Exercises Functions

Exercise 1.

For the functions

$$f = \{3 \mapsto 9, 4 \mapsto 16, 5 \mapsto 25\}$$

$$g = \{2 \mapsto 7, 3 \mapsto 16, 4 \mapsto 17\})$$

What is the value of the following

- 1. $g \oplus f$
- 2. $f \sim \oplus g \sim$
- 3. $(\{5\} \triangleleft f) \oplus (g \rhd \{17,7\})$
- 4. $(f \cap g) \oplus (f \cup g)$
- 5. $(f \sim g) \oplus g$

Exercise 2.

For any two functions, f and g, in what circumstances could the following be true?

- 1. $f \cup g = f \oplus g$
- $2. \ f \oplus g = g \oplus f$
- 3. $f \cap g = f \oplus g$
- 4. $f \setminus g = f \oplus g$

Exercise 3.

The following does not include functions but allows you to practice schema operations.

Given the following:

[PERSON, MODULE]

Write the following schema operations:

- 1. Add a student s? to the set of registered students.
- 2. Delete a student s? from the system (what are the conditions under which a student can be removed?)
- 3. Add a degree module **degM?** to the set of registered degree modules.
- 4. Delete a degree module **degM?** from the set of registered degree modules (what are the conditions under which a module can be removed?)
- 5. Add a new 'student registers for a module' mapping. (Check preconditions).

Exercise 4.

A warehouse holds stocks of various items *carried* by a company. A computer system records the *level* of all items carried, the *withdrawal* of items from stock and the *delivery* of stock.

Occasionally, a new item will be *carried* and items will be *discontinued*, provided that their stock level is *zero*. The systems state is given as:

[ITEM] the set of all items.

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-Warehouse
-carried : \mathbb{P}ITEM
-level : ITEM \to \mathbb{N}
-level = carried
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Every carried item has a level, even if it is zero.

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Withdraw \\ \Delta Warehouse \\ i?: ITEM \\ qty?: \mathbb{N} \\ \hline i? \in carried \\ leveli? \geq qty? \\ level' = level \oplus \{i? \mapsto level(i?) + qty?\} \\ carried' = carried \\ \hline
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Write schemas for the following operations:

- 1. Deliver a quantity (qty?) of item i? to the warehouse (the item must be already carried). There is no upper limit on stock held.
- 2. Add a new item i? to be carried.
- 3. Discontinue an item (i?). The item must currently be carried and have a stock-level of zero

Functions- Exercises 3