

Anchors for the cosmic distance scale: the Cepheids U Sagittarii, CF Cassiopeiae, and CEab Cassiopeiae

D. Majaess^{1,2}, G. Carraro³, C. Moni Bidin⁴, C. Bonatto⁵, L. Berdnikov^{6,7}, D. Balam⁸, M. Moyano⁴, L. Gallo¹, D. Turner¹, D. Lane¹, W. Gieren⁹, J. Borissova¹⁰, V. Kovtyukh^{11,12}, and Y. Beletsky¹³

¹ Saint Mary's University, Halifax, Nova Scotia, Canada

² Mount Saint Vincent University, Halifax, Nova Scotia, Canada

³ European Southern Observatory, Av. Alonso de Cordova, 3107, 19001 Casilla, Santiago, Chile

⁴ Instituto de Astronomía, Universidad Católica del Norte, Av. Angamos 0610, 1270709 Antofagasta, Chile

⁵ Departamento de Astronomía, Universidade Federal do Rio Grande do Sul, Av. Bento Gonçalves 9500, 91501-970 Porto Alegre, RS, Brazil

⁶ Sternberg Astronomical Institute, Moscow M. V. Lomonosov State University, 119992 Moscow, Russia

⁷ Isaac Newton Institute of Chile, Moscow Branch, Universitetskij Pr. 13, 119992 Moscow, Russia

⁸ Dominion Astrophysical Observatory, Victoria, British Columbia, Canada

⁹ Departamento de Astronomía, Universidad de Concepción, 160 Casilla, Concepción, Chile

¹⁰ Departamento de Física y Astronomía, Facultad de Ciencias, Universidad de Valparaíso, Av. Gran Bretaña 1111, 5030 Casilla, Valparaíso, Chile

¹¹ Astronomical Observatory, Odessa National University, Odessa, Ukraine

¹² Isaac Newton Institute of Chile, Odessa Branch, T. G. Shevchenko Park, 65014 Odessa, Ukraine

¹³ Las Campanas Observatory, Carnegie Institution of Washington, Colina el Pino, 601 Casilla, La Serena, Chile

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ABSTRACT

New and existing X-ray, $UBVJHK_sW_{(1-4)}$, and spectroscopic observations were analyzed to constrain fundamental parameters for M 25, NGC 7790, and dust along their sight-lines. The star clusters are of particular importance because they host the classical Cepheids U Sgr, CF Cas, and the visual binary Cepheids CEa and CEb Cas. Precise results from the multiband analysis, in tandem with a comprehensive determination of the Cepheids' period evolution (dP/dt) from ~ 140 years of observations, helped to resolve concerns raised regarding the clusters and their key Cepheid constituents. Specifically, the distances derived for members of M 25 and NGC 7790 are 630 ± 25 pc and 3.40 ± 0.15 kpc, respectively.

Key words. stars: variables: Cepheids – Hertzsprung-Russell and C-M diagrams

1. Introduction

The latest suite of cosmological parameters deduced from the *Planck* satellite has renewed concerns regarding the Cepheid distance scale and the standard Λ CDM model (e.g., [Neilson et al. 2013](#), see also [Kroupa et al. 2012](#) and [Peebles 2013](#)). The Hubble constant cited by the [Planck Collaboration \(2013\)](#) differs by $\sim 5\%$ from that determined by the SH₀ES and Carnegie Hubble projects ([Riess et al. 2011](#); [Freedman et al. 2012](#)), whereby the latter efforts rely partly on Cepheids for determining H_0 (see also [Tammann & Reindl 2013](#), and references therein). The discrepancy is sufficient to hinder efforts to constrain the nature of dark energy (for which $\sigma_w \sim 2\sigma_{H_0}$, [Macri & Riess 2009](#)), and could be linked to a systematic offset in the Cepheid calibration, or unreliable photometry for remote extragalactic Cepheids owing to crowding effects ([Mochejska et al. 2004](#); [Majaess 2010, 2011a](#), see also Table 2 in [Riess et al. 2011](#)). Research continues on the aforementioned topics irrespective of the discrepancy, namely to resolve the putative degeneracy between the impact of crowding and metallicity on Cepheid parameters ([Majaess et al. 2011a, 2013a](#); [Chavez et al. 2012](#), and references therein), and to strengthen the Galactic Cepheid calibration (e.g., [Majaess et al. 2012a](#); [Anderson et al. 2013](#)). That calibration is likewise important for defining the metallicity gradient of the Milky Way

([Luck et al. 2011](#)), benchmarking standard candles ([Matsunaga 2012](#); [Kudritzki et al. 2012](#)), and constraining the behavior of intermediate mass stars ([Neilson et al. 2012](#); [Bono et al. 2013](#), and references therein). Indeed, the Galactic calibration may serve as the basis for the cosmic distance scale in concert with LMC ([Soszyński et al. 2008](#)) and NGC 4258¹ Cepheids.

Improving the Cepheid calibration by deriving solid parameters for cluster Cepheids using X-ray, $UBVJHK_sW_{(1-4)}$, and spectroscopic observations is the principal impetus of this analysis. In particular, the star clusters M 25 and NGC 7790 are examined given they host the classical Cepheids U Sgr, CF Cas, and the visual binary Cepheids CEab Cas ([Berdnikov 1990](#); [Szabados 2003](#), and references therein). P. Doig suggested that U Sgr may be a member² of M 25 ([Sandage 1960](#)), and O. Eggen was among the first to propose a Cepheid connection with

¹ The [Humphreys et al. \(2013\)](#) maser distance for NGC 4258 is $\sim 5\%$ larger than the original [Herrnstein et al. \(1999\)](#) result. The new distance can be reconciled with the Cepheid photometry for NGC 4258 ([Macri et al. 2006](#)) if the crowding bias endemic to the latter is considered (Fig. 4 in [Majaess et al. 2009](#), and see also [Bono et al. 2008, 2010](#); [Majaess 2010](#); [Bresolin 2011](#)).

² [Anderson et al. \(2013\)](#) hinted that Y Sgr could likewise be a member of M 25.

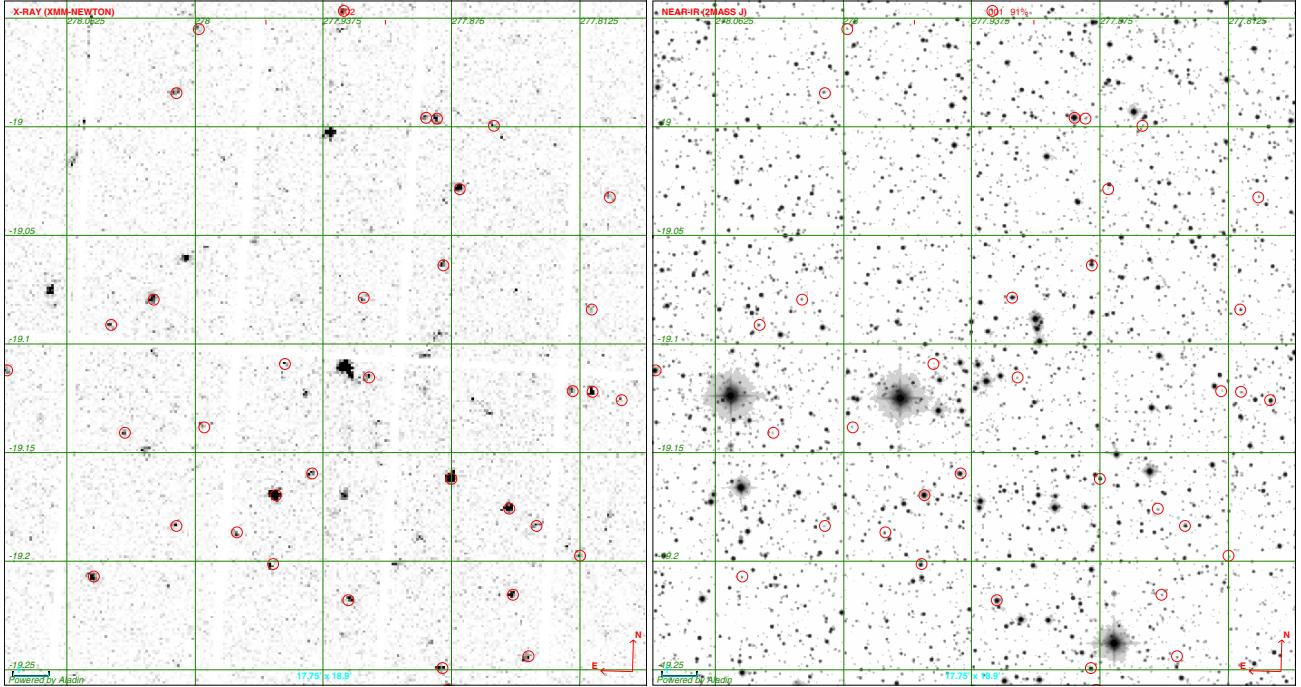


Fig. 1. *XMM-Newton* X-ray data (ObsID:040472) were used to help segregate fainter cluster members from field stars, thus facilitating the application of an isochrone and reducing uncertainties associated with the cluster distance derived (e.g., [Majaess et al. 2012a](#); [Carraro et al. 2013](#)). Left panel: a cropped *XMM-Newton* image of the field encompassing M 25, while a near-infrared 2MASS J-band image is shown on the right. Red circles are 2MASS (AAA) sources that exhibit X-ray emission.

NGC 7790 ([Sandage 1958](#)). Yet generations after those discoveries ambiguities linger regarding the parameters for the host clusters (e.g., [Matthews et al. 1995](#); [Hoyle et al. 2003](#), and discussion therein). Indeed, the uncertainty led [Turner \(2010\)](#) to bypass NGC 7790 when constructing the 2010 iteration of the Galactic Cepheid calibration. Analyses of M 25 are complicated by systematic offsets between relatively shallow observations published for the cluster, as well as its projection upon a rich background field.

New and existing multiband data are analyzed here with the aim of mitigating uncertainties tied to M 25, NGC 7790, their key constituent Cepheids, and invariably the important Galactic Cepheid calibration ([Joner & Laney 2012](#); [Monson et al. 2012](#); [Ngeow 2012](#); [Groenewegen 2013](#)).

2. Analysis

2.1. M 25

Distinguishing cluster members from field stars is a principal challenge associated with establishing reliable parameters for open clusters. Late-type cluster dwarfs can prove difficult to distinguish from field stars that are of comparable brightness, hence the pertinence of X-ray data. [Majaess et al. \(2012a\)](#) used X-ray observations to identify low-mass stars associated with the Cepheid SU Cas, and its host cluster Alessi 95 ([Turner et al. 2012](#)). X-ray emitting stars associated with relatively young Cepheids ($\tau \sim 100$ Myr, [Turner 2012](#)) are typically cooler than F5–F8 V, where convection becomes an important mode of energy transport in the stellar atmosphere. The X-rays stem from a hot coronal plasma driven by convection and the magnetic dynamo. X-ray emission drops with stellar age, since the angular momentum inherited from the accretion process dissipates (i.e., via stellar winds and magnetic braking) and the dynamo weakens. Consequently, relatively young stars associated with

classical Cepheids can be separated from field stars along the same sight-line, since the latter are typically old slow-rotators that are X-ray quiet. X-rays are also useful for identifying companions to massive cluster stars ([Evans 2011](#); [Majaess et al. 2012a](#)).

XMM-Newton X-ray images (ObsID:040472, PI: Motch) of the field were examined to identify fainter cluster members (Fig. 1). Sources were identified using SExtractor ([Bertin & Arnouts 1996](#)). The elongation option was selected since sources on the *XMM-Newton* image were asymmetric. A 2.5σ criterion was chosen to reduce spurious detections. The X-ray targets were subsequently matched with newly acquired *UBV* photometry and 2MASS near-infrared (AAA) photometry, and the resulting sample is displayed in Figs. 1 and 2. The new optical CCD photometry was obtained from the 1 m Henrietta Swope telescope (Las Campanas, Chile). The data were reduced following [Carraro \(2009\)](#). Bright saturated stars were swapped with unpublished photoelectric photometry obtained from Las Campanas using the 0.6 m Helen Sawyer Hogg telescope. Deeper near-infrared photometry was also obtained via the Osiris instrument on the 4 m SOAR telescope (Cerro Pachón, Chile). The [Stetson \(1987\)](#) DAOPHOT routines were employed to extract photometry from the images since the sources exhibited satisfactory stellar PSFs (point spread functions). The deeper near-infrared data revealed numerous field stars occupying the region of the color–magnitude diagram associated with cluster M-dwarfs. 2MASS observations constitute the bulk of the data displayed in the near-infrared color–magnitude diagram for M 25 (Fig. 2), with photometry for several faint X-ray sources supplied by the SOAR observations. Deeper X-ray data are needed to fully exploit the SOAR data.

Field contamination was likewise minimized by selecting stars that exhibit bright *U*-band photometry. Bright (*U*) early-type stars are comparatively rare in a field owing to a steep initial

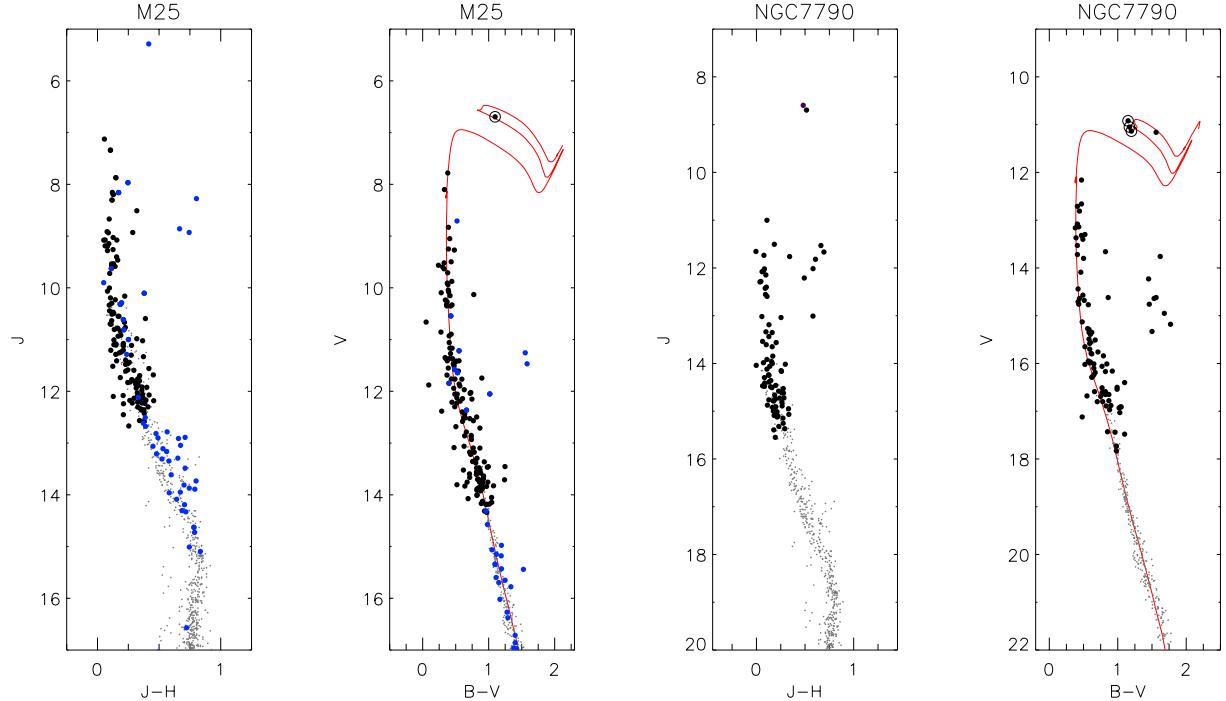


Fig. 2. Optical and near-infrared color–magnitude diagrams for M 25 and NGC 7790. For M 25 the blue and black filled circles are X-ray and bright U -band selected sources, respectively. Color cuts were made to reduce field star contamination. For NGC 7790 the black filled circles are 2MASS (near-infrared) and ARO (optical) field decontaminated photometry (Bonatto & Bica 2011, and references therein). Black dots in the color–magnitude diagrams represent the intrinsic relation (Majaess et al. 2011b) shifted to match the observations. Optical photometry for the cluster Cepheids are conveyed by circled dots (Berdnikov et al. 2000; Berdnikov 2008).

mass function and relatively short lifetimes. Moreover, background B-stars are faint given M 25 is comparatively nearby. Most field stars that remained after imposing the U -band limit did not traverse the cluster sequence. The combined X-ray and U -band selected stars populate the bulk of the cluster sequence (Fig. 2), thus facilitating the application of an isochrone. Fewer X-ray stars were identified in the optical dataset relative to the near-infrared owing to the reduced field of view of the former (by contrast 2MASS is all-sky).

The optical color excess was determined via the UBV color–color diagram, and yielded $E_{B-V} = 0.513 \pm 0.034\sigma$ (Fig. 4). The intrinsic UBV color–color relation of Turner (1989, and references therein) was used, in tandem with the reddening line for the broader field determined by Turner (1976). B-stars were solely considered in the fit to avoid the Hyades anomaly (Turner 1979). To within the uncertainties the cluster reddening matches the estimate cited for U Sgr by Turner (2010), $E_{B-V} = 0.50 \pm 0.03$. However, the cluster reddening is larger than the average color-excess cited for U Sgr by Laney & Caldwell (2007, and references therein), $E_{B-V} = 0.42 \pm 0.02$. The source of the reddening discrepancy is unknown, and differential extinction cannot be invoked since B-stars encompassing U Sgr share the mean cluster reddening.

The near-infrared reddening for M 25 was inferred using spectral types cited for bright B-stars by Wampler et al. (1961) and Skiff (2013)³, in conjunction with JHK_s intrinsic colors from Straižys & Lazauskaitė (2009). The resulting mean color excess is $E(J-H) = 0.165 \pm 0.032\sigma$. The Wampler et al. (1961) spectral types are offset in temperature and luminosity class from those established by Feast (1957) and Wallerstein (1957). The latter, although comprehensive, often cite dwarf classifications

for evolved B-stars. The evolved luminosity class determinations of Wampler et al. (1961) are in better agreement with the color–magnitude diagram (Fig. 2, see also Houk & Cowley 1975).

With the reddening established, the isochrone and the intrinsic Majaess et al. (2011b) relation were shifted along the ordinate of the color–magnitude diagram to match the observations. The near-infrared empirical calibration derived by Majaess et al. (2011b) was used to establish the cluster distance. That calibration was constructed from revised HIPPARCOS parallaxes for nearby stars (van Leeuwen 2007), and yields distances to seven benchmark clusters (e.g., α Per) that are consistent with the van Leeuwen (2009)⁴ HIPPARCOS determinations. The relation is not tied to the Pleiades cluster, an important consideration granted a dispute continues concerning its parameters (van Leeuwen 2009; Majaess et al. 2011b; de Grijs 2012, and references therein). A comprehensive analysis of B-stars in M 25 by Luck et al. (2000) demonstrated that cluster stars exhibit near solar abundances. U Sgr likewise displays near solar abundances (Laney & Caldwell 2007; Klagyivik & Szabados 2009, and references therein). Metallicity effects in the near-infrared are negligible in this instance (Alonso et al. 1996; Majaess et al. 2011b).

The resulting distance and age for M 25 are $d = 630 \pm 25$ pc and $\log \tau = 7.88 \pm 0.10$, respectively. The parameters were inferred from the near-infrared (the calibration) and optical data, respectively. The latter dataset exhibits more reliable photometry for bright cluster members. The distance determined for M 25 agrees with a preliminary estimate deduced by Turner (2010)

³ Catalogue of stellar spectral classifications.

⁴ van Leeuwen (2009) suggests that HIPPARCOS parallaxes and the Hyades anomaly (e.g., see Sect. 2 of Turner 1979; and Fig. 29 of van Leeuwen 2009) imply that traditional main-sequence fitting is flawed, as there exists an additional parameter affecting the luminosity (i.e., age). Majaess et al. (2011b) provide an alternate interpretation to consider.

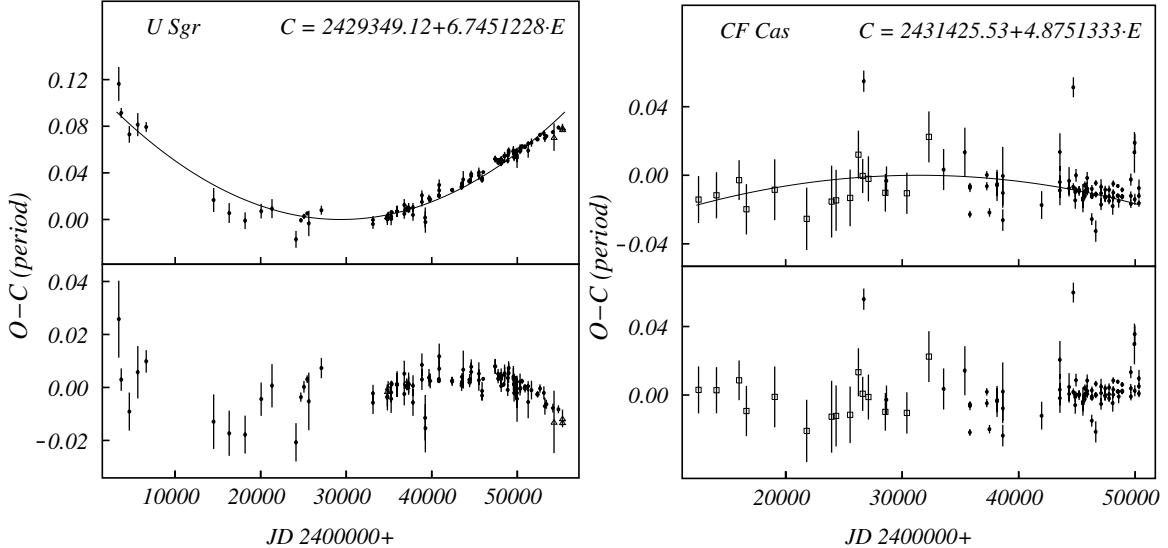


Fig. 3. Period evolution (O–C) diagrams for U Sgr ($dP/dt = +0.073 \text{ s yr}^{-1}$) and CF Cas ($dP/dt = -0.072 \text{ s yr}^{-1}$) facilitate the selection of an isochrone (Fig. 2). The new results imply that U Sgr is traversing the instability strip for the third time and is evolving toward the cool-end of the instability strip, whereas CF Cas may be a second crosser venturing toward hotter temperatures (the scatter is admittedly large). The lower panels display the residuals from the polynomial fits applied. [Sterken \(2005\)](#) relays comprehensive information regarding period evolution (O–C) diagrams.

(see also [Kharchenko et al. 2005](#)), yet is larger than the distance established for U Sgr from the infrared surface brightness technique ([Storm et al. 2011](#), $d = 579 \pm 6 \text{ pc}$). The age was ascertained by matching the isochrone to evolved blue and red cluster stars, whereby a solar isochrone was selected ([Padova, Girardi et al. 2002](#); [Bonatto et al. 2004](#)). The period evolution of U Sgr ($dP/dt = +0.073 \pm 0.010 \text{ s yr}^{-1}$, Fig. 3) was likewise considered in the aforementioned determination, since it implies that the Cepheid lies in the third crossing of the instability strip according to the [Turner et al. \(2006\)](#) framework (see also [Szabados 1983](#); [Becker 1985](#); [Neilson et al. 2012](#)). The duration of each instability strip crossing differs, whereby the first traversal is shortest ([Becker 1985](#)). The positive rate (dP/dt) implies U Sgr is evolving toward the cool side of the instability strip, provided the period evolution is primarily tracking density changes ([Eddington 1918](#)). However, recent and precise observations exhibit a superposed variation (Fig. 3). The aforementioned conclusions stem from a comprehensive analysis featuring more than 100 years of U Sgr observations⁵ (Fig. 3).

A distance based on the optical measurements was evaluated with the aim of supporting (to first-order) the near-infrared solution. The analysis yielded $d = 650 \text{ pc}$, but the result is tied to the canonical extinction law ($R_V = A_V/E_{B-V} \sim 3.1$, [Turner 1976](#)). The ratio varies throughout the Galaxy, e.g., [Carraro et al. \(2013\)](#) obtain $R_V \simeq 3.85$ for the cluster Westerlund 2, while [Nataf et al. \(2013\)](#) derived $R_V = 2.5$ for the Galactic bulge. Majaess et al. (in prep.) mapped R_V variations throughout the region and determined that $R_V \sim 3.25$ (Fig. 5).⁶ That implies an optical-based distance for M 25 ($d = 640 \text{ pc}$) that matches the near-infrared solution. Admittedly, obtaining new spectra to confirm existing classifications is desirable, and would allow for a separate estimate of R_V (e.g., [Wegner 2002](#)).

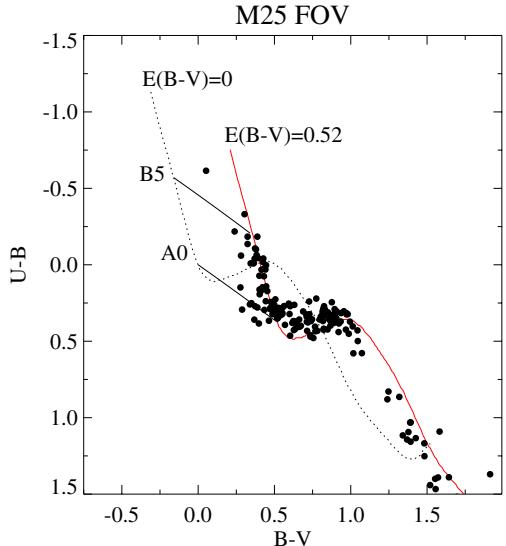


Fig. 4. New observations for stars in the field of M 25 that exhibit bright U -band photometry. The intrinsic relation and reddening law by [Turner \(1989](#), and references therein) and [Turner \(1976\)](#) were adopted, respectively. A mismatch to the intrinsic relation appears just beyond A0 and may be indicative of a standardization offset or the Hyades anomaly. A mean cluster reddening was determined ($E_{B-V} = 0.513 \pm 0.034\sigma$) from the B-stars to avoid the aforementioned problem ([Turner 1979](#)).

2.2. NGC 7790

Reddening estimates for NGC 7790 exhibit a sizable spread, and it was speculated that dust along the sight-line is peculiar ([Hoyle et al. 2003](#), their Fig. 14 and references therein). However, the UBV color–color diagram constructed by [Mateo & Madore \(1988\)](#) does not support that finding. It is unclear whether problems endemic to standardizing U -band photometry are the source of the discrepancy ([Cousins & Caldwell 2001](#); [Massey 2002](#); [Turner et al. 2011](#)), or a Hyades-like anomaly is present.

⁵ An elaborate listing of references tied to the O–C analyses (Fig. 3) is obtainable from the coauthor L. Berdnikov.

⁶ The Majaess et al. (in prep.) analysis used mid-infrared WISE data ([Wright et al. 2010](#)) to determine R_V via the color-extrapolation method.

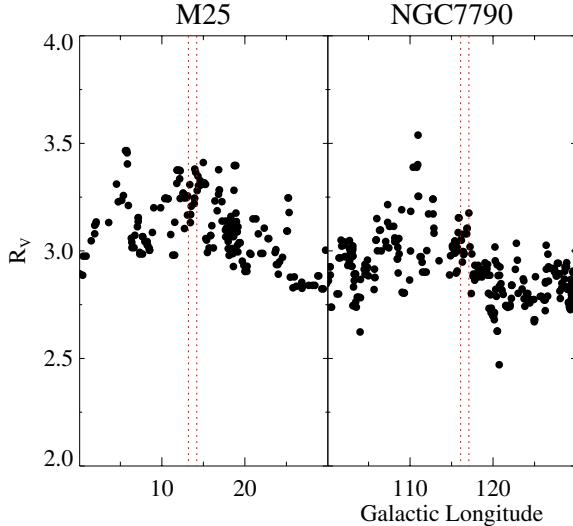


Fig. 5. Estimated extinction law ($R_V = A_V/E_{B-V}$) variations binned as a function of Galactic longitude (Majaess et al., in prep.). The broader sight-lines encompassing M 25 ($\ell \sim 14^\circ$) and NGC 7790 ($\ell \sim 117^\circ$) exhibit higher and marginally lower values of R_V than the canonical extinction law ($R_V \sim 3.1$, Turner 1976), respectively.

New spectroscopic observations were acquired to constrain the reddening. Six cluster B-stars were observed using the 1.8 m Plaskett telescope (Dominion Astrophysical Observatory (DAO), Victoria). The spectra were reduced via IRAF and are shown in Fig. 6. Spectral classifications and coordinates for the sample are listed in Table 1, the former being derived using the precepts highlighted by Gray & Corbally (2009). The results are generally confirmed by fitting synthetic spectra to the observations (see Sect. 2.2.1, and Moni Bidin et al. 2007, 2012).

Four additional B-stars featured in the Skiff (2013) catalog were included to evaluate a mean color-excess of $E(J-H) = 0.14 \pm 0.04\sigma$ and $E_{B-V} = 0.52 \pm 0.05\sigma$. The former was computed using 2MASS photometry and near-infrared intrinsic colors from Straizys & Lazauskaitė (2009), whereas the latter stemmed from new ARO⁷ BV photometry in conjunction with the intrinsic colors of Turner (1989, and references therein). To within the uncertainties the reddening for NGC 7790 is consistent with estimates cited previously for CF Cas (Lane & Caldwell 2007; Fouqué et al. 2007, and references therein, $E_{B-V} = 0.553$).

The optical CCD observations obtained at the ARO were standardized (Fig. 2) to unpublished photoelectric photometry obtained at Kitt Peak during August 1984 (the 0.9 m and 1.3 m telescopes were used in tandem with a 1P21 system). The ARO photometry was generated using DAOPHOT, and a search for variability was carried out via the VaST⁸ routine (Sokolovsky & Lebedev 2005). No cluster variables were detected to sufficient precision other than the Cepheids. New JHK_s photometry was obtained from the Observatoire Mont-Mégantic (Artigau et al. 2010) for the field hosting NGC 7790. However, the photometry could not be placed on the 2MASS system since nonlinearities appeared near the faint end of the standardization, which rendered the zero-point uncertain for any key data beyond the

2MASS limits. Those observations were thus omitted from the analysis.

NGC 7790 is too distant to exhibit reliable proper motion or X-ray data that could facilitate the identification of cluster members. A field star decontamination algorithm was therefore employed (Bonatto & Bica 2011, and references therein), whereby the morphology displayed in the color-magnitude diagram by a field sample was removed from a diagram featuring field and cluster stars (of equal area). The results for NGC 7790 are shown in Fig. 2.

The distance to NGC 7790 was established in the manner described for M 25 (Sect. 2.1). The near-infrared distance is $d = 3.40 \pm 0.15$ kpc, which fits the solution based on optical measurements (Fig. 2). The cluster distance and reddening are larger and marginally smaller, respectively, than estimates recently inferred from MegaCam images (Davidge 2012, $d \sim 3176$ pc and $E(B-V) = 0.56$, see also his Table 2). Kharchenko et al. (2005) advocated cluster parameters of $d = 2944$ pc and $E(B-V) = 0.53$. The cluster age ($\log \tau = 8.0 \pm 0.1$) was inferred by matching a solar isochrone to precise optical photometry for evolved members (the authors are unaware of complete near-infrared data for CEab Cas). Here too an analysis of the Cepheids' period evolution was considered to facilitate the age determination. An examination of over 100 years of CF Cas observations implies that the Cepheid is in the second crossing ($dP/dt = -0.0721 \pm 0.014$ s yr⁻¹), given its low rate of period change (the second crossing is generally longest, Becker 1985). CEa and CEB Cas were analyzed by Berdnikov (1990), and the objects may be third crossers. Photometry for the Cepheids (Berdnikov et al. 2000; Berdnikov 2008) support the aforementioned conclusions (i.e., CEa Cas is brighter than CF Cas), although uncertainties associated with the period change and crossing mode determined render the conclusion tentative. However, the period analysis certainly indicates that none of the Cepheids are first crossers (the crossing mode with the shortest duration, i.e., rapid period change).

2.2.1. Synthetic spectra fits

Fundamental parameters for the DAO target stars (T_{eff} , $\log g$, $V \sin i$) were estimated by fitting the Balmer and helium lines with synthetic spectra. Solar metallicity was assumed because new abundance estimates derived for this study imply that CF Cas, CEa Cas, and CEB Cas have $[\text{Fe}/\text{H}] = -0.08, -0.03$, and -0.01 ($\sigma = 0.15$ dex), respectively (Kovtyukh 2013, unpublished). A grid of model spectra ($T_{\text{eff}} = 12\,000\text{--}32\,000$ K and $\log g = 3.5\text{--}5.0$ dex) was generated via Lemke's version⁹ of the LINFOR program (developed originally by Holweger, Steffen, and Steenbock at Kiel University). Local thermodynamic equilibrium (LTE) model atmospheres were computed with ATLAS9 (Kurucz 1993). Extensive details about the synthetic spectra fitting procedure are found in Moni Bidin et al. (2012).

The stellar parameters were derived via a χ^2 fit, as implemented in the *fitprof21* code developed by Bergeron et al. (1992) and Saffer et al. (1994), and subsequently modified by Napiwotzki et al. (1999). The routine returns formal statistical uncertainties and neglects uncertainties stemming from the normalization procedure, sky subtraction, and flat-fielding. Therefore the uncertainties cited are likely underestimated (Table 1). Balmer lines from H β to H 12 were fitted simultaneously, with the exception of He (when blended with the

⁷ The Abbey Ridge observatory (ARO) is a remotely operated facility hosting a 0.3 m telescope and is engaged in supernova, variable star, and cluster research (e.g., Lane & Gray 2011; Majaess et al. 2012b).

⁸ Variability Search Toolkit (VaST): <http://scan.sai.msu.ru/vast/>

⁹ <http://a400.sternwarte.uni-erlangen.de/~ai26/linfit/linfot.html>

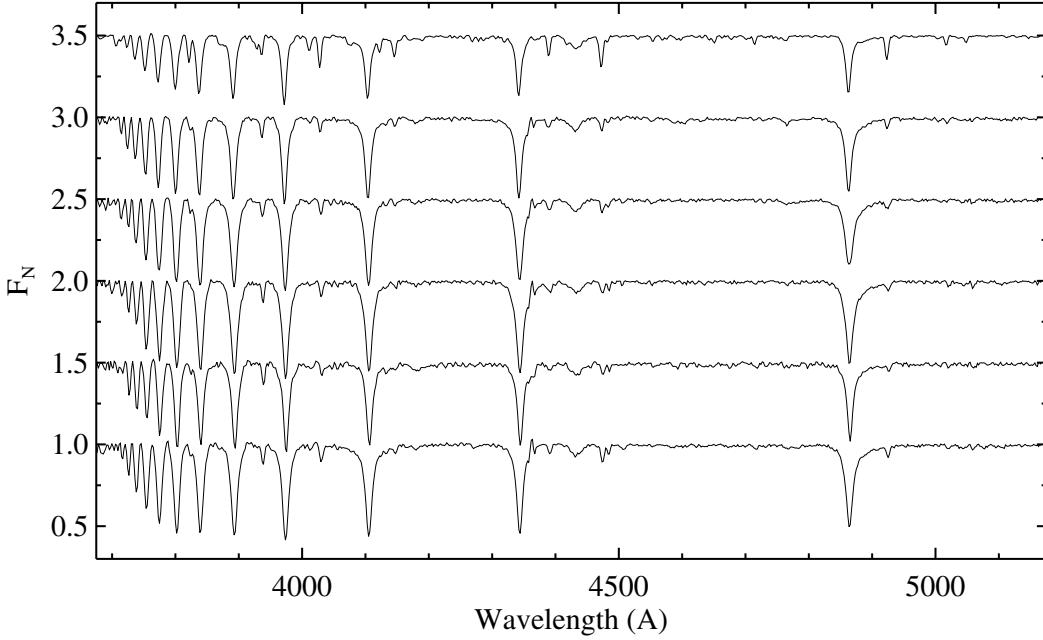


Fig. 6. New DAO spectra for B-stars in NGC 7790 were used in determining the mean reddening ($E_{B-V} = 0.52 \pm 0.05\sigma$). The spectra are listed in order of increasing ID. Pertinent details regarding the stars are highlighted in Table 1.

Table 1. Spectroscopically observed stars encompassing NGC 7790.

ID	RA/Dec (J2000)	SpT ^a	$V \sin i$ (km s ⁻¹) ^b	T_{eff} (± 100 K) ^b	$\log g$ (± 0.03 dex) ^b
0 ^c	23:58:07.40 +61:11:44.9	B1V	150	24 500	4.11
1	23:58:28.10 +61:12:03.1	B5IV	170	14 700	3.63
2	23:58:23.19 +61:12:25.0	B7IV	220	13 400	3.72
3	23:58:29.05 +61:12:41.4	B8IV	0	13 400	3.98
4	23:58:30.68 +61:12:18.7	B8IV	190	14 000	3.60
5	23:58:31.32 +61:12:49.8	B6IV	190	13 000	3.73

Notes. ^(a) Classified by visual inspection using the precepts outlined by Gray & Corbally (2009). ^(b) Inferred from synthetic spectra fits to the observations (Sect. 2.2.1). The statistical uncertainties produced by the fitting routine are cited and may underestimate the combined uncertainty by 2–4× (Napiwotzki 1999, priv. comm.). ^(c) Spectroscopic parameters for evolved M 25 stars are also presented by Luck et al. (2000, their Table 2).

Table 2. Cluster parameters.

Cluster	$E(J - H)$	$E(B - V)$	d (pc)	$\log \tau$
M 25	$0.165 \pm 0.032\sigma$	$0.513 \pm 0.034\sigma$	630 ± 25	7.88 ± 0.10
NGC 7790	$0.14 \pm 0.04\sigma$	$0.52 \pm 0.05\sigma$	3400 ± 150	8.0 ± 0.1

Ca II H line). The derived values of T_{eff} and $\log g$ are most sensitive to the hydrogen lines. Four weak helium lines ($\lambda 4026$, 4388 , 4471 , and 4922 Å) were also matched, and those features generate a better estimate for $V \sin i$ than broad Balmer lines. $V \sin i$ was an input quantity that was iteratively tweaked until a minimum χ^2 was achieved. Admittedly, $V \sin i$ is not precisely determined at the resolution of the spectra obtained. Numerous factors may alter the effective line width (e.g., instrumental profile, variations of the true resolution owing to seeing), although rapid rotation endemic to such hot targets is the dominant line-broadening effect. A precise $V \sin i$ estimate would likewise require a zero-point calibration to standard stars (e.g., Recio Blanco et al. 2004; Monaco et al. 2011). The results presented in Table 1 are thus deemed suggestive and may be affected by systematic offsets (e.g., systematic offsets exist between parameters inferred from NLTE and LTE models, Young & Short, in prep.).

Results inferred from the synthetic spectra are consistent with the spectral types assigned from a visual inspection (to within the expected uncertainties), thus supporting the cluster parameters deduced.

3. Conclusion

A new multiband X-ray, $UBVJHK_sW_{(1-4)}$, and spectroscopic investigation was carried out to establish precise cluster parameters (Table 1). Parameters tabulated for M 25 are $d = 630 \pm 25$ pc and $\log \tau = 7.88 \pm 0.10$, as deduced from isochrone fits to color-magnitude diagrams populated by X-ray and U -band selected members (Figs. 1, 2). The age is partly associated with a comprehensive period-change analysis for U Sgr (Fig. 3). The period evolution of U Sgr ($dP/dt = +0.073$ s yr⁻¹) implies the Cepheid is in the third crossing according to the Turner et al. (2006) framework, and is evolving toward cooler temperatures. Dust

along the line of sight to M 25 is characterized by color excesses of $E(J - H) = 0.165 \pm 0.032\sigma$ and $E_{B-V} = 0.513 \pm 0.034\sigma$ (Fig. 4), the former being tied to the Wampler et al. (1961) spectral types. The Wampler et al. (1961) spectral types are offset from previously published designations, but they match the evolved (IV-III) luminosity classifications expected for late-to-mid B-stars associated with intermediate-period Cepheids (Fig. 2). The Majaess et al. (in prep.) analysis implies that dust along the broader sight-line encompassing M 25 follows a marginally higher extinction law ($R_V \simeq 3.25$). Adopting that value reduces the offset between the near-infrared and optical distance solutions for the cluster.

Parameters determined for NGC 7790 are $d = 3.40 \pm 0.15$ kpc and $\log \tau = 8.0 \pm 0.1$, where the results rely partly on the application of a field decontamination algorithm (Bonatto & Bica 2011, and references therein) since X-ray data are unavailable. The period evolution of the cluster's constituent Cepheids CF Cas and CEab Cas (Berdnikov 1990) were considered when deriving the cluster age. An elaborate period analysis for CF Cas ($dP/dt = -0.0721$ s yr $^{-1}$, Fig. 3) indicates that it is a second crosser evolving toward the hot end of the instability strip. It was previously suggested that dust along the line of sight to NGC 7790 is anomalous, as implied by *UBV* color–color diagrams constructed from various published datasets (Hoyle et al. 2003, their Fig. 14 and references therein). However, an inspection of the *UBV* color–color diagram assembled by Mateo & Madore (1988) for cluster stars does not support that finding. Nonetheless, the impact of inhomogeneous or stellar parameter sensitive *U*-band photometry was reduced by using unpublished *UBV* photoelectric photometry, near-infrared photometry, and new DAO spectroscopic observations for several B-stars (Fig. 6). The observations imply color excesses of $E(J-H) = 0.14 \pm 0.04\sigma$ and $E_{B-V} = 0.52 \pm 0.05\sigma$, and rely on spectroscopic classifications assigned by visual inspection that were generally confirmed via synthetic spectral fits (Sect. 2.2.1, Table 1). The R_V for the broader region encompassing NGC 7790 is marginally lower than the canonical $R_V \sim 3.1$ extinction law (Fig. 5).

Lastly, the Galactic Wesenheit (VI_c) function based on the Turner (2010) and Benedict et al. (2007) calibrators was updated using the suite of new parameters established here and elsewhere (e.g., V340 Nor and QZ Nor, Majaess et al. 2013b). The resulting function is described by

$$W_{VI_c,0} = (-3.31 \pm 0.07) \times \log P_0 - (2.56 \pm 0.06), \quad (1)$$

where P_0 is the pulsation period (fundamental mode), $W_{VI_c,0}$ is the absolute Wesenheit magnitude, and the apparent Wesenheit magnitude is $W_{VI_c} = V - 2.55 \times (V - I_c)$. The slope of the Galactic W_{VI_c} function (Eq. (1)) matches that derived for LMC and SMC Cepheids (Ngeow et al. 2009), but is inconsistent with the slope established for distant solar extragalactic Cepheids associated with known supernova-host galaxies (Majaess 2010; Riess et al. 2009). Continued research aimed at reducing uncertainties associated with the Cepheid calibration (e.g., Benedict et al. 2007; Gieren et al. 2013) and the impact of crowding on remote extragalactic Cepheid photometry may eventually help identify the source behind discrepant values of H_0 cited in the literature (e.g., Riess et al. 2011; Freedman et al. 2012; Tammann & Reindl 2013; Planck Collaboration 2013).

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