

Test Case Design Methods- White Box

What subset of all possible test cases has the highest probability of detecting the most errors?

References

- [4] – Chapter 1, 4
- [5] – Chapter 17
- [6] – Chapter 10, 11

Content

- Overview
- Basis Path Testing
- Control-flow / Coverage Testing
- Loop Testing
- Data Flow Testing
- Limitation

Overview

- White box testing involves looking at the structure of the code
- Why spend time and energy worrying about (and testing) logical minutiae when we might better expend effort ensuring that program requirements have been met?
 - Logic errors and incorrect assumptions are inversely proportional to the probability that a program path will be executed
 - We often believe that a logical path is not likely to be executed when, in fact, it may be executed on a regular basis
 - Typographical errors are random.

Overview

- The general white box testing process:
 - The (Software Under Test) SUT's implementation is analyzed.
 - Paths through the SUT are identified.
 - Inputs are chosen to cause the SUT to execute selected paths. This is called path sensitization. Expected results for those inputs are determined.
 - The tests are run.
 - Actual outputs are compared with the expected outputs.
 - A determination is made as to the proper functioning of the SUT

Overview

- White box testing is more than code testing—it is path testing
 - Generally, the paths that are tested are within a module (Unit Testing, Module Testing)
 - Test paths between modules within subsystems, between subsystems within systems, and even between entire systems?

Content

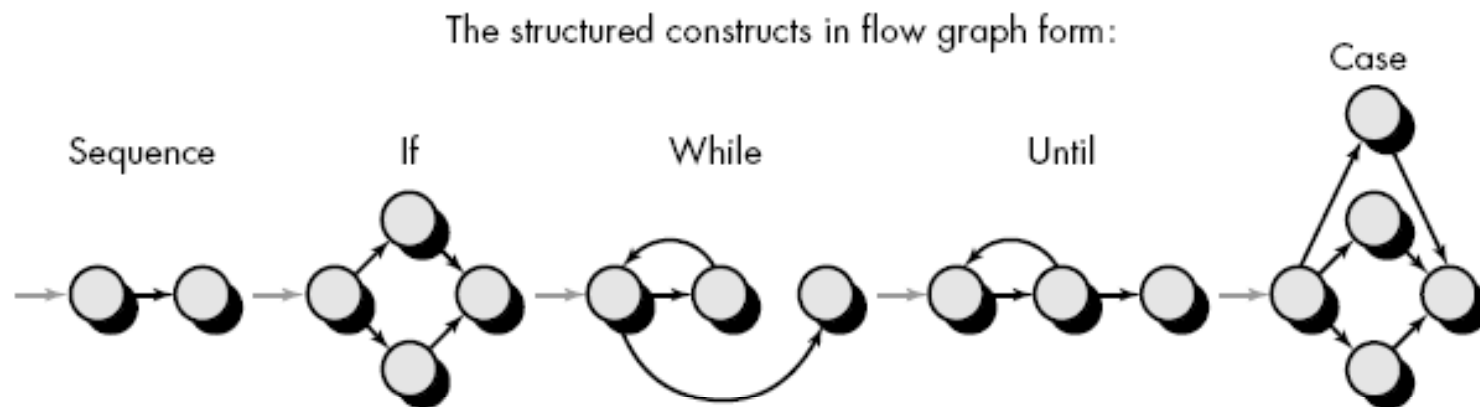
- Overview
- Basis Path Testing
- Control-flow / Coverage Testing
- Loop Testing
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- Limitation

Basis Path Testing

- Flow Graph Notation
- Cyclomatic Complexity
- Deriving Test Cases
- Graph Matrices

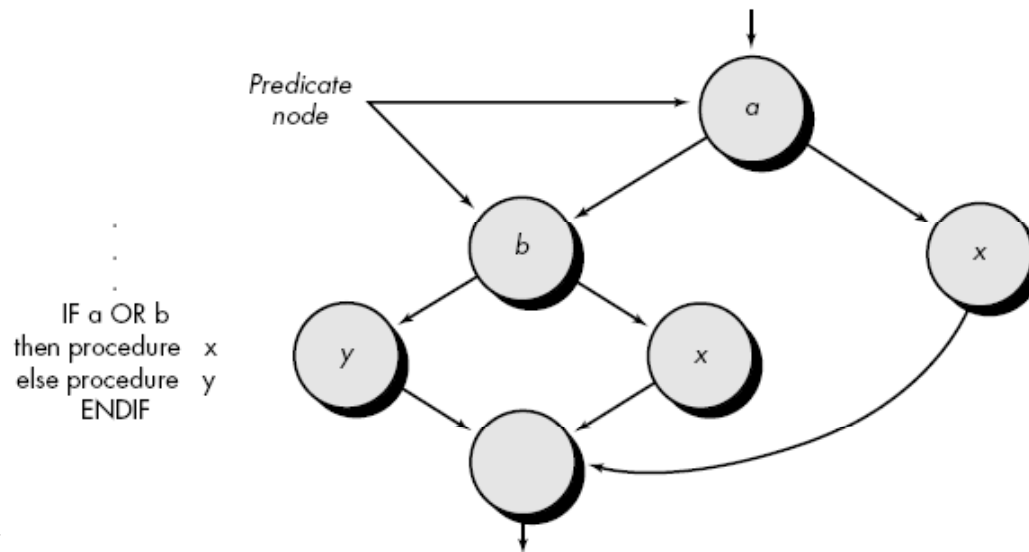
Flow Graph Notation

- Flow graph (or program graph):
 - A simple notation for the representation of control flow.
 - Depicts logical control flow using the following notation



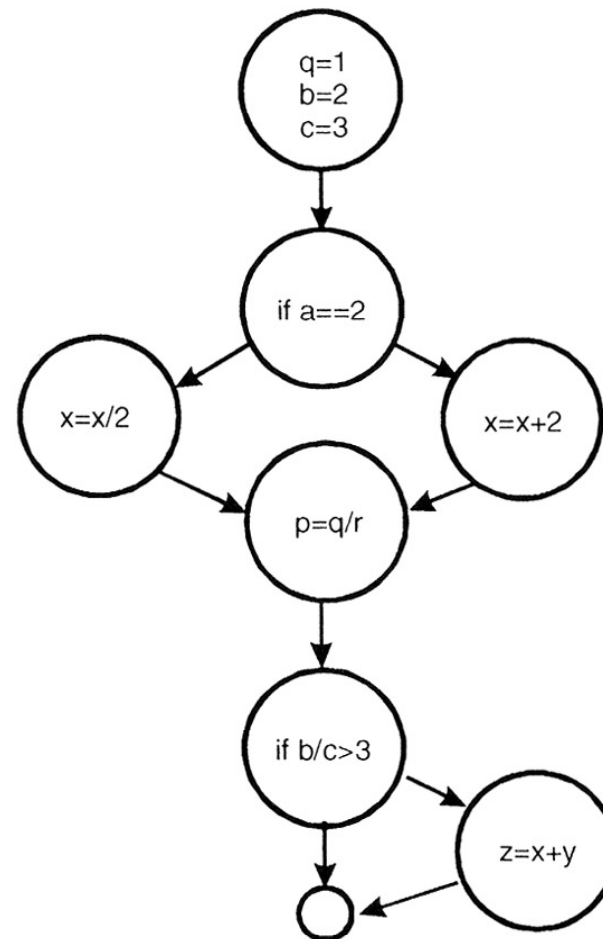
Flow Graph Notation

- Flow graph (or program graph):
 - A compound condition occurs when one or more Boolean operators (logical OR, AND, NAND, NOR) is present in a conditional statement.
 - Each node that contains a condition is called a predicate node and is characterized by two or more edges emanating from it



Flow Graph Notation

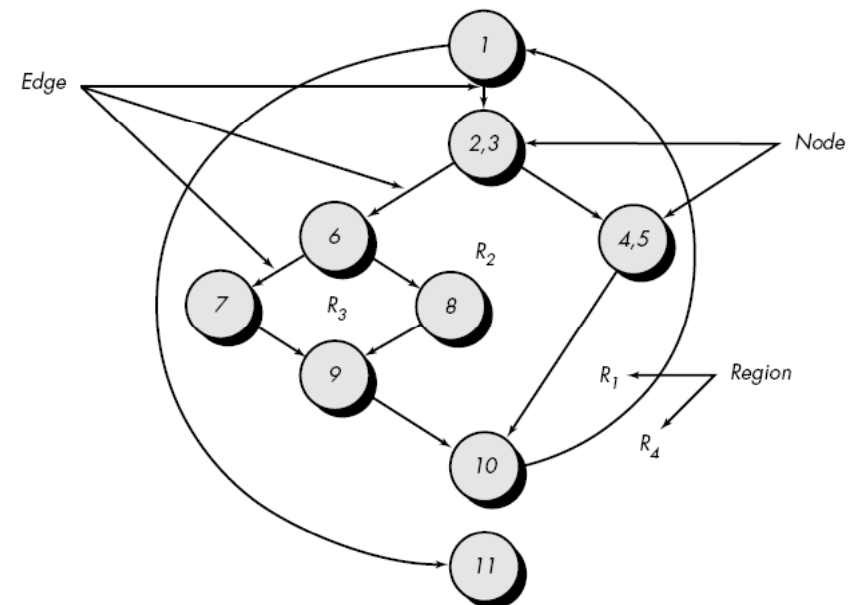
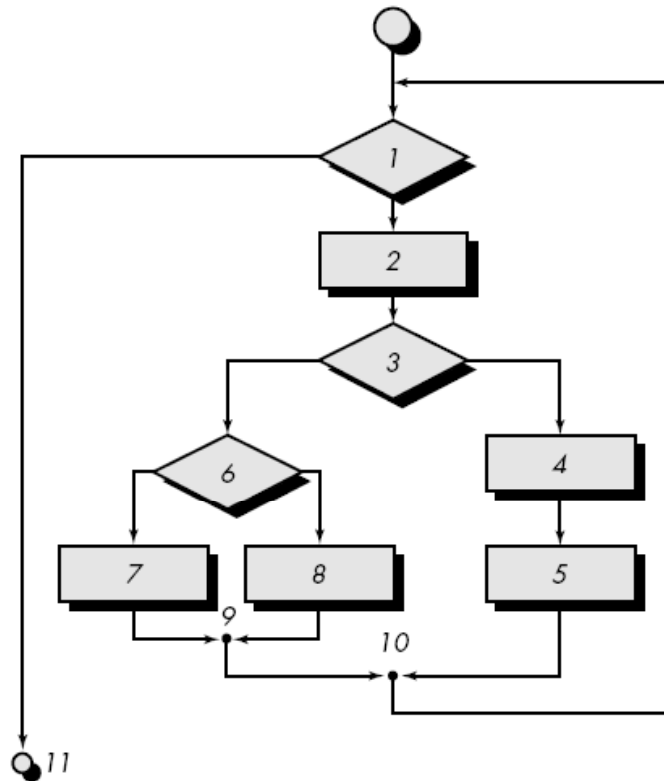
```
q=1;  
b=2;  
c=3;  
if (a==2) {x=x+2;}  
else {x=x/2;}  
p=q/r;  
if (b/c>3) {z=x+y;}  
    
```



Cyclomatic Complexity

- An **independent path**
 - Any path through the program that introduces at least one new set of processing statements or a new condition
 - Must move along at least one edge that has not been traversed before the path is defined

Cyclomatic Complexity



Cyclomatic Complexity

- Independent Paths
 - path 1: 1-11
 - path 2: 1-2-3-4-5-10-1-11
 - path 3: 1-2-3-6-8-9-10-1-11
 - path 4: 1-2-3-6-7-9-10-1-11
- Paths 1, 2, 3, and 4 constitute a basis set for the flow graph
 - If tests can be designed to force execution of these paths (a basis set):
 - Every statement in the program will have been guaranteed to be executed at least one time
 - Every condition will have been executed on its true and false sides

Cyclomatic Complexity

- Cyclomatic complexity, $V(G)$, for a flow graph, G , is defined as $V(G) = E - N + 2$ (E is the number of flow graph edges, N is the number of flow graph nodes)
- If all decisions in the graph are binary,
 - $V(G) = P + 1$ (P is the number of predicate nodes contained in the flow graph G)
- The value computed for cyclomatic complexity
 - Defines the number of independent paths in the basis set of a program
 - Basis path testing provides a minimum, lower-bound on the number of test cases that need to be written

Deriving Test Cases

- Using the design or code as a foundation, draw a corresponding flow graph
- Determine the cyclomatic complexity of the resultant flow graph
- Determine a basis set of linearly independent paths
- Prepare test cases that will force execution of each path in the basis set

Deriving Test Cases

PROCEDURE average;

- * This procedure computes the average of 100 or fewer numbers that lie between bounding values; it also computes the sum and the total number valid.

INTERFACE RETURNS average, total.input, total.valid;

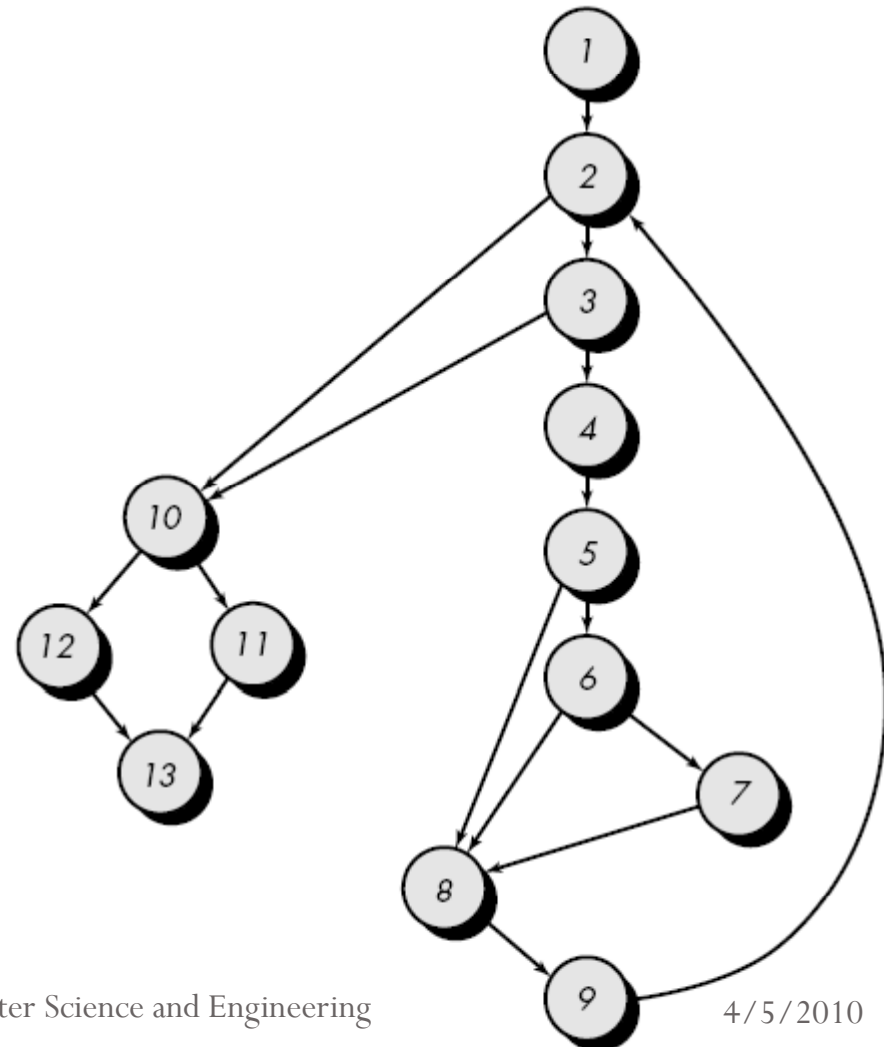
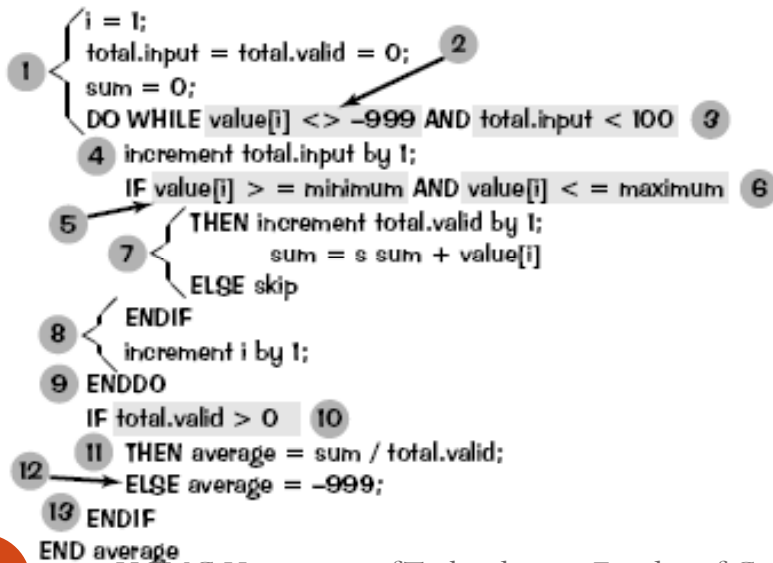
INTERFACE ACCEPTS value, minimum, maximum;

TYPE value[1:100] IS SCALAR ARRAY;

TYPE average, total.input, total.valid;

minimum, maximum, sum IS SCALAR;

TYPE i IS INTEGER;



Deriving Test Cases

$$V(G) = 5 \text{ predicate nodes} + 1 = 6$$

path 1: 1-2-10-11-13

path 2: 1-2-10-12-13

path 3: 1-2-3-10-11-13

path 4: 1-2-3-4-5-8-9-2-...

path 5: 1-2-3-4-5-6-8-9-2-...

path 6: 1-2-3-4-5-6-7-8-9-2-...

Deriving Test Cases

Path 1 test case:

$\text{value}(k) = \text{valid input, where } k < i \text{ for } 2 \leq i \leq 100$

$\text{value}(i) = 999 \text{ where } 2 \leq i \leq 100$

Expected results: Correct average based on k values and proper totals.

Note: Path 1 cannot be tested stand-alone but must be tested as part of path 4, 5, and 6 tests.

Path 2 test case:

$\text{value}(1) = 999$

Expected results: Average = 999; other totals at initial values.

Path 3 test case:

Attempt to process 101 or more values.

First 100 values should be valid.

Expected results: Same as test case 1.

Path 4 test case:

$\text{value}(i) = \text{valid input where } i < 100$

$\text{value}(k) < \text{minimum where } k < i$

Expected results: Correct average based on k values and proper totals.

Path 5 test case:

$\text{value}(i) = \text{valid input where } i < 100$

$\text{value}(k) > \text{maximum where } k \leq i$

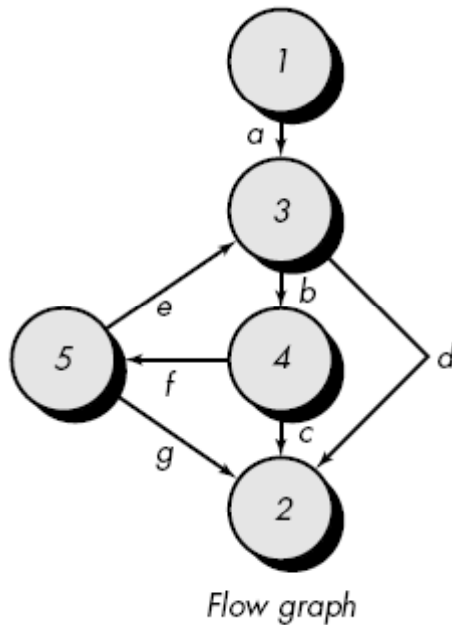
Expected results: Correct average based on n values and proper totals.

Path 6 test case:

$\text{value}(i) = \text{valid input where } i < 100$

Expected results: Correct average based on n values and proper totals.

Graph Matrices



Connected to node		1	2	3	4	5
Node		1	2	3	4	5
1				a		
2						
3			d		b	
4			c			f
5			g	e		

Graph matrix

Connected to node		1	2	3	4	5	
Node		1	2	3	4	5	Connections
1				1			1 - 1 = 0
2							
3			1		1		2 - 1 = 1
4			1			1	2 - 1 = 1
5			1	1			2 - 1 = 1

Graph matrix

$\overline{3 + 1}$

$\overline{3} + 1 = 4$

 Cyclomatic complexity

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- Overview
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Control-flow/Coverage Testing

- Control flow of the program
- Consider various aspects of this flow graph in order to ensure that we have an adequate set of test cases
- Coverage is a measure of the completeness of the set of test cases
 - Method Coverage
 - Statement Coverage
 - Branch Coverage
 - Condition Coverage

Method Coverage

- A measure of the percentage of methods that have been executed by test cases.
- Objective: 100% method coverage
- Examples
 - Test Case 1: foo(0, 0, 0, 0, 0.), expected return value of 0.

```
1  int foo (int a, int b, int c, int d, float e) {  
2      float e;  
3      if (a == 0) {  
4          return 0;  
5      }  
6      int x = 0;  
7      if ((a==b) OR ((c == d) AND bug(a) )) {  
8          x=1;  
9      }  
10     e = 1/x;  
11     return e;  
12 }
```

Statement Coverage

- Statement coverage is a measure of the percentage of statements that have been executed by test cases
- Objective: 100% statement coverage
- Examples:
 - In Test Case 1, the program statements on lines 1-5 out of 12 lines of code are executed \Rightarrow 42% (5/12) statement coverage.
 - Add Test Case 2: the method call `foo(1, 1, 1, 1, 1.)`, expected return value of 1 \Rightarrow 100% statement coverage

```
1  int foo (int a, int b, int c, int d, float e) {  
2      float e;  
3      if (a == 0) {  
4          return 0;  
5      }  
6      int x = 0;  
7      if ((a==b) OR ((c == d) AND bug(a) )) {  
8          x=1;  
9      }  
10     e = 1/x;  
11     return e;  
12 }
```


Branch Coverage

- Branch coverage is a measure of the percentage of the decision points (Boolean expressions) of the program have been evaluated as both true and false in test cases
- For decision/branch coverage, we evaluate an entire Boolean expression as one true-or-false predicate even if it contains multiple logical-and or logical-or operators
- Objective:
 - 100% Branch Coverage
 - Only 50% branch coverage is practical in very large systems of 10 million source lines of code or more (Beizer, 1990).
- Examples:

```
3    if (a == 0) {  
7    if ((a==b) OR ((c == d) AND bug(a) )) {
```

Branch Coverage

Line	Predicate	True	False
3	(a == 0)	Test Case 1 foo(0, 0, 0, 0, 0) return 0	Test Case 2 foo(1, 1, 1, 1, 1) return 1
7	((a==b) OR ((c == d) AND bug(a)))	Test Case 2 foo(1, 1, 1, 1, 1) return 1	

- Branch Coverage: 75%
- Test Case 3: foo(1, 2, 1, 2, 1) => 100% Branch Coverage
(uncovers a previously undetected division-by-zero problem
on line 10!)

Condition Coverage

- Condition coverage is a measure of percentage of Boolean sub-expressions of the program that have been evaluated as both true or false outcome [applies to compound predicate] in test cases
- There are no industry standard objectives for condition coverage
- Example:
7 if ((a==b) OR ((c == d) AND bug(a))) {

Condition Coverage

Predicate	True	False
(a==b)	Test Case 2 foo(1, 1, x, x, 1) return value 0	Test Case 3 foo(1, 2, 1, 2, 1) division by zero!
(c==d)		Test Case 3 foo(1, 2, 1, 2, 1) division by zero!
bug(a)		

- Condition Coverage: 50%
 - (c==d) -> TRUE: never been tested
 - short-circuit Boolean has prevented the method bug(int) from ever being executed

Condition Coverage

Predicate	True	False
(a==b)	Test Case 2 foo(1, 1, x, x, 1) return value 0	Test Case 3 foo(1, 2, 1, 2, 1) division by zero!
(c==d)	Test Case 4 foo(1, 2, 1, 1, 1) return value 1	Test Case 3 foo(1, 2, 1, 2, 1) division by zero!
bug(a)	Test Case 4 foo(1, 2, 1, 1, 1) return value 1	Test Case 5 foo(3, 2, 1, 1, 1) division by zero!

- bug(a)
 - If $a > 1$ return FALSE
 - Else return TRUE

Content

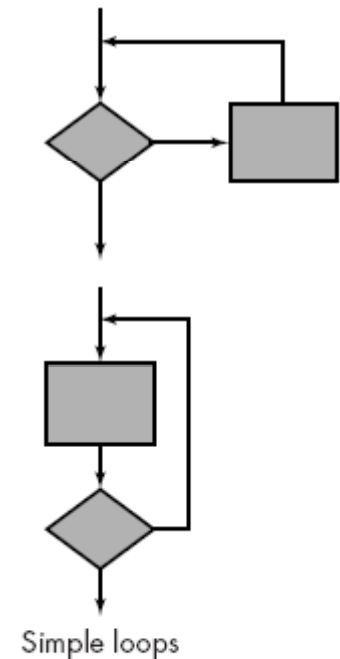
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Loop Testing

- Focuses exclusively on the validity of loop constructs.
- Types of Loop
 - Simple loops
 - Nested Loops
 - Concatenated Loops
 - Unstructured Loops

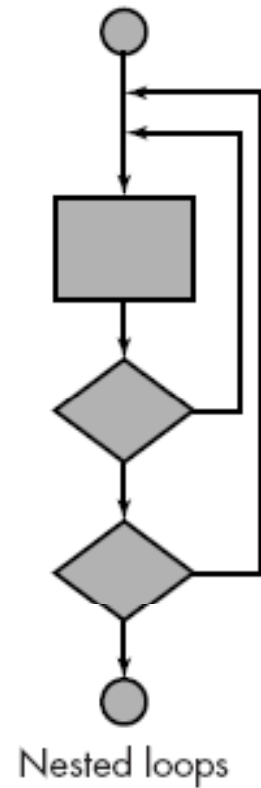
Simple loops

- The following set of tests can be applied to simple loops, where n is the maximum number of allowable passes through the loop
 - Skip the loop entirely.
 - Only one pass through the loop.
 - Two passes through the loop.
 - m passes through the loop where $m < n$.
 - $n - 1, n, n + 1$ passes through the loop



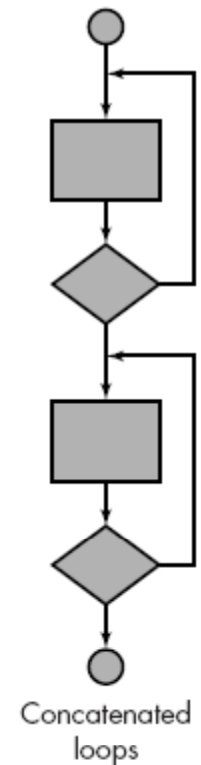
Nested Loops

- Start at the innermost loop. Set all other loops to minimum values.
- Conduct simple loop tests for the innermost loop while holding the outer loops at their minimum iteration parameter (e.g., loop counter) values. Add other tests for out-of-range or excluded values.
- Work outward, conducting tests for the next loop, but keeping all other outer loops at minimum values and other nested loops to "typical" values.
- Continue until all loops have been tested.



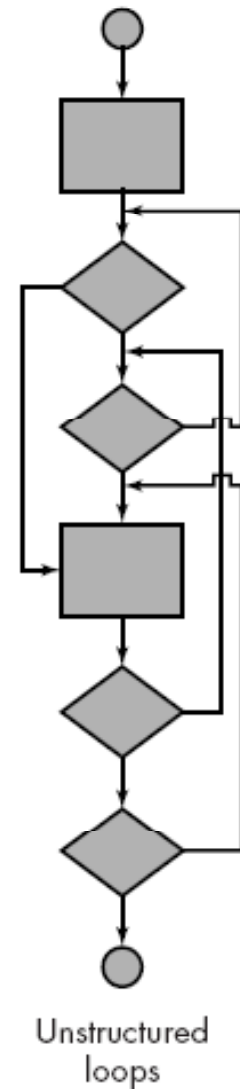
Concatenated Loops

- If each of the loops is independent of the other:
 - Concatenated loops can be tested using the approach defined for simple loops,
- Else
 - the approach applied to nested loops is recommended.



Unstructured Loops

- Whenever possible, this class of loops should be redesigned to reflect the use of the structured programming constructs



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Data Flow Testing

- The data flow testing method selects test paths of a program according to the locations of definitions and uses of variables in the program
- Data flow testing is a powerful tool to detect improper use of data values due to coding errors
 - Incorrect assignment or input statement
 - Definition is missing (use of null definition)
 - Predicate is faulty (incorrect path is taken which leads to incorrect definition)

Data Flow Testing

- Variables that contain data values have a defined life cycle: created, used, killed (destroyed).
- The "scope" of the variable

```
{          // begin outer block
  int x;    // x is defined as an integer within this outer block
  ...;     // x can be accessed here
  {        // begin inner block
    int y;  // y is defined within this inner block
    ...;    // both x and y can be accessed here
  }        // y is automatically destroyed at the end of
           // this block
  ...;     // x can still be accessed, but y is gone
}          // x is automatically destroyed
```

Data Flow Testing

- Three possibilities exist for the first occurrence of a variable through a program path:
 - $\sim d$ - the variable does not exist (indicated by the \sim), then it is defined (d)
 - $\sim u$ - the variable does not exist, then it is used (u)
 - $\sim k$ - the variable does not exist, then it is killed or destroyed (k)

Data Flow Testing

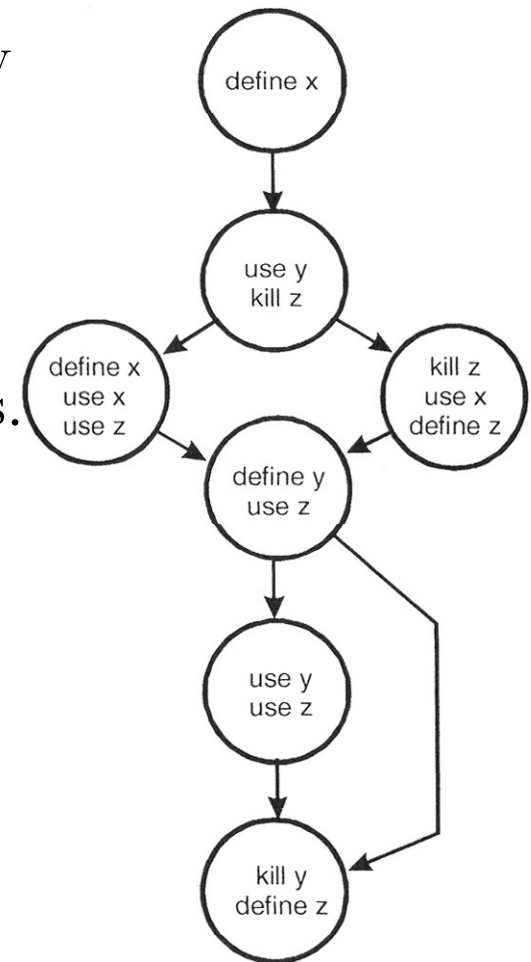
- Time-sequenced pairs of defined (d), used (u), and killed (k):
 - dd - Defined and defined again—not invalid but suspicious. Probably a programming error.
 - du - Defined and used—perfectly correct. The normal case.
 - dk - Defined and then killed—not invalid but probably a programming error.
 - ud - Used and defined—acceptable.
 - uu - Used and used again—acceptable.
 - uk - Used and killed—acceptable.
 - kd - Killed and defined—acceptable. A variable is killed and then redefined.
 - ku - Killed and used—a serious defect. Using a variable that does not exist or is undefined is always an error.
 - kk - Killed and killed—probably a programming error

Data Flow Testing

- A data flow graph is similar to a control flow graph in that it shows the processing flow through a module.

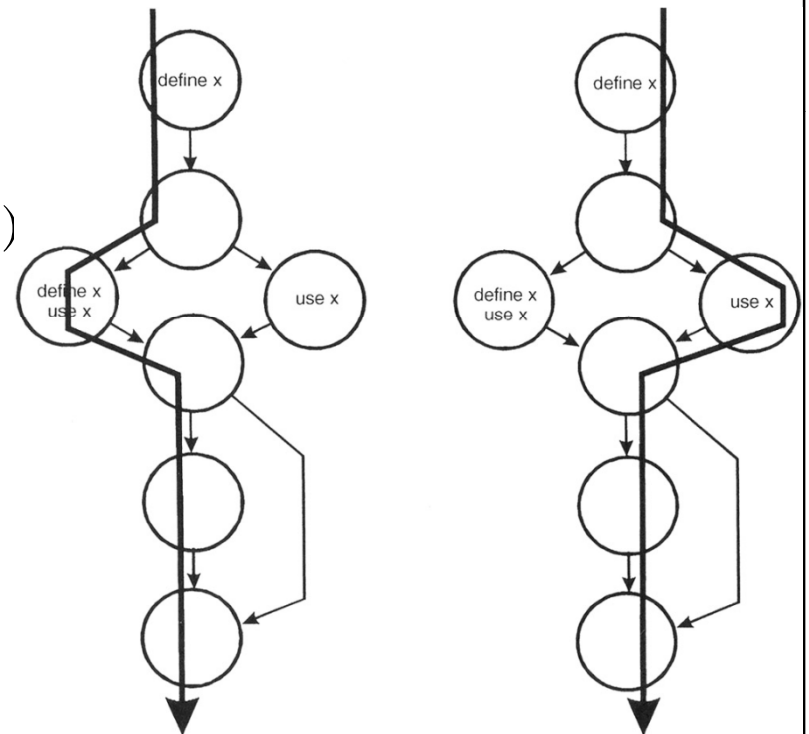
In addition, it details the definition, use, and destruction of each of the module's variables.

- Technique
 - Construct diagrams
 - Perform a static test of the diagram
 - Perform dynamic tests on the module



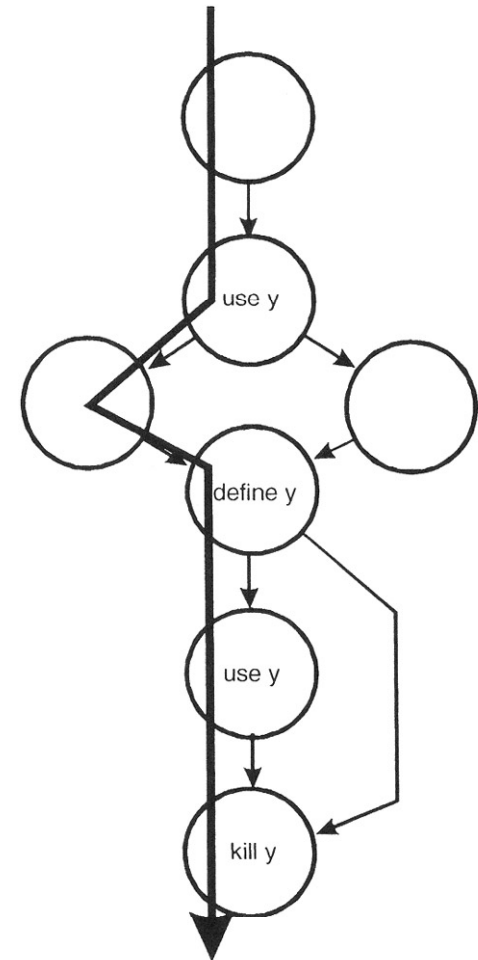
Data Flow Testing

- Perform a static test of the diagram
 - For each variable within the module we will examine define-use-kill patterns along the control flow paths
 - The define-use-kill patterns for x (taken in pairs as we follow the paths) are:
 - \sim define - correct, the normal case
 - define-define - suspicious, perhaps a programming error
 - define-use - correct, the normal case



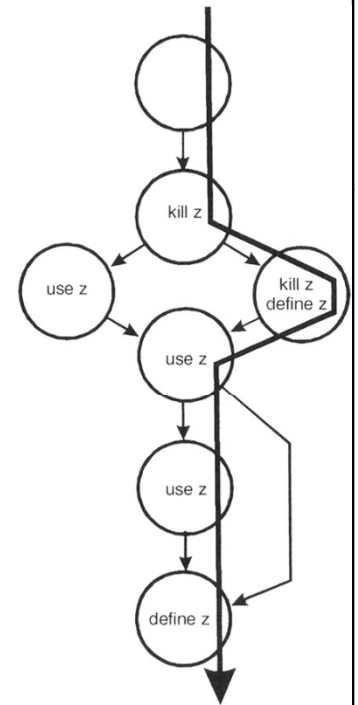
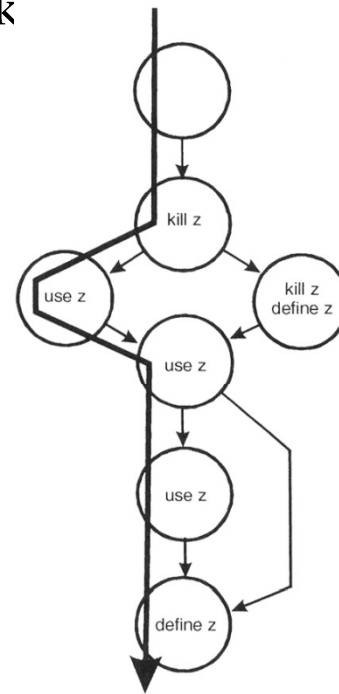
Data Flow Testing

- Perform a static test of the diagram
 - The define-use-kill patterns for y (taken in pairs as we follow the paths) are:
 - \sim use - major blunder
 - use-define - acceptable
 - define-use - correct, the normal case
 - use-kill - acceptable
 - define-kill - probable programming error



Data Flow Testing

- Perform a static test of the diagram
 - The define-use-kill patterns for z (taken in pairs as we follow the paths) are:
 - ~kill - programming error
 - kill-use - major blunder
 - use-use - correct, the normal case
 - use-define - acceptable
 - kill-kill - probably a programming error
 - kill-define - acceptable
 - define-use - correct, the normal case



Data Flow Testing

- In performing a static analysis on this data flow model the following problems have been discovered:
 - x: define-define
 - y: \sim use
 - y: define-kill
 - z: \sim kill
 - z: kill-use
 - z: kill-kill

Data Flow Testing

- While static testing can detect many data flow errors, it cannot find them all \Rightarrow Dynamic Data Flow Testing
- Dynamic Data Flow Testing
 - Every "define" is traced to each of its "uses"
 - Every "use" is traced from its corresponding "define"
 - Steps
 - Enumerate the paths through the module
 - For every variable, create at least one test case to cover every define-use pair.

Limitation

- The tester must have sufficient programming skill to understand the code and its control flow.
- Can be very time consuming because of all the modules and basis paths that comprise a system

Q&A