

# *Machine Learning-Based Generalized Model for Finite Element Analysis of Roll Deflection During the Austenitic Stainless Steel 316L Strip Rolling*

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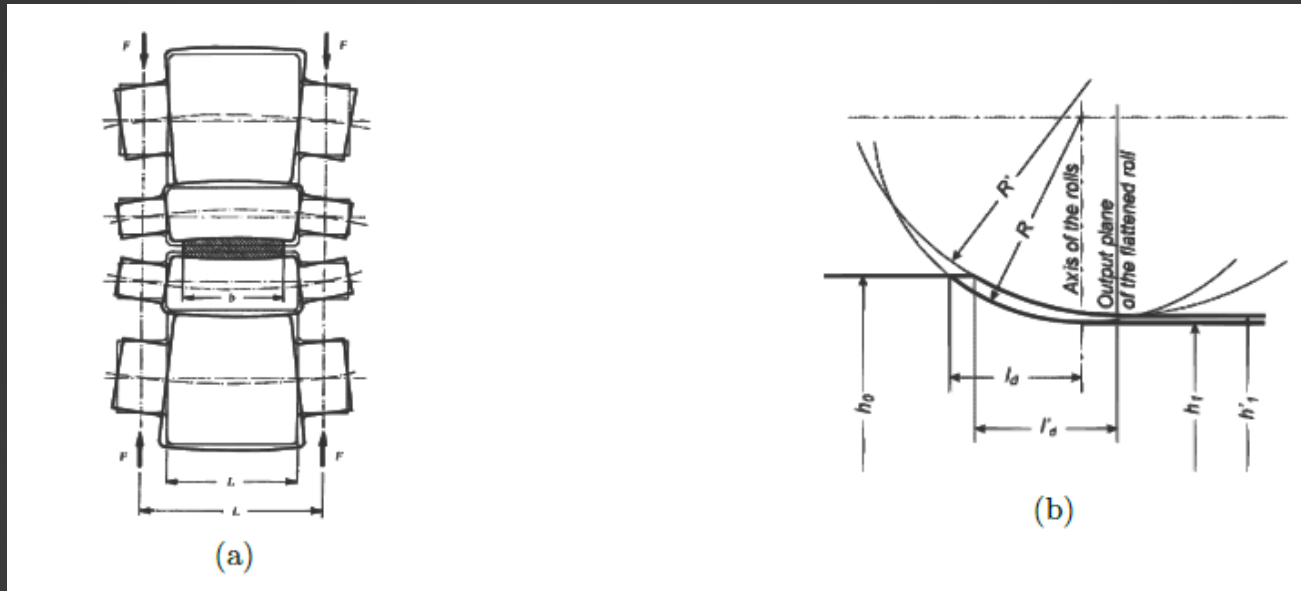
# Overview

- **Introduction**
- **Methodology and Model**
- **Deflection and Work-roll Characteristics**
- **Artificial Neural Network (ANN)**
- **Evaluation and Results**
- **Conclusion and Discussion**

# Introduction

- What is work-roll Deflection?

Forces acting within the roll gap, caused by the resistance of the metal deformation, result in the elastic deformation of the roll, which changes the roll dimensions.



*(a) elastic deflection of the rolls*

*(b) Elastic flattening of the rolls*

# Introduction

Which characteristic of Austenitic Stainless Steel 316L makes it to behave differently from other kind of steels?

The results of the X-Ray pattern diffraction of the deformed ASS 316L show three phases including  $\varepsilon$ -Martensite, Austenite, and  $\alpha'$ -Martensite.



# Methodology and Model



**Following Orowan's Theorem and solve the Equilibrium Equation using an FD Approach**



**Mean Pressure which the Strip applies to the Roll**



**Utilizing Numerical FEA for One-Dimensional (1D) Cantilevered Beam to obtain the Roll Deflection.**



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**Mechanical Tensile Tests;**

- **$0.001, 0.00052, 0.0052, 0.052 \text{ s}^{-1}$**
- **In a Room Temperature**
- **Annealed at  $1030^{\circ}\text{C}$  for 30 minutes**

**Collect the strain and stress from tests to make a required Dataset.**

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Inputs

Strain & Strain rates



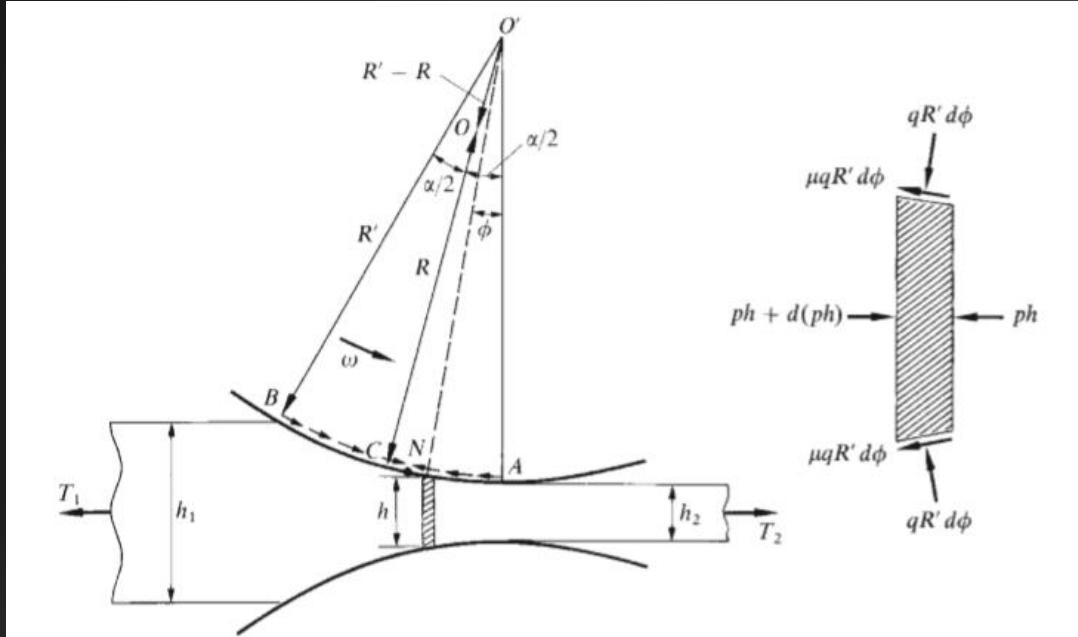
Outputs

Dynamic Flow Stress



# Methodology and Model

## Equation of Equilibrium



### Yield Criterion

$$q - p = 2k$$

$$h = h_2 + 2R'(1 - \cos \phi) \approx h_2 + R^2 \phi^2$$

$$\frac{d}{d\phi}(hp) = 2qR'(\sin \phi \mp \mu \cos \phi)$$

- Forward Difference for both Sides
- Dynamic Flow Stress updates from ANN



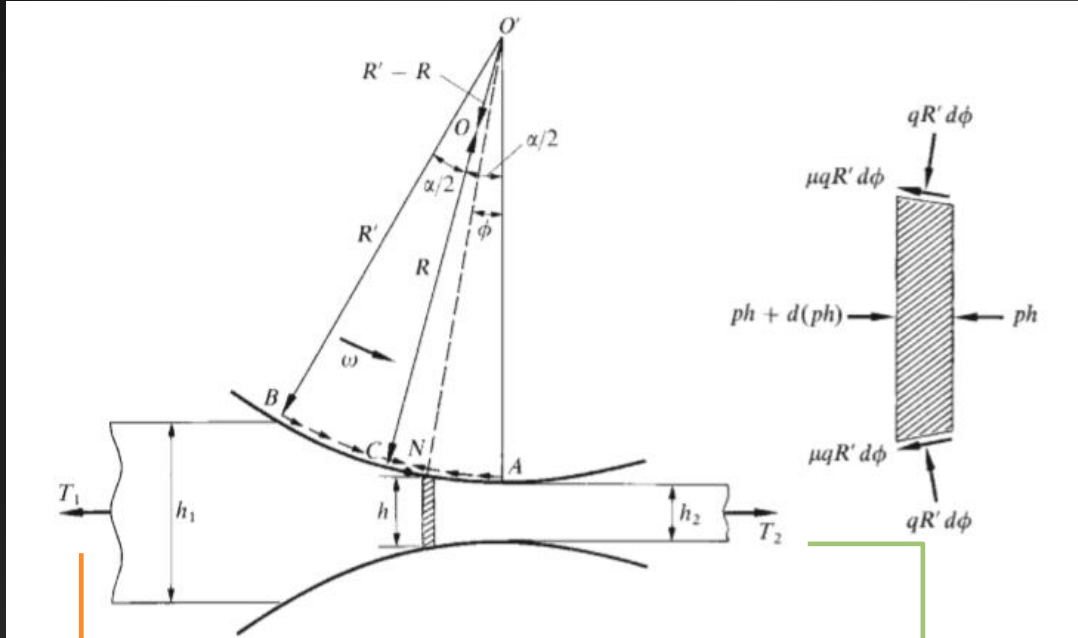
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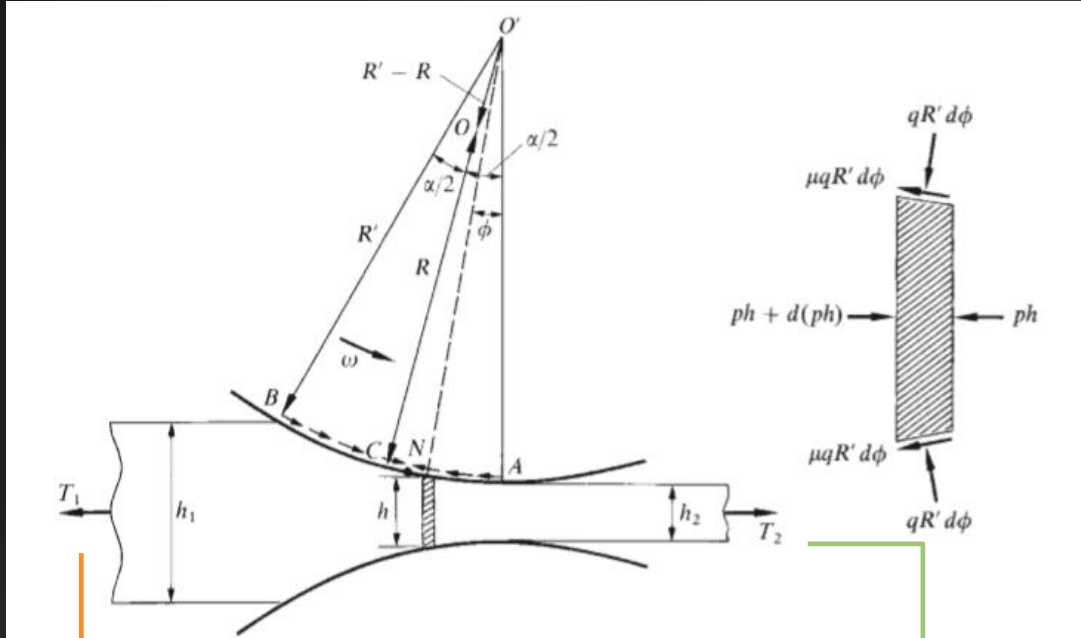
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$$\frac{h_i(q_{i+1} - 2k_{i+1} - q_i + 2k_i)}{\phi_{i+1} - \phi_i} + 2\mu R q_0 = 4kR\phi_i$$

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# Deflection and Work-roll Characteristics



**Distributed Load**

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$$\frac{d^2}{dx^2} \left( EI \frac{d^2 w}{dx^2} \right) = p(x)$$

w: Work-Roll Deflection  
x: Length of the Roll

$$I = \frac{\pi d^4}{64}$$

I: The Second Moment of Inertia

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Calculate the Work-Roll Deflection  
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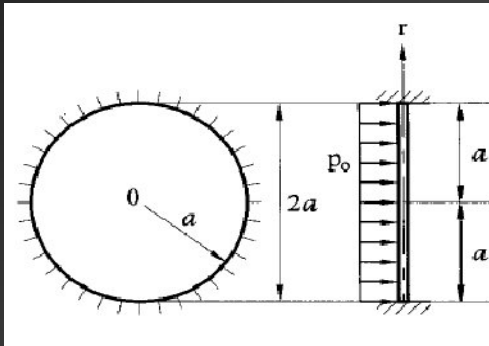
(1)

Galerkin Weighted-Residual

Finite Element formulation  
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Calculate the Work-Roll Deflection  
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(2)



$$Deflection (Max) = \frac{pa^2}{16\pi D} \quad \text{at } r = 0$$

$$D = \frac{Et^3}{12(1-\nu)}$$

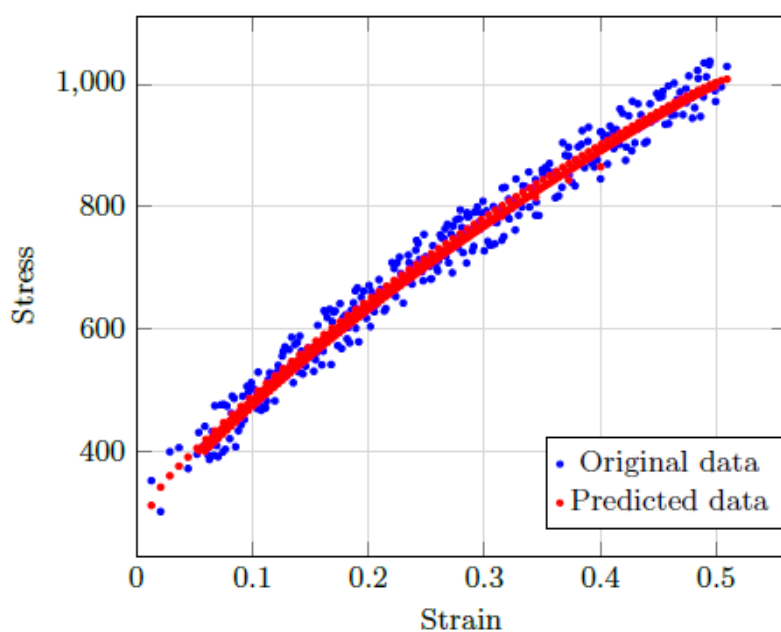
Calculate the Work-Roll Deflection  
using Analytical Analysis



# Artificial Neural Network (ANN)



Linear Regression



$$y = X\beta + \epsilon$$

$$X = \begin{bmatrix} 1 & x_{11} & x_{12} \\ 1 & x_{21} & x_{22} \\ \vdots & \vdots & \vdots \\ 1 & x_{n1} & x_{n2} \end{bmatrix}$$

X: Feature vectors of our data

y: Output Prediction

n: Total Number of Data

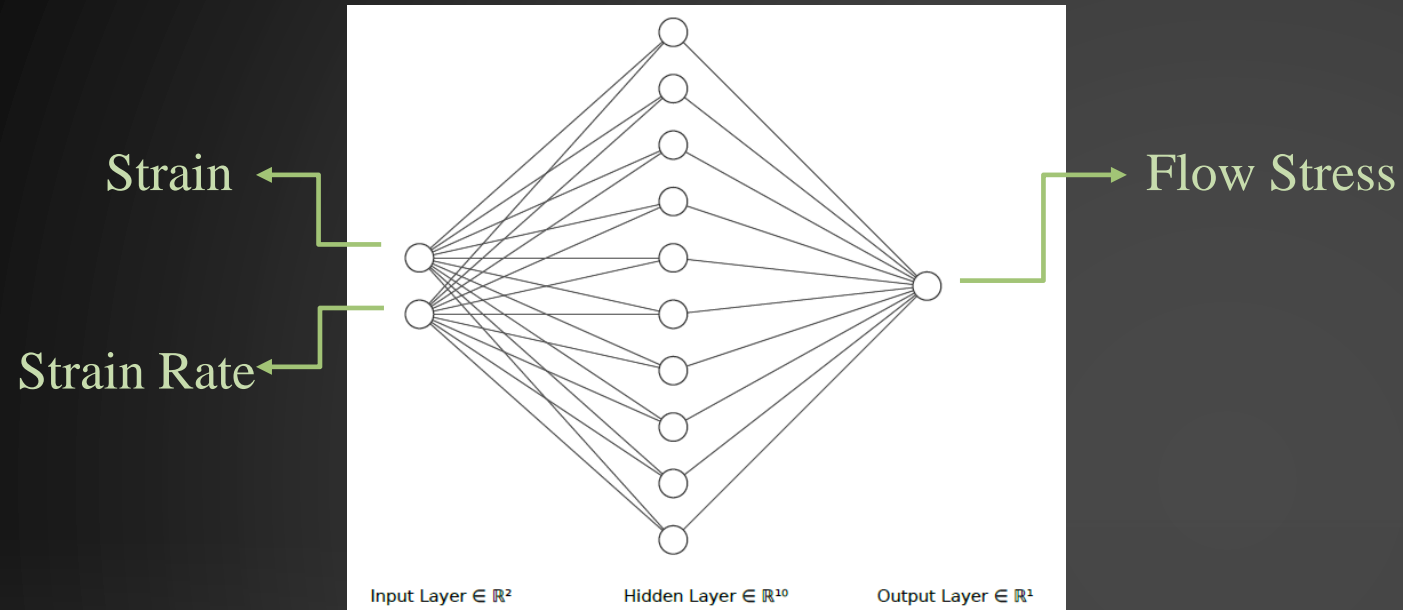
$\beta$ : Weights

$\epsilon$ : Biases

X: Strain and Strain rate values

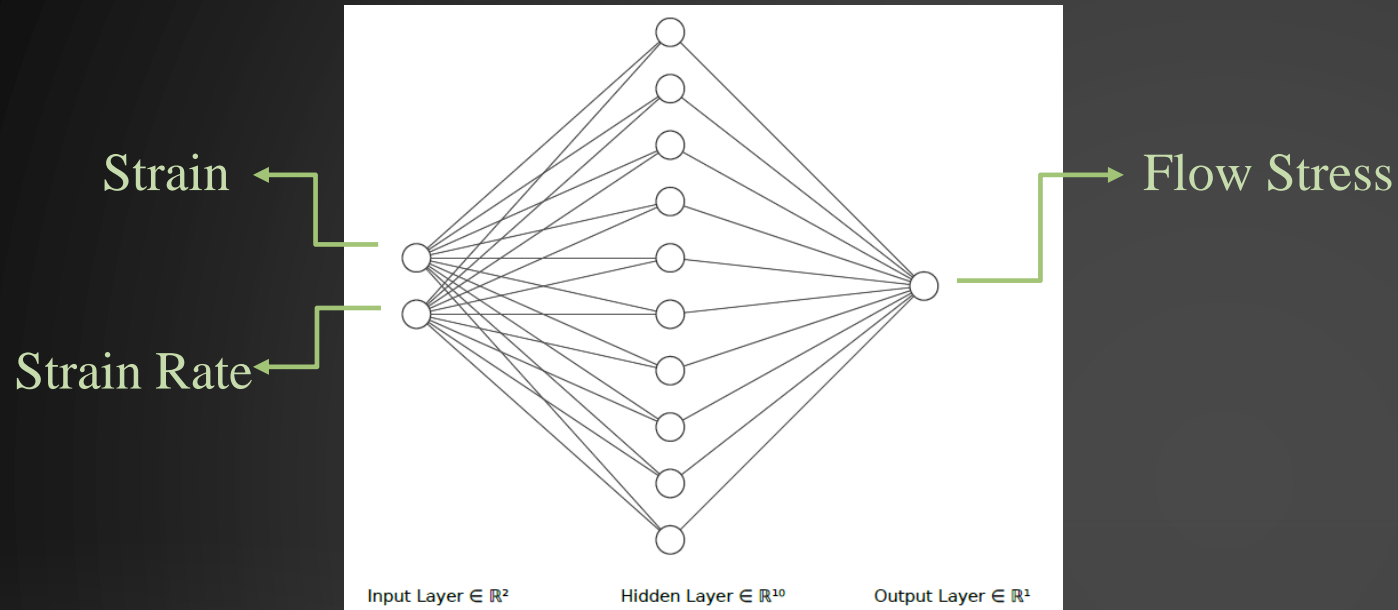
y: Predicted Dynamic Flow Stress

# Artificial Neural Network (ANN)



Model Architecture.

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$$MSE = \frac{\sum_{i=1}^n (y_i - y'_i)^2}{n}$$

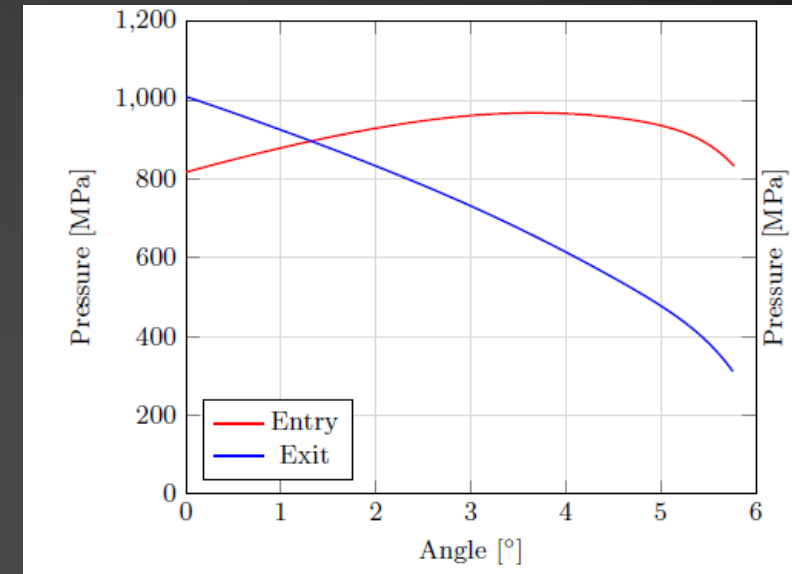
Training Data: 70%  
Test Data: 15%  
Validation Data: 15%

# Evaluation and Results



Final thicknesses of specimens after multi-pass rolling.

2-Pass	3-Pass	4-Pass	5-Pass	6-Pass	7-Pass
2.8	2.48	2.23	1.99	1.74	1.44



The angle of the neutral point for 1-pass rolling, using proposed Finite Difference Method;

Is **1.31°**

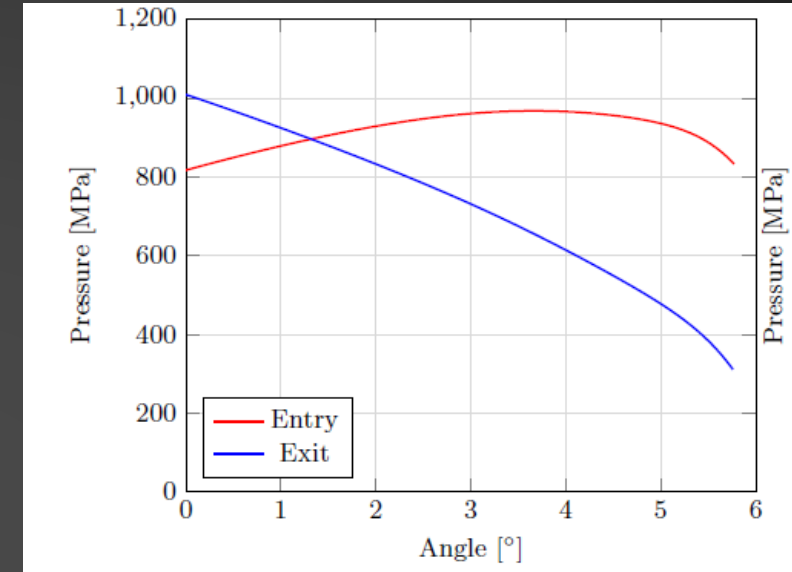


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(1) The angle of the neutral point for 1-pass rolling, using proposed Finite Difference Method; **Is 1.31°**

(2) While using an analytical manner;  $\sin \gamma_n = \frac{\sin \alpha}{2} + \frac{\cos \alpha - 1}{2\mu}$  **Is 1.42°**

# Evaluation and Results



Mean pressure values as distributed loads for multi-pass rolling.

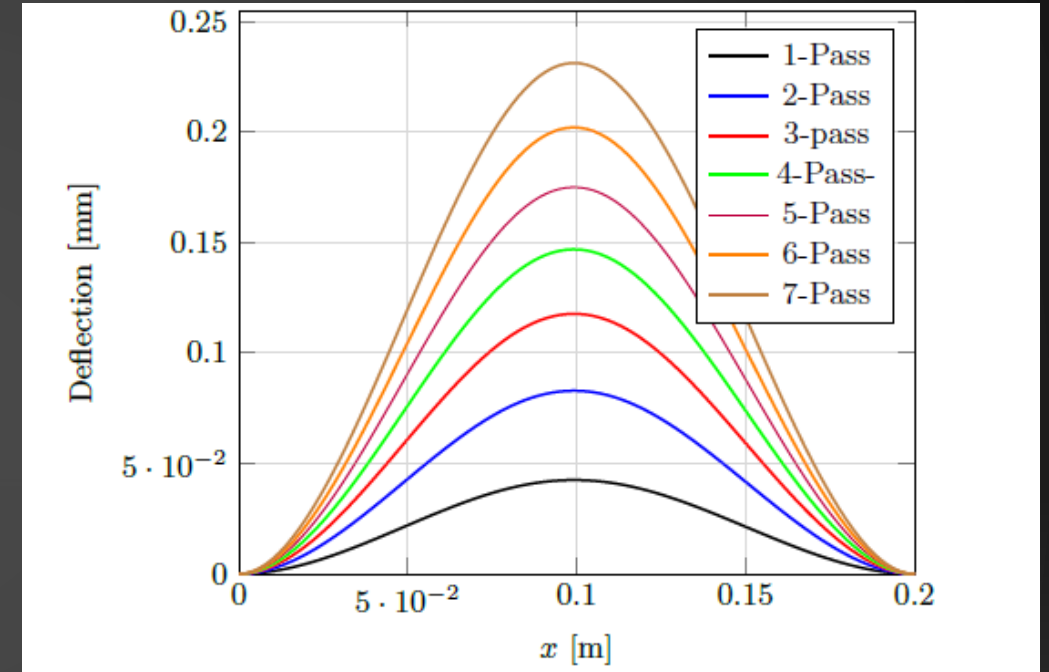
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Comparing deflection values along the roll widths, which are caused by the multi-pass rolling of the ASS 316L in the room temperature.

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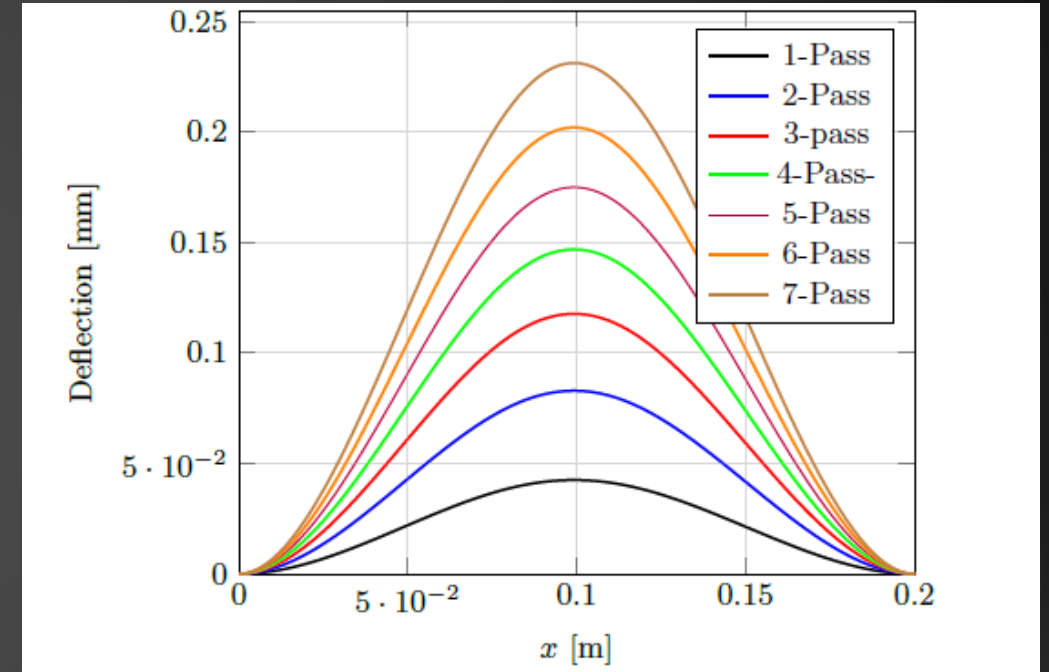
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Plain-Strain condition



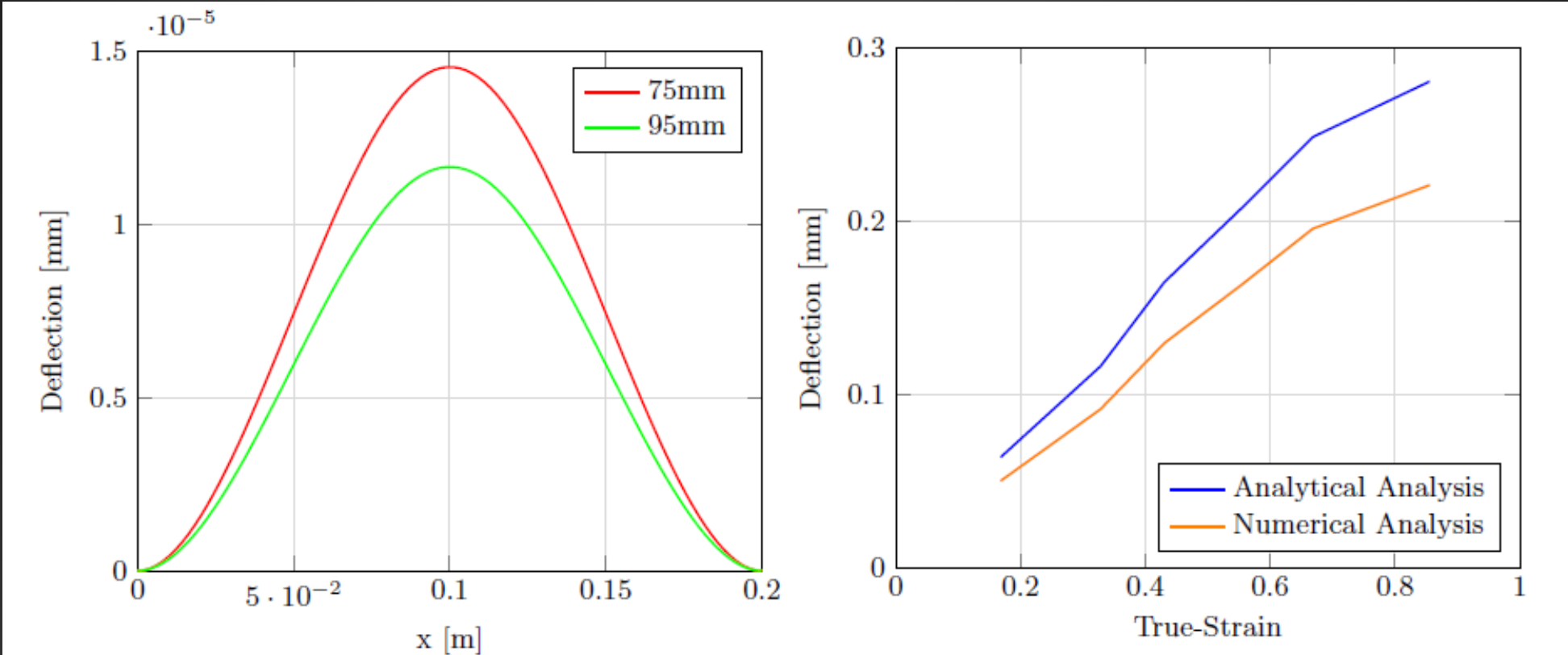
Deflection values vary according to the normal distribution along the width of the roll.



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# Evaluation and Results



Evaluation results.

# Conclusion and Discussion



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- ⚡ Additionally, we created Stress316L, the first public dataset for Strain-Stress values of ASS 316L during cold tension from real experiments.

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- ⚡ With increasing the dimensionality of the feature vectors, we could utilize deeper networks. Training different networks and ensembling the resulting fits would also be beneficial.

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**Thank you for listening!**