

2.(b)

It can be seen from the truth table that A_3 & D_0 are identical,

$$\therefore \boxed{D_0 = A_3}$$

For D_1 ,

For $A_0 A_1 A_2 = 000$, we have the following expression

$$f_{000}(A_3, A_4, A_5, A_6) = \sum m(3, 7) + d(2, 4, 5, 6, 8, 9, 10, 11, 12, 13, 14)$$

(Note: All the combination not mentioned in the truth table can be considered as 'don't care'.

$A_3 A_4$	$A_5 A_6$			
	00	01	11	10
00	0 ₀	0 ₁	1 ₃	X ₂
01	X ₄	X ₅	1 ₇	X ₆
11	X ₁₂	X ₁₃	0 ₁₅	X ₁₄
10	X ₈	X ₉	X ₁₁	X ₁₀

$$f_{000} = \bar{A}_3 A_5$$

For $A_0 A_1 A_2 = 001$,

$$f_{001}(A_3, A_4, A_5, A_6) = d(2, 4, 5, 6, 8, 9, 10, 11, 12, 14, 13, 7, 0)$$

$$f_{001} = 0$$

~~For $A_0 A_1 A_2 = 011$~~

$$f_{011} = \sum m(15) + d(0,1,2,3,4,5,7,8,9,10,11,12,13,14)$$

$A_3 A_2$	$A_1 A_0$			
	00	01	11	10
00	X	X	X	X
01	X	X	X	X
11	X	X	1	X
10	X	X	X	X

$$f_{011} = 1$$

$$111, f_{111} = 1$$

$$\therefore D_1 = \bar{A}_0 \bar{A}_1 \bar{A}_2 (\bar{A}_3 A_4) + \bar{A}_0 \bar{A}_1 A_2 (0) + \bar{A}_0 A_1 A_2 (1) + A_0 A_1 A_2 (1)$$

$$D_1 = \bar{A}_0 \bar{A}_1 \bar{A}_2 \bar{A}_3 A_4 + \bar{A}_0 \bar{A}_1 A_2 + A_0 A_1 A_2$$

For D_2 ,

$$f_{000} = \sum m(1,4) + d(2,3,5,6,8,9,10,11,12,13,14)$$

$A_3 A_2$	$A_1 A_0$			
	00	01	11	10
00	0	1	0	X
01	X	X	1	X
11	X	X	0	X
10	X	X	X	X

$$f_{000} = \bar{A}_3 A_4 + \bar{A}_2 A_4$$

$$f_{001} = 1$$

$$f_{011} = 0$$

$$f_{111} = 1$$

$$\therefore D_2 = \bar{A}_0 \bar{A}_1 \bar{A}_2 (\bar{A}_3 A_4 + \bar{A}_2 A_4) + \bar{A}_0 \bar{A}_1 A_2$$