

1.1

Q1

- Thermometer: measures temperature, could be stored as double
- camera: measures visible lights, could be stored as 2d-array/matrix (of pixels)
- radar: measures the reflected pulse of energy, could be stored as tuple (wavelength, frequency)
- odometer: measures the distance traveled by a vehicle, could be stored as double
- LIDAR: measures pulsed laser (similar to radar), could be stored as tuple (wavelength, frequency)
- IMU: measures angular rate, could be stored as 1d-array (the length depends on the number of axes it measures)

Q2

sonar, infrared, touch sensor, GPS, compass

Q3

Robotic leg, shaft, headlight, brake

1.2

Q1

For a normal ellipse, the parametric equation looks like

$$x(t) = 2 \cos(t)$$

$$y(t) = \sin(t)$$

Then, we rotate the coordinates for 30 degrees and get

$$x(t) = \sqrt{3} \cos(t) - \frac{1}{2} \sin(t) + 3$$

$$y(t) = \cos(t) + \frac{\sqrt{3}}{2} \sin(t) + 2$$

To find the control policy $\mathbf{u}(t)$, we need to find the derivative of the parametric equation shown above with respect to t . And we will get

$$\mathbf{u}(t) = \left[-\sqrt{3} \sin(t) - \frac{1}{2} \cos(t), -\sin(t) + \frac{\sqrt{3}}{2} \cos(t) \right]^T$$

Q2

For such an ∞ -shape graph, its parametric equation looks like

$$x(t) = \cos(t)$$

$$y(t) = \frac{1}{2} \sin(2t)$$

Then, we rotate the coordinates for 45 degrees and get

$$x(t) = \frac{\sqrt{2}}{2} \cos(t) - \frac{\sqrt{2}}{4} \sin(2t)$$

$$y(t) = \frac{\sqrt{2}}{2} \cos(t) + \frac{\sqrt{2}}{4} \sin(2t)$$

Similar to Q1, we find the derivative with respect to t to obtain the control policy

$$\mathbf{u}(t) = \left[-\frac{\sqrt{2}}{2} \sin(t) - \frac{\sqrt{2}}{2} \cos(2t), -\frac{\sqrt{2}}{2} \sin(t) + \frac{\sqrt{2}}{2} \cos(2t) \right]^T$$

Q3

The helix curve is simply a circle on the xy-plane with a constant velocity in z-axis. The parametric equation looks like

$$x(t) = \cos(t)$$

$$y(t) = \sin(t)$$

$$z(t) = t$$

Then we can find the control policy by taking derivative

$$\mathbf{u}(t) = [-\sin(t), \cos(t), 1]^T$$

1.3

Q1

waypoints I chose:

$$p_0(-5, -7), p_1(10, -7), p_2(10, -3), p_3(4, -3), p_4(3, 7), p_5(0, 7), p_6(0, -3), p_7(3, -3), p_8(4, 10), p_f(9, 10)$$

The straight-line trajectories are

$$\gamma_{0,1}(t) = [1, 0]^T t, \quad \text{if } t \in [0, 15]$$

$$\gamma_{1,2}(t) = [0, 1]^T t, \quad \text{if } t \in [15, 19]$$

$$\gamma_{2,3}(t) = [-1, 0]^T t, \quad \text{if } t \in [19, 25]$$

$$\gamma_{3,4}(t) = [-0.1, 1]^T t, \quad \text{if } t \in [25, 35]$$

$$\gamma_{4,5}(t) = [-1, 0]^T t, \quad \text{if } t \in [35, 38]$$

$$\gamma_{5,6}(t) = [0, -1]^T t, \quad \text{if } t \in [38, 48]$$

$$\gamma_{6,7}(t) = [1, 0]^T t, \quad \text{if } t \in [48, 51]$$

$$\gamma_{7,8}(t) = [0.1, 1.3]^T t, \quad \text{if } t \in [51, 61]$$

$$\gamma_{8,f}(t) = [1, 0]^T t, \quad \text{if } t \in [61, 66]$$

Q2

Similar to Q1 but with the point_to_point_traj() function. See 1.3.2.ipynb.

Q3

Firstly, I set the center of each red sphere as waypoints, and used the point_to_point_traj() and piecewise2D() to graph the trajectory. Then, with tests and simulations, I kept modifying the velocity at each waypoint to avoid collisions. Also, I added some necessary waypoints. The final result is shown in 1.3.3.ipynb. And here's the link of the simulation video:

<https://drive.google.com/file/d/1goMLzoa9TO77zgb8cSSbPGMtakQSugNW/view?usp=sharing>

Q4

Similar to the previous question, I first set all green spheres as waypoints. Then I modified point_to_point_traj() and piecewise2D() to let them generate 3D trajectories instead of 2D. I tested and modified the trajectory for several times, and some extra waypoints were added. The final result is shown in 1.3.4.ipynb. The link of the simulation video is:

<https://drive.google.com/file/d/1zqwUnAVgeAT0C24sDviKtIQUiYAstcmv/view?usp=sharing>