

SYLHET CADET COLLEGE

TEST EXAMINATION - 2024

CLASS: XII

STATISTICS (CREATIVE)

SECOND PAPER

TIME – 2 hours & 35 minutes

FULL MARKS – 50

Set	A
-----	---

Subject Code:	1	3	0
---------------	---	---	---

[N.B. – The figures of the right margin indicate full marks. Read the stems carefully and answer the associated questions. Answer any **FIVE** questions taking at least two questions from each group]

Group–A

1. As part of an experiment, a neutral coin is tossed 5 times.

- |  |   |
|--|---|
| (a) What is a neutral coin?  | 1 |
| (b) If a coin is flung n times, show the no. of outcomes generated.  | 2 |
| (c) What is the probability of getting a) at least 3 heads, b) at most 3 heads?  | 3 |
| (d) Are these probabilities equal? a) Getting at least 2 heads & b) Getting at least 2 tails.<br>Also justify logically. | 4 |

2. A sorcerer draws 3 cards from a pack (i) with replacement and then (ii) without replacement. The cards were well-shuffled before drawing.

- |   |   |
|---|---|
| (a) What is an uncertain event?   | 1 |
| (b) Differentiate between classical and empirical approach of probability.      | 2 |
| (c) As per (i), what is the probability that the cards have different color?    | 3 |
| (d) As per (ii), what is the probability that the cards are aces of same color? | 4 |

3. A continuous random variable X follows the following probability density function (pdf).

$$f(x) = 6x(x - 1); 0 \leq x \leq 1$$

- |  |   |
|--|---|
| (a) Give an example of a continuous random variable. | 1 |
| (b) Examine whether the given function is a pdf.     | 2 |
| (c) If $P(X > a) = P(X < a)$ , find the value of a.  | 3 |
| (d) Should $P(0.5 \leq X \leq 1)$ be equal to 0.5?   | 4 |

4. A random variable is distributed as below:

$$P(X) = \frac{3-|4-x|}{k}; x = 2, 3, 4, 5, 6$$

- |   |   |
|---|---|
| (a) What is the Expectation equivalent to?  | 1 |
| (b) Find the value of k.                    | 2 |
| (c) Determine the value of the expectation. | 3 |
| (d) Find $V(2X - 1)$                        | 4 |

Group–B

5. A random variable is distributed as follows:

Value	0	1	2	3	4	5
Frequency	70	73	27	15	4	1

- |   |   |
|---|---|
| (a) What is the mean of Poisson distribution?   | 1 |
| (b) What is the relationship between mean and standard deviation of Poisson distribution? | 2 |
| (c) Find the mean and variance of the given distribution.                                 | 3 |
| (d) Compare the observed and expected frequencies, assuming a Poisson distribution.       | 4 |

6. The number of defective pens produced by a company follows a binomial distribution with expectation 1.5 and variance 1.125.

- |  |   |
|--|---|
| (a) What is the mean of binomial distribution  | 1 |
| (b) Can variance be greater than mean in binomial distribution?                                  | 2 |
| (c) Determine the probability function of the number of defective items produced by the company. | 3 |
| (d) What is the probability that the number of defective items is no less than 3?                | 4 |

7. The number of customers coming at a shop per minute follows a Poisson distribution, whose mean is 3.

- (a) What is a Poisson variate?1
- (b) Can the mean of Poisson distribution be negative?2
- (c) Find the probability that the number of customers coming is between 1 and 2.3
- (d) Analyze the statement:  $P(X=2) = P(X=3)$ .4

8. As part of an analysis, a researcher collected data on women and live births.

Age	15-19	20-24	25-29	30-34	35-39	40-44	45-49
No. of Women	540	760	530	495	450	505	430
No. of live births	109	198	86	90	65	76	60

- (a) What is the formula of death rate?1
- (b) Write down the uses of vital statistics.2
- (c) Find teh Age Specific Birth Rates (ASFR).3
- (d) Find the GFR and compare its concept and value with ASFRs.4