15.075 Statistical Thinking and Data Analysis

Computer Exercises 3 Due December 8, 2011

Instructions: Please solve the following exercises using MATLAB. One simple way to present your solutions is to copy all of your code and results (plots, numerical answers, etc.) into a Word document, which you should submit in class. There is no online submission. **Do NOT share code!**

Exercise 1 (30 pts)

To determine whether glaucoma affects the corneal thickness, measurements were made in 8 people affected by glaucoma in one eye but not in the other. The corneal thicknesses (in microns) were as follows:

Person	1	2	3	4	5	6	7	8
Eye affected by glaucoma	488	478	480	426	440	410	458	460
Eye not affected by glaucoma	484	478	492	444	436	398	464	476

Assume the corneal thicknesses are normally distributed with mean μ_1 and variance σ_1^2 for eyes affected by glaucoma, and mean μ_2 and variance σ_2^2 for eyes not affected by glaucoma. Test H_0 : $\mu_1 = \mu_2$ against H_1 : $\mu_1 < \mu_2$ using $\alpha = 0.1$. What kind of test will you perform? Base your conclusion on a 90% confidence interval.

Solution

Here is the script and the results:

```
stats =
```

tstat: -1.0530 df: 7

sd: 10.7438

The upper 90% CI is $(-\infty, 1.3746]$, which includes 0, so we do not reject H_0 .

Exercise 2 (70 pts)

The following data give the barometric pressure x (in inches of mercury) and the boiling point y (in °F) of water in the Alps.

х	У	х	У	Х	У
20.79	194.5	23.89	200.9	28.49	209.5
20.79	194.3	23.99	201.1	27.76	208.6
22.40	197.9	24.02	201.4	29.04	210.7
22.67	198.4	24.01	201.3	29.88	211.9
23.15	199.4	25.14	203.6	30.06	212.2
23.35	199.9	26.57	204.6		

- a. Make a scatterplot with pressure *x* on the *x*-axis and boiling point *y* on the *y*-axis. Does the relationship appear to be approximately linear?
- b. Fit a least-squares line. What are the coefficients of the line? What are their t-statistics?
- c. Plot the least-squares line in the same figure with the scatterplot.
- d. What proportion of variation in the boiling point is explained by the linear regression model on the barometric pressure?
- e. Is the slope coefficient significantly different from zero? How do you know? If yes, at what significance level?
- f. What are SSR, SSE, SST, MSR, MSE and F?

Solution

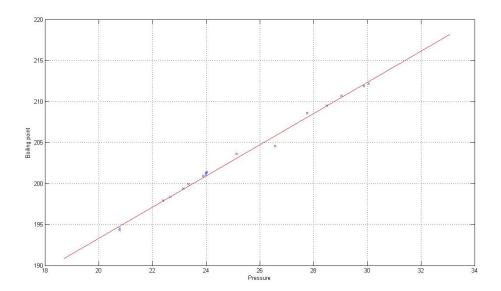
Here is the script and the results:

```
a,c.
clear all;
clc;
close all;

pressure = [20.79, 20.79, 22.40, 22.67, 23.15, 23.35, 23.89, 23.99, 24.02,
24.01, 25.14, 26.57, 28.49, 27.76, 29.04, 29.88, 30.06];
boiling_point = [194.5, 194.3, 197.9, 198.4, 199.4, 199.9, 200.9, 201.1,
201.4, 201.3, 203.6, 204.6, 209.5, 208.6, 210.7, 211.9, 212.2];

% Scatterplot
plot(pressure, boiling_point,'x');
grid;
```

```
xlabel('Pressure');
ylabel('Boiling point');
hold on;
```



Yes, the relationship appears approximately linear.

```
b.
% Run the regression
whichstats = {'beta','r', 'mse', 'rsquare', 'tstat', 'fstat'};
stats = regstats(boiling_point, pressure, 'linear', whichstats);

betas = stats.beta
tstats = stats.tstat.t
pvals = stats.tstat.pval
rsquare = stats.rsquare

betas =

155.2965
    1.9018

tstats =

167.4650
    51.7408

pvals =

1.0e-017 *
```

- 0.0000
- 0.2528

rsquare =

0.9944

The coefficients of the line are $\hat{\beta}_0=155.2965$ and $\hat{\beta}_1=1.9018$.

- d. The proportion of variation in boiling point explained by the model is $r^2 = 0.9944$.
- e. Yes, $\hat{\beta}_1$ is significantly different from zero. The p-value is nearly zero (<2e-16), so the difference is significant for any reasonable α .

f.

Regression ANOVA

Source	df	SS	MS	F	P
Regr	1.0000	527.8249	527.8249	2677.1053	0.0000
Resid	15.0000	2.9574	0.1972		
Total	16.0000	530.7824			

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