

# Exercises

## Higher-order functions

### Exercise 1

Show how the list comprehension

$$[f\ x \mid x \leftarrow xs, p\ x]$$

can be re-expressed using the higher-order functions *map* and *filter*.

### Exercise 2

Without looking at the definitions from the standard prelude, define the following higher-order library functions on lists.

1. Decide if all elements of a list satisfy a predicate:

$$\mathbf{all} :: (a \rightarrow \mathbf{Bool}) \rightarrow [\mathbf{Bool}] \rightarrow \mathbf{Bool}$$

2. Decide if all elements of a list satisfy a predicate:

$$\mathbf{any} :: (a \rightarrow \mathbf{Bool}) \rightarrow [\mathbf{Bool}] \rightarrow \mathbf{Bool}$$

3. Select elements from a list while they satisfy a predicate:

$$\mathbf{takeWhile} :: (a \rightarrow \mathbf{Bool}) \rightarrow [a] \rightarrow \mathbf{Bool}$$

4. Remove elements from a list while they satisfy a predicate

$$\mathbf{dropWhile} :: (a \rightarrow \mathbf{Bool}) \rightarrow [a] \rightarrow \mathbf{Bool}$$

### Exercise 3

Redefine the functions

**map** f

and

**filter** p

using

**foldr**