Exercises Relations

** Exercise 1

Given the following sets:

$$A=\{1\}$$

$$B=\{2,3\}$$

Write down the sets:

- 1. $A \times B$
- 2. $\mathbb{P}(A) \times B$
- 3. $\mathbb{P}(A \times B)$
- 4. $(A \times B) \times (A \times B)$

*** Exercise 2

Given the relation

$$R=\{1\mapsto 1, 2\mapsto 4, 3\mapsto 9, 4\mapsto 16, 5\mapsto 25\}$$
 and the set
$$S=\{1,4,5\}$$

Simplify the value of each of the following expressions :

- 1. $S \triangleleft R$
- 2. $R \triangleright S$
- 3. $(S \triangleleft R) \triangleright S$
- 4. $(R \Rightarrow \operatorname{dom} R) \sim \Rightarrow S$

**** Exercise 3

Citing Papers

Given the following:

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\begin{split} &[PAPER]\\ &cites: PAPER \leftrightarrow PAPER\\ &\text{and that}\\ &(paper1, paper2) \in cites \text{ has the meaning that paper1 cites paper2} \;. \end{split}
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Write down the following:

- 1. Write a Z expression for the set of all papers cited directly or indirectly by paper x.
- 2. Write a Z expression for the set of all papers which cite other papers (directly or indirectly) but themselves are not cited (directly or indirectly).
- 3. Write a Z expression which states that if any paper cites another (directly or indirectly) the second one must not cite the first (directly or indirectly).
- 4. Write a Z expression for the number of papers cited directly by paper x.
- 5. Write a Z expression for the number of papers cited directly or indirectly by paper x.

Relations- Exercises 2

**** Exercise 4

Family Relations

Given

[PERSON]

and $parent: PERSON \leftrightarrow PERSON$

 $male, female : \mathbb{P} PERSON$

and that

 $(abe, homer) \in parent$ has the meaning that abe is homer's parent.

- 1. Write a Z expression for each of the following:
 - (a) The parents of person x.
 - (b) The grandparents of person x.
 - (c) The grandchildren of person x.
 - (d) The descendants of person x.
 - (e) The siblings of person x.
 - (f) The aunts of person x.
- 2. Give a Z expression for the set of all people in the database who have no relatives in the database.
- 3. Write an invariant to say that no person can have more than 2 parents.

Relations- Exercises 3