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The Caesar Cypher

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Caesar Cipher

Example of string encoding with constant shift factor of 3 ...

- "abc" would be encoded to "def"
- "haskell is fun" would be encoded to "kdnnhoo lv ixg"

More Generally

With a shift factor of 4, for example:

• "abc" would be encoded to "def"

How will we use Haskell to implement the Caesar and more \dots

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Encoding and Decoding

import Data. Char — imports standard function

For simplicity, we will only encode the lower-case characters within a string and leave the other characters unchanged. Firstly

```
let2Int :: Char -> Int
let2Int c = ord c - ord 'a'
```

```
int2Let :: Int -> Char
int2Let n = chr (ord 'a' + n)
```

We can see them called in Figure 1

```
*Main> let2int 'a'
0
*Main> int2let 0
'a'
```

Figure: Calling int2let and let2in

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Encoding and Decoding contd.

We define a function *shift* as follows:

```
isLower :: Char -> Bool returns True if it's a lower-case letter. )
```

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Encoding and Decoding contd.

Using *shift* within a list comprehension, it is now easy to define a function that encodes a string using a given string factor.

```
encode :: Int \rightarrow String \rightarrow String encode n xs = [shift n x | x <- xs]
```

We call this as shown in Fig 2

```
*Main> encode 3 "haskell is fun"
"kdvnhoo lv ixq"
*Main> encode (-3) "kdvnhoo lv ixq"
"haskell is fun"
```

Figure: Calling encode with positive and negative values

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Frequency Tables

Table of approximate percentage frequencies of the twenty-six letters of the alphabet :

```
table :: [Float] table = [8.1, 1.5, 2.8, 4.1, 12.7, 2.2, 2.0, 6.1, 7.0, 0.2, 0.8, 4.0, 2.4, 6.7, 7.5, 1.9, 0.1, 6.0, 6.3, 9.0, 2.8, 1.0, 2.4, 0.2, 2.0, 0.1]
```

we define a percent function

```
percent :: Int -> Int -> Float
percent n m =
    (fromIntegral n / fromIntegral m ) * 100
```

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Frequency Tables cont.

We now look at producing a frequency table for a string. We use *count* and *lowers* as follows:

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Frequency Tables cont.

```
\begin{array}{lll} \text{freqs} & :: & \textbf{String} \rightarrow [\textbf{Float}] \\ \text{freqs} & \text{xs} = [\text{percent (count x xs) n } | \\ & & \text{x} < - \text{['a'...'z']}] \\ & & \textbf{where n} = \text{lowers xs} \end{array}
```

We can see how it's called in Fig 3



Figure: Calling freqs on a string

the letter 'a' occurs with a frequency of approximately 6.6%, the letter 'b' with a frequency of 13.3% etc.

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Frequency Tables cont.

A standard method for comparing

- a list of observed frequencies os with
- a list of expected frequencies es

is the *chi-square statistic*, defined by the following summation in which n denotes the length of the two lists.

$$\sum_{i=0}^{n-1} \frac{(os_i - es_i)^2}{es_i}$$

Frequency tables

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Frequency Tables cont.

Using *zip* and list comprehension we translate the previous formula into code

```
chisqr :: [Float] \rightarrow [Float] \rightarrow Float chisqr os es = sum [((o-e)^2)/e | (o,e) <- zip os es]
```

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Now, we define a function that rotates the elements of a list n places the left, wrapping around the start of the list, and assuming that the integer arguments n is between 0 and the length of the list

Now, suppose that we are given an encoded string, but not the shift factor that was used to encode it, and wish to determine this number in order that we can decode the string. This can usually be achieved by producing the frequency table of the encoded string, calculating the chi-square statistic for each possible rotation of the table with respect to the table of expected frequencies, and using the position of the minimum chi-square value as the shift factor. For example, if we let table

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table ' = freqs "kdvnhoo_lv_ixq"

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For example:

crack "kdvnhoo_lv_ixq"

"haskell_is_fun"