Chapter 1—The discrete case: mulitnomial Bayesian networks

mz

1.1 Introduction example: Train use survey

```
# preliminaries:
library(bnlearn)
## Loading required package: methods
##
## Attaching package: 'bnlearn'
## The following object is masked from 'package:stats':
##
##
       sigma
library(vcd)
## Loading required package: grid
library(gRain)
## Loading required package: gRbase
## Attaching package: 'gRbase'
## The following objects are masked from 'package:bnlearn':
       ancestors, children, parents
##
note that some caution must be exercised in interpreting both direct and indirect dependencies. The presence
of arrows or arcs seems to imply, at an intuitive level, that for each arc one variable should be interpreted as
a cause and the other as an effect. This interpretation, which is called causal, is difficult to justify in most
situations; for this reason in general we speak about dependence relationships instead of causal effects. s dddd
dag <- empty.graph(nodes = c("A", "S", "E", "O", "R", "T"))</pre>
dag
##
##
     Random/Generated Bayesian network
##
##
     model:
      [A] [S] [E] [O] [R] [T]
##
##
     nodes:
                                                 6
                                                 0
##
     arcs:
##
       undirected arcs:
                                                 0
##
       directed arcs:
##
     average markov blanket size:
                                                 0.00
##
     average neighbourhood size:
                                                 0.00
##
     average branching factor:
                                                 0.00
##
##
     generation algorithm:
                                                 Empty
```

```
dag <- set.arc(dag, from = "A", to = "E")</pre>
dag <- set.arc(dag, from = "S", to = "E")</pre>
dag <- set.arc(dag, from = "E", to = "0")</pre>
dag <- set.arc(dag, from = "E", to = "R")</pre>
dag <- set.arc(dag, from = "0", to = "T")</pre>
dag <- set.arc(dag, from = "R", to = "T")</pre>
modelstring(dag)
## [1] "[A][S][E|A:S][O|E][R|E][T|O:R]"
arcs(dag)
##
         from to
## [1,] "A" "E"
## [2,] "S" "E"
## [3,] "E"
              "0"
## [4,] "E"
             "R"
## [5,] "O" "T"
## [6,] "R" "T"
A.lv <- c("young", "adult", "old")
S.lv \leftarrow c("M", "F")
E.lv <- c("high", "uni")</pre>
0.lv <- c("emp", "self")</pre>
R.lv <- c("small", "big")
T.lv <- c("car", "train", "other")</pre>
A.prob \leftarrow array(c(0.3, 0.5, 0.2), dim = 3,
                  dimnames = list(A = A.lv))
S.prob \leftarrow array(c(0.6, 0.4), dim = 2,
                  dimnames = list(S = S.lv))
R.prob \leftarrow array(c(0.25, 0.75, 0.2, 0.8), dim = c(2,2),
                  dimnames = list(R = R.lv, E = E.lv))
0.\text{prob} \leftarrow \text{array}(c(0.96, 0.04, 0.92, 0.08), \text{dim} = c(2,2),
                  dimnames = list(0 = 0.1v, E = E.1v))
E.prob \leftarrow array(c(.75, .25, .72, .28, .88, .12, .64, .36, .70, .30, .90, .10),
                  \dim = c(2,3,2),
                  dimnames = list(E = E.lv, A = A.lv, S = S.lv))
T.prob \leftarrow array(c(.48, .42, .10, .56, .36, .08, .58, .24, .18, .70, .21, .09),
                  \dim = c(3,2,2),
                  dimnames = list(T = T.lv, 0 = 0.lv, R = R.lv)
dag3 <- model2network("[A][S][E|A:S][0|E][R|E][T|0:R]")</pre>
all.equal(dag, dag3)
## [1] TRUE
cpt <- list(A = A.prob, S = S.prob, E = E.prob, O = O.prob, R = R.prob, T = T.prob)
bn <- custom.fit(dag, cpt)</pre>
```

```
nparams(bn)
## [1] 21
arcs(bn)
##
        \quad \hbox{from to} \quad
## [1,] "A" "E"
## [2,] "S" "E"
## [3,] "E" "O"
## [4,] "E" "R"
## [5,] "O" "T"
## [6,] "R" "T"
bn$R
##
    Parameters of node R (multinomial distribution)
##
##
## Conditional probability table:
##
##
          Ε
## R
          high uni
     small 0.25 0.20
##
     big 0.75 0.80
coef(bn$R)
##
## R
          high uni
     small 0.25 0.20
##
     big 0.75 0.80
##
```