Exercises Higher-order functions

*** Exercise 1

Show how the list comprehension

$$[f x \mid x \leftarrow xs, p x]$$

can be re-expressed using the higher-order functions map and filter.

*** Exercise 2

Without looking at the definitions from the standard prelude, define the following higher-order library functions on lists.

1. Decide if all elements of a list satisfy a predicate:

$$all \ :: \ (a \ -\!\!\!> Bool) \ -\!\!\!\!> \ [Bool] \ -\!\!\!\!> Bool$$

2. Decide if all elements of a list satisfy a predicate:

$$\mathbf{any} \ :: \ (\mathtt{a} \ {\mathord{\text{--}}} \mathsf{Bool}) \ {\mathord{\text{--}}} \mathsf{bool} \ {\mathord{\text{--}}} \mathsf{bool}$$

3. Select elements from a list while they satisfy a predicate:

$$\mathbf{takeWhile} \ :: \ (\mathtt{a} \ -\!\!\!> \ \mathbf{Bool}) \ -\!\!\!\!> \ [\mathtt{a}] \ -\!\!\!\!> \ \mathbf{Bool}$$

4. Remove elements from a list while they satisfy a predicate

$$\mathbf{dropWhile} \ :: \ (\mathtt{a} \ -\!\!\!> \ \mathbf{Bool}) \ -\!\!\!\!> \ [\mathtt{a}] \ -\!\!\!\!> \ \mathbf{Bool}$$

**** Exercise 3

Redefine the functions

map f

and

filter p

using

foldr

**** Exercise 4

Noting that String is the same as [Char]. Define a function *capitalises*, of type $String \rightarrow String$, which takes a list of characters as its argument and returns the same list as its value except that each lower-case letter has been replaced by its upper-case equivalent. Thus,

capitalises "Bohemian Rhapsody" = "BOHEMIAN RHAPSODY".

Hint: Use *toupper* which returns the uppercase of a letter and *map*. This should be written as a function-level definition.

*** Exercise 5

Define a function $squareall :: [Int] \to [Int]$ which takes a list of integers and produces a list of the squares of those integers. For example, squareall[6, 1, (-3)] = [36, 1, 9].

Hint: Using map, this should be written as a function-level definition.

**** Exercise 6

Define a function nested reverse which takes a list of strings as its argument and reverses each element of the list and then reverses the resulting list. Thus, nested reverse ["in", "the", "end"] = ["dne", "eht", "ni"].

Hint: Using map, this should be written as a function-level definition.

**** Exercise 7

Define a function $atfront :: a \to [[a]] \to [[a]]$ which takes an object and a list of lists and prepends the object at the front of every component list. For example,

at $front \ 7 \ [[1,2],[],[3]] = [[7,1,2],[7],[7]].$

Hint: Using map, this should be written as a function-level definition.

*** Exercise 8

Define a function lengths which takes a list of strings as its argument and returns the list of their lengths. For example,

lengths ["the", "end", "is", "nigh"] = [3, 3, 2, 4].

Hint: Using map, this may be written as an object-level definition.

*** Exercise 9

Using the higher-order function map define a function sumsq which takes an integer n as its argument and returns the sum of the squares of the first n integers. That is to say, $sumsq n = 1^2 + 2^2 + 3^2 + \ldots + n^2$

**** Exercise 10

The function filter can be defined in terms of concat and map:

filter p = concat.map box where box <math>x = ...

*** Exercise 11

Define a function wvowel (without vowels) which removes every occurrence of a vowel from a list of characters.

**** Exercise 12

Define a function wiv (without internal vowels) which takes a list of strings as its argument and removes every occurrence of a vowel from each element. For example,