the more E°, stronger the red. agent
 - the more + E°, stronger the ox. agent

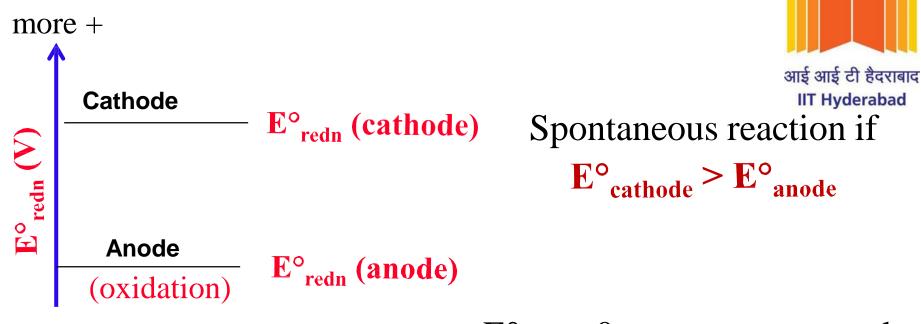
Standard Reduction Potentials

Ox. agent strength increases

Reduction Half-Reaction	E°(V)
$F_2(g) + 2e^- \rightarrow 2F^-(aq)$	2.87
$Au^{3+}(aq) + 3e^- \rightarrow Au(s)$	1.50
$Cl_2(g) + 2 e^- \rightarrow 2Cl^-(aq)$	1.36
$Cr_2O_7^{2-}(aq) + 14H^+(aq) + 6e^- \rightarrow 2Cr^{3+}(aq) + 7H_2O$	1.33
$O_2(g) + 4H^+ + 4e^- \rightarrow 2H_2O(l)$	1.23
$Ag^{+}(aq) + e^{-} \rightarrow Ag(s)$	0.80
$Fe^{3+}(aq) + e^- \rightarrow Fe^{2+}(aq)$	0.77
$Cu^{2+}(aq) + 2e^- \rightarrow Cu(s)$	0.34
$\operatorname{Sn^{4+}}(\operatorname{aq}) + 2e^{-} \to \operatorname{Sn^{2+}}(\operatorname{aq})$	0.15
$2H^{+}(aq) + 2e^{-} \rightarrow H_{2}(g)$	0.00
$\operatorname{Sn^{2+}}(\operatorname{aq}) + 2e^{-} \to \operatorname{Sn}(s)$	-0.14
$Ni^{2+}(aq) + 2e^- \rightarrow Ni(s)$	-0.23
$Fe^{2+}(aq) + 2e^{-} \rightarrow Fe(s)$	-0.44
$Zn^{2+}(aq) + 2e^- \rightarrow Zn(s)$	-0.76
$Al^{3+}(aq) + 3e^- \rightarrow Al(s)$	-1.66
$Mg^{2+}(aq) + 2e^- \rightarrow Mg(s)$	-2.37
$\mathbf{Li^+(aq) + e^- \to Li(s)}$ आई आई टी हैदराबाद IIT Hyderabad	-3.04

Uses of Standard Reduction Potentials

 Determine if oxidizing and reducing agent react spontaneously.

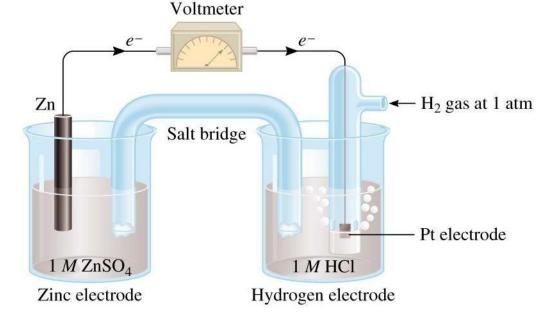


more -

• E°_{cell} > 0 : spontaneous redox reactions

Standard Reduction Potentials

$$E_{cell}^{0} = 0.76V$$





Standard emf (E_{cell})

$$E_{\text{cell}}^{\text{O}} = E_{\text{cathode}}^{\text{O}} - E_{\text{anode}}^{\text{O}}$$

$$E_{cell}^{0} = E_{H^{+}/H_{2}}^{0} - E_{Zn^{2+}/Zn}^{0}$$

$$0.76 \text{ V} = 0 - E_{Zn^{2+}/Zn}^{0}$$

$$E_{Zn^{2+}/Zn}^{0} = -0.76 \text{ V}$$

$$Zn^{2+}$$
 (1 M) + $2e^{-}$ Zn E° = -0.76 V

Equilibrium Constants from Ecell

- Is there a relationship between E_{cell} and ΔG for a redox reaction?
- Relationship between E_{cell} and ΔG :
 - $\Delta G = -nFE_{cell}$
 - F = Faraday constant = 96500 C/moles, n = # e-'s transferred redox rxn.
 - 1 J = CV
 - $\Delta G < 0$, $E_{cell} > 0$ = spontaneous
- Under standard state conditions:
 - $\Delta G^{\circ} = -nFE^{\circ}_{cell}$

And
$$\Delta G^{\circ} = -RT \ln K$$

So
$$-nFE_{cell}^{\circ} = -RTlnK$$

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Spontaneity of Redox Reactions

$$\Delta G = -nFE_{cell}$$
 $n = number of moles of electrons in reaction$

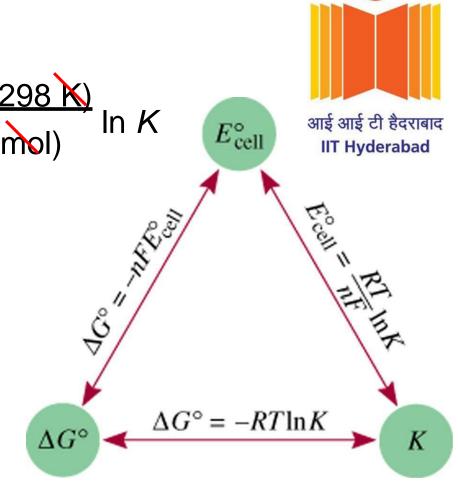
$$\Delta G^0 = -nFE_{cell}^0$$
 $F = 96,500 \frac{J}{V \cdot mol} = 96,500 \text{ C/mol}$

$$\Delta G^0 = -RT \ln K = -nFE_{cell}^0$$

$$E_{\text{cell}}^0 = \frac{RT}{nF} \ln K = \frac{(8.314 \text{ J/K} \cdot \text{mol})(298 \text{ K})}{n (96,500 \text{ J/V} \cdot \text{mol})} \ln K$$

$$E_{\text{cell}}^0 = \frac{0.0257}{n} \text{In} K$$

$$E_{\text{cell}}^0 = \frac{0.0592 \text{ V}}{n} \log K$$



The Nernst Equation

- $E_{cell} = E_{cell}^{\circ} (RT/nF) lnK$ (Nernst eqn.)
 - At 298 K (25°C)



n = number of moles of electrons in reaction

$$F = 96,500 \frac{J}{V \cdot mol} = 96,500 \text{ C/mol}$$

$$E_{cell} = E_{cell}^{\circ} - \frac{(8.314 \text{ WK-mol})(298 \text{ K})}{n (96,500 \text{ WV-mol})} \ln K$$

SO

•
$$E_{cell} = E_{cell}^{\circ} - (0.0257/n) nK$$

 $E_{cell} = E_{cell}^{\circ} - (0.0592/n) \log K$ Nernst Equation

Application of Gibb's - Helmholtz equation

Calculation of enthalpy change for the cell reaction (galvanic cell)

If a cell yields *nF* Columbus of electricity in a reversible manner, it must equal to the decrease in the free energy, then

$$-\Delta G = nFE^{o}$$

Where n = no. of electrons involved in the process

F = Faraday = 96,500 coulombs

 E° = Energy in volts

Gibb's - Helmholtz equation

Substituting,
$$-\Delta G = nFE^o$$

$$E^o = -\frac{\Delta H}{nF} + T \left(\frac{\partial E^o}{\partial T} \right)_P$$



(1)

$$\Delta G = \Delta H + T \left(\frac{\partial \Delta G}{\partial T} \right)_{P}$$

$$-nFE^{o} = \Delta H + T \left(\frac{\partial (-nFE^{o})}{\partial T} \right)_{p}$$

$$-nFE^{o} = \Delta H - nFT \left(\frac{\partial E^{o}}{\partial T} \right)_{p}$$

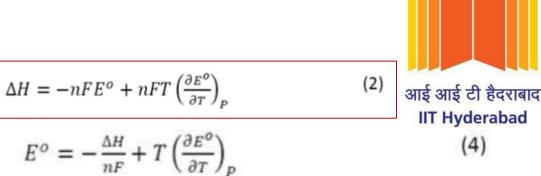
$$\Delta H = -nFE^o + nFT \left(\frac{\partial E^o}{\partial T} \right)_{D} \tag{2}$$

$$\Delta H = -nF \left[E^o - T \left(\frac{\partial E^o}{\partial T} \right)_p \right] \tag{3}$$

Application of Gibb's - Helmholtz equation (cont.

Calculation of EMF of the cell

Diving eqn. (2) by nF



Calculation of entropy change

 ΔH and ΔS are related by eqn.

$$\Delta G = \Delta H - T \Delta S$$

(5)

But, $-\Delta G = nFE^o$ and ΔH can be calculated from eqn. (3). Using these values ΔS can be calculated from eqn. (5)

$$\Delta H = -nF \left[E^o - T \left(\frac{\partial E^o}{\partial T} \right)_p \right] \tag{3}$$

Gibb's – Helmholtz equation is applicable to all process occurring at constant pressure. It is used to calculate ΔH from values of free energy change at two different temperature.

Factors affecting the battery performance

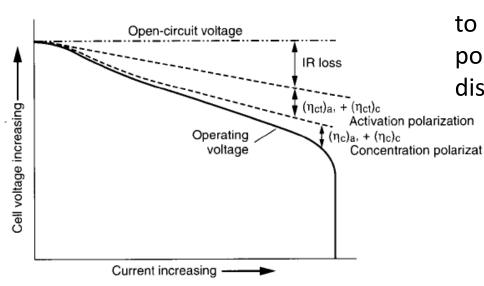
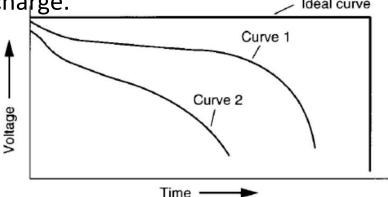


FIGURE 2.1 Cell polarization as a function of operating current.

The difference is caused by IR losses due to cell (and battery) resistance and polarization of the active materials during discharge. Ideal curve



The voltage also drops during discharge as the cell resistance increases due to the accumulation of discharge products, activation and concentration, polarization, and related factors.

When connected to an external load R, the cell voltage E can be expressed as

$$E = E_0 - [(\eta_{ct})_a + (\eta_c)_a] - [(\eta_{ct})_c + (\eta_c)_c] - iR_i = iR$$
 (2.1)

 E_0 = electromotive force or open-circuit voltage of cell where

 $(\eta_{ct})_a$, $(\eta_{ct})_c$ = activation polarization or charge-transfer overvoltage at anode and cathode

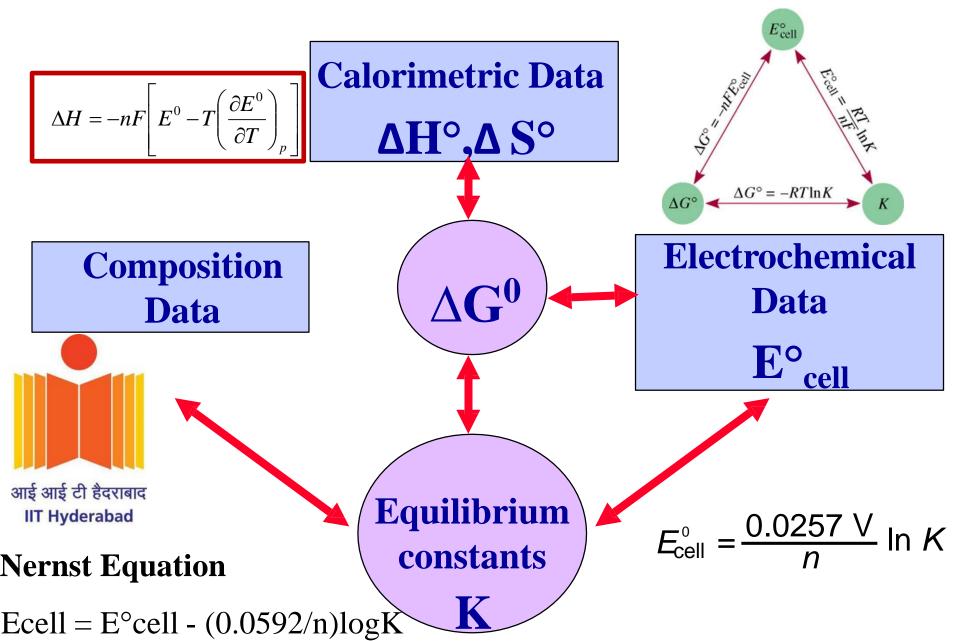
 $(\eta_c)_a$, $(\eta_c)_c$ = concentration polarization at anode and cathode i = operating current of cell on load

 R_i = internal resistance of cell

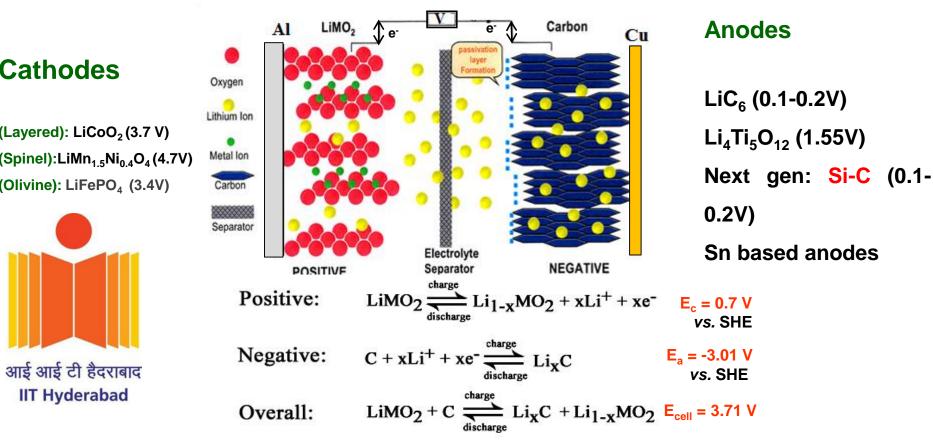


D. Linden, Hand Book of Batteries, 3rd Edition

Equilibrium Constant from Ecell



Schematic presentation of a Li-ion cell



Electrolyte: EC:DMC (1:2) /LiPF₆ (1 M)

Composite Cathodes for Li-ion batteries Positive active mass: LiCoO₂, LiFePO₄ *Conductive additive (e.g. Carbon, carbon nanofibers, graphenes, graphites) *Binder: PVDF, *Current collector (AI)

Composite Anodes for Li-ion batteries

Negative active mass: LiC₆, Li₄Ti₅O₁₂

❖ Conductive additive (e.g. Carbon, carbon nanofibers, graphenes, graphites)

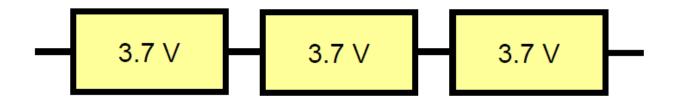
❖ Binder: PVDF, SCMC, Teflon

❖ Current collector (Cu)

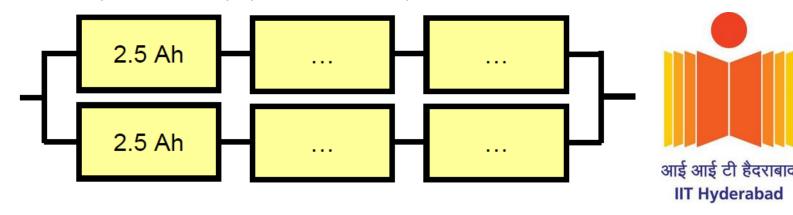
Lithium Ion Batteries

How to combine Li-ion cells?

→ Connect your battery (3.7 V, 2.5 Ah) in series

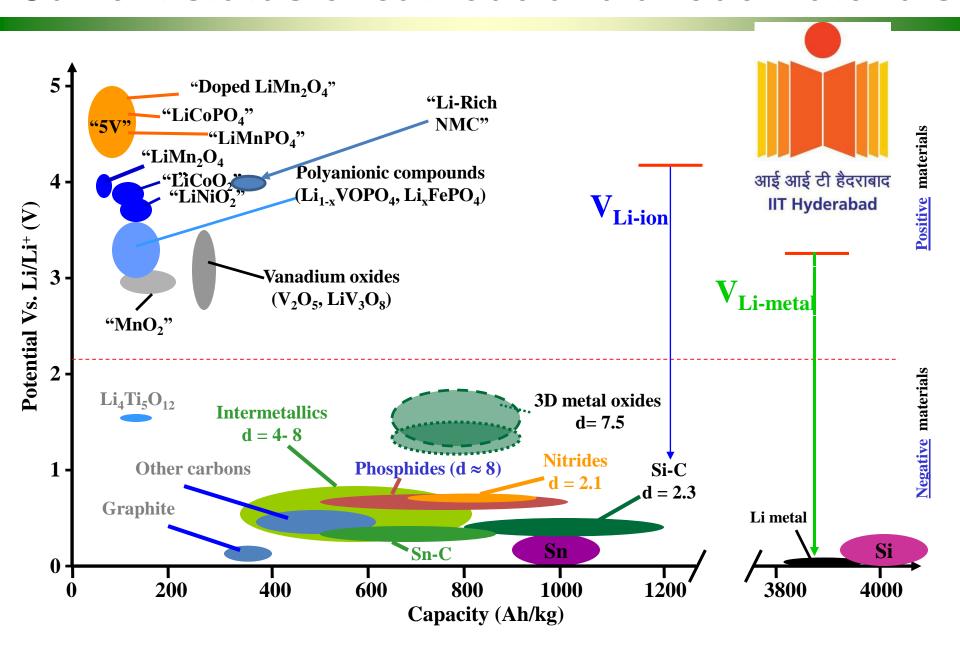


- → 3 times 3.7 V gives you 11.1 V (you get the voltage you need)
- → Connect your battery (3.7 V, **2.5 Ah**) in parallel

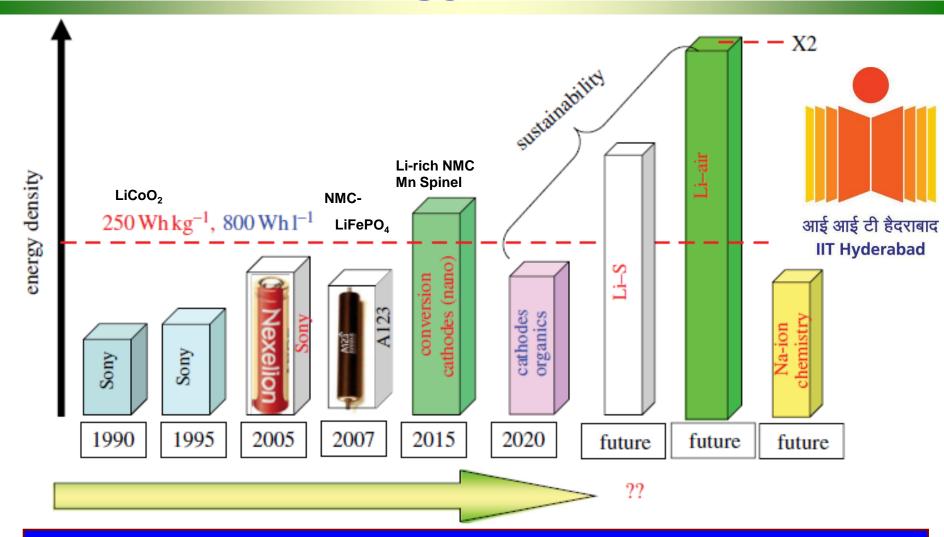


2 times 2.5 Ah gives you 5 Ah (you get the capacity you need)

Current status of cathode and anode Materials



The lithium battery cathode technology landscape



Cathode materials are detrimental to the performance and safety of Li-ion batteries.

Electrochemistry of Lead-Acid Battery

Negative Electrode: Lead

Positive Electrode: Lead dioxide

Electrolyte: Sulfuric acid



At Positive Electrode

$$PbO_2 + H_2SO_4 + 2H^+ + 2e^{-\frac{tasendage}{charge}} PbSO_4 + 2H_2O (E_c = 1.7 V vs. SHE)$$

At Negative Electrode

Pb +
$$H_2SO_4$$
 $\xrightarrow{discharge}$ PbSO₄ + 2H⁺ + 2e⁻ ($E_a = -0.36V$ vs. SHE)

Net Cell Reaction

$$PbO_2 + Pb + 2H_2SO_4 \xrightarrow{discharge} 2PbSO_4 + 2H_2O \quad (E_{cell} = 2.06 \text{ V})$$

Lead-Acid Batteries for Start-Stop Applications

How does a Start-Stop system work?









STOP at red traffic light→ Engine off



Battery is DISCHARGED START at green traffic light

→ Engine crank



Battery is DISCHARGED

Driving phase



Battery is RECHARGED



CELLS AND BATTERIES

1.The anode or negative electrode—the reducing or fuel electrode—which gives up electrons to the external circuit and is oxidized during the electrochemical reaction.

Anode should have following properties:

- 1. Efficiency as a reducing agent,
- 2.high coulombic out put (Ah/g),
- 3.good conductivity,
- 4.stability, ease of fabrication, and low cost.

Practically, metals are mainly used as the anode materials.

Ex: Lithium



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Cathode should have following properties:

- 1. The cathode must be an efficient oxidizing agent,
- 2. be stable when in contact with the electrolyte,
- 3. Have a useful working voltage.



The most of the common cathode materials are **metallic oxides**. Other cathode materials, such as the **halogens** and the **oxyhalides**, **sulfur and its oxides**, are used for special battery systems

Separator:

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Physically the anode and cathode electrodes are electronically isolated in the cell to prevent internal short-circuiting, but are surrounded by the electrolyte.

The separator, however, is permeable to the electrolyte in order to maintain the desired ionic conductivity.

In some cases the electrolyte is immobilized for a non-spill design.

Electrically conducting grid structures or materials may also be added to the electrodes to reduce internal resistance.

- **The electrolyte—the ionic conductor** —which provides the medium for transfer of charge, as ions, inside the cell between the anode and cathode.
- ❖The electrolyte is typically a liquid, such as water or other solvents, with dissolved salts, acids, or alkalis to impart ionic conductivity.
- ❖Some batteries use solid electrolytes, which are ionic conductors at the operating temperature of the cell.

The electrolyte must have good ionic conductivity but not be electronically conductive, as this would cause internal short-circuiting.

- Other important characteristics are non-reactivity with the electrode materials, little change in properties with change in temperature, safety in handling, and low cost.
- Most electrolytes are aqueous solutions, but there are important exceptions as, for example, in thermal and lithium anode batteries, where molten salt and other non-aqueous electrolytes are used to avoid the reaction of the anode with the electrolyte.

Electrolytic conductance

Electrolytic conductance occurs when a voltage is applied to the electrode dipped into an electrolyte solution, ions of the electrolyte move and electric current flows through the electrolytic solution.

- This power of the electrolyte to conduct electricity is known as conductance or conductivity.
- Electrolytic solution also obey Ohm's Law just like metallic conductor.







Electronic conductors	Electrolytic conductors
(1) Flow of electricity take place without the decomposition of substance.	(1)Flow of electricity takes place by the decomposition of the substance.
(2) Conduction is due to the flow of electron	(2) Flow of electricity is due to the movement of ions
(3) Conduction decreases with increase in temperature	(3) Conduction increases with increase in temperature



The conductivity of a solution of water is highly dependent on its concentration of dissolved salts and sometimes other chemical species which tend to ionize in the solution.

Electrical conductivity of water samples is used as an indicator of how salt free or impurity free the sample is; the purer the water, the lower the conductivity.

Solution	Electric Conductivity (Sm ⁻¹)	
Seawater	5	आई आई टी हैदराबाद IIT Hyderabad
Drinking water	0.0005 to 0.05	
De-ionized water	5.5 x 10 ⁻⁶	

What is electrolyte?

 Any substance that produce ions when dissolved in a solvent (usually water) is an electrolyte.

Dissociate in a solvent to give two or more particles.

Consequently, the total number of particles increases in solution

Types of electrolytes

Strong electrolyte

$$NaCl+H_2O
ightarrow Na^+ + Cl^-$$
 आई आई टी हैदराबार $HCl+H_2O
ightarrow H_3O^+ + Cl^-$ IIT Hyderabad

Weak electrolyte

$$CH_3COOH + H_2O \rightarrow CH_3COO^- + H^+$$

 $NH_3 + H_2O \rightarrow NH_4^+ + OH^-$

Non-electrolyte

 $C_{12}H_{22}O_{11} + H_2O \rightarrow Glu\cos e + Fructose$ Slutions of cane sugar, glucose, urea etc.

Degree of dissociation

It is defined as the fraction of total substance that undergoes dissociated into ions.

No. of moles of substance dissociated

$$\alpha = \frac{\text{No. of moles of substance dissociated}}{\text{Total no. of moles of the substance taken}}$$

$$\alpha = \frac{C_{\text{dissociated}}}{C_{\text{Total}}} = \frac{N_{\text{dissociated}}}{N_{\text{Total}}}$$



Percent (%) of dissociation =
$$\frac{[HA]_{dissociated}}{[HA]_{Initial}} \times 100$$

Or Degree of dissociation can be written as
$$\alpha = \frac{i-1}{m-1}$$

where m is the number of particles in solution, i is Van't Hoff factor

For example: the electrolytes of the type AB, such as KCl, NaCl, etc., the number of particles in solution m = 2 Then α = i-1

<u>Van't Hoff factor 'i'</u> to express the extent of association or dissociation of solutes in solution.

- $i = \frac{normal\ molar\ mass\ of\ the\ solute}{observed\ molar\ mass\ of\ the\ solute}$
- ❖ In case of association, observed molar mass being more than the normal, the factor 'i' has a value less than 1.
- In case of dissociation, the Van't Hoff factor is more than 1 because the observed molar mass has a lesser value.
 For most ionic compounds dissolved in water, the van 't Hoff factor is equal to
- the number of discrete ions in a formula unit of the substance (Ex: NaCl, KCl etc. i= 1+1=2.
- In case of solutes which do not undergo any association or dissociation in a solvent. Van't Hoff factor 'i' will be equal to 1 because the observed and normal molar masses will be same.
- Example: For most non-electrolytes dissolved in water, the van't Hoff factor is essentially 1.
- ❖ The deviation for the van 't Hoff factor tends to be greatest where the ions have multiple charges.

According to the Degree of dissociation (α) electrolytes can be classified into the following:

strong electrolytes are compounds that dissociate to a large extent (α > 30%) into ions when dissolved in water. For example, HCl, H₂SO₄, HNO₃, HI, NaOH, KOH, KCl.

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- medium strong electrolytes $\alpha = 2 30\%$. H₃PO₄, H₃PO₃.
- weak electrolytes are compounds that dissociate to only a small extent α <2%. For example, NH₄OH, H₂S, HCN, H₂CO₃.
- nonelectrolytes α = 0 are compounds that don't dissociate when dissolved in water. Example: alcohols, H₂O

Activity and Concentration

❖ Activity – "effective concentration" of a species in a mixture



- The activity of an ion is particularly influenced by its surroundings.
 - Activity is treated as a dimensionless quantity
 - The activity of pure substances in condensed phases (solid or liquids) is normally taken as unity.
- Activity depends on temperature, pressure and composition of the mixture
- For gases, the effective partial pressure is usually referred to as fugacity.

Activity and Mean Ionic Activity of Electrolytes

- ❖ We take into account of activity of Individual ions
- There is no expt. method by which activities of individual ions can be determined. Because it is not possible to have solutions of one kind of ion.
- ❖ Therefore activity or mean ionic activity a_± of the electrolyte is considered.

For uni-univalent electrolyte: Ex: HCl ($H^+=a_+$ and $Cl^-=a_-$ Activity $a = a_+ a_-$

or Mean ionic activity =
$$\,a_{\pm} = \sqrt{a_{+}a_{-}}\,$$

Squaring
$$\Rightarrow (a_{\pm})^2 = a_{+}a_{-}$$

$$\Rightarrow (a_{\pm})^2 = a$$

Mean Ionic Activity of Electrolytes

Consider an electrolyte A_xB_v ionzing as

$$A_x B_y \longrightarrow x A^+ + y B^-$$

Then activity $a = (a_+)^x(a_-)^y = (a\pm)^{x+y}$



Activity coefficient of the electrolyte

- ❖ Ion-ion and ion-H₂O interactions (hydration shell) cause number of ions available to react chemically ("free" ions) to be less than the number present.
- Concentration can be related to activity using the activity coefficient γ, where [a] = γ (m)

Until now we have assumed that activity, a, is equal to concentration, m, by Setting $\gamma = 1$ when dealing with dilute aqueous solutions...

Activity coefficient of the electrolyte

The activity coefficient of the electrolyte A_xB_y is given by

$$a = \left(\gamma_+ m_+\right)^x \left(\gamma_- m_-\right)^y = \left(\gamma_+ x m\right)^x \left(\gamma_- y m\right)^y = x^x y^y \left(m \gamma_\pm\right)^{x+y}$$

$$(\gamma_{\pm})^{x+y} = \gamma_{\pm}^x \gamma_{\pm}^y$$

For uni-univalent electrolyte:

$$HCI, x = 1, y = 1$$

$$a = (a_{\pm})^2 = (\gamma_{\pm} m)^2$$



For uni-bivalent electrolyte: Ex: Na_2SO_4 , x=2 and y =1.

Hence
$$a = (a_{\pm})^3 = 2^2 \times 1(\gamma_{\pm} m)^3 = 4m^3 \gamma_{\pm}^3$$

The value of γ depends on:

- Concentration of ions and charge in the solution
- Charge of the ion

Ionic strength

The ionic strength of a solution is a measure of the concentration of ions in that solution.

The total electrolyte concentration in solution will affect important properties such as the dissociation or the solubility of different salts.

The ionic strength, I, of a solution is a function of the concentration of all ions present in that solution.

$$I = \frac{1}{2} \sum_{i=1}^{n} m_i z_i^2$$

m_i the molal concentration of ion i (M, mol/Kg), z_i is the charge number of that ion, and the sum is taken over all ions in the solution.

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For a 1:1 electrolyte such as sodium chloride, the ionic strength is given by

$$I = \frac{1}{2} (m_{Na^{+}} z_{Na^{+}}^{2} + m_{Cl^{-}} z_{Cl^{-}}^{2}) = \frac{1}{2} (m_{Na^{+}} 1^{2} + m_{Cl^{-}} 1^{2}) = \frac{1}{2} (m_{Na^{+}} + m_{Cl^{-}})$$

Calculate the ionic strength of 0.15 molal KCl solution

Debye-Hückel theory of strong electrolytes

For evaluation of mean ionic activity coefficient

Assumptions

The Debye-Hückel theory is based on three assumptions of how ions act in solution:



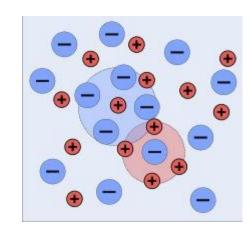
- Electrolytes completely dissociate into ions in solution.
- Ions of electrolytes interact with themselves according to the electrostatic's law.
- The nature of solvent influences on the interaction between ions.
- A central ion is surrounded by the ion's atmosphere (ions of opposite charge).
- The size of the central ion is like a point charge.

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Debye-Hückel theory continuing....

The ions are shown as spheres with unit electrical charge.

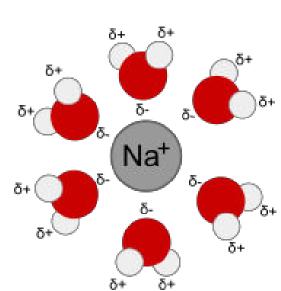
lons of charge z_1e^+ and z_2e^- , where z can be any integer.



The principal assumption is that departure from ideality is due to electrostatic interactions between ions, mediated by Coulomb's law: the force of interaction between two ions, separated by a distance, r in a medium of relative permittivity ε_r is given by

$$Force = \frac{z_1 z_2 e^2}{4\pi \varepsilon_r \varepsilon r^2}$$

❖ If the solvent has high dielectric constant the electrostatic between ions will be small.



Debye-Hückel theory continuing....

- 2. Solutions of Electrolytes are very dilute, on the order of 0.01 M.
- Solution is very dilute, the distance between the ions will be large.
- 3. Each ion is surrounded by ions of the opposite charge, on average.

Activity coefficient of single ion i in dilute solution of strong electrolyte

$$\log \gamma_{i} = -A z_{i}^{2} \sqrt{I}$$
where $I = \frac{1}{2} \sum_{i} m_{i} z_{i}^{2} = \frac{1}{2} (m_{1} z_{1}^{2} + m_{2} z_{2}^{2} + m_{i} z_{i}^{2})$

where
$$A = \frac{e^3}{4.606(DkT)^{\frac{3}{2}}} \times \sqrt{\frac{8\pi N_A \rho}{10^3}}$$

T = 298K and water as a solvent,

D = dielectric constant = 78.3

$$\rho$$
= 1 g/cc,

 N_A = Avogardo's number= 6.023 X 10²³,

 $k=Boltzmann constant = 1.38 \times 10^{16} erg/K$



Debye-Hückel theory continuing....

Putting these values: A = 0.51 at 298K.

$$\log \gamma_i = -0.51 \, z_i^2 \sqrt{I}$$



Mean ionic activity coefficient of strong electrolytes in dilute solution containing the electrolyte $A_x B_y$ in general is given by.

$$\log \gamma_{\pm} = -A z_{+} z_{-} \sqrt{I}$$

$$\log \gamma_{\pm} = -0.51 z_{+} z_{-} \sqrt{I}$$

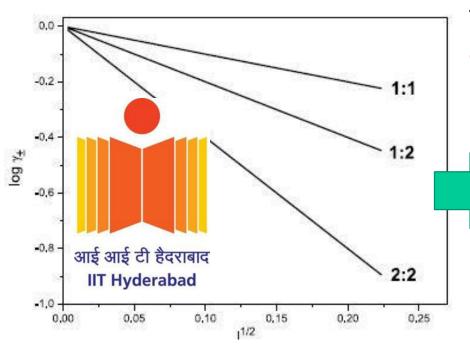
Debye-Hückel limiting law and used to calculate mean ionic activity coefficient of the strong electrolytes in dilute solution.

The activity coefficient of the electrolytes depends only upon the ionic strength of the solution.

Debye-Hückel theory continuing....

Negative value means mean ionic activity coefficient is less than 1.

According to Debye–Hückel equation if z_{+} and z_{-} are same, the activity coefficient varies with ionic strength of the solution and not with nature of the electrolytes.



Predictions of Debye-Huckel limiting law

Thus all electrolytes of same valency type should have equal activity coefficient at the same ionic strength.

- ❖ All the electrolytes should give st. line passing through origin.
- ❖ All slopes depends on Z₊Z₋
- ❖ For uni-univalent= slope = 0.51
- ❖ Bi, Uni-bi, bi-univalent = 2 X 0.51