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QUESTION

Design an algorithm to merge two sorted lists that are passed as parameters, and return one merged sorted list.

```
function merge_sorted_lists(list_one, list_two):
```

```
    merged_list = []
    i = 0
    j = 0
```

```
    while i < len(list_one) and j < len(list_two):
        if list_one[i] <= list_two[j]:
            merged_list.append(list_one[i])
            i += 1
        else:
            merged_list.append(list_two[j])
            j += 1
```

```
    while i < len(list_one):
        merged_list.append(list_one[i])
        i += 1
```

```
    while j < len(list_two):
        merged_list.append(list_two[j])
        j += 1
```

```
    return merged_list
```

Derive a recurrence relation for this algorithm.

$$T(n) = \begin{cases} 0 & \text{if } n=0 \\ 1 & \text{if } n=1 \\ T(n-1) + O(1) & \text{if } n \geq 2 \end{cases}$$

$$T(n) = T(n-1) + C$$

Estimate time and space complexities for the same algorithm.

Time complexity

$O(n)$ as all elements are compared and appended exactly once.

Space complexity

The primary data structure used is the merged_list, which stores the combined elements of the input lists. The merged_list will contain all n elements. Hence, the space complexity is $O(n)$.