

The Caesar Cypher

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1 Introduction

A well known method of encoding a string in order to disguise its contents is the *Caesar Cipher*, named after its use by Julius Caesar. To encode a string, Caesar simply replaced each letter in the string by the letter places further down in the alphabet.

Caesar Cipher

Example of string encoding with constant shift factor of 3 ...

- "abc" would be encoded to "def"
- "haskell is fun" would be encoded to "kdnnhoo lv ixq"

More Generally the specific shift factor of three used by Caesar can be replaced by any integer between one and twenty-five, thereby giving twenty-five different ways of encoding a string. So, more generally, with

With a shift factor of 4, for example:

- "abc" would be encoded to "def"

How will we use Haskell to implement the Caesar and more ...

2 Encoding and decoding

We will use a number of standard functions on characters that are provided in a library called *Data.Char* which can be loaded into a Haskell script by including the following declaration at the start of the script

Encoding and Decoding

```
import Data.Char  — imports standard functions on characters
```

For simplicity, we will only encode the lower-case characters within a string and leave the other characters unchanged. Firstly *chr* and *ord* are *Data.Char* functions. *chr* returns a character given its ordinal number. *ord* returns a given character's ordinal number.

```
*Main> let2int 'a'
0
*Main> int2let 0
'a'
```

Figure 1: Calling int2let and let2int

```
let2Int :: Char -> Int
let2Int c = ord c - ord 'a'
```

```
int2Let :: Int -> Char
int2Let n = chr (ord 'a' + n)
```

We can see them called in Figure ??

Encoding and Decoding contd.

We define a function *shift* that applies a shift factor to a lower-case letter by converting the letter into the corresponding integer, adding on the shift factor and taking the remainder when divided by 26 (thereby wrapping around the end of the alphabet) and converting the resulting integer back into a lower-case letter.

```
• shift :: Int -> Char -> Char
  shift n c | isLower c = int2let (
              (let2int c + n) `mod` 26)
            | otherwise = c
```

(The library function

```
isLower :: Char -> Bool
```

returns True if it's a lower-case letter.)

Encoding and Decoding contd.

Using *shift* within a list comprehension, it is now easy to define a function that encodes a string using a given string factor.

```
encode :: Int -> String -> String
encode n xs = [shift n x | x <- xs]
```

We call this as shown in Fig ??

3 Frequency tables

We now look at cracking the Caesar Cipher. The key to this is the observation that some letters are used more frequently than others in English text. By analysing a large volume of such text one can derive the following table of approximate percentage frequencies of the twenty-six letters of the alphabet :

```
*Main> encode 3 "haskell is fun"
"kdvnhoo lv ixq"
*Main> encode (-3) "kdvnhoo lv ixq"
"haskell is fun"
```

Figure 2: Calling `encode` with positive and negative values

Frequency Tables

```
table :: [Float]
table = [8.1, 1.5, 2.8, 4.1, 12.7, 2.2, 2.0,
        6.1, 7.0, 0.2, 0.8, 4.0, 2.4, 6.7,
        7.5, 1.9, 0.1, 6.0, 6.3, 9.0, 2.8,
        1.0, 2.4, 0.2, 2.0, 0.1]
```

For example, the letter 'e' occurs most often, with a frequency of 12.7% while 'q' and 'z' occur least often with a frequency of just 0.1%. It is also useful to produce frequency tables for individual strings. To this end, we first define a function that calculates the percentage of one integer with respect to another, returning the result as a floating point number. This function uses `fromIntegral` which is a library function converts an integer into a floating point number

```
percent :: Int -> Int -> Float
percent n m =
    (fromIntegral n / fromIntegral m) * 100
```

Frequency Tables cont.

We now look at producing a frequency table for a string. We use *count* and *lowers* as follows:

```
count :: Eq a => a -> [a] -> Int
count x xs = length [ x' | x' <- xs, x==x' ]
```

```
lowers :: [Char] -> Int
lowers xs =
    length [x | x <- xs,
               x >= 'a' && x <= 'z']
```

Frequency Tables cont.

```
freqs :: String -> [Float]
freqs xs = [percent (count x xs) n |
            x <- ['a'.. 'z']]
    where n = lowers xs
```

We can see how it's called in Fig ??

That is, the letter 'a' occurs with a frequency of approximately 6.6%, the letter 'b' with a frequency of 13.3% etc. The use of the *lowers* function ensures that the percentages are based only on the total number of lower-case letters.


```
[chisqr (rotate ' n table ') table | n <- [0..25]]  
will give us
```

```
[1409.1558,639.92175,612.2969,  
202.32024, 1440.2488, 4247.621, 650.89923, ...]
```

```
crack :: String -> String  
crack xs = encode (-factor) xs  
  where  
    factor = head (positions  
      ( minimum chitab) chitab )  
    chitab = [chisqr (rotate ' n table ') table |  
      n <- [0..25]]  
    table ' = freqs xs
```

For example:

```
crack "kdvnhoo_lv_ixq"
```

```
"haskell_is_fun"
```