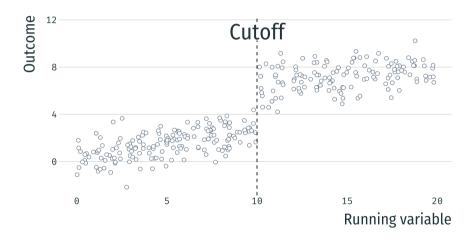
How Far is Too Far? Generalization of a Regression Discontinuity Design Away from the Cutoff

Magdalena Bennett

September 11, 2020

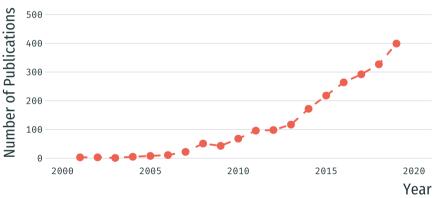
McCombs School of Business, UT Austin DLP Seminar, Department of Economics at UT Austin

Regression discontinuity design

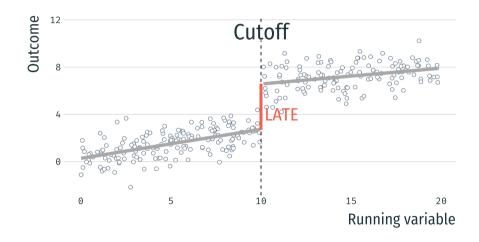


Regression discontinuity design: Increasingly popular

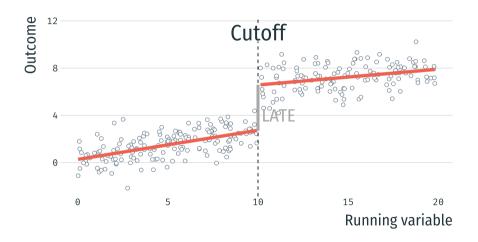




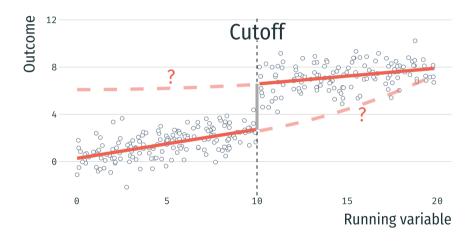
Regression discontinuity design: Strong interval validity



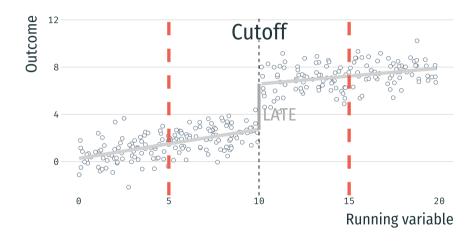
Regression discontinuity design: Limited external validity



Regression discontinuity design: Limited external validity



Regression discontinuity design: Generalization bandwidth?



This paper

Estimation of ATT for population within a generalization interval:

• Pre-intervention period informs generalization interval

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(Wing & Cook, 2013; Keele, Small, Hsu, & Fogarty, 2019)
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 Leverage the use of predictive covariates for breaking link between running variable and outcome

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(Angrist & Rokkanen, 2015; Rokkanen, 2015; Keele, Titiunik, & Zubizarreta, 2015)
```

• Based on local randomization near the cutoff

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(Lee, 2008; Cattaneo, Frandsen, & Titiunik, 2015)
```

This paper

Main advantages:

- Gradual approach
 - No need for "All or Nothing"
 - Interval informed by the data (Cattaneo et al., 2015)
- No extrapolation of population characteristics
 - Compare like-to-like (Rosenbaum, 1987)
 - Makes overlap region explicit
- Generalization to population of interest
 - Use of representative template matching

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(Silber et al, 2014; Bennett, Vielma, & Zubizarreta, 2020)
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• Sensitivity analysis to hidden bias (Rosenbaum, 2010; Keele et al., 2019)

Outline

Motivation

Generalized Regression Discontinuity Design

Framework

GRD in practice

Application: Free Higher Education in Chile

Conclusions

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Generalized Regression Discontinuity Design (GRD)

Two-part problem:

- 1. Identification of generalization interval \mathbf{H}^* using pre-intervention period.
- 2. Estimation of ATT for population within \mathbf{H}^* for post-intervention period.

Generalized Regression Discontinuity Design (GRD)

Setup:

- ullet Two periods: pre- and post-intervention $(t=0 \ {\sf and} \ t=1)$
- R determines assignment to Z in t = 1, e.g.:

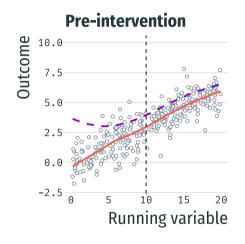
$$Z = \mathbb{I}(R < c)$$

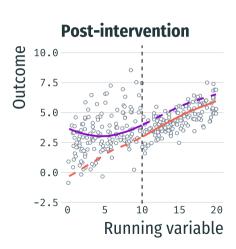
• Potential outcomes under treatment z = 0, 1:

$$Y_{it}^{(z)} = g_z(\mathbf{X}_{it}, \mathbf{u}_{it}, r_{it}) + z_{it} \cdot \underbrace{\tau_{it}(\mathbf{X}_{it}, \mathbf{u}_{it}, r_{it})}_{\mathsf{Treat. Effect}} + \underbrace{\alpha_t}_{\mathsf{Period FE}}$$

- X: Predictive covariates
- u: Unobserved confounder
- τ_i : individual causal effect

Two periods for GRD





$$- Y0(R) - Y1(R)$$

GRD: A gradual approach

Conditional expectations of potential outcomes:

$$Y_0^{(0)}(R) = \mathbb{E}[Y_{i0}^{(0)}|R] = \mu_0(R)$$
 $Y_0^{(1)}(R) = \mathbb{E}[Y_{i0}^{(1)}|R] = \underbrace{\mu_0(R)}_{ ext{Avg. Outcome by R}} + \underbrace{ au_0(R)}_{ ext{Treat. Effect by R}}$

• Identify generalization interval $H = [H_-, H_+]$ for t = 0:

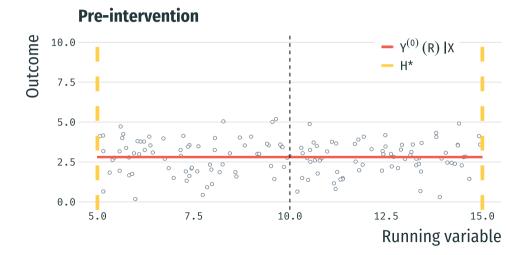
$$R_i = h(\mathbf{X}_i) + \eta_i \quad \forall \ R_i \in H$$

where $H^* = \max\{|H|\}$.

• If H^* exists, then for a set of covariates $\mathbf{X} = \mathbf{X}_T$:

$$Y_0^{(0)}(R')|\mathbf{X}_T = Y_0^{(0)}(R'')|\mathbf{X}_T \text{ for any } R', R'' \in H^*$$

Conditional Outcome within Generalization Interval



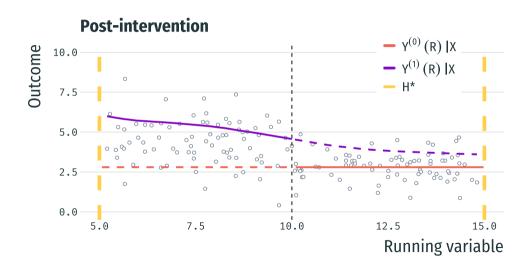
GRD: Main assumption for generalization to t=1

Assumption: Conditional time-invariance under control

$$Y_0^{(0)}(R|\mathbf{X}) = Y_1^{(0)}(R|\mathbf{X}) + \alpha, \quad \forall \ R \in H^*$$

- ullet No changes in unobserved confounders between t=0 and t=1
- Partially testable for Z = 0 in t = 1

GRD: Estimating effects away from the cutoff



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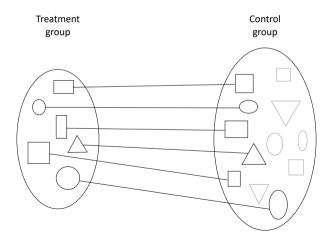
GRD in practice

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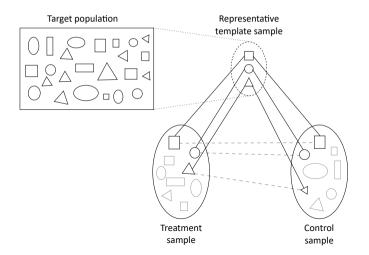
Overview: Representative Template Matching

Traditional Matching



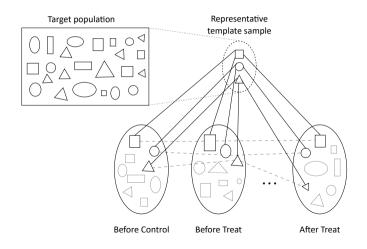
Overview: Representative Template Matching

Representative Template Matching for Two Groups

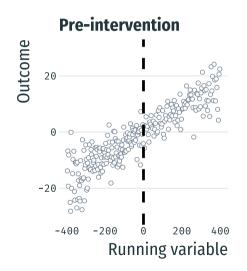


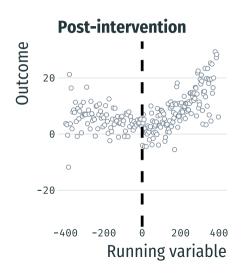
Overview: Representative Template Matching

Representative Template Matching for Diff-in-Diff

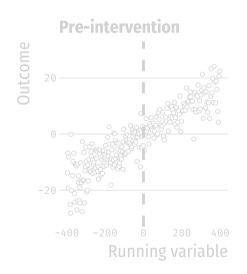


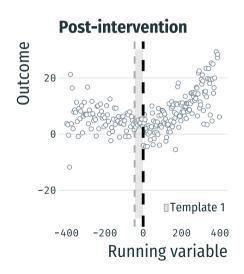
GRD: Start with two periods





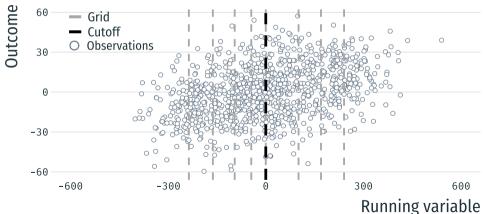
GRD: Select template sample from post-intervention

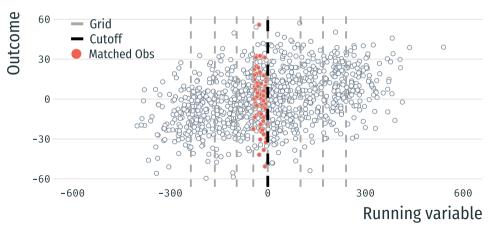


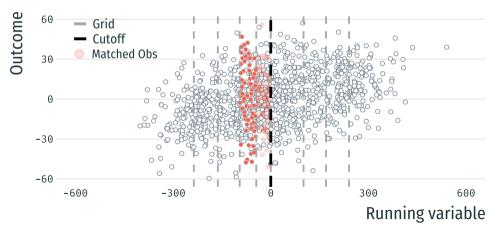


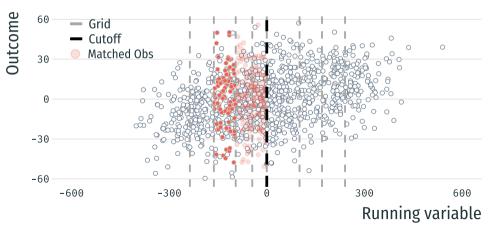
GRD: Divide pre-intervention into grid

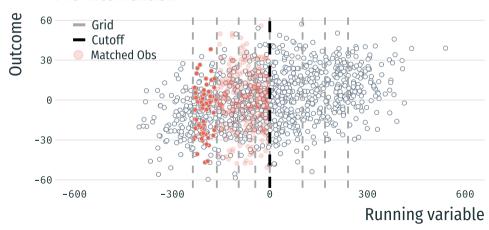






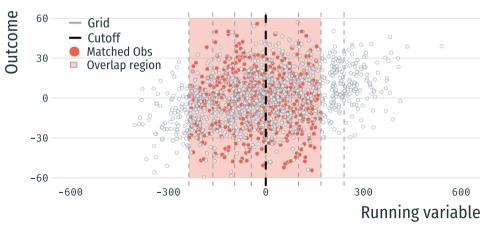




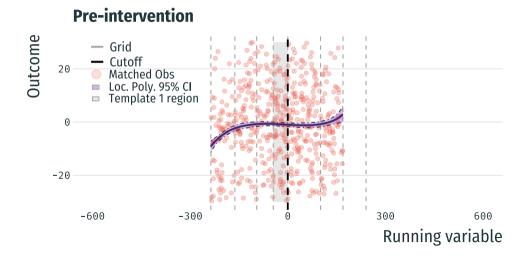


GRD: Explicit overlap region

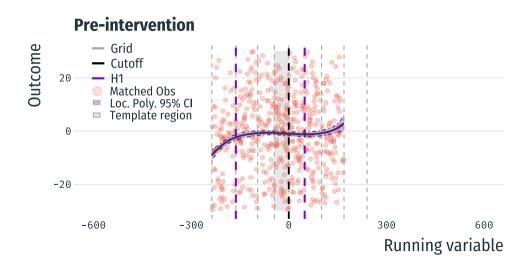




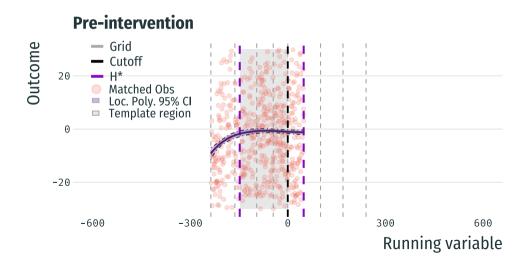
GRD: Estimate local polynomial on matched sample



GRD: Identify generalization interval H₁

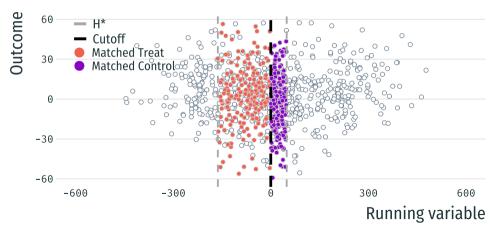


GRD: Repeat procedure until $H_j \subseteq T$



GRD: Match post-intervention period to the template

Post-intervention



GRD: ATT Estimation

Straightforward estimation given matched sample:

• E.g. paired t-test:

$$\hat{\tau}_{ATT} = \sum_{k=1}^{N} \frac{Y_{k(1)1} - Y_{k(0)1} - (Y_{k(1)0} - Y_{k(0)0})}{N} = \sum_{k=1}^{N} \frac{d_k}{N}$$

 $Y_{k(z)t}$: outcome within matched group k with treatment $z=\{0,1\}$ for period $t=\{0,1\}$

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Free Higher Education (FHE) in Chile

Higher education in Chile:

- Centralized admission system (deferred admission mechanism)
- Admission score: PSU score + GPA score + ranking score
- Before 2016: Scholarships + government-backed loans

Free higher education policy:

- Introduced in December 2015 (unanticipated)
- Eligibility: Lower 50% income distribution + admitted to eligible program

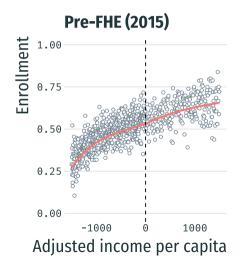
FHE: Research Question

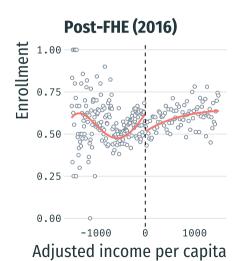
- Treatment: SE eligibility for FHE
- Two outcomes: Application to university and enrollment
 - ullet Lower-income students o financial constraints
 - Salience of policy
- Larger effects for students away from the cutoff?
 - Compare RD and GRD results

FHE: Data

- 3 Cohorts: 2014, 2015, and 2016. (~ 200,000 students)
- Rich baseline data: Demographic and socioeconomic data at student level, 10th (8th) grade standardized scores, school characteristics.
- **Application data:** Scores by subject, application, enrollment.

FHE: How does the RDs look like?



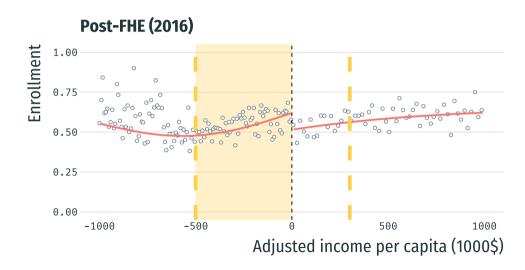


GRD for Free Higher Education

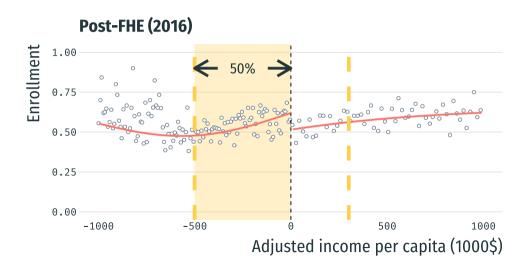
Steps for GRD:

- Select template size: N = 1,000
- 20 bins for grid
- MIP matching:
 - Restricted mean balance (0.05 SD):
 - Academic performance, school characteristics, demographic/socioeconomic variables.
 - Fine balance:
 - Gender, mother's and father's education (8 cat), PSU Language score (deciles), PSU math score (deciles), HS GPA (quintiles).
- Generalization interval: [-M\$500.3, M\$300.9]

For what population are we generalizing for?

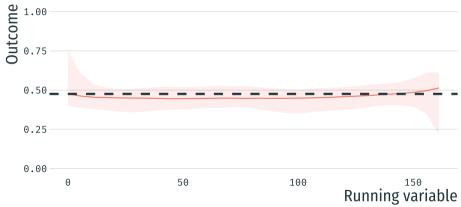


For what population are we generalizing for?



Local Polynomial for Control Outcome in t=1

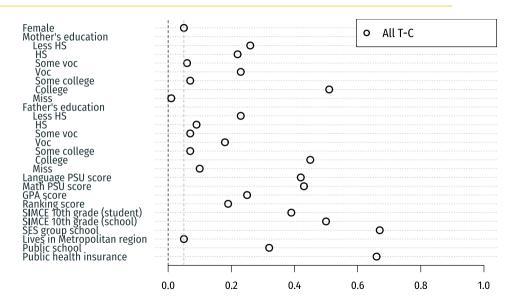




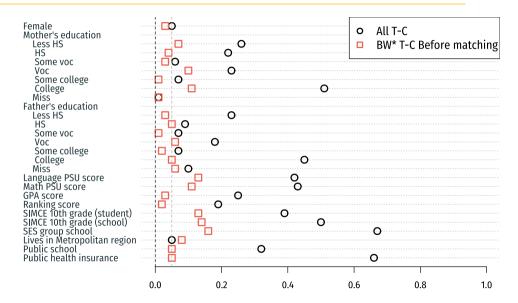
Comparison between treatment groups

	Treat group (All)	Treat group within H*
Female	0.55	0.55
Mother's education (years)	11.37	11.57
Father's education (years)	11.52	11.67
Language PSU score	504.08	510.20
Math PSU score	507.69	513.30
GPA score	554.88	558.11
Ranking score	579.84	583.11
SIMCE 10th grade (student)	274.90	276.95
SIMCE 10th grade (school)	266.91	268.52
SES group school	2.68	2.73
Lives in Metropolitan region	0.40	0.42
Public school	0.35	0.34
Public health insurance	0.82	0.79

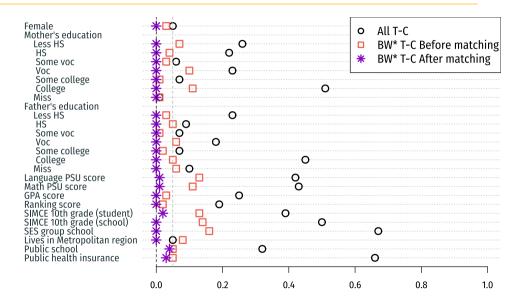
Balance: Entire sample



Balance: Within H^* before matching



Balance: Within H^* after matching



Effects of introduction of FHE: RD and GRD

	Robust RD results		GRD results	
	Application	Enrollment	Application	Enrollment
Effect	0.035	0.069**	0.052**	0.077***
	[-0.007, 0.077]	[0.026, 0.112]	[0.008, 0.096]	[0.029, 0.125]
Effective N Obs	6,588	6,458	2,000	2,000
Control Mean	0.606	0.515	0.568	0.472

Generalization interval [-M\$500, M\$301]

95% CI in brackets

Effects of introduction of FHE: Application

	Robust RD results		GRD results	
	Application	Enrollment	Application	Enrollment
Effect	0.035	0.069**	0.052**	0.077***
	[-0.007, 0.077]	[0.026, 0.112]	[0.008, 0.096]	[0.029, 0.125]
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95% CI in brackets

Effects of introduction of FHE: Enrollment

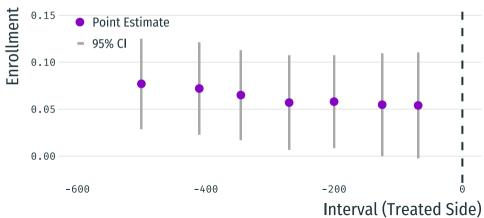
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Generalization interval [-M\$500, M\$301]

95% CI in brackets

How does the effect change with interval width?





Sensitivity Analysis to Hidden Bias

- Quantify bias of unobserved confounder to change qualitative results of the study
- Adaptation of Keele et al. (2019) sensitivity analysis for Diff-in-Diff.
- Moderately sensitive to hidden bias: $\Gamma=1.6$

$$\rightarrow \Pr(Z_{i1} = 1) = 0.62 \land \Pr(Z_{i1} = 0) = 0.38$$

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- GRD as a gradual approach for generalization (not "all or nothing")
- Use data to inform interval for generalization
- Use of matching to avoid extrapolation
- Limitations
 - More data: two periods
 - ullet Conditional time invariance assumption for t=1
- Multiple applications for DD-RD: e.g. geographic RDs.

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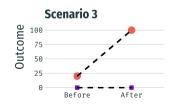
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Different Diff-in-Diff Scenarios







Treat Control

