

Multi-Label Classification

Multilabel classification

+

Interstellar (2014)

PG-13 | 2h 49min | **Adventure, Drama, Sci-Fi** | 7 November 2014 (USA)

★ 8.6

1,315,559

☆

Rate This





2:28 Trailer

13 VIDEOS | 396 IMAGES

A team of explorers travel through a wormhole in space in an attempt to ensure humanity's survival.

Multilabel Classification

0
votes

Can we get (Percentage ratio, eg (detected object) person obtains 60% of the image) from Output of Image segmentation using Tensorflow

0
answers

I am trying to read what percent of the image the detected object covers . I've already tried Tensorflow object detection and its working great, but due to changing of requirements now I want the ...

3 views

tensorflow

object-detection

image-segmentation

tensorflow-datasets

tensorflow-lite

asked 3 mins ago



Karan Gada

15 ● 6

0
votes

Getting "Unexpected reserved word" when doing await in export module?

0
answers

In my export module, I want to use await export default { template : await (await fetch("template.html")).text(); } but this doesn't work. It gets Unexpected reserved word because of await. ...

10 views

javascript

import

async-await

export

asked 3 mins ago



omega

10.8k ● 50 ● 137 ● 294

Multilabel Classification

Applications: E-mail

Enron, e-mails messages made public from the Enron corporation.

"a few beers after work?" work personal important

For example, the **UC Berkeley Enron Email Analysis Project** multi-labeled 1702 *Enron* e-mails into 53 categories:

Company Business, Strategy, etc.

Purely Personal

Empty Message

Forwarded email(s)

...

Multilabel Classification



Single-label classification: Is this a picture of a beach?

$\in \{\text{yes}, \text{no}\}$

Multi-label classification: Which labels are relevant to this picture?

$\subseteq \{\text{beach}, \text{sunset}, \text{foliage}, \text{field}, \text{mountain}, \text{urban}\}$

Multilabel Classification

Labelling music/tracks with genres / voices, concepts, etc.



e.g., Emotions dataset, audio tracks labelled with different moods, among:
{

- amazed-surprised,
- happy-pleased,
- relaxing-calm,
- quiet-still,
- sad-lonely,
- angry-aggressive

Multi-label Classification

Sub-Story Detection in Twitter with Hierarchical Dirichlet Processes

P. K. Srijith¹, Mark Hepple¹, Kalina Bontcheva¹, Daniel Preotiuc-Pietro²

¹ Department of Computer Science, The University of Sheffield, UK

² Computer & Information Science, University of Pennsylvania, USA

{pk.srijith, m.r.hepple, k.bontcheva}@sheffield.ac.uk
danielpr@sas.upenn.edu

Abstract

Social media has now become the de facto information source on real world events. The challenge, however, due to the high volume and velocity nature of social media streams, is in how to follow all posts pertaining to a given event over time – a task referred to as story detection. Moreover, there are often several different stories pertaining to a given event, which we refer to as *sub-stories* and the corresponding task of their automatic detection – as *sub-story detection*. This paper proposes hierarchical Dirichlet processes (HDP), a probabilistic topic model, as an effective method for automatic sub-story detection. HDP can learn sub-topics associated with sub-stories which enables it to handle subtle variations in sub-stories. It is compared with state-of-the-art story detection approaches based on locality sensitive hashing and spectral clustering. We demonstrate the superior performance of HDP for sub-story detection on real world Twitter data sets using various evaluation measures. The ability of HDP to learn sub-topics helps it to recall the sub-stories with high precision. Another contribution of this paper is in demonstrating that the conversational structures within the Twitter stream can be used to improve sub-story detection performance significantly.

keywords : sub-story detection, hierarchical Dirichlet process, spectral clustering, locality sensitive hashing

Multilabel classification



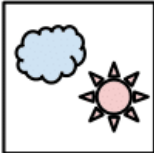


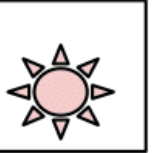




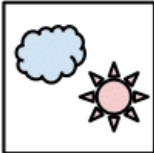

Multi-Class		Multi-Label	
C = 3	Samples	Samples	
			
			
			
	Labels (t)	Labels (t)	
	[0 0 1] [1 0 0] [0 1 0]	[1 0 1] [0 1 0] [1 1 1]	

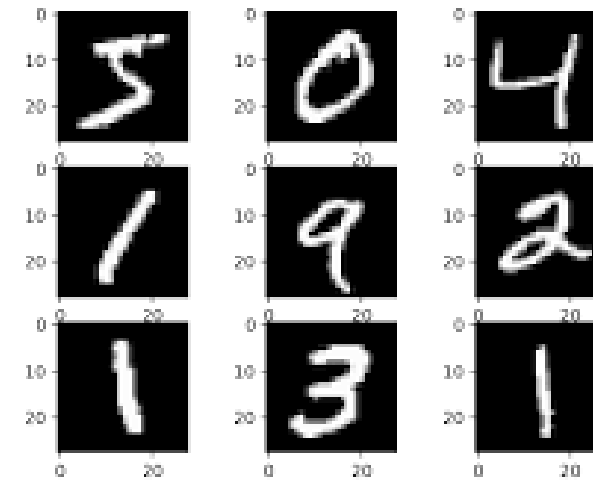
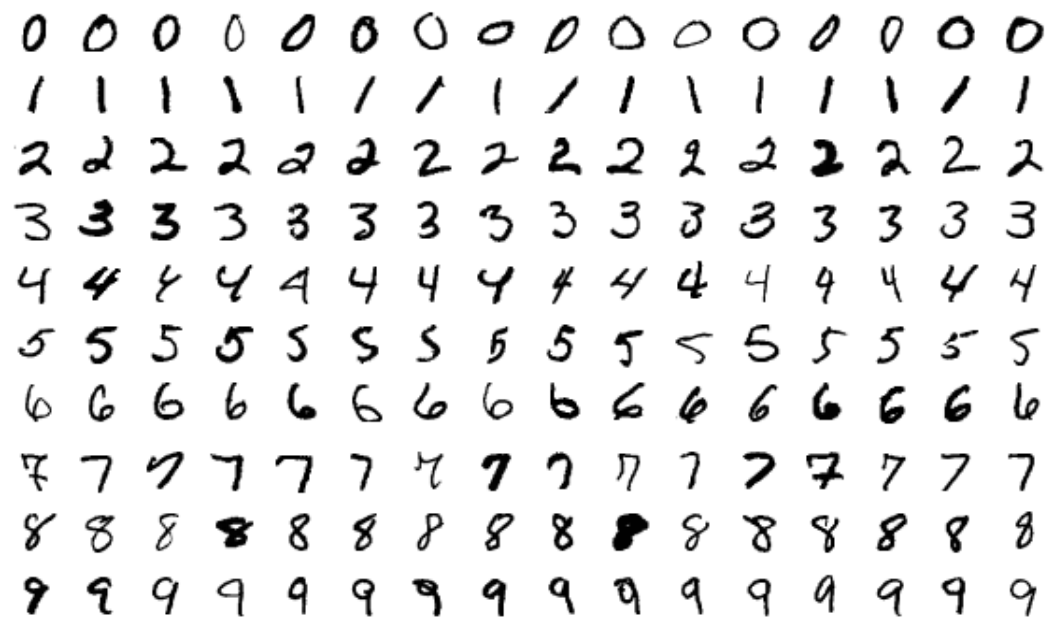
Table : Single-label $Y \in \{0, 1\}$

X_1	X_2	X_3	X_4	X_5	Y
1	0.1	3	1	0	0
0	0.9	1	0	1	1
0	0.0	1	1	0	0
1	0.8	2	0	1	1
1	0.0	2	0	1	0
0	0.0	3	1	1	?

Table : Multi-label $Y_1, \dots, Y_L \in 2^L$

X_1	X_2	X_3	X_4	X_5	Y_1	Y_2	Y_3	Y_4
1	0.1	3	1	0	0	1	1	0
0	0.9	1	0	1	1	0	0	0
0	0.0	1	1	0	0	1	0	0
1	0.8	2	0	1	1	0	0	1
1	0.0	2	0	1	0	0	0	1
0	0.0	3	1	1	?	?	?	?

Multi-class Classification



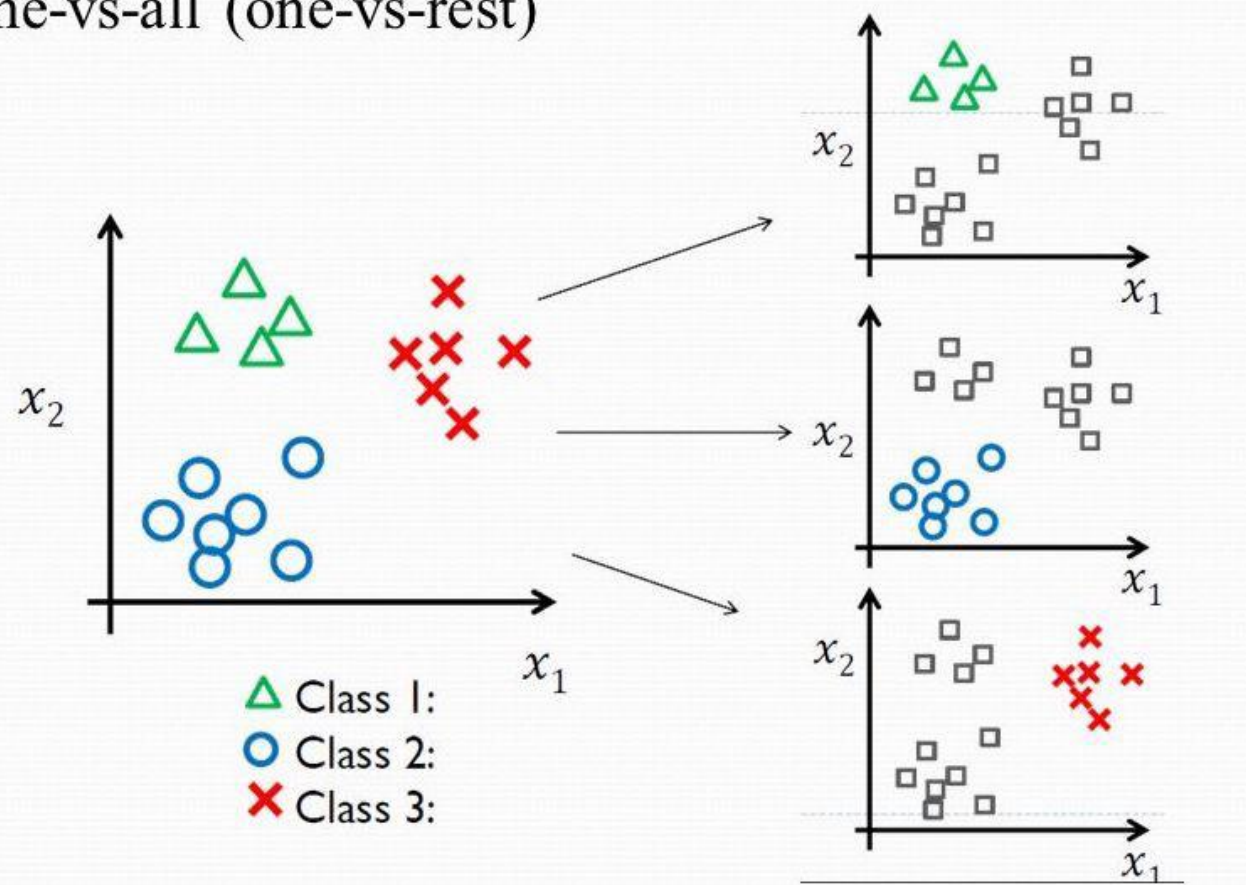
- In multi class classification, a sample belongs to only one class

X1	X2	X3	X4	X5	Y1	Y2	Y3	Y4
1	0.1	3	1	0	0	1	0	0
0	0.9	1	0	1	1	0	0	0
0	0.0	1	1	0	0	1	0	0
1	0.8	2	0	1	1	0	0	0
1	0.0	2	0	1	0	0	0	1
0	0.0	3	1	1	?	?	?	?

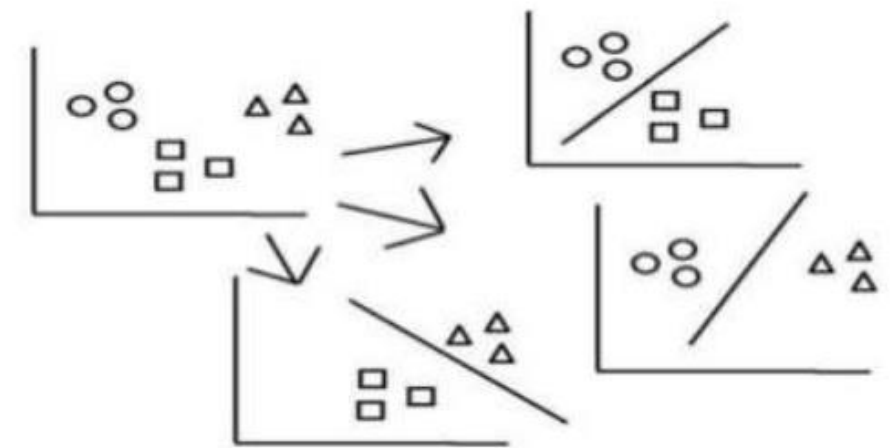
Multi-class Classification

- In multi class classification, a sample belongs to only one class
- Logistic Regression with Softmax, K-NN... or using Binary classifiers

One-vs-all (one-vs-rest)



One-vs-One (OVO)



Multilabel classification

There are **dependencies** (i.e., *correlations, relationships, co-occurrences*) among labels

- e.g., {relaxing-calm, quiet-still} vs. {relaxing-calm, angry-aggressive}
- e.g., {beach, sunset} vs. {beach, field}

From the IMDb dataset:

- $P(\text{family})P(\text{adult}) = 0.068 \cdot 0.015 = 0.001$ (≈ 121 movies)
- $P(\text{family}, \text{adult}) = 0.0$ (**0** movies!)

On most datasets:

- $P(\mathbf{y} = [1, 1, 1, 1, 1, 1]) = 0$

Multilabel classification

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On most datasets:

- $P(\mathbf{y} = [1, 1, 1, 1, 1, 1]) = 0$

The main challenges are to

- model **label dependencies**; and
- do this **efficiently**.

Methods for Multi-Label Classification

Problem Transformation Methods

- Transforms the multi-label problem into single-label problem(s)
- Use any off-the-shelf single-label classifier to suit requirements
- i.e., **Adapt your data to the algorithm**

Algorithm Adaptation Methods

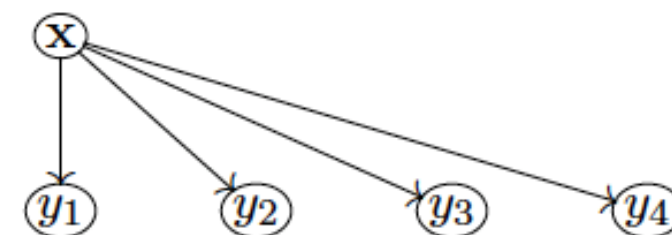
- Adapt a single-label algorithm to produce multi-label outputs
- Benefit from specific classifier advantages (e.g., efficiency)
- i.e., **Adapt your algorithm to the data**

Many methods involve a mix of both approaches.

Binary Relevance

\mathbf{X}	Y_1	Y_2	Y_3	Y_4
$\mathbf{x}^{(1)}$	0	1	1	0
$\mathbf{x}^{(2)}$	1	0	0	0
$\mathbf{x}^{(3)}$	0	1	0	0
$\mathbf{x}^{(4)}$	1	0	0	1
$\mathbf{x}^{(5)}$	0	0	0	1

Prediction: $\hat{\mathbf{y}} = [h_1(\tilde{\mathbf{x}}), \dots, h_L(\tilde{\mathbf{x}})]$



... just make L separate binary problems (one for each label):

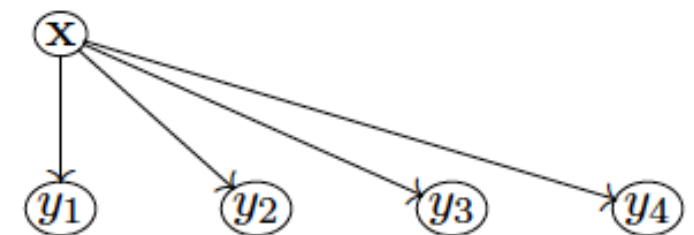
\mathbf{X}	Y_1	\mathbf{X}	Y_2	\mathbf{X}	Y_3	\mathbf{X}	Y_4
$\mathbf{x}^{(1)}$	0	$\mathbf{x}^{(1)}$	1	$\mathbf{x}^{(1)}$	1	$\mathbf{x}^{(1)}$	0
$\mathbf{x}^{(2)}$	1	$\mathbf{x}^{(2)}$	0	$\mathbf{x}^{(2)}$	0	$\mathbf{x}^{(2)}$	0
$\mathbf{x}^{(3)}$	0	$\mathbf{x}^{(3)}$	1	$\mathbf{x}^{(3)}$	0	$\mathbf{x}^{(3)}$	0
$\mathbf{x}^{(4)}$	1	$\mathbf{x}^{(4)}$	0	$\mathbf{x}^{(4)}$	0	$\mathbf{x}^{(4)}$	1
$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	1

and train with any off-the-shelf binary classifier.

Binary Relevance

\mathbf{X}	Y_1	Y_2	Y_3	Y_4
$\mathbf{x}^{(1)}$	0	1	1	0
$\mathbf{x}^{(2)}$	1	0	0	0
$\mathbf{x}^{(3)}$	0	1	0	0
$\mathbf{x}^{(4)}$	1	0	0	1
$\mathbf{x}^{(5)}$	0	0	0	1

Prediction: $\hat{\mathbf{y}} = [h_1(\tilde{\mathbf{x}}), \dots, h_L(\tilde{\mathbf{x}})]$



...just make L separate binary problems (one for each label):

\mathbf{X}	Y_1	\mathbf{X}	Y_2	\mathbf{X}	Y_3	\mathbf{X}	Y_4
$\mathbf{x}^{(1)}$	0	$\mathbf{x}^{(1)}$	1	$\mathbf{x}^{(1)}$	1	$\mathbf{x}^{(1)}$	0
$\mathbf{x}^{(2)}$	1	$\mathbf{x}^{(2)}$	0	$\mathbf{x}^{(2)}$	0	$\mathbf{x}^{(2)}$	0
$\mathbf{x}^{(3)}$	0	$\mathbf{x}^{(3)}$	1	$\mathbf{x}^{(3)}$	0	$\mathbf{x}^{(3)}$	0
$\mathbf{x}^{(4)}$	1	$\mathbf{x}^{(4)}$	0	$\mathbf{x}^{(4)}$	0	$\mathbf{x}^{(4)}$	1
$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	1

and train with any off-the-shelf binary classifier.

Disadvantages

Does not Model label dependency
Class Imbalance

Stacked Binary Relevance

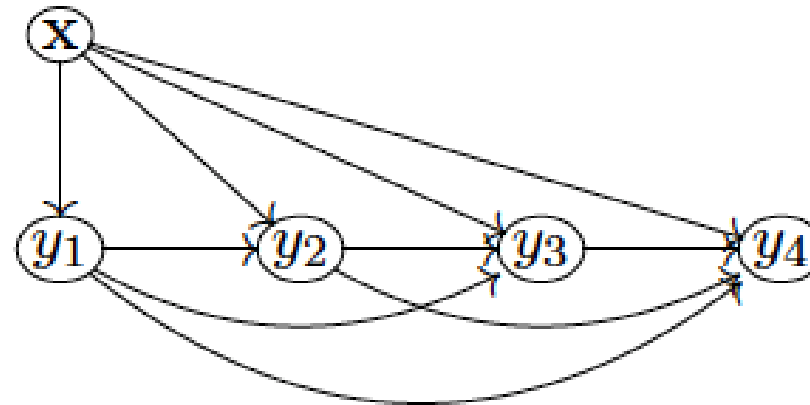
$$\hat{y} = h^2(h^1(\tilde{x}))$$

For example, given \tilde{x} ,

	\hat{Y}_1	\hat{Y}_2	\hat{Y}_3	\hat{Y}_4
$h^1(\tilde{x})$	1	0	0	1
$\hat{y} = h^2(h^1(\tilde{x}))$	1	0	0	0

BR stacked with feature outputs. For more information see: Shantanu Godbole, Sunita Sarawagi:
Discriminative Methods for Multi-labeled Classification. In: Advances in Knowledge Discovery and
Data Mining, 22-30, 2004.

Chain Classifier



Like BR, make L binary problems, but include previous predictions as feature attributes.

\mathbf{X}	Y_1	\mathbf{X}	Y_1	Y_2	\mathbf{X}	Y_1	Y_2	Y_3	\mathbf{X}	Y_1	Y_2	Y_3	Y_4
$\mathbf{x}^{(1)}$	0	$\mathbf{x}^{(1)}$	0	1	$\mathbf{x}^{(1)}$	0	1	1	$\mathbf{x}^{(1)}$	0	1	1	0
$\mathbf{x}^{(2)}$	1	$\mathbf{x}^{(2)}$	1	0	$\mathbf{x}^{(2)}$	1	0	0	$\mathbf{x}^{(2)}$	1	0	0	0
$\mathbf{x}^{(3)}$	0	$\mathbf{x}^{(3)}$	0	1	$\mathbf{x}^{(3)}$	0	1	0	$\mathbf{x}^{(3)}$	0	1	0	0
$\mathbf{x}^{(4)}$	1	$\mathbf{x}^{(4)}$	1	0	$\mathbf{x}^{(4)}$	1	0	0	$\mathbf{x}^{(4)}$	1	0	0	1
$\mathbf{x}^{(5)}$	0	$\mathbf{x}^{(5)}$	0	0	$\mathbf{x}^{(5)}$	0	0	0	$\mathbf{x}^{(5)}$	0	0	0	1

Label Powerset Method

To model label correlations, we can ...

\mathbf{X}	Y_1	Y_2	Y_3	Y_4
$\mathbf{x}^{(1)}$	0	1	1	0
$\mathbf{x}^{(2)}$	1	0	0	0
$\mathbf{x}^{(3)}$	0	1	1	0
$\mathbf{x}^{(4)}$	1	0	0	1
$\mathbf{x}^{(5)}$	0	0	0	1

... make a single multi-*class* problem with 2^L possible class values:

\mathbf{X}	$Y \in 2^L$
$\mathbf{x}^{(1)}$	0110
$\mathbf{x}^{(2)}$	1000
$\mathbf{x}^{(3)}$	0110
$\mathbf{x}^{(4)}$	1001
$\mathbf{x}^{(5)}$	0001

and train with any off-the-shelf multi-*class* classifier.

Label Powerset Method

To model label correlations, we can ...

X	Y_1	Y_2	Y_3	Y_4
$x^{(1)}$	0	1	1	0
$x^{(2)}$	1	0	0	0
$x^{(3)}$	0	1	1	0
$x^{(4)}$	1	0	0	1
$x^{(5)}$	0	0	0	1

... make a single multi-*class* problem with 2^L possible class values:

X	$Y \in 2^L$
$x^{(1)}$	0110
$x^{(2)}$	1000
$x^{(3)}$	0110
$x^{(4)}$	1001
$x^{(5)}$	0001

- **complexity**: many class labels
- **imbalance**: not many examples per class label

and train with any off-the-shelf multi-*class* classifier.

Ensembles of Random k-label Subsets (RAKEL)

- Do LP on M subsets $\subset \{\lambda_1, \dots, \lambda_L\}$ of size k

\mathbf{X}	$Y \in 2^k$	\mathbf{X}	$Y \in 2^k$	\mathbf{X}	$Y \in 2^k$	\mathbf{X}	$Y \in 2^k$
$\mathbf{x}^{(1)}$	011	$\mathbf{x}^{(1)}$	010	$\mathbf{x}^{(1)}$	010	$\mathbf{x}^{(1)}$	110
$\mathbf{x}^{(2)}$	100	$\mathbf{x}^{(2)}$	100	$\mathbf{x}^{(2)}$	100	$\mathbf{x}^{(2)}$	000
$\mathbf{x}^{(3)}$	011	$\mathbf{x}^{(3)}$	010	$\mathbf{x}^{(3)}$	010	$\mathbf{x}^{(3)}$	110
$\mathbf{x}^{(4)}$	100	$\mathbf{x}^{(4)}$	101	$\mathbf{x}^{(4)}$	101	$\mathbf{x}^{(4)}$	001
$\mathbf{x}^{(5)}$	000	$\mathbf{x}^{(5)}$	001	$\mathbf{x}^{(5)}$	001	$\mathbf{x}^{(5)}$	001

- 2^k problems much easier to deal with than 2^L (but still models label dependencies)
- use k and M (number of models) to trade-off dependency modelling and scalability

Ensemble Methods : Prediction

Make Prediction by voting

	\hat{y}_1	\hat{y}_2	\hat{y}_3	\hat{y}_4
$\mathbf{h}^1(\tilde{\mathbf{x}})$	1	0	1	
$\mathbf{h}^2(\tilde{\mathbf{x}})$		1	1	0
$\mathbf{h}^3(\tilde{\mathbf{x}})$	1		1	0
$\mathbf{h}^4(\tilde{\mathbf{x}})$	1	0		0
$\mathbf{h}(\tilde{\mathbf{x}})$	3	1	3	0
$\hat{\mathbf{y}}$	1	0	1	0

Grigorios Tsoumakas, Ioannis Katakis, and Ioannis Vlahavas. Random k-labelsets for multilabel classification. *IEEE Transactions on Knowledge and Data Engineering*, 23(7): 1079–1089, 2011a.

Multi-label Data: Datasets

	\mathcal{X} (data inst.)	\mathcal{Y} (labels)	L	N	D	LC
Music	audio data	emotions	6	593	72	1.87
Scene	image data	scene labels	6	2407	294	1.07
Yeast	genes	biological fns	14	2417	103	4.24
Genbase	genes	biological fns	27	661	1185	1.25
Medical	medical text	diagnoses	45	978	1449	1.25
Enron	e-mails	labels, tags	53	1702	1001	3.38
Reuters	news articles	categories	103	6000	500	1.46
TMC07	textual reports	errors	22	28596	500	2.16
Ohsumed	medical articles	disease cats.	23	13929	1002	1.66
IMDB	plot summaries	genres	28	120919	1001	2.00
20NG	posts	news groups	20	19300	1006	1.03
MediaMill	video data	annotations	101	43907	120	4.38
Del.icio.us	bookmarks	tags	983	16105	500	19.02

- L number of labels
- N number of examples
- D number of input feature attributes
- Label Cardinality (LC) $\frac{1}{N} \sum_{i=1}^N \sum_{j=1}^L y_j^{(i)}$ (Average number of labels per example)

Multi-Label Evaluation

0/1 LOSS

$$= \frac{1}{N} \sum_{i=1}^N \mathcal{I}(\hat{\mathbf{y}}^{(i)} \neq \mathbf{y}^{(i)})$$
$$= 0.60$$

	$\mathbf{y}^{(i)}$	$\hat{\mathbf{y}}^{(i)}$
$\tilde{\mathbf{x}}^{(1)}$	[1 0 1 0]	[1 0 0 1]
$\tilde{\mathbf{x}}^{(2)}$	[0 1 0 1]	[0 1 0 1]
$\tilde{\mathbf{x}}^{(3)}$	[1 0 0 1]	[1 0 0 1]
$\tilde{\mathbf{x}}^{(4)}$	[0 1 1 0]	[0 1 0 0]
$\tilde{\mathbf{x}}^{(5)}$	[1 0 0 0]	[1 0 0 1]

HAMMING LOSS

$$= \frac{1}{NL} \sum_{i=1}^N \sum_{j=1}^L \mathcal{I}[\hat{y}_j^{(i)} \neq y_j^{(i)}]$$
$$= 0.20$$

Multi-Label Evaluation

	$\mathbf{y}^{(i)}$	$\hat{\mathbf{y}}^{(i)}$
$\tilde{\mathbf{x}}^{(1)}$	[1 0 1 0]	[1 0 0 1]
$\tilde{\mathbf{x}}^{(2)}$	[1 0 0 1]	[1 0 0 1]
$\tilde{\mathbf{x}}^{(3)}$	[0 1 1 0]	[0 1 0 0]
$\tilde{\mathbf{x}}^{(4)}$	[1 0 0 0]	[1 0 1 1]
$\tilde{\mathbf{x}}^{(5)}$	[0 1 0 1]	[0 1 0 1]

Multi-Label Evaluation

	$\mathbf{y}^{(i)}$	$\hat{\mathbf{y}}^{(i)}$
$\tilde{\mathbf{x}}^{(1)}$	[1 0 1 0]	[1 0 0 1]
$\tilde{\mathbf{x}}^{(2)}$	[1 0 0 1]	[1 0 0 1]
$\tilde{\mathbf{x}}^{(3)}$	[0 1 1 0]	[0 1 0 0]
$\tilde{\mathbf{x}}^{(4)}$	[1 0 0 0]	[1 0 1 1]
$\tilde{\mathbf{x}}^{(5)}$	[0 1 0 1]	[0 1 0 1]

- HAM. Loss 0.3
- 0/1 Loss 0.6

Multi-Label classification softwares

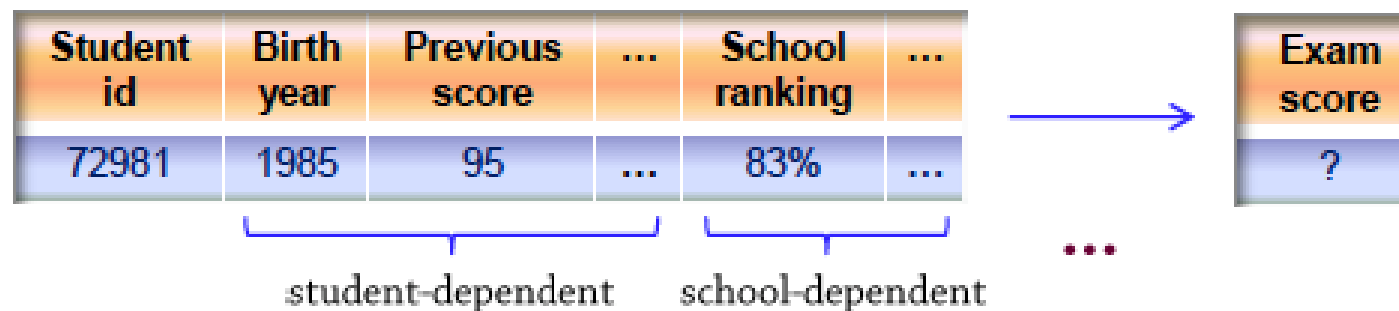
- MULAN and MEKA based on WEKA provides multi-label classification
- scikit-multilearn: A scikit-based Python environment for performing multi-label classification

Multi-Task Learning

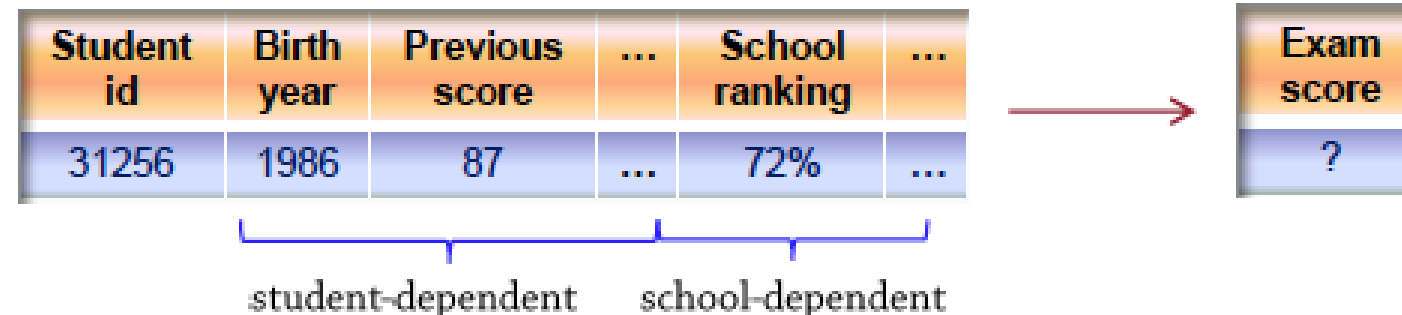
Multiple Tasks

○ Examination Scores Prediction¹ (Argyriou et. al.'08)

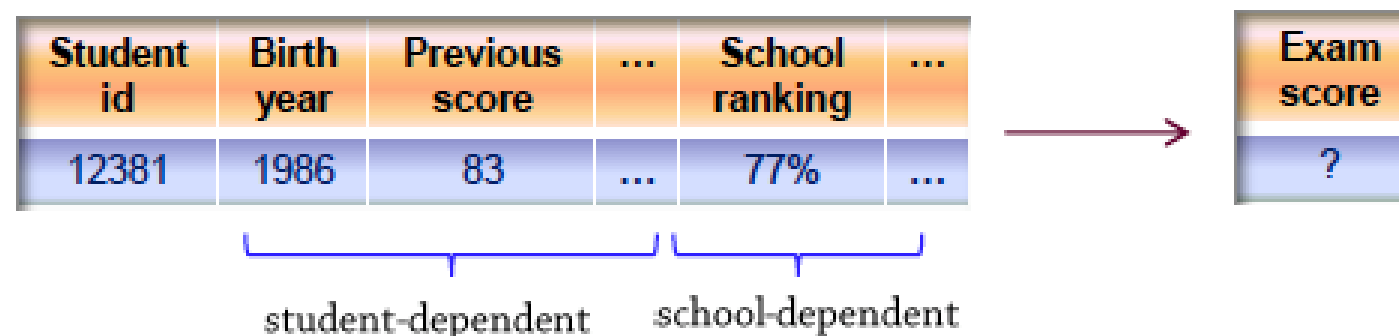
School 1 - Alverno High School



School 138 - Jefferson Intermediate School

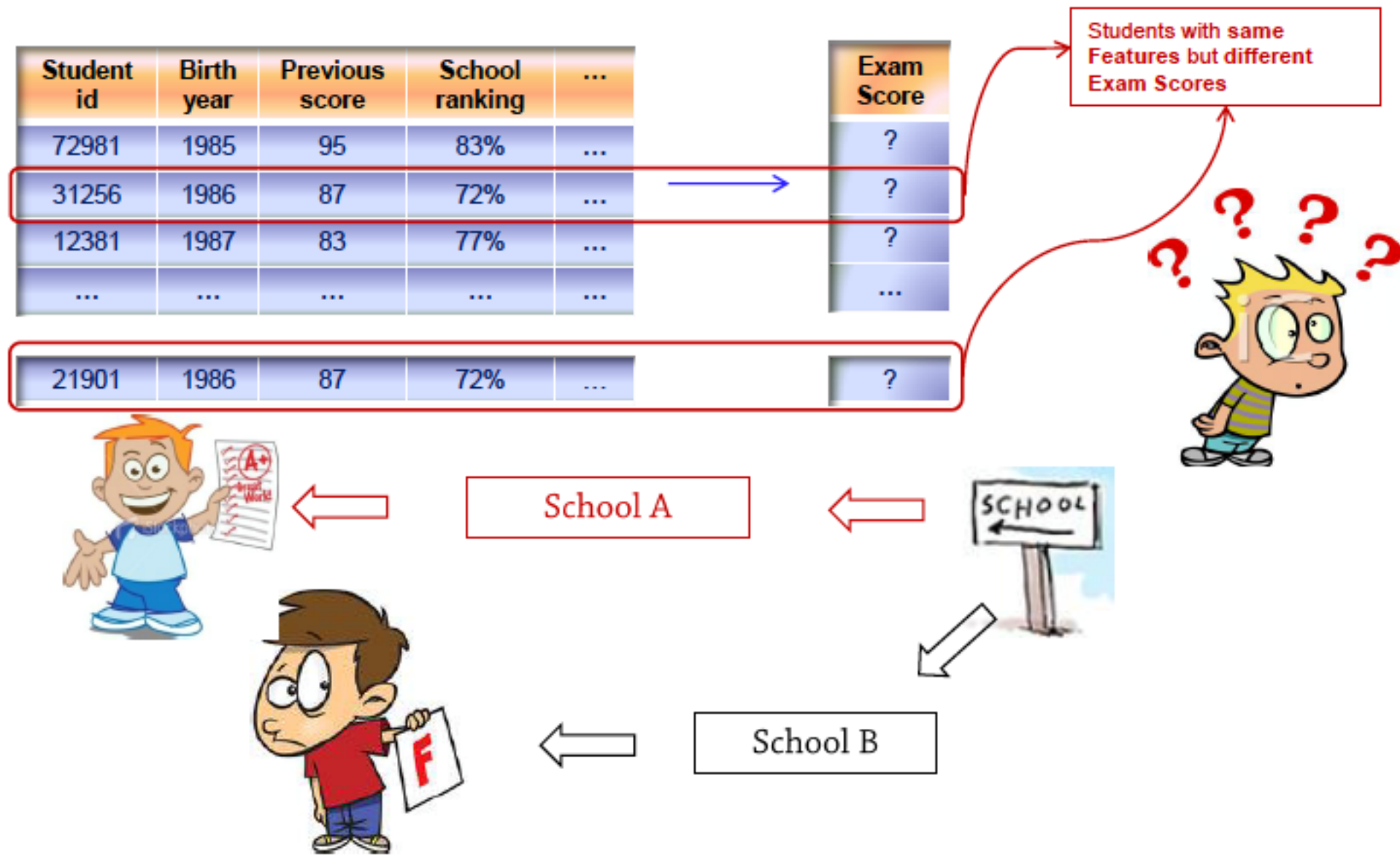


School 139 - Rosemead High School



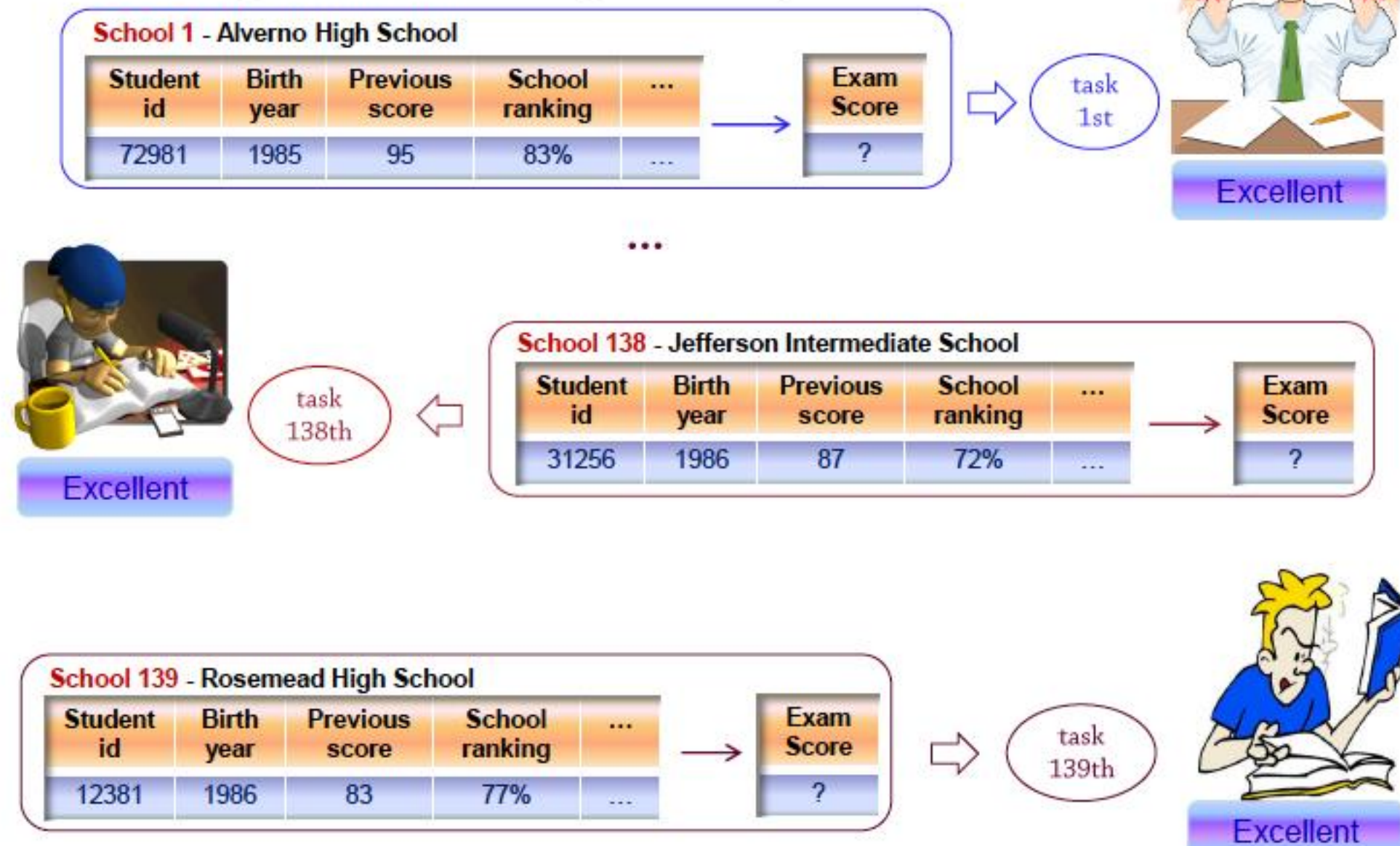
Learn Multiple Tasks

- Learning from the pool of all tasks



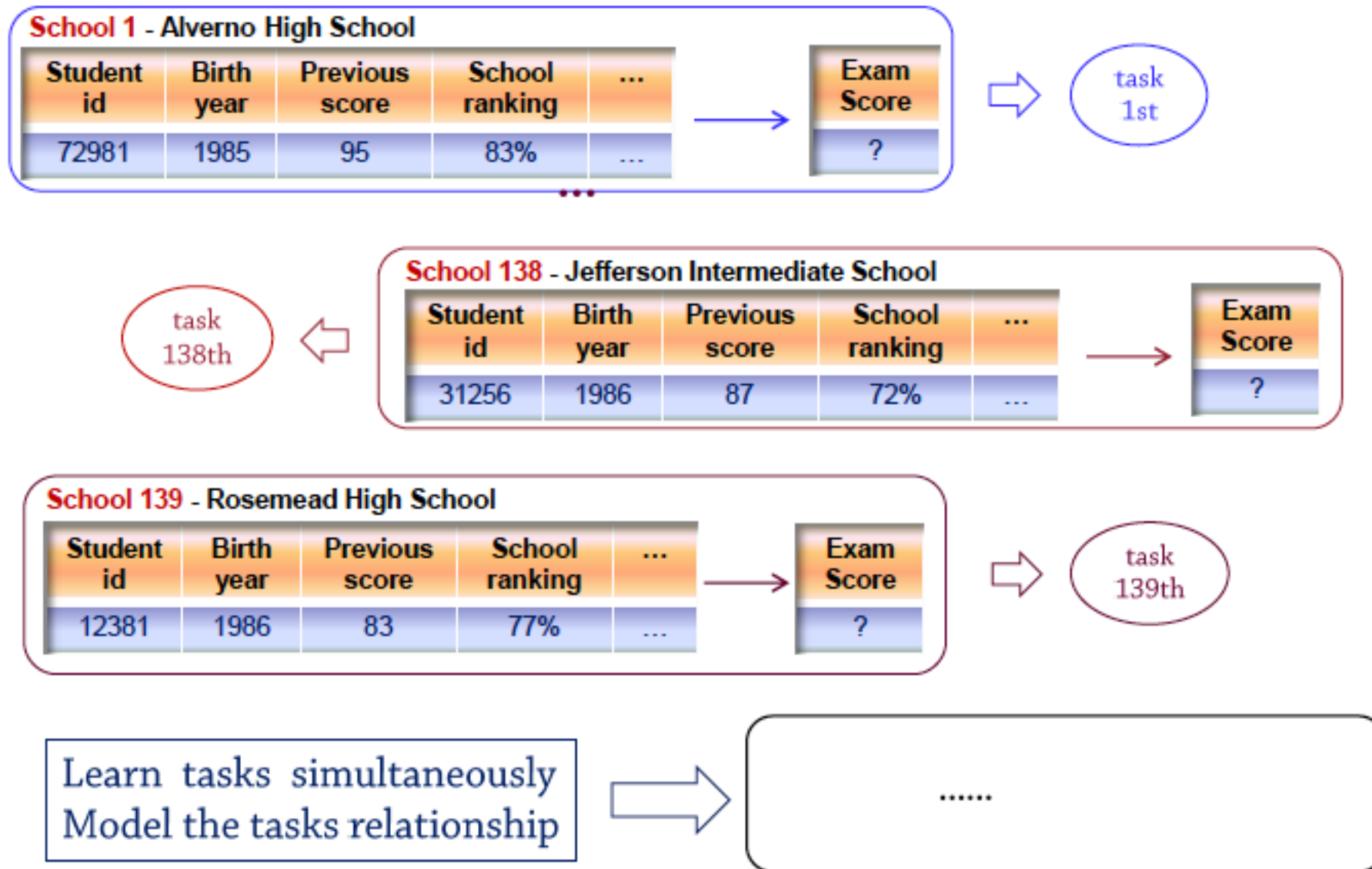
Learning Multiple Tasks

- Learning each task independently



Learning Multiple Tasks

- Learning multiple tasks simultaneously



MultiTask Learning

- The preference prediction of each user can be modeled using ordinal regression
- Some users have similar tastes and their predictions may also have similarities

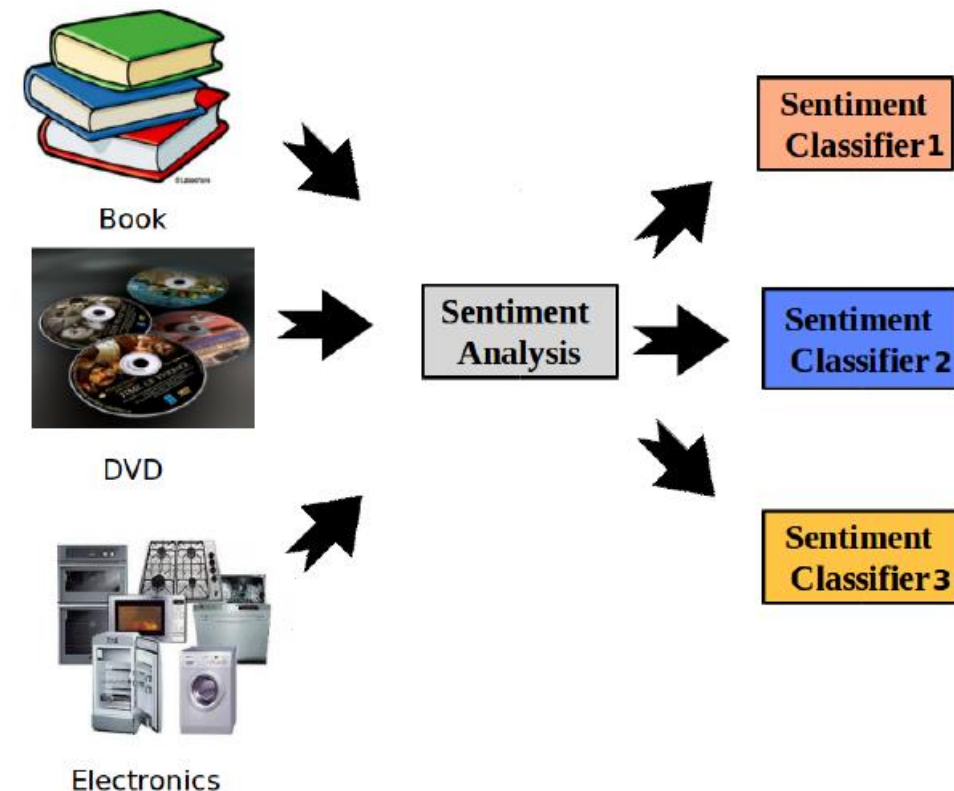
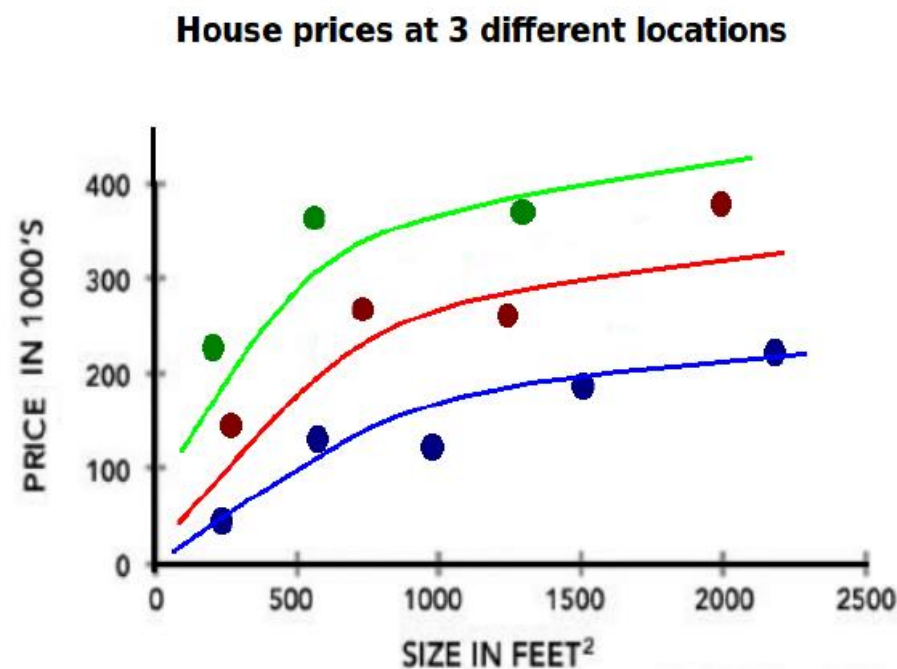


MultiTask Learning

Multi-task Learning (MTL)

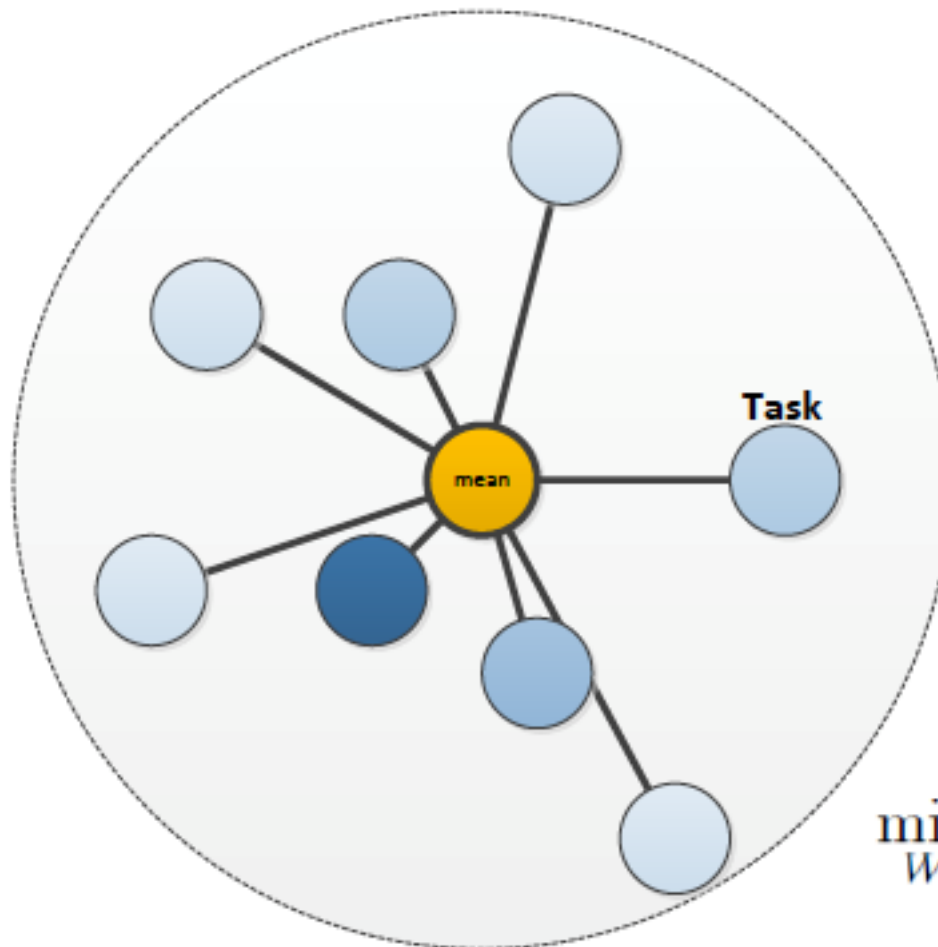
- Several **related learning** problems.
- Each learning problem is associated with **limited data**
- Models each problem as a task and learns all the tasks simultaneously.

Problem T tasks, $\mathbf{D}^t = (\mathbf{X}^t, \mathbf{y}^t) = \{\mathbf{x}_i^t, y_i^t\}_{i=1}^{N^t} \forall t = 1, \dots, T$ $y_i^t \in \mathcal{Y}$
Learn $f^t : \mathcal{X} \rightarrow \mathcal{Y}$ for each task t .



MultiTask Learning - Regularization Based

- Assume all tasks are related in that the models of all tasks come from a particular distribution (Evgeniou & Pontil, KDD 04)



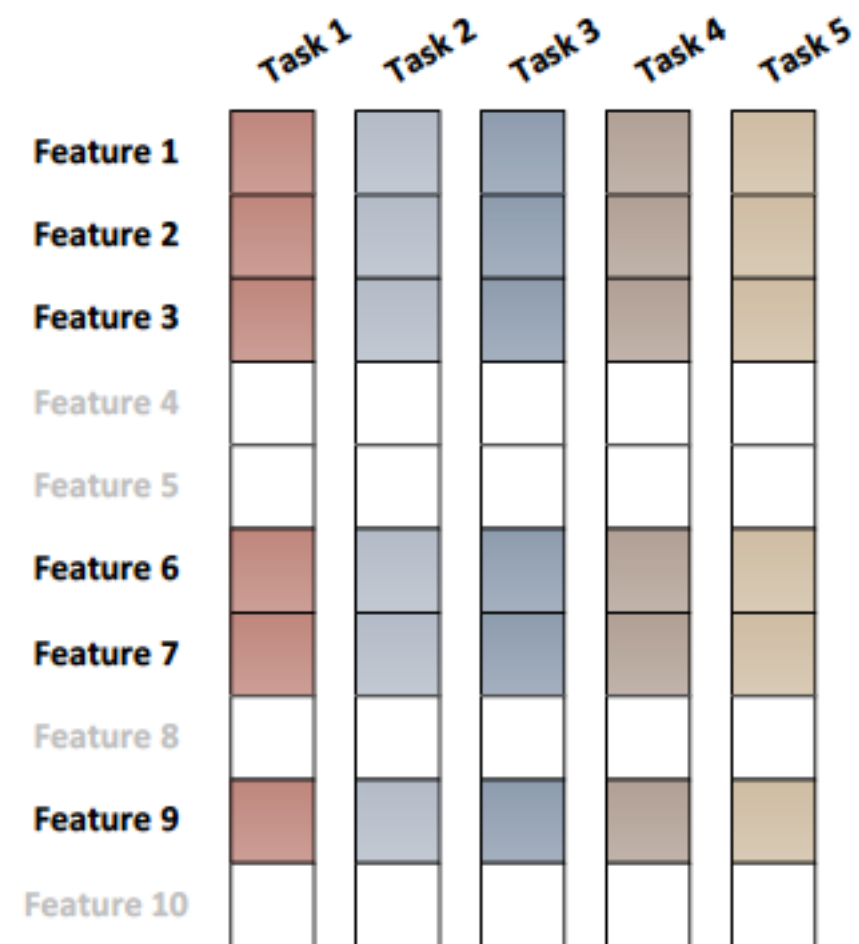
Regularization

penalizes the deviation of each task from the mean

$$\min_W \text{Loss}(W) + \lambda \sum_{t=1}^T \|W_t - \frac{1}{T} \sum_{s=1}^T W_s\|$$

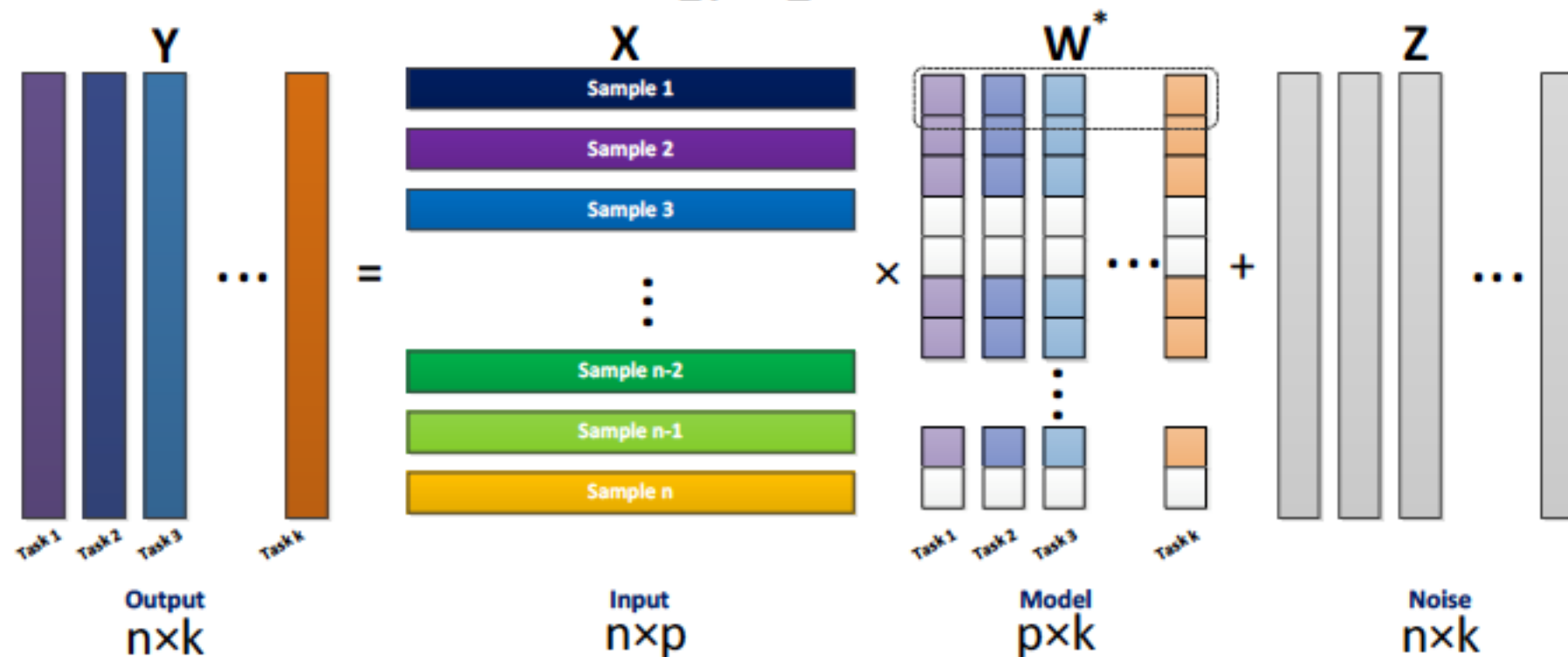
MultiTask Learning - Joint Feature Selection

- One way to capture the task relatedness from multiple related tasks is to constrain all models to share a common set of features.
- For example, in school data, the scores from different schools may be determined by a similar set of features.



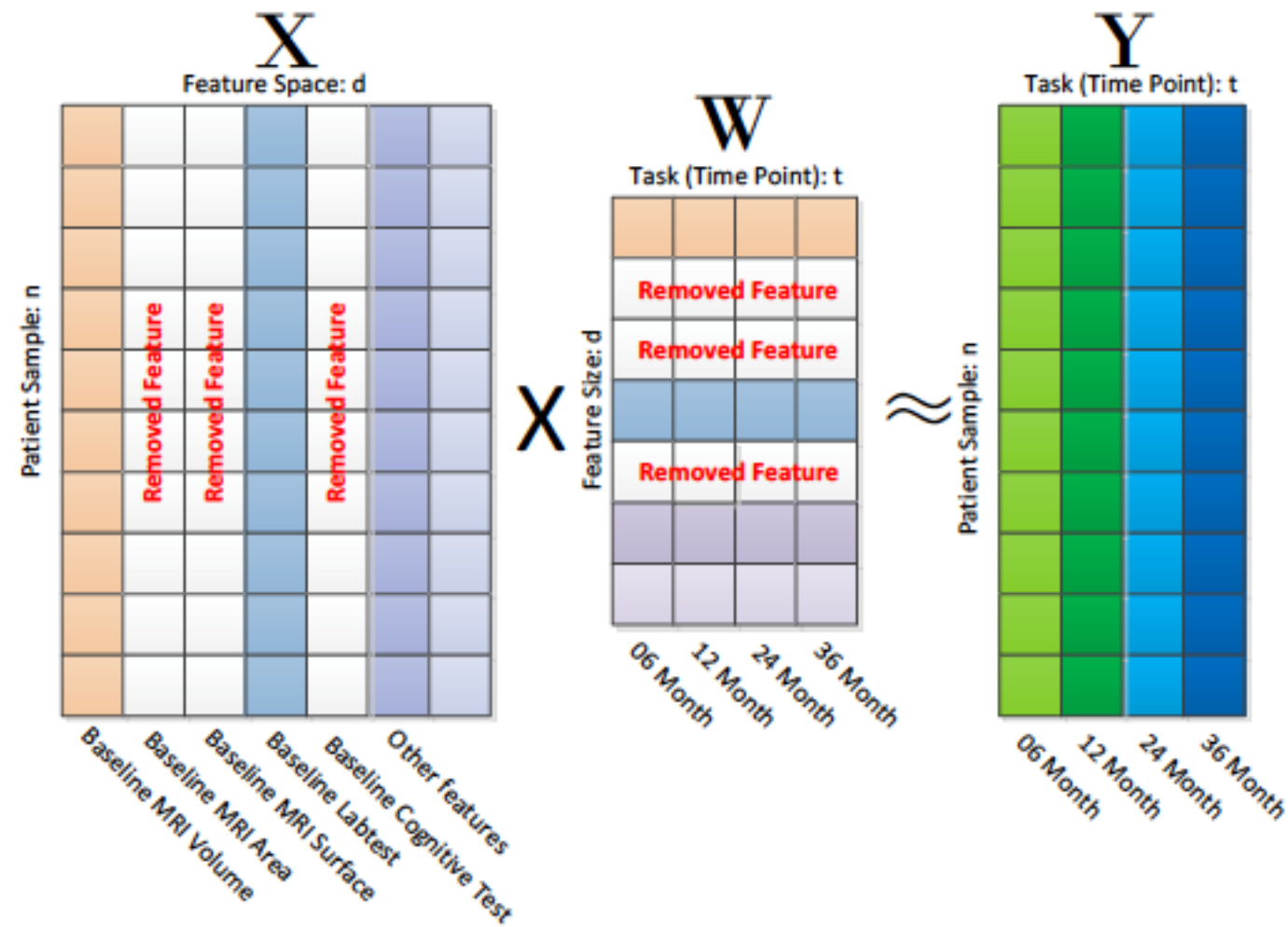
MultiTask Learning - Joint Feature Selection

Using group sparsity: ℓ_1/ℓ_2 -norm regularization



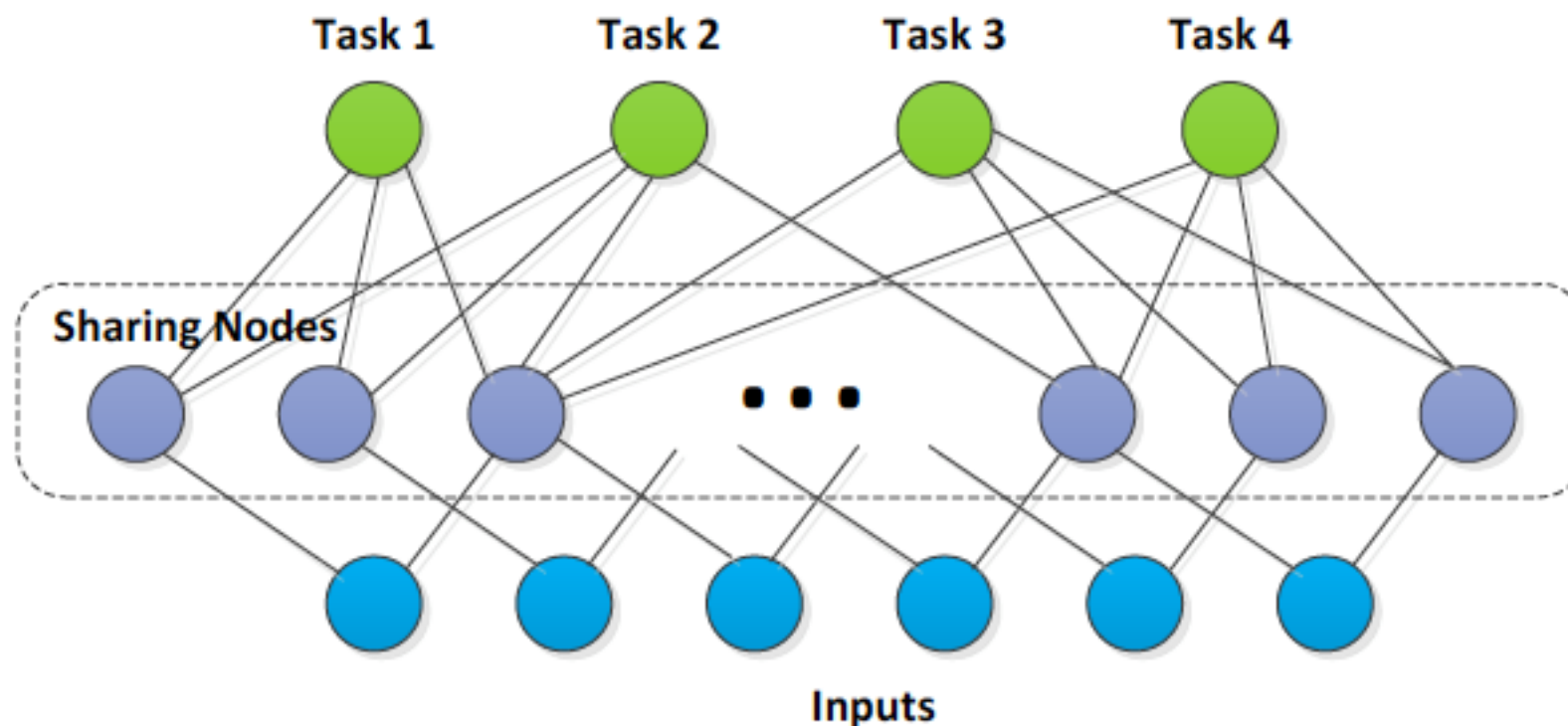
$$\min_W \frac{1}{2} \|XW - Y\|_F^2 + \lambda \sum_{i=1}^p \|\mathbf{w}_i\|_2$$

MultiTask Learning - Joint Feature Selection

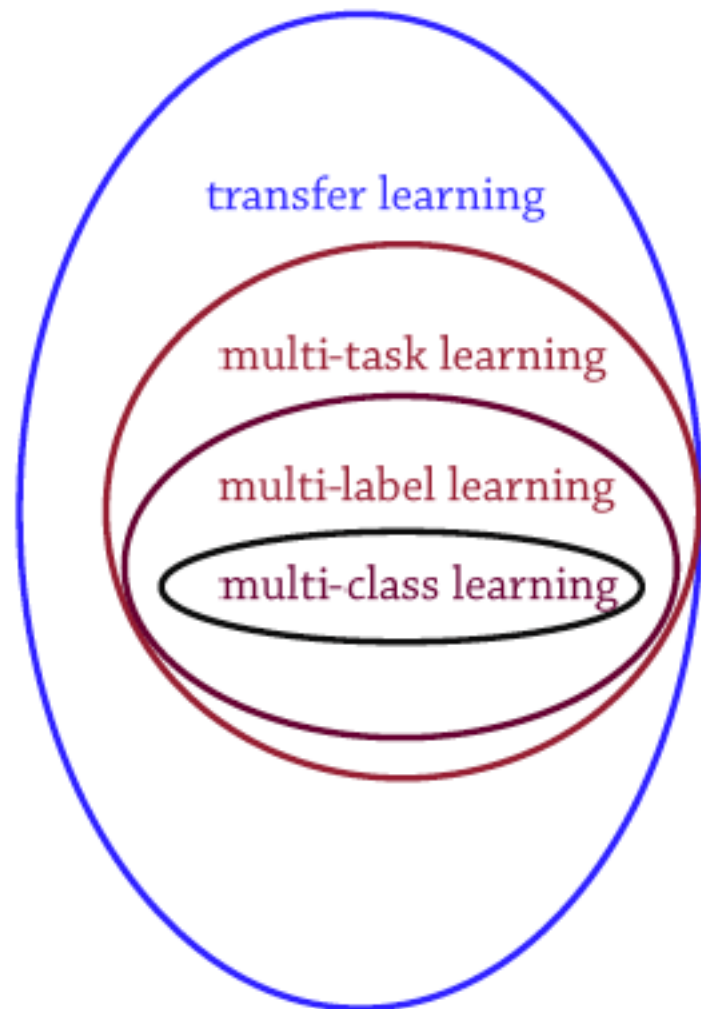


MultiTask Learning in Neural Networks

- Sharing the Hidden Nodes
 - Neural network has been well studied for learning multiple related tasks for improved generalization performance.
 - A set of hidden units are shared among multiple tasks for improved generalization (Caruana ML 97).



Learning Methods



- Transfer Learning
 - Define source & target domains
 - Learn on the source domain
 - Generalize on the target domain
- Multi-task Learning
 - Model the task relatedness
 - Learn all tasks simultaneously
 - Tasks may have different data/features
- Multi-label Learning
 - Model the label relatedness
 - Learn all labels simultaneously
 - Labels share the same data/features
- Multi-class Learning
 - Learn the classes independently
 - All classes are exclusive

MALSAR : Multi-task learning Software