## Junior Balkan MO 2003

Kusadasi, Turkey

- 1 Let n be a positive integer. A number A consists of 2n digits, each of which is 4; and a number B consists of n digits, each of which is 8. Prove that A + 2B + 4 is a perfect square.
- 2 Suppose there are n points in a plane no three of which are collinear with the property that if we label these points as  $A_1, A_2, \ldots, A_n$  in any way whatsoever, the broken line  $A_1 A_2 \ldots A_n$  does not intersect itself. Find the maximum value of n.

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- 3 Let D, E, F be the midpoints of the arcs BC, CA, AB on the circumcircle of a triangle ABC not containing the points A, B, C, respectively. Let the line DE meets BC and CA at G and GA and GA and GA and GA and GA are GA and GA and GA and GA are GA and GA and GA are GA are GA and GA are GA are GA and GA are GA and GA are GA are GA are GA and GA are GA are GA are GA and GA are GA are GA and GA are GA are GA are GA and GA are GA and GA are GA are
  - a) Find the angles of triangle DMN;
  - b) Prove that if P is the point of intersection of the lines AD and EF, then the circumcenter of triangle DMN lies on the circumcircle of triangle PMN.
- $\boxed{4}$  Let x, y, z > -1. Prove that

$$\frac{1+x^2}{1+y+z^2} + \frac{1+y^2}{1+z+x^2} + \frac{1+z^2}{1+x+y^2} \ge 2.$$

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