

# 1\_Multiple Linear Regression

October 17, 2021

## 1 Multiple Linear Regression

### 1.1 Importing the libraries

```
[1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

```
[2]: from sklearn.impute import SimpleImputer
from sklearn.compose import ColumnTransformer
from sklearn.preprocessing import OneHotEncoder
from sklearn.preprocessing import LabelEncoder
```

```
[3]: from sklearn.model_selection import train_test_split
```

```
[4]: from sklearn.linear_model import LinearRegression
```

```
[5]: import statsmodels.api as sm
```

```
[6]: import seaborn as sns
```

### 1.2 Importing the data set

```
[7]: data_set = pd.read_csv("housing.csv")
print(data_set)
```

	price	area	bedrooms	bathrooms	stories	mainroad	guestroom	basement	\
0	13300000	7420	4	2	3	yes	no	no	
1	12250000	8960	4	4	4	yes	no	no	
2	12250000	9960	3	2	2	yes	no	yes	
3	12215000	7500	4	2	2	yes	no	yes	
4	11410000	7420	4	1	2	yes	yes	yes	
..	...	...	...	...	...	...	...	...	
540	1820000	3000	2	1	1	yes	no	yes	
541	1767150	2400	3	1	1	no	no	no	
542	1750000	3620	2	1	1	yes	no	no	
543	1750000	2910	3	1	1	no	no	no	
544	1750000	3850	3	1	2	yes	no	no	

	hotwaterheating	airconditioning	parking	prefarea	furnishingstatus
0	no	yes	2	yes	furnished
1	no	yes	3	no	furnished
2	no	no	2	yes	semi-furnished
3	no	yes	3	yes	furnished
4	no	yes	2	no	furnished
..	...	...	...	...	...
540	no	no	2	no	unfurnished
541	no	no	0	no	semi-furnished
542	no	no	0	no	unfurnished
543	no	no	0	no	furnished
544	no	no	0	no	unfurnished

[545 rows x 13 columns]

```
[8]: x = data_set.iloc[:,1:].values
     y = data_set.iloc[:,0].values
```

```
[9]: print(x)
```

```
[[7420 4 2 ... 2 'yes' 'furnished']
 [8960 4 4 ... 3 'no' 'furnished']
 [9960 3 2 ... 2 'yes' 'semi-furnished']
 ...
 [3620 2 1 ... 0 'no' 'unfurnished']
 [2910 3 1 ... 0 'no' 'furnished']
 [3850 3 1 ... 0 'no' 'unfurnished']]
```

```
[10]: print(y)
```

```
[13300000 12250000 12250000 12215000 11410000 10850000 10150000 10150000
 9870000 9800000 9800000 9681000 9310000 9240000 9240000 9100000
 9100000 8960000 8890000 8855000 8750000 8680000 8645000 8645000
 8575000 8540000 8463000 8400000 8400000 8400000 8400000 8400000
 8295000 8190000 8120000 8080940 8043000 7980000 7962500 7910000
 7875000 7840000 7700000 7700000 7560000 7560000 7525000 7490000
 7455000 7420000 7420000 7420000 7350000 7350000 7350000 7350000
 7343000 7245000 7210000 7210000 7140000 7070000 7070000 7035000
 7000000 6930000 6930000 6895000 6860000 6790000 6790000 6755000
 6720000 6685000 6650000 6650000 6650000 6650000 6650000 6650000
 6629000 6615000 6615000 6580000 6510000 6510000 6510000 6475000
 6475000 6440000 6440000 6419000 6405000 6300000 6300000 6300000
 6300000 6300000 6293000 6265000 6230000 6230000 6195000 6195000
 6195000 6160000 6160000 6125000 6107500 6090000 6090000 6090000
 6083000 6083000 6020000 6020000 6020000 5950000 5950000 5950000
 5950000 5950000 5950000 5950000 5950000 5943000 5880000 5880000
 5873000 5873000 5866000 5810000 5810000 5810000 5803000 5775000
 5740000 5740000 5740000 5740000 5740000 5652500 5600000 5600000
 5600000 5600000 5600000 5600000 5600000 5600000 5600000 5565000]
```

5565000	5530000	5530000	5530000	5523000	5495000	5495000	5460000
5460000	5460000	5460000	5425000	5390000	5383000	5320000	5285000
5250000	5250000	5250000	5250000	5250000	5250000	5250000	5250000
5250000	5243000	5229000	5215000	5215000	5215000	5145000	5145000
5110000	5110000	5110000	5110000	5075000	5040000	5040000	5040000
5040000	5033000	5005000	4970000	4970000	4956000	4935000	4907000
4900000	4900000	4900000	4900000	4900000	4900000	4900000	4900000
4900000	4900000	4900000	4900000	4893000	4893000	4865000	4830000
4830000	4830000	4830000	4795000	4795000	4767000	4760000	4760000
4760000	4753000	4690000	4690000	4690000	4690000	4690000	4690000
4655000	4620000	4620000	4620000	4620000	4620000	4613000	4585000
4585000	4550000	4550000	4550000	4550000	4550000	4550000	4550000
4543000	4543000	4515000	4515000	4515000	4515000	4480000	4480000
4480000	4480000	4480000	4473000	4473000	4473000	4445000	4410000
4410000	4403000	4403000	4403000	4382000	4375000	4340000	4340000
4340000	4340000	4340000	4319000	4305000	4305000	4277000	4270000
4270000	4270000	4270000	4270000	4270000	4235000	4235000	4200000
4200000	4200000	4200000	4200000	4200000	4200000	4200000	4200000
4200000	4200000	4200000	4200000	4200000	4200000	4200000	4200000
4193000	4193000	4165000	4165000	4165000	4130000	4130000	4123000
4098500	4095000	4095000	4095000	4060000	4060000	4060000	4060000
4060000	4025000	4025000	4025000	4007500	4007500	3990000	3990000
3990000	3990000	3990000	3920000	3920000	3920000	3920000	3920000
3920000	3920000	3885000	3885000	3850000	3850000	3850000	3850000
3850000	3850000	3850000	3836000	3815000	3780000	3780000	3780000
3780000	3780000	3780000	3773000	3773000	3773000	3745000	3710000
3710000	3710000	3710000	3710000	3703000	3703000	3675000	3675000
3675000	3675000	3640000	3640000	3640000	3640000	3640000	3640000
3640000	3640000	3640000	3633000	3605000	3605000	3570000	3570000
3570000	3570000	3535000	3500000	3500000	3500000	3500000	3500000
3500000	3500000	3500000	3500000	3500000	3500000	3500000	3500000
3500000	3500000	3500000	3500000	3493000	3465000	3465000	3465000
3430000	3430000	3430000	3430000	3430000	3430000	3423000	3395000
3395000	3395000	3360000	3360000	3360000	3360000	3360000	3360000
3360000	3360000	3353000	3332000	3325000	3325000	3290000	3290000
3290000	3290000	3290000	3290000	3290000	3290000	3255000	3255000
3234000	3220000	3220000	3220000	3220000	3150000	3150000	3150000
3150000	3150000	3150000	3150000	3150000	3150000	3143000	3129000
3118850	3115000	3115000	3115000	3087000	3080000	3080000	3080000
3080000	3045000	3010000	3010000	3010000	3010000	3010000	3010000
3010000	3003000	2975000	2961000	2940000	2940000	2940000	2940000
2940000	2940000	2940000	2940000	2870000	2870000	2870000	2870000
2852500	2835000	2835000	2835000	2800000	2800000	2730000	2730000
2695000	2660000	2660000	2660000	2660000	2660000	2660000	2660000
2653000	2653000	2604000	2590000	2590000	2590000	2520000	2520000
2520000	2485000	2485000	2450000	2450000	2450000	2450000	2450000
2450000	2408000	2380000	2380000	2380000	2345000	2310000	2275000
2275000	2275000	2240000	2233000	2135000	2100000	2100000	2100000

```
1960000 1890000 1890000 1855000 1820000 1767150 1750000 1750000
1750000]
```

## 2 Taking care of missing data

```
[11]: imputer = SimpleImputer(missing_values = np.nan, strategy="mean")
imputer.fit(x[:,0:4])
x[:,0:4] = imputer.transform(x[:,0:4])
print(x)
```

```
[[7420.0 4.0 2.0 ... 2 'yes' 'furnished']
 [8960.0 4.0 4.0 ... 3 'no' 'furnished']
 [9960.0 3.0 2.0 ... 2 'yes' 'semi-furnished']
 ...
 [3620.0 2.0 1.0 ... 0 'no' 'unfurnished']
 [2910.0 3.0 1.0 ... 0 'no' 'furnished']
 [3850.0 3.0 1.0 ... 0 'no' 'unfurnished']]
```

### 2.1 Encoding categorical data

```
[12]: le = LabelEncoder()
for i in range(4,9):
    x[:,i]=le.fit_transform(x[:, i])
x[:,10] = le.fit_transform(x[:, 10])
df2 = pd.DataFrame(x,
                    columns=['area', 'bedrooms', 'bathrooms', 'stories', 'mainroad', 'guestroom', 'basement', 'hotwaterheating', 'airconditioning', 'parking', 'prefarea', 'furnishingstatus'])
print(df2)
```

	area	bedrooms	bathrooms	stories	mainroad	guestroom	basement	\
0	7420.0	4.0	2.0	3.0	1	0	0	
1	8960.0	4.0	4.0	4.0	1	0	0	
2	9960.0	3.0	2.0	2.0	1	0	1	
3	7500.0	4.0	2.0	2.0	1	0	1	
4	7420.0	4.0	1.0	2.0	1	1	1	
..	...	...	...	...	...	...	...	
540	3000.0	2.0	1.0	1.0	1	0	1	
541	2400.0	3.0	1.0	1.0	0	0	0	
542	3620.0	2.0	1.0	1.0	1	0	0	
543	2910.0	3.0	1.0	1.0	0	0	0	
544	3850.0	3.0	1.0	2.0	1	0	0	

	hotwaterheating	airconditioning	parking	prefarea	furnishingstatus
0	0	1	2	1	furnished
1	0	1	3	0	furnished
2	0	0	2	1	semi-furnished
3	0	1	3	1	furnished
4	0	1	2	0	furnished

..	...	...	...	...	...
540	0	0	2	0	unfurnished
541	0	0	0	0	semi-furnished
542	0	0	0	0	unfurnished
543	0	0	0	0	furnished
544	0	0	0	0	unfurnished

[545 rows x 12 columns]

```
[13]: ct = ColumnTransformer(transformers=[('encoder', OneHotEncoder(), [-1])],
    ↳ remainder = 'passthrough')
x = ct.fit_transform(x)
```

```
[14]: print(x)
```

```
[[1.0 0.0 0.0 ... 1 2 1]
 [1.0 0.0 0.0 ... 1 3 0]
 [0.0 1.0 0.0 ... 0 2 1]
 ...
 [0.0 0.0 1.0 ... 0 0 0]
 [1.0 0.0 0.0 ... 0 0 0]
 [0.0 0.0 1.0 ... 0 0 0]]
```

```
[15]: x = x[:, 1:]
```

## 2.2 Splitting the dataset into the Training set and Test set

```
[16]: x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.2, random_state=
    ↳ 0)
```

## 2.3 Training Multiple linear Regression Model on Training set

```
[17]: Regressor = LinearRegression()
Regressor.fit(x_train, y_train)
```

```
[17]: LinearRegression()
```

## 2.4 Predict Test Result

```
[18]: y_predict = Regressor.predict(x_test)
print(y_predict)
```

```
[ 3950288.61876196  6173868.81883061  4483635.98836272  7258732.75105198
 2836727.58490499  7032947.0974906   3203851.47112406  3270994.00904074
 3472554.03645932  8289978.32623682  6605321.62954614  3723366.23684106
 3812376.95976104  4548966.84544599  4020476.3484966   1969836.22090165
 4057262.98087856  3704586.86711732  3282767.93188815  4609423.64909571
 5968243.73637128  6363698.62063799  4751300.32389003  2659595.27633066
 5305573.24662102  5680819.58784482  5404106.90027122  5543050.5219253]
```

```

5768360.4798223  5801753.70839269  3389277.96110617  6399092.02678457
7081030.31411738  2913042.40387681  4498664.01335446  5210561.68059354
5013457.84122302  3707596.71347599  2916603.45485358  3937761.75634098
8041334.20180879  4942174.6114205  6432605.21981742  3511338.78156419
3813475.39540813  6434856.19540018  4447687.02885148  2696243.71724915
4180018.706258  6455973.25779215  4056226.34306799  7124571.30073128
2530661.67791795  3033278.46419645  3500830.32062843  5119451.01676899
7110973.93249708  4127705.79986428  2970005.36861369  4325732.61744607
5986119.70766227  6824682.68794762  3325637.45729309  7191804.55935353
2609468.55099856  5056521.66455864  6636269.77589372  2565659.89128227
3751294.03758704  5080427.99370204  4281895.68812439  7361447.18275847
5088033.19021914  6022539.93047597  4176648.2040903  4639478.54662236
2898083.34640804  7564393.66040171  2583102.74086279  3764386.73199941
4281895.68812439  6064669.4160839  5199726.50699991  5402615.00751849
3900783.41794339  4206866.26507446  4785571.46071508  5125782.90220209
3843109.12191378  4373515.96292211  3233779.57826289  5800152.85515771
3086788.94075898  3736808.50597401  4475695.33317646  10490600.69498214
3044861.09249697  7172608.23555207  4348859.16641385  4508307.36728241
6607800.84902966  3393091.94230324  4545560.49433471  3313363.08812188
7340959.28328457  5235408.60082988  4134159.03053657  5058911.23363261
6279957.32173079]

```

```
[19]: df = pd.DataFrame({"Actual value":y_test,"predicted value":np.round(y_predict,
↪2),"difference":y_test-np.round(y_predict, 2)})
```

```
[20]: print(df)
```

	Actual value	predicted value	difference
0	4585000	3950288.62	634711.38
1	6083000	6173868.82	-90868.82
2	4007500	4483635.99	-476135.99
3	6930000	7258732.75	-328732.75
4	2940000	2836727.58	103272.42
..	...	...	...
104	6650000	7340959.28	-690959.28
105	5810000	5235408.60	574591.40
106	4123000	4134159.03	-11159.03
107	3080000	5058911.23	-1978911.23
108	5530000	6279957.32	-749957.32

```
[109 rows x 3 columns]
```

## 2.5 Building the optimal model using Backward Elimination

```
[21]: x = np.append(arr = np.ones((545, 1)).astype(int), values = x, axis = 1)
print(x)
```

```
[[1 0.0 0.0 ... 1 2 1]
 [1 0.0 0.0 ... 1 3 0]
```

```
[1 1.0 0.0 ... 0 2 1]
...
[1 0.0 1.0 ... 0 0 0]
[1 0.0 0.0 ... 0 0 0]
[1 0.0 1.0 ... 0 0 0]]
```

```
[22]: x_opt = x[:, [0, 1, 2, 3, 4, 5]]
x_opt = x_opt.astype(np.float64)
print(x_opt)
```

```
[[1.00e+00 0.00e+00 0.00e+00 7.42e+03 4.00e+00 2.00e+00]
 [1.00e+00 0.00e+00 0.00e+00 8.96e+03 4.00e+00 4.00e+00]
 [1.00e+00 1.00e+00 0.00e+00 9.96e+03 3.00e+00 2.00e+00]
 ...
 [1.00e+00 0.00e+00 1.00e+00 3.62e+03 2.00e+00 1.00e+00]
 [1.00e+00 0.00e+00 0.00e+00 2.91e+03 3.00e+00 1.00e+00]
 [1.00e+00 0.00e+00 1.00e+00 3.85e+03 3.00e+00 1.00e+00]]
```

```
[23]: regressor_OLS = sm.OLS(endog = y, exog = x_opt).fit()
regressor_OLS.summary()
```

```
[23]: <class 'statsmodels.iolib.summary.Summary'>
"""
```

```

                                OLS Regression Results
=====
Dep. Variable:                  y      R-squared:                0.514
Model:                            OLS      Adj. R-squared:           0.509
Method:                 Least Squares      F-statistic:             113.8
Date:                Sun, 17 Oct 2021      Prob (F-statistic):       5.59e-82
Time:                  12:40:16      Log-Likelihood:          -8447.2
No. Observations:                545      AIC:                   1.691e+04
Df Residuals:                    539      BIC:                   1.693e+04
Df Model:                          5
Covariance Type:                nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	4.696e+05	2.92e+05	1.607	0.109	-1.04e+05	1.04e+06
x1	-2.808e+05	1.42e+05	-1.983	0.048	-5.59e+05	-2620.471
x2	-7.93e+05	1.52e+05	-5.234	0.000	-1.09e+06	-4.95e+05
x3	358.8673	26.769	13.406	0.000	306.283	411.451
x4	3.756e+05	8.26e+04	4.546	0.000	2.13e+05	5.38e+05
x5	1.33e+06	1.22e+05	10.869	0.000	1.09e+06	1.57e+06

```

=====
Omnibus:                        75.630      Durbin-Watson:           1.006
Prob(Omnibus):                  0.000      Jarque-Bera (JB):       152.634
Skew:                          0.789      Prob(JB):               7.18e-34
Kurtosis:                      5.058      Cond. No.:              3.12e+04
=====
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 3.12e+04. This might indicate that there are strong multicollinearity or other numerical problems.

"""

```
[24]: x_opt = x[:, [0, 1, 3, 4, 5]]
x_opt = x_opt.astype(np.float64)
regressor_OLS = sm.OLS(endog = y, exog = x_opt).fit()
regressor_OLS.summary()
```

```
[24]: <class 'statsmodels.iolib.summary.Summary'>
```

"""

#### OLS Regression Results

```
=====
Dep. Variable:          y      R-squared:          0.489
Model:                  OLS    Adj. R-squared:      0.485
Method:                 Least Squares    F-statistic:      129.1
Date:                  Sun, 17 Oct 2021    Prob (F-statistic):  2.72e-77
Time:                  12:40:16    Log-Likelihood:     -8460.7
No. Observations:      545    AIC:              1.693e+04
Df Residuals:          540    BIC:              1.695e+04
Df Model:               4
Covariance Type:       nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	-2.229e+05	2.67e+05	-0.835	0.404	-7.47e+05	3.01e+05
x1	1.589e+05	1.17e+05	1.361	0.174	-7.05e+04	3.88e+05
x2	378.8844	27.134	13.963	0.000	325.583	432.186
x3	4.02e+05	8.45e+04	4.759	0.000	2.36e+05	5.68e+05
x4	1.384e+06	1.25e+05	11.080	0.000	1.14e+06	1.63e+06

```
=====
Omnibus:                74.733    Durbin-Watson:          0.955
Prob(Omnibus):           0.000    Jarque-Bera (JB):       156.197
Skew:                    0.768    Prob(JB):               1.21e-34
Kurtosis:                5.126    Cond. No.:              2.67e+04
=====
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 2.67e+04. This might indicate that there are strong multicollinearity or other numerical problems.



```
"""
```

```
[25]: x_opt = x[:, [0, 3, 4, 5]]
x_opt = x_opt.astype(np.float64)
regressor_OLS = sm.OLS(endog = y, exog = x_opt).fit()
regressor_OLS.summary()
```

```
[25]: <class 'statsmodels.iolib.summary.Summary'>
"""
```

```

                        OLS Regression Results
=====
Dep. Variable:          y      R-squared:                0.487
Model:                  OLS    Adj. R-squared:            0.484
Method:                 Least Squares    F-statistic:        171.3
Date:                  Sun, 17 Oct 2021    Prob (F-statistic):    4.80e-78
Time:                  12:40:16    Log-Likelihood:       -8461.6
No. Observations:      545    AIC:                1.693e+04
Df Residuals:          541    BIC:                1.695e+04
Df Model:              3
Covariance Type:       nonrobust
=====
                        coef      std err          t      P>|t|      [0.025      0.975]
-----
const      -1.732e+05    2.65e+05     -0.655     0.513    -6.93e+05    3.47e+05
x1           378.7628     27.155     13.948     0.000     325.420    432.105
x2          4.068e+05    8.45e+04     4.817     0.000     2.41e+05    5.73e+05
x3          1.386e+06    1.25e+05    11.089     0.000     1.14e+06    1.63e+06
=====
Omnibus:                 70.408    Durbin-Watson:           0.952
Prob(Omnibus):            0.000    Jarque-Bera (JB):        142.930
Skew:                    0.738    Prob(JB):                9.19e-32
Kurtosis:                5.029    Cond. No.                2.64e+04
=====
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 2.64e+04. This might indicate that there are strong multicollinearity or other numerical problems.

```
"""
```

```
[26]: x_opt = x[:, [0, 3, 5]]
x_opt = x_opt.astype(np.float64)
regressor_OLS = sm.OLS(endog = y, exog = x_opt).fit()
regressor_OLS.summary()
```

```
[26]: <class 'statsmodels.iolib.summary.Summary'>
```

```
"""
                                OLS Regression Results
=====
Dep. Variable:                  y    R-squared:                  0.465
Model:                        OLS    Adj. R-squared:             0.463
Method:                    Least Squares    F-statistic:                235.6
Date:                Sun, 17 Oct 2021    Prob (F-statistic):        2.32e-74
Time:                12:40:16    Log-Likelihood:            -8473.0
No. Observations:                545    AIC:                      1.695e+04
Df Residuals:                    542    BIC:                      1.697e+04
Df Model:                        2
Covariance Type:                nonrobust
=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const         6.992e+05    1.97e+05     3.554     0.000     3.13e+05     1.09e+06
x1              390.1749      27.600     14.137     0.000       335.958     444.391
x2             1.6e+06    1.19e+05     13.422     0.000     1.37e+06     1.83e+06
=====
Omnibus:                 84.006    Durbin-Watson:           0.922
Prob(Omnibus):            0.000    Jarque-Bera (JB):        182.089
Skew:                     0.840    Prob(JB):                 2.88e-40
Kurtosis:                 5.280    Cond. No.                 2.04e+04
=====

Notes:
[1] Standard Errors assume that the covariance matrix of the errors is correctly
specified.
[2] The condition number is large, 2.04e+04. This might indicate that there are
strong multicollinearity or other numerical problems.
"""
```

```
[27]: x_opt = x[:, [0, 3]]
x_opt = x_opt.astype(np.float64)
regressor_OLS = sm.OLS(endog = y, exog = x_opt).fit()
regressor_OLS.summary()
```

```
[27]: <class 'statsmodels.iolib.summary.Summary'>
```

```
"""
                                OLS Regression Results
=====
Dep. Variable:                  y    R-squared:                  0.287
Model:                        OLS    Adj. R-squared:             0.286
Method:                    Least Squares    F-statistic:                218.9
Date:                Sun, 17 Oct 2021    Prob (F-statistic):        7.39e-42
Time:                12:40:16    Log-Likelihood:            -8551.2
=====
```

```

No. Observations:      545    AIC:      1.711e+04
Df Residuals:         543    BIC:      1.712e+04
Df Model:              1
Covariance Type:      nonrobust

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const      2.387e+06    1.74e+05     13.681     0.000    2.04e+06    2.73e+06
x1          461.9749     31.226      14.795     0.000     400.637    523.313
=====

Omnibus:            92.668    Durbin-Watson:           0.565
Prob(Omnibus):      0.000    Jarque-Bera (JB):       183.673
Skew:               0.954    Prob(JB):               1.31e-40
Kurtosis:           5.108    Cond. No.               1.44e+04
=====

```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 1.44e+04. This might indicate that there are strong multicollinearity or other numerical problems.

"""

```
[28]: print(x_opt)
```

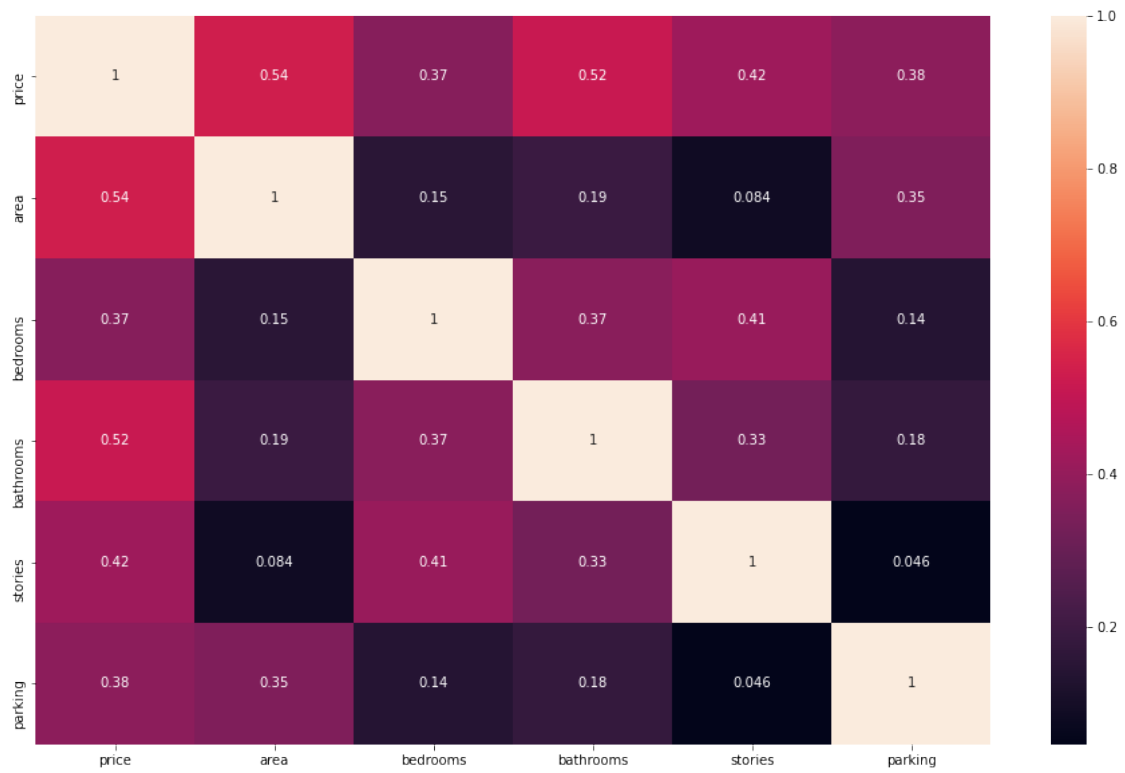
```

[[1.00e+00  7.42e+03]
 [1.00e+00  8.96e+03]
 [1.00e+00  9.96e+03]
 ...
 [1.00e+00  3.62e+03]
 [1.00e+00  2.91e+03]
 [1.00e+00  3.85e+03]]

```

```
[29]: %matplotlib inline
```

```
[30]: plt.figure(figsize = (16,10))
sns.heatmap(data_set.corr(),annot= True)
plt.show()
```



[ ]:

[ ]: