

## Calculating the Entropy for Decision Tree

Buy Computer

Buy Computer		
yes	no	sum
12	8	20

Age

	Buy computer	Buy computer	
	yes	no	sum
<30	2	6	8
31...40	6	0	6
>40	4	2	6

Income

	Buy computer	Buy computer	
	yes	no	sum
high	3	2	5
medium	5	3	8
low	4	3	7

Student

	Buy computer	Buy computer	
	yes	no	sum
yes	8	1	9
no	4	7	11

Credit rating

	Buy computer	Buy computer	
	yes	no	sum
Fair	7	3	10
Excellent	5	5	10

Calculated with ID3 method from [http://www.saedsayad.com/decision\\_tree.htm](http://www.saedsayad.com/decision_tree.htm)

Entropy Buy Computer

$$\begin{aligned}E(\text{BuyComputer}) &= E(12,8) \\ &= 0.971\end{aligned}$$

**Entropy(BuyComputer, Age)**

$$\begin{aligned}E(\text{BuyComputer, Age}) &= P(<30)*E(2,6) + P(31..40)*E(6,0) + P(>40)*E(4,2) \\ &= (8/20)*0.811 + (6/20)*0 + (6/20)*0.918 \\ &= 0.6\end{aligned}$$

**Entropy(BuyComputer, Income)**

$$\begin{aligned}E(\text{BuyComputer, Income}) &= P(\text{high})*E(3,2) + P(\text{medium})*E(5,3) + P(\text{low})*E(4,3) \\ &= (5/20)*E(3,2) + (8/20)*E(5,3) + (7/20)*E(4,3) \\ &= 0.25*0.971 + 0.4*0.954 + 0.35*0.9855 \\ &= 0.96\end{aligned}$$

**Entropy(BuyComputer, Student)**

$$\begin{aligned}E(\text{BuyComputer, Student}) &= P(\text{IsStudent})*E(8,1) + P(\text{noStudent})*E(4,7) \\ &= (9/20)*E(8,1) + (11/20)*E(4,7) \\ &= 0.45*0.5044 + 0.55*0.9457 \\ &= 0.747\end{aligned}$$

**Entropy(BuyComputer, CreditRating)**

$$\begin{aligned}E(\text{BuyComputer, CreditRating}) &= P(\text{Fair})*E(7,3) + P(\text{Excellent})*E(5,5) \\ &= (10/20)*E(7,3) + 10/20*E(5,5) \\ &= 0.5*0.881 + 0.5*1 \\ &= 0.941\end{aligned}$$

