

Prospective Ageing—Literature review

mz

Independent discoveries of this principle: Ryder (1975), Fuchs (1984) and Sanderson and Scherbov (2005), also Bayó and Faber (1981).

Siegel (1980) also mentions Jackson's 1980 Minorities and aging as a source, but haven't been able to get a copy yet.

This link here is the IIASA list of their publications and data.

Cain1974—*The growing importance of legal age in determining the status of the elderly*

The distinction between the elderly and adults as a special status is first formalised by Bismarck, who got passed in 1899 the Old Age Insurance Law, for which workers were eligible at age 71.

Cain speaks of the paradox that the more we use chronological age as a legal category delimiter, the more obvious it is that it is inadequate due to differences in maturation and retention of skills, adaptability etc.

The American Social Security Act of 1935 defined a distinct legal status for the elderly at age 65. Although the number was not based on any serious analysis or anything, it just felt that lower would be too expensive and higher would not get support due to high unemployment levels at the time.

Ryder (1975)—*Notes on stationary populations*

“challenged the conventional view in which people are classified as old based on a fixed chronological age. In the study of aging he argued that it would be preferable to consider people as old not based on their chronological ages, but instead on their expected remaining lifetimes.” Sanderson and Scherbov (2015)

Ryder seems to first come up with the old age threshold, but calls it the *index of old age*:

“We propose that some arbitrary length of time, such as 10 years, be selected and that we determine at what age the expectation of life is 10 years, that age to be considered the point of entry into old age [...]” Ryder (1975)

siegel1980—*On the demography of Ageing*

This is a presidential address at the Population association of America from 1980.

Definitions of ageing are not obvious. Cultural definitions vary; demographers use chronological age, but these require an arbitrary cut off point. An alternative concept is based on the average number of years until death. Here quotes Ryder and Jackson (the book I can't get).

“Like average life expectancy, it applies to population groups rather than individuals.”

What are the implications of this? Should benefits and privileges of old age be accorded to men and blacks at younger ages than whites and women? Mentions Cain (1974) discussing the use of chronological age vs prospective age in court decisions.

One issue with *old age based on age at death* is the lack of data. You need life tables for sub-groups of race, gender, even specific health conditions. But nothing else directly relevant in this paper I don't think

Bayó and Faber (1981)—*Equivalent Retirement Ages, 1940-2050*

Actuarial note by the US Social security administration - office of the Actuary. They propose four measures, one of them (Measure A) is one where the retirement expectancy—time until death really—is kept the same as in the base year. They also have a more ‘fair’ measure, where they keep the ratio of work and retirement the same. They also say:

“[These measures] take into account mortality, but do not take into account morbidity. That is, they adjust for the expected length of life spent in retirement, but they ignore the question of whether that life is spent in a more or less healthy condition.”

One reason is that it is difficult to quantify, the other that it probably correlates with mortality

Fuchs (1984)—*Though much is taken—reflections on ageing, health and medical care*

Quoted in Sanderson and Scherbov (2008) and Sanderson and Scherbov (2015) as an independent discovery of this principle, more elaborate than Ryder.

All literature about ageing starts off with sth on the proportion of people over 65. Why? The assumption is they are not in work, so output must be transferred from the working population to them. Additionally they are less healthy. So the definition of old age is very important. The chronological definition “*is largely a concession to administrative convenience rather than the logical result of a closely reasoned argument.*” One alternative would be to look at e.g. people within 5 years of death (but only ones already over 65). Or people over 65 but not in the labour force. These measures focus on the health and transfer payments respectively.

Health care utilization: projected to increase as the age distribution of the elderly is shifting towards older ages and health care utilization increases with age. This assumes the age-spending relationship holds constant over time. **But** this results in an overestimate: “*health care spending among the elderly is not so much a function of time since birth as it is a function of time to death.*” *How much health care will a 75 year old utilize in 10 years time? That depends on medical technology, health care policy etc. but “to the extent that fewer 75-year-olds will be in the last or next-to-last year of life, a simple extrapolation from past utilization of 75-year olds is inappropriate.*” Mind blown.

This eliminates the age related increases in expenditures as well as the excess male over female expenditure: “*the only reason why older men use more medical care than older women at any given age is because a higher proportion of them men are in the last year of their life.*” And so because age-specific mortality rates are changing over time, this affects their age-specific health expenditures, they should not simply be applied cross-sectionally.

So there is not a monotonic relationship between ageing and health care expenditure. And it’s not simple anyway, the question is why are the death rates falling: is it because people are living healthier lives? Then conventional measures will over-estimate their health care costs. But if the reason is more complex technological interventions, then this cost will tend to be offset by the reduced number of people in the end of life.

Labour force participation Men, really hard core declines in the 50s-80s! over 65 they fell from 46% to 19%. Why!? common answer is health, but scepticism: ill health is just a socially acceptable thing to say. Mandatory retirement and age discrimination might be another reason. This has to do with contracts that increase your wages, even though your productivity is probably declining. Which should not be called discrimination if the labour is more expensive! Another issue is the number of elderly people. Moving from a pyramid-like structure, which coincides with workplace hierarchies to a more rectangular one: there are fewer senior positions if workplaces if old people stay in the labour force. Social security is a major reason for lower labour force participation of older men.

Income another interesting point. Older people are better off than ever (this is in the 80s) with social security, but this is an annuity-like income which doesn’t come from work or ownership like stocks and

bonds or a business. Research shows kids' frequency of visits is proportional to bequeathable wealth, not non-bequeathable wealth: seniors are "better off and feeling worse" as no longer have control over assets.

Sanderson and Scherbov (2005)—*Average remaining lifetimes can increase as human populations age* (Nature paper)

Two new measures: (i) *the standardized median age* (ii) *the rescaled dependency ratio*

Median age is the most commonly used measure of population ageing apparently. This piece describes the idea of standardizing median ages in some sort of way to account for increased life expectancy, although it does not do a very good job at explaining it intuitively at all. . .

"Here we propose a new measure of ageing: the median age of the population standardized for expected remaining years of life."

So while populations are growing older measured by median age, they can also be growing younger as measured by *standardized median age*. Similarly adjusting the old-age dependency ratio shows ageing is a lot slower than usually thought, and at times even reversing.

"Population ageing differs from the ageing of an individual. People who survive grow older with each year they live. Populations, on the other hand, can grow younger."

A lot of things don't depend on chronological age, but on time left to live e.g. the costs of medical care, retirement, bequests, consumption and the accumulation of capital.

So, using period life tables, you've got the *median age* and the *life expectancy at median age*. The first the age that divides the population into half. And it keeps going up. The lex at median is also the median remaining lex - since half the population has a higher remaining life expectancy (those younger than the median) and the other half a lower remaining lex (those older than the median).

If median ages stayed the same (e.g. through migration), then remaining lex at the median age would go up—due to increases in longevity. But with the median age also going up, depending on how quickly it is increasing the remaining lex can go up slowly or even reverse. In the latter case the improvement in mortality rates are outweighed by the increased median age.

An example of this is the projection for Japan 2000 - 2040 where the median age is expected to increase from 41 to 55, while the remaining life expectancy at the median age will fall from 41 to 35. Afterwards the slow down of the median age increase leads to life expectancy at the median to increase as well. Their median age is rising so fast because of low fertility, high life expectancy and little in migration. In the US it is rising slowly, because of high fertility and migration.

The problem with *life expectancy at median age* is "that it is not directly comparable to the median age itself." That's why we need the *standardized median age* this means **the median age of the the life expectancy standardized population**. So you pick a reference year, e.g. 2000, and use that life table to assign people ages that have the same remaining life expectancy as they did in 2000. And then calculate the median age of this standardized population. By definition—if you've used the same country's life table as the reference—the standardized median age will be the same as the median age in the reference year.

OK, so you take a population age distribution in a certain year, as well as the remaining life expectancies for each age. Then you match those with the remaining life expectancies in the reference year and replace their ages. Still not seeing an intuitive way to comprehend what is happening. So the remaining life expectancy at the standardized median age is now constant—it is the remaining life expectancy at the median age in the reference year.

Then in part II they use Lee and Goldstein (2003) rescaling—namely proportional rescaling—to compare the regular old age dependency ratio to one where the start and end of the work phase (20 and 65) rescale proportionally to changes in life expectancy. And it is of course very slow, considerably slower than the sometimes even quadrupling of the standard measure.

Lee and Goldstein (2003)—Rescaling the life cycle: Longevity and Proportionality

Referenced in Sanderson and Scherbov (2005) - but unclear, perhaps as the source of the dependency ratio idea - rescaling it obviously.

Speculation about how the life cycle will be modified in response to increased life expectancy.

Proportional rescaling is a convenient benchmark, seems neutral, but there are biological constraints, institutional constraints and *stock-flow* inconsistencies can cause human and physical capital to rise more rapidly than the labour force. Time in retirement is rising faster than longevity, not proportionally. (not sure I get this human capital thing, hopefully later).

Strong proportional rescaling affects both the average timings of transitions as well as their distribution. E.g. if the timing of the menopause doubled, the spread around the mean age of menopause would also double. If the variance stayed the same then we call it *weak proportionality*.

flow or *rate* variables are measured per unit of time, and **stock* variables are not. Completed fertility, accumulated wealth, probability of ever marrying etc. are stocks. Birth, death rates, income etc. are flows.

Perfectly proportional rescaling means all stocks stay the same (relative to the same % of the life cycle), and the flow variables reduce proportionally.

In biology the study of proportional rescaling between species is the study of *biological invariants*. One example is the relationship between age at maturity and expected years of adulthood. Biological invariants are the result of maximisation of reproductive fitness i.e. the forces of natural selection. **But** human's increased longevity is not the result of natural selection, but technological advances, changes in life style, social organization, nutrition etc. So we should not expect the biological invariants to apply here necessarily. But then again there seems to be some sort of common underlying biological principle.

Increasing life expectancy is added to different life phases depending on when it happens. When l_{ex} is 20 then the majority of an additional year is gained in the 15-65 period (0.7), 0.2 in the 0-15 period and only 0.1 in the over 65 one. But at $l_{ex} = 77$ the majority, 0.7 is over 65. Historically mortality has declined faster in infancy, but not proportionally with the rescaling. The actual change of mortality is (Fries) *compression of morbidity*. Compare $l(x)$ in 1900 and 1995 for example. $l(1)$ in 1900 = $l(59)$ in 1995!!! That's 5800% increase. Corresponding increases for $l(30)$, $l(60)$ and $l(90)$ are 137%, 33% and 10%. Under strong proportionality these increases would be the same at all ages.

"Under proportional stretching of the life cycle the time spent disabled or in ill health would rise in proportion to longevity, as would the time spent free of disability" this is apparently confirmed by data i.e. people that live longer are healthier longer, and health costs in old age are more closely related to time until death than to chronological age. This means (see also Fuchs (1984)) that (*ceteris paribus*) increased longevity means fewer persons at any age are about to die, so health costs should go down. So disability and health could be proportional, but could also be shrinking (i.e. *compression of morbidity*)

Other things apart from survivalship and health and disability that are part of the life cycle for humans are adulthood transitions: education, marriage and onset of childbearing. All are being postponed at a faster pace than the pace of longevity increase. All three are shifting to later ages, but also at different rates, so their interrelationship is changing. Education is also lasting longer, but is also starting faster, which is completely off the proportionality hypothesis, since it is an acceleration in life cycle timing.

Biologically there is also an acceleration of menarche and physical maturity. But there is no change in the timing of the menopause.

Population level implications of rescaling: with imperfect proportionality where the mean age of reproduction does not change at the same pace as longevity this will affect population size, the overlap of generations and dependency ratios. So if fertility stays the same but longevity increases then population size and number of generations increases and dependency ratio decreases.

But this also works in the opposite direction: if you have sub-replacement fertility then you can rescale old age, e.g. from 65 to 70, to keep pensioners as a constant proportion of the population.

Rescaling and economic behaviour: retirement trends: quote Kotlikoff (1981) as proposing two options for dealing with longer life expectancy: rise retirement in proportion with life expectancy or more than in proportion, which would keep the years of retirement constant. In fact age of retirement has been falling - until the end of the 20th century anyway.

If you look at the ratio of years worked to years in retirement, it used to be .1 in 1900 US and by 1995 it had almost quadrupled to .38

Working hours as a proportion of available hours has declined from 50% to 20% of our lifetime! Of course this is not only to do with longevity, we have more money and leisure is a luxury good.

Also there are institutional factors leading to early departure from the labour force: age discrimination, incentives in employer provided defined benefit pensions especially in combination with tax and benefit policies. All of these have led to early retirement in contradiction to the rescaling of the life cycle.

So, in summary: the proportional rescaling of the life-cycle is a convenient baseline. In practice it does not occur, different stages are changing in different directions and at non-proportional rates. This is due to behavioural reasons (e.g. more leisure), institutional (incentives for early retirement) and biological reasons (menopause) because longevity increases are not the results of evolutionary forces that fundamentally change our biology, so these changes are not accompanied by other biological changes.

Sanderson and Scherbov (2006)-A new perspective on population ageing

Summarises the standardized age they introduced in 2005, which they now start calling prospective age.

Recognizing two different ages:

- chronological or retrospective age
- prospective age, forward looking

Many behaviours depend on the number of years left! Which ones?

E.g. saving and investment, acquisition of education, certain medical procedures and other individual behaviours, but also important socially e.g. medical expenditures are especially high in the last year of life: if this is happening at later and later years, then this will lead to estimates of expenditures that are too high if you only look at retrospective age.

“Prospective age also helps in assessing future policies concerning the age at the entitlement to a full public pension. By computing the prospective age at the current entitlement age and holding it constant in population forecasts we demarcate the border between policies that allow an increase in the expected number of years of pension receipt and those that do not.”

And they don't say to stop using chronological age, just to supplement it with this one as well.

Distinction between individuals and populations: Individuals can only get older one year per year. Populations can grow older faster or grow younger. But then when you use two different measurements, they can also grow older by one measure and younger by another.

OK, first they will describe it etc. Then technical: you would naturally want to use cohort life tables, that's the expected remaining life expectancy: the *cohort life expectancy*, but period life tables are much more widely available. So next step is to figure out if they produce the same results, which would allow us to use period tables whenever they are available.

Then a historical comparison of both types of ages for England and Sweden and some other comparisons. And finally another definition of the age dependency ratio - using the prospective age of 65, whatever that means?

Hmm, this is awkward, they use prospective age, which is defined with reference to an index age, and another option is to use years of life remaining, which they recognize Ryder had already come up with in 1975.

Another contribution anticipating this came up in 1944 by Hersch, who talked of *potential life years*.

Hmm, ok, they say prospective age is better than RLE, since it is generally insensitive to whether or not is is computed using period or cohort life tables, which is not the case with remaining life expectancy. Do I get this? No. I mean kinda..

OK, nice analogy with regard to why both period and cohort life tables result in similar prospective age calculations: like translating a paragraph into german and then back or into french and then back. In the end they are very similar, even though the translation intermediate step was quite different.

Historical examples from Sweden and England and Wales.

Medial age is a common measure of population ageing. You can also look at the prospective median age of a population relative to some standard year. So, 1800 to 1944, Sweden looks like constant, slightly falling median age until 1900, then slow, then faster increase. But both period and cohort based prospective median ages had been falling constantly until 1920 when started to rise a bit. Over the period as a whole prospective median age fell by 9 years, while the retrospective median rose by 8 years.

Population ageing in the future—forcasts mortality rates, create period and cohort life tables and calculate teh propspective median ages. The alternative is based on which mortality rate trend they use, the UN one or the one where it's .2 years increase of life expectancy per year. But in both cases the medians are similar regardless of the type of life table.

Recent history of ageing in developend countries—how is prospective median age a useful complement to median age in studying populaiton agien. Well, you have to pick a population/year as a standard and that then allows you to compare countris over time. “*Because of increasing life expectancies, prospective median ages rise less rapidly than median ages.*”

age as a twodimensional concept

Old-age dependency ratios are great for looking at retirement and burden of public pensions. But using 65 as the onset of ‘old age dependency’ has become outdated, and will become more and more so. So Prospective Old Age Dependency Ration POADR is defined using a standard year and then the prospective age of 65. They seem to generally rise at half the speed of conventional dependency ratios. They also seem to peak and then reverse, which never happens with conventional ones.

!!Important. Here they are defining POADR using a standard year, e.g. starting in 2000 and the retrospective age of 65, then calculate the prospective age in other years and just use that to calculate the dependency ratio. And not to use e.g. RLE15 as the threshold of old age. In the 2008 paper they redefine it as the latter though Sanderson and Scherbov (2008).

Conventional measures provide an incomplete picture of ageing and can result in poorly designed policies. Intead of backward looking measures they propose to supplement it with a forward looking measure.

Lutz, Sanderson, and Scherbov (2008)—*The coming acceleration of global population ageing*

Nature paper - summarizing their spiel?

So, first the motivation. Then they suggest three alternative measures to the conventional measures:

- prop over 60 vs prop over RLE15 (quoting Ryder as suggesting a similar measure).
- median age vs. prospective median age (standardized to the year 2000)
- average age vs population average remaining years of life (the weighted average of age-specific remaining life expectancies) - which is from Hersch 1944, also mentioned in Sanderson and Scherbov (2006)

So basiclaly all three measures that are adjusted for longevity show a slower increase. The speed at which these three are increasing peaks before 2035 then slows down.

Then last bit of the paper is abotu their probabilistic projections used, so not really about prospective ageing. Ironically the last figure is the predicted distributions of people over 80, haha. But their point is that there is loads of disagreement amongst scientists about trends in mortality in the future, especially in old age. And

apparently the UN variants only look at fertility uncertainty, which leads to gross underestimation of the uncertainty of future proportions of elderly.

Overall: ageing levels are changing, but speed is also important for adaption. And it will be accelerating for the coming decades (until 2035 or so) before slowing down.

Sanderson and Scherbov (2008)—*Rethinking Age and Ageing*

“In contrast to the growth of interest in and concern about population ageing, the concepts used in analyzing it have remained static.”

60-year-old in 1800 and 2000.

Even the media has picked this up; “40 is the new 30” etc.

The concept of age Increases in life expectancy are not taken into account in common measures of ageing: proportion over 65 and old-age dependency ratio, both use the chronological age 65. They innovatively suggest we all have two ages: chronological age and prospective age based on remaining life expectancy.

So conventional demography is making the unjustified assumption that improvements in health and longevity can be disregarded when looking at ageing.

1984 Fuchs suggested people have nominal and real ages: nominal is the chronological age at current prices, and real is the inflation adjusted, prospective age. Although he never actually said that. In 2005 then Sanderson and Scherbov independently come up with this idea.

OK, chart explaining prospective age, and explanation is here:

1. We start with a french woman born in 1922, which means that in 1952 she is 30 years old. In that year the prior life expectancy for a 30 year old was 44.7.
2. Now let's take another 30-year old woman, this time in 2005. She has also survived 30 years and her life expectancy is 54.4 years. Both women have a retrospective age of 30 years.

But are they really the same age? The second one has almost ten years longer to live.

3. Now let's look at the same woman in 1952 again. She has 44.7 years to live. Now starting from the other end: who has the same remaining life expectancy in 2005?
4. French women with 44.7 years left to live in 2005 were exactly 40 years old.

So looking this end, the 30-year old and the 40-year old have the same remaining life expectancy, so the prospective age of the 40-year old in 2005 is actually 30 if we use 1952 as the reference year.

Then there's the inflation analogy.

So, prospective age is important because it affects how people live their lives and plan for the future, and how pension plans are designed.

Defining old Age

Ryder et al suggested this already, defining old age as a threshold after which people have a certain number of years left to live has its faults, but it's simple and we have data to measure it.

Proportion of elderly Globally: prop over 65 looks like we've been ageing since 1955, while prop over 75 looks like it's been getting younger until around 85, then stable until 2015 and only growing older now.

Old-age dependency ratio and prospective OADR. The latter is way less extreme than the former, changes the ranking of ageing countries dramatically. POADR is redefined here compared to the 2006 paper (Sanderson and Scherbov (2006)), where it was defined prospectively like the median age, with reference to a standard year. Now it is simply based on the old-age threshold.

Median age - in order to calculate the prospective median age you need to use a standard life table, which you don't need for the other two.

Ranking by POADR and OADR changes, I need to do that for prop over 65/RLE15

New thinking applied to policy: Older people are more active today than they were in previous generations. The oldest person to climb Mt everest was 80 years old. None of the standard measures adjust for increases in life expectancy. How do we take prospective age into account in policy?

- fixed chronological retirement age is not fair on younger generations. But of course a fixed prospective retirement age is not fair on older generations: they would work longer and longer and get the same number of years of benefits. S&S suggest averaging them - which is silly, obviously you do another measure which keeps the proportion constant.. This was in Fuchs, was it not?
- Formulating policies based on prospective ages is important also if life expectancy gains reverse.
- The argument has been made that an older electorate will lead to more short-termism, but that's ignoring the increase in life expectancy. So increased median ages can actually be decreases in prospective median age, which means a longer time horizon.

“Perhaps the most innovative feature of our approach is that we think about people as simultaneously having two ages.”

Hm, what about thinking about people as having a relative age instead, instead of being 65 years old and 15 left to live, how about having 18 percent left to live? So instead of two absolute ages, have a single relative age. me.

D’Albis and Collard (2013) - *Age groups and the measure of Population ageing*

Not sure where i found this paper?

Start off with Ryder’s Ryder (1975) idea of using the number of years left to live, which was then pursued by Sanderson and Scherbov (2005). The problem with this approach is that at any time you do not know an individual’s life expectancy, but have to use life tables to estimate it. The second problem is that proportional rescaling affects it: if life expectancy increases all else remaining equal, then the proportion over the threshold gets smaller. Is this a problem? So under prospective age in a stationary population with a rectangular survival curve, an increase in longevity would meant the population is getting younger.

References

- Bayó, Francisco, and Joseph F Faber. 1981. *Equivalent Retirement Ages, 1940-2050*. 105. US Department of Health; Human Services, Social Security Administration.
- Cain, L. D. 1974. “The growing importance of legal age in determining the status of the elderly.” *Gerontologist* 14 (2):167–74. <https://doi.org/10.1093/geront/14.2.167>.
- D’Albis, Hippolyte, and Fabrice Collard. 2013. “Age groups and the measure of population aging.” *Demographic Research* 29:617–40. <https://doi.org/10.4054/DemRes.2013.29.23>.
- Fuchs, Victor R . 1984. “Though Much is Taken - Reflections on Aging, health and Medical Care Working Paper No . 1269.” Cambridge, MA: NATIONAL BUREAU OF ECONOMIC RESEARCH.
- Lee, Ronald, and Joshua R Goldstein. 2003. “Rescaling the life cycle: Longevity and proportionality.” *Population and Development Review* 29. JSTOR:183–207.
- Lutz, Wolfgang, Warren Sanderson, and Sergei Scherbov. 2008. “The coming acceleration of global population ageing.” *Nature* 451 (7179). Nature Publishing Group:716.
- Ryder, Norman B . 1975. “Notes on Stationary Populations.” *Population Index* 41 (1):3–28.
- Sanderson, Warren C., and Sergei Scherbov. 2005. “Average remaining lifetimes can increase as human populations age.” *Nature* 435 (7043):811–13. <https://doi.org/10.1038/nature03593>.

- . 2006. “A new perspective on population aging.” *Demographic Research* 16. <https://doi.org/10.4054/DemRes.2007.16.2>.
- . 2015. “Faster increases in human life expectancy could lead to slower population aging.” *PLoS ONE* 10 (4):1–9. <https://doi.org/10.1371/journal.pone.0121922>.
- Sanderson, Warren, and Sergei Scherbov. 2008. *Rethinking age and aging*. Population Reference Bureau Washington, DC.
- Siegel, Jacob S. 1980. “On the demography of aging.” *Demography* 17 (4). Springer:345–64.