

# Topic 9: Building Robot Behaviours

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## 9.1 Introduction

### **Behaviour-based Robotics:**

- ☐ The world is fundamentally unknown and dynamically changing.
- ☐ It is wasting time to over plan a sequence of actions
- ☐ Key idea: to develop a library of useful behaviours (=controllers).
- ☐ To switch among controllers or behaviours in response to changes in environments

### **Behaviour definition:**

Robot behaviour is a control action based on a stimulus from a dynamic and unknown environment.

## 9.1 Introduction

### Questions:

- What are behaviours for a robot?
- Where do robot behaviours come from?
- How are these behaviours effectively co-ordinated?
- How are behaviours grounded to sensors and actuators?

### A navigation example:

Consider a robot going to the kitchen. It may involve:

- finding the destination from its current position
- walking towards the destination without bumping into anything
- observing and giving way to someone who is on the way.
- coping with changes on the way & doing whatever is necessary
- reaching the destination timely and successfully

## 9.1 Introduction



## 9.2 Behaviour Expression

**To implement** the navigation task described above, we have to build a robot which has particular behaviours needed.

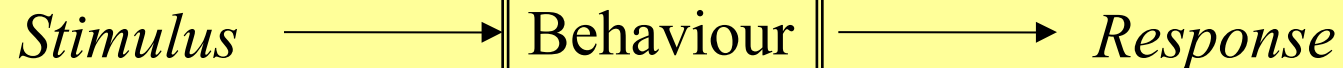
### **Expression of robot behaviours:**

Several methods are available for expressing robotic behaviours, including

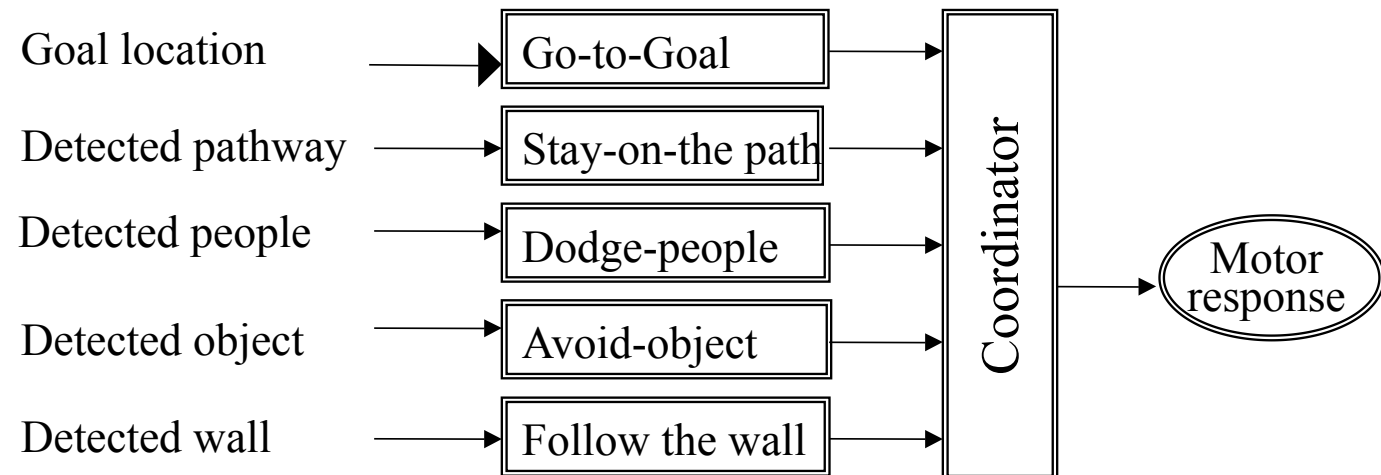
- *Stimulus-response (SR) diagrams:*
  - used for graphic representations of specific behavioural configurations
- *Functional notation:*
  - used for clarity in design of the systems
- *Finite state acceptor (FSA) diagrams:*
  - used for temporal sequencing of robot behaviours
- *Formal method:*
  - used as a common language for expressing robot behaviours

## 9.2.1 Stimulus-response (SR) diagrams

- SR is the most intuitive and the less formal method of expression.



For example:



- Motor response is corresponding to the behaviour with the highest priority.
- The coordinator is to coordinate different behaviours according to their priority.

## 9.2.2 Function notation

It is a mathematical method to express robot behaviours. For example:

$b(s) = r$  which means that behaviour  $b$  at a given stimulus  $s$  yields a response  $r$ .

The kitchen navigation task can be expressed:

```
Coordinate-behaviours[  
    go-to-kitchen(detect-kitchen-location),  
    avoid-objects(detect-objects),  
    dodge-people(detect-people),  
    stay-on-path(detect-path),  
    follow-the-wall(detect-wall)  
] = motor-response
```

**Coordinated functions** permits a recursive formulation of robot behaviours.  
It is easy to write in LISP, C/C++.

```
coordinate-behaviours[  
    coordinate-behaviours(behavioural-set-1)  
    .....  
    coordinate-behaviours(behavioural-set-N)  
]
```

## 9.2.3 Finite state acceptor (FSA) diagrams:

An FSA,  $M$ , is specified by:

$$M = (Q, \delta, q_0, F)$$

where:

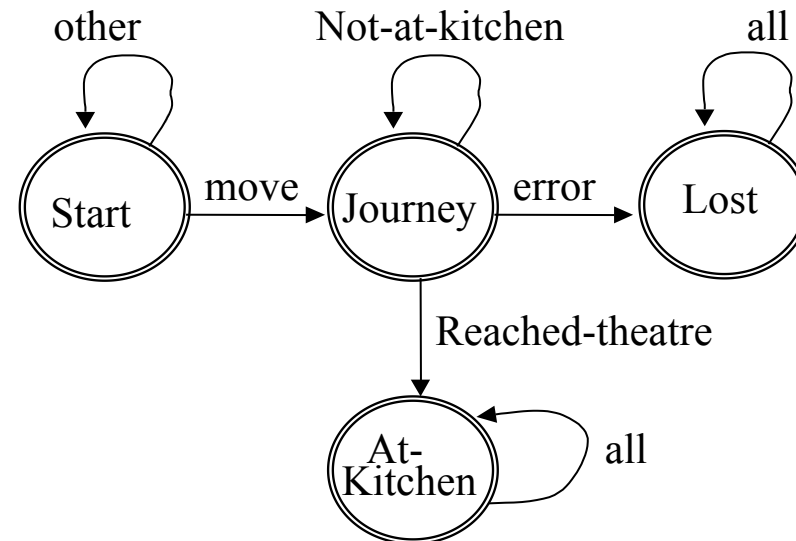
$Q$  -- represents the set of allowable behavioural states.

$\delta$  -- is a transition function mapping the input & the current state to another, or even the same, state.

$q_0$  -- denotes the starting behavioural configuration.

$F$  -- represents a set of accepting states, indicating completion of the sensorimotor task.

FSA used for the kitchen navigation example:



$$M = \{\{start, journey, lost, at-kitchen\}, \delta, start, \{lost, at-kitchen\}\}$$



## 9.2.4 Formal Methods

Two typical formal methods:

*The robot schema (RS) model*

-- developed by Lyons and Arbib (1989)

*The situated automata model*

-- developed by Kaelbling and Rosenschein (1991)

- They can be used to verify designer's intentions.
- They can facilitate the automatic generation of robotic control systems.
- They provide a complete common language for expressing robot behaviours.
- They provide a framework for conducting formal analysis of a specific program's properties, adequacy, and/or completeness.
- They provide support for high-level programming language design.

## 9.2.4 Formal Methods

### The Robot Schema (*RS*) model:

- *RS* model expresses a sensor-driven robot behaviour which encodes its response to any input messages.
- Schemas communicate with each other via pre-defined input-output ports using synchronous message passing techniques.
- Schemas are aggregated via a nesting mechanism termed an assemblage.

### The way to build:

- A process algebra is used to composite a network of schemas (behaviours).
- Process composition operators include methods for conditional, sequential, parallel and iterative structures.
- Preconditions are established for coordination operators to ensure a smooth control during execution.

## 9.2.4 Formal Methods

### The RS model for the kitchen navigation:

```
Service-Robot = (Start_up; (done? , Journey) : At-kitchen)
Journey = (move-to-kitchen, avoid-objects, dodge-people,
           stay-on-path, follow-the-wall)
```

where the sequential operator is denoted ‘;’(*semicolon*), the concurrency operator is denoted as ‘,’(*comma*), the conditional operator is ‘:’(*colon*).

### The main features:

- The Service-robot consists of a robot that, beginning from an initial start-up state, transitions to the Journey state, and remains there until it is at the kitchen indicated by a concurrent monitor process.
- The Journey state consists of the concurrent execution of the behaviours specified during travel from one location to the next.

## 9.2.4 Formal Methods

### The *Situated Automata (SA)* model:

- The model employs logical formalisms corresponding to a robot's goals & intentions.
- The use of logic such as operators **and**, **or**, **not** and **if**, enables reasoning over the system leading to create high-level goals.
- A LISP-based system and the Gapps language recently developed are basic tools.

SA model for  
the kitchen  
navigation  
task:

```
(defgoalr (ach in-theatre)
  (if (not start-up)
    (maint (and (maint move-to-kitchen)
                (maint avoid-objects)
                (maint dodge-people)
                (maint stay-on-path)
                (maint follow-the-wall))))
)
```

## 9.2.5 Behaviour Expression Video

Georgia Tech School of Electrical and Computer Engineering College of Engineering

### Lecture 2.1 – Driving Robots Around?

- What does it take to drive a robot from point A to point B?

Mhys Egerstedt, Control of Mobile Robots, Georgia Institute of Technology

## 9.3 Behaviour Encoding

**A behaviour** can be expressed as:

$$\beta: S \rightarrow R$$

where  $S$  -- the domain of all interpretable stimuli

$R$ -- the range of possible responses

$\beta$ -- mapping from the stimulus to possible responses

### Three general categories of $\beta$ :

- Null: The stimulus produces no motor response.
- Discrete: The stimulus produces a response from a set of prescribed choices (e.g. turn right, go-straight, stop, travel-at-speed-5).
- Continuous: The stimulus domain produces a motor response that is continuous over  $R$ 's range (e.g. increase/decrease speed).

## 9.3 Behaviour Encoding

### 9.3.1 Discrete encoding

$\beta$  is represented as a collection of *if-then* rules in the general form:

**IF** *antecedent* **Then** *consequent*

where the antecedent consists of a list of preconditions, and the consequent contains the motor responses (forward, backward, left...)

#### Examples:

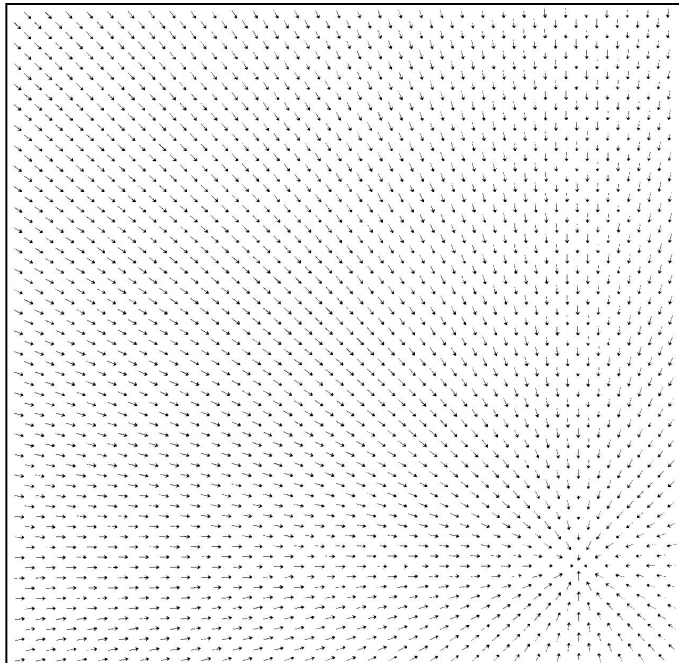
**If-then** behaviour rules used for a wheelchair (Connell100)

- Approach-- **If** an object is detected far away, **Then** go forward.
- Retreat -- **If** an object is nearby, **Then** move backward.
- Stymie -- **If** all the front IR sensors see an object, **Then** turn left.

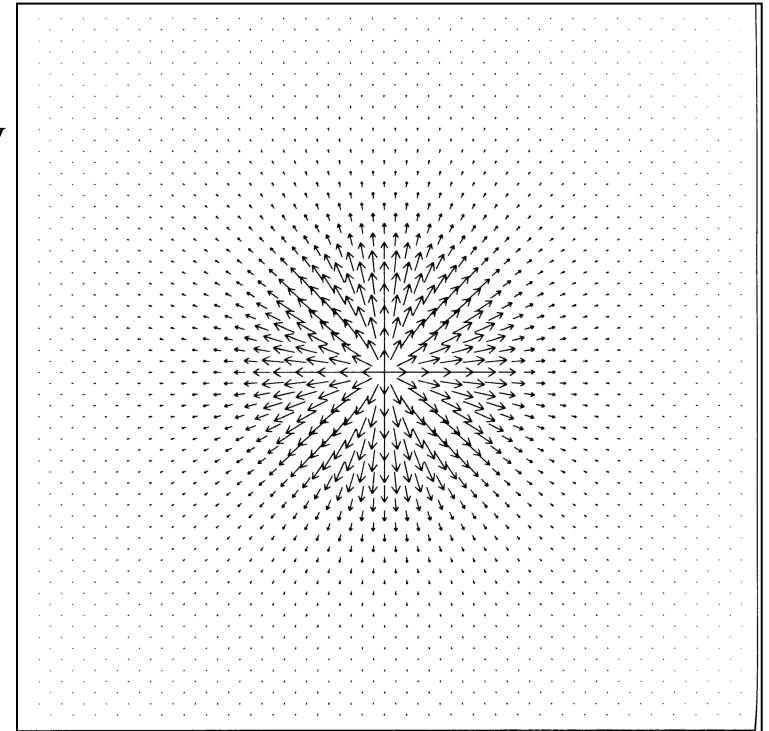
## 9.3 Behaviour Encoding

### 9.3.2 Continuous functional encoding

- ❑ This encoding technique is to transform the sensory input into a continuous behaviour response.
- ❑ **The potential fields method** (Khatib & Krough).



$$Force \propto \frac{1}{Distance^2}$$



(a) A repulsive force field for an obstacle

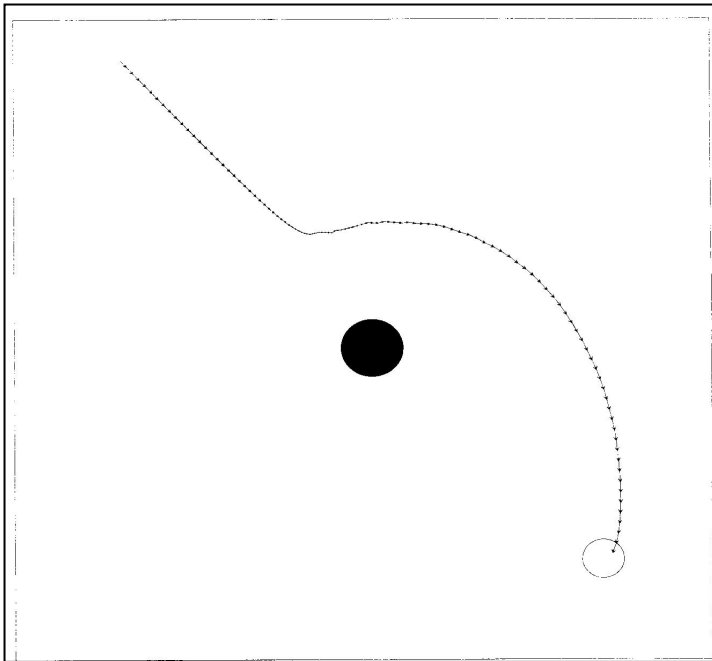
(b) A ballistic attraction field for a goal



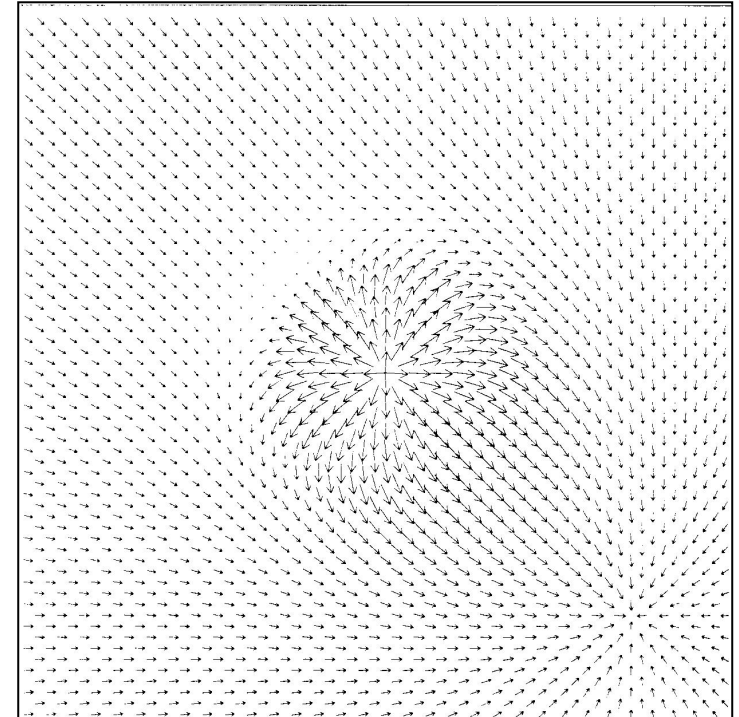
## 9.3 Behaviour Encoding

### Main features:

- ❑ Potential fields encode a continuous navigation space through the sensed world, and provide an infinite set of possible actions.
- ❑ There is a local minimum problem in potential fields, where a robot may get stuck or oscillation.

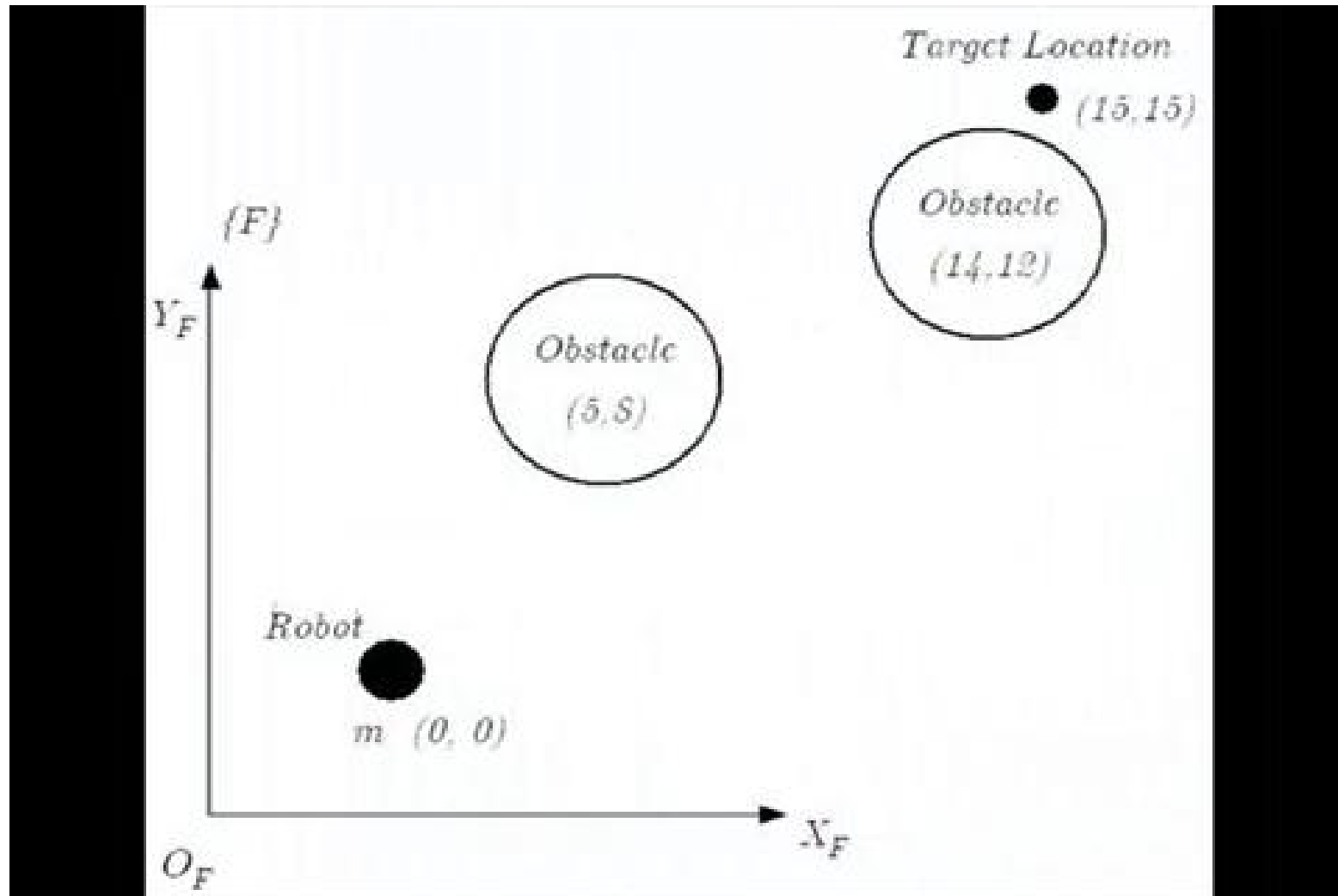


(d) An example trajectory for a robot moving within this simple world



(c) A linear superposition of these two fields

## 9.3 Behaviour Encoding



## 9.4 Behaviour Assembling

### 9.4.1 Behaviour Assembling

Since multiple behaviours may be concurrently active within a robotic system, we define additional notation as follows:

- **S** -- a vector of all stimuli  $\mathbf{s}_i$  relevant for each behaviour  $\beta_i$  detectable at time  $t$ .
- **B** -- a vector of all active behaviours  $\beta_i$  at a given time  $t$ .
- **R** -- a vector of all responses  $\mathbf{r}_i$  generated by the set of active behaviours.
- **G** -- a vector encoding the relative strength or gain  $g_i$  of each active behaviour  $\beta_i$ .

$$\mathbf{R} = \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \\ \vdots \\ \mathbf{r}_n \end{bmatrix}, \quad \mathbf{S} = \begin{bmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \\ \mathbf{s}_3 \\ \vdots \\ \mathbf{s}_n \end{bmatrix}, \quad \mathbf{B} = \begin{bmatrix} \beta_1 \\ \beta_2 \\ \beta_3 \\ \vdots \\ \beta_n \end{bmatrix}, \quad \mathbf{G} = \begin{bmatrix} g_1 \\ g_2 \\ g_3 \\ \vdots \\ g_n \end{bmatrix}$$

## 9.4 Behaviour Assembling

**Definition:** The overall robotic system response is defined as follows:

$$\rho = \mathbf{C}(\mathbf{G} * \mathbf{B}(\mathbf{S})) = \mathbf{C}(\mathbf{G} * \mathbf{R})$$

where  $\mathbf{C}$  is a new behaviour coordination function.

**Example:** the kitchen navigation

Given the robot's current perceptions at time  $t$ , we have

$$\mathbf{S} = \begin{bmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \\ \mathbf{s}_3 \\ \mathbf{s}_4 \\ \mathbf{s}_5 \end{bmatrix} = \begin{bmatrix} (\textit{kitchen} - \textit{location}, 1.0) \\ (\textit{detected} - \textit{object}, 0.2) \\ (\textit{detected} - \textit{people}, 0.8) \\ (\textit{detected} - \textit{path}, 1.0) \\ (\textit{detected} - \textit{wall}, 0.0) \end{bmatrix}$$

## 9.4 Behaviour Assembling

The behaviour responses are represented as:

$$\mathbf{B}(\mathbf{S}) = \begin{bmatrix} \beta_{go-to-kitchen}(\mathbf{s}_1) \\ \beta_{avoid-object}(\mathbf{s}_2) \\ \beta_{dodge-student}(\mathbf{s}_3) \\ \beta_{stay-on-path}(\mathbf{s}_4) \\ \beta_{follow-the-wall}(\mathbf{s}_5) \end{bmatrix} \Rightarrow \begin{bmatrix} \mathbf{r}_{go-to-kitchen} \\ \mathbf{r}_{avoid-object} \\ \mathbf{r}_{dodge-people} \\ \mathbf{r}_{stay-on-path} \\ \mathbf{r}_{follow-the-wall} \end{bmatrix}$$

$= \mathbf{R}$

We arbitrarily choose component vector magnitudes in  $\mathbf{R}$  as follows

$$\mathbf{R}_{magnitude} = [1.0 \quad 0 \quad 0.8 \quad 1.0 \quad 0]^T$$

where *avoid-object* and *defer-to-elder* are below threshold and generate no response.  
*go-to-theatre* and *stay-right/left* are at maximum strength.

## 9.4 Behaviour Assembling

Then we choose the gain vector as follows:

$$\mathbf{G} = \begin{bmatrix} g_{go-to-kitchen} \\ g_{avoid-object} \\ g_{dodge-people} \\ g_{stay-on-path} \\ g_{follow-the-wall} \end{bmatrix} = \begin{bmatrix} 0.8 \\ 1.2 \\ 1.5 \\ 0.4 \\ 0.8 \end{bmatrix}$$

Finally, we have

$$\rho = \mathbf{C}(\mathbf{G} * \mathbf{R}) = \mathbf{C} \left( \begin{bmatrix} g_1 * \mathbf{r}_1 \\ g_2 * \mathbf{r}_2 \\ g_3 * \mathbf{r}_3 \\ g_4 * \mathbf{r}_4 \\ g_5 * \mathbf{r}_5 \end{bmatrix} \right) \Rightarrow \mathbf{R}'_{magnitude} = \begin{bmatrix} 0.8 \\ 0 \\ 1.2 \\ 0.4 \\ 0 \end{bmatrix}$$

**It should be noted** that if using winner-take-all coordination strategy, the *dodge-people* behaviour will be chosen as it has a greatest magnitude.

## 9.4 Behaviour Assembling

### 9.4.2 Behaviour coordination

The coordination function **C** has two predominant classes:  
competitive & cooperative

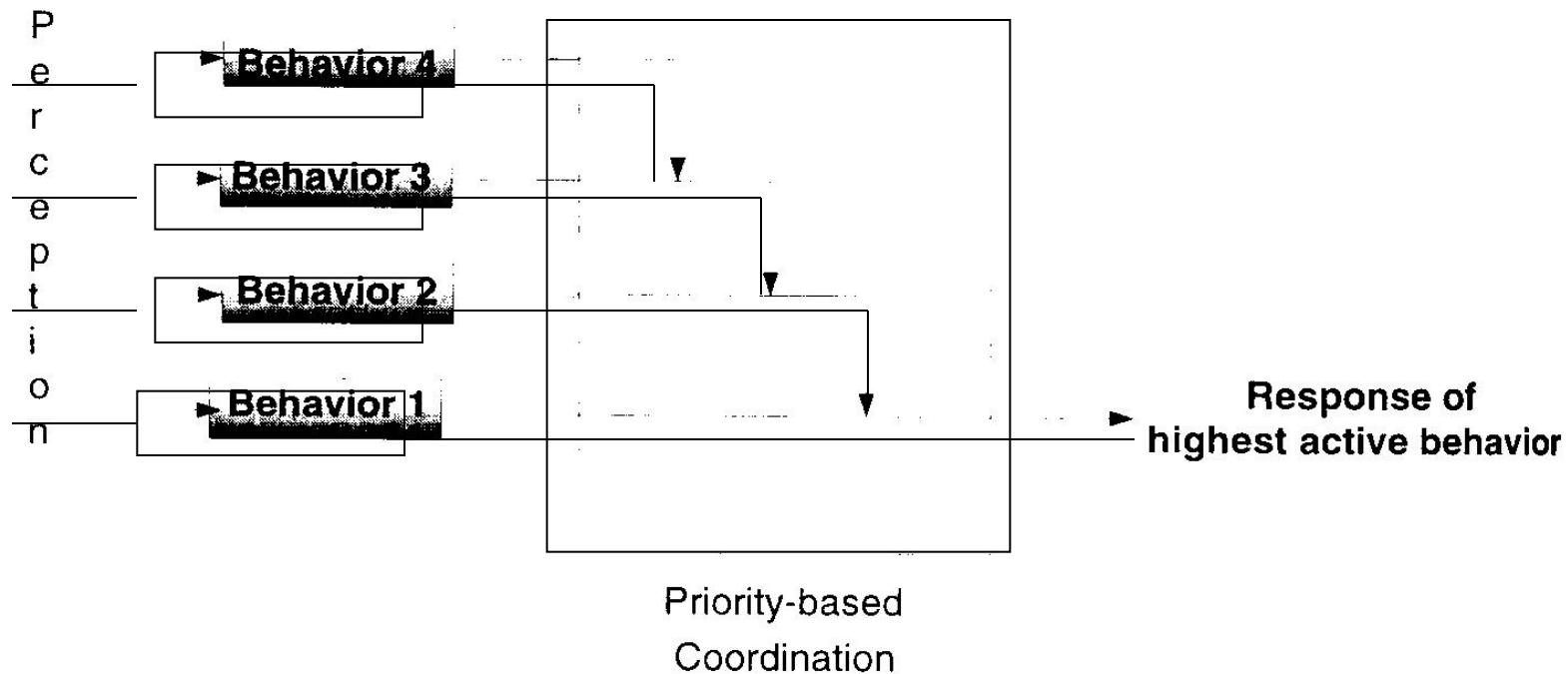
#### Competitive methods

- Competitive methods provide a means of coordinating behaviours response for conflict situation when two or more behaviours are active.
- Coordination is done through a *winner-take-all* strategy.
- There are mainly three popular competitive methods as follows:
  - Priority-based coordination
  - Action-selection coordination
  - Voting-based coordination

## 9.4 Behaviour Assembling

### Priority-based coordination (*Brooks, 1986*)

- A coordination function serves as an arbiter in a fixed priority.
- Only a single behavioural response is allowed at any time.

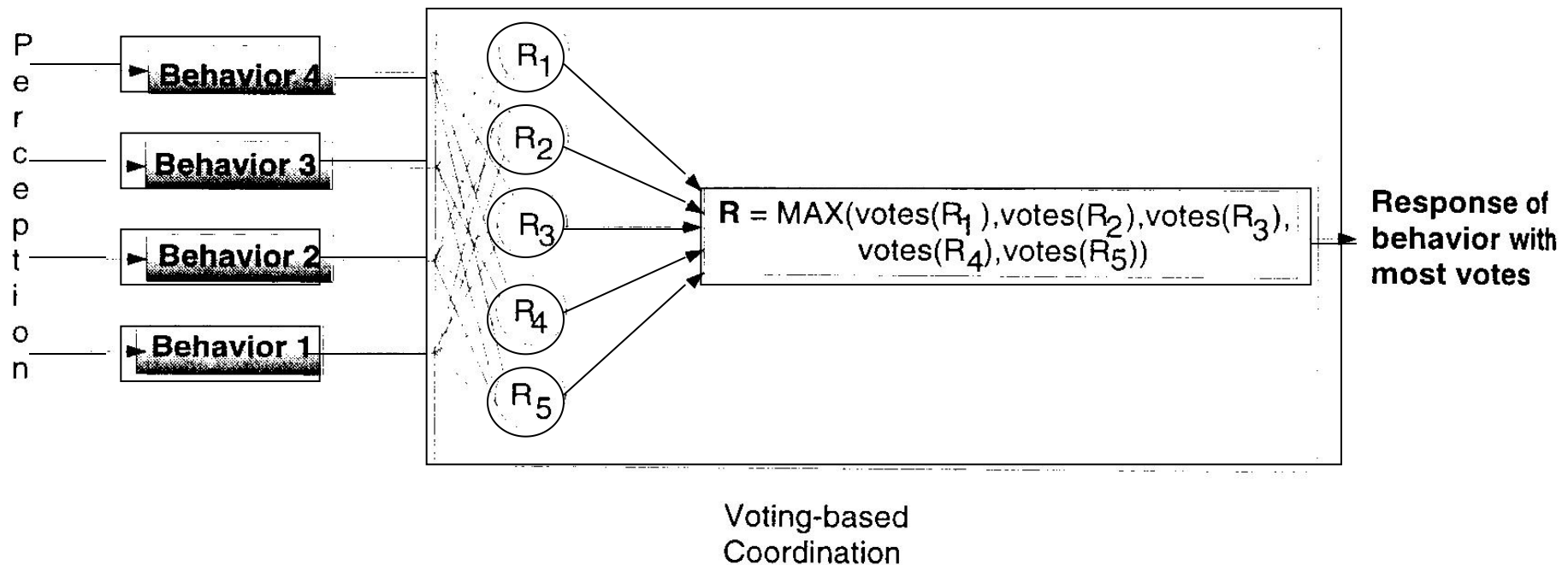




## 9.4 Behaviour Assembling

### Voting-based coordination (*Rosenblatt & Payton*)

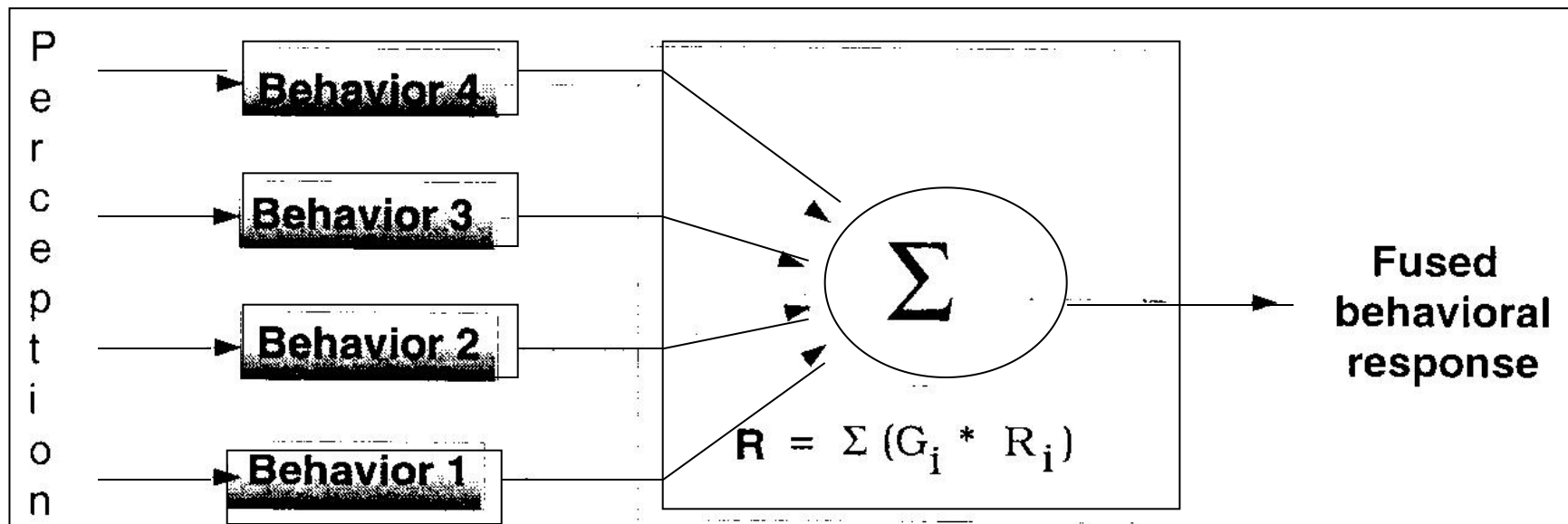
- A democratic competitive: voting for action
- The single response with the most votes is enacted.



## 9.4 Behaviour Assembling

### Cooperative methods

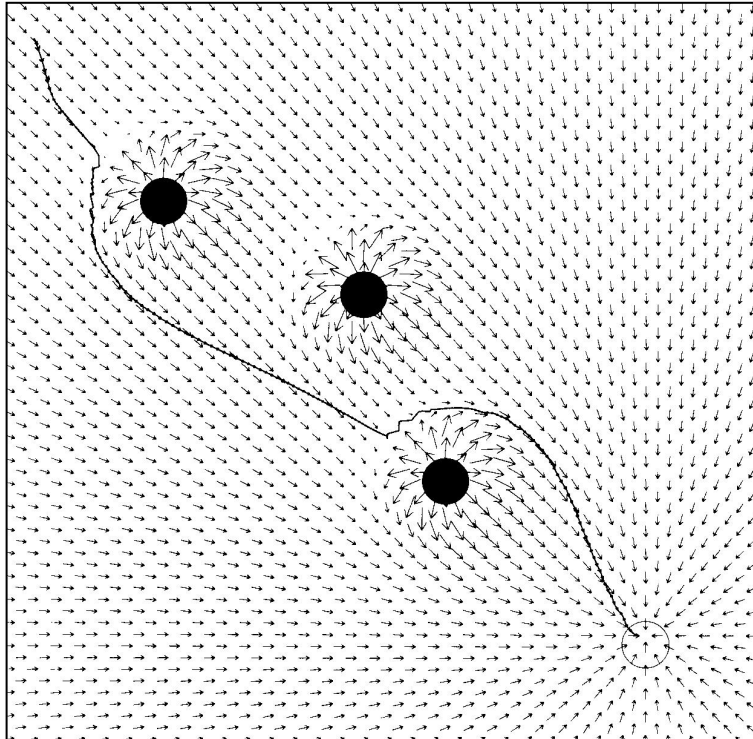
- Cooperative methods combines the outputs of multi behaviours.
- Vector addition & superpositioning are popular ways for combining.



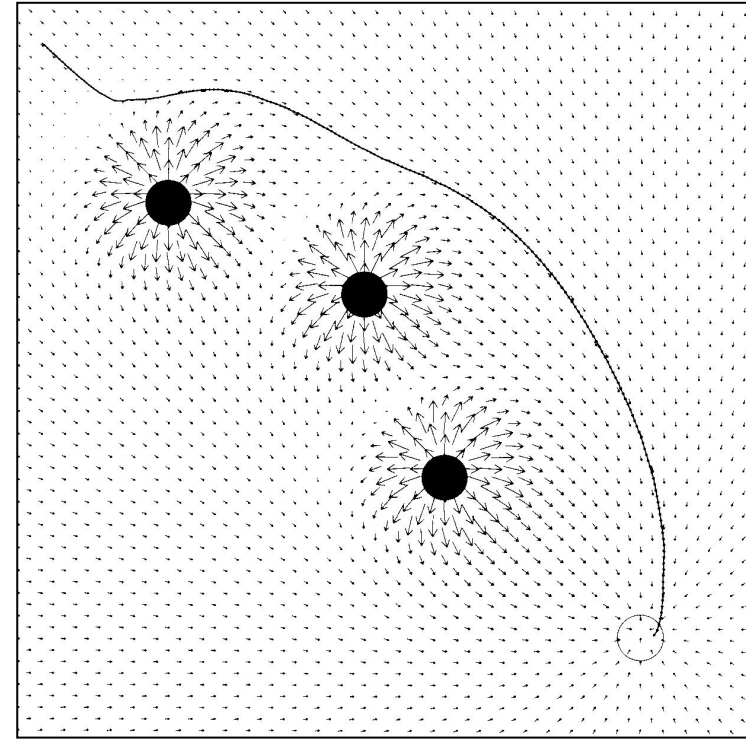
Behaviour fusion via vector summation

## 9.4 Behaviour Assembling

### Behaviour fusion

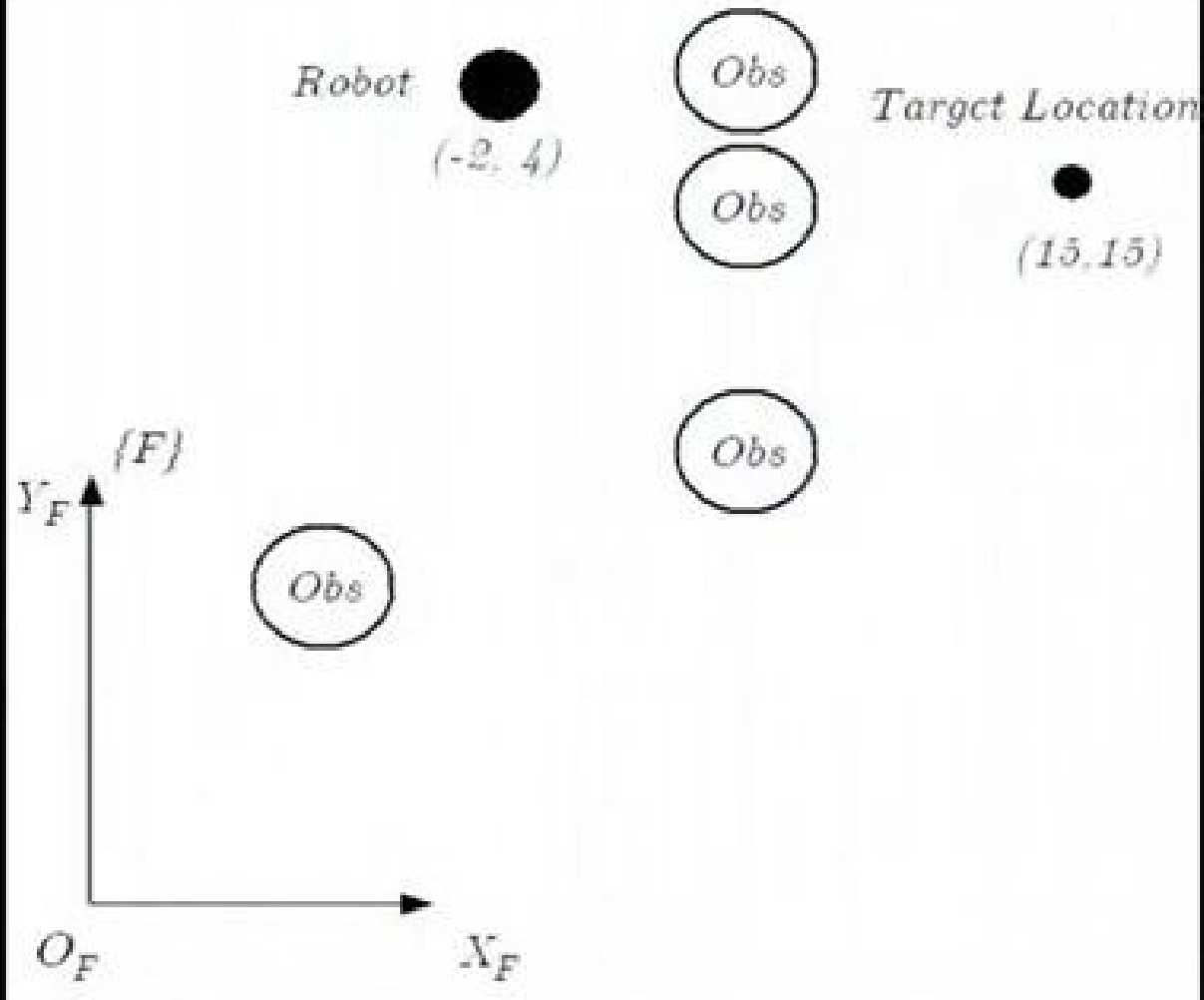


(a) goal attraction dominates



(b) obstacle avoidance dominates

## 9.4 Behaviour Assembling



## 9.5 Conclusions

- ❑ Robot behaviours generate a motor response from a given perceptual stimulus, and avoid the use of explicit representational knowledge.
- ❑ Reactive or behaviour-based systems are inherently modular in design based on biological models.

The four popular expressions of robot behaviours:

- ***SR diagrams*** intuitively convey the flow of the control within a reactive system.
- ***Function notation***: is a mathematical method to express robot behaviours
- ***FSA diagrams***: are well suited for representing behaviour assemblages in time-varying composition.
- ***Formal methods***: include RS models and SA models.

## 9.5 Conclusions

- Robot behaviours are encoded in two forms:
  - *discrete encoding*: rule-based methods are often used.
  - *continuous encoding*: the potential-field methods are often used.
- The two primary methods for behavioural coordination are competitive and cooperative. They can be combined if necessary.
  - *Competitive methods*: result in the selection of the output of a single behaviour, typically either by arbitration or action-selection.
  - *Cooperative methods*: often use super-positioning of forces or gradients generated from field-based methods, e.g. potential fields.

## 9.5 Conclusions

