

NOTE ROAD



GET STARTED

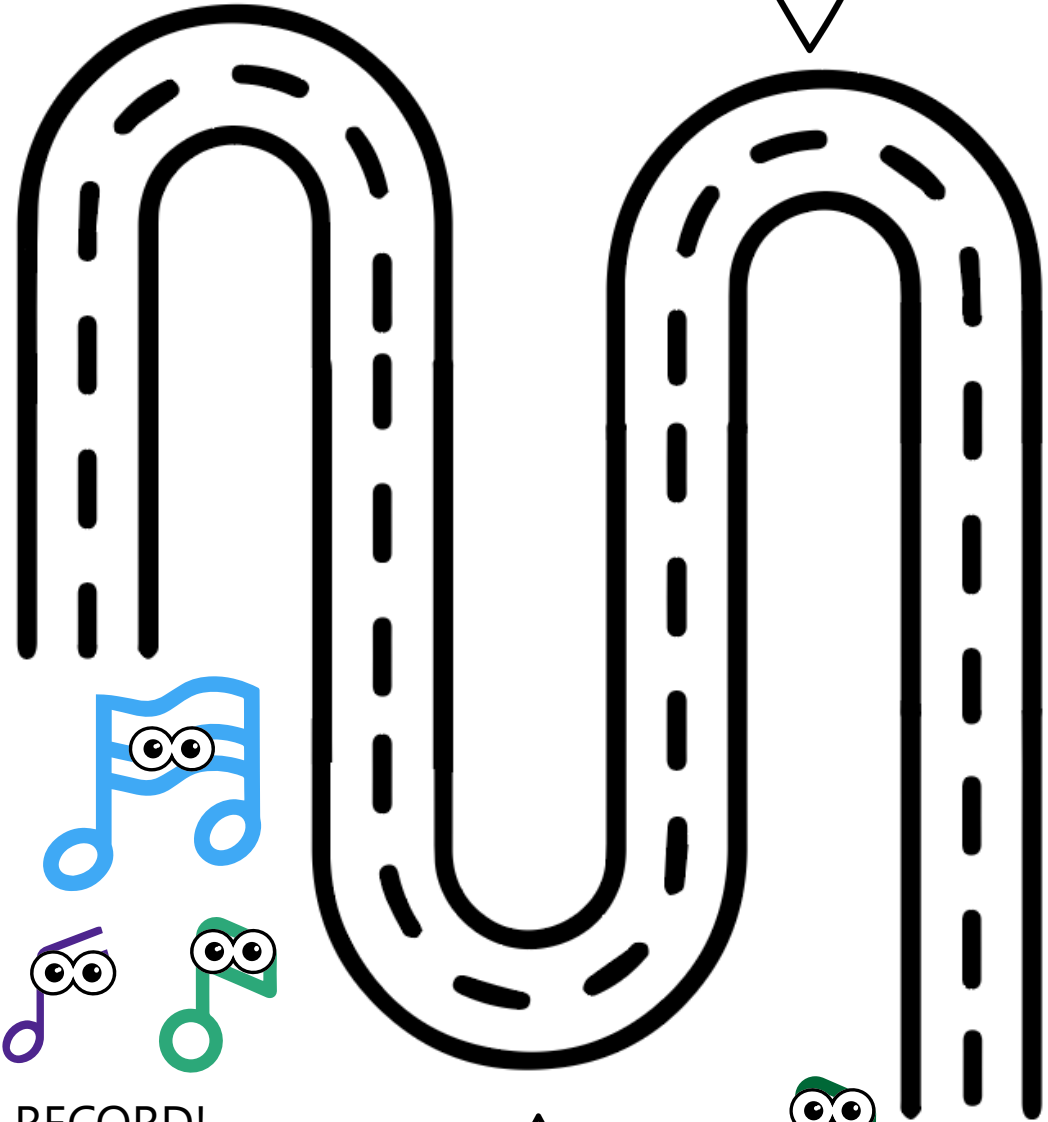
HERE'S A MAP OF OUR JOURNEY!

Record your unique sound and watch as it transforms!
Click on each step along the way to learn more!

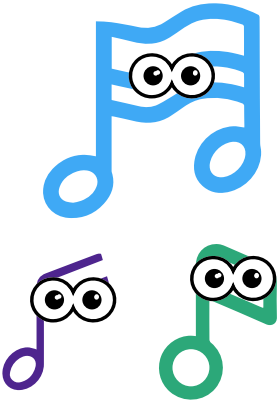
FILTERING



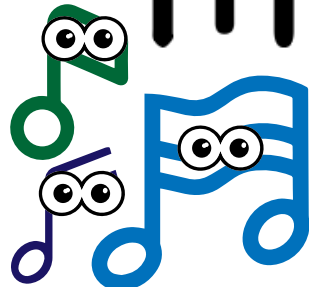
DISCRETE TIME FFT



RECORD!



DISCRETIZATION



SUCCESS!

RECORD A UNIQUE SOUND

CLICK THE MICROPHONE TO START



DONE!

CLICK THE MICROPHONE TO CONTINUE



FILTERING

WHAT IS FILTERING AND WHY DO WE DO IT?

Filtering is when we try to take out signals which don't meet certain standards or don't fall within a criteria which we specify. We filter in order to remove noise from signals and only listen to the sounds we most care about hearing.

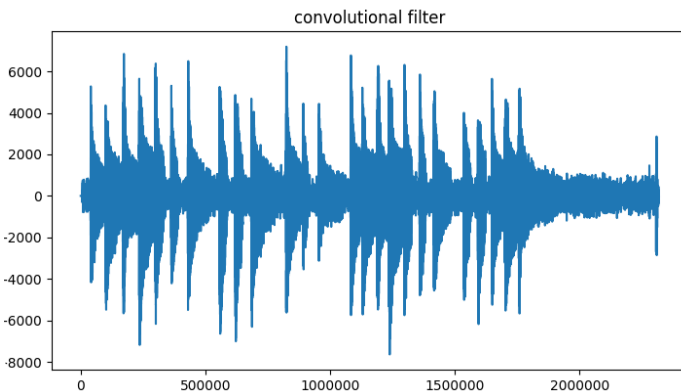
WHAT IS BAND PASS FILTERING?

Band pass filters are filters which only let in signals within a certain range. When filtering this note, we look specifically at only signals that fall in between two frequencies. Every other sound that doesn't fall within those bounds is taken out.

WHAT IS CONVOLUTIONAL FILTERING?

Convolution is a filter that suppresses or enhances components of the signal by taking a running average. Given a sound input, the output is a sound of the same frequency but an amplitude and phase closer to that of the running average. This creates a more normalized sound.

YOUR FILTERED SIGNAL:



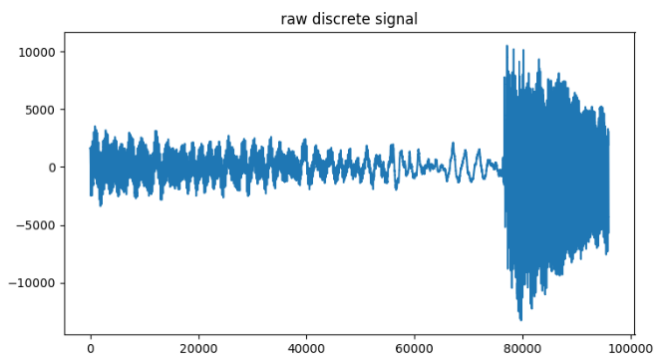
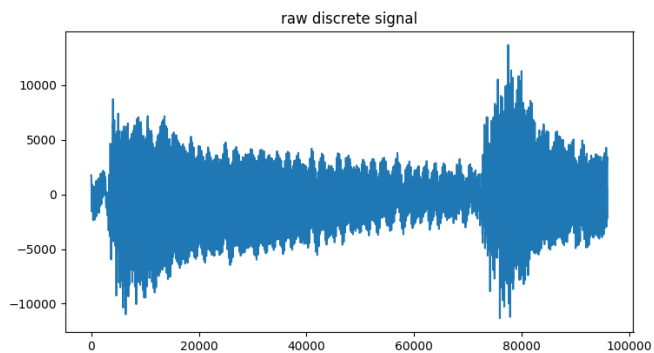
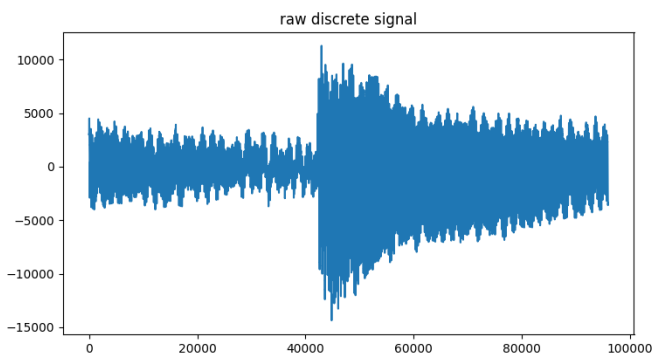
BACK

DISCRETIZATION

WHAT IS DISCRETIZATION?

Discretization is the process of turning continuous signals into discrete chunks. Transforming a signal into discrete time spaces is useful because it allows you to independently process and compare the samples.

YOUR DISCRETIZED SIGNALS:



BACK

DISCRETE-TIME FT

WHAT IS A FOURIER TRANSFORM?

A fourier transform is a change in perspective from a complete signal to its parts. It allows you to analyze a signal and learn about it's attributes. Fourier transforms change the axes of a regular sound wave from amplitude vs time to amount of a frequency vs frequency.

WHAT IS DISCRETE-TIME FT?

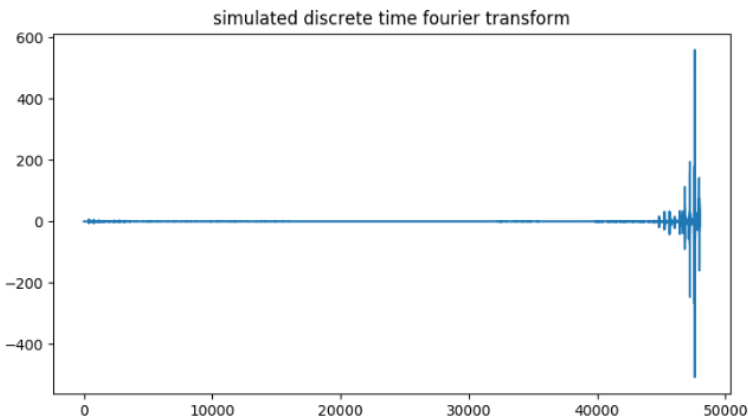
A discrete-time fourier transform is a special type of fourier transform that uses a function of continuous frequency that is broken into discrete time samples.

HOW DOES IT WORK?

Discrete Time Fourier Transforms work similarly to fourier transforms, except the math is a bit different. The way in which signals are added together is done through a sum (as opposed to an integral which adds things continually).

REVEAL MATH

YOUR UNIQUE SIGNAL:



BACK

THE MATH BEHIND DTFT

The following equation shows how a regular continuous-time signal can be represented in the frequency domain.

$$X(\omega) = \int_{-\infty}^{\infty} x(t)e^{-j\omega t} dt.$$

A discrete-time signal is summable meaning: $\sum_{n=-\infty}^{\infty} |x[n]| < +\infty$

has a DTFT $X(\Omega)$, $-\infty < \Omega < \infty$, that can be written as:

$$X(\Omega) = \sum_{n=-\infty}^{\infty} x[n]e^{-jn\Omega}$$

Notice that this is very similar to the continuous-time signal above, the only difference is the integral. This is because the integral is taking the sum of all of the entries continuously, but the discrete time fourier transform adds up all of the entries in discrete chunks, thus the summation symbol.

HOW IS DTFT DIFFERENT THAN DFT?

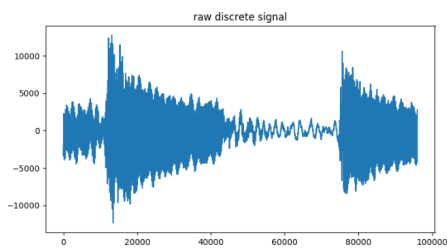
The Discrete Fourier Transform is a type of DTFT. The discrete fourier transform is similar to the DTFT except that it uses discrete frequency points instead of a continuous frequency. It is often used to analyze signals on computers because computers work on a finite number of points.

DTFTs can be simulated on computers by including a large number of samples. As the number of samples gets closer to infinity, the frequency domain becomes a continuous signal. We tried to increase the number of samples in small amounts of time to create things that are similar to DTFTs. It is also important to say that the DFT is just a DTFT which is sampled at equally spaced frequency points.

WE FOUND OUR NOTE!

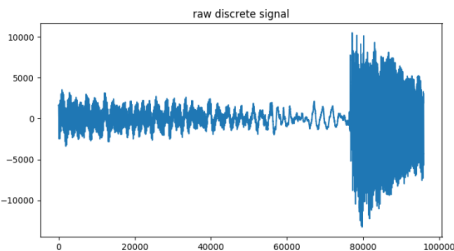


Using the frequency vs. amplitude graphs we generated using discrete-time fourier transforms, we can find note being played in a given sample.

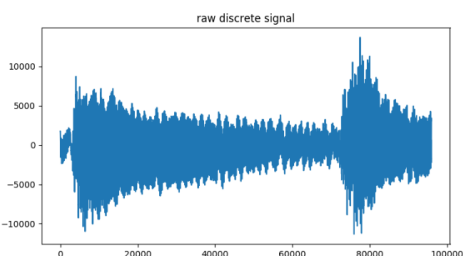


CORRESPONDING NOTE

A5



C5



G4

Map Your Adventure Reflection

Dhara and Maia

10, December 2019

For this assignment, we decided to create an experience for a child which covered content like Discrete Time Fourier Transforms and Convolutional filtering in an engaging and informative way. To do that, we thought about music and how it could relate to these topics in a way that would be entertaining for a child. From there, we decided to document a music note in the midst of an identity crisis and show how using these techniques could lead us to identify music notes.

We did this by analyzing a sample song (Mary had a Little Lamb) and visualizing the data in matlab and python at each step in the process as well as creating an app experience which has more information about each of these steps. The app outlines why the steps are important and how they work.

The steps of the app and analysis are: taking in a sound, filtering that sound, separating that sound into discrete time sections, running discrete time fourier transforms on each discrete time section, and identifying the note from the resulting discrete time fourier transform.

We hit two main areas of technical depth in this project (and reviewed much of the content we were a little less sure of ourselves in!) The first was convolutional filtering as a means of digital signal processing. To be honest, we learned tons about digital signal processing in an effort to create a filter which we liked and did what we needed it to. This is most evident in our code, both in the matlab where we are currently doing our filtering, and in the python where we have left many of the filtering methods we tried in the comments. The second major point of learning was a detailed understanding of discrete time fourier transforms and how they differ from the discrete fourier transform and the continuous fourier transform. This is especially evident in the way in which discrete time fourier transforms are explained in our app and the way in which we outline the math. One of the biggest challenges we faced was trying to relay this extremely complex technical content to a non technical audience. We hope that we did a decent job in that endeavour.

The analysis was mostly done in python, with the filtering completed in MATLAB. This allowed us many visualization options for our final graphs. At the moment, the name of the note is the title for plots which depict each step in the filtering process, making it intuitive to see how the signal changes over time to reach a solution.

FILTERING AND DISCRETE-TIME FFT

```
[x, Fs] = audioread("lamb.wav");
sound(x, Fs);

N = length(x);
f = linspace(-Fs/2, Fs/2 - Fs/N, N) + Fs/(2*N)*mod(N, 2);

X = fft(x);
```

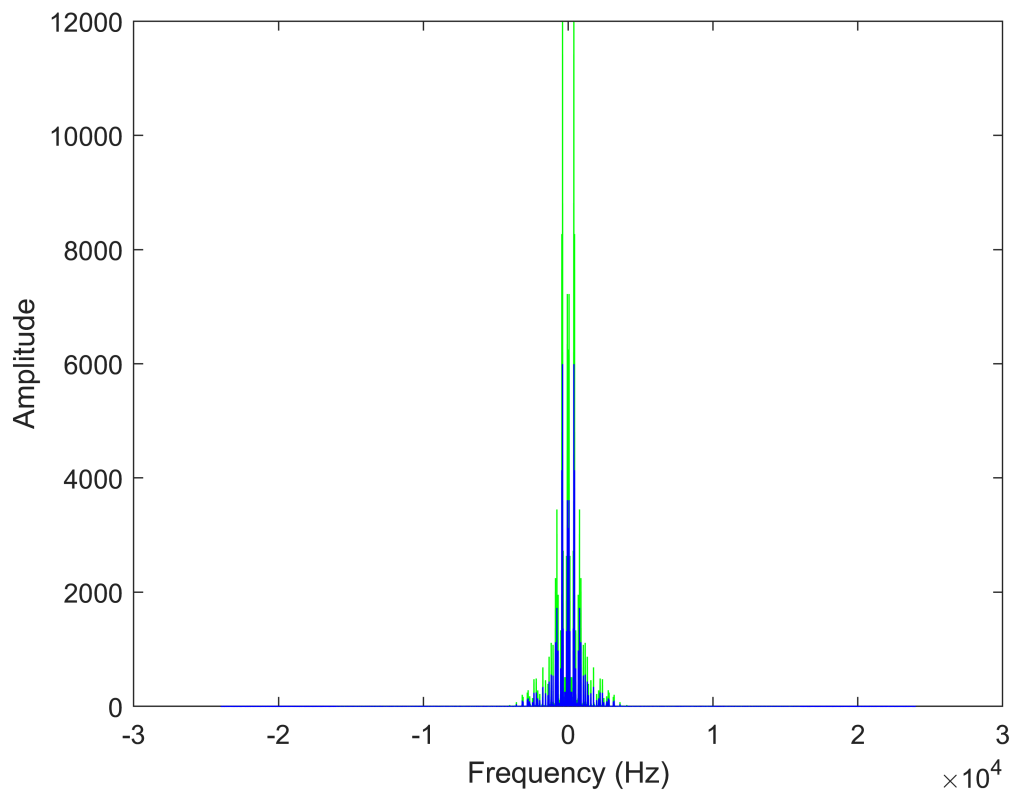
CONVOLUTION FILTER:

```
xSmooth = conv2(x, 0.5, "same")
```

```
xSmooth = 1159158x2
    0     0
    0     0
    0     0
    0     0
    0     0
    0     0
    0     0
    0     0
    0     0
    0     0
    0     0
    ⋮
    ⋮
```

```
sound(xSmooth, Fs);
XSmooth = fft(xSmooth);

%frequency vs. amplitude of filtered and unfiltered
plot(f, fftshift(abs(X)), 'g', f, fftshift(abs(XSmooth)), 'b');
xlabel('Frequency (Hz)');
ylabel('Amplitude')
```



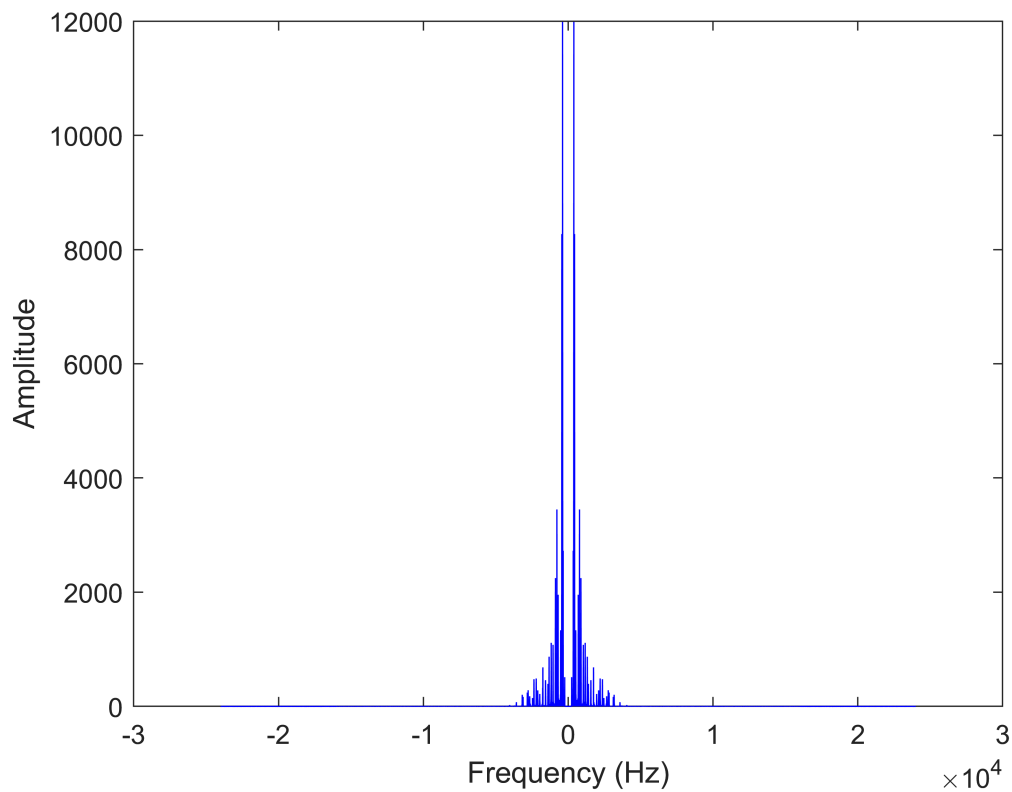
BAND PASS FILTER:

```
xBand = bandpass(x,[.01, .999])
```

```
xBand = 1159158x2
-0.1254 -0.1254
-0.1248 -0.1248
-0.1240 -0.1240
-0.1232 -0.1232
-0.1222 -0.1222
-0.1212 -0.1212
-0.1200 -0.1200
-0.1187 -0.1187
-0.1173 -0.1173
-0.1157 -0.1157
⋮
```

```
sound(xBand, Fs);
XBand = fft(xBand);

%frequency vs. amplitude of filtered and unfiltered
plot(f,fftshift(abs(XBand)), 'b');
xlabel('Frequency (Hz)');
ylabel('Amplitude')
```



```
%DTFT
omega = linspace(-pi, (pi*(1-2/N)),N)
```

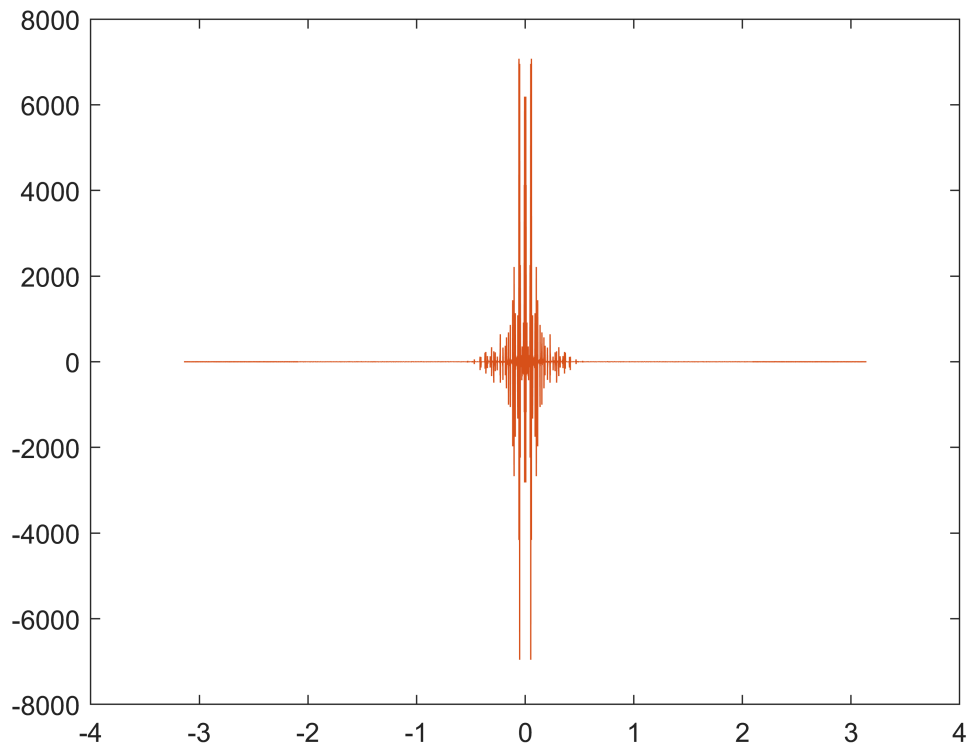
```
omega = 1x1159158
-3.1416 -3.1416 -3.1416 -3.1416 -3.1416 -3.1416 -3.1416 -3.1416 ...
```

```
c = fftshift(fft(fftshift(x)))
```

```
c = 1159158x2 complex
104 x
 0.0000 + 0.0000i  0.0000 + 0.0000i
 0.0000 - 0.0000i  0.0000 - 0.0000i
-0.0000 - 0.0000i -0.0000 - 0.0000i
-0.0000 - 0.0000i -0.0000 - 0.0000i
 0.0000 - 0.0000i  0.0000 - 0.0000i
-0.0000 - 0.0000i -0.0000 - 0.0000i
-0.0000 + 0.0000i -0.0000 + 0.0000i
-0.0000 - 0.0000i -0.0000 - 0.0000i
-0.0000 - 0.0000i -0.0000 - 0.0000i
 0.0000 - 0.0000i  0.0000 - 0.0000i
  ⋮
```

```
plot(omega, c)
```

Warning: Imaginary parts of complex X and/or Y arguments ignored



```
audiowrite("bandpass.wav",xBand,Fs);  
audiowrite("convolution.wav",xSmooth,Fs);
```

Visualizer Code

```
import numpy as np
import sounddevice as sd
from matplotlib import pyplot as plt
import pylab as pl
from pydub import AudioSegment
from pydub.playback import play
from scipy import signal, fft, fftpack
from scipy.io.wavfile import write, read

class SoundProcessing:

    def __init__(self):
        pass

    def record_sound(self):
        """
        Not taking in our own sound, but if we were this method would process the file to make it usable for us
        """
        fs = 44100 # Sample rate
        seconds = 90 # Duration of recording

        myrecording = sd.rec(int(seconds * fs), samplerate=fs, channels=2)
        sd.wait() # Wait until recording is finished
        write('output.wav', fs, myrecording) # Save as WAV file

    def break_up_sound(self):
        audio_chunk_list = []
        audio_file = "lamb.wav"
        audio = AudioSegment.from_wav(audio_file)
        print(type(audio))
        list_of_timestamps = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24] #and so on in "seconds"

        start = 0
        for idx, t in enumerate(list_of_timestamps):
            #break loop if at last element of list
            if idx == len(list_of_timestamps):
                break

            end = t * 1000 #pydub works in millisec
            print("split at [{:}] ms".format((start/1000), (end/1000)))
            audio_chunk = audio[start:end]
            audio_chunk.export("audio_chunk_{:}.wav".format(end), format="wav")

            start = end #pydub works in millisec
            print(type(audio_chunk))
            print(audio_chunk.max_dBFS)
            print(audio_chunk.max_possible_amplitude)
            audio_chunk_list.append(audio_chunk)
        return audio_chunk_list

class MusicClip:

    def __init__(self, clip):
        self.music_clip = clip

    def filter(self):
        """
        We ended up doing our filtering in matlab, but this method shows some of the many filters and ways in which we tried to filter in python. Ultimately, we decided that MATLAB would allow us more flexibility
        """
        num_array = AudioSegment.get_array_of_samples(self.music_clip)
        # print(num_array)
        print(np.shape(num_array))

        #hilbert transforms
        # plt.plot((np.array(num_array)))
        # # plt.plot(np.real(signal.hilbert(np.array(num_array))))
        # plt.show()

        # print(np.real(signal.hilbert(np.array(num_array))))
        # filtered = signal.hilbert(np.array(num_array))
        # plt.plot(filtered, label = 'hilbert filtering ')
        # plt.show(block = False)
        num_array = np.array(num_array)
        num_array = num_array/1000
        # act_num_array =[]
        # for row in np.real(signal.hilbert(np.array(num_array[1]))):
        #     print(row)
        #     act_num_array.append(row[1])

        max_sound = np.asarray(num_array).max()
        print(np.asarray(num_array).max())
        print(max_sound)
        print((np.asarray(num_array).max() == max_sound))
        print(type(num_array))

        # hann window
        # print(num_array.si)
        # win = signal.hann(np.size(num_array)/2, False)
        # # plt.plot(win)
        # # plt.show()
        # win = win*(max_sound)
        # # plt.plot(win)
        # # plt.show()
        # print(np.shape(num_array))
        # # win = signal.hann(20)
        # print(type(win))
        # # plt.plot(num_array)
        # # # # plt.show()
        # # plt.plot(win)
        # plt.show(block = False)

        # time = np.linspace(0,1,np.size(num_array))
```

Visualizer Code

```
105 # high pass filters with fourier transforms
106 # W = fftpack.fftfreq(np.size(num_array))
107 # print(W)
108 # f_signal = fftpack.rfft(num_array)
109
110 # cut_f_signal = f_signal.copy()
111 # cut_f_signal[(W>200000000000000000000)] = 0
112 # cut_signal = fftpack.irfft(cut_f_signal)
113
114 # plt.subplot(221)
115 # plt.plot(time,num_array)
116 # plt.subplot(222)
117 # plt.plot(W,f_signal)
118 # plt.xlim(0,1)
119 # plt.subplot(223)
120 # plt.plot(W,cut_f_signal)
121 # plt.xlim(0,1)
122 # plt.subplot(224)
123 # plt.plot(time,cut_signal)
124 # plt.show()
125
126 # plt.plot(fftpack.rfft(num_array))
127
128 # plt.show()
129
130 fs = 44100
131 t = np.arange(np.size(num_array))
132 fc = 30 # Cut-off frequency of the filter
133 w = fc / (fs / 2) # Normalize the frequency
134 b, a = signal.butter(7, w, 'high')
135 output = signal.filtfilt(b, a, num_array)
136 plt.plot(t, output, label='filtered')
137 plt.legend()
138 plt.show()
139
140 # convolutional ffts to filter
141 # filtered = np.fft.fftshift(signal.fftconvolve(num_array, win, mode = 'same'))
142 # filtered = filtered/1000000
143 # fw = signal.firwin(17,.11, pass_zero='highpass')
144 # f3 = signal.sosfilt(fw, num_array)
145 # plt.plot(f3)
146 # plt.show()
147
148 # butterworth filter
149 # butter1, butter2 = signal.butter(15, .99, 'hp', output='ba', analog = True)
150 # filtered2 = signal.filtfilt(butter1, butter2, num_array)
151 # # plt.plot(num_array)
152 # plt.plot(filtered2)
153
154 # plt.show()
155
156 # convolutional filter
157 # conv = signal.convolve(num_array, win, mode = 'same')
158 # plt.plot((np.array(num_array)), label = 'Signal')
159 # plt.show(block = False)
160 # plt.plot(win, label = 'hann window')
161 # plt.show(block = False)
162 # plt.plot(butter, label = 'fft convolve with hann filter')
163 # # plt.show(block = False)
164 # # plt.plot(conv/1000000, label = 'normal convolution')
165 # plt.show()
166
167
168 filt = write('output_fr.wav', 44100, filtered2)
169
170 # filt = AudioSegment.from_numpy_array(filtered)
171 print(filt)
172
173
174 def run_fft(self):
175     data = AudioSegment.get_array_of_samples(self.music_clip)
176     play(self.music_clip)
177     # signal.freqz()
178     fft_d = np.fft.fftshift(fft(np.fft.fftshift(data)))
179     fft_norm = fft_d/len(data)
180     fft_norm = fft_norm[range(int(len(data)/2))]
181     real_d = np.real(fft_d)
182
183     tp = len(data)/1000
184     vals = np.arange(int(len(data)/2))
185     freq = vals/tp
186     # hist_bins, hist_vals = self.music_clip.fft()
187     # hist_vals_real_normed = np.abs(hist_vals) / len(hist_vals)
188     # plt.plot(hist_bins / 1000, hist_vals_real_normed)
189     # plt.xlabel("kHz")
190     # plt.ylabel("dB")
191     # plt.plot(hist_vals_real_normed)
192     # plt.plot(freq, abs(fft_norm))
193     print(max(np.real(fft_d))/100000)
194     note = self.identify_note(max(np.real(fft_d))/100000)
195     print(type(note))
196
197     plt.title(note)
198     plt.subplot(221)
199     plt.plot(np.real(fft_norm))
200     plt.title('simulated discrete time fourier transform')
201     plt.subplot(223)
202     plt.plot(AudioSegment.get_array_of_samples(AudioSegment.from_wav('lamb.wav')))
203     plt.title('raw entire signal')
204     plt.subplot(224)
205     plt.plot(AudioSegment.get_array_of_samples(AudioSegment.from_wav('convolution.wav')))
206     plt.title('convolutional filter')
207     plt.subplot(222)
208     plt.plot(data)
209     plt.title('raw discrete signal')
210     plt.suptitle("Note: " + note)
211
212     # plt.legend()
```


Visualizer Code

```
212     # plt.legend()
213     plt.show()
214     pass
215
216 def identify_note(self, num):
217     notes = [16.35, 17.32, 18.35, 19.45, 20.60, 21.83, 23.12, 24.50, 25.96, 27.50, 29.14, 30.87, 32.70, 34.65, 36.71, 38.89, 41.20, 43.65, 46.25, 49.00, 51.91, 55.00, 58.27, 61.74, 65.41, 69.30, 73.42, 77.78]
218
219     # Take in the max of the fft, then run through this
220     fr_in = notes.index(min(notes, key=lambda x: abs(x - num)))
221     print(min(notes, key=lambda x: abs(x - num)))
222
223     notes_list = ['C0', 'C#0/Db0', 'D0', 'D#0/Eb0', 'E0', 'F0', 'F#0/Gb0', 'G0', 'G#0/Ab0', 'A0', 'A#0/Bb0', 'B0', 'C1', 'C#1/Db1', 'D1', 'D#1/Eb1', 'E1', 'F1', 'F#1/Gb1', 'G1', 'G#1/Ab1', 'A1', 'A#1/Bb1', 'B1', 'C2', 'C#2/Db2', 'D2', 'D#2/Eb2', 'E2', 'F2', 'F#2/Gb2', 'G2', 'G#2/Ab2', 'A2', 'A#2/Bb2', 'B2', 'C3', 'C#3/Db3', 'D3', 'D#3/Eb3', 'E3', 'F3', 'F#3/Gb3', 'G3', 'G#3/Ab3', 'A3', 'A#3/Bb3', 'B3', 'C4', 'C#4/Db4', 'D4', 'D#4/Eb4', 'E4', 'F4', 'F#4/Gb4', 'G4', 'G#4/Ab4', 'A4', 'A#4/Bb4', 'B4', 'C5', 'C#5/Db5', 'D5', 'D#5/Eb5', 'E5', 'F5', 'F#5/Gb5', 'G5', 'G#5/Ab5', 'A5', 'A#5/Bb5', 'B5', 'C6', 'C#6/Db6', 'D6', 'D#6/Eb6', 'E6', 'F6', 'F#6/Gb6', 'G6', 'G#6/Ab6', 'A6', 'A#6/Bb6', 'B6', 'C7', 'C#7/Db7', 'D7', 'D#7/Eb7', 'E7', 'F7', 'F#7/Gb7', 'G7', 'G#7/Ab7', 'A7', 'A#7/Bb7', 'B7', 'C8', 'C#8/Db8', 'D8', 'D#8/Eb8', 'E8', 'F8', 'F#8/Gb8', 'G8', 'G#8/Ab8', 'A8', 'A#8/Bb8', 'B8', 'C9', 'C#9/Db9', 'D9', 'D#9/Eb9', 'E9', 'F9', 'F#9/Gb9', 'G9', 'G#9/Ab9', 'A9', 'A#9/Bb9', 'B9', 'C10', 'C#10/Db10', 'D10', 'D#10/Eb10', 'E10', 'F10', 'F#10/Gb10', 'G10', 'G#10/Ab10', 'A10', 'A#10/Bb10', 'B10', 'C11', 'C#11/Db11', 'D11', 'D#11/Eb11', 'E11', 'F11', 'F#11/Gb11', 'G11', 'G#11/Ab11', 'A11', 'A#11/Bb11', 'B11', 'C12', 'C#12/Db12', 'D12', 'D#12/Eb12', 'E12', 'F12', 'F#12/Gb12', 'G12', 'G#12/Ab12', 'A12', 'A#12/Bb12', 'B12', 'C13', 'C#13/Db13', 'D13', 'D#13/Eb13', 'E13', 'F13', 'F#13/Gb13', 'G13', 'G#13/Ab13', 'A13', 'A#13/Bb13', 'B13', 'C14', 'C#14/Db14', 'D14', 'D#14/Eb14', 'E14', 'F14', 'F#14/Gb14', 'G14', 'G#14/Ab14', 'A14', 'A#14/Bb14', 'B14', 'C15', 'C#15/Db15', 'D15', 'D#15/Eb15', 'E15', 'F15', 'F#15/Gb15', 'G15', 'G#15/Ab15', 'A15', 'A#15/Bb15', 'B15', 'C16', 'C#16/Db16', 'D16', 'D#16/Eb16', 'E16', 'F16', 'F#16/Gb16', 'G16', 'G#16/Ab16', 'A16', 'A#16/Bb16', 'B16', 'C17', 'C#17/Db17', 'D17', 'D#17/Eb17', 'E17', 'F17', 'F#17/Gb17', 'G17', 'G#17/Ab17', 'A17', 'A#17/Bb17', 'B17', 'C18', 'C#18/Db18', 'D18', 'D#18/Eb18', 'E18', 'F18', 'F#18/Gb18', 'G18', 'G#18/Ab18', 'A18', 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