# Exercises List Comprehensions

#### \* Exercise 1

Using list comprehension define the list of cubes of the values between (and including) 1 and 10.

squares = 
$$[(1,1),(2,4),(3,9),(4,16),(5,25),(6,36),(7,49),(8,64),(9,81),(10,100)]$$

# \* Exercise 2

Using list comprehension define the following list (note that the second element in the 2-tuple is always 1.

$$myConstFunc = [(1,1),(2,1),(3,1),(4,1),(5,1)]$$

# \*\* Exercise 3

Write down the values as defined in the following lists 11, 12, 13. Check your answers.

f1 :: 
$$[(Int, Int)]$$
  
f1 =  $[(x, y) | x < -[1..3], y < [4..5]]$   
f2 ::  $[(Int, Int)]$   
f2 =  $[(x, y) | y < [4..5], x < -[1..3]]$   
f3 ::  $[(Int, Int)]$   
f3 =  $[(y, x) | x < -[1..3], y < [4..5]]$ 

#### \*\* Exercise 4

Given the following definition of

```
isEven :: Integer -> Bool
isEven n = (n 'mod' 2 == 0)
```

Write down the values as defined in the following list: Check your answer.

$$[2*n \mid n \leftarrow [2,4,7], \text{ isEven } n, n>3]$$

# \*\* Exercise 5

Give a definition of a function

which doubles all the elements of a list of integers.

# \*\* Exercise 6

Give a definition of a function

which converts all small letters in a String into capitals.

*Hint*: You can use the following function (having imported Data.Char):

import Data.Char

toupper :: Char -> Char

# \*\* Exercise 7

Using a list comprehension, give an expression that calculates the sum of

$$\sum_{i=1}^{i=100} i^2$$

# \*\* Exercise 8

Using a list comprehension, write a function sigma'

$$sigma' :: Int \rightarrow Int$$

that takes an integer n and calculates

$$\sum_{i=1}^{i=n} i^2$$

# \*\*\*\* Exercise 9

Define the function

matches :: Integer -> [Integer] -> [Integer]

which picks out all occurences of an integer in a list. For instance:

Using matches or otherwise, define a function

elem':: Integer -> [Integer] -> Bool --elem is already defined in Prelude which is True is the Integer is an element of the list, and False otherwise.

# \*\*\* Exercise 10

Suppose that a *coordinate grid* of size m x n is given by the list of all pairs (x,y) of integers such that  $0 \le x \le m$  and  $0 \le y \le n$ . Using a list comprehension, define a function:

```
grid :: Int -> Int -> [(Int, Int)]
```

that returns a coordinate grid of a given size. For example:

```
[*Main> grid 1 2
[(0,0),(0,1),(0,2),(1,0),(1,1),(1,2)]
*Main>
```

# \*\*\* Exercise 11

Using a list comprehension and the function **grid** above, define a function

```
square :: Int -> [(Int, Int)]
```

that returns a coordinate square of size n, excluding the diagonal from (0,0) to (n,n). For example:

```
[*Main> square 2
[(0,1),(0,2),(1,0),(1,2),(2,0),(2,1)]
*Main> ■
```

#### \*\*\* Exercise 12

In a similar way to the function *length*, show how the library function

```
replicate :: Int \rightarrow a \rightarrow [a]
```

that produces a list of identical elements can be defined using list comprehension. (Call your version **myReplicate**) For example:

# \*\*\* Exercise 13

A triple (x, y, z) of positive integers is called pythagorean if  $x^2 + y^2 = z^2$ . Using a list comprehension, define a function

```
pyths :: Int -> [(Int,Int,Int)]
```

that returns a list of all such triples whose components are at most a given limit. For example

# \*\*\*\* Exercise 14

A positive integer is perfect if it equals the sum of all of its factors, excluding the number itself. Using a list comprehension and the function **factors**, define a function

```
perfects :: Int -> [Int]
```

that returns the list of all perfect numbers up to a given limit. For example:

# Solutions

#### Solution to Exercise 1

```
cubes :: [Int] cubes = [x^3 | x \leftarrow [1..10]]
```

#### Solution to Exercise 2

```
\begin{array}{ll} myConstFunc & :: & [\left(\mathbf{Int}\,,\;\mathbf{Int}\,\right)] \\ myConstFunc & = & \left[\left(\,x\,,\;\;1\right)|\;\;x<-\;\;\left[\,1\,..\,5\,\right]\,\right] \end{array}
```

#### Solution to Exercise 3

```
11 = [(1,4),(1,5),(2,4),(2,5),(3,4),(3,5)]
12 = [(1,4),(2,4),(3,4),(1,5),(2,5),(3,5)]
13 = [(4,1),(5,1),(4,2),(5,2),(4,3),(5,3)]
```

#### Solution to Exercise 4

[8]

#### Solution to Exercise 5

```
doubleAll :: [Integer] \rightarrow [Integer] doubleAll ns = [n*2 \mid n < -ns]
```

#### Solution to Exercise 6

```
capitalize :: String -> String
capitalize xs = [toUpper(c) | c<- xs ]</pre>
```

#### Solution to Exercise 7

#### Solution to Exercise 8

```
sigma' :: Int \rightarrow Int

sigma' n = sum[x^2 | x \leftarrow [1..n]]
```

# Solution to Exercise 9

 $\begin{array}{lll} \textbf{elem} \, ' :: & \textbf{Integer} \, -\!\!\!\!> \, [\, \textbf{Integer} \,] \, -\!\!\!\!> \, \textbf{Bool} \\ \textbf{elem} \, ' \, \times \, \times s \, = \, \text{matches} \, \times \, \times s \, \, \, /\!\!\!= \, [\,] \end{array}$