

Exercises

Higher-order functions

*** Exercise 1

Show how the list comprehension

$$[f\ x \mid x \leftarrow xs, p\ x]$$

can be re-expressed using the higher-order functions *map* and *filter*.

*** Exercise 2

Without looking at the definitions from the standard prelude, define the following higher-order library functions on lists.

1. Decide if all elements of a list satisfy a predicate:

all :: (a -> Bool) -> [Bool] -> Bool

2. Decide if all elements of a list satisfy a predicate:

any :: (a -> Bool) -> [Bool] -> Bool

3. Select elements from a list while they satisfy a predicate:

takeWhile :: (a -> Bool) -> [a] -> Bool

4. Remove elements from a list while they satisfy a predicate

dropWhile :: (a -> Bool) -> [a] -> Bool

**** Exercise 3

Redefine the functions

map f

and

filter p

using

foldr

**** Exercise 4

Noting that *String* is the same as *[Char]*. Define a function *capitalises*, of type *String* \rightarrow *String*, which takes a list of characters as its argument and returns the same list as its value except that each lower-case letter has been replaced by its upper-case equivalent. Thus, *capitalises* "Bohemian Rhapsody" = "BOHEMIAN RHAPSODY".

Hint: Use *toupper* which returns the uppercase of a letter and *map*. This should be written as a function-level definition.

*** Exercise 5

Define a function *squareall* :: *[Int]* \rightarrow *[Int]* which takes a list of integers and produces a list of the squares of those integers. For example, *squareall*[6, 1, (-3)] = [36, 1, 9].

Hint: Using *map*, this should be written as a function-level definition.

**** Exercise 6

Define a function *nestedreverse* which takes a list of strings as its argument and reverses each element of the list and then reverses the resulting list. Thus, *nestedreverse* ["in", "the", "end"] = ["dne", "eht", "ni"].

Hint: Using *map*, this should be written as a function-level definition.

**** Exercise 7

Define a function *atfront* :: *a* \rightarrow *[[a]]* \rightarrow *[[a]]* which takes an object and a list of lists and prepends the object at the front of every component list. For example,

atfront 7 [[1, 2], [], [3]] = [[7, 1, 2], [7], [7, 3]].

Hint: Using *map*, this should be written as a function-level definition.

*** Exercise 8

Define a function *lengths* which takes a list of strings as its argument and returns the list of their lengths. For example,

lengths ["the", "end", "is", "nigh"] = [3, 3, 2, 4].

Hint: Using *map*, this may be written as an object-level definition.

*** Exercise 9

Using the higher-order function *map* define a function *sumsq* which takes an integer *n* as its argument and returns the sum of the squares of the first *n* integers. That is to say, *sumsq* *n* = $1^2 + 2^2 + 3^2 + \dots + n^2$

**** Exercise 10

The function *filter* can be defined in terms of *concat* and *map*:

```
filter p = concat.map box where box x = ...
```

***** Exercise 11**

Define a function *wvowel* (without vowels) which removes every occurrence of a vowel from a list of characters.

****** Exercise 12**

Define a function *wiv* (without internal vowels) which takes a list of strings as its argument and removes every occurrence of a vowel from each element. For example,

```
wiv ["the", "end", "is", "nigh"] = ["th", "nd", "s", "ngh"]
```

Solutions

Solutions to exercise 4

```
capitalises :: String -> String
capitalises = map toUpper
```

Solutions to exercise 5

```
squareall :: [Int] -> [Int]
squareall = map (\x -> x*x)
```

Solutions to exercise 6

```
nestedreverse :: [String] -> [String]
nestedreverse = reverse . map reverse
```

Solutions to exercise 7

```
atfront :: a -> [[a]] -> [[a]]
atfront x = map (x:)
```

Solutions to exercise 8

```
lengths :: [String] -> [Int]
lengths = map length
```

Solutions to exercise 9

```
square :: Num a => a -> a
square x = x * x
sumsq :: Integral a => a -> a
sumsq n = sum (map square [1..n])
```

Solutions to exercise 10

```
filter1 :: (a -> Bool) -> [a] -> [a]
filter1 p = concat.map box
where box x
      | p x = [x]
      | otherwise = []
```

Solutions to exercise 11

```
wvowel :: String -> String
wvowel xs = filter f xs where f x = not (x == 'a' ||
                                           x == 'e' ||
                                           x == 'i' ||
                                           x == 'o' ||
                                           x == 'u' )
```

Solutions to exercise 12

```
wiv :: [String] -> [String]
wiv = map wvowel
```