

```
import numpy as np
from numpy.fft import fft2, ifft2, fftshift
from scipy.signal import convolve2d, correlate2d
import matplotlib.pyplot as plt

from Functions import *
from gaussfft import gaussfft
#import cv2
import time

tools = np.load("/content/few256.npy")
house = np.load("/content/godthem256.npy")

# Approximate the first order partial derivatives
# Sobel filter smoothens the image when convolved

delta_x = [[-1, 0, 1], # Horizontal Edges
            [-2, 0, 2],
            [-1, 0, 1]]

delta_y = [[-1, -2, -1], # Vertical Edges
            [0, 0, 0],
            [1, 2, 1]]

# Discrete Derivation Approximations
# 'Valid' -> Return convolution parts without zero padded. Hence,
# size of dxtools & dytools reduces by 2.
dxtools = convolve2d(tools, delta_x, 'valid') # Convolution
dytools = convolve2d(tools, delta_y, 'valid')


print("Size of dxmask", np.shape(delta_x)) # (5,5)
print("Size of dymask", np.shape(delta_y)) # (5,5)
print("Size of Image", np.shape(tools)) # (256,256)
print("Size of dxtools", np.shape(dxtools)) # (254,254)
print("Size of dytools", np.shape(dytools)) # (254,254)

# plotting
plt.close("all")
plt.figure()

ax = plt.subplot(2, 3, 1)
ax.axis("off")
ax.imshow(tools, cmap='gray')
ax.set_title("image")

ax = plt.subplot(2, 3, 2)
ax.axis("off")
ax.imshow(dxtools, cmap='gray')
ax.set_title("Gradient along x")

ax = plt.subplot(2, 3, 3)
ax.axis("off")
ax.imshow(dytools, cmap='gray')
ax.set_title("Gradient along y")
plt.show()

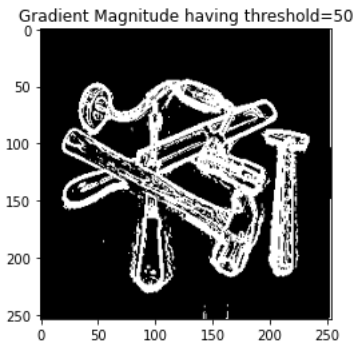
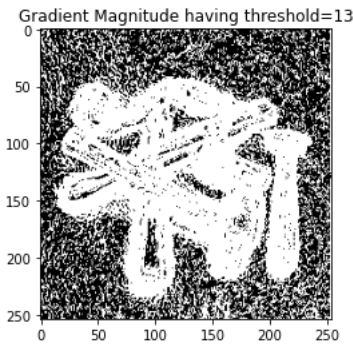
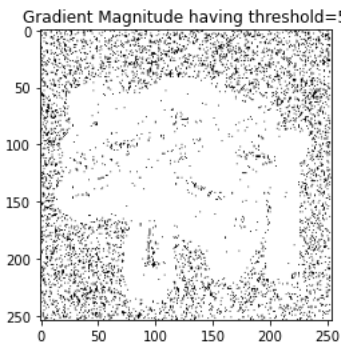
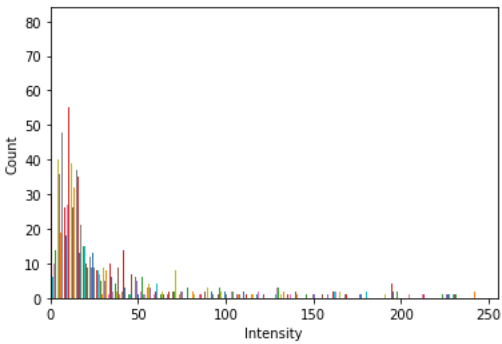
Size of dxmask (3, 3)
Size of dymask (3, 3)
Size of Image (256, 256)
Size of dxtools (254, 254)
Size of dytools (254, 254)
image Gradient along x Gradient along y


# 2. Point-wise thresholding of gradient magnitudes

# If magnitude at a pixel exceeds a threshold,report a possible edge point
gradmagntools = np.sqrt(dxtools**2+dytools**2)
plt.hist(gradmagntools,255)
plt.ylabel("Count")
plt.xlabel("Intensity")
plt.xlim([0,255])
plt.show()

thresholds=[5,13,50,100,150,200]

for i in thresholds: #range(1,len(thresholds)):
    plt.title('Gradient Magnitude having threshold=%i' %i)
    plt.imshow(((gradmagntools-i)>0).astype(int),cmap='gray')
    plt.show()
```



```
sigma_x = [[-1, 0, 1],
            [-2, 0, 2],
            [-1, 0, 1]]

sigma_y = [[-1, -2, -1],
            [0, 0, 0],
            [1, 2, 1]]

shape = 'same'

def Lv(inpic, shape):
    Lx = convolve2d(inpic, sigma_x, shape)
    Ly = convolve2d(inpic, sigma_y, shape)
    return np.sqrt(Lx**2+Ly**2)

resultt = Lv(tools, shape)
plt.imshow(resultt, cmap='gray')
plt.title("few256 Image magnitude")
plt.show()

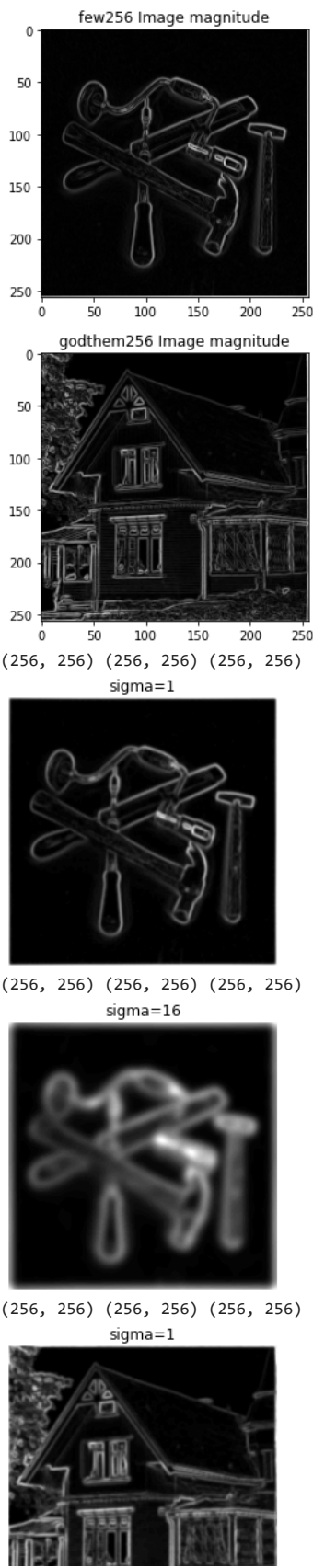
resultt2 = Lv(house, shape)
plt.imshow(resultt2, cmap='gray')
plt.title("godthem256 Image magnitude")
plt.show()

plt.title(label="sigma=1")
showgrey((discgaussfft(resultt, 1))) # Kernel variance=0.1
plt.show()

plt.title(label="sigma=16")
showgrey((discgaussfft(resultt, 16))) # Kernel variance=16
plt.show()

plt.title(label="sigma=1")
showgrey((discgaussfft(resultt2, 1))) # Kernel variance=0.1
plt.show()

plt.title(label="sigma=16")
showgrey((discgaussfft(resultt2, 16))) # Kernel variance=16
plt.show()
```



```
### 4. Computing differential geometry descriptors

# Extracting thin edges by considering points for which gradient magnitude
# reaches local maxima in gradient direction.

# Lvv= 2nd order derivative of smoothened intensity function L in v direction.

sigmax = [[0, 0, 0, 0, 0],
          [0, 0, 0, 0, 0],
          [0, -0.5, 0, 0.5, 0],
          [0, 0, 0, 0, 0],
          [0, 0, 0, 0, 0]]

sigmay = [[0, 0, 0, 0, 0],
          [0, 0, -0.5, 0, 0],
          [0, 0, 0, 0, 0],
          [0, 0, 0.5, 0, 0],
          [0, 0, 0, 0, 0]]

sigmaxx = [[0, 0, 0, 0, 0],
           [0, 0, 0, 0, 0],
           [0, 1, -2, 1, 0],
           [0, 0, 0, 0, 0],
           [0, 0, 0, 0, 0]]

sigmayy = [[0, 0, 0, 0, 0],
           [0, 0, 1, 0, 0],
           [0, 0, -2, 0, 0],
           [0, 0, 1, 0, 0],
           [0, 0, 0, 0, 0]]

shape = 'same'
sigmaxy = convolve2d(sigmax, sigmay, shape)
sigmaxx = convolve2d(sigmax, sigmaxx, shape)
sigmayy = convolve2d(sigmay, sigmayy, shape)
sigmaxy = convolve2d(sigmax, sigmaxy, shape)
sigmaxy = convolve2d(sigmax, sigmayy, shape)

def Lvtilde(pic, shape):
    Lx = convolve2d(pic, sigmax, shape)
    Ly = convolve2d(pic, sigmay, shape)
    Lxx = convolve2d(pic, sigmaxx, shape)
    Lxy = convolve2d(pic, sigmaxy, shape)
    Lyy = convolve2d(pic, sigmayy, shape)

    first_term = (Lx**2)*(Lxx)
    second_term = 2*(Lx)*(Ly)*(Lxy)
    third_term = (Ly**2)*Lyy
    Lv = first_term+second_term+third_term
    #print("Lv Sign:")
    #print(np.sign(Lv))
```

```

    return Lvv

def Lvvtilde(pic, shape='same'):
    Lx = convolve2d(pic, sigmaa_x, shape)
    Ly = convolve2d(pic, sigmaa_y, shape)
    Lxx = convolve2d(pic, sigmaa_xx, shape)
    Lxy = convolve2d(pic, sigmaa_xy, shape)
    Lyy = convolve2d(pic, sigmaa_yy, shape)

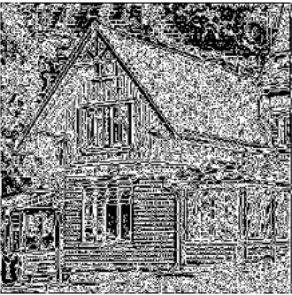



    Lxxx = convolve2d(pic, sigmaa_xxx, shape)
    Lyxy = convolve2d(pic, sigmaa_yxy, shape)
    Lxxy = convolve2d(pic, sigmaa_xxy, shape)
    Lxyy = convolve2d(pic, sigmaa_xyy, shape)

    Lvvt = ((Lx**3)*Lxxx) + 3*(Lx**2)*Ly*Lxy + 3*Lx*(Ly**2)*Lxy + (Ly**3)*Lyxy
    #print("Lvvt Sign:")
    #print(np.sign(Lvvt))
    return Lvvt

scale = [0.0001, 1.0, 4.0, 16.0, 64.0]
for i in scale:
    plt.title("Contours (house) for scale %i " % i)
    # Computing zero-crossings of Lvv on scale
    showgrey(contour(Lvtild(discgaussfft(house, i), shape)))

for i in scale:
    plt.title("3rd order derivative (few256) for scale %i " % i)
    res=discgaussfft(tools, i)
    showgrey((Lvvtild(res, shape)<0).astype(int))

[x, y] = np.meshgrid(range(-5, 6), range(-5, 6))
#print(convolve2d(x**3, sigmaa_xxx, 'valid'))
#print(convolve2d(x**3, sigmaa_xx, 'valid'))
#print(convolve2d(x**2*y, sigmaa_xxy, 'valid'))
```

```
(256, 256) (256, 256) (256, 256)
Contours (house) for scale 0

(256, 256) (256, 256) (256, 256)
Contours (house) for scale 1

(256, 256) (256, 256) (256, 256)
Contours (house) for scale 4

(256, 256) (256, 256) (256, 256)
Contours (house) for scale 16


### 5. Extractions of edge segments

def extractedge(inpic, scale, threshold, shape):
    zeropic = Lvvtilde(discgaussfft(inpic, scale), shape)
    Lvvttil = Lvvttilde(discgaussfft(inpic, scale), shape)
    Lv1 = Lv(discgaussfft(inpic, scale), shape)

    maskpic1 = np.array((Lvvttil < 0))
    maskpic2 = np.array(Lv1 > threshold)
    # Extract level curves in image & rejects points based on sign of 2nd input arguement
    curves = zerocrosscurves(zeropic, maskpic1)
    # Thresholds these curves wrt sign of another image
    curves = thresholdcurves(curves, maskpic2)
    return curves

# Threshold for the gradient magnitude
# Find best scale for each image & adjust threshold accordingly
scale = [0.0001,1, 2, 4, 16, 64]
#threshold = 0.7
thresholds=[1,5,10,15,17,20]

fig = plt.figure(figsize=(16, 16))
for i in range(len(thresholds)):
    edgecurves = extractedge(tools,scale[4],thresholds[i], shape)
    ax=fig.add_subplot(2,3,i+1)
    ax.plot()
    plt.title("Scale=16, threshold %i" % thresholds[i])
    overlaycurves(tools, edgecurves)
plt.show()

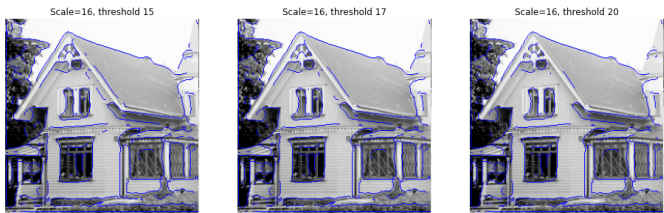
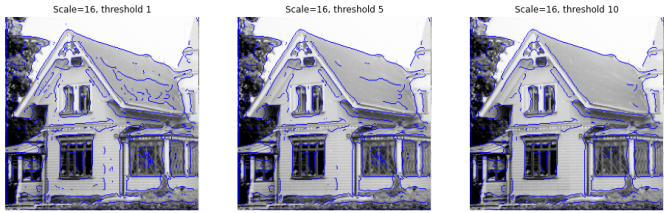
fig = plt.figure(figsize=(16, 16))
for i in range(len(scale)):
    edgecurves = extractedge(tools,scale[i], thresholds[3], shape)
    ax=fig.add_subplot(2,3,i+1)
    ax.plot()
    plt.title("T=15,Scale= %i" % scale[i])
    overlaycurves(tools, edgecurves)
plt.show()

fig = plt.figure(figsize=(16, 16))
for i in range(len(scale)):
    edgecurves = extractedge(house,scale[i], thresholds[3], shape)
    ax=fig.add_subplot(2,3,i+1)
    ax.plot()
    plt.title("T=15,Scale= %i" % scale[i])
    overlaycurves(house, edgecurves)
plt.show()

fig = plt.figure(figsize=(16, 16))
for i in range(len(thresholds)):
    edgecurves = extractedge(house,scale[4],thresholds[i], shape)
    ax=fig.add_subplot(2,3,i+1)
    ax.plot()
    plt.title("Scale=16, threshold %i" % thresholds[i])
    overlaycurves(house, edgecurves)
plt.show()
```



```
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
(256, 256) (256, 256) (256, 256)
```



# 6. Hough Transform

```
def houghline(pic, curves, magnitude, nrho, ntheta, threshold, nlines=10, verbose=False, scale = 0):
    accumulator = np.zeros((nrho, ntheta))
    x, y = magnitude.shape
    r = np.sqrt(np.square(x) + np.square(y))
    rho = np.linspace(-r, r, nrho)
    theta = np.linspace(-np.pi/2, np.pi/2, ntheta)

    for i in range(len(curves[0])):
        x = curves[0][i]
        y = curves[1][i]
        curve_magnitude = magnitude[x][y]
        if curve_magnitude > threshold:
            for j in range(ntheta):
                rho_Val = (x*np.cos(theta[j])) + (y*np.sin(theta[j]))
                rho_Index = np.argmin(abs(rho - rho_Val))
                accumulator[rho_Index][j] += 1

    linepar = []

    # Detecting local maxima in accumulator by locmax8()
    pos, value, _ = locmax8(accumulator)
    indexvector = np.argsort(value)[-nlines:] # Index
    pos = pos[indexvector]

    f = plt.figure(figsize=(4, 4), dpi=200)
    f.subplots_adjust(wspace=0.2, hspace=0.4)
```



```
xx = f.add_subplot(1, 2, 1)
showgrey(accumulator, False)
xx.title.set_text("Accumulator")

xx = f.add_subplot(1, 2, 2)
overlaycurves(pic, curves)
xx.title.set_text("Hough Edge Lines")

for idx in range(nlines): # Index values correspond to nlines
    thetaidxacc = pos[idx][0]
    rhoidxacc = pos[idx][1]

    rhoMax = rho[rhoidxacc]
    thetaMax = theta[thetaidxacc]
    linepar.append([rhoMax, thetaMax])

    # Convert (rho,theta) back to cartesian coordinates (x,y)
    x0 = rhoMax * np.cos(thetaMax)
    y0 = rhoMax * np.sin(thetaMax)
    dx = r * (-np.sin(thetaMax))
    dy = r * (np.cos(thetaMax))

    plt.plot([y0 - dy, y0, y0 + dy],[x0 - dx, x0, x0 + dx], "g-")

plt.show()
return linepar, accumulator

def houghedgeline(pic, scale, thresholdd, nrho, ntheta, nlines=10, verbose=False):
    curves = extractedge(pic, scale, thresholdd, "same")
    gaussianSmooth = discgaussfft(pic, scale) # Smoothen the histogram before detecting local maxima
    gradmagn = Lv(gaussianSmooth, "same")

    linepar, acc = houghline(pic,curves,gradmagn,nrho,ntheta,thresholdd,nlines,verbose,scale)
    return None
```

```
start_time = time.time()

testimage1=np.load("/content/triangle128.npy")
smalltest1=binsubsample(testimage1)
#scale = [0.0001,1, 2, 4, 16, 64]
#threshold = 0.7
#thresholds=[1,5,10,15,17,20]
scale=4
thresholdd= 5 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)
ntheta = 100 # Number of Accumulator in theta direction
nrho = 200 # Number of Accumulators in rho direction

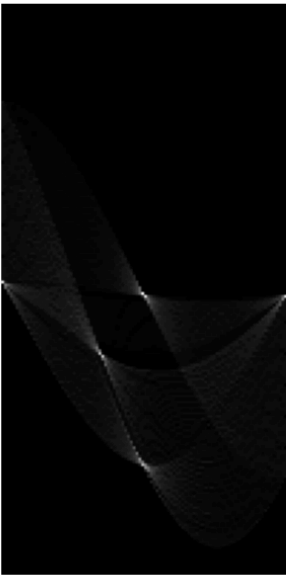
houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=10)

# For large rho/theta values, lines will be of low accuracy
# For samll rho/theta values, result may contain multiple responses for same line.
```

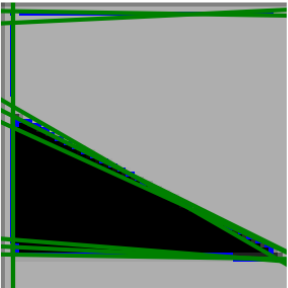
```
print("--- %s seconds ---" % (time.time() - start_time))

[[0.0625 0.125  0.0625]
 [0.125  0.25   0.125 ]
 [0.0625 0.125  0.0625]]
(64, 64) (64, 64) (64, 64)
(64, 64) (64, 64) (64, 64)
(64, 64) (64, 64) (64, 64)
(64, 64) (64, 64) (64, 64)
(64, 64) (64, 64) (64, 64)
(64, 64) (64, 64) (64, 64)
(64, 64) (64, 64) (64, 64)
```

Accumulator



Hough Edge Lines



--- 0.585442066192627 seconds ---



```
start_time = time.time()

testimage1=np.load("/content/houghtest256.npy")
smalltest1=binsubsample(testimage1)
#scale = [0.0001,1, 2, 4, 16, 64]
#threshold = 0.7
#thresholds=[1,5,10,15,17,20]
scale=4
thresholdd= 5 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)
ntheta = 100 # Number of Accumulator in theta direction
nrho = 200 # Number of Accumulators in rho direction

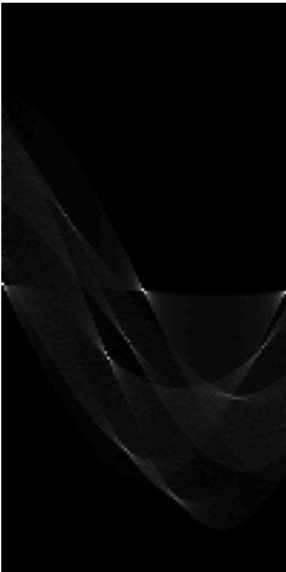
houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=15)

# For large rho/theta values, lines will be of low accuracy
# For samll rho/theta values, result may contain multiple responses for same line.

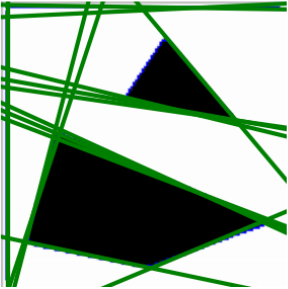
print("--- %s seconds ---" % (time.time() - start_time))
```

```
[[0.0625 0.125  0.0625]
 [0.125  0.25   0.125 ]
 [0.0625 0.125  0.0625]]
(128, 128) (128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128) (128, 128)
```

Accumulator



Hough Edge Lines



--- 1.261528491973877 seconds ---

```
start_time = time.time()

testimage1=np.load("/content/few256.npy")
smalltest1=binsubsample(testimage1)
#scale = [0.0001,1, 2, 4, 16, 64]
#threshold = 0.7
#thresholds=[1,5,10,15,17,20]
scale=4
thresholdd= 5 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)
ntheta = 100 # Number of Accumulator in theta direction
nrho = 200 # Number of Accumulators in rho direction

houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=15)

# For large rho/theta values, lines will be of low accuracy
# For samll rho/theta values, result may contain multiple responses for same line.

print("--- %s seconds ---" % (time.time() - start_time))
```

```
[[0.0625 0.125 0.0625]
 [0.125 0.25 0.125 ]
 [0.0625 0.125 0.0625]]
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)

start_time = time.time()

testimage1=np.load("/content/godthem256.npy")
smalltest1=binsubsample(testimage1)
#scale = [0.0001,1, 2, 4, 16, 64]
#threshold = 0.7
#thresholds=[1,5,10,15,17,20]
scale=10
thresholdd= 1 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)
ntheta = 100 # Number of Accumulator in theta direction
nrho = 200 # Number of Accumulators in rho direction

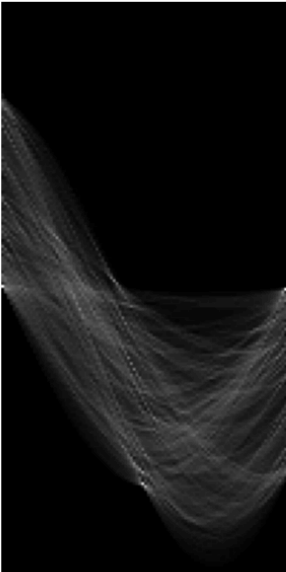
houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=12)

# For large rho/theta values, lines will be of low accuracy
# For samll rho/theta values, result may contain multiple responses for same line.

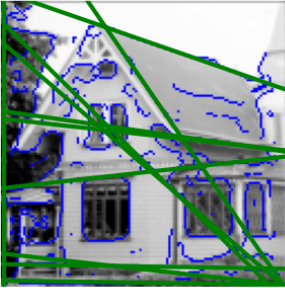
print("--- %s seconds ---" % (time.time() - start_time))

[[0.0625 0.125 0.0625]
 [0.125 0.25 0.125 ]
 [0.0625 0.125 0.0625]]
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
```

Accumulator



Hough Edge Lines



--- 3.19510817527771 seconds ---

**\*Q.9 How do the results and computational time depend on the number of cells in the accumulator? \***

```
start_time = time.time()

testimage1=np.load("/content/houghtest256.npy")
smalltest1=binsubsample(testimage1)

scale=4
thresholdd= 5 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)

ntheta = 200 # Number of Accumulator in theta direction
nrho = 200 # Number of Accumulators in rho direction

houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=15)
print("ntheta:",ntheta," ", "nrho:",nrho)
print("--- %s seconds ---" % (time.time() - start_time))
```

```
[[0.0625 0.125 0.0625]
start_time = time.time()

testimage1=np.load("/content/houghtest256.npy")
smalltest1=binsubsample(testimage1)

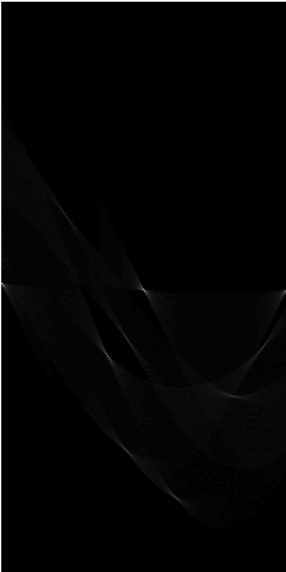
scale=4
thresholdd= 5 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)

ntheta = 200 # Number of Accumulator in theta direction
nrho = 400 # Number of Accumulators in rho direction

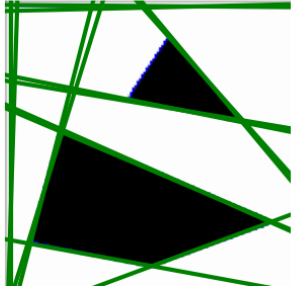
houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=15)
print("ntheta:",ntheta," ", "nrho:",nrho)
print("--- %s seconds ---" % (time.time() - start_time))
```

[[0.0625 0.125 0.0625]
[0.125 0.25 0.125 ]
[0.0625 0.125 0.0625]]
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)
(128, 128) (128, 128) (128, 128)

Accumulator



Hough Edge Lines



ntheta: 200 nrho: 400
--- 2.2067702415618896 seconds ---

```
start_time = time.time()

testimage1=np.load("/content/houghtest256.npy")
smalltest1=binsubsample(testimage1)

scale=4
thresholdd= 5 # Lowest value allowed for given magnitude
edgecurves = extractedge(smalltest1,scale, thresholdd, shape)

ntheta = 200 # Number of Accumulator in theta direction
nrho = 800 # Number of Accumulators in rho direction

houghedgeline(smalltest1, scale, thresholdd, nrho, ntheta, nlines=15)
print("ntheta:",ntheta," ", "nrho:",nrho)
print("--- %s seconds ---" % (time.time() - start_time))
```

