

Dear editor,

Accurate characterisation of the nuclear spin environment is pivotal for understanding of an environment of a solid state register. This information is crucial for purification of the register operation but also is a resource for extending the register itself, utilising the spins in the environment as so. As recently the success of the pushing the registers using environmental nuclear spins reached around 50 qubits with most studied NV centers in diamond, a surge for spin characterisation techniques suitable for many other colour centers is long awaited in our opinion. Partially this is also motivated by the challenge and interest which a simplest $S=1/2$ electron spin systems present. The most successful and widespread technique - namely the dynamical decoupling is not applicable in their case. Quite interestingly, a detour to the world of conventional EPR type techniques, such as ESEEM, (5p, 3p and more exotic, such as HYSCORE) appears useful. Now applied at the level of single $S=1/2$ systems, it might overperform the conventional DD sequences in terms of resolution and sensitivity to the hyperfine parameters of the nuclear spins in the bath. We quantitatively demonstrate how such sequence performs in various scenarios on the example of the well studied 27 nuclear spin bath. We utilise the Cramer Rao bound for estimating the uncertainty and number of identified nuclear spins using various techniques.

We strongly believe that our work is of importance for future development of colour centers with $S=1/2$ electron spins, such as Group IV heavy elements split vacancies, as well as newly developed T centers in Silicon and many others.

On behalf of all authors,
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