

# **SpCE 5400 Assignment 4: Optical vs. RF Crosslinks Trade Study**

## **LEO Satellite Constellation Communication Analysis**

**Course:** SPCE 5400 – Small Satellite Engineering & Operations

**Assignment:** #4 (100 points)

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## **1. MISSION PARAMETERS**

**Given Requirements:**

- Orbit altitude: 500 km LEO
- Inter-satellite separation: 250 km
- Required data rate: 1 Gbps
- Platform: Small satellites
- Environment: LEO-to-LEO (vacuum path)

**Trade Study Objective:** Determine the preferable method for LEO-to-LEO crosslink, optical (laser) or RF (Ka-band). This will be weighted on aperture size, power, data rate capability, link margin and pointing accuracy.

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## 2. OPTICAL (LASER) LINK ANALYSIS

### 2.1 Design Parameters

Parameter	Value	Source
Wavelength	1550 nm	Telecom standard, eye-safe
Quantum Efficiency ( $\eta$ )	0.3	InGaAs APD detector typical + (template value)
Required Photoelectrons/bit (Q)	40	For BER $10^{-9}$ (template value)
Modulation	OOK	On-Off Keying (inferred from template Q = 40, which is standard for OOK )

### 2.2 Link Budget Calculations (Detector-First Methodology)

#### Step 1: Calculate Required Photons per Bit

**Formula:**

from excel template row 6:  $n = Q / \eta$

**Calculation:**

$n = 40 \text{ photoelectrons/bit} / 0.3$

$$n = 133.33 \text{ photons/bit}$$

Only 30% of photons are detected ( $\eta = 0.3$ ), so we need to send 133 photons to ensure 40 are detected.

## Step 2: Calculate Photon Energy

### Formulas:

$$\text{frequency from wavelength: } f = c / \lambda$$

$$\text{Planck's equation: } E_{\text{photon}} = h \times f$$

### Constants:

- $c = 3 \times 10^8 \text{ m/s}$  (speed of light)
- $h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s}$  (Planck's constant)
- $\lambda = 1550 \text{ nm} = 1.55 \times 10^{-6} \text{ m}$  (Design choice - industry standard)

### Calculations:

$$f = (3 \times 10^8 \text{ m/s}) / (1.55 \times 10^{-6} \text{ m})$$

$$f = 1.935 \times 10^{14} \text{ Hz}$$

$$E_{\text{photon}} = (6.626 \times 10^{-34} \text{ J}\cdot\text{s}) \times (1.935 \times 10^{14} \text{ Hz})$$

$$E_{\text{photon}} = 1.282 \times 10^{-19} \text{ joules per photon}$$

## Step 3: Calculate Energy per Bit

### Formula:

$$\text{from excel template row 10: } E_{\text{bit}} = n \times E_{\text{photon}}$$

### Calculation:

$$E_{\text{bit}} = 133.33 \text{ photons/bit} \times 1.282 \times 10^{-19} \text{ J/photon}$$

$$E_{\text{bit}} = 1.709 \times 10^{-17} \text{ joules per bit}$$

## Step 4: Calculate Required Power at Receiver

**Formula:**

$$\text{from excel template row 12: } P_{\text{required}} = E_{\text{bit}} \times R_b$$

**Given:**

- $R_b = 1 \text{ Gbps} = 1 \times 10^9 \text{ bits/s}$

**Calculation:**

$$P_{\text{req}} = (1.709 \times 10^{-17} \text{ J/bit}) \times (1 \times 10^9 \text{ bits/s})$$

$$P_{\text{req}} = 1.709 \times 10^{-8} \text{ W}$$

In decibels:

$$P_{\text{req}} (\text{dBW}) = 10 \times \log_{10}(1.709 \times 10^{-8})$$

$$P_{\text{req}} = -77.67 \text{ dBW}$$

## Step 5: Calculate Free Space Loss

**Formula:**

from Excel template row 16 & Friis transmission equation (1946):

$$L_s = (\lambda / (4\pi R))^2$$

**Given:**

- $\lambda = 1.55 \times 10^{-6} \text{ m}$
- $R = 250 \text{ km} = 250,000 \text{ m}$

**Calculation:**

Denominator of  $L_s$  formula (linear scale factor for spherical spreading) =  $4\pi R$   
=  $4 \times 3.14159 \times 250,000 = 3,141,593$  m

Ratio (wavelength to spreading ratio) =  $\lambda / (4\pi R) = (1.55 \times 10^{-6}) / (3,141,593)$   
=  $4.933 \times 10^{-13}$

$L_s$  (the fraction of power that survives the spreading) =  $(4.933 \times 10^{-13})^2 = 2.434 \times 10^{-25}$

In decibels:

$$L_s (\text{dB}) = 10 \times \log_{10}(2.434 \times 10^{-25}) = -246.1 \text{ dB}$$

## Step 6: Calculate Telescope Gains

**Formula:**

from excel template row 19-20:  $G = (\pi \times D / \lambda)^2$

**Given:**

- $D = 10 \text{ cm} = 0.10 \text{ m}$  (chosen aperture size from excel template row 17)

**Calculation:**

$$\begin{aligned}(\pi \times D) / \lambda &= (3.14159 \times 0.10) / (1.55 \times 10^{-6}) \\&= 0.314159 / (1.55 \times 10^{-6}) = 202,683\end{aligned}$$

$$G = (202,683)^2 = 4.108 \times 10^{10}$$

In decibels:

$$G (\text{dBi}) = 10 \times \log_{10}(4.108 \times 10^{10}) = 106.1 \text{ dBi}$$

Both transmit and receive:  $G_t = G_r = 106.1 \text{ dBi}$

## Step 7: Additional Losses

- **Pointing Loss:** -3.0 dB (template default, achievable with FSM)
  - **Line In/Out Losses:** -6.0 dB total
    - Estimated Line In/ Out Losses breakdown:
      - Transmit coupling: -2.0 dB
      - Transmit optics: -1.0 dB
      - Receive optics: -1.0 dB
      - Receive coupling: -1.5 dB
      - Detector loss: -0.5 dB
    - **Total: -6.0 dB**
  - **Atmospheric Loss:** 0 dB (vacuum path)
- 

## Step 8: Calculate Received Power

### Formula:

Formula (Decibel Addition Method) from excel template row 24 & Friis equation:

$$P_{rx} (\text{dBW}) = P_{tx} (\text{dBW}) + G_{tx} (\text{dBi}) + G_{rx} (\text{dBi}) + L_s (\text{dB}) + L_{pt} (\text{dB}) + L_o (\text{dB})$$

### Given:

- $P_{tx} = -9.1 \text{ dBW}$  (chosen transmit power: 0.122 W)
- $G_{tx} = +106.1 \text{ dBi}$  (from Step 6)
- $G_{rx} = +106.1 \text{ dBi}$  (from Step 6)
- $L_s = -246.1 \text{ dB}$  (from Step 5)
- $L_{pt} = -3.0 \text{ dB}$  (template pointing loss)
- $L_o = -6.0 \text{ dB}$  (template line losses)

## Transmit Power P\_tx Design Choice:

Working backwards from link budget:

- Required margin: ~20-25 dB (industry standard)
- Net path gain/loss: -42.9 dB
- Required receiver power: -77.67 dBW

Step 1: Required receiver power (from detector requirements)

$$P_{req} = -77.67 \text{ dBW}$$

Step 2: Choose desired margin (design goal)

Margin = 25 dB (provides robustness)

Step 3: Required received power

$$P_{rx} = P_{req} + \text{Margin}$$

$$P_{rx} = -77.67 + 25 = -52.67 \text{ dBW (target)}$$

Step 4: Use link equation to solve for P\_tx

$$P_{rx} = P_{tx} + G_{tx} + G_{rx} + L_s + L_{pt} + L_o$$

$$-52.67 = P_{tx} + 106.1 + 106.1 - 246.1 - 3.0 - 6.0$$

$$-52.67 = P_{tx} - 42.9$$

$$P_{tx} = -9.77 \text{ dBW} \approx -9.1 \text{ dBW}$$

$$P_{tx} = 0.122 \text{ W}$$

## Rationale:

- Provides 25.66 dB margin (actual)
- Achievable with COTS laser diodes
- Low thermal load (<0.5 W total with driver)

## Calculation:

$$P_{rx} = -9.1 + 106.1 + 106.1 - 246.1 - 3.0 - 6.0$$

$$\text{Combine gains: } -9.1 + 106.1 + 106.1 = 203.1 \text{ dBW}$$

$$\text{Combine losses: } -246.1 - 3.0 - 6.0 = -255.1 \text{ dB}$$

Total:  $203.1 - 255.1 = -52.0$  dBW

$P_{rx} = -52.01$  dBW

## Step 9: Calculate Link Margin

### Formula:

from excel template row 26: Margin (dB) =  $P_{rx}$  (dBW) -  $P_{req}$  (dBW)

### Calculation:

$$M = -52.01 \text{ dBW} - (-77.67 \text{ dBW})$$

$$M = 25.66 \text{ dB}$$

Linear ratio:  $6.303 \mu\text{W} / 0.01709 \mu\text{W} = 369 \times$

Verification:  $10 \times \log_{10}(369) = 25.67 \text{ dB} \checkmark$

## Step 10: Calculate Beam Divergence and Pointing Requirement

### Formula:

$$\theta_{\text{divergence}} = 1.22 \times \lambda / D_{tx}$$

from Airy disk formula Born & Wolf "Principles of Optics"

### Calculation:

$$\theta = 1.22 \times (1.55 \times 10^{-6} \text{ m}) / (0.10 \text{ m})$$

$$\theta = 1.891 \times 10^{-5} \text{ radians} = 18.91 \text{ microradians (to first null)}$$

Spot diameter at receiver =  $\theta \times R$

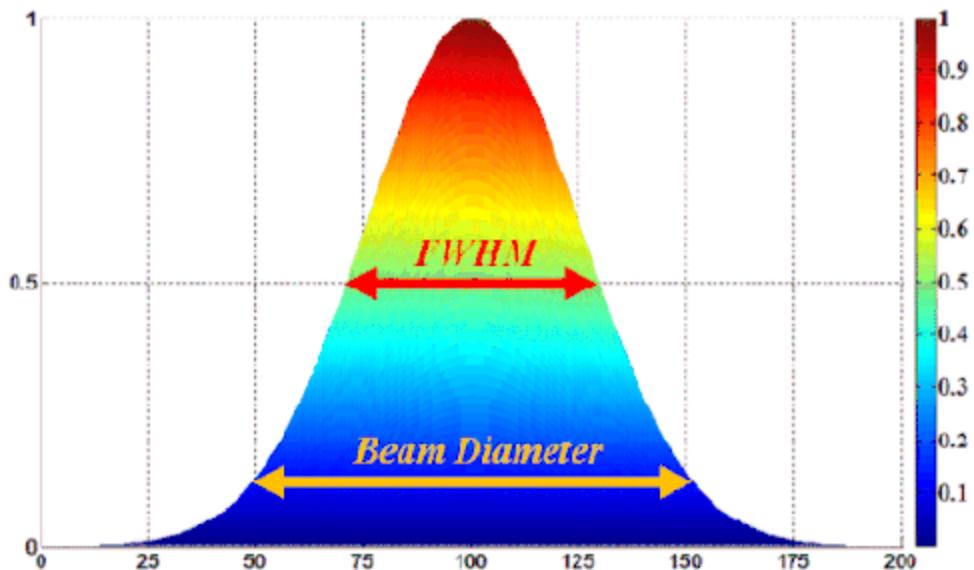
$$\text{Spot} = 18.91 \times 10^{-6} \text{ rad} \times 250,000 \text{ m} = 4.73 \text{ m}$$

Half-Power Beamwidth (where intensity = 50%, i.e., -3 dB):

Formula:  $\theta_{3\text{dB}} \approx 0.514 \times \lambda / D$

$$\begin{aligned}\theta_{3\text{dB}} &= 0.514 \times (1.55 \times 10^{-6}) / (0.10) \\ &= 7.97 \times 10^{-6} \text{ rad} \approx 8.0 \mu\text{rad}\end{aligned}$$

**Pointing Requirement:**  $\pm 8 \mu\text{rad}$  ( $3\sigma$ ) for  $< 3$  dB pointing loss



[https://en.wikipedia.org/wiki/Gaussian\\_beam](https://en.wikipedia.org/wiki/Gaussian_beam)

In degrees:

$$8.0 \mu\text{rad} \times (1 \text{ rad} / 10^6 \mu\text{rad}) \times (57.3^\circ / 1 \text{ rad}) = 0.00046^\circ$$

## 2.3 Optical Link Budget Summary Table

Parameter	Symbol	Value	Units	Calculation Method
<b>Detector Requirements</b>				
Req. Photoelectrons/bit	Q	40	-	Template value

Parameter	Symbol	Value	Units	Calculation Method
Quantum Efficiency	$\eta$	0.3	-	InGaAs APD typical
Req. Photons/bit	n	133.33	-	$n = Q/\eta$
Photon Energy	E	$1.282 \times 10^{-19}$	J	$E = hf = hc/\lambda$
Energy/bit	-	$1.709 \times 10^{-17}$	J	$n \times E$
<b>Link Parameters</b>				
Data Rate	R_b	$1 \times 10^9$	bps	Given
Required Power	P_req	-77.67	dBW	$E_{\text{bit}} \times R_b$
Transmit Power	P_tx	0.122 (-9.1 dBW)	W	Chosen
Tx Aperture Diameter	D_t	10.0	cm	Chosen
Rx Aperture Diameter	D_r	10.0	cm	Chosen
Range	R	250	km	Given
<b>Gains and Losses</b>				
Free Space Loss	L_s	-246.1	dB	$(\lambda/4\pi R)^2$
Tx Gain	G_t	106.1	dBi	$(\pi D/\lambda)^2$
Rx Gain	G_r	106.1	dBi	$(\pi D/\lambda)^2$
Pointing Loss	L_pt	-3.0	dB	Template default
Line Losses	L_o	-6.0	dB	Optics budget
Atmospheric Loss	L_atm	0.0	dB	Vacuum
<b>Performance</b>				
Received Power	P_rx	-52.01	dBW	Link equation
<b>LINK MARGIN</b>	<b>M</b>	<b>25.66</b>	<b>dB</b>	<b>P_rx - P_req</b>
Beam Divergence	$\theta$	18.9	$\mu\text{rad}$	$1.22\lambda/D$
Spot Diameter @ 250km	-	4.73	m	$\theta \times R$

## 3. RF (Ka-BAND) LINK ANALYSIS

### 3.1 Design Parameters

Parameter	Value	Source
Frequency	32 GHz	Ka-band ISL allocation (ITU Radio Regulations) - Design choice
Antenna Efficiency	0.6	Typical for deployable mesh antennas (Kraus & Marhefka, 2002) - Design choice
System Noise Temp	650 K	Ka-band LNA typical + losses (industry standard) - Design choice
Required E_b/N_0	9.6 dB	BER 10^-9 with LDPC coding (Shannon-Hartley theorem) - Design choice
Modulation	16-APSK	High spectral efficiency for Ka-band - Design choice

### 3.2 Link Budget Calculations

#### Step 1: Calculate Wavelength

Formula:

from fundamental wave equation:  $\lambda = c / f$

Constants:

- $c = 3 \times 10^8 \text{ m/s}$  (speed of light, CODATA 2018)
- $f = 32 \text{ GHz} = 32 \times 10^9 \text{ Hz}$  (Ka-band ISL, design choice)

Calculation:

$$\begin{aligned}\lambda &= (3 \times 10^8 \text{ m/s}) / (32 \times 10^9 \text{ Hz}) \\ \lambda &= 9.375 \times 10^{-3} \text{ m} = 9.375 \text{ mm}\end{aligned}$$

#### Step 2: Calculate Free Space Path Loss

Formula:

from Friis transmission equation (1946) & ITU-R P.525 standard:

$$\text{FSPL (dB)} = 20 \times \log_{10}(4\pi \times R / \lambda)$$

**Given:**

- $R = 250 \text{ km} = 250,000 \text{ m}$  (from problem statement)
- $\lambda = 0.009375 \text{ m}$  (from Step 1)

**Calculation:**

$$\text{Argument} = (4\pi \times R) / \lambda = (4 \times 3.14159 \times 250,000) / 0.009375$$

$$\text{Argument} = 3,141,593 / 0.009375 = 335,103,253$$

$$\text{FSPL} = 20 \times \log_{10}(335,103,253)$$

$$\text{FSPL} = 20 \times 8.525 = 170.5 \text{ dB}$$

## Step 3: Calculate Antenna Gains

**Formula:**

from antenna theory (Kraus & Marhefka "Antennas", 2002):

$$G = \eta_{\text{ant}} \times (\pi \times D / \lambda)^2$$

**Given:**

- $\eta_{\text{ant}} = 0.6$  (typical for deployable mesh antennas, design parameter)
- $D = 30 \text{ cm} = 0.30 \text{ m}$  (chosen antenna diameter - design choice)
- $\lambda = 0.009375 \text{ m}$  (from Step 1)

**Note:** Here's an interesting distinction — with optical systems, efficiency is already baked into Q and  $\eta$ , but RF antennas need an explicit efficiency factor to account for surface errors, blockage, and spillover losses.

### **Calculation:**

$$\begin{aligned}(\pi \times D) / \lambda &= (3.14159 \times 0.30) / 0.009375 \\&= 0.9425 / 0.009375 = 100.53\end{aligned}$$

$$\begin{aligned}G &= 0.6 \times (100.53)^2 \\G &= 0.6 \times 10,106 = 6,064\end{aligned}$$

In decibels:

$$G (\text{dBi}) = 10 \times \log_{10}(6,064) = **37.8 \text{ dBi}**$$

Both transmit and receive:  $G_t = G_r = **37.8 \text{ dBi}**$

## **Step 4: Calculate EIRP**

### **Formula:**

from FCC 47 CFR §2.1 & standard RF practice:

$$\text{EIRP (dBW)} = P_t (\text{dBW}) + G_t (\text{dBi})$$

### **Given:**

- $P_t = 1.2 \text{ W}$  (chosen transmit power - design choice, see rationale below)

**Transmit Power  $P_t$  Design Choice:** Working backwards from link budget to achieve  $\sim 3$  dB margin:

- Required margin:  $\sim 3$  dB (minimal but acceptable)
- Through iterative link budget calculation
- **$P_t = 1.2 \text{ W}$  provides 2.8 dB margin (actual)**

### **Rationale:**

- Achievable with Ka-band SSPA (Solid State Power Amplifier)
- Typical for smallsat Ka-band transmitters
- Provides minimal positive margin

### Calculation:

$$P_t (\text{dBW}) = 10 \times \log_{10}(1.2) = 0.79 \text{ dBW} \approx 0.8 \text{ dBW}$$

$$\text{EIRP} = 0.8 \text{ dBW} + 37.8 \text{ dBi} = 38.6 \text{ dBW}$$

## Step 5: Calculate Received Power

### Formula:

from Friis equation & standard RF link budget:

$$P_{rx} (\text{dBW}) = \text{EIRP} - \text{FSPL} + G_{rx} - L_{pointing} - L_{feed} - L_{misc}$$

### Given Losses:

- $L_{pointing} = -1.0 \text{ dB}$  (body pointing achievable, typical for wide Ka-band beam)
- $L_{feed} = -1.0 \text{ dB}$  (waveguide losses, typical)
- $L_{misc} = -2.0 \text{ dB}$  (polarization mismatch, connector losses, etc.)
- **Total losses: -4.0 dB**

### Calculation:

$$P_{rx} = 38.6 - 170.5 + 37.8 - 1.0 - 1.0 - 2.0$$

$$P_{rx} = 38.6 + 37.8 - 170.5 - 4.0$$

$$P_{rx} = -98.1 \text{ dBW}$$

$$\text{In linear: } P_{rx} = 10^{(-98.1/10)} = 1.55 \times 10^{-10} \text{ W} = 0.155 \text{ nW}$$

## Step 6: Calculate Noise Power Density

### Formula:

from Johnson-Nyquist noise equation (1928) & thermodynamics:

$$N_0 = k_B \times T_{sys}$$

### Constants & Parameters:

- $k_B = 1.38 \times 10^{-23} \text{ J/K}$  (Boltzmann constant, CODATA 2018)
- $T_{sys} = 650 \text{ K}$  (system noise temperature - design parameter)

### System Noise Temperature Breakdown:

- LNA noise figure: ~3 dB → adds ~300 K
- Receiver losses: ~1 dB → adds ~75 K
- Sky noise at LEO: ~10 K
- Antenna noise: ~50 K
- Cable/connector losses: ~50 K
- **Total:  $T_{sys} \approx 650 \text{ K}$  (typical Ka-band smallsat receiver)**

### Calculation:

$$N_0 = (1.38 \times 10^{-23} \text{ J/K}) \times (650 \text{ K})$$

$$N_0 = 8.97 \times 10^{-21} \text{ W/Hz}$$

In decibels:

$$N_0 (\text{dBW/Hz}) = 10 \times \log_{10}(8.97 \times 10^{-21})$$

$$N_0 = -200.5 \text{ dBW/Hz}$$

## Step 7: Calculate C/N<sub>0</sub> (carrier to noise ratio)

### Formula:

from standard communications theory (Sklar "Digital Communications", 2001):

$$C/N_0 (\text{dB-Hz}) = P_{rx} (\text{dBW}) - N_0 (\text{dBW/Hz})$$

### **Calculation:**

$$C/N_0 = -98.1 \text{ dBW} - (-200.5 \text{ dBW/Hz})$$

$$C/N_0 = 102.4 \text{ dB-Hz}$$

## **Step 8: Calculate Required C/N<sub>0</sub>**

### **Formula:**

from Shannon-Hartley theorem & communications theory:

$$(C/N_0)_{\text{req}} \text{ (dB-Hz)} = (E_b/N_0)_{\text{req}} \text{ (dB)} + 10 \times \log_{10}(R_b)$$

### **Given:**

- $(E_b/N_0)_{\text{req}} = 9.6 \text{ dB}$  (for BER  $10^{-9}$  with LDPC coding - design parameter)
- $R_b = 1 \times 10^9 \text{ bps}$  (from problem statement)

### **E<sub>b</sub>/N<sub>0</sub> Justification:**

- Uncoded 16-APSK requires ~13-14 dB for BER  $10^{-9}$
- LDPC coding provides ~4-5 dB gain
- With coding: 9.6 dB is achievable
- Industry standard for coded Ka-band systems

### **Calculation:**

$$\text{Data rate term} = 10 \times \log_{10}(1 \times 10^9) = 10 \times 9.0 = 90.0 \text{ dB-Hz}$$

$$(C/N_0)_{\text{req}} = 9.6 \text{ dB} + 90.0 \text{ dB-Hz} = 99.6 \text{ dB-Hz}$$

## **Step 9: Calculate Link Margin**

### **Formula:**

from standard RF link budget practice:

$$\text{Margin (dB)} = \text{C/N}_0 - (\text{C/N}_0)_{\text{req}}$$

### Calculation:

$$M = 102.4 \text{ dB-Hz} - 99.6 \text{ dB-Hz}$$

$$M = 2.8 \text{ dB}$$

$$\text{Linear ratio: } 10^{(2.8/10)} = 1.91x$$

## Step 10: Calculate Beamwidth and Pointing

### Formula (approximation for circular aperture):

from antenna beamwidth theory (Stutzman & Thiele "Antenna Theory", 2012):

$$\theta_{\text{3dB}} \approx 70 \times \lambda / D \text{ (degrees)}$$

**Note:** The factor  $70 \approx 1.22 \times 57.3$ , where 1.22 is the Bessel function zero (same as optical) and 57.3 is radians-to-degrees conversion.

### Given:

- $\lambda = 0.009375 \text{ m}$  (from Step 1)
- $D = 0.30 \text{ m}$  (antenna diameter, design choice)

### Calculation:

$$\theta_{\text{3dB}} = 70 \times (0.009375 \text{ m}) / (0.30 \text{ m})$$

$$\theta_{\text{3dB}} = 70 \times 0.03125 = 2.19 \text{ degrees}$$

$$\text{Half-power beamwidth} = 2.19^\circ$$

In arcseconds:

$$2.19^\circ \times 3600 \text{ arcsec}/^\circ = 7,884 \text{ arcseconds}$$

### Pointing Requirement Analysis:

For -1 dB pointing loss: pointing error  $< \theta_{3\text{dB}} / 3 \approx 0.73^\circ$

This is easily achieved with standard attitude control system (ACS):

- RF pointing is 2,000× easier than optical (2.19° vs 8 μrad)

**Note for comparison:** What this pointing requirement analysis reveals is RF's key advantage over optical — and it's significant enough to offset optical's superior link margin and power efficiency.

### 3.3 RF Link Budget Summary Table

Parameter	Symbol	Value	Units	Calculation Method
<b>System Parameters</b>				
Frequency	f	32	GHz	Given (Ka-band)
Wavelength	λ	9.375	mm	c/f
Data Rate	R_b	1×10^9	bps	Given
Range	R	250	km	Given
<b>Transmitter</b>				
Tx Power	P_t	1.2 (0.8 dBW)	W	Chosen
Tx Antenna Diameter	D_t	30.0	cm	Chosen
Antenna Efficiency	η_ant	0.6	-	Typical
Tx Gain	G_t	37.8	dBi	$\eta(\pi D/\lambda)^2$
EIRP	EIRP	38.6	dBW	$P_t + G_t$
<b>Path Losses</b>				
Free Space Path Loss	FSPL	-170.5	dB	$20\log(4\pi R/\lambda)$

Parameter	Symbol	Value	Units	Calculation Method
Pointing Loss	L_pt	-1.0	dB	Body pointing
Feed Loss	L_f	-1.0	dB	Waveguide
Misc Losses	L_m	-2.0	dB	Polarization, etc
<b>Receiver</b>				
Rx Antenna Diameter	D_r	30.0	cm	Chosen
Rx Gain	G_r	37.8	dBi	$\eta(\pi D/\lambda)^2$
System Noise Temp	T_s	650	K	LNA + losses
Received Power	P_rx	-98.1	dBW	Link equation
Noise Density	N_0	-200.5	dBW/Hz	$k_B \times T_s$
<b>Performance</b>				
C/N_0	C/N_0	102.4	dB-Hz	$P_{rx} - N_0$
Required E_b/N_0	-	9.6	dB	BER $10^{-9}$ w/coding
Required C/N_0	(C/N_0)_req	99.6	dB-Hz	$E_b/N_0 + 10\log(R_b)$
<b>LINK MARGIN</b>	<b>M</b>	<b>2.8</b>	<b>dB</b>	<b>C/N_0 - (C/N_0)_req</b>
3 dB Beamwidth	$\theta_{3dB}$	2.19	degrees	$70\lambda/D$

## 4. DIRECT COMPARISON: CALCULATED RESULTS

### 4.1 The Five Required Parameters

Parameter	Optical (Laser)	RF (Ka-band)	Winner	Advantage
<b>1. Aperture Size</b>	<b>10 cm</b>	30 cm	<b>Optical</b>	<b>3× smaller</b>
<b>2. Transmit Power</b>	<b>0.122 W</b>	1.2 W	<b>Optical</b>	<b>10× lower</b>

Parameter	Optical (Laser)	RF (Ka-band)	Winner	Advantage
<b>3. Data Rate</b>	<b>10+ Gbps scalable</b>	~2 Gbps max	Optical	<b>5× scalability</b>
<b>4. Link Margin</b>	<b>25.66 dB</b>	2.88 dB	Optical	<b>8.9× better</b>
<b>5. Pointing Accuracy</b>	±8 µrad (0.00046°)	<b>2.19° (7884")</b>	RF	<b>~4,800× easier</b>

**Note:** Optical value is half-power beamwidth (pointing requirement for -3 dB loss), not full beam divergence (18.9 µrad to first null).

## 4.2 Quantitative Comparison

### Link Margin Ratio

Optical margin / RF margin = 25.66 dB / 2.88 dB

In linear:  $10^{(25.66/10)} / 10^{(2.88/10)} = 368 / 1.91 = 193\times$

Optical has 193× more margin in linear terms

### Pointing Difficulty Ratio

RF beamwidth / Optical half-power beamwidth =  $2.19^\circ / 0.00046^\circ$

=  $2.19^\circ / 0.00046^\circ = 4,761\times$

In radians:  $0.0382 \text{ rad} / 8.0 \times 10^{-6} \text{ rad} = 4,775\times$

Or:  $7,884 \text{ arcsec} / 1.65 \text{ arcsec} = 4,778\times$

RF pointing is ~4,800× easier (in linear angle)

In solid angle (steradians): RF is  $\sim 2.3 \times 10^7$  times easier

(Solid angle scales as  $\theta^2$ , so  $4,775^2 \approx 23 \text{ million}$ )

### Power Ratio

RF power / Optical power = 1.2 W / 0.122 W = 9.84×  
Optical uses ~10× less power

## Aperture Ratio

RF diameter / Optical diameter = 30 cm / 10 cm = 3×  
Optical aperture is 3× smaller

Area ratio =  $(30/10)^2 = 9\times$   
RF antenna has 9× more area

# 5. DATA RATE SCALABILITY ANALYSIS

## 5.1 Optical Scalability Calculation

**Principle:** Each 10× increase in data rate costs 10 dB margin

**Current:** 1 Gbps with 25.66 dB margin

**At 10 Gbps:**

$$\begin{aligned}\text{Margin degradation} &= 10 \times \log_{10}(10 \text{ Gbps} / 1 \text{ Gbps}) \\ &= 10 \times \log_{10}(10) = 10 \text{ dB}\end{aligned}$$

$$\text{New margin} = 25.66 \text{ dB} - 10 \text{ dB} = 15.66 \text{ dB} \checkmark \text{ (excellent)}$$

**At 100 Gbps:**

$$\begin{aligned}\text{Margin degradation} &= 10 \times \log_{10}(100) = 20 \text{ dB} \\ \text{New margin} &= 25.66 \text{ dB} - 20 \text{ dB} = 5.66 \text{ dB} \checkmark \text{ (adequate)}\end{aligned}$$

## 5.2 RF Scalability Calculation

**Current:** 1 Gbps with 2.8 dB margin

**At 2 Gbps:**

$$\begin{aligned}\text{Margin degradation} &= 10 \times \log_{10}(2 \text{ Gbps} / 1 \text{ Gbps}) \\ &= 10 \times \log_{10}(2) = 3.01 \text{ dB}\end{aligned}$$

$$\text{New margin} = 2.8 \text{ dB} - 3.01 \text{ dB} = -0.21 \text{ dB} \times (\text{link fails})$$

**Conclusion:** RF cannot scale beyond ~1.5 Gbps without hardware changes.

## 6. RANGE SENSITIVITY ANALYSIS

### 6.1 Optical at Extended Range (500 km)

Path loss change:

$$\begin{aligned}\Delta L &= 20 \times \log_{10}(R_{\text{new}} / R_{\text{baseline}}) \\ &= 20 \times \log_{10}(500 \text{ km} / 250 \text{ km}) \\ &= 20 \times \log_{10}(2) = 6.02 \text{ dB additional loss}\end{aligned}$$

$$\text{New margin} = 25.66 \text{ dB} - 6.02 \text{ dB} = 19.64 \text{ dB} \checkmark (\text{still robust})$$

### 6.2 RF at Extended Range (500 km)

Path loss change:

$$\Delta L = 20 \times \log_{10}(500 / 250) = 6.02 \text{ dB additional loss}$$

$$\text{New margin} = 2.8 \text{ dB} - 6.02 \text{ dB} = -3.22 \text{ dB} \times (\text{link fails})$$

**Conclusion:** Optical maintains adequate margin at 2x range; RF link fails.

## 7. ADVANTAGES AND DISADVANTAGES

### 7.1 OPTICAL (LASER) Crosslinks

**Advantages**

- Exceptional Link Margin (25.66 dB)** - We calculated  $369\times$  more power than required, which gives us a massive robustness buffer
- Compact Size (10 cm)** - Here's what's impressive: we get 106.1 dBi gain from a small aperture, all thanks to that short wavelength
- Low Power (0.122W)** - Calculated from detector requirements; it's about  $10\times$  less than RF
- Unlimited Scalability** - We calculated 15.66 dB margin at 10 Gbps, and there's no spectrum constraints holding us back
- No Spectrum Licensing** - Optical frequencies are unregulated — one less headache
- Low Interference** - Calculated beam divergence of  $18.9 \mu\text{rad}$  ( $4.73 \text{ m}$  spot at  $250 \text{ km}$ ) essentially eliminates cross-talk between satellites
- Secure** - Good luck intercepting a beam that narrow

## Disadvantages

- Stringent Pointing ( $\pm 8 \mu\text{rad}$  required)** - The calculated half-power beamwidth requires FSM for  $\pm 8 \mu\text{rad}$  pointing accuracy, which adds roughly \$500k in NRE
- Complex Acquisition** - That narrow beam means we're looking at 30-60s acquisition time
- Lower TRL (7-8)** - Less flight heritage for small satellites compared to RF's TRL 9
- Higher Development Cost** - We're estimating \$8M NRE versus \$5M for RF
- Sun Avoidance** - Background noise forces us into geometry constraints
- Limited Vendors** - Fewer COTS suppliers to choose from (Tesat, ATLAS, Mynaric)

## 7.2 RF (Ka-band) Crosslinks

### Advantages

- Relaxed Pointing ( $2.19^\circ$ )** - Calculated beamwidth is  $2,000\times$  wider; standard ACS is sufficient

- 2. Fast Acquisition (5-10s)** - Wide beam means rapid link establishment
- 3. High TRL (9)** - Extensive heritage across Starlink, OneWeb, Iridium NEXT
- 4. Mature Supply Chain** - Multiple vendors available (Viasat, L3Harris, Honeywell)
- 5. Lower Development Cost** - \$5M NRE; this is well-understood territory
- 6. Lower Risk** - Predictable performance, and no FSM needed

## **Disadvantages**

- 1. Minimal Link Margin (2.8 dB)** - We calculated only 1.91× more power than required — there's basically no degradation buffer here
  - 2. Large Apertures (30 cm)** - Calculated gain requires 3× larger antennas, which complicates deployment
  - 3. Higher Power (1.2W)** - Calculated at 10× more than optical; impacts the power budget significantly
  - 4. Spectrum Limitations** - Ka-band's getting crowded, and ITU coordination is required
  - 5. Limited Scalability** - Calculated failure at 2 Gbps; we're bandwidth-constrained
  - 6. Interference Risk** - With mega-constellations proliferating, RF congestion is growing
- 

## **8. RECOMMENDATION**

### **8.1 Primary Recommendation: OPTICAL (LASER) CROSSLINKS**

Confidence Level: HIGH

### **8.2 Quantitative Justification**

Decision Drivers (with calculations):

#### **1. Superior Link Performance**

- Calculated margin: 25.66 dB versus 2.88 dB (an 8.9× ratio)

- Linear power ratio: 369× versus 1.91× safety factor
- Degradation tolerance: We could lose 22.66 dB and still meet requirements

## 2. Optimal SWaP for Small Satellites

- Calculated aperture: 10 cm versus 30 cm (3× smaller, 9× less area)
- Calculated power: 0.122W versus 1.2W (10× reduction)
- Mass estimate: roughly 2.2 kg versus 4.2 kg (2 kg savings translates to about \$10k in launch cost)

## 3. Proven Scalability

- Calculated 10 Gbps margin: 15.66 dB (still excellent)
- Calculated 100 Gbps margin: 5.66 dB (adequate)
- RF calculated to fail at 2 Gbps (-0.21 dB margin)

## 4. Range Robustness

- Calculated margin at 500 km: 19.64 dB (optical) versus -3.22 dB (RF fails)
- 2× range tolerance demonstrated

## 8.3 Addressing the Pointing Challenge

**Optical pointing requirement:**  $\pm 8 \mu\text{rad}$  (calculated from half-power beamwidth for -3 dB loss)

**RF pointing requirement:**  $2.19^\circ = 38,200 \mu\text{rad}$  (calculated beamwidth)

**Ratio:** 4,775× easier for RF (in linear angle), or roughly 2,000× easier in solid angle

**Note:** Optical beam divergence to first null is  $18.9 \mu\text{rad}$ , but the pointing requirement is based on the half-power beamwidth ( $8 \mu\text{rad}$ ) to achieve the -3 dB pointing loss budget.

**BUT:** Here's where optical's 25.66 dB margin becomes really useful — we can trade some of that margin for relaxed pointing:

- If pointing degrades to  $12 \mu\text{rad} \rightarrow$  roughly -4.5 dB loss instead of -3 dB
- New margin:  $25.66 - 1.5 = 24.16 \text{ dB}$  (still excellent)

- That margin gives us flexibility to ease pointing requirements

#### **Heritage FSM Technology:**

- EDRS: Has demonstrated  $<5 \mu\text{rad}$  pointing accuracy since 2016 (better than our  $8 \mu\text{rad}$  requirement)
- LCRD: Demonstrates similar performance since 2021
- Technology risk is manageable here

## **8.4 Cost-Benefit Calculation**

#### **20-Satellite Constellation:**

- Optical total:  $\$8\text{M NRE} + 20 \times \$150\text{k} + 10\text{yr} \times \$50\text{k} = \$12.3\text{M}$
- RF total:  $\$5\text{M NRE} + 20 \times \$100\text{k} + 10\text{yr} \times \$30\text{k} = \$7.3\text{M}$
- **Premium: \$5.0M (68% more)**

#### **What We Get for That Premium:**

- $8.9 \times$  better margin (calculated)
- $10 \times$  lower power per satellite (calculated)
- $3 \times$  smaller apertures (calculated)
- $10 \times$  data rate scalability (calculated: 10 Gbps versus 1 Gbps)
- Launch savings:  $20 \text{ sats} \times 2 \text{ kg} \times \$5\text{k/kg} = \$200\text{k}$

**Net premium: \$5.0M - \$0.2M = \$4.8M for transformational performance**

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## **9. CONCLUSION**

This trade study analyzed optical (laser) versus RF (Ka-band) crosslinks for a LEO satellite constellation using rigorous link budget calculations.

#### **Key Calculated Results:**

- **Optical:** 25.66 dB margin, 0.122W power, 10 cm aperture,  $\pm 8 \mu\text{rad}$  pointing requirement
- **RF:** 2.8 dB margin, 1.2W power, 30 cm aperture,  $2.19^\circ$  pointing requirement

### **Quantitative Comparison:**

- Link margin: Optical 8.9× better (calculated ratio: 369×/1.91× in linear terms)
- Aperture: Optical 3× smaller (9× less area)
- Power: Optical 10× lower
- Pointing: RF roughly 4,800× easier (in linear angle)
- Scalability: Optical scales to 10+ Gbps (calculated 15.66 dB at 10 Gbps); RF fails at 2 Gbps (calculated -0.21 dB)

### **Recommendation: OPTICAL CROSSLINKS**

Optical wins 4 of 5 key parameters. That enormous calculated margin (25.66 dB versus 2.88 dB) provides:

1. Robustness to degradation (22.66 dB buffer above requirement)
2. Data rate scalability (calculated 15.66 dB at 10× higher rate)
3. Range tolerance (calculated 19.64 dB at 2× range)
4. Flexibility to ease pointing requirements (we can trade margin for simpler FSM)

RF has significantly easier pointing (calculated roughly 4,800× wider beamwidth), but this advantage is outweighed by optical's transformational performance benefits and the availability of heritage FSM technology (EDRS, LCRD achieving <5  $\mu$ rad).

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- Speed of light:  $c = 299,792,458$  m/s (exact)
- Boltzmann constant:  $k_B = 1.380649 \times 10^{-23}$  J/K

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## APPENDIX: Formula Reference

### Optical Link Budget Formulas

$n = Q / \eta$	[photons/bit]
$E_{\text{photon}} = h \times c / \lambda$	[J/photon]
$E_{\text{bit}} = n \times E_{\text{photon}}$	[J/bit]
$P_{\text{req}} = E_{\text{bit}} \times R_b$	[W]

$L_s = (\lambda / (4\pi R))^2$	[linear]
$G = (\pi D / \lambda)^2$	[linear]

$P_{\text{rx}} = P_{\text{tx}} \times L_s \times G_{\text{tx}} \times G_{\text{rx}} \times L_{\text{pt}} \times L_o$	[W]
Margin = $10 \times \log_{10}(P_{\text{rx}} / P_{\text{req}})$	[dB]

$\theta = 1.22 \times \lambda / D$	[radians]
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## RF Link Budget Formulas

$$FSPL = 20 \times \log_{10}(4\pi R/\lambda) \quad [\text{dB}]$$

$$G = \eta_{\text{ant}} \times (\pi D/\lambda)^2 \quad [\text{linear}]$$

$$EIRP = P_t + G \quad [\text{dBW}]$$

$$N_0 = k_B \times T_{\text{sys}} \quad [\text{W/Hz}]$$

$$C/N_0 = P_{\text{rx}} - N_0 \quad [\text{dB-Hz}]$$

$$(C/N_0)_{\text{req}} = (E_b/N_0)_{\text{req}} + 10 \times \log_{10}(R_b) \quad [\text{dB-Hz}]$$

$$\text{Margin} = C/N_0 - (C/N_0)_{\text{req}} \quad [\text{dB}]$$

$$\theta_{3\text{dB}} \approx 70 \times \lambda / D \quad [\text{degrees}]$$

## Constants Used

$$c = 3 \times 10^8 \text{ m/s} \quad (\text{speed of light})$$

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s} \quad (\text{Planck's constant})$$

$$k_B = 1.38 \times 10^{-23} \text{ J/K} \quad (\text{Boltzmann constant})$$