



# Filling in the blanks in morphological productivity: a word-completion task



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## Motivation

### Are humans systematically biased in judgments of language frequency?

-In a classic study, (Tversky & Kahneman, 1973, 1983), participants were asked to judge how many words in a hypothetical text of 2,000 English words would fit the pattern \_ \_ \_ \_ n \_ . The median guess was *higher* for \_ \_ \_ \_ i n g than for \_ \_ \_ \_ n \_ , despite this being a logical impossibility.

-Tversky and Kahneman interpret this result as a failure of rational judgment, and attribute it the greater *availability* of words ending in *-ing*.

-We believe this greater availability follows naturally from morphological productivity, and that people's overestimation for **productive** morphemes follows rationally from the ability of these morphemes to form new words.

-We test this hypothesis by extending Tversky and Kahneman's work using a variety of English derivational suffixes of varying levels of productivity. We derive productivity estimates for various suffixes and predict that more productive suffixes (e.g., -ness) are more likely to have their frequencies overestimated than lower productivity suffixes (e.g., -ity).

How many words fit this pattern?

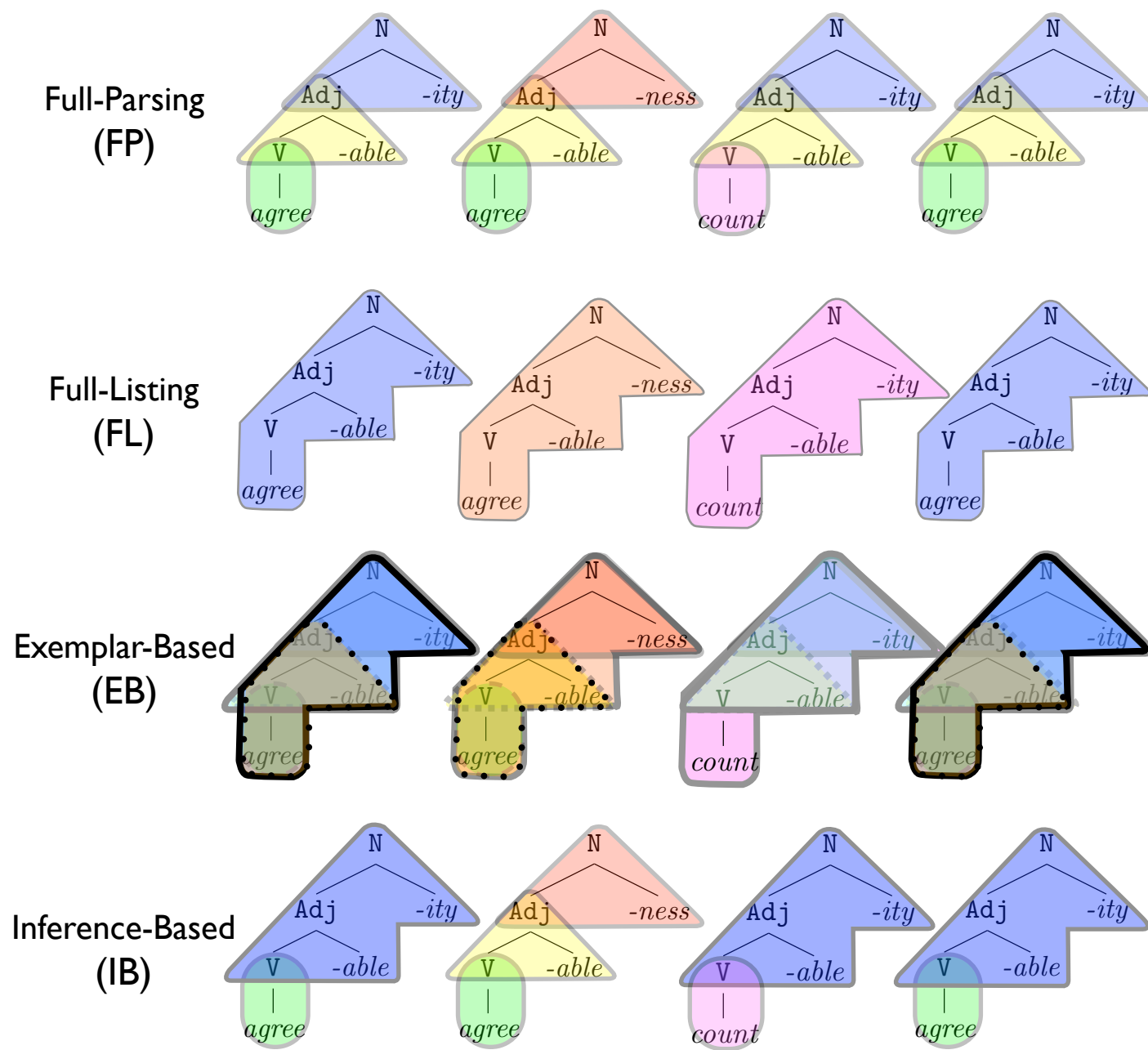
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## Morphological Productivity

-The ability to give rise to novel forms in language is known as linguistic *productivity* (Bauer 2001). This phenomenon is evident in derivational morphology.

	Suffix	examples
Productive	-ness	happiness, psycholinguistic-ness, coolness
Semi-productive	-ity	sparsity, scarcity, coolity*
Unproductive	-th	warmth, coolth*

-To compare the productivity of various affixes, we use two theoretical measures of productivity: First, quantities computed from the Bayesian model of productivity known as Fragment Grammars (FG; O'Donnell 2011) and, second, Baayen's P\*, A Good-Turing based estimator (Baayen 1994).



## Task

-Using Amazon's Mechanical Turk, we presented 206 participants with 105 word frames. Participants were asked to guess how many times a given pattern would occur in a 100,000 word novel. The 105 word frames presented to participants fell into one of four categories: (i) full-suffix frames like \_ \_ \_ \_ n e s s , (ii) partial-suffix frames like \_ \_ \_ \_ n \_ s \_ , (iii) frames based on mono-morphemic words like r \_ \_ d (road, reed, etc.), and (iv) impossible frames like z s q \_ \_ \_ .

-We ultimately analyzed 40 suffixes of 3 or more letters drawn from the corpus of O'Donnell (2011). For suffix-derived frames, each participant saw at most one instance of a given suffix. Partial-suffix frames were created by randomly deleting letters from full suffix frames. Mono-morphemic frames were sampled to have a wide spread of frames, from those with many possible completions like s \_ \_ \_ \_ to those with few, like b r i c \_ .

## Results

### Controls

- log token frequency of the pattern (from Subtlex)
- log type frequency of the pattern (from Subtlex)
- number of missing letters in pattern
- number of present letters in pattern
- interaction between number of present letters and number of missing letters

### Overall effect

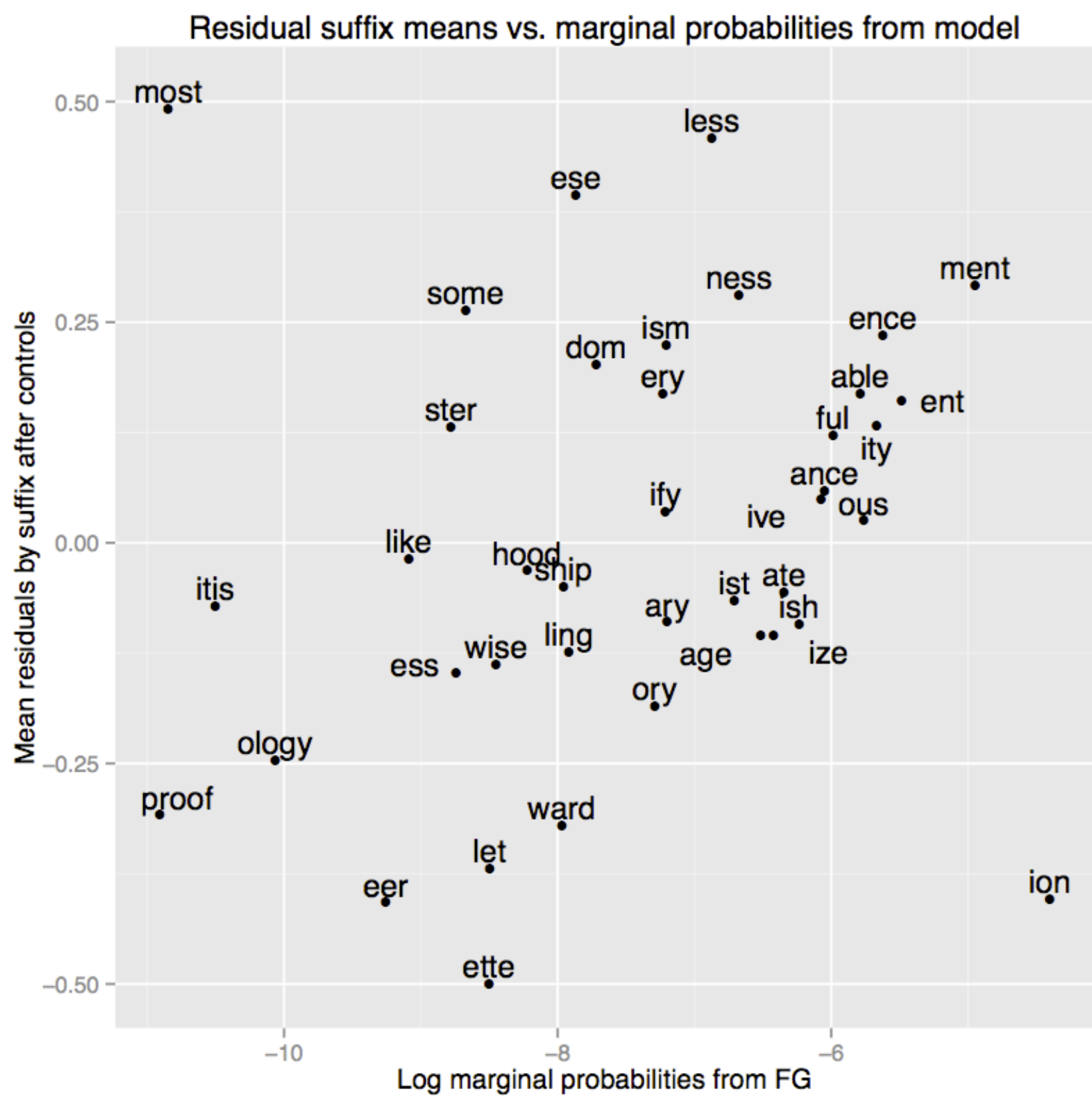
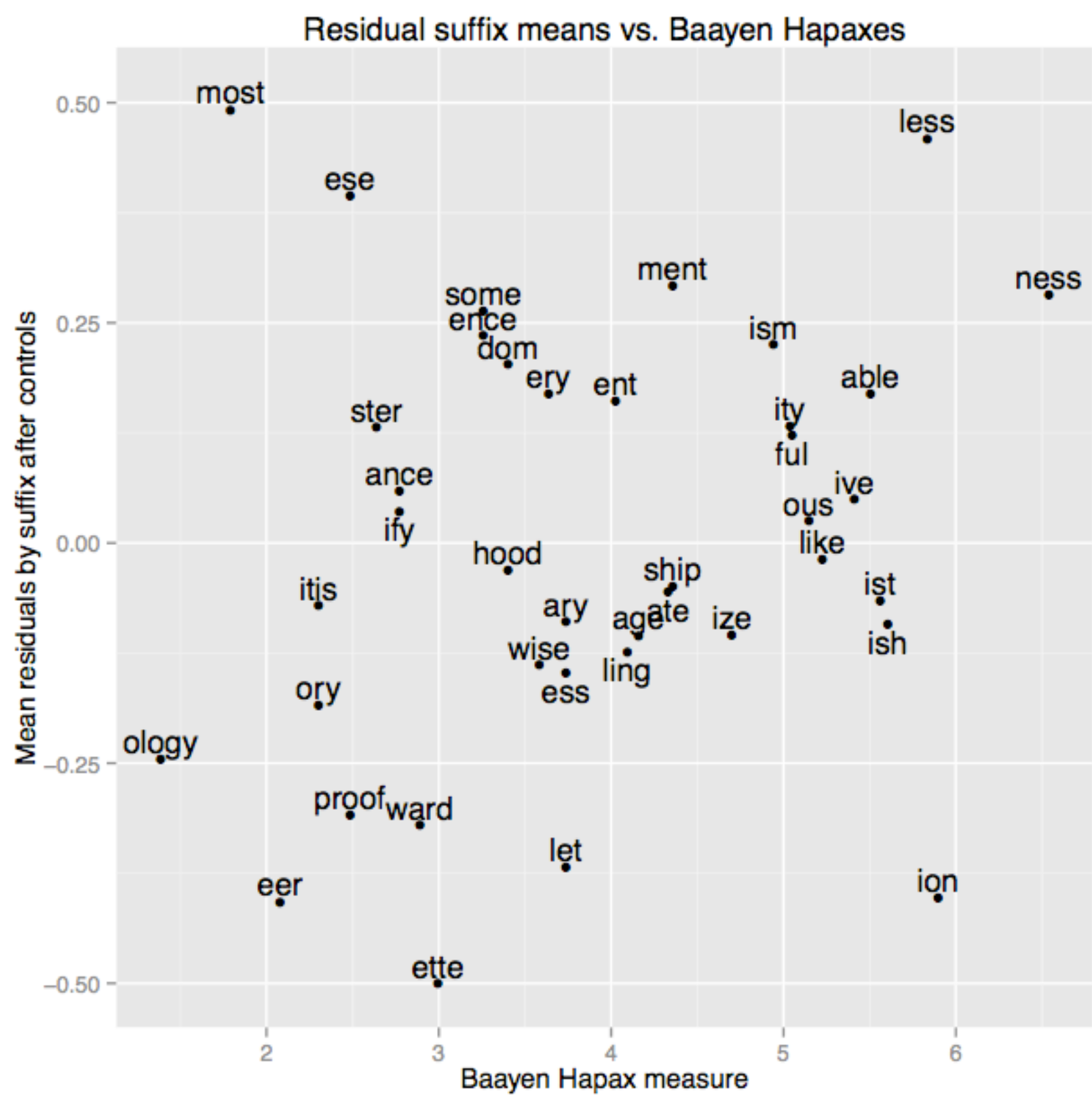
-We fit a mixed effect model with the above controls and a maximal random effect structure for subject. As predicted by T&K full suffix frames were inflated relative to a baseline for partial suffix frames while controlling for frequency ( $\beta=.97$ ,  $t=20.43$ ,  $\chi^2=61$ ,  $p<.001$ ), and both full and partial frames were overestimated relative to mono-morphemic frames ( $\beta=.35$ ,  $t=8.41$ ,  $\chi^2=229$ ,  $p<.001$ ).

### Productivity effect

-The FG model produces marginal probability scores that can be thought of as the probability of seeing a given suffix in either an existing word **or** in a novel word. Thus, the score can be thought of as a rational integration of the expected frequency of the suffix in the existing lexicon along with its expected probability of generalization.

-A higher marginal probability as estimated by FG was predictive of the residuals after regressing out the nuisance variables ( $\beta=.03$ ,  $t=10.06$ ,  $p<.0001$ ).

-Baayen's P\* was also significantly predictive of the residuals ( $\beta=.03$ ,  $t=10.89$ ,  $p<.0001$ ).



## Conclusion

- The role of morphological productivity in these estimates suggests that T&K's effect is likely caused by a "hallucinatory" effect of productive morphemes.
- Productive morphemes can give rise to unbounded numbers of novel forms, the presence of a productive suffix in isolation causes overestimation of the frequency of the pattern, with more productive morphemes leading to greater rates of overestimation.
- Thus, while T&K's result indicates that special purpose mechanisms can lead people to fallacious probabilistic reasoning, these mechanisms may be optimal in their intended domain, in this case, morphology.

## Citations

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