

STA 235H - Regression Discontinuity Design

Fall 2023

McCombs School of Business, UT Austin

Announcements

- Midterm is next week
 - Please be on time!
 - Make sure HonorLock works without problems.
 - Check the course website for recommendations.
- Answer key for Homework 3 is posted on the course website.
- Review session for the midterm on Friday 2.00pm at UTC 3.102
- Remember that all submissions for JITTs are formal submissions for an assignment.
 - Use proper language (e.g. "nah" or "meh" are not actual words) and keep answers pertinent to the class.

Last class

- **Natural Experiments**
 - RCTs in the wild.
 - Importance of the context and checking balance.
- **Difference-in-Differences (DD):**
 - How we can use two wrong estimates to get a right one.
 - Assumptions behind DD.
 - *Make sure to check the JITT answer on the course website.*



Today



- **Regression Discontinuity Design (RDD):**
 - How can we use discontinuities to recover causal effects?
 - Assumptions behind RD designs.
- **Structure for this class:**
 - Start: Material + Examples
 - Finish: Exercise

Mind the gap

Another identification strategy

RCTs

Selection on observables

Natural experiments

Difference-in-Differences

Regression Discontinuity Designs

Tell me something about the readings/videos you had to watch for this week

Introduction to Regression Discontinuity Designs

Regression Discontinuity (RD) Designs

Arbitrary rules determine treatment assignment

E.g.: If you are above a threshold, you are assigned to treatment, and if you're below, you are not (or vice versa)

Geographic discontinuities

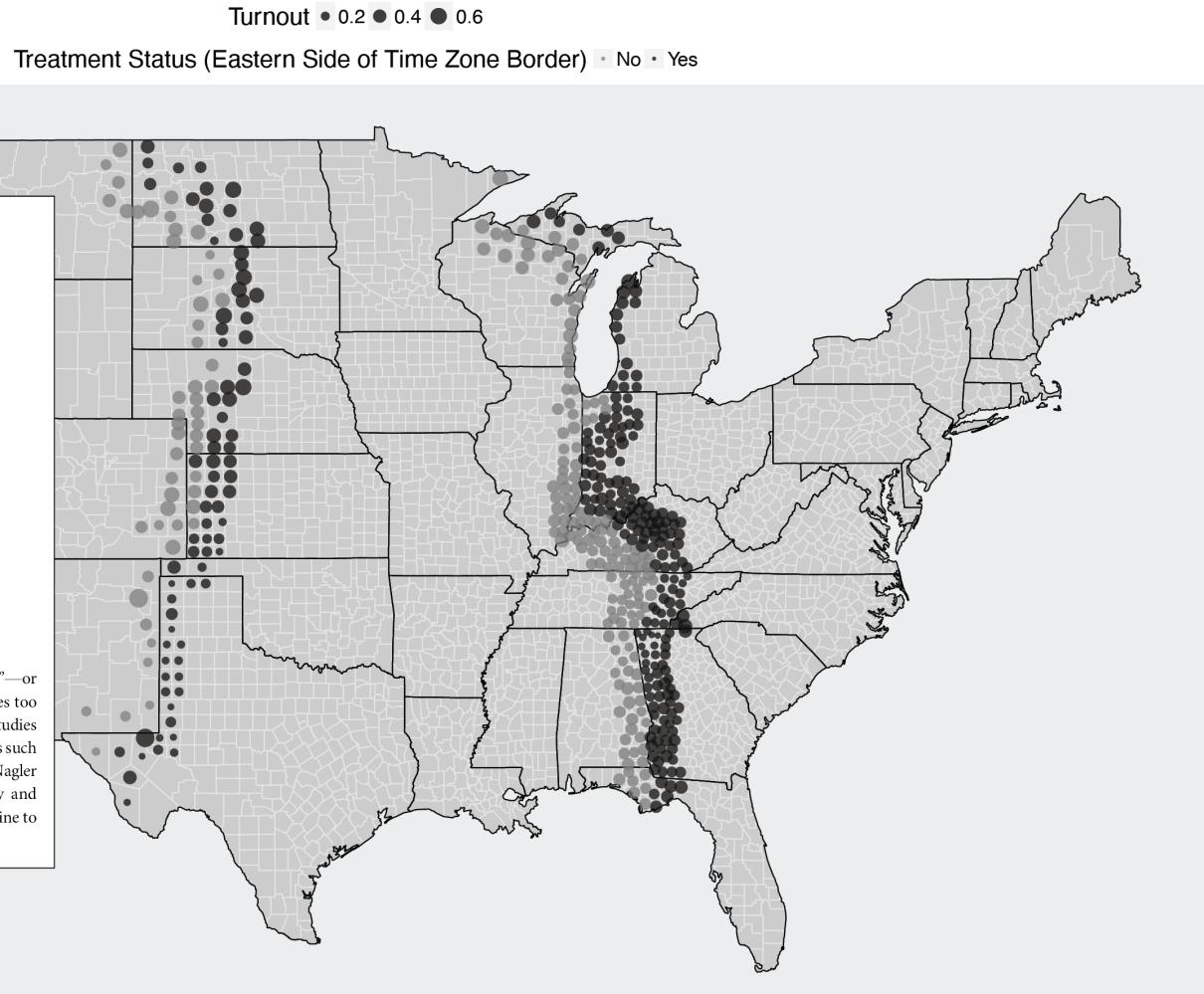
When Time Is of the Essence: A Natural Experiment on How Time Constraints Influence Elections

Jerome Schafer, Ludwig Maximilian University of Munich
John B. Holbein, University of Virginia

Foundational theories of voter turnout suggest that time is a key input in the voting decision, but we possess little causal evidence about how this resource affects electoral behavior. In this article, we use over two decades of elections data and a novel geographic regression discontinuity design that leverages US time zone boundaries. Our results show that exogenous shifts in time allocations have significant political consequences. Namely, we find that citizens are less likely to vote if they live on the eastern side of a time zone border. Time zones also exacerbate participatory inequality and push election results toward Republicans. Exploring potential mechanisms, we find suggestive evidence that these effects are the consequence of insufficient sleep and moderated by the convenience of voting. Regardless of the exact mechanisms, our results indicate that local differences in daily schedules affect how difficult it is to vote and shape the composition of the electorate.

Although in recent years the administrative barriers to voting have declined in many democracies (Blais 2010), many eligible citizens still fail to vote. In the United States, about 40% of registered voters do not participate in presidential elections, with abstention rates soaring as high as 60% in midterms and 70% in local elections (Hajnal and Trounstine 2016). Moreover, rates of political participation have remained stubbornly low among vulnerable groups—

vote, many nonvoters report “not having enough time”—or a close derivative (e.g., “I’m too busy” or “[Voting] takes too long”; Pew Research Center 2006). Moreover, recent studies suggest that levels of turnout may be shaped by time costs such as how long it takes to register to vote (Leighley and Nagler 2013), to find and travel to a polling location (Brady and McNulty 2011; Dyck and Gimpel 2005), and to wait in line to vote (Pettigrew 2016).



Time discontinuities

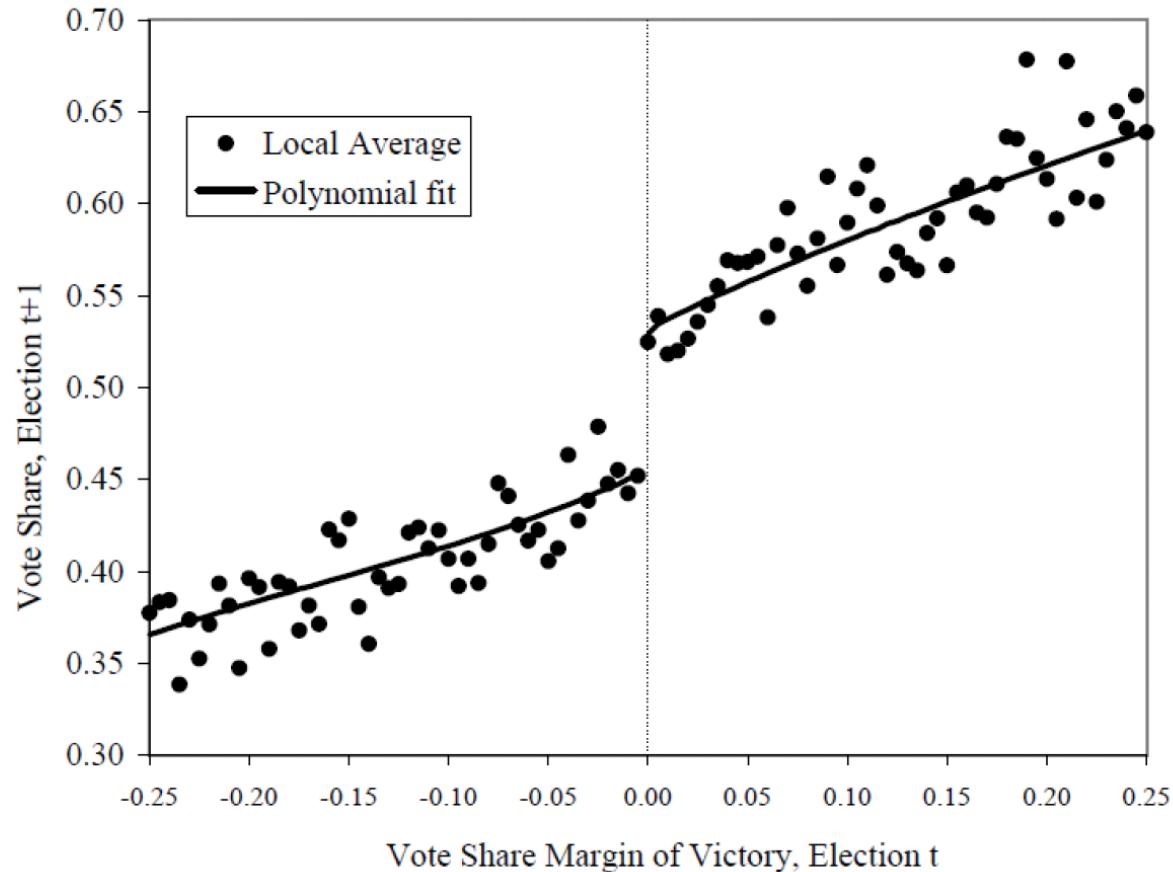
After Midnight: A Regression Discontinuity Design in Length of Postpartum Hospital Stays[†]

By DOUGLAS ALMOND AND JOSEPH J. DOYLE JR.*

Estimates of moral hazard in health insurance markets can be confounded by adverse selection. This paper considers a plausibly exogenous source of variation in insurance coverage for childbirth in California. We find that additional health insurance coverage induces substantial extensions in length of hospital stay for mother and newborn. However, remaining in the hospital longer has no effect on readmissions or mortality, and the estimates are precise. Our results suggest that for uncomplicated births, minimum insurance mandates incur substantial costs without detectable health benefits. (JEL D82, G22, I12, I18, J13)

Voting discontinuities

Figure IVa: Democrat Party's Vote Share in Election $t+1$, by Margin of Victory in Election t : local averages and parametric fit



You can find discontinuities
everywhere!

Key Terms

Running/ forcing variable

Index or measure that determines eligibility

Cutoff/ cutpoint/ threshold

Number that formally assigns you to a program or treatment

Let's look at an example

Hypothetical tutoring program

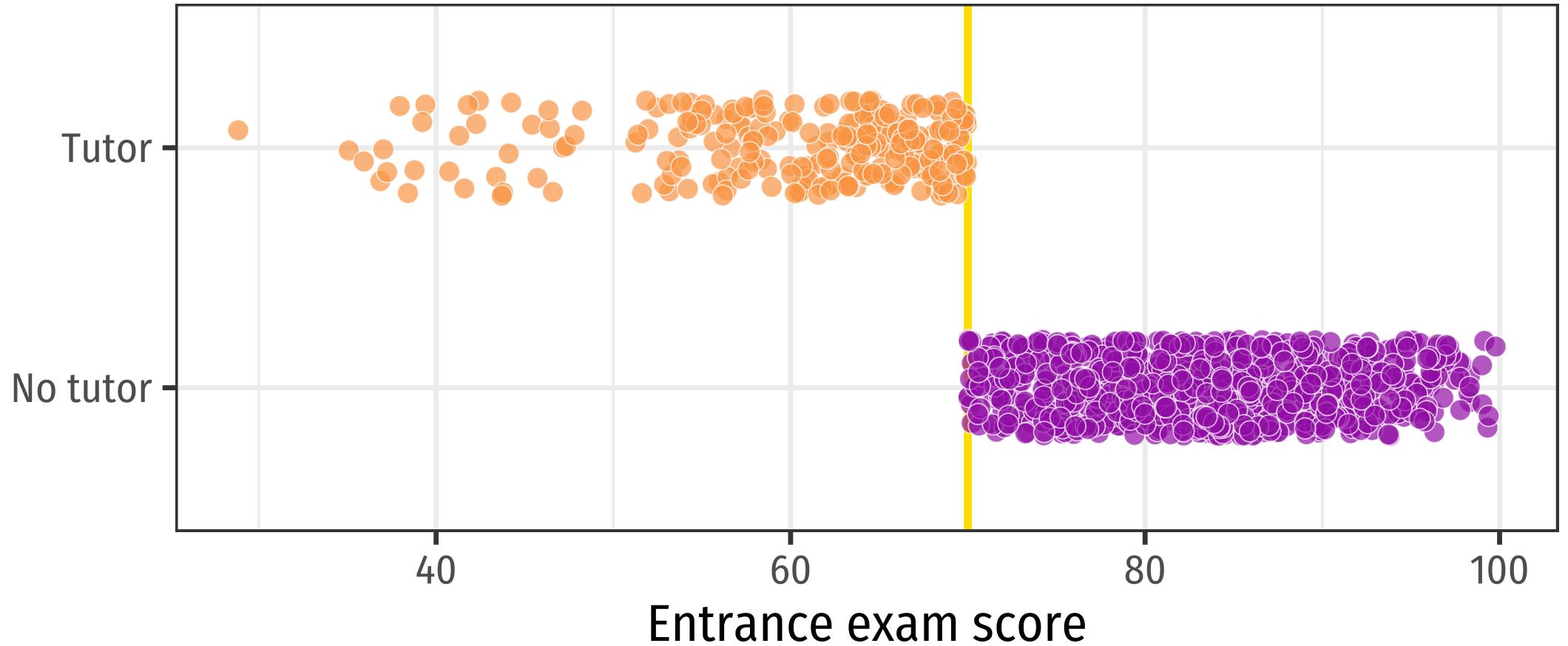
Students take an entrance exam

**Those who score 70 or lower
get a free tutor for the year**

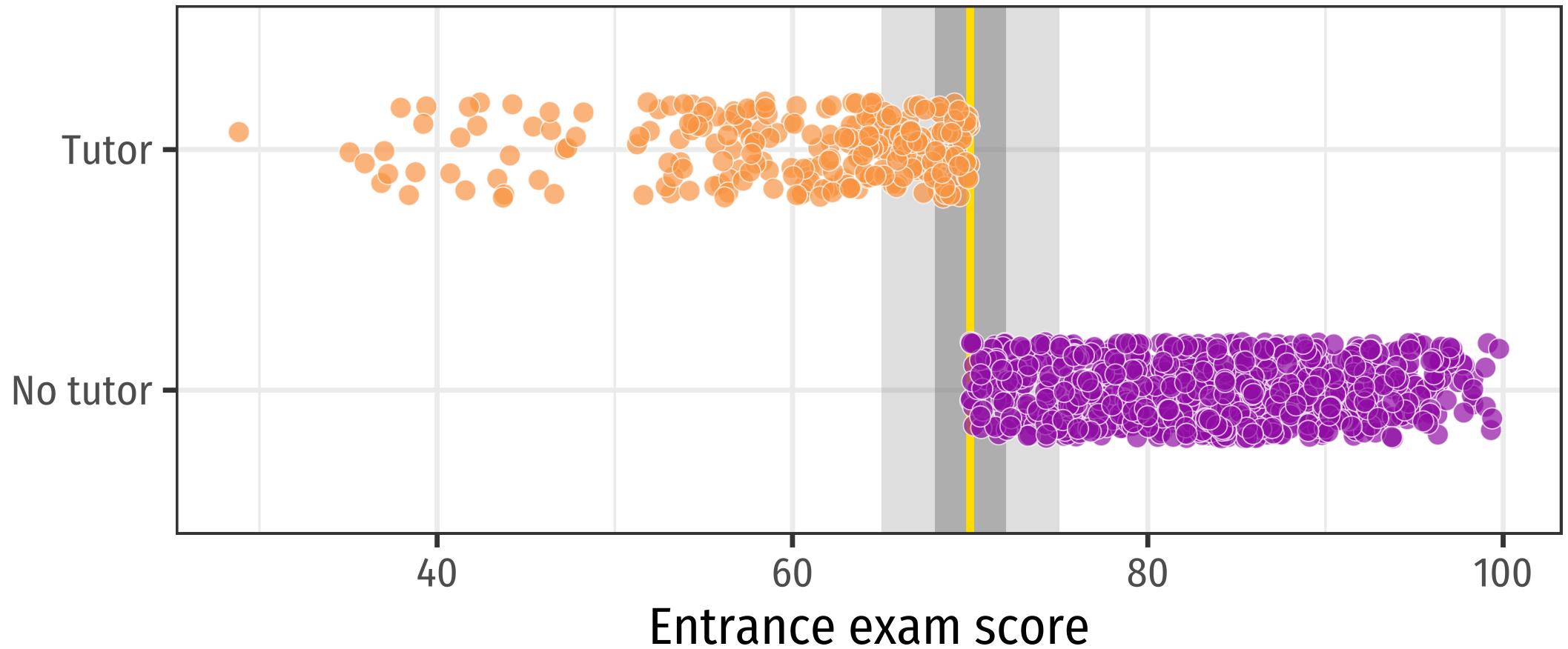
**Students then take an exit exam
at the end of the year**

Can we compare students who got
a tutor vs those that did not to
capture the effect of having a
tutor on their exit exam?

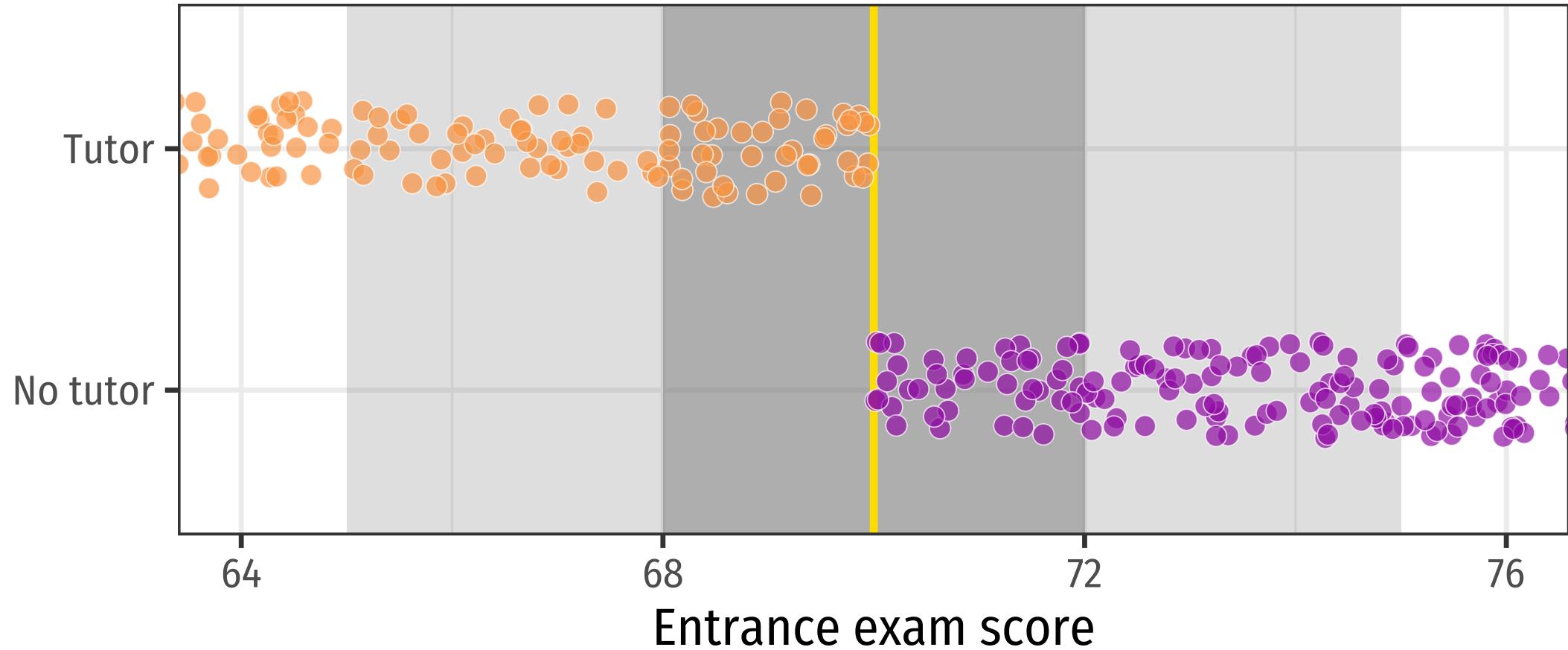
Assignment based on entrance score



Let's look at the area close to the cutoff



Let's get closer



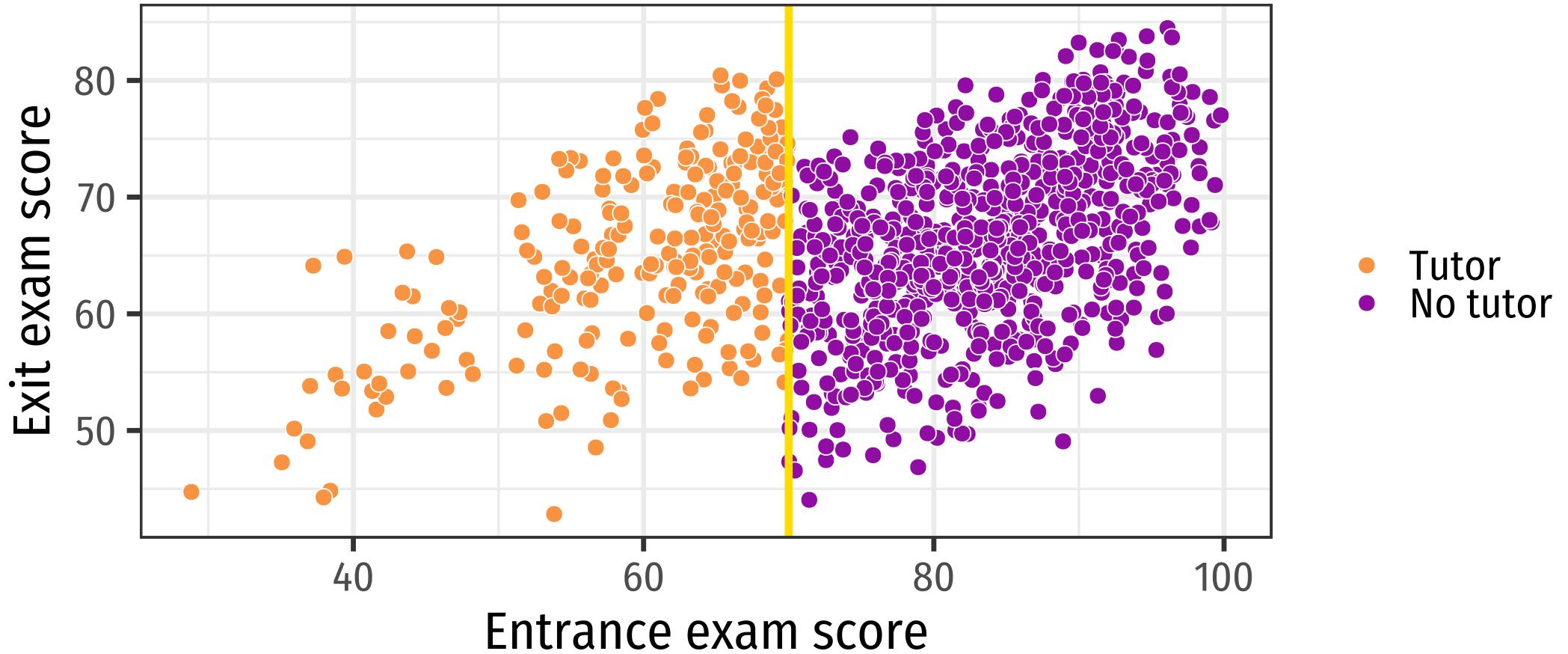
Causal inference intuition

Observations right before and after the threshold are
essentially the same

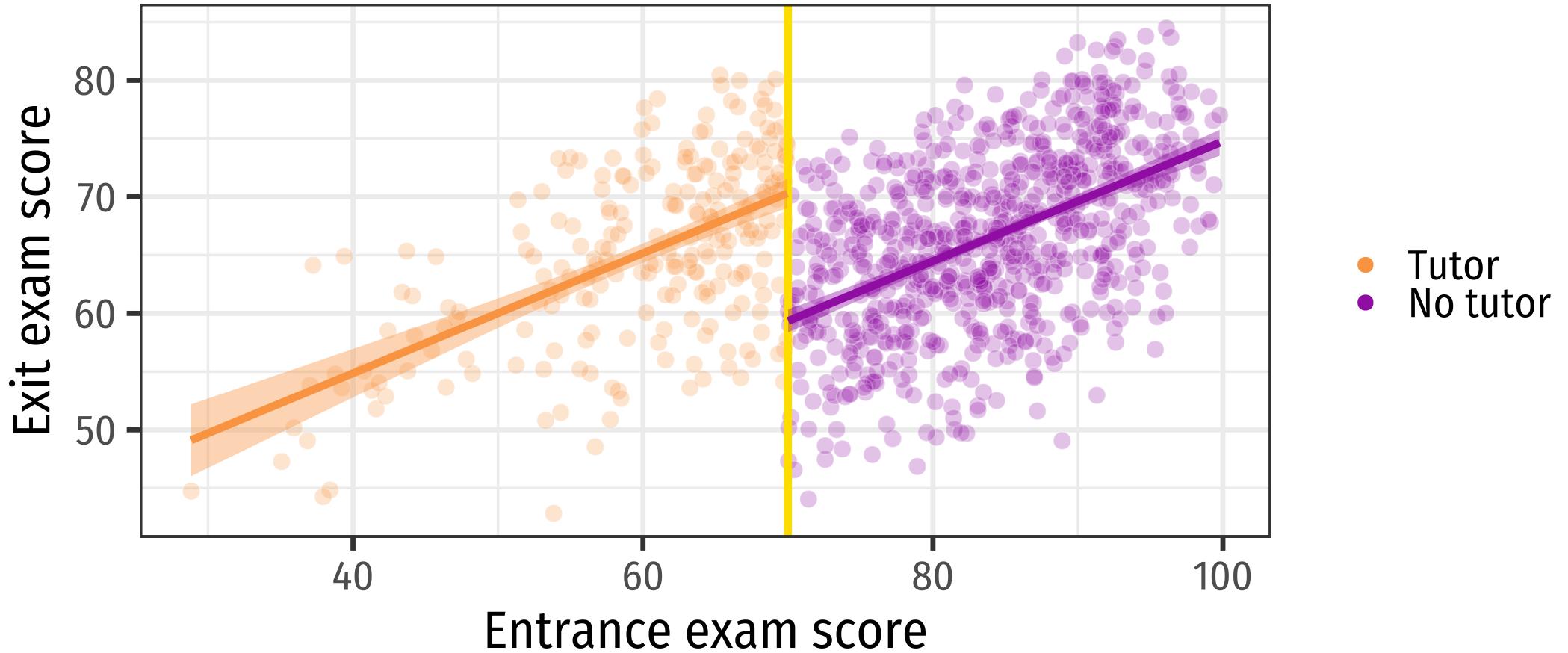
Pseudo treatment and control groups!

Compare outcomes right at the cutoff

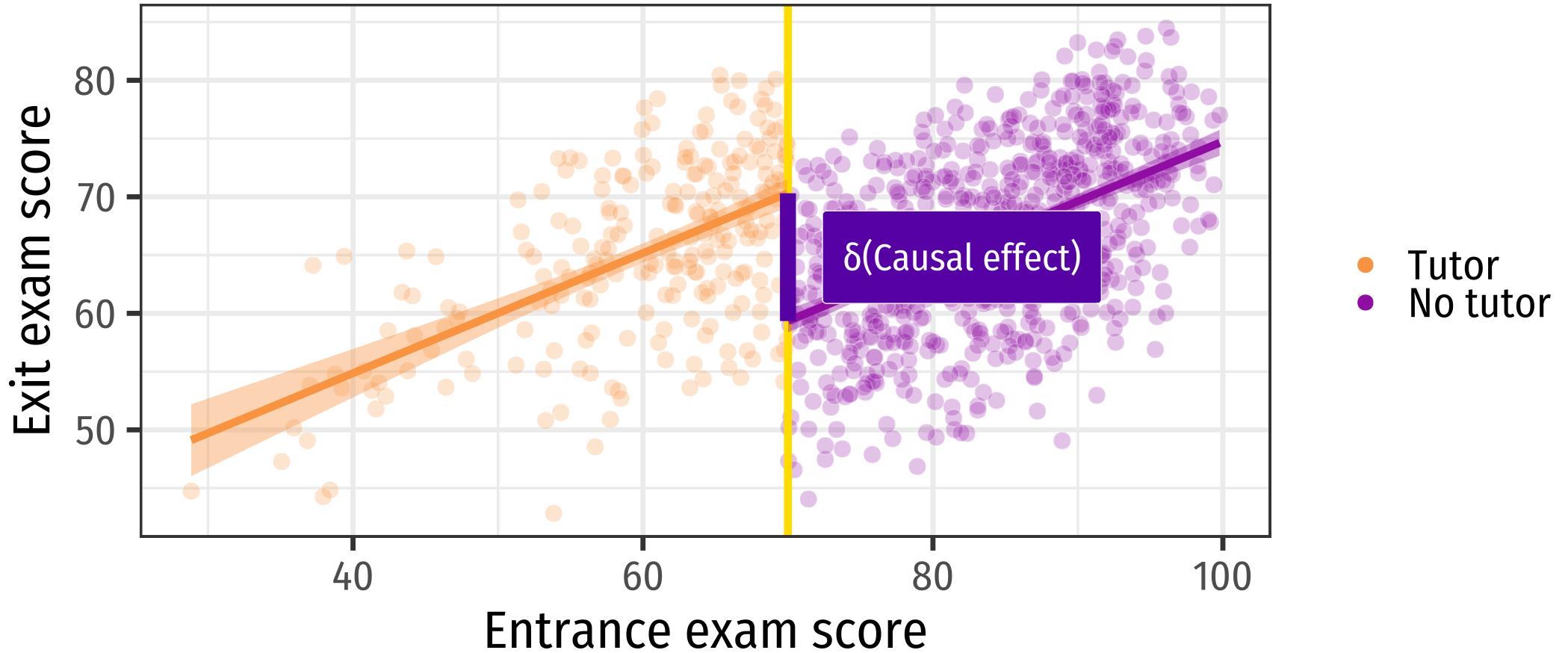
Exit exam results according to running variable



Fit a regression at the right and left side of the cutoff



Fit a regression at the right and left side of the cutoff



What population within my sample am I comparing?

My estimand is the
Local Average Treatment Effect
(LATE) for units at $R=c$

Is that what we want?

Probably not ideal, there may not be *any* units with $R=c$

... but better LATE than nothing!

Conditions required for identification

- Threshold rule **exists** and cutoff point is **known**
 - There needs to be a discontinuity in treatment assignment, and we need to know where it happens!
- The running variable R_i is **continuous** near c .
 - If we are working with a coarse variable, this might not work.
- **Key assumption:**

Continuity of $E[Y(1)|R]$ and $E[Y(0)|R]$ at $R=c$

That's the math-y way to say that the only thing that changes right at the cutoff is the treatment assignment!

Estimation in practice

How do we actually estimate an RDD?

- The simplest way to do this is to fit a regression using **an interaction of the treatment variable and the running variable**:

$$Y = \beta_0 + \beta_1(R - c) + \beta_2I[R > c] + \beta_3(R - c)I[R > c] + \varepsilon$$

How do we actually estimate an RDD?

- The simplest way to do this is to fit a regression using **an interaction of the treatment variable and the running variable**:

$$Y = \beta_0 + \beta_1 \underbrace{(R - c)}_{\text{Distance to the cutoff}} + \beta_2 \underbrace{\mathbf{I}[R > c]}_{\text{Treatment}} + \beta_3 \underbrace{(R - c)}_{\text{Distance to the cutoff}} + \underbrace{\mathbf{I}[R > c]}_{\text{Treatment}} + \varepsilon$$

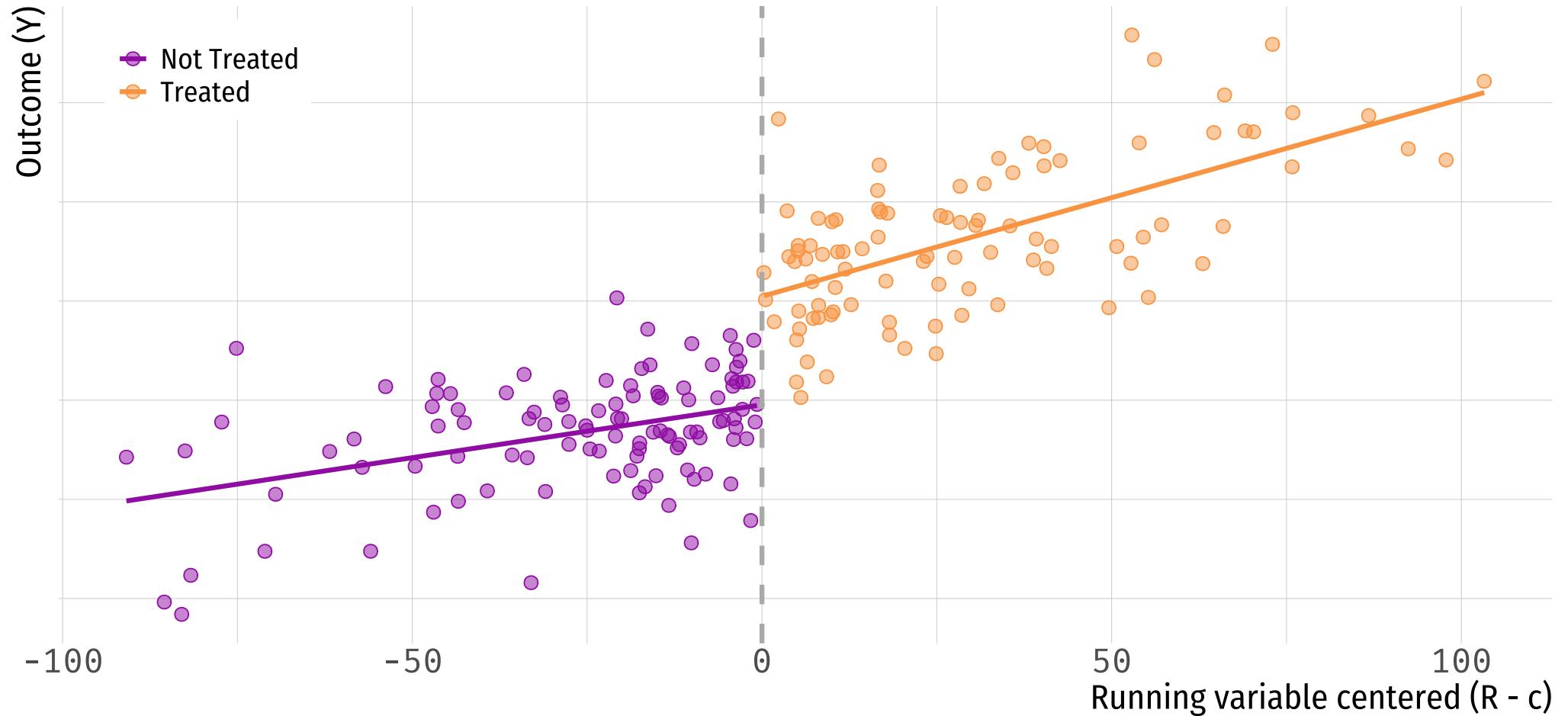
- We can simplify this with new notation:

$$Y_i = \beta_0 + \beta_1 R' + \beta_2 Treat + \beta_3 R' \times Treat$$

where *Treat* is a binary treatment variable and *R'* is the running variable centered around the cutoff

Can you identify these parameters in a plot?

Let's identify coefficients



Steps for analyzing an RDD

1) Check that there is a discontinuity in **treatment assignment** at the cutoff.

2) Check that **covariates change smoothly** across the threshold.

- You can think about this as the equivalent of a *balance table*.

3) Run the **regression discontinuity design model**.

- Interpret this effect *for individuals right at the cutoff*.

Let's see an example

Discount and sales

- You are managing a retail store and notice that sales are low in the mornings, so you want to improve those numbers.
- You decide to give the first 1,000 customers that show up **10% off**



Discounts and sales: Data available

- We have the following dataset, with time of arrival for customers, a few covariates, and the outcome of interest (sales)

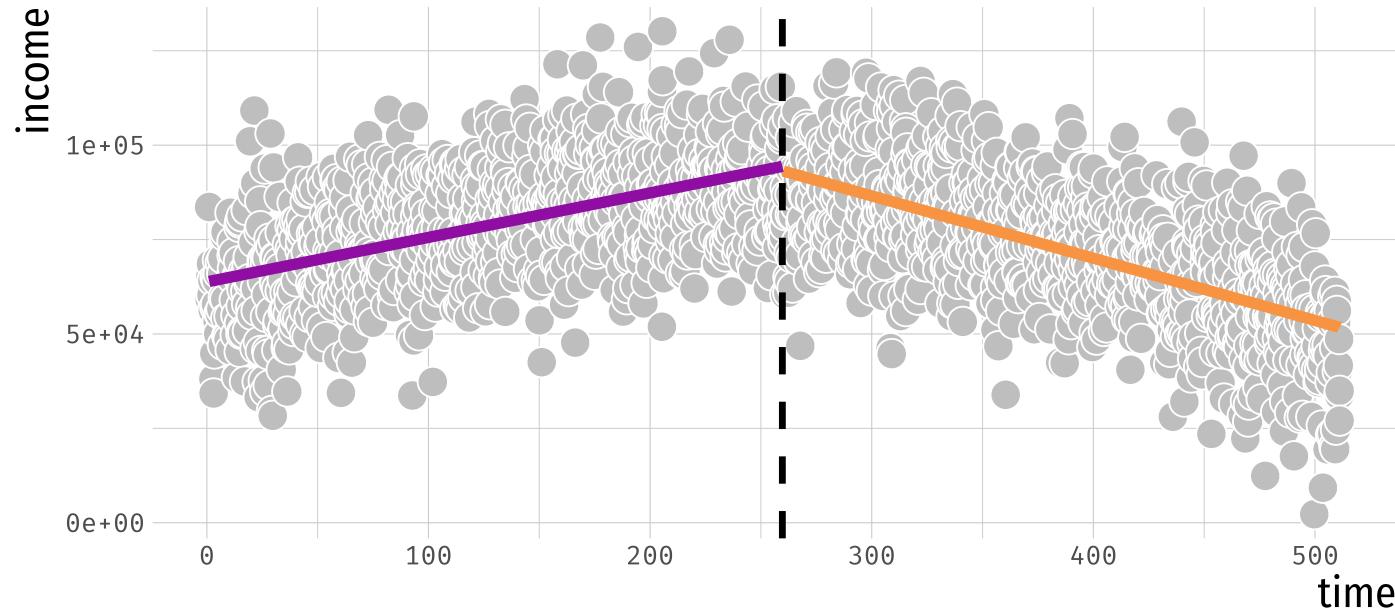
```
sales = read.csv("https://raw.githubusercontent.com/maibennett/sta235/main/exampleSite/content/Class%2010%20-%20Data.csv")
head(sales)
```

```
##   id      time age female  income    sales treat
## 1  1 1.050000 49      1 83622.63 231.0863     1
## 2  2 1.203883 50      1 67265.61 215.6148     1
## 3  3 1.332719 46      1 59151.46 200.5003     1
## 4  4 1.608881 49      0 67308.17 203.9145     1
## 5  5 1.637072 50      1 65420.20 217.6668     1
## 6  6 1.871347 47      0 68566.67 222.0601     1
```

Discounts and sales: Can we use an RDD?

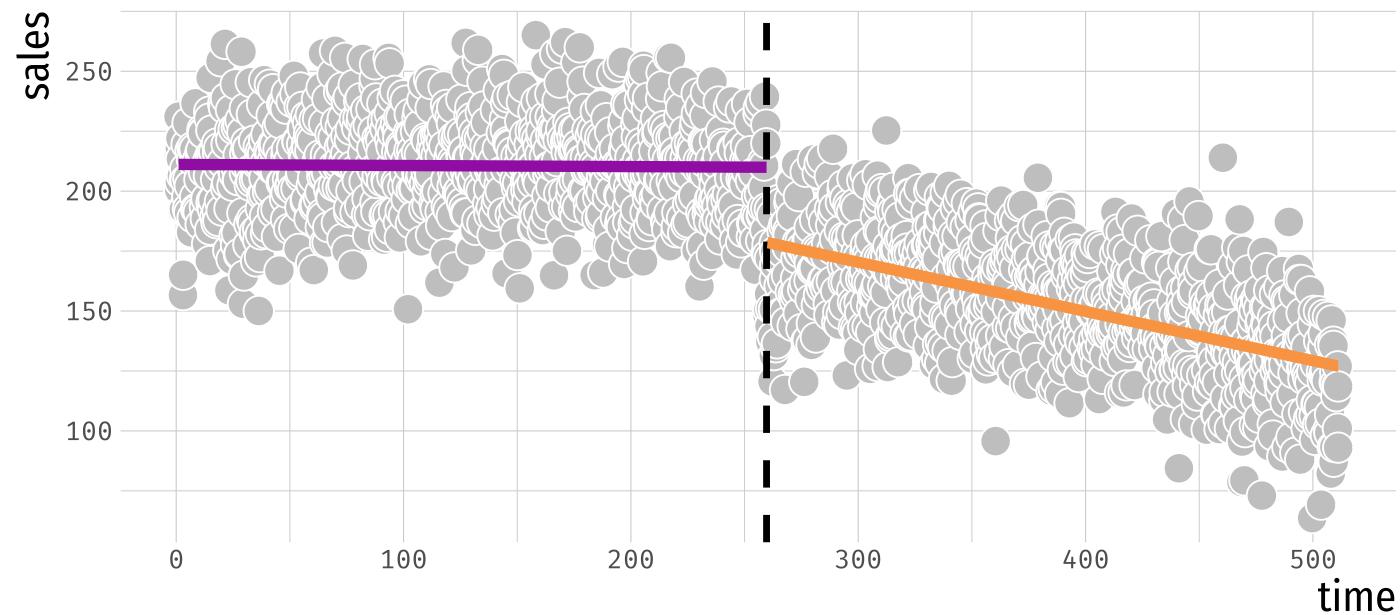
- In RDD, we need to check that there are **no unbalances in covariates across the threshold**.

```
sales = sales %>% mutate(dist = c-time)  
lm(income ~ dist*treat, data = sales)
```



RDD on sales using linear models

```
lm(sales ~ dist*treat, data = sales)
```



RDD on sales using linear models

```
summary(lm(sales ~ dist*treat, data = sales))

##
## Call:
## lm(formula = sales ~ dist * treat, data = sales)
##
## Residuals:
##     Min      1Q  Median      3Q     Max 
## -65.738 -13.940   0.051  13.538  76.515 
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 178.640954   1.300314 137.38 <2e-16 ***
## dist         0.205355   0.008882  23.12 <2e-16 ***
## treat        31.333952   1.842338  17.01 <2e-16 ***
## dist:treat   -0.200845   0.012438 -16.15 <2e-16 ***
## ---    
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## 
## Residual standard error: 20.52 on 1996 degrees of freedom
## Multiple R-squared:  0.6939,    Adjusted R-squared:  0.6934 
## F-statistic: 1508 on 3 and 1996 DF,  p-value: < 2.2e-16
```

On average, providing a 10% discount increases sales by \$31.3 for the 1,000 customer, compared to not having a discount

We can be more flexible

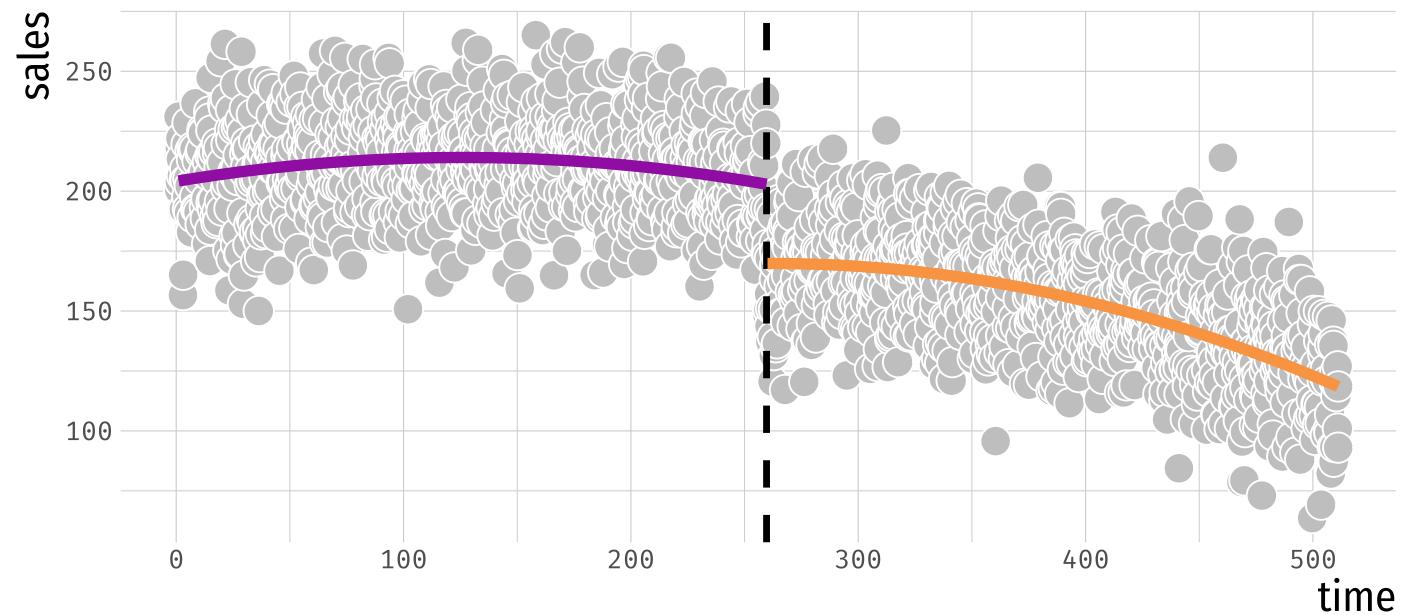
- The previous example just included linear terms, but you can also be more flexible:

$$Y = \beta_0 + \beta_1 f(R') + \beta_2 Treat + \beta_3 f(R') \times Treat + \varepsilon$$

- Where f is any function you want.

What happens if we fit a quadratic model?

```
lm(sales ~ dist*treat + treat*I(dist^2), data = sales)
```



What happens if we fit a quadratic model?

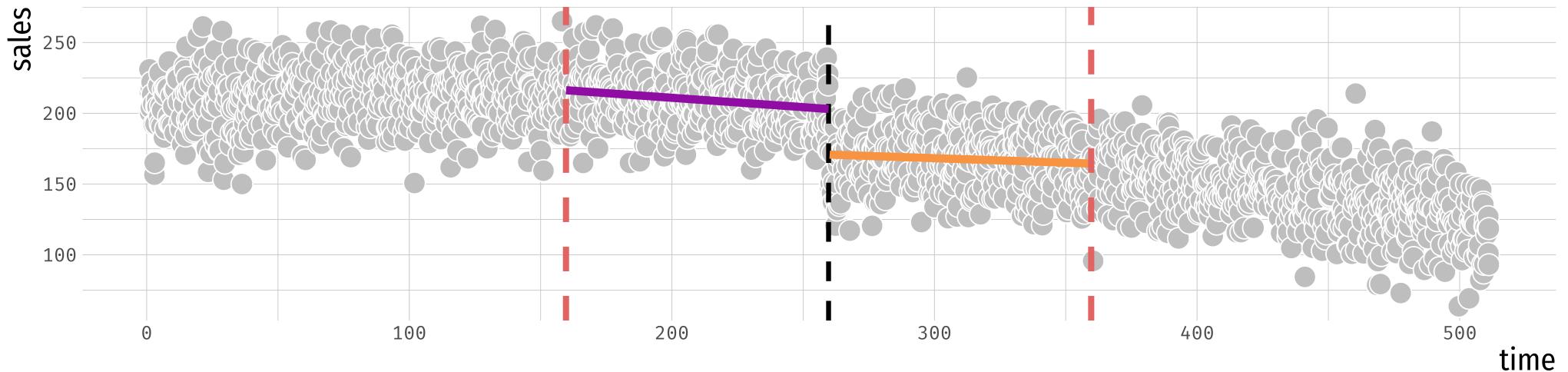
```
summary(lm(sales ~ dist*treat + treat*I(dist^2), data = sales))
```

```
##  
## Call:  
## lm(formula = sales ~ dist * treat + treat * I(dist^2), data = sales)  
##  
## Residuals:  
##     Min      1Q  Median      3Q     Max  
## -66.090 -13.979   0.239  13.154  76.656  
##  
## Coefficients:  
##                 Estimate Std. Error t value Pr(>|t|)  
## (Intercept) 1.698e+02 1.937e+00 87.665 < 2e-16 ***  
## dist        -4.302e-03 3.556e-02 -0.121 0.903725  
## treat        3.308e+01 2.747e+00 12.041 < 2e-16 ***  
## I(dist^2)   -8.288e-04 1.363e-04 -6.083 1.41e-09 ***  
## dist:treat   1.713e-01 4.964e-02  3.452 0.000569 ***  
## treat:I(dist^2) 2.034e-04 1.877e-04  1.084 0.278554  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 20.23 on 1994 degrees of freedom  
## Multiple R-squared:  0.7029,    Adjusted R-squared:  0.7021  
## F-statistic: 943.5 on 5 and 1994 DF,  p-value: < 2.2e-16
```

On average, providing a 10% discount increases sales by \$33.1 for the 1,000 customer, compared to not having a discount

What happens if we only look at observations close to c?

```
sales_close = sales %>% filter(dist>-100 & dist<100)  
lm(sales ~ dist*treat, data = sales_close)
```



How do they compare?

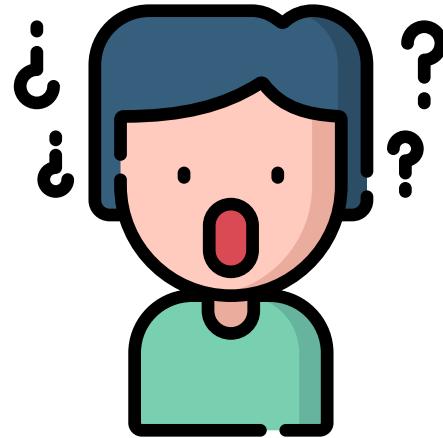
```
summary(lm(sales ~ dist*treat, data = sales_close))

##
## Call:
## lm(formula = sales ~ dist * treat, data = sales_close)
##
## Residuals:
##     Min      1Q  Median      3Q     Max 
## -53.241 -14.764   0.268  12.938  57.811 
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 170.84457  2.05528  83.125 <2e-16 ***
## dist        0.06345  0.03542   1.791  0.0736 .  
## treat       32.21243  2.93614  10.971 <2e-16 ***
## dist:treat  0.06909  0.05047   1.369  0.1714    
## ---      
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## 
## Residual standard error: 20.25 on 782 degrees of freedom
## Multiple R-squared:  0.5261,    Adjusted R-squared:  0.5243 
## F-statistic: 289.4 on 3 and 782 DF,  p-value: < 2.2e-16
```

On average, providing a 10% discount increases sales by \$32.2 for the 1,000 customer, compared to not having a discount

Potential problems

- There are **many potential problems** with the previous examples:
 - Which polynomial function should we choose? Linear, quadratic, other?
 - What bandwidth should we choose? Whole sample? [-100,100]?



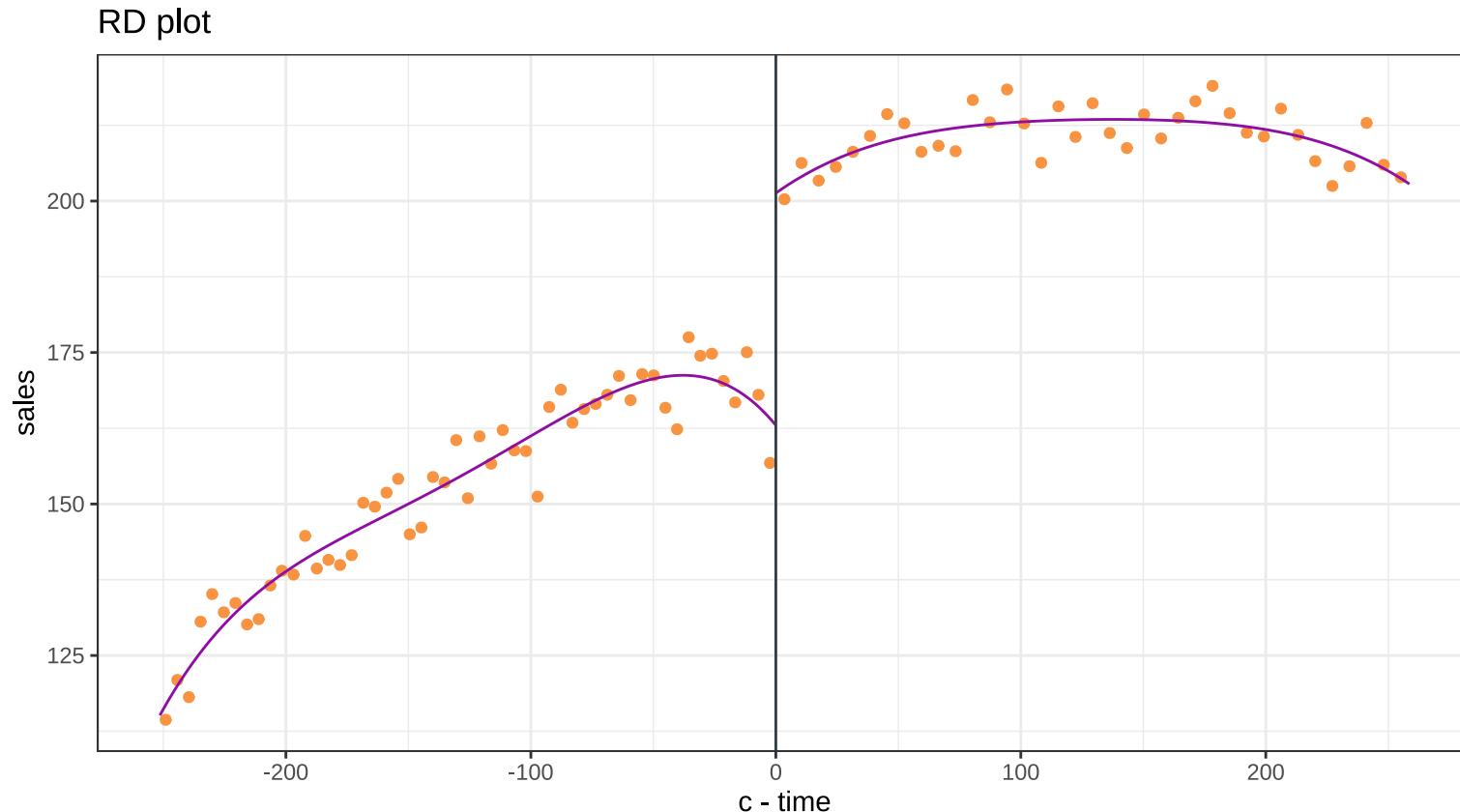
- There are some ways to address these concerns.

Package `rdrobust`

- Robust Regression Discontinuity introduced by Cattaneo, Calonico, Farrell & Titiunik (2014).
- Use of **local polynomial** for fit.
- **Data-driven optimal bandwidth** (bias vs variance).
- `rdrobust`: Estimation of LATE and opt. bandwidth
- `rdplot`: Plotting RD with nonparametric local polynomial.

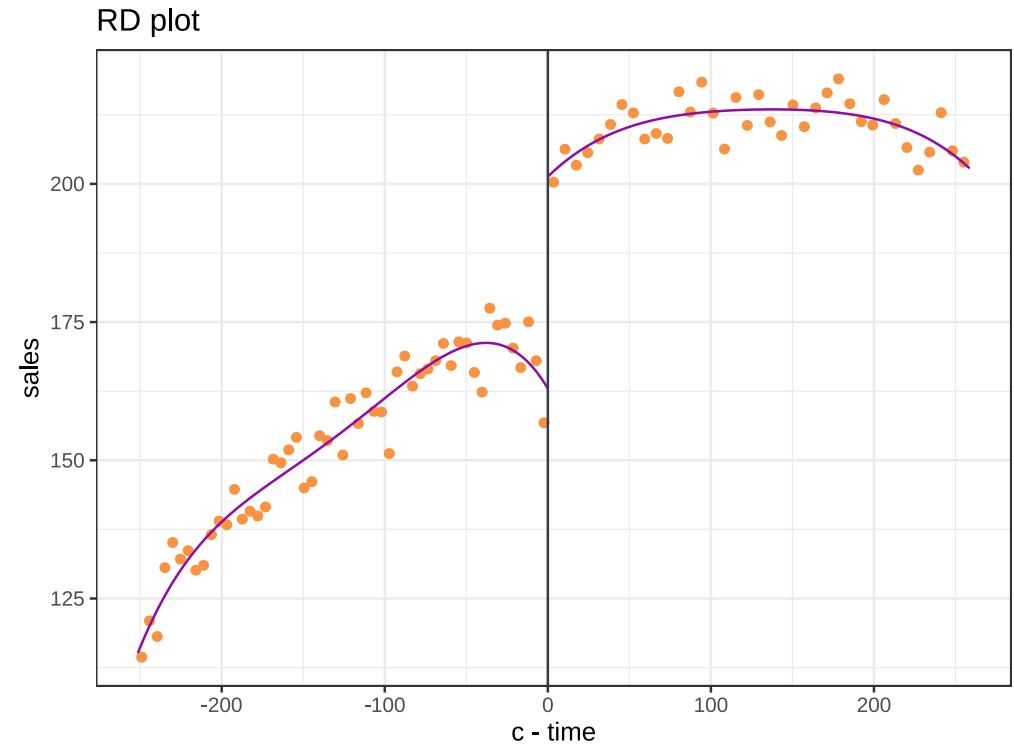
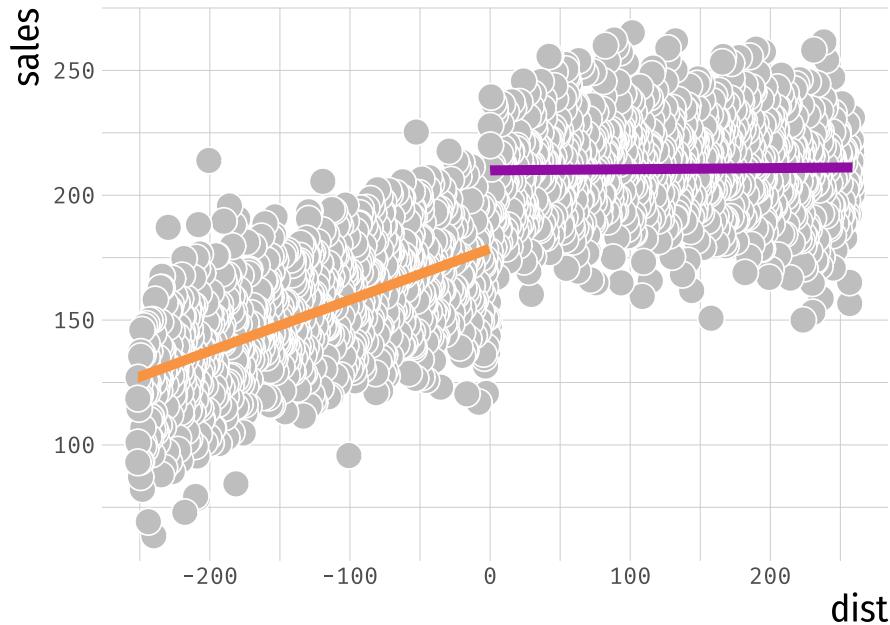
Let's compare with previous parametric results

```
rdplot(y = sales$sales, x = sales$dist, c = 0,  
       title = "RD plot", x.label = "c - time", y.label = "sales")
```



Let's compare with previous parametric results

```
rdplot(y = sales$sales, x = sales$dist, c = 0,  
       title = "RD plot", x.label = "c - time", y.label = "sales")
```



Let's compare with previous parametric results

```
summary(rdrobust(y = sales$sales, x = sales$dist, c = 0))

## Sharp RD estimates using local polynomial regression.
##
## Number of Obs.          2000
## BW type                 mserd
## Kernel                  Triangular
## VCE method               NN
##
## Number of Obs.          1000      1000
## Eff. Number of Obs.     209       200
## Order est. (p)          1         1
## Order bias (q)          2         2
## BW est. (h)              53.578    53.578
## BW bias (b)              87.522    87.522
## rho (h/b)                0.612    0.612
## Unique Obs.             1000      1000
##
## =====
##      Method   Coef. Std. Err.      z   P>|z|   [ 95% C.I. ]
## =====
## Conventional   37.772    4.370    8.644    0.000  [29.208 , 46.336]
## Robust        -         -       7.684    0.000  [29.124 , 49.070]
## =====
```

Your turn!

Takeaway points

- RD designs are **great** for causal inference!
 - Strong internal validity
 - Number of robustness checks
- **Limited** external validity.
- Make sure to check your data:
 - Discontinuity in treatment assignment
 - Smoothness of covariates



References

- Angrist, J. and S. Pischke. (2015). "Mastering Metrics". *Chapter 4*.
- Social Science Research Institute at Duke University. (2015). "Regression Discontinuity: Looking at People on the Edge: Causal Inference Bootcamp"