

Ex 1: Design a combinational circuit with three inputs and one output.

- (a) The output is 1 when the binary value of the inputs is less than 3. The output is 0 otherwise.
- (b) The output is 1 when the binary value of the inputs is an even number.

Ex 2: Design a combinational circuit with three inputs, x , y , and z , and three outputs, A , B , and C . When the binary input is 0, 1, 2, or 3, the binary output is one greater than the input. When the binary input is 4, 5, 6, or 7, the binary output is two less than the input.

Ex 3: A majority circuit is a combinational circuit whose output is equal to 1 if the input variables have more 1's than 0's. The output is 0 otherwise. Design a 3-input majority circuit by finding the circuit's truth table, Boolean equation, and a logic diagram.

Ex 4: Design a combinational circuit that converts a four-bit Gray code to a bit four-binary number.

Ex 5: Design a code converter that converts a decimal digit from

- (a) The 8, 4, -2, -1 code to BCD
- (b) The 8, 4, -2, -1 code to Gray code.

Ex 6: Design a four-bit combinational circuit 2's complementer. (The output generates the 2's complement of the input binary number.) Show that the circuit can be constructed with exclusive-OR gates. Can you predict what the output functions are for a five-bit 2's complementer?

Ex:1

A	B	C	(a) Y_1	(b) Y_2
0	0	0	1	1
0	0	1	1	0
0	1	0	1	1
0	1	1	0	0
1	0	0	0	1
1	0	1	0	0
1	1	0	0	1
1	1	1	0	0

(a)

A	BC			
	00	01	11	10
0	1	1	0	1
1	0	0	0	0

$$Y_1 = \bar{A}\bar{B} + \bar{A}\bar{C} = \bar{A}(\bar{B} + \bar{C})$$

(b)

A	BC			
	00	01	11	10
0	1	0	0	1
1	1	0	0	1

$$Y_2 = \bar{C}$$

Ex:2

x	y	z	A	B	C
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	1	0
1	0	1	0	1	1
1	1	0	1	0	0
1	1	1	1	0	1

A

$x\backslash yz$	00	01	11	10
0	0	0	1	0
1	0	0	1	1

$$A = yz + xy = \underline{y(x+z)}$$

B

$x\backslash yz$	00	01	11	10
0	0	1	0	1
1	1	1	0	0

$$\begin{aligned} B &= \bar{x}y\bar{z} + x\bar{y} + \bar{y}z \\ &= y\bar{x}\bar{z} + \bar{y}(x+z) \\ &= y(\bar{x}+z) + \bar{y}(x+z) = \underline{y \oplus (x+z)} \end{aligned}$$

C

$x\backslash yz$	00	01	11	10
0	1	0	0	1
1	0	1	1	0

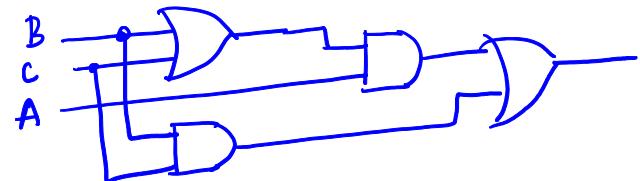
$$C = \bar{x}\bar{z} + xz = \underline{\bar{x} \oplus z}$$

Ex: 3

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

$x\backslash BC$	00	01	11	10
0	0	0	1	0
1	0	1	1	1

$$Y = AC + AB + BC = A(B+c) + BC$$



Ex: 4

A	B	C	D	y_3	y_2	y_1	y_0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	1	0	0	1	0
0	0	1	0	0	0	1	1
0	1	1	0	0	1	0	0
0	1	1	1	0	1	1	0
0	1	0	1	0	1	1	1
0	1	0	0	0	1	0	0
1	1	0	0	1	0	0	0
1	1	0	1	1	0	0	1
1	1	1	1	1	0	1	0
1	1	1	0	1	0	1	1

1	0	1	0	1	1	0	0
1	0	1	1	1	1	0	1
1	0	0	1	1	1	1	0
1	0	0	0	1	1	1	1

$\overline{Y_3}$

AB	CD	00	01	11	10
00	00	0	0	0	0
01	00	0	0	0	0
11	00	1	1	1	1
10	00	1	1	1	1

$\underline{Y_3} = A$

$\overline{Y_2}$

AB	CD	00	01	11	10
00	00	0	0	0	0
01	00	0	0	0	0
11	00	0	0	0	0
10	00	1	1	1	1

$$\begin{aligned} Y_2 &= \bar{A}B + A\bar{B} \\ &= \underline{\underline{A \oplus B}} \end{aligned}$$

$\overline{Y_1}$

AB	CD	00	01	11	10
00	00	0	0	1	1
01	00	1	1	0	0
11	00	0	0	1	1
10	00	1	1	0	0

$$\begin{aligned} Y_1 &= \bar{A}\bar{B}C + \bar{A}B\bar{C} \\ &\quad + ABC + A\bar{B}\bar{C} \\ &= \bar{A}(\bar{B}C + B\bar{C}) \\ &\quad + A(BC + \bar{B}\bar{C}) \\ &= \bar{A}(B \oplus C) + A(\bar{B} \oplus C) \\ &= \underline{\underline{A \oplus B \oplus C}} \end{aligned}$$

$\overline{Y_0}$

AB	CD	00	01	11	10
00	00	0	1	0	1
01	00	1	0	1	0
11	00	0	1	0	1
10	00	1	0	1	0

$$\begin{aligned} Y_0 &= \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + AB\bar{C}\bar{D} + ABC\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} \\ &= \bar{A}\bar{B}(\bar{C}\bar{D} + C\bar{D}) + \bar{A}B(\bar{C}\bar{D} + C\bar{D}) + AB(\bar{C}\bar{D} + C\bar{D}) + A\bar{B}(\bar{C}\bar{D} + CD) \\ &= (\bar{C}\bar{D} + C\bar{D})(\bar{A}\bar{B} + AB) + (\bar{C}\bar{D} + CD)(\bar{A}B + A\bar{B}) \\ &= (C \oplus D)(\overline{A \oplus B}) + (\overline{C \oplus D})(A \oplus B) \\ &= \underline{\underline{A \oplus B \oplus C \oplus D}} \end{aligned}$$

Ex: 5

(a)

8 4 -2 -1				BCD				Gray			
A	B	C	D	γ_3	γ_2	γ_1	γ_0	γ_3	γ_2	γ_1	γ_0
0	0	0	0	0	0	0	0	0	0	0	0
0	1	1	1	0	0	0	1	0	0	0	1
0	1	1	0	0	0	1	0	0	0	1	1

0	1	0	1	0	0	1	1	0	0	1	0
0	1	0	0	0	1	0	0	0	1	1	1
1	0	1	1	1	0	1	0	0	1	0	1
1	0	1	0	0	0	1	1	0	0	1	0
1	0	0	1	0	1	1	1	1	0	1	0
1	0	0	0	1	0	0	0	1	1	0	0
1	1	1	1	1	1	0	0	1	1	0	1

y_3

AB	CD	00	01	11	10
00	0	X	X	X	
01	0	0	0	0	
11	X	X	1	X	
10	1	0	0	0	

$$y_3 = AB + A\bar{C}\bar{D}$$

y_2

AB	CD	00	01	11	10
00	0	X		X	X
01	1	0	0	0	
11	X	X	0	X	
10	0	1	1	1	

$$\begin{aligned}
 y_2 &= \bar{B}D + \bar{B}C + B\bar{C}\bar{D} \\
 &= \bar{B}(C+D) + B(C+D) \\
 &= \underline{\underline{B \oplus (C+D)}}
 \end{aligned}$$

y_1

AB	CD	00	01	11	10
00	0	X		X	X
01	0	1	0	1	
11	X	X	0	X	
10	0	1	0	1	

$$\underline{\underline{y_1 = \bar{C}D + C\bar{D} = C \oplus D}}$$

y_0

AB	CD	00	01	11	10
00	0	X	X	X	
01	0	1	1	0	
11	X	X	1	X	
10	0	1	1	0	

$$\underline{\underline{y_0 = D}}$$

b)

		CD	00	01	11	10
		AB	00	01	11	10
Y ₃	AB	00	0	X	X	X
		01	0	0	0	0
Y ₂	AB	CD	00	01	11	10
Y ₁	AB	CD	00	01	11	10
Y ₀	AB	CD	00	01	11	10

$$Y_3 = AB + A\bar{C}\bar{D} = A[B + \overline{(C+D)}]$$

$$\begin{aligned} Y_2 &= A + B\bar{C}\bar{D} \\ &= A + B(\overline{C+D}) \end{aligned}$$

$$\begin{aligned} Y_1 &= B\bar{C} + B\bar{D} + \bar{B}CD \\ &= B(\bar{C} + \bar{D}) + \bar{B}CD \\ &= B\bar{C}\bar{D} + \bar{B}CD \\ &= B(\overline{C+D}) \end{aligned}$$

$$\underline{Y_0 = C}$$

Ex: 6

A	B	C	D	γ_3	γ_2	γ_1	γ_0
0	0	0	0	0	0	0	0
0	0	0	1	1	1	1	1
0	0	1	0	1	1	1	0
0	0	1	1	1	1	0	1
0	1	0	0	1	1	0	0
0	1	0	1	1	0	1	1
0	1	1	0	1	0	1	0
0	1	1	1	1	0	0	1
1	0	0	0	1	0	0	0
1	0	0	1	0	1	1	1
1	0	1	0	0	1	1	0
1	0	1	1	0	1	0	1
1	1	0	0	0	1	0	0
1	1	0	1	0	0	1	1
1	1	1	0	0	0	1	0
1	1	1	1	0	0	0	1

γ_3

AB \ CD	00	01	11	10
00	0	1	1	1
01	1	1	1	1
11	0	0	0	0
10	1	0	0	0

$$\begin{aligned}
 \gamma_3 &= \bar{A}B + \bar{A}D + \bar{A}C + A\bar{B}\bar{C}\bar{D} \\
 &= \bar{A}(B+C+D) + A(\bar{B}+\bar{C}+\bar{D}) \\
 &= \underline{\underline{A \oplus (B+C+D)}}
 \end{aligned}$$

γ_2

AB \ CD	00	01	11	10
00	0	1	1	1
01	1	0	0	0
11	0	0	0	0
10	0	1	1	1

$$\begin{aligned}
 \gamma_2 &= B\bar{C}\bar{D} + \bar{B}D + \bar{B}C \\
 &= B(\bar{C}+D) + \bar{B}(C+D) \\
 &= \underline{\underline{B \oplus (C+D)}}
 \end{aligned}$$

γ_1	AB	CD	00	01	11	10
	00		0	1	0	1
	01		0	1	0	1
	11		0	1	0	1
	10		0	1	0	1

$$\begin{aligned} \gamma_1 &= \overline{C}D + C\overline{D} \\ &= \underline{\underline{C \oplus D}} \end{aligned}$$

γ_0	AB	CD	00	01	11	10
	00		0	1	1	0
	01		0	1	1	0
	11		0	1	1	0
	10		0	1	1	0

$$\underline{\underline{\gamma_0 = D}}$$

