# The Caesar Cypher

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February 4, 2019

# Caesar Cipher

#### Example of string encoding with constant shift factor of 3 ...

- "abc" would be encoded to "def"
- "haskell is fun" would be encoded to "kdnnhoo lv ixq"

#### More Generally

With a shift factor of 4, for example:

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How will we use Haskell to implement the Caesar and more ...

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# **Encoding and Decoding**

# import Data. Char — imports standard function

For simplicity, we will only encode the lower-case characters within a string and leave the other characters unchanged. Firstly

```
let2Int :: Char \rightarrow Int
let2Int c = ord c - ord 'a'
```

```
int2Let :: Int -> Char
int2Let n = chr (ord 'a' + n)
```

We can see them called in Figure 1

```
*Main> let2int 'a'
0
*Main> int2let 0
'a'
```

Figure: Calling int2let and let2in

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Figure: Calling int2let and let2int

# Encoding and Decoding contd.

We define a function *shift* as follows:

returns True if it's a lower-case letter. )

# Encoding and Decoding contd.

Using *shift* within a list comprehension, it is now easy to define a function that encodes a string using a given string factor.

```
encode :: Int \rightarrow String \rightarrow String encode n xs = [shift n x | x <- xs]
```

We call this as shown in Fig 2

```
*Main> encode 3 "haskell is fun"
"kdvnhoo lv ixq"
*Main> encode (-3) "kdvnhoo lv ixq"
"haskell is fun"
```

Figure: Calling encode with positive and negative values

#### Frequency Tables

Table of approximate percentage frequencies of the twenty-six letters of the alphabet :

```
table :: [Float] table = [8.1, 1.5, 2.8, 4.1, 12.7, 2.2, 2.0, 6.1, 7.0, 0.2, 0.8, 4.0, 2.4, 6.7, 7.5, 1.9, 0.1, 6.0, 6.3, 9.0, 2.8, 1.0, 2.4, 0.2, 2.0, 0.1]
```

we define a percent function

```
percent :: Int -> Int -> Float
percent n m =
    (fromIntegral n / fromIntegral m ) * 100
```

We now look at producing a frequency table for a string. We use *count* and *lowers* as follows:

We can see how it's called in Fig 3



Figure: Calling freqs on a string

the letter 'a' occurs with a frequency of approximately 6.6%, the letter 'b' with a frequency of 13.3% etc.

A standard method for comparing

- a list of observed frequencies os with
- a list of expected frequencies es

is the *chi-square statistic*, defined by the following summation in which n denotes the length of the two lists.

$$\sum_{i=0}^{n-1} \frac{(os_i - es_i)^2}{es_i}$$

Using *zip* and list comprehension we translate the previous formula into code

Now, we define a function that rotates the elements of a list n places the left, wrapping around the start of the list, and assuming that the integer arguments n is between 0 and the length of the list

```
rotate :: Int \rightarrow [a] \rightarrow [a]
rotate n xs = drop n xs ++ take n xs
```

Now, suppose that we are given an encoded string, but not the shift factor that was used to encode it, and wish to determine this number in order that we can decode the string. This can usually be achieved by producing the frequency table of the encoded string, calculating the chi-square statistic for each possible rotation of the table with respect to the table of expected frequencies, and using the position of the minimum chi-square value as the shift factor. For example, if we let table

table ' = freqs "kdvnhoo\_lv\_ixq"

```
ММ
```

```
[chisqr (rotate'n table') table | n <- [0 will give us  [1409.1558,639.92175,612.2969, \\ 202.32024, 1440.2488, 4247.621, 650.89923 ]
```

For example:

crack "kdvnhoo\_lv\_ixq"

"haskell\_is\_fun"